

# Neutrino Beam Flux Systematics

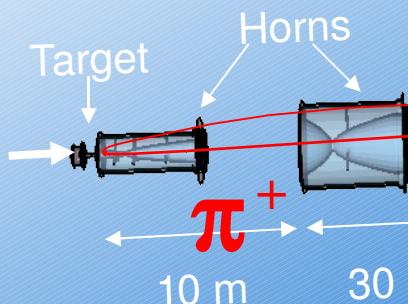
Laura Loiacono

University of Texas at Austin

NuFact 2009

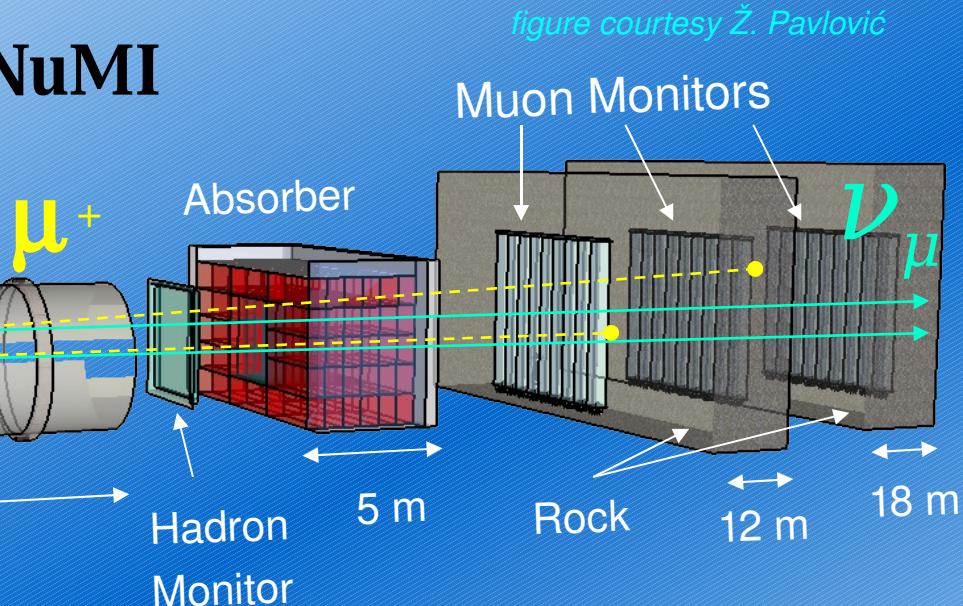
- Modern ν Beams.
- Systematic Flux Errors.
  - Beam transportation.
  - Hadron Production.
  - Other.
- Flux Measurements.
- Flux measurement from the NuMI μMonitors.

# Modern Beams

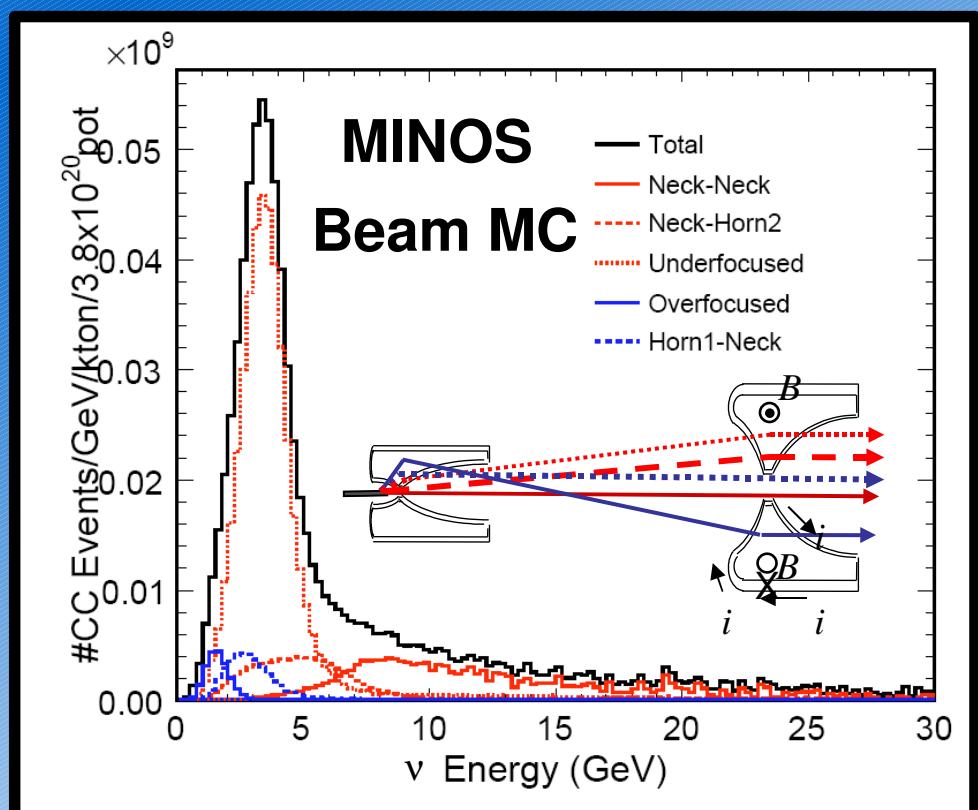


Decay Pipe

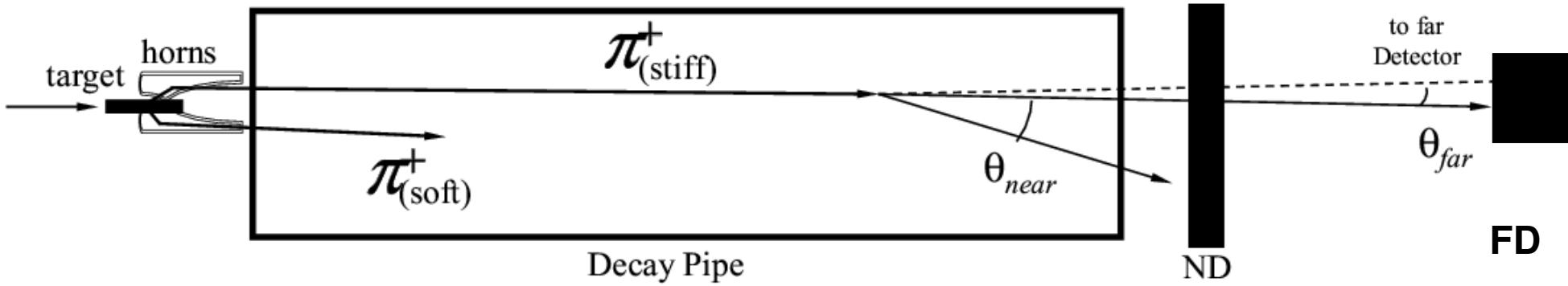
NuMI



- Point to parallel focusing,  
 $f \propto p$ , selects peak energy of  
the beam.
- Magnetic horn focusing  
increases the flux of  
neutrinos to downstream  
detectors by  $\sim 25$ .

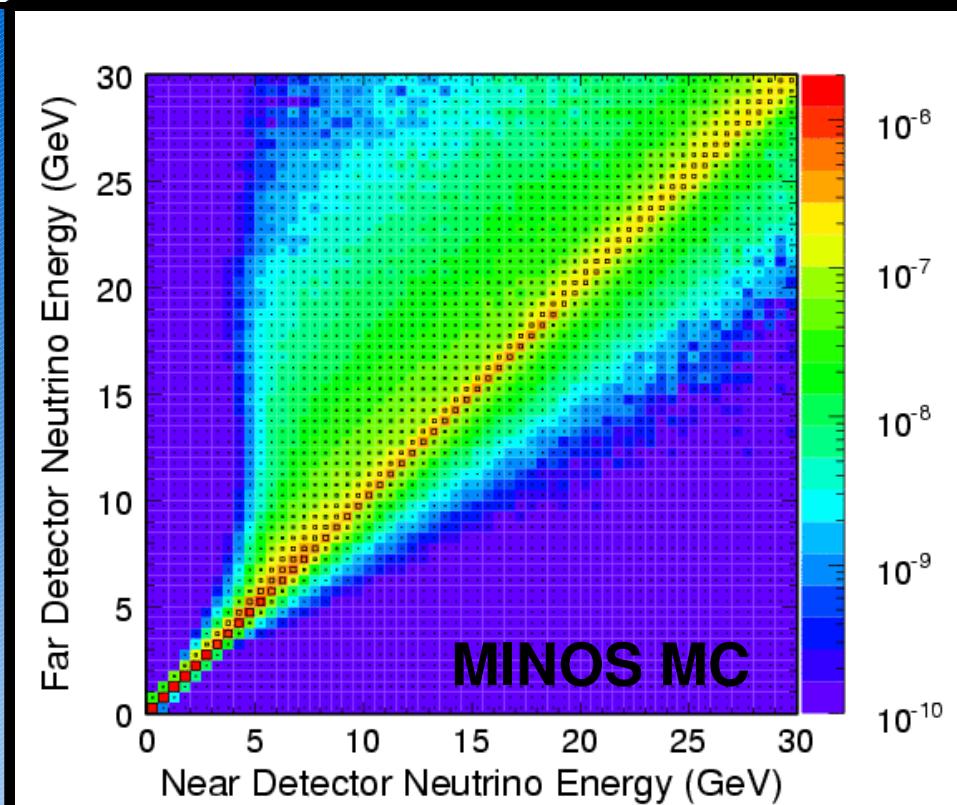


# Two Detector Experiments



$$E_\nu = \frac{0.43 E_\pi}{1 + \gamma^2 \theta^2} \quad \text{Flux} \propto \frac{1}{L^2} \left( \frac{1}{1 + \gamma^2 \theta^2} \right)^2$$

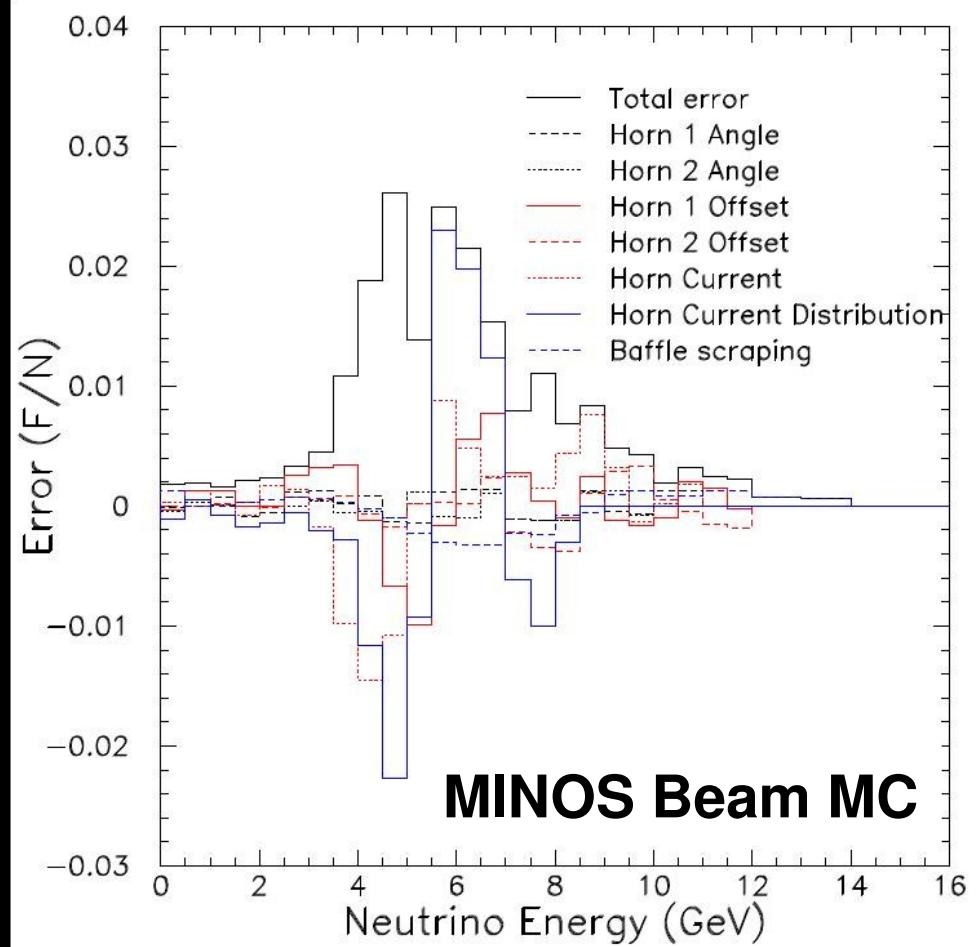
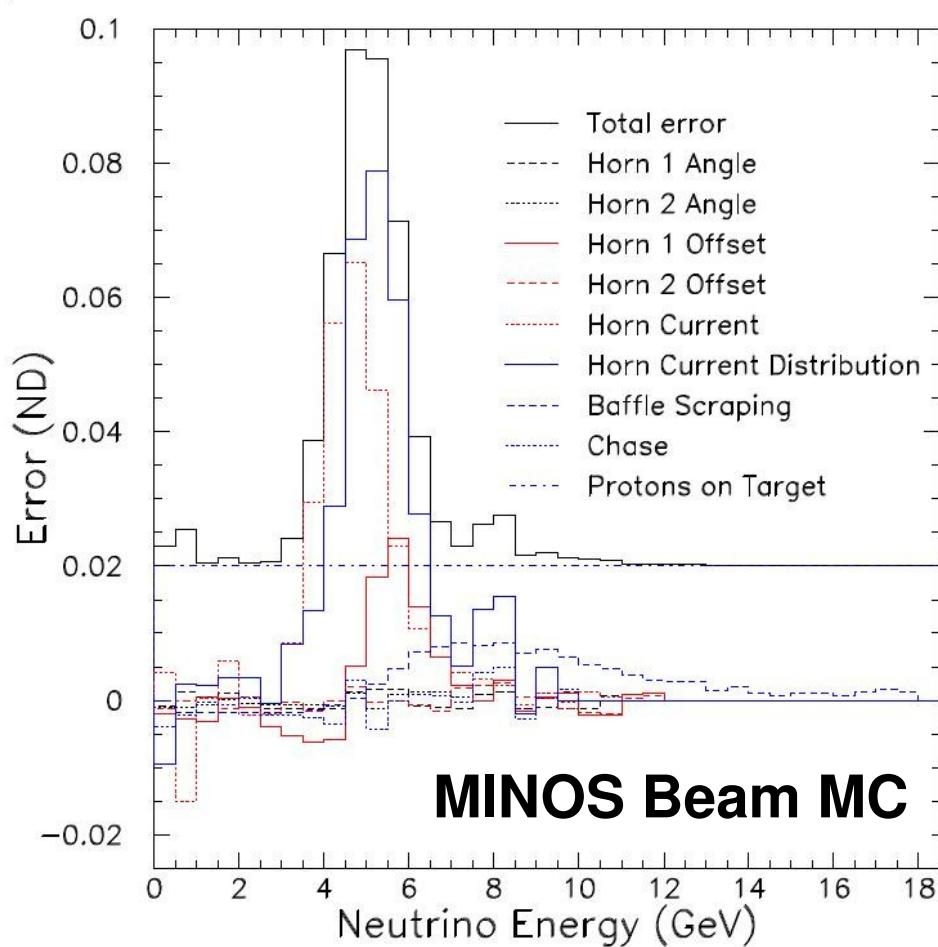
- Flux at ND is from a line source.
- Oscillation experiments use the Near Detector spectrum to predict the far detector spectrum.



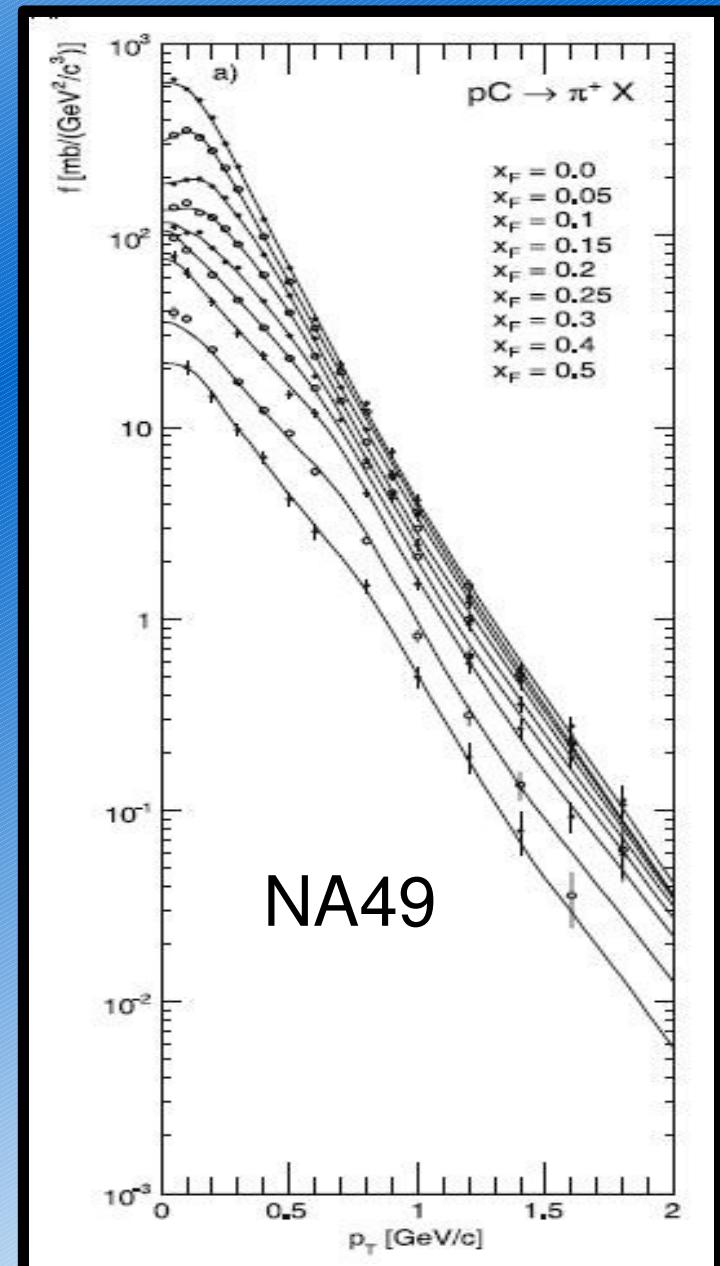
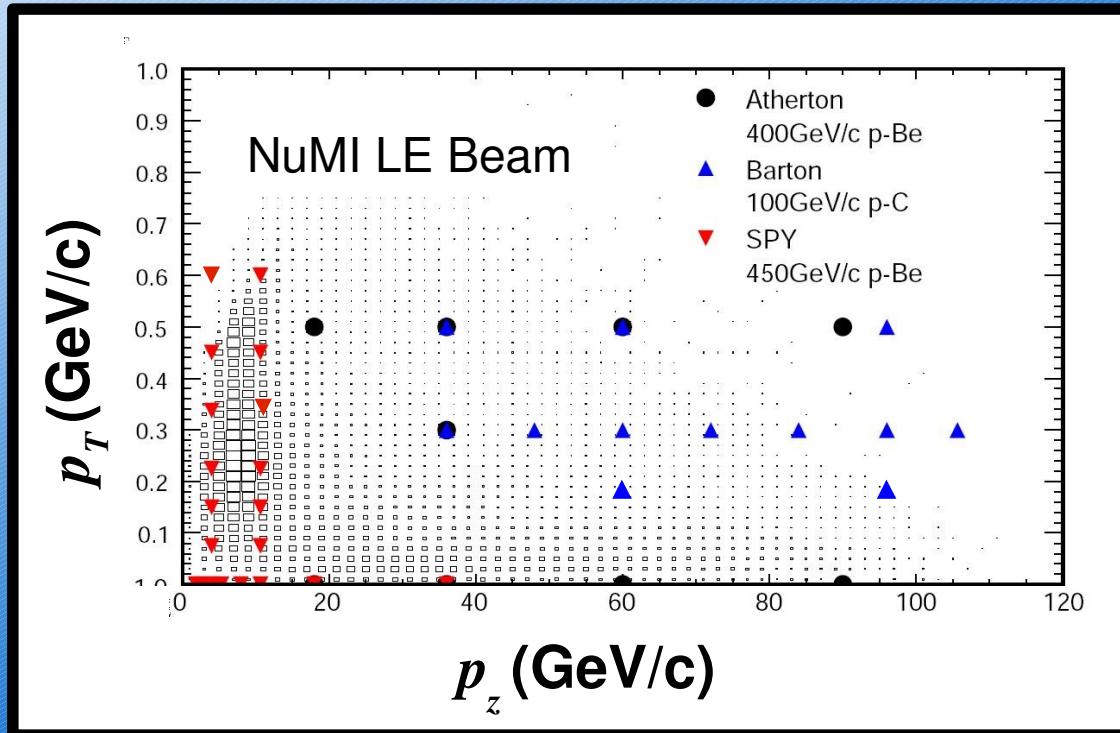
# Systematic Errors on the Flux: Beam Transportation

Most important for cross section experiments

Important for oscillation experiments



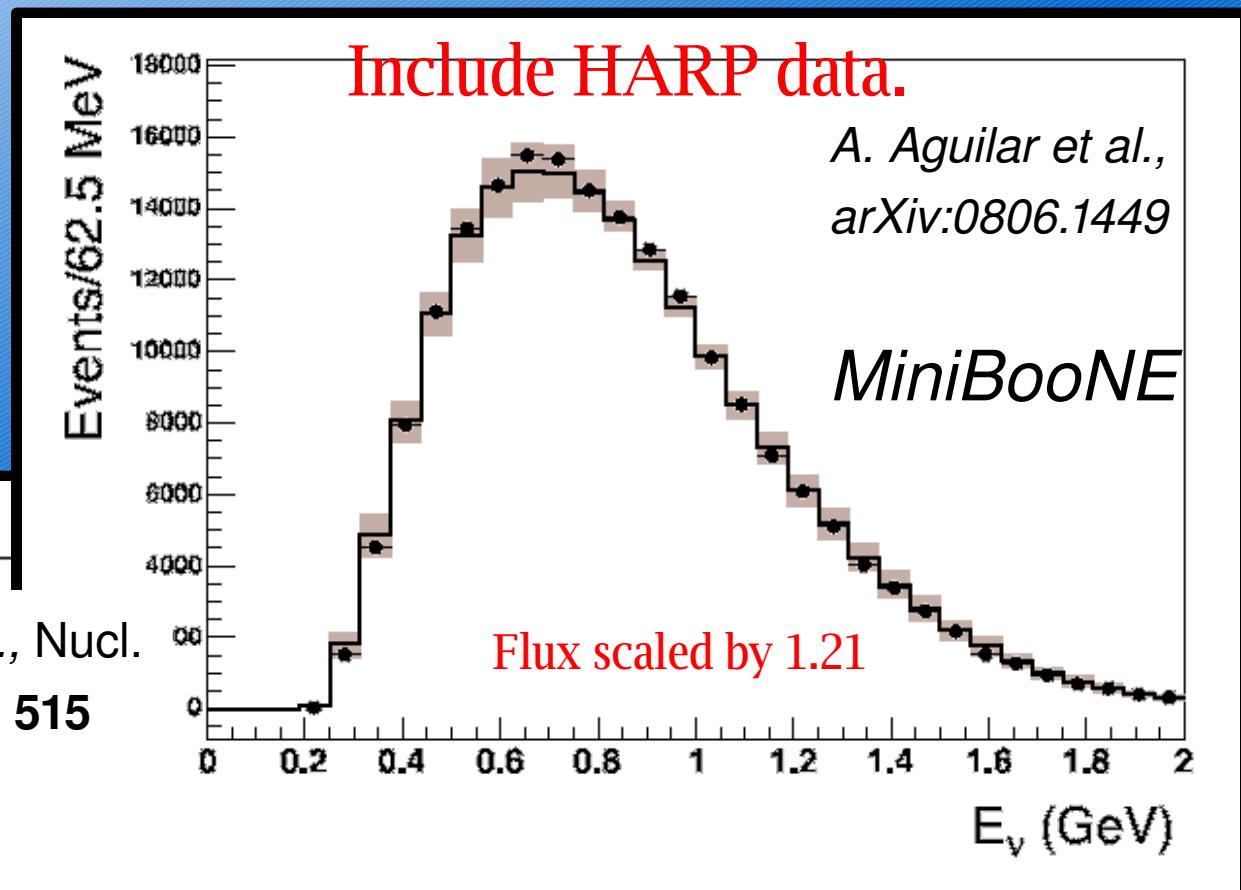
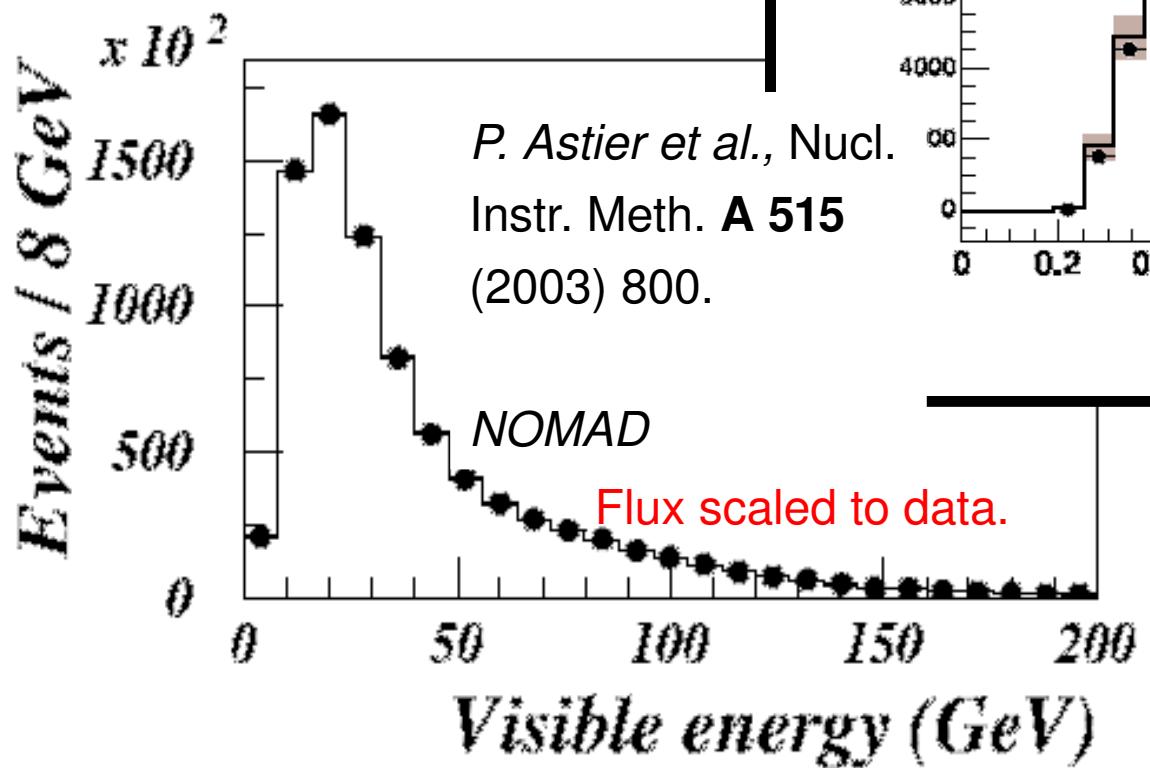
# Systematic Errors on the Flux: Hadron Production



- Most neutrino experiments use MC tuned to existing hadron production measurements to simulate the production of neutrino parents in the beam line.

# Incorporating Hadron Production

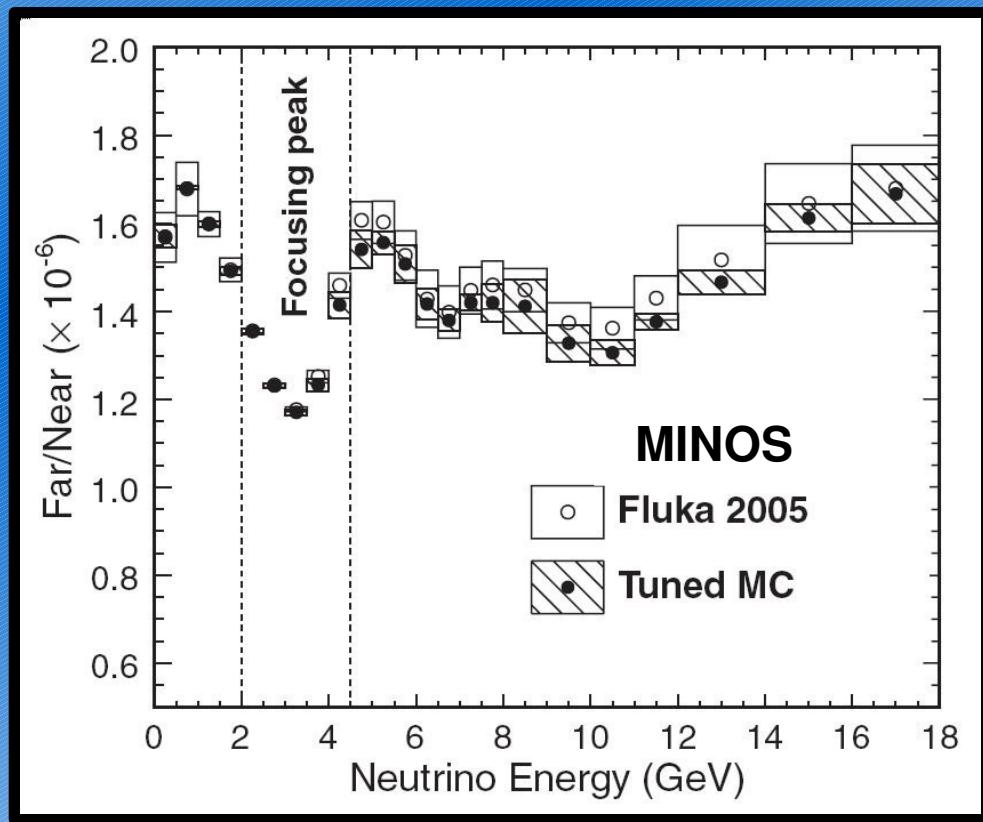
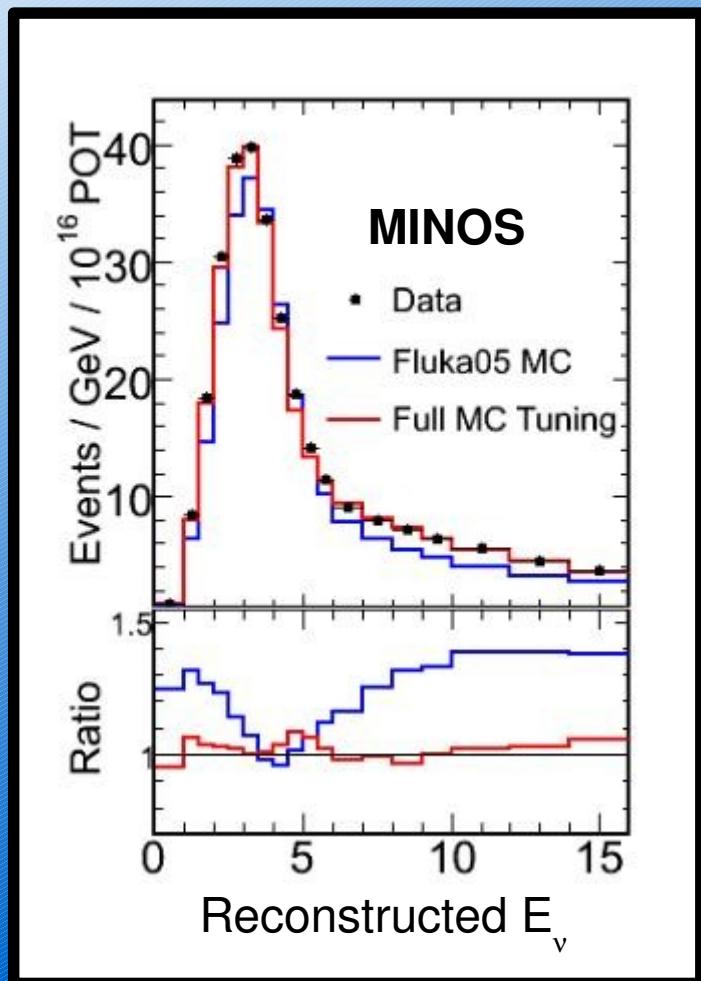
- K2K flux RATIO error is 2-9% after including HARP data.



- Shapes agree well.
- Normalization is still questionable.

# Tuning Hadron Production

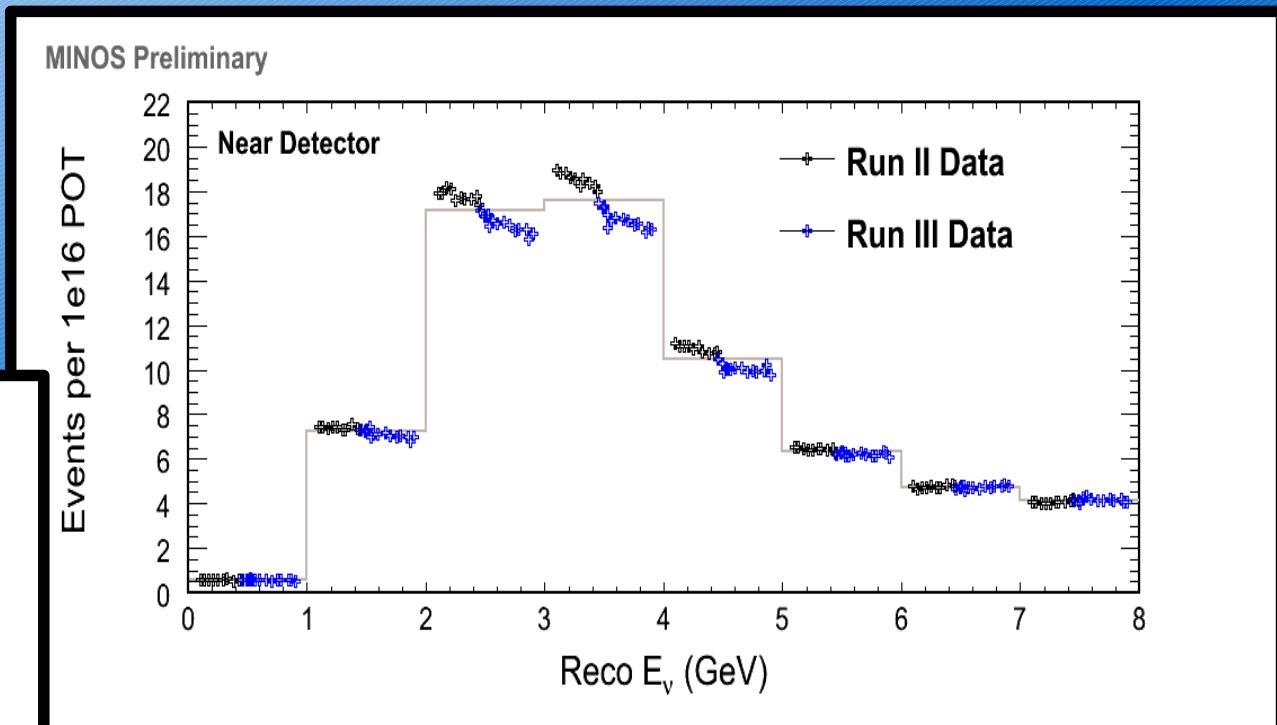
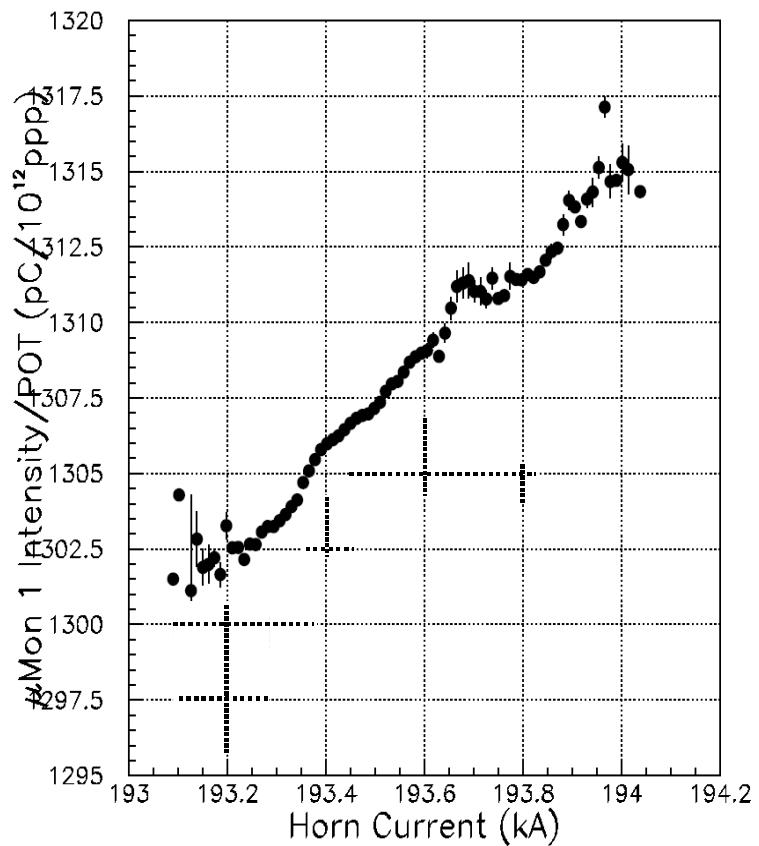
- Tune MC to MINOS ND data.
- Reduces error on FD prediction.



- But must assume knowledge of  $\nu$  cross-sections.

# Systematic Errors on the Flux: Other

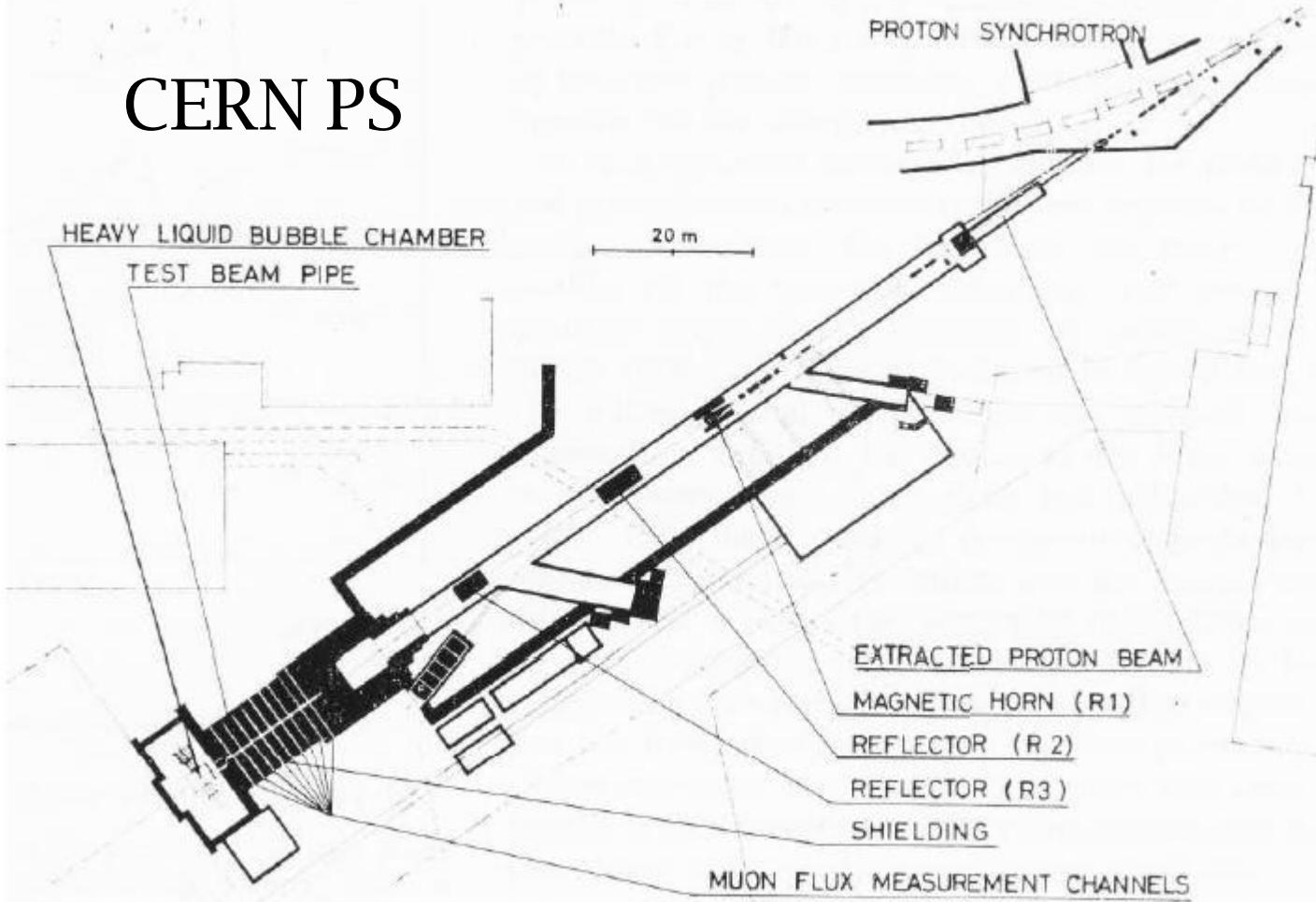
- Flux changes due to horn current variation with temperature.



- Possible target degradation over time.
- Also have downstream interactions on rock and concrete which are not covered in hadron production experiments.

# In situ Flux Measurements

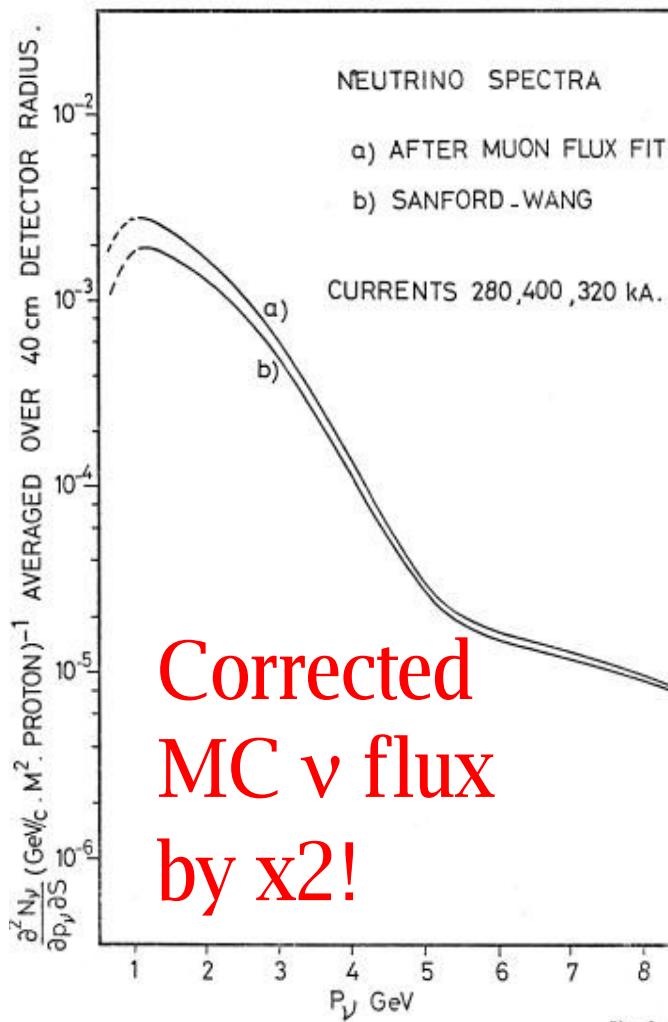
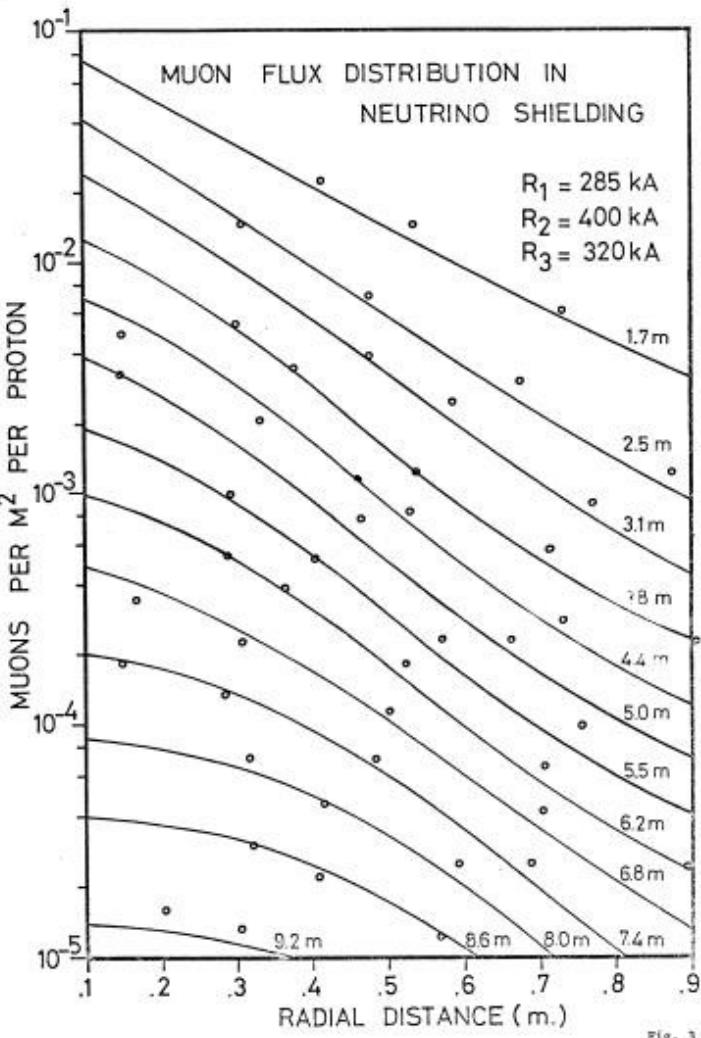
CERN PS



- BNL
- CERN-PS, WANF
- IHEP
- FNAL E616
- Typical ~20%

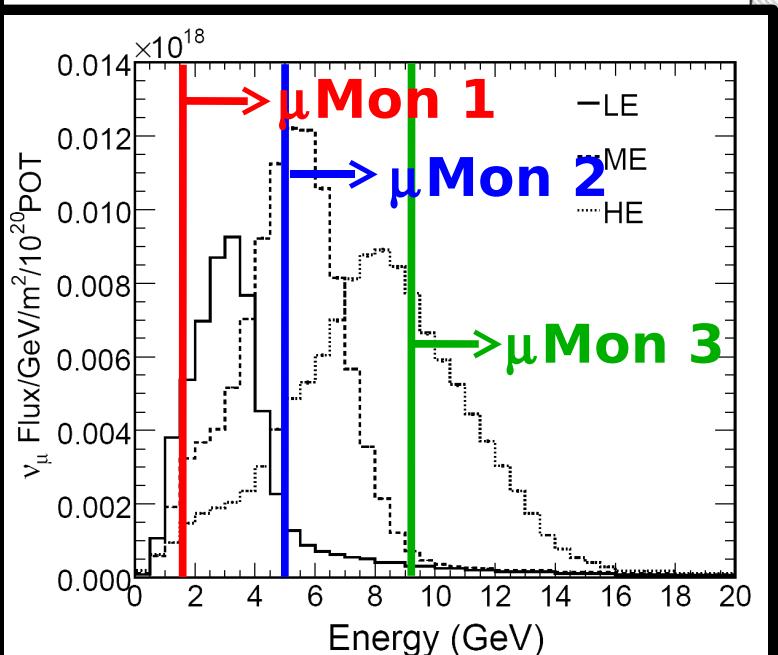
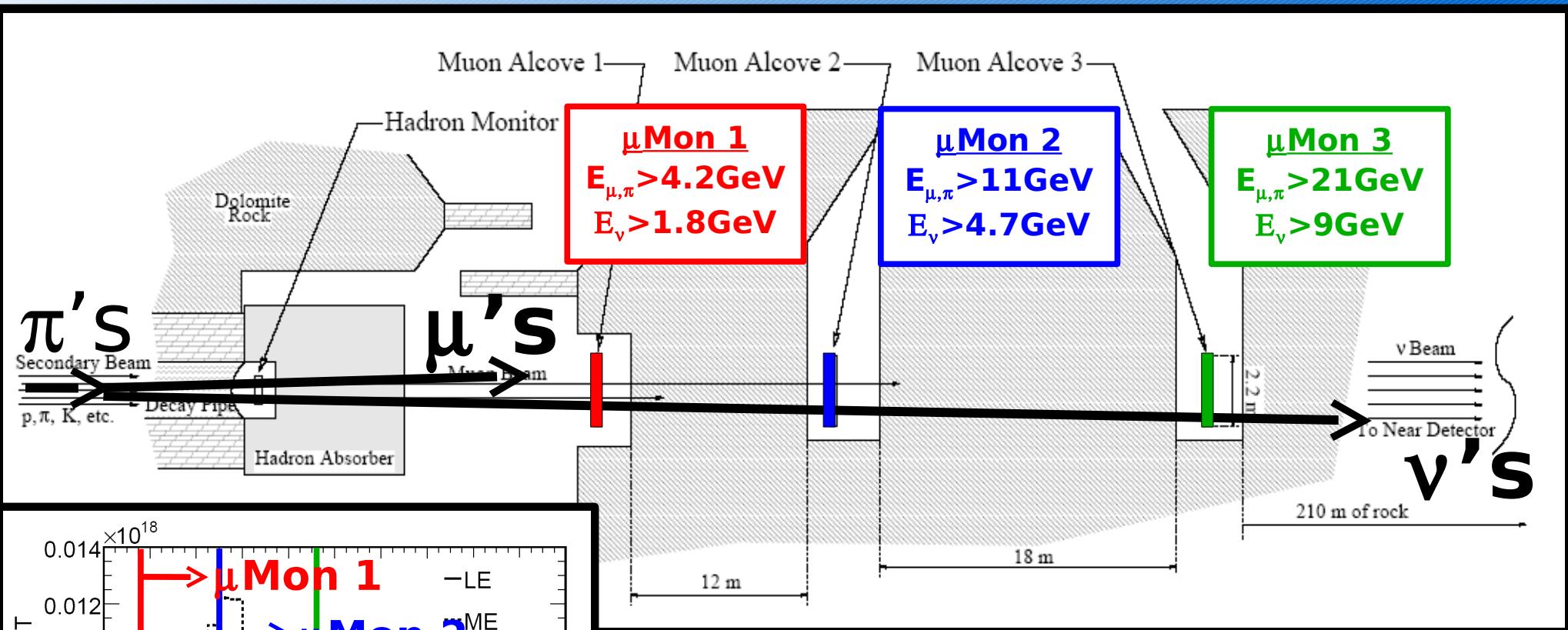
➤ Not an easy measurement.

# Experience from CERN PS



- Originally tuned MC to HP data.
- Flux measurement from  $\mu$ Mons indicated x2 off.
- New HP experiment – agreed with  $\mu$  tuned  $\nu$  flux to 15%.

# NuMI Flux Measurement



- 3 arrays of ionization chambers; Signal = ionized electrons.
- Sampling  $\mu$  flux = Sampling hadrons off target = Sampling  $\nu$  flux.
- Sample different energy regions of the flux.

# NuMI Variable Beam Energy

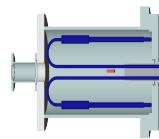
“Low”  
Energy

*proton*

*target*

*Horn 1*

*target*



$$\begin{matrix} p \\ p_T \\ p_z \end{matrix}$$

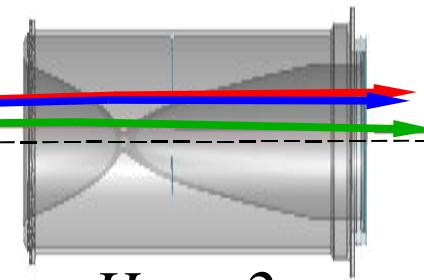
Pions with

$p_T = 300\text{MeV}$

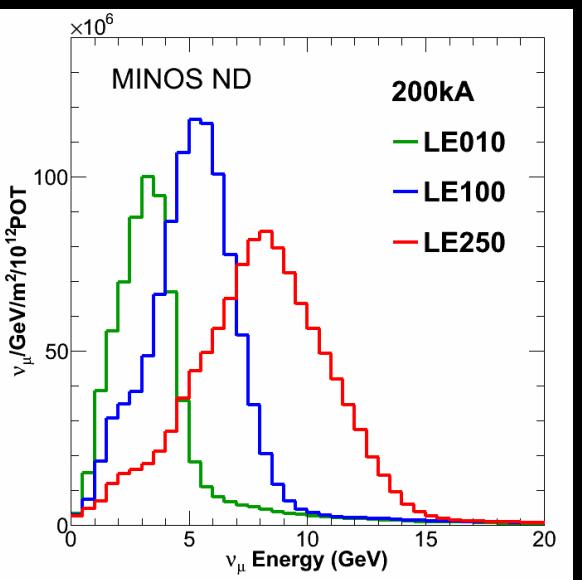
$p = 5\text{ GeV}/c$

$p = 10\text{ GeV}/c$

$p = 20\text{ GeV}/c$

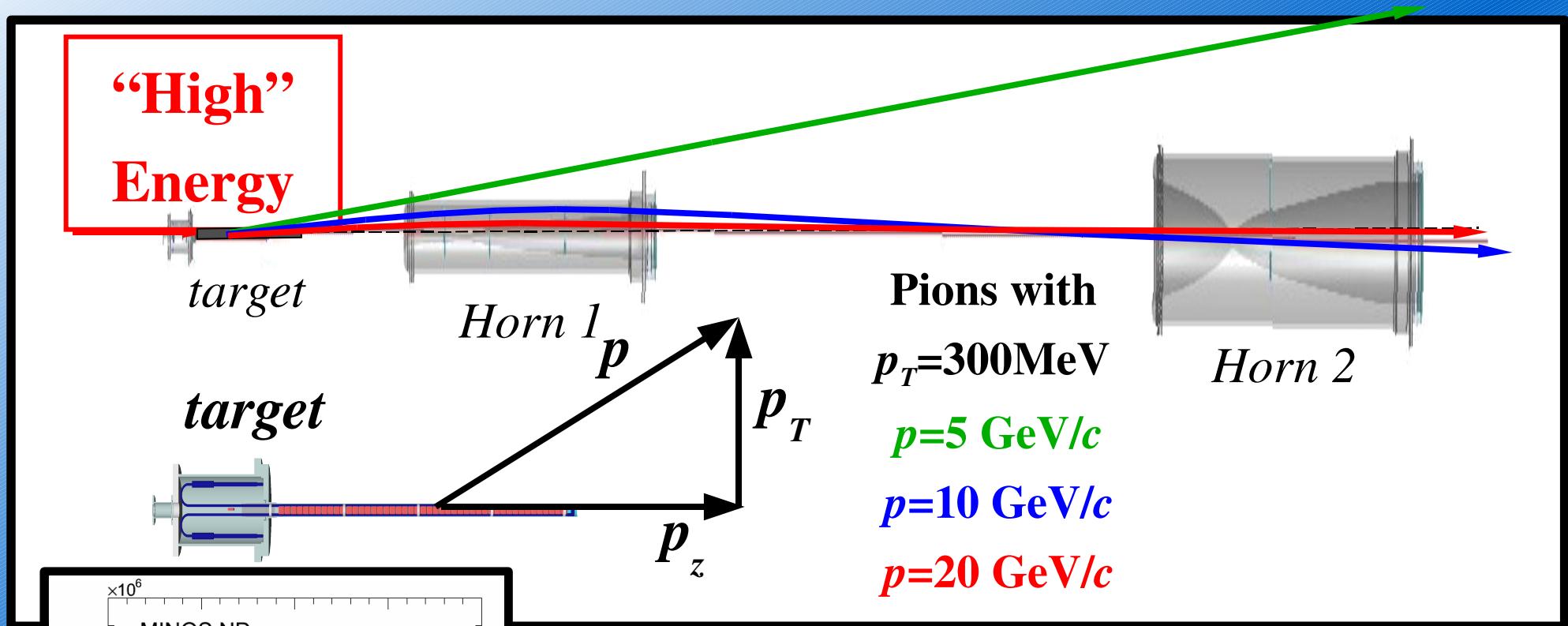


*Horn 2*



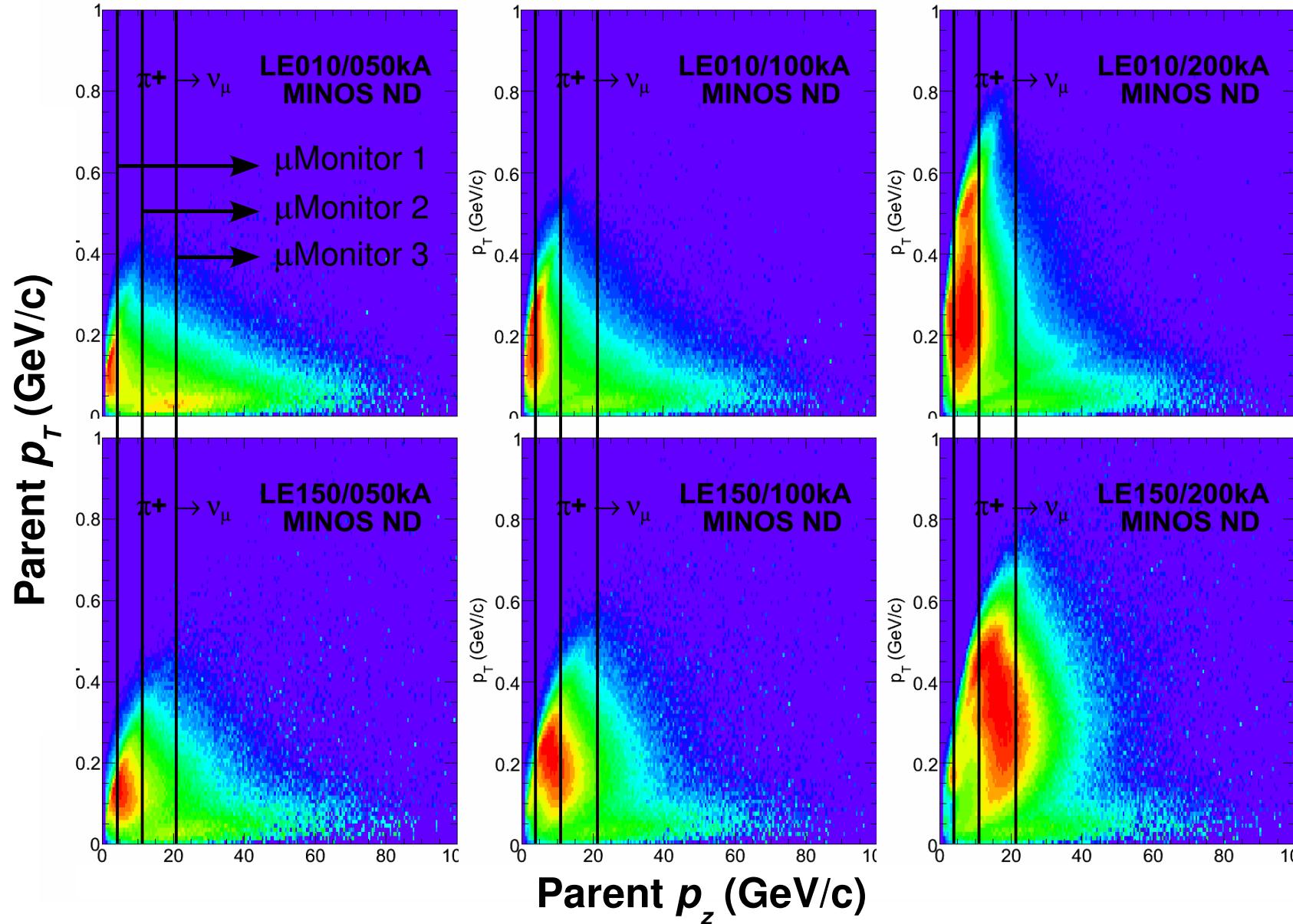
- Hadrons diverge from the target → horns focus hadrons along the beamline.
- Varying target position samples variety of  $E_\pi$ ,  $E_\mu$  and  $E_\nu$ .

# NuMI Variable Beam Energy



- Hadrons diverge from the target → horns focus hadrons along the beamline.
- Varying target position samples variety of  $E_\pi$ ,  $E_\mu$  and  $E_\nu$ .

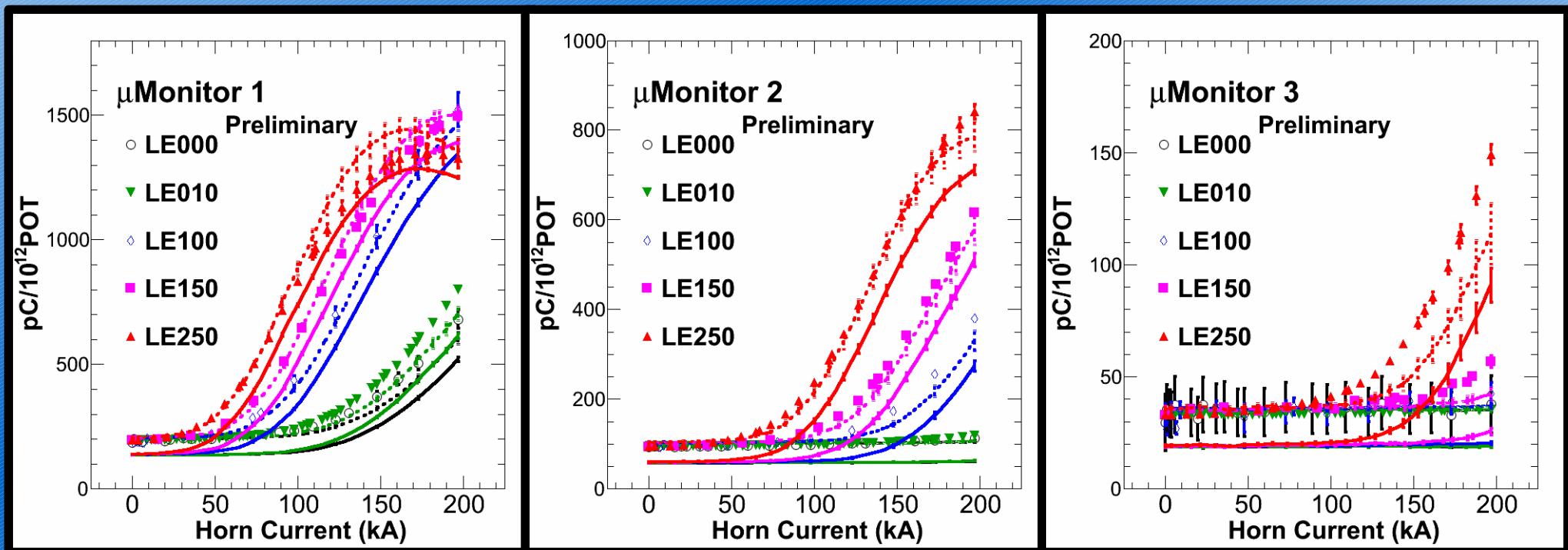
$$\varphi_v(E_\nu) \leftrightarrow \varphi_v(p_T, p_z)$$



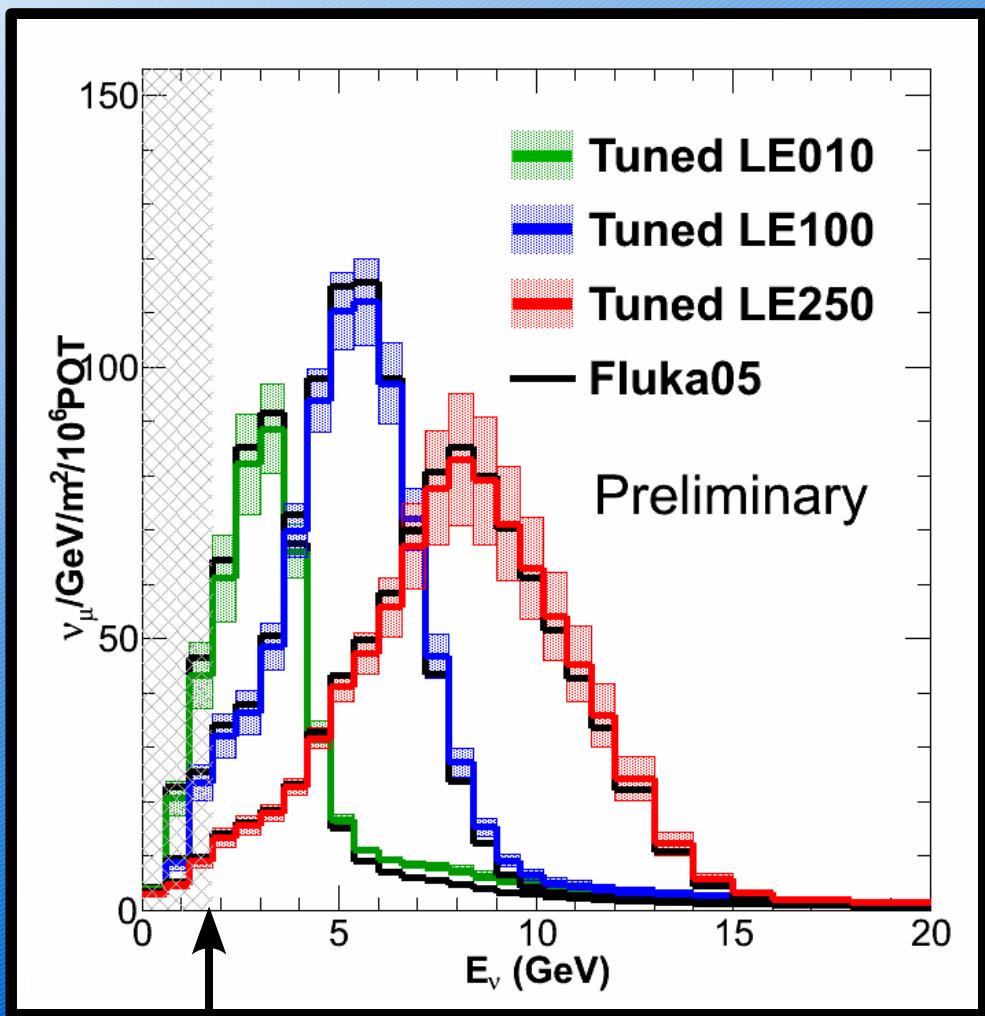
# $\mu$ Monitor Tuning

- Empirical parameterization for hadron production,  $f(p_T, p_z)$ .
- Warp  $p_T$  and  $p_z$  to tune default MC to  $\mu$  Monitor data.

● Data      — Monte-Carlo      - - - Tuned Monte-Carlo



# NuMI v Flux



- Preliminary shape flux measurement.
- Rate measurement is excluded due to uncertainty in pC/ $\mu$  scale factor and backgrounds from  $\delta$ -rays.
- In-situ measurement; accounts for real beamline conditions.
- Can measure  $\nu$  cross-sections:

$$\sigma_\nu(E_\nu) = \frac{N_\nu(E_\nu)}{\varphi_\nu(E_\nu)}$$

# Summary

- Flux uncertainties/normalization particularly important for neutrino cross section experiments; but absolute fluxes benefit everyone.
- Unexpected/Unknown *In situ* effects can add uncertainty to flux predictions.
- *In situ* NuMI Flux measurement has been made.
- $\nu$  cross sections to follow.

# References

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- S. Kopp, “*Accelerator Neutrino Beams*,” *Phys. Rep.* 439, 101 (2007).
- A.A. Aguilar-Arevalo, et al., MiniBooNE Collaboration, ``The Neutrino Flux prediction at MiniBooNE," arXiv:0806.1449 [hep-ex].
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- M. H. Ahn, it et al., K2K Collaboration, ``Measurement of Neutrino Oscillation by the K2K Experiment," *Phys. Rev.* D 74, 072003 (2006).

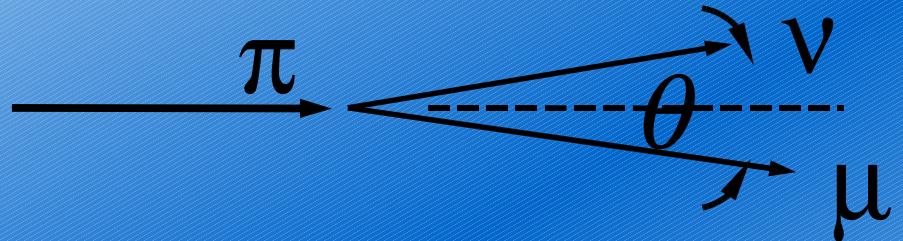
# References

- D. Bloess, et al., Determination of the  $\nu$  spectrum in the CERN 1967 neutrino experiment, Nucl. Inst. Meth. **91** (1971) 605.
- E. H. M. Heijne, ``Muon Flux Measurement With Silicon Detectors In The Cern Neutrino Beams," CERN-YELLOW-83-06.
- A.P. Bugorsky, et al., "Muon flux measuring system for neutrino experiments at the IHEP accelerator", Nucl. Instrum. Methods 146 (1977).
- R. Blair, et al., ``Monitoring And Calibration System For Neutrino Flux Measurement In A High-Energy Dichromatic Beam," Nucl. Instrum. Meth. A **226**, 281 (1984).

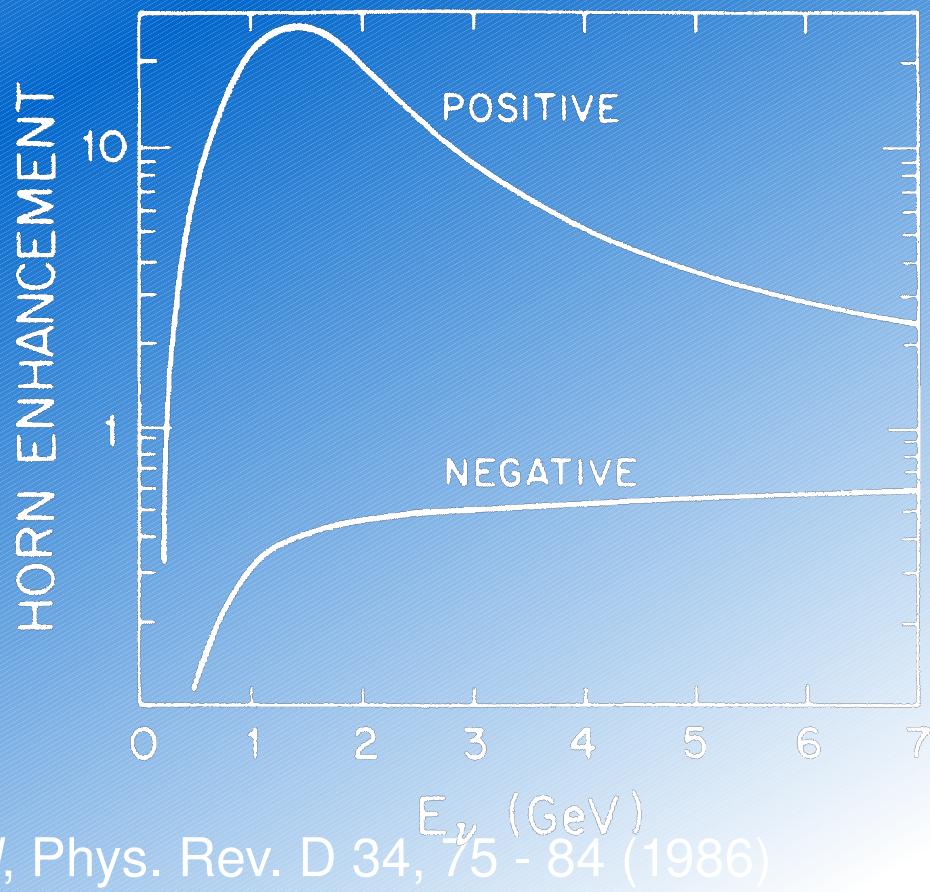
# Backup Slides

# Why Focus?

$$\frac{dP}{d\Omega_\nu} = \frac{A}{4\pi z^2} \left( \frac{2\gamma}{1 + \gamma^2 \theta^2} \right)^2$$



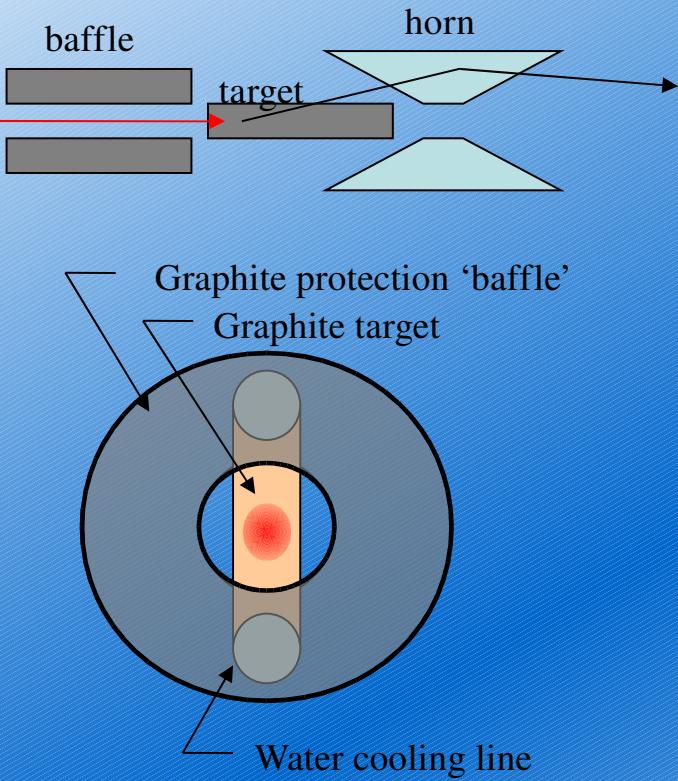
- ‘Cocconi divergence’  
 $\theta_\pi \sim \langle p_T \rangle / p_L \sim 2m_\pi / E_\pi \sim 2/\gamma_\pi$
- Neutrino divergence  
 $\theta_\nu \sim 1/\gamma_\pi$
- Reduce divergence  $\sim 3$ , flux goes up by  $\sim 25$



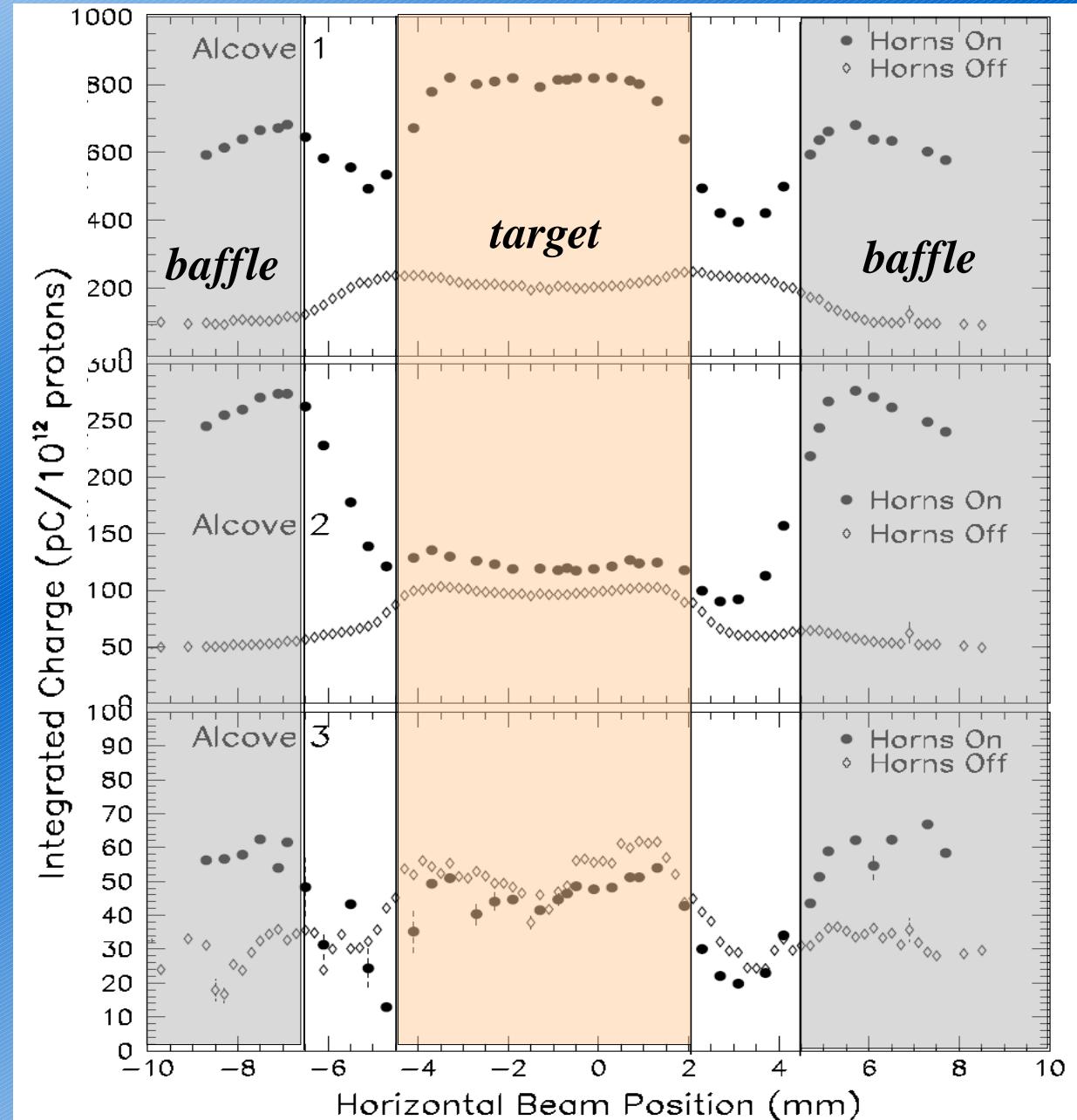
L. Ahrens *et al*, Phys. Rev. D 34, 75 - 84 (1986)

# Systematic Errors on the Flux: Targeting

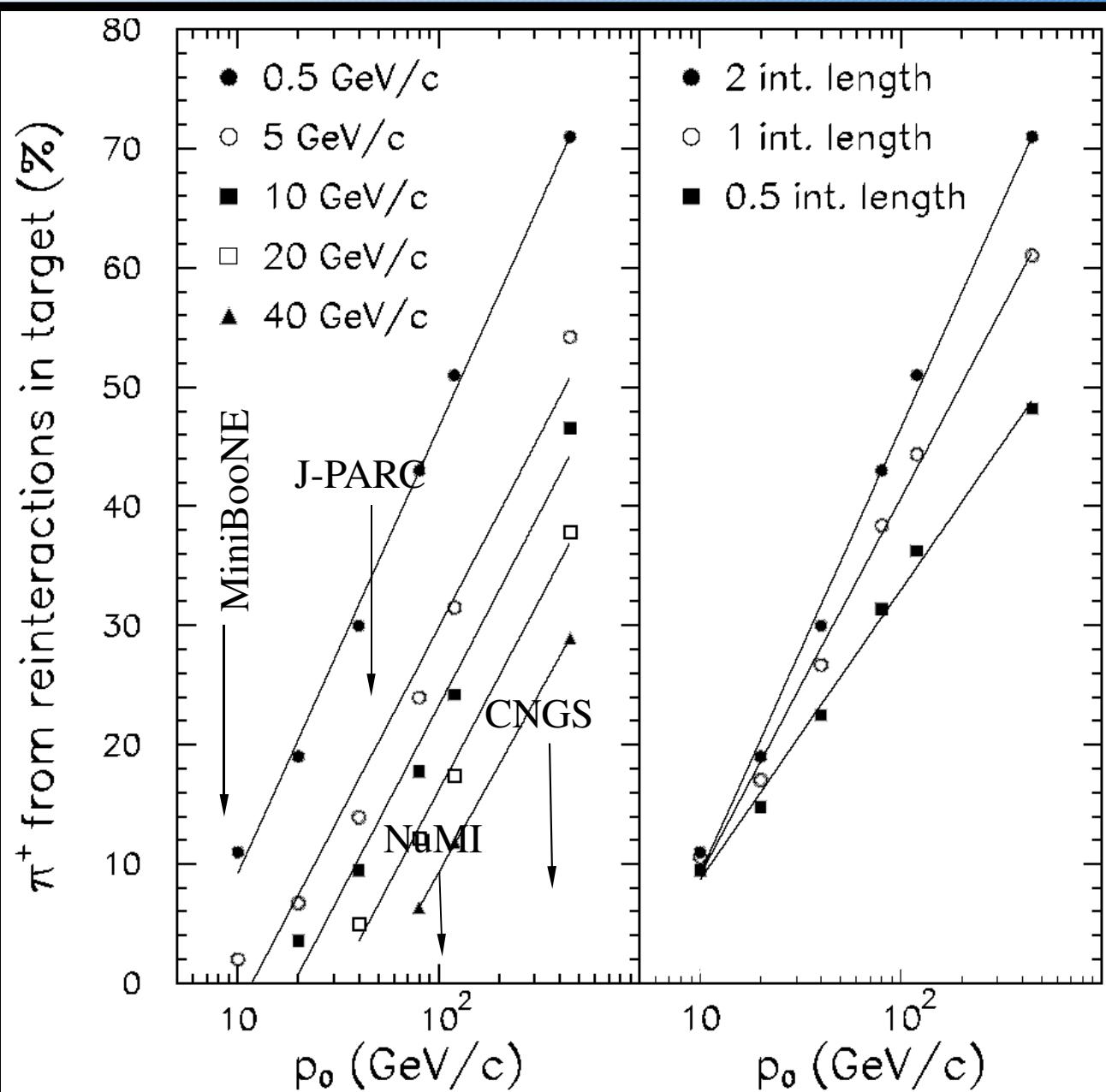
## ➤ Targeting.



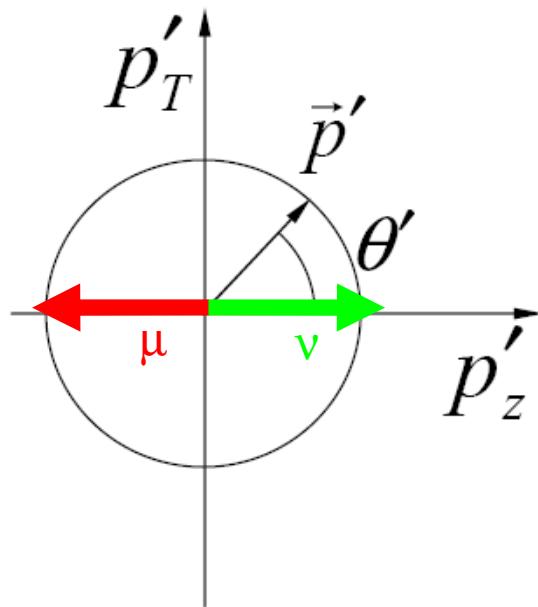
➤ Flux is sensitive to beam position on the target.



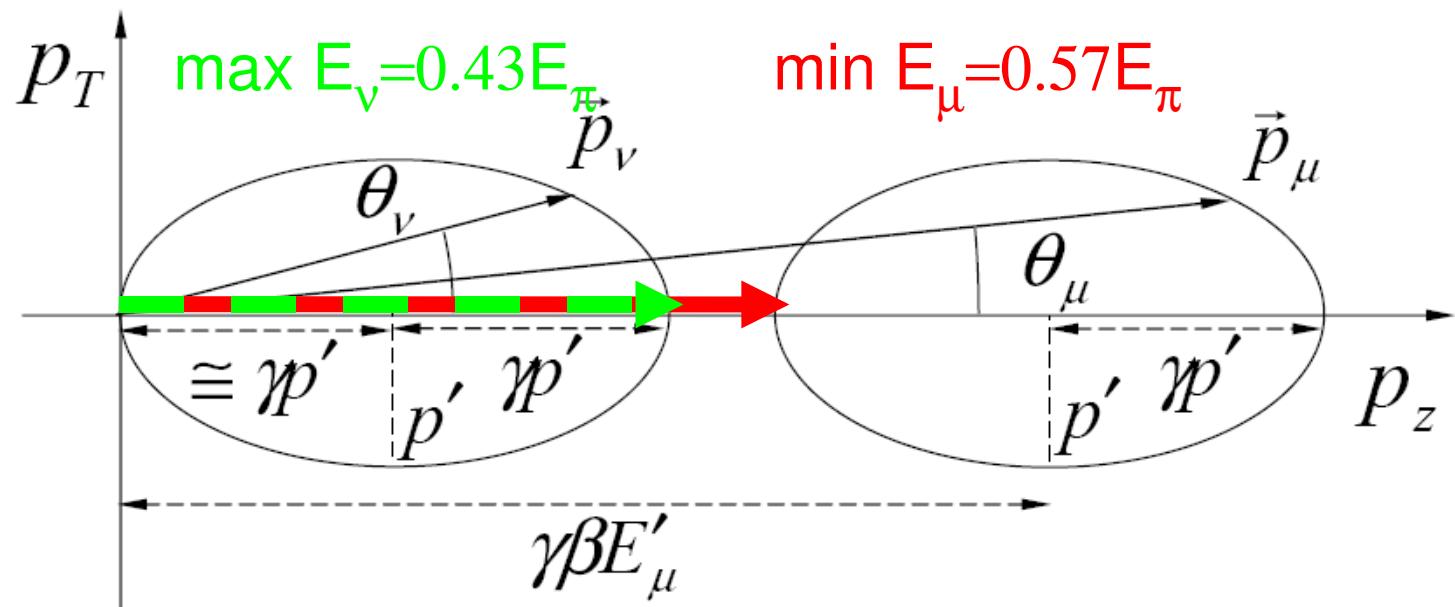
# Thick Target Effects



- Most particle production experiments on 'thin' targets.
- Neutrino production target >  $\lambda_{\text{int}}$
- Reinteractions are 20-30% effect for NuMI.



CM Frame



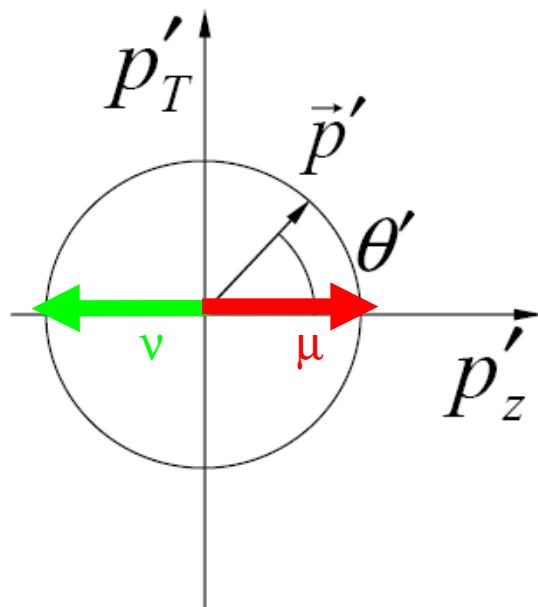
Laboratory Frame

- Neutrinos seen in MINOS and MINERVA come from forward decays in CM frame
- Such decays give highest energy  $E_\nu$  for given pion energy and lowest energy muons

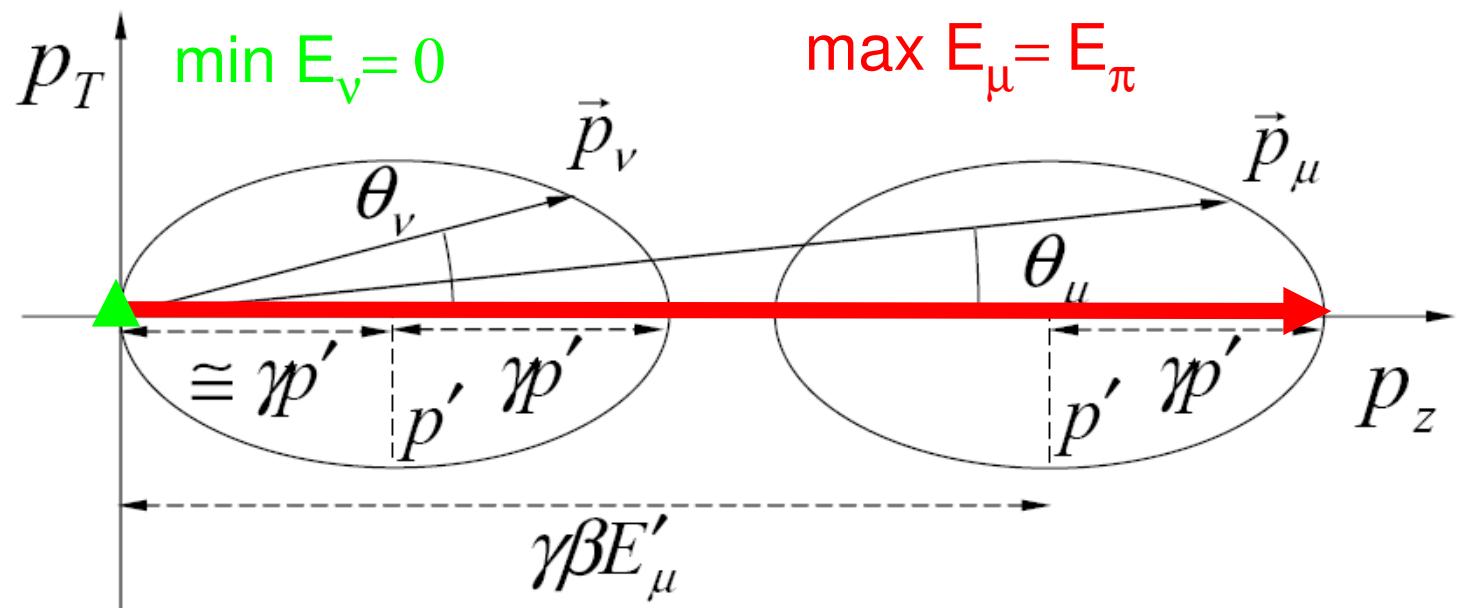
$E_\nu$	$E_\mu$	$E_\pi$
1.6	2.4	4
3	4	7

Seems to imply min  $E_\nu$  that can be seen by the monitors is 3GeV.

$$E_\nu = \frac{(1 - m_\mu^2/M^2) E}{1 - \gamma^2 \tan^2 \theta_\nu}$$



CM Frame



Laboratory Frame

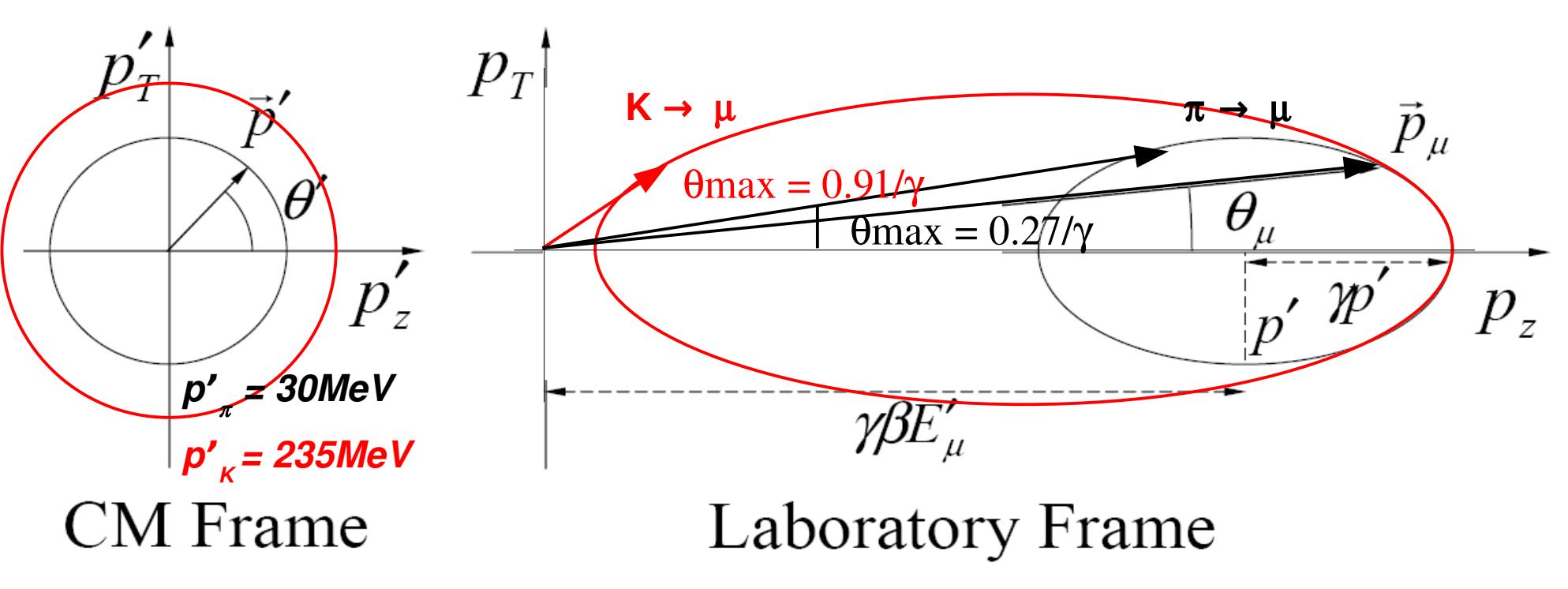
- Forward-going muons give  $E_\nu \sim 0$  and  $E_\mu \sim E_\pi$
- Muon Monitors can see lower effective pion parent threshold, just not in the same decays as give neutrinos in the  $\nu$  detectors

	$E_\nu$	$E_\mu$	$E_\pi$
Forward $\nu$	1.6	2.4	4
Forward $\mu$	0	4	4

Implies min  $E_\nu$  that can be seen by the monitors is 1.6 GeV.

$$E_\nu = \frac{(1 - m_\mu^2/M^2) E}{1 - \gamma^2 \tan^2 \theta_\nu}$$

# Kinematics

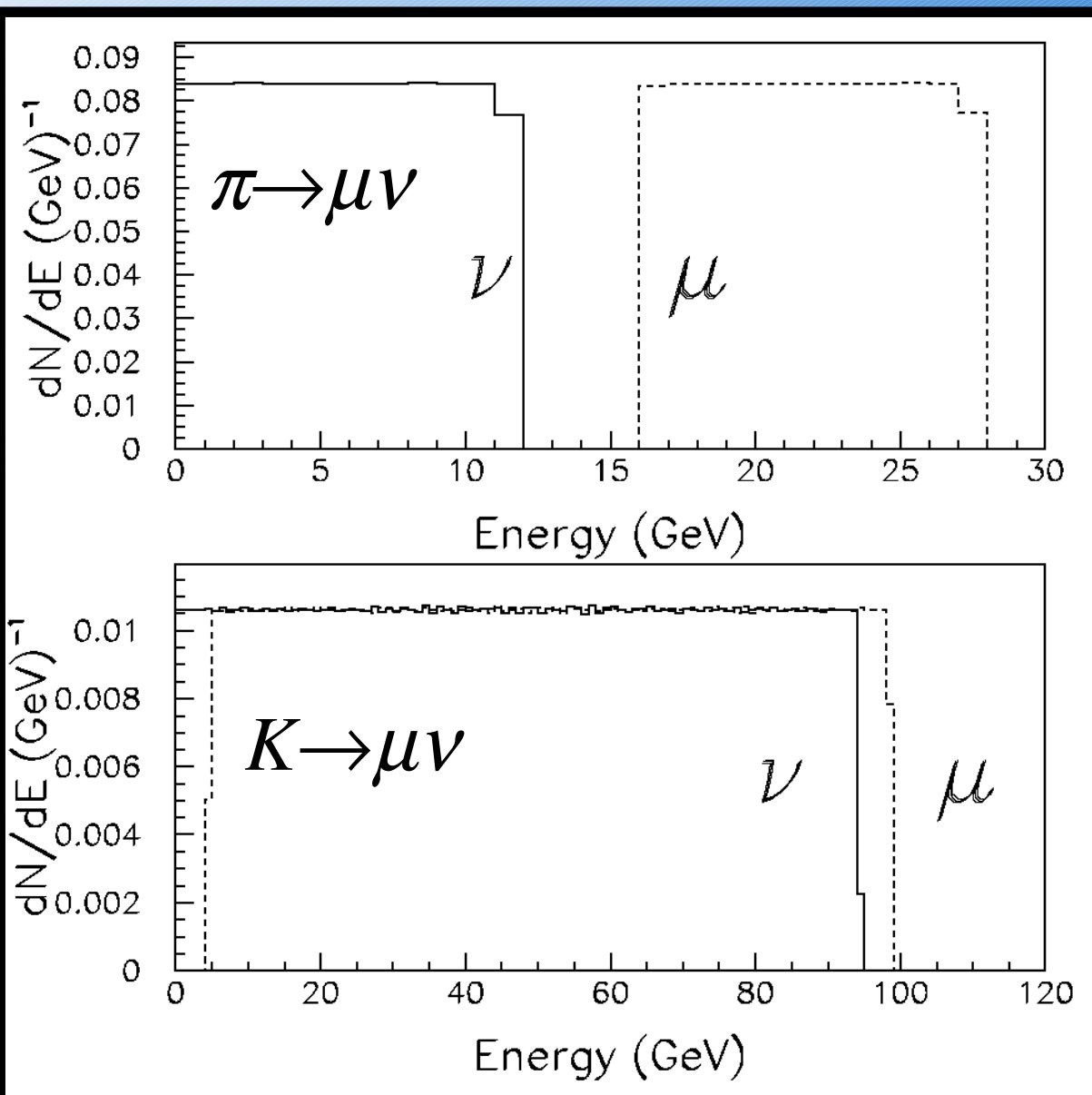


$$p'^2_T + p'^2_z = p'^2$$

$$\frac{(p_z - \beta \gamma E')^2}{\gamma^2 p'^2} + \frac{p'^2_T}{p'^2} = 1$$

- Larger Kaon mass means muons decay at larger angles than pions.
- Shorter Kaon life time means kaons decay farther upstream than pions.

# Flat Energy Spectrum



Just as many high energy  $\mu$ 's  
as high-energy  $\nu$ 's

$$\frac{dP}{dE_\nu} = \frac{1}{\left(1 - \frac{m_\mu^2}{M^2}\right) E}$$

Muon Monitors see only  
momenta  $p_\mu > 4 \text{ GeV}/c$

Such come from  $E_\pi > 4 \text{ GeV}$

In other decays, such pions  
give  $E_\nu > 1.6 \text{ GeV}$

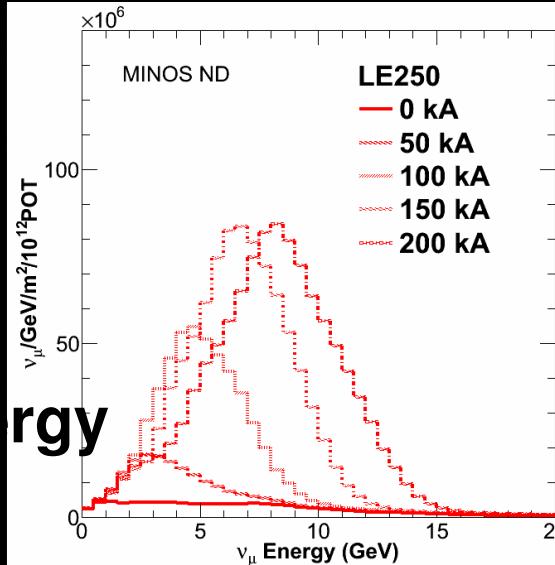
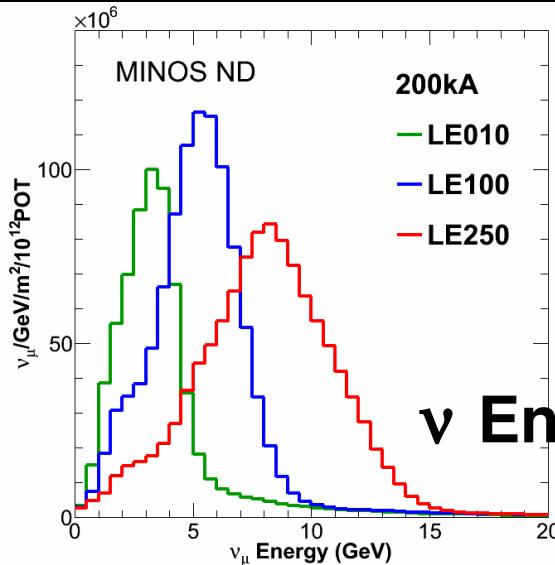
Sets actual “neutrino  
threshold” of the alcoves

$$\frac{\phi}{\nabla} \vec{E}_{\nabla} ) \leftrightarrow \phi(p_T, p_z)$$

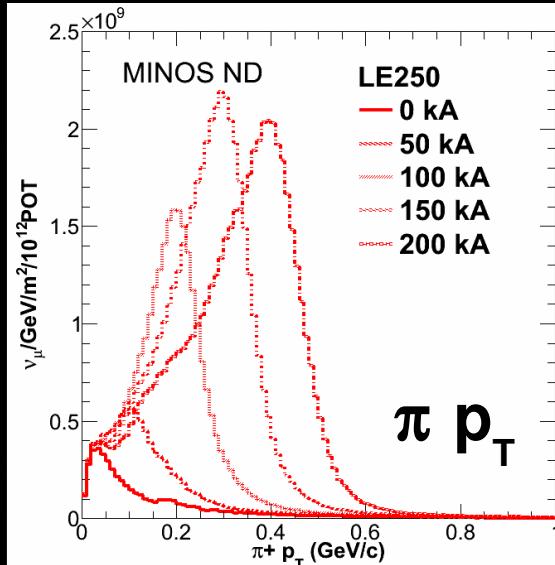
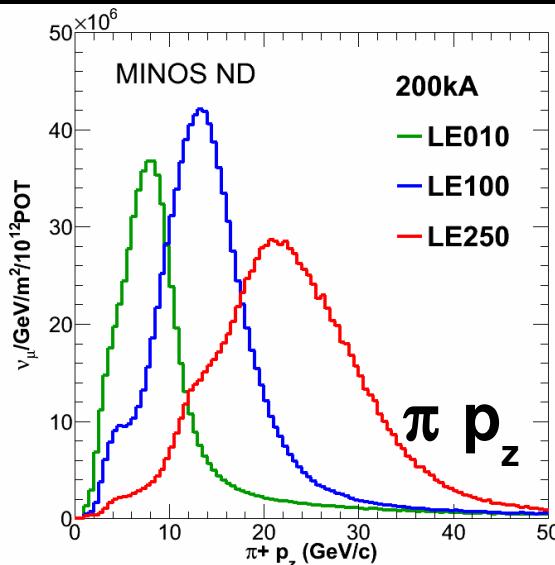
Vary Target Z

Vary Horn I

$$\frac{\phi}{\nabla} \vec{E}_{\nabla} )$$

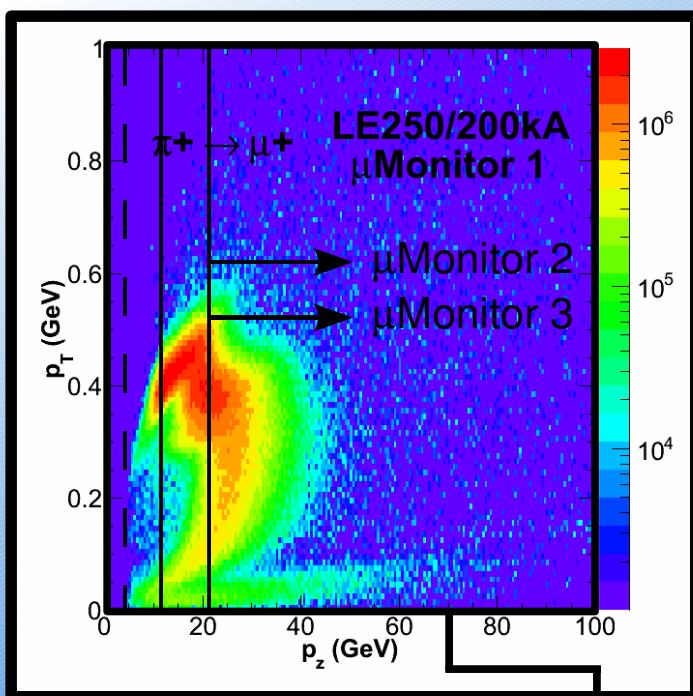


$$\phi_{\nabla}(p_T, p_z)$$

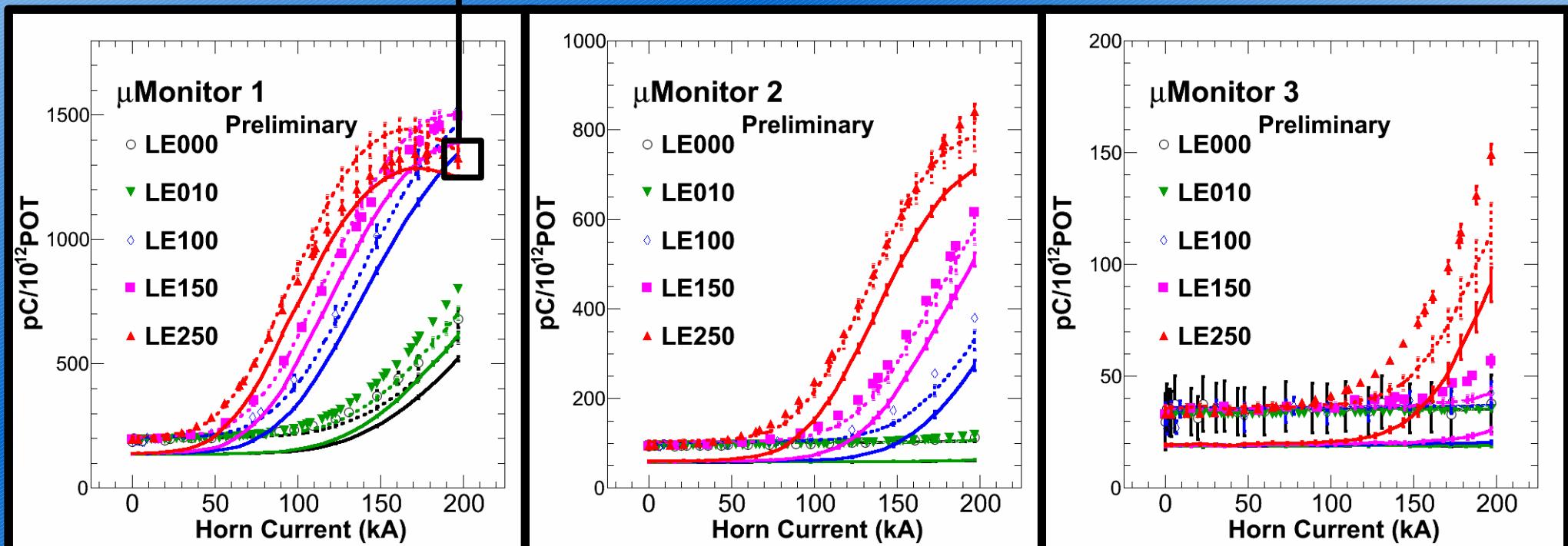


# $\mu$ Monitor Tuning

- Empirical parameterization for hadron production,  $f(p_T, p_z)$ . Warp  $p_T$  and  $p_z$  to tune default MC to  $\mu$  Monitor data.

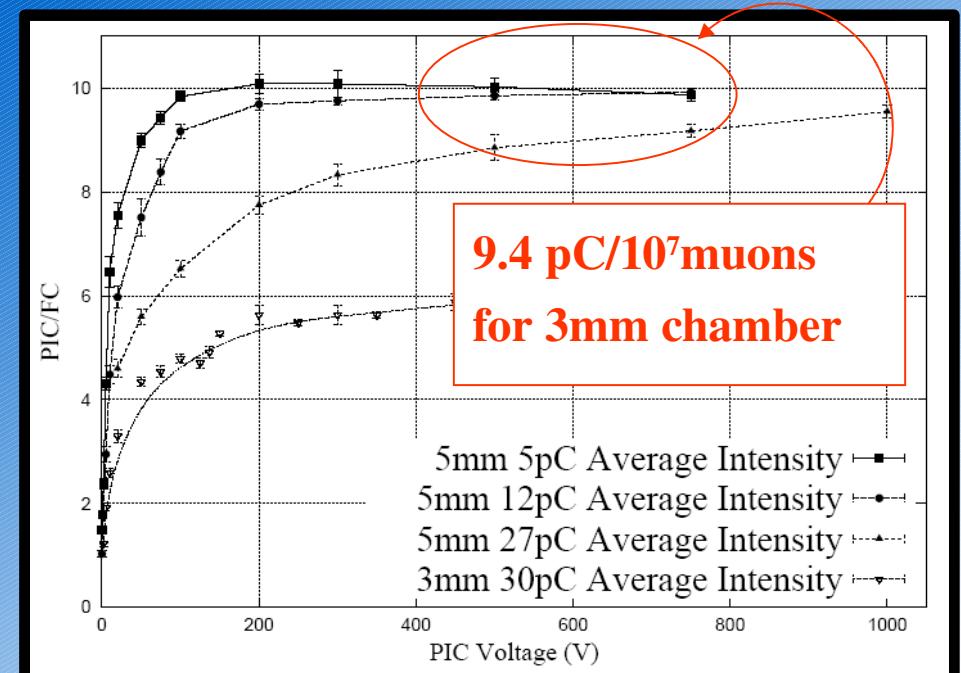
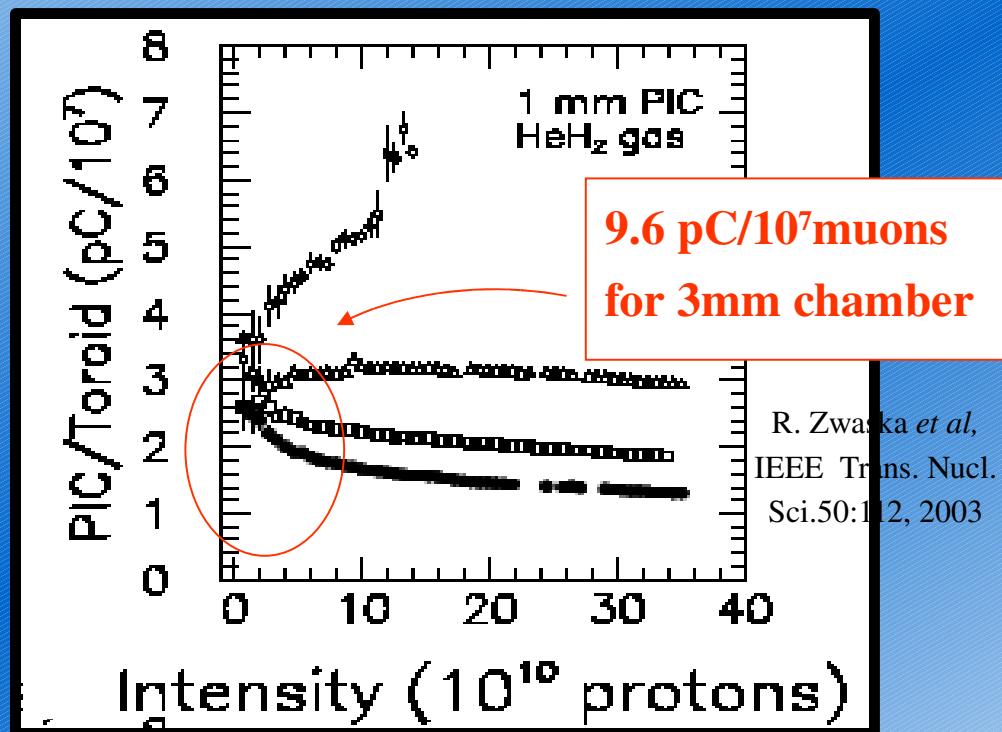


● Data      — Monte-Carlo  
 — - - Tuned Monte-Carlo

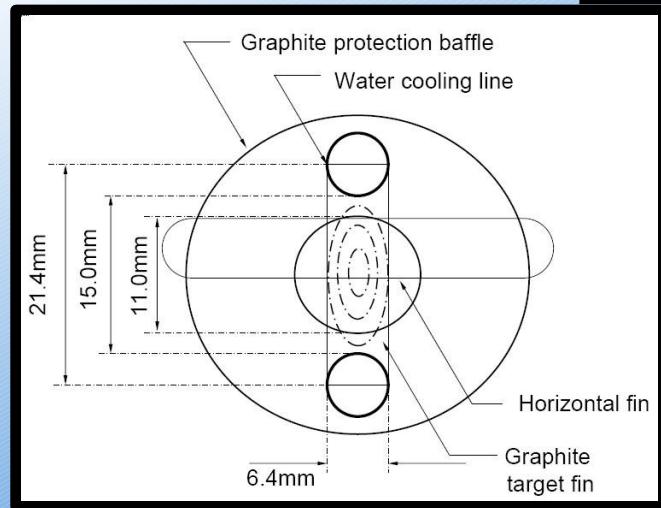


# Charge per Muon

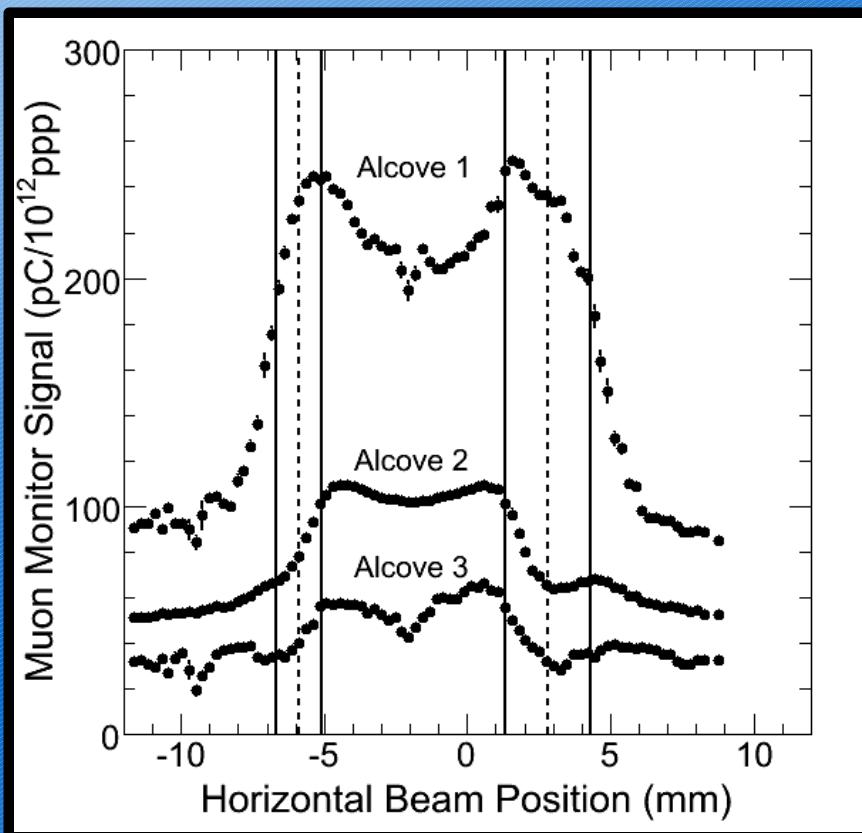
- Would like to know pCoul/muon passing through the chambers.
- This is non-trivial for two reasons
  - He gas is easily contaminated (20ppm O<sub>2</sub> causes 5–10% variation in this scale factor)
- Taking  $(dE/dx)$  for a minimum-ionizing particle and  $w=42$  eV/ion-pair, can calculate ionization per muon. Some texts claim  $w=31$  eV/i.p. for ‘dirty’ He. Using that, we’d expect approximately 5.5 pC/10<sup>7</sup>muons.
- We have two beam tests (BNL e- beam, FNAL p beam) which made measurements of this quantity in He gas of unknown quality (cylinder gas of 99.995% purity, but chamber contamination?). These might actually be well-translated to present gas system. I will scale them to the expectation for a 3mm gap chamber (like μMons)



# Dump Backgrounds

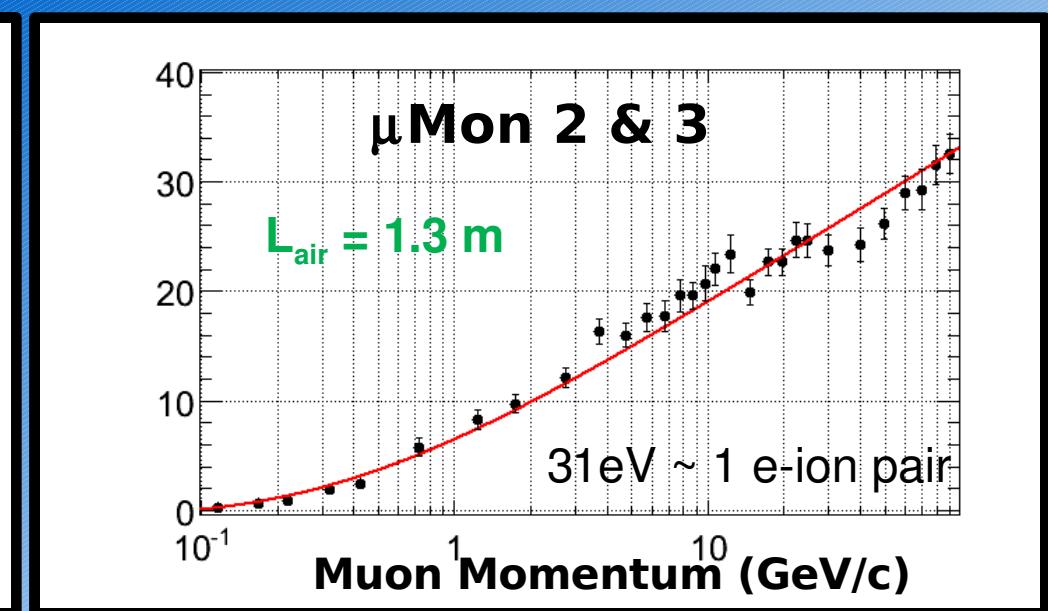
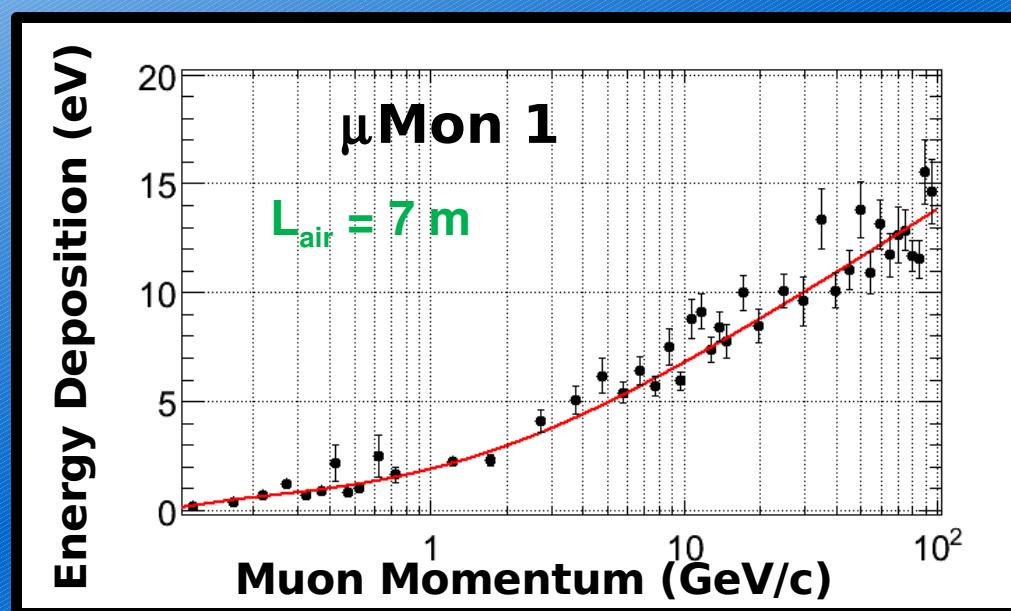
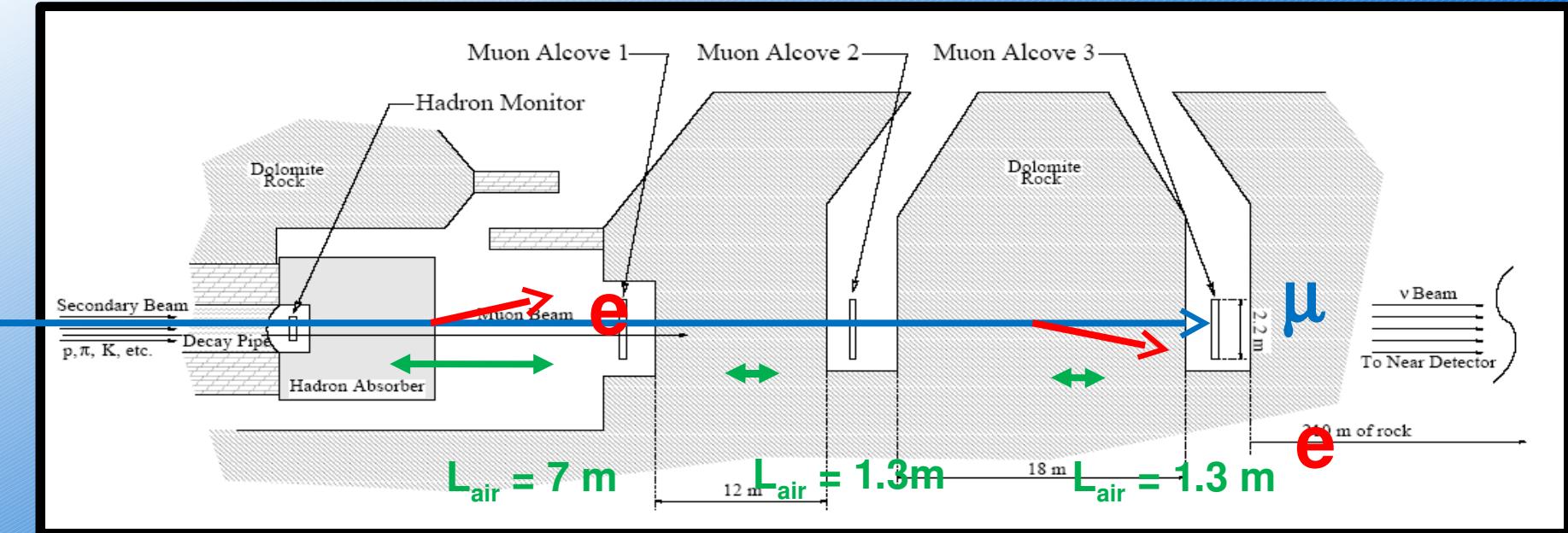


- 13.5% of proton beam doesn't interact in NuMI target  $\Rightarrow$  transported to absorber creating muons, neutrons, gammas.
- Measurements from No-Target spills
- Measurements from Target Scans.
- Take average.

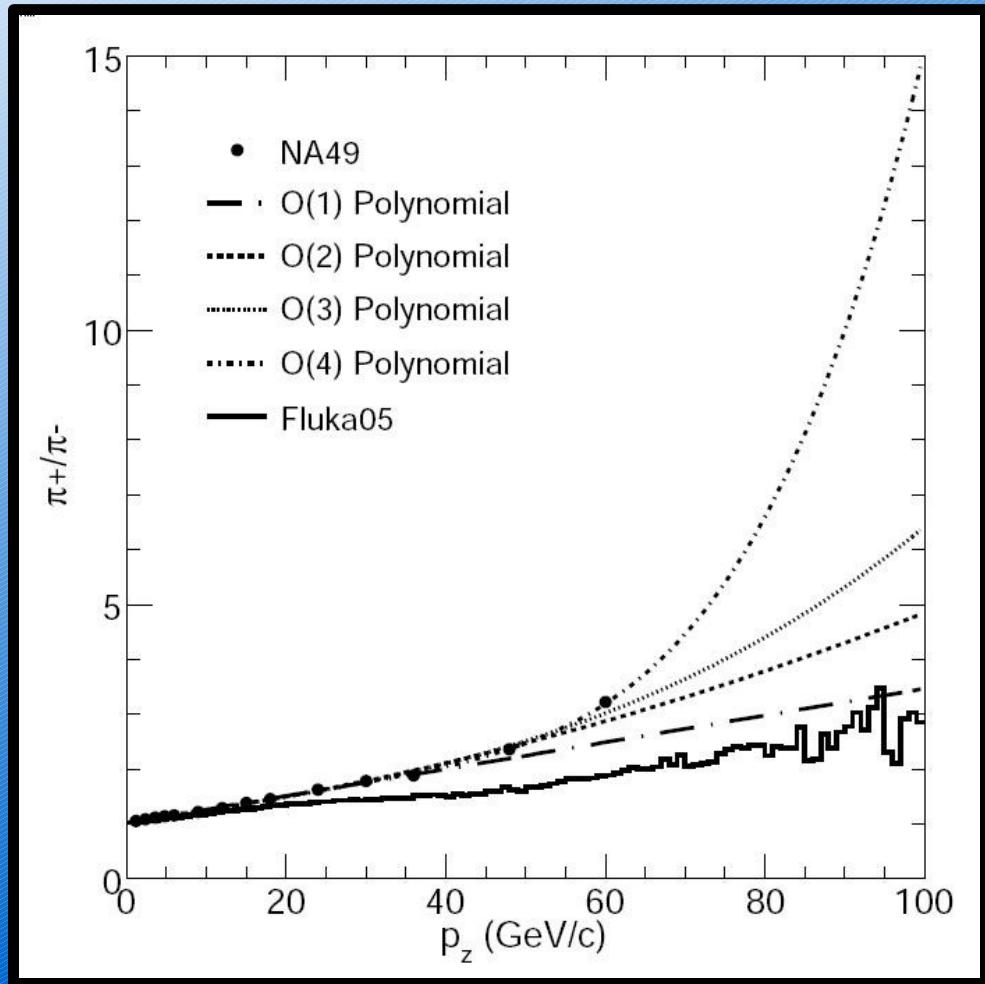


Muon Alcove	Signal Before Gas Corrections ( $\text{pC}/10^{12} \text{ ppp}$ )	Signal After Gas Corrections ( $\text{pC}/10^{12} \text{ ppp}$ )	Extrapolated to 13.5% Unreacted Proton Beam
Data from No-Target Spills (Section 4.1)			
1	$270 \pm 22$	$251 \pm 21$	$34 \pm 3$
2	$59 \pm 5$	$54 \pm 5$	$7.3 \pm 1$
3	$20 \pm 15$	$12 \pm 9$	$1.6 \pm 1.2$
Data from Target Scans (Section 4.2)			
1	$236 \pm 13$	$223 \pm 16$	$30 \pm 2$
2	$63 \pm 4$	$58 \pm 4$	$7.8 \pm 0.5$
3	$29 \pm 2$	$20 \pm 3$	$2.7 \pm 0.4$

# $\delta$ -Rays (Knock-On Electrons)



# Uncertainties



- Particle Ratios.
  - $\pi^+/\pi^-$
  - $K^+/\pi^+$ .
- Data corrections.
- $pC/\mu$  conversion factor .
- Backgrounds.
  - Dump.
  - $\delta$ -rays.