

# Progress in PDFs

PDF Status  
Evolution  
Nuclear Corrections  
Target Mass Corrections

Strange Quark PDF  
Drell-Yan  
Heavy Quark Effects

Fred Olness

SMU

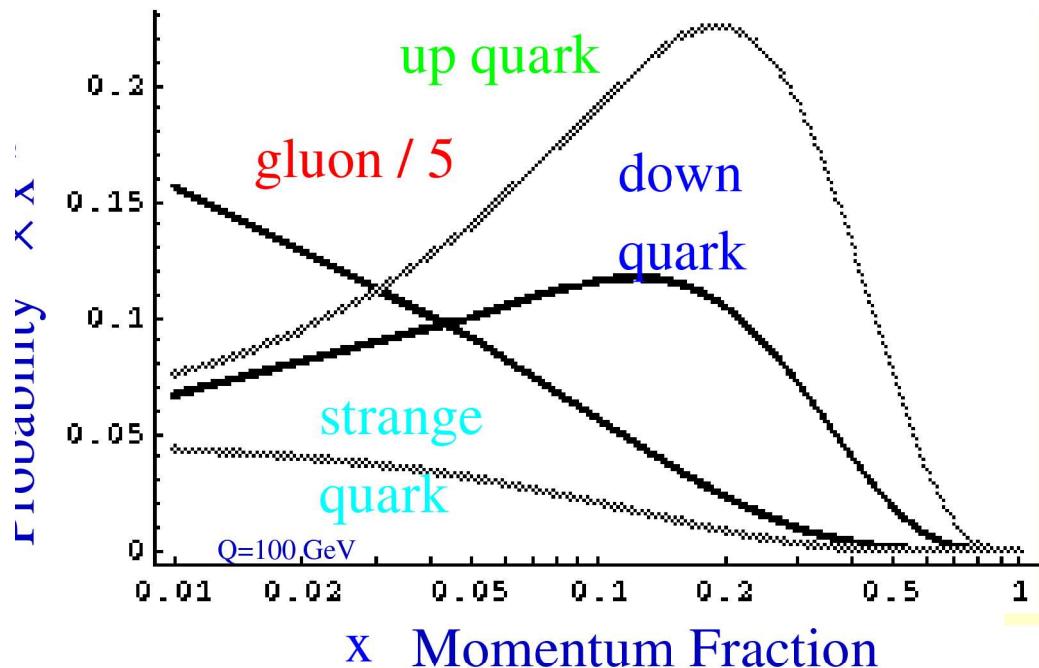
Conspirators:  
P. Nadolsky, S. Berge, I Schienbein,  
J.-Y. Yu, W. Tung, S. Kretzer,  
J. Owens, S. Kuhlmann, J. Pumplin, H. Lai  
J. Morfin, C. Keppel, V. Radeşcu, D. Mason

Workshop on Intersections of  
Nuclear Physics with  
Neutrinos and Electrons

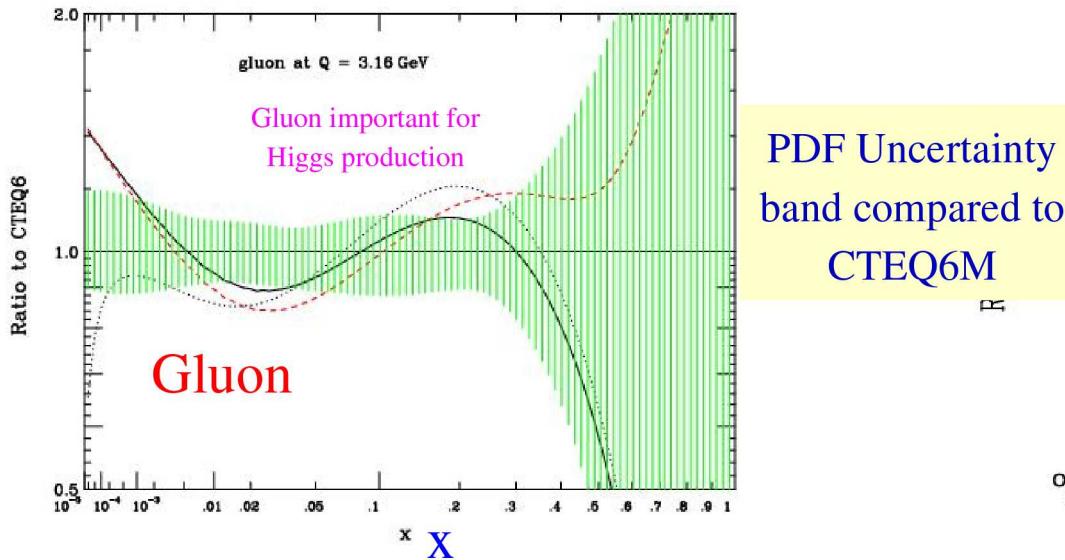
4 May 2006

*Special thanks to Jeff Owens for his APS 2005 material*

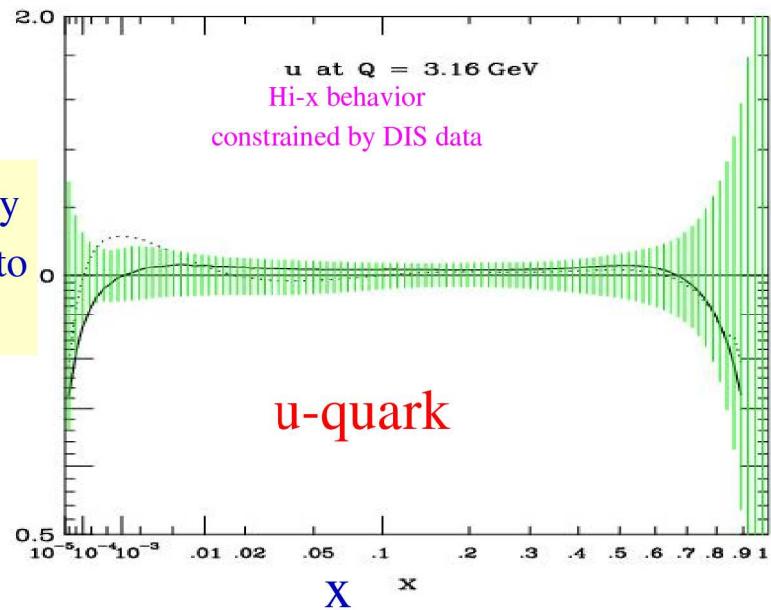
## PDF STATUS



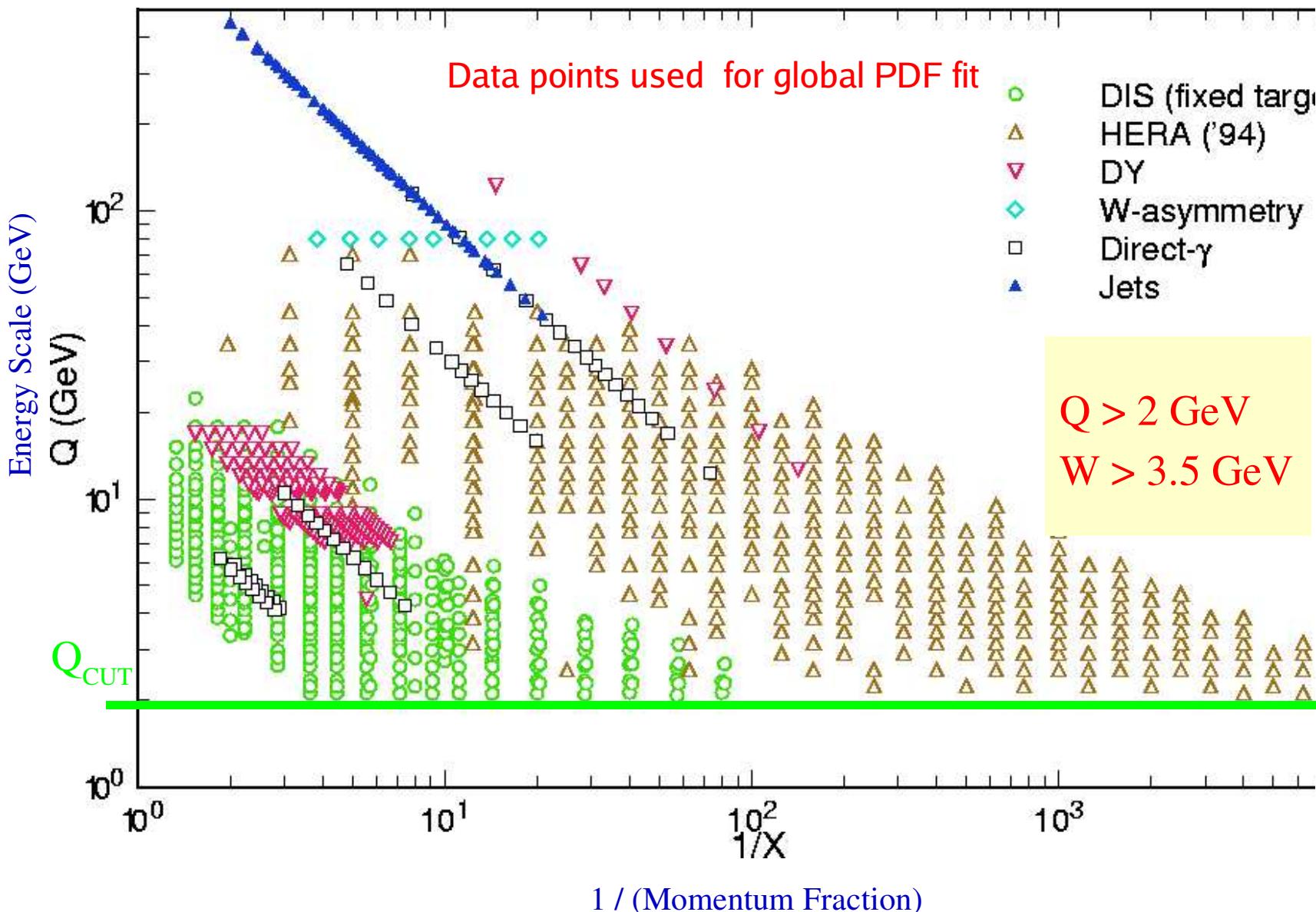
- u and d valence distributions well determined
- improved determination of flavor sea  $\bar{u}, \bar{d}, \bar{s}$
- Improved Gluon
- PDF Uncertainties



PDF Uncertainty  
band compared to  
CTEQ6M



## Many different experiments are required for Global Fit to proton structure



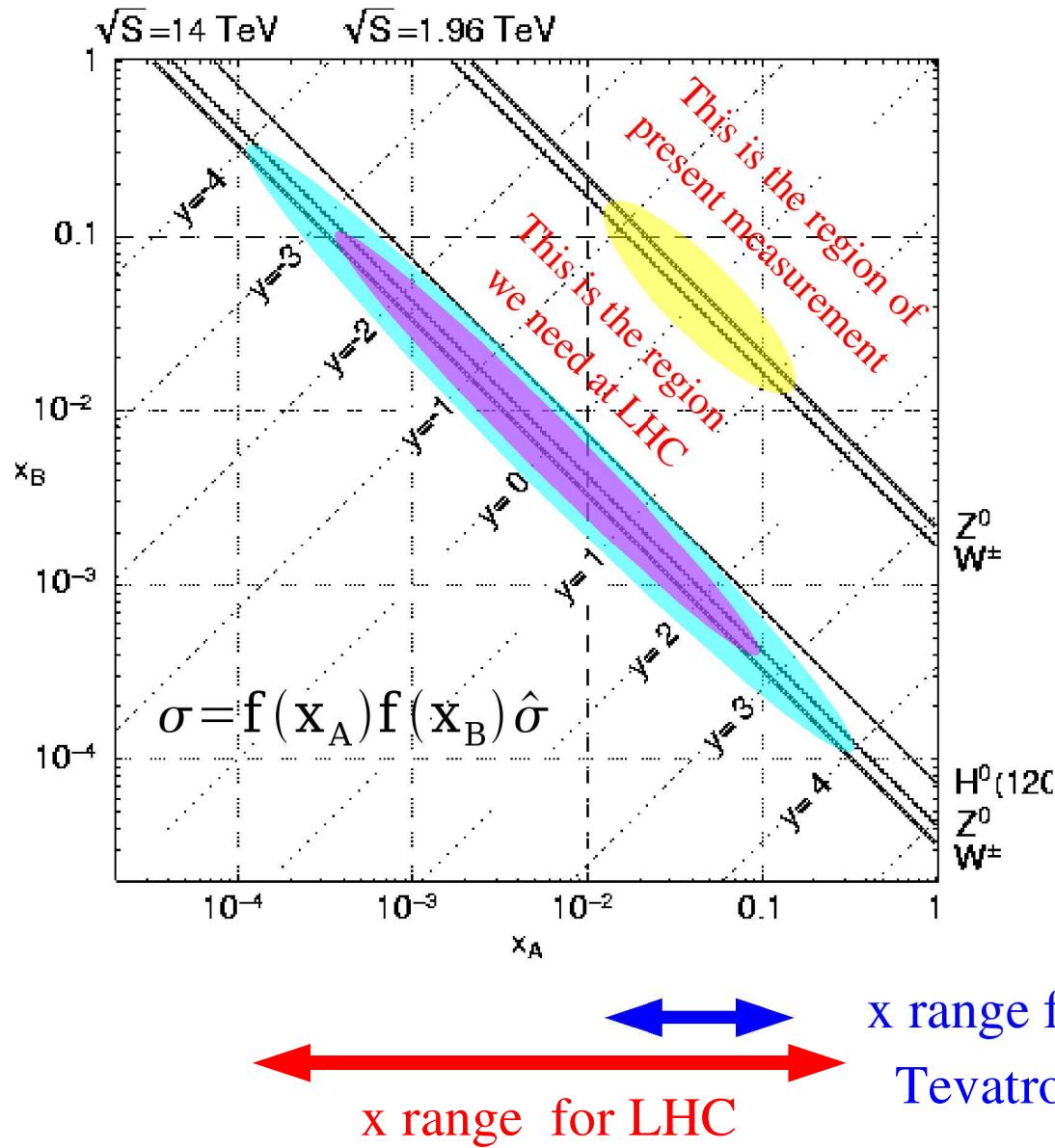
Kinematics

&

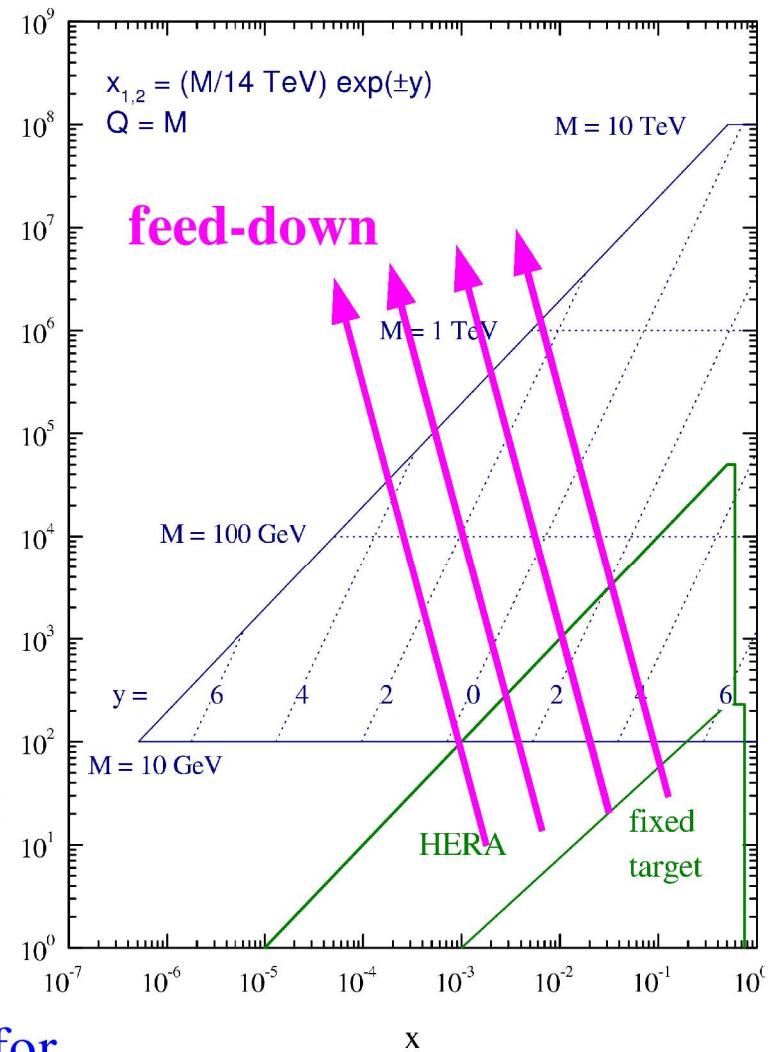
Evolution

## Low Q & Hi-x: Feeds down to Hi Q & intermediate x

### Kinematics of boson production



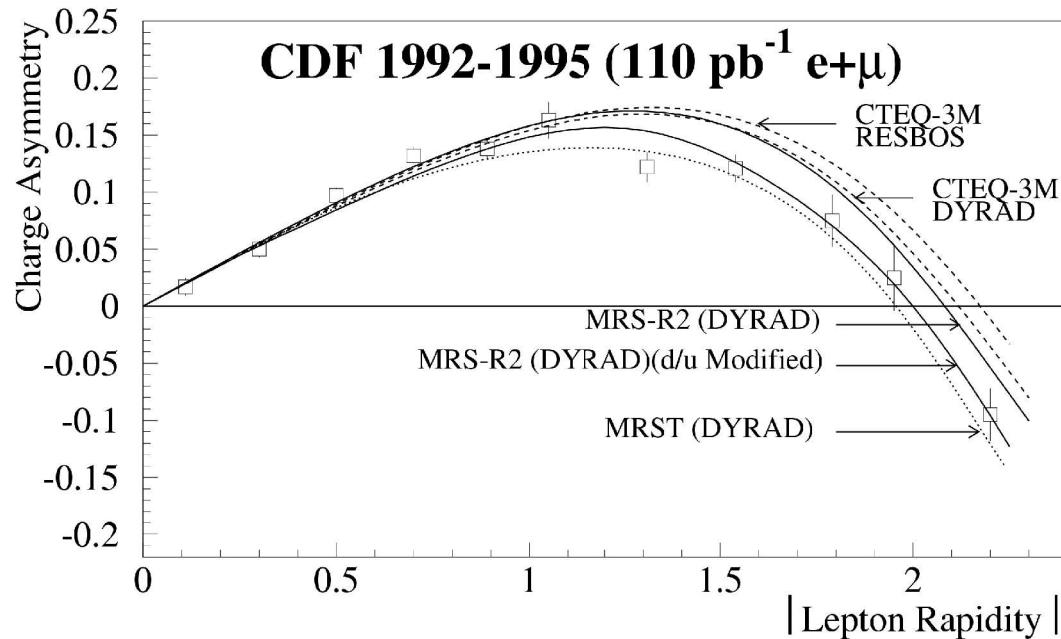
### LHC parton kinematics



borrowed from R. Thorne, et al.,  
hep-ph/0507015

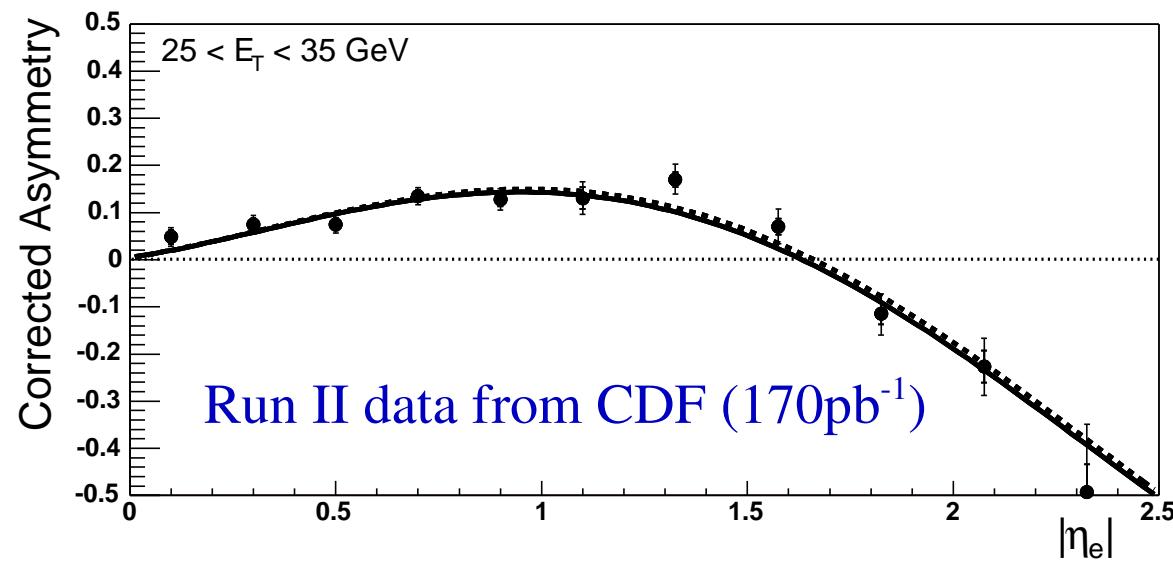
# *Nuclear Corrections*

# W Asymmetry from Tevatron: Constraints d/u



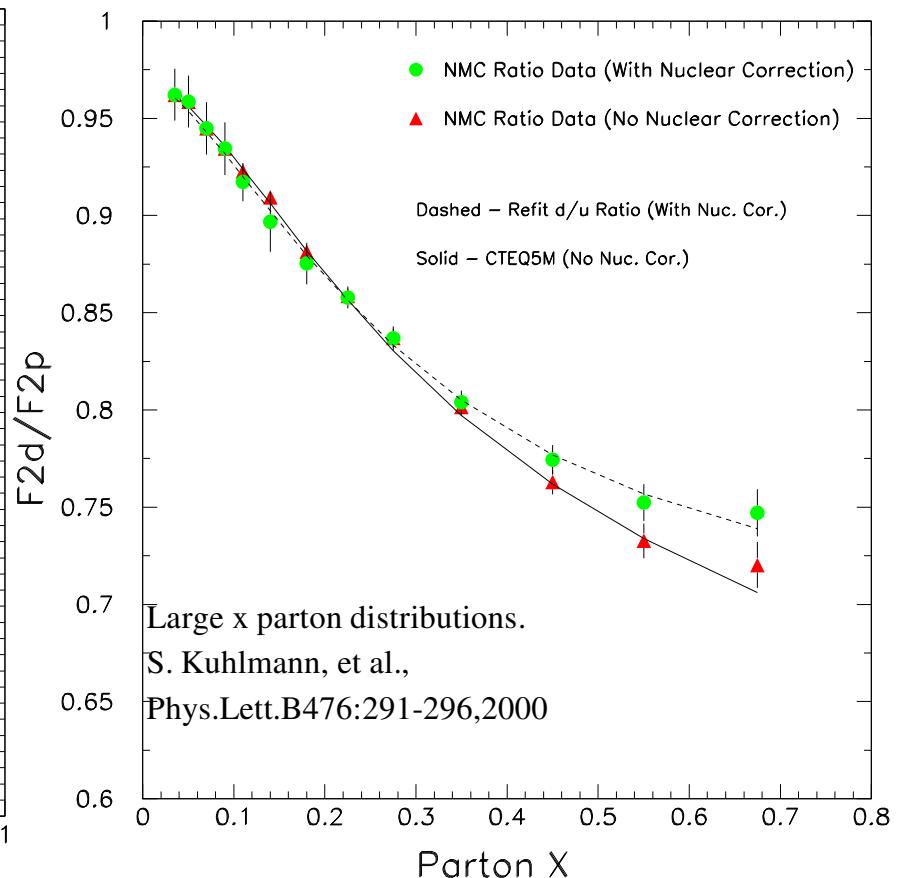
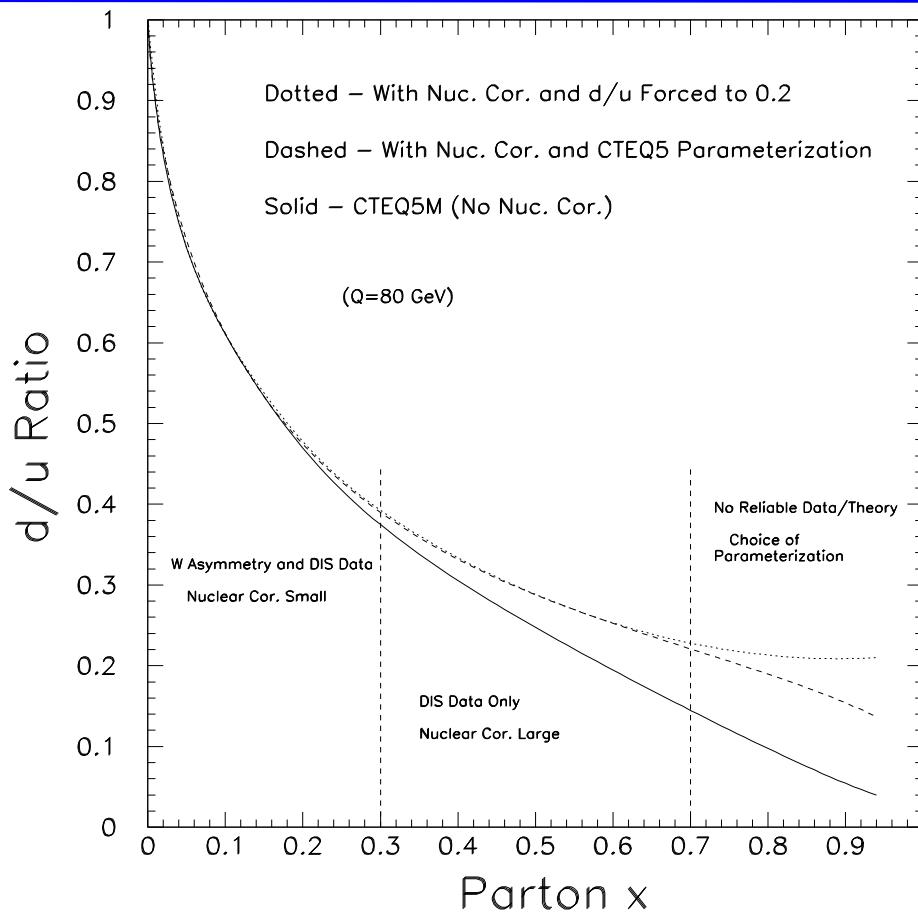
$u\bar{d} \rightarrow W^+ \rightarrow \ell^+ \nu_\ell$   
 $d\bar{u} \rightarrow W^- \rightarrow \ell^- \bar{\nu}_\ell$

Run I data provided  
constraints out to  $x \approx 0.3$



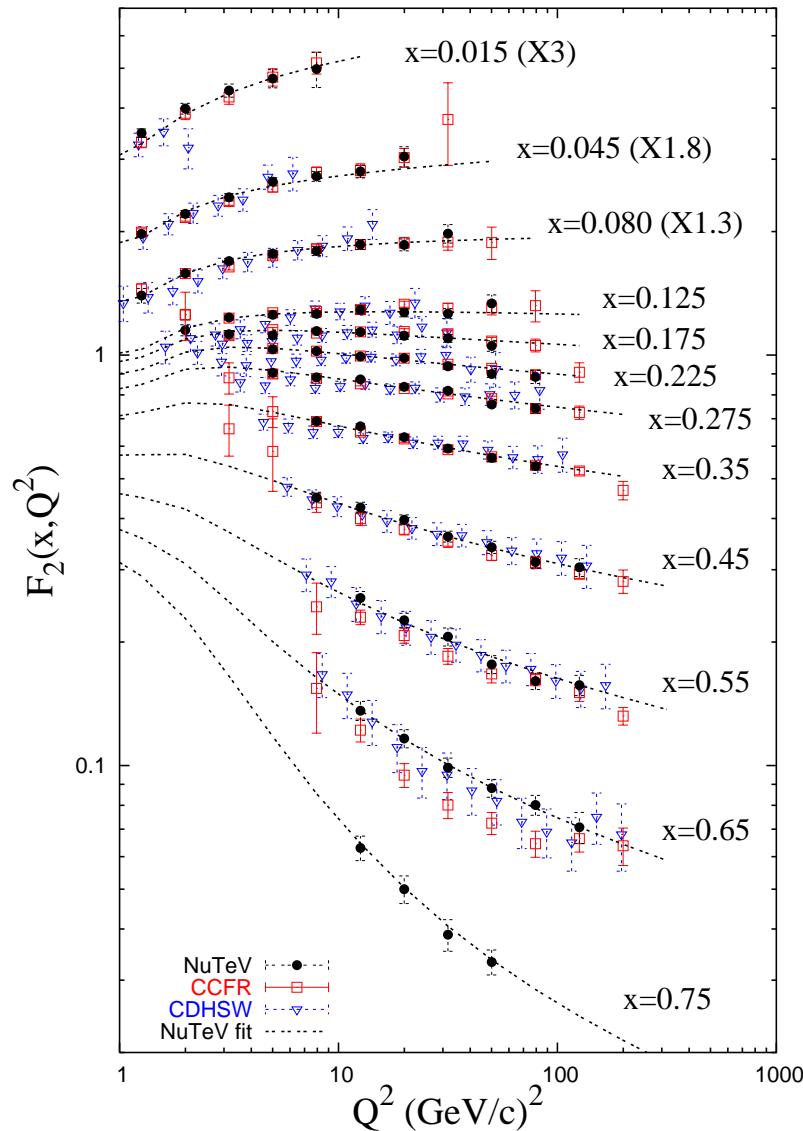
Run II  
improved statistics

# Nuclear Corrections at Large-x

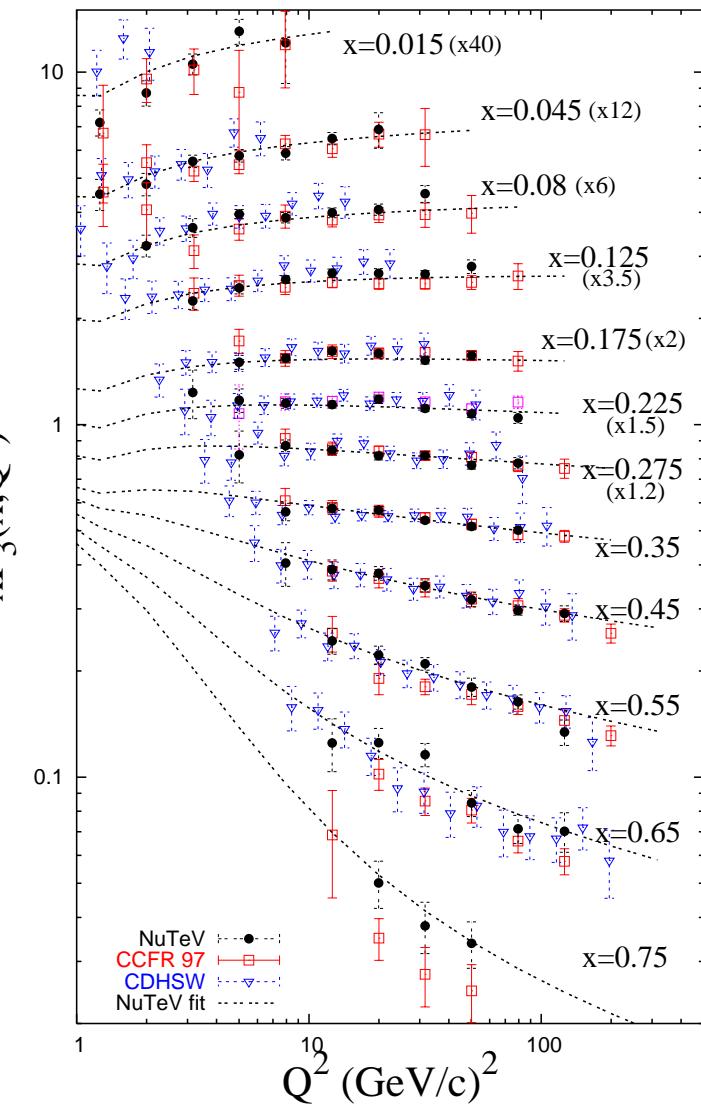


- Tevatron W-Asymmetry data constrains  $d/u$  out to  $x \approx 0.3$
- DIS data extends to higher  $x$ , but Nuclear Corrections important
- Time to revisit

# NuTeV Structure Functions

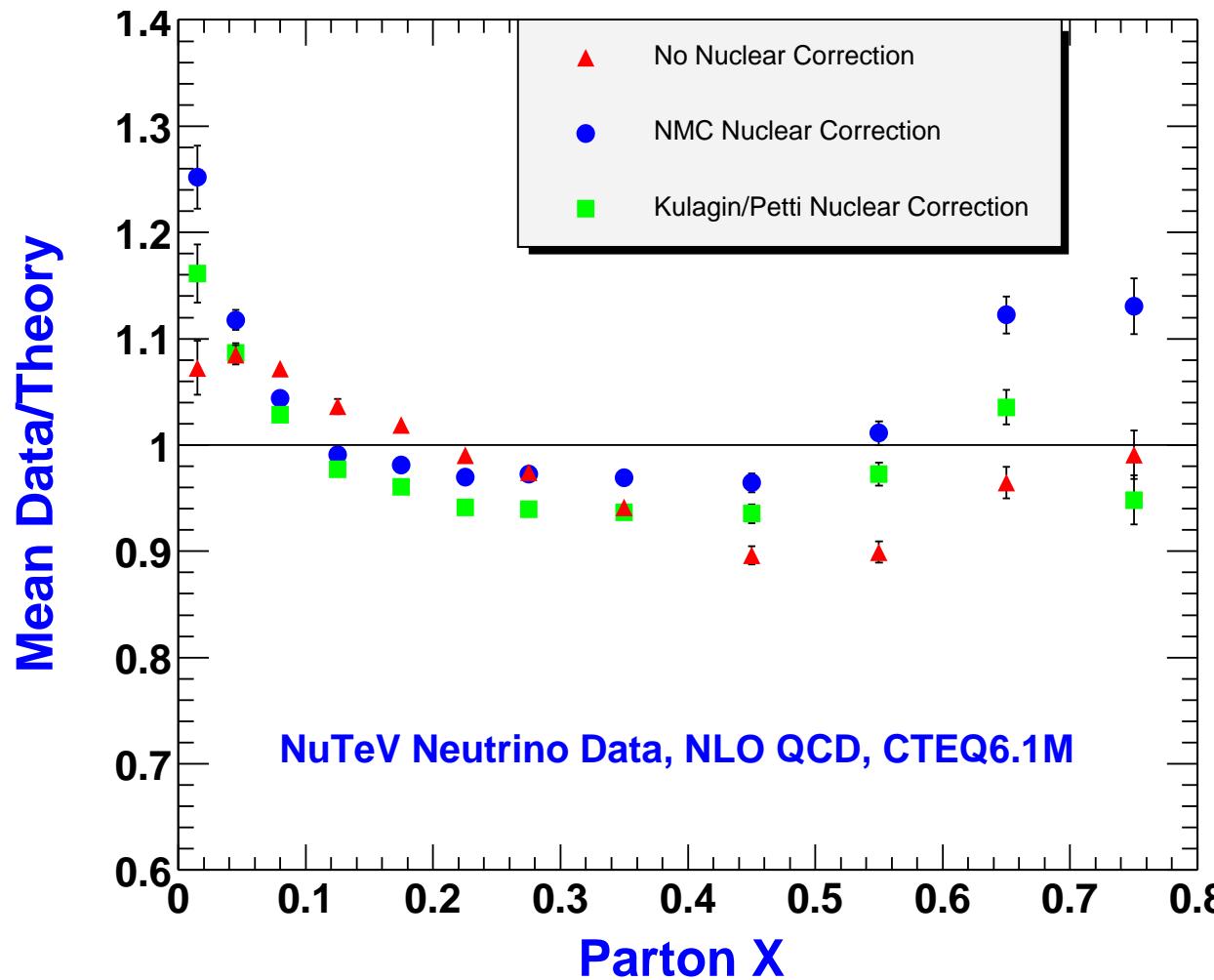


NuTeV higher at large-x  
Implications for valence PDF



Nuclear Corrections  
important at large-x

# Nuclear Corrections for Neutrino Data



NMC too large at both small & large-x

K/P does better

Shape not ideal

Large-x not too bad

Small-x: what to do??

K/P depends on  $F_{123}$

Should correction depend on NC/CC???

In progress: NuTeV Cross section data analysis

*Target  
Mass  
Corrections*

## Sources of Target Mass Corrections

---

1) Nachtmann variable  $\xi$

$$\xi = \frac{2x}{1 + \sqrt{1 + 4M^2 \frac{x^2}{Q^2}}}$$

2)  $p^- \neq \xi P^-$  results in mixing partonic & hadronic F's  
(diagonal in helicity basis)

3) Transverse momentum ( $k_T$ ) effects

4) Threshold effects as  $x \rightarrow 1$

## Target Mass Corrections:

$$F_j^{TMC}(x, Q^2) = \sum_{i=1,5} A_i^j F_j^{(0)}(\eta, Q^2) + B_i^j h_j^{(0)}(\eta, Q^2) + C_i^j g_j^{(0)}(\eta, Q^2)$$

Kretzer, Reno PRD69, 034002 (2004)

$$F_j^{(0)}(\eta, Q^2) \equiv \left\{ \lim_{M \rightarrow 0} F_j(x, Q^2) \right\} \Big|_{x \rightarrow \eta}$$

$$\bar{\eta} = x R_M R_{ij}$$

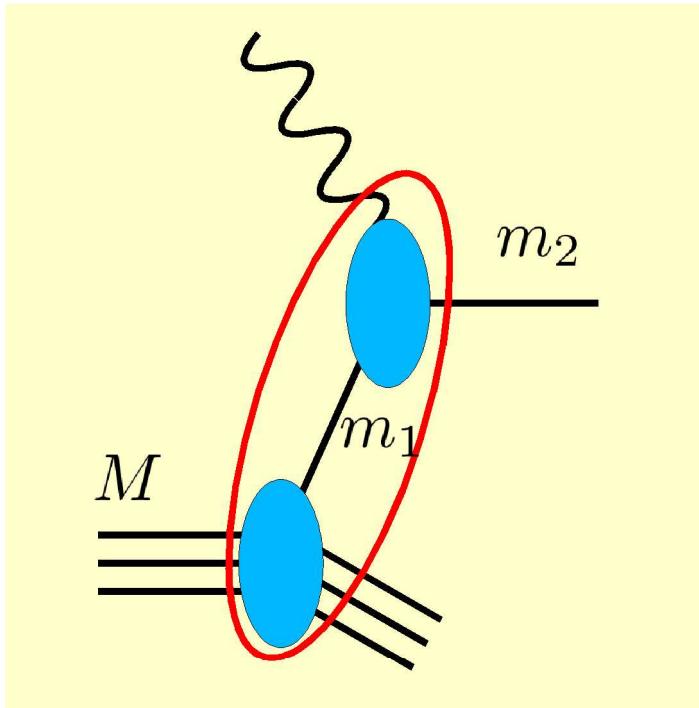
$$\eta = x R_M$$

$$R_M = \frac{2}{1 + \sqrt{1 + 4x^2 M^2 / Q^2}}$$

$$R_{ij} = \frac{(Q^2 - m_1^2 + m_2^2) + \Delta}{2Q^2}$$

$$\Delta = \Delta[-Q^2, m_1^2, m_2^2]$$

$$\Delta[a, b, c]^2 = a^2 + b^2 + c^2 - 2(ab + bc + ca)$$



## Size of TMC vs. Q and X

---

$$F_j^{TMC}(x, Q^2) = \sum_{i=1,5} A_i^j F_j^{(0)}(\eta, Q^2) + B_i^j h_j^{(0)}(\eta, Q^2) + C_i^j g_j^{(0)}(\eta, Q^2)$$

[1, 2, 3, 4, 10, 32, 56, 100, 178, 320, 562, 1000][1, 2, 3, 4, 10, 32, 56, 100, 178, 320, 562, 1000]

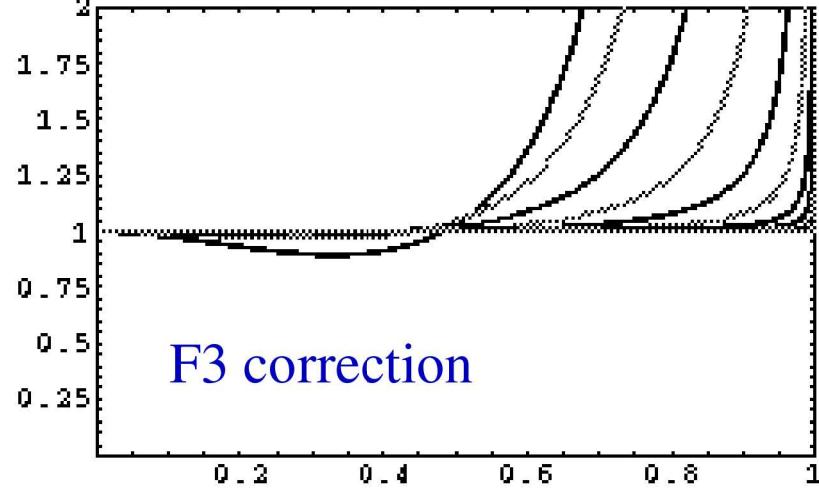
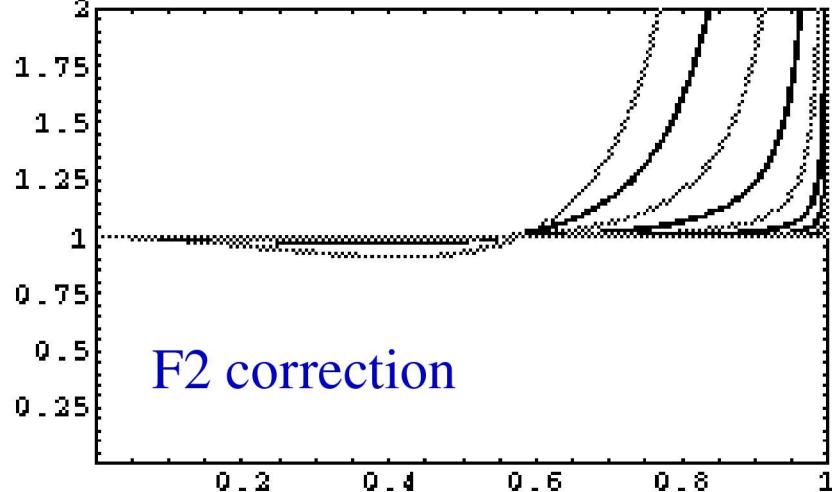
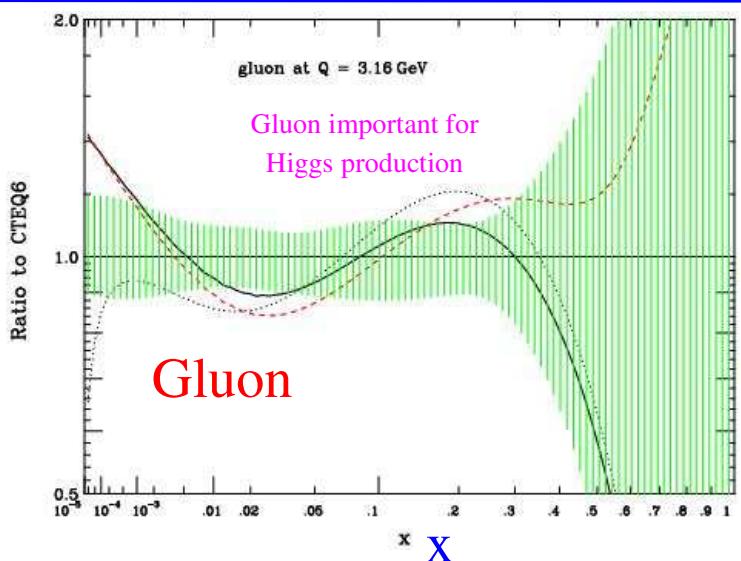


TABLE 1. Coefficients  $A_j^i$  in Eq. (3.17).

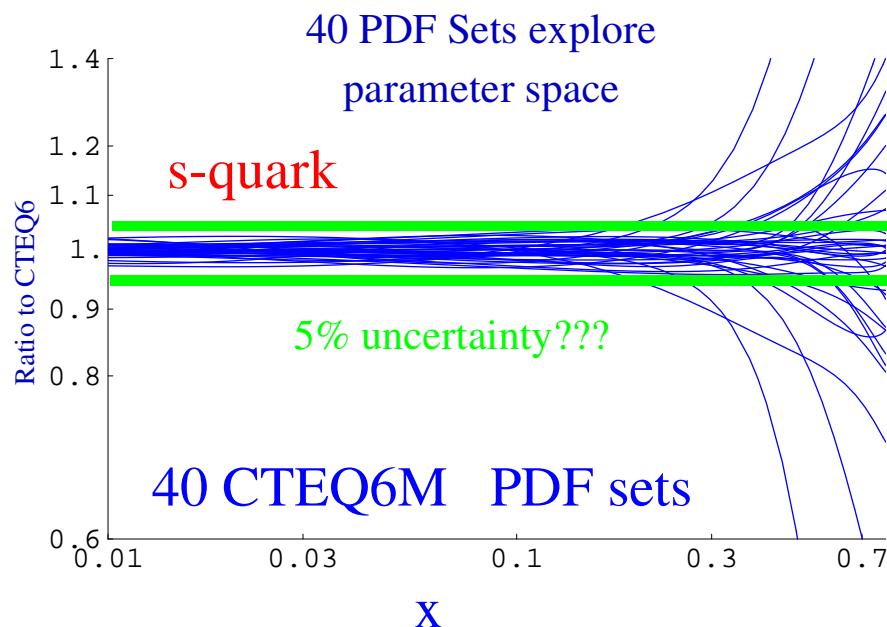
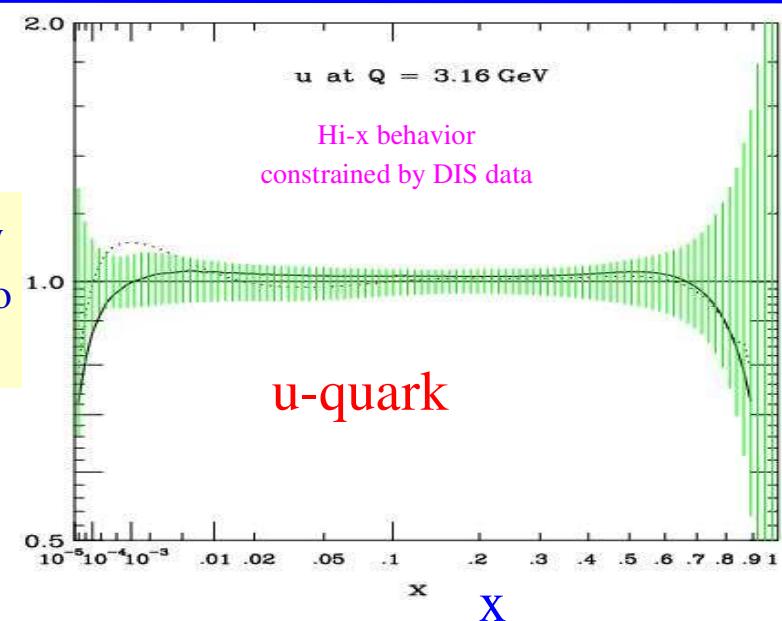
$A_j^i$	$i=1$	$i=2$	$i=3$	$i=4$	$i=5$
$j=1$	$\frac{x}{\xi p}$	0	0	0	0
$j=2$	0	$\frac{x^2}{p^2 \xi^2}$	0	0	0
$j=3$	0	0	$\frac{x}{p^2 \xi}$	0	0
$j=4$	0	$\frac{\mu^2 x^3}{p^3}$	0	$\frac{1}{(1+\mu \xi^2)}$	$-\frac{2\mu x^2}{p^2}$
$j=5$	0	$-\frac{\mu x^2}{p^3 \xi}$	0	0	$\frac{x}{p^2 \xi}$

# *Strange Quark PDF*

## What is relative uncertainty on PDFs' ???



PDF Uncertainty  
band compared to  
CTEQ6M



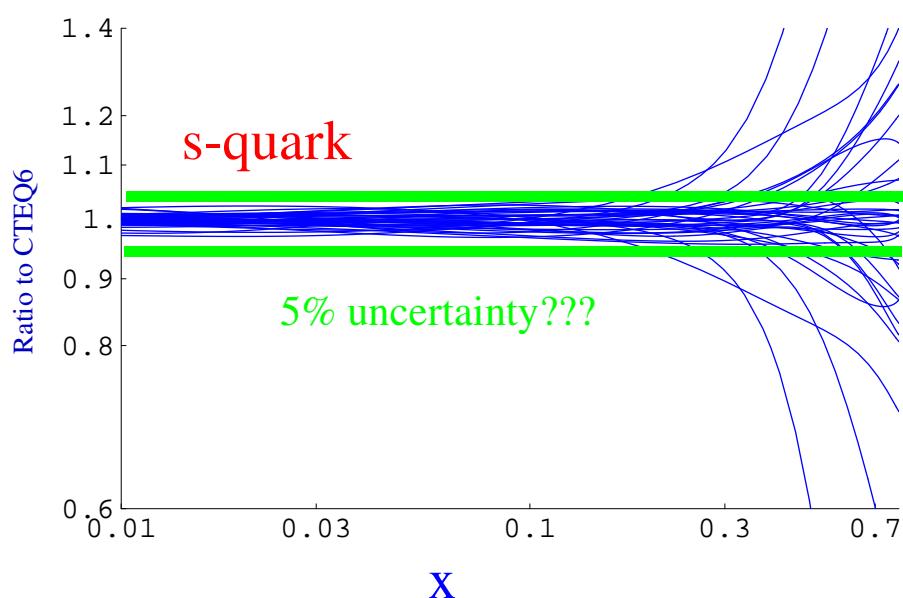
Previously,  $s(x)$  was tied to  
u-bar and d-bar via kappa:

$$s(x) = \bar{s}(x) = \kappa \frac{\bar{u}(x) + \bar{d}(x)}{2}$$

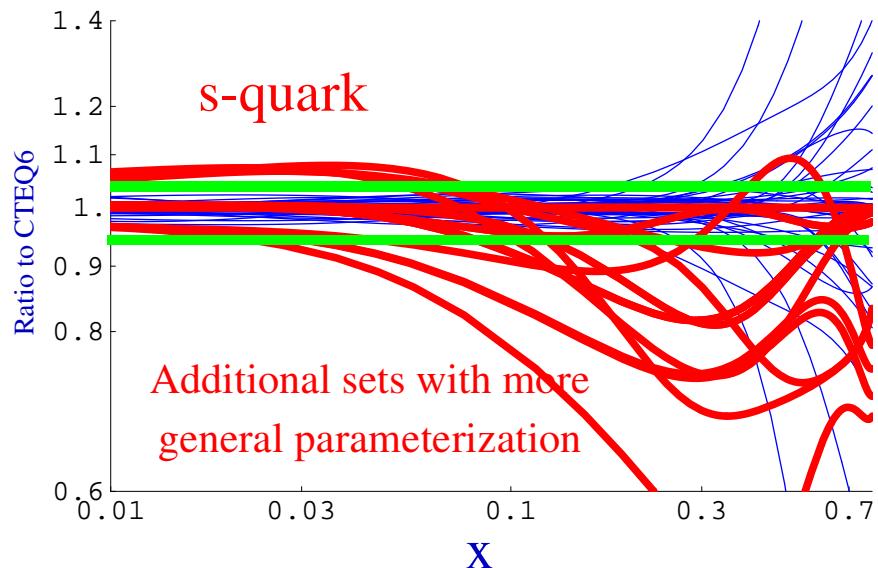
**Question:** Do we really know  
the s-quark PDF to 5%???

## What is true uncertainty on s-quark PDF???

40 CTEQ6M PDF sets



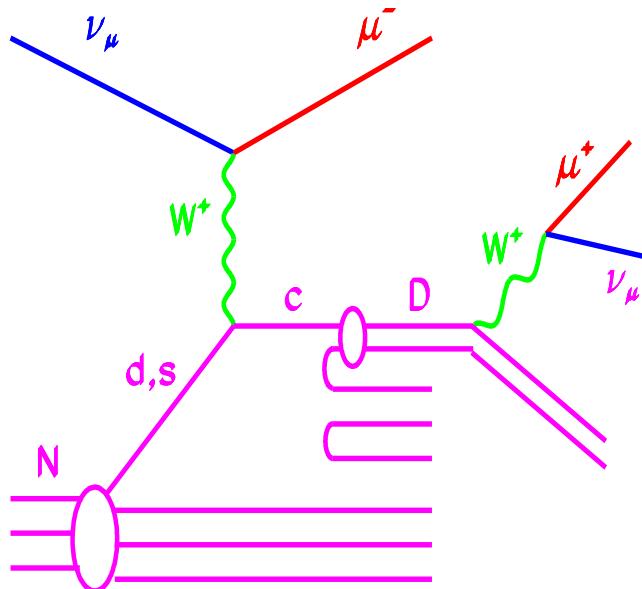
Closer to the true error



Curves shown are examples; this is not an exhaustive set

Warning: The Director General has determined the band of PDF's can greatly underestimate the true uncertainty

## Dimuons are ideal signal of s(x)



di-muon	NuTeV	CCFR	Combined
Neutrino	5012	5030	10042
Anti-Nu	1458	1060	2518

- \* High stats & high precision data
- \* Best constraints on strange quark

$$\frac{d\sigma_{\mu^\pm \mu^\mp}^+}{dx dy} = \int d\Gamma d\Omega \frac{d\sigma_{\mu^\mp c}}{dx dy d\Gamma} \otimes D_c(\Gamma) \otimes \Delta_c(\Omega)|_{E_{\mu^\pm} > 5 \text{ GeV}}$$

Di-muon  
cross-section

Charm  
Production  
cross-section

Fragmentation  
Function

Decay  
Distribution

## Global Fit: vary $s(x)$ distribution

$\chi^2 / \text{DOF}$	CTEQ6M	Constrained	Mixed	Free
CCFR Nu	1.02	0.85	0.79	0.72
CCFR Nu-bar	0.58	0.54	0.59	0.59
NuTeV Nu	1.81	1.70	1.55	1.44
NuTeV Nu-bar	1.48	1.30	1.15	1.13
BCDMS F2p	1.11	1.11	1.11	1.11
BCDMS F2d	1.10	1.10	1.10	1.11
H1 96/97	0.94	0.95	0.94	0.94
H1 98/99	1.02	1.03	1.03	1.03
ZEUS 96/97	1.14	1.14	1.14	1.15
NMC F2p	1.52	1.50	1.51	1.49
NMC F2d/F2p	0.91	0.91	0.91	0.91
NMC F2d/F2p $\langle Q^2 \rangle$	1.05	1.07	1.06	1.03
CCFR F2	1.70	1.71	1.81	1.88
CCFR F3	0.42	0.42	0.44	0.42
E605	0.82	0.82	0.82	0.83
NA51	0.62	0.61	0.52	0.52
CDF $\ell$ Asym	0.82	0.83	0.82	0.82
E866	0.39	0.40	0.39	0.38
D0 Jets	0.71	0.65	0.70	0.67
CDF Jets	1.48	1.48	1.48	1.47
TOTAL	2173	2144	2142	2133

Total of 1991 data points

Reasonable  $\chi^2$  values

(*CTEQ6 did not fit di-muon data*)

More parameters,  
lower value of  $\chi^2$

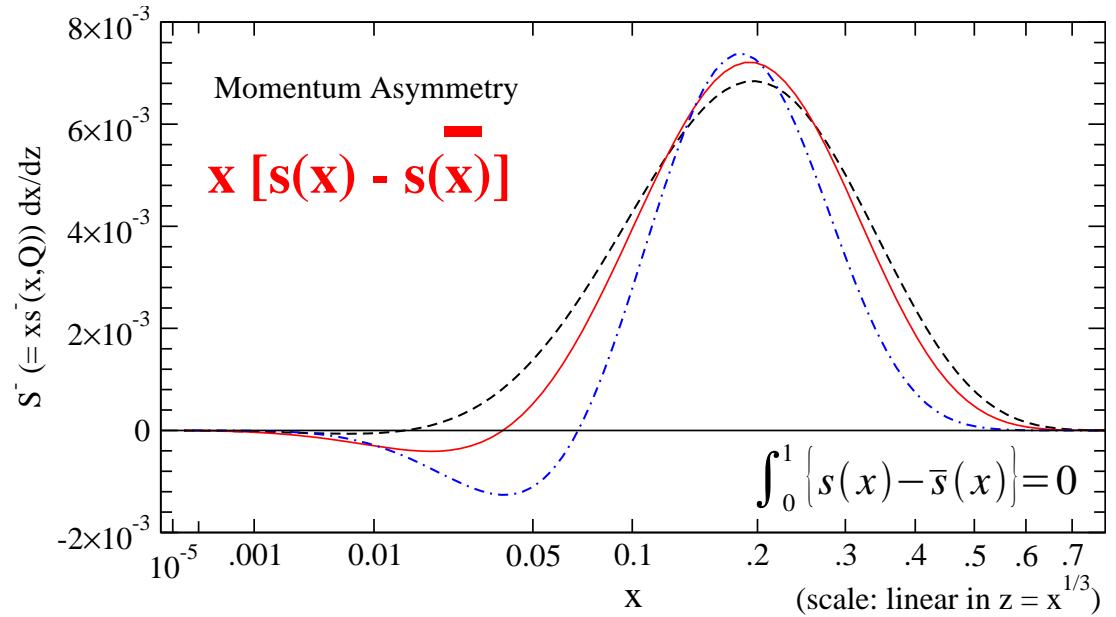
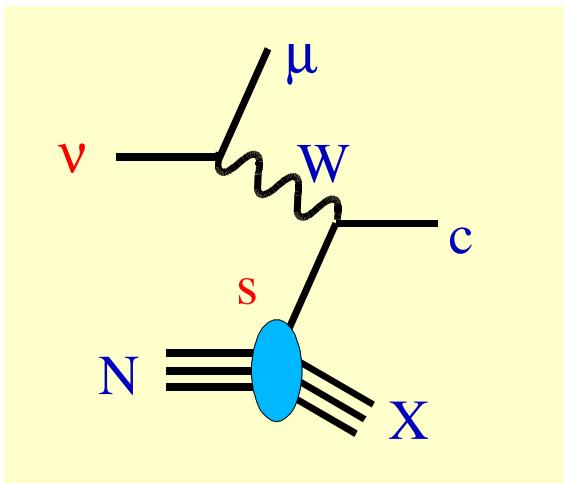
Only di-muon data is  
sensitive to  $s(x)$  !!!

⋮

Idea:  $\nu$  and  $\nu\bar{\nu}$  data  
separately determine  
 $s$  and  $s\bar{s}$  distributions

Only di-muon  
data is sensitive  
to  $s(x)$  !!!

## What does the $\Delta s(x)$ strange PDF look like?



General range of the asymmetry

$$[S^-] \equiv \int_0^1 x [s(x) - \bar{s}(x)] dx$$

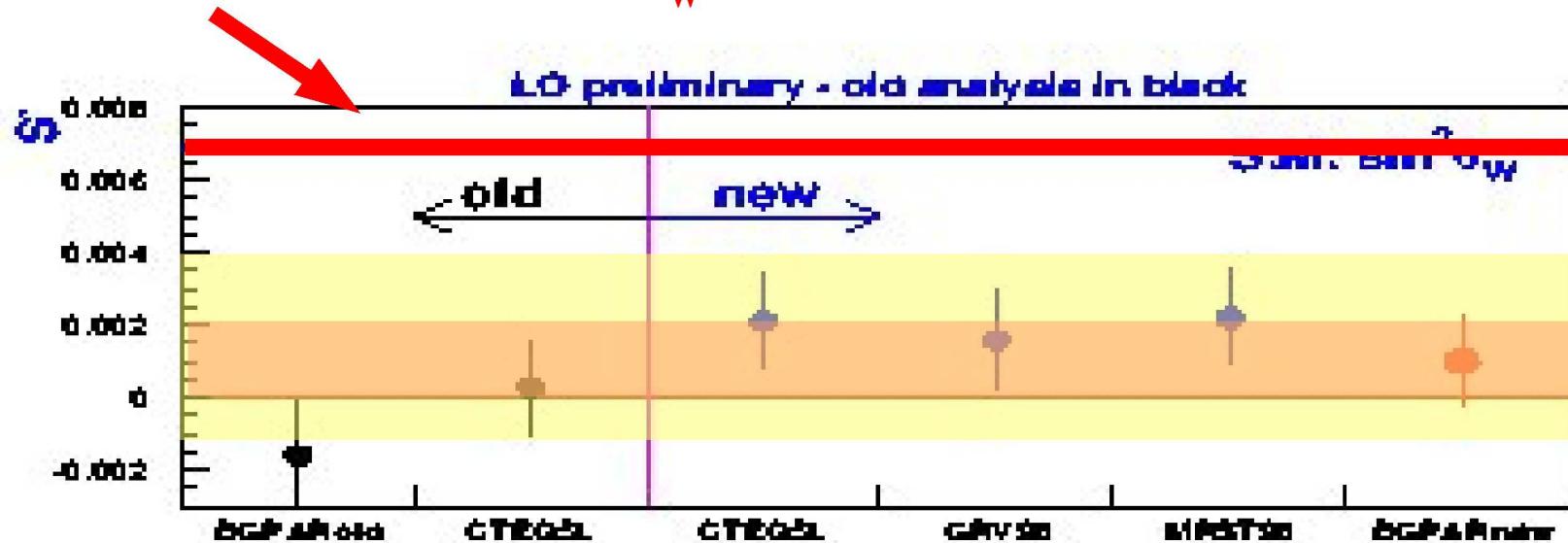
$$+0.0040 \geq [S^-] \geq -0.0010$$

$\Delta s(x)$ : large uncertainty affected by:

- charm fragmentation
- charm mass
- PDF set

## Does this solve the $\sin\theta_w$ problem???

Required to resolve  $\sin\theta_w$  discrepancy



- Tremendous new information on BOTH  $s+\bar{s}$  and  $s-\bar{s}$
- Work is ongoing: extend to higher orders
- Include this information in next generation PDF sets

D. Mason for the NuTeV Collaboration; AIP Conf.Proc.792:851-854,2005  
Kretzer, Mason, Olness PRD 65:074010 (2002)

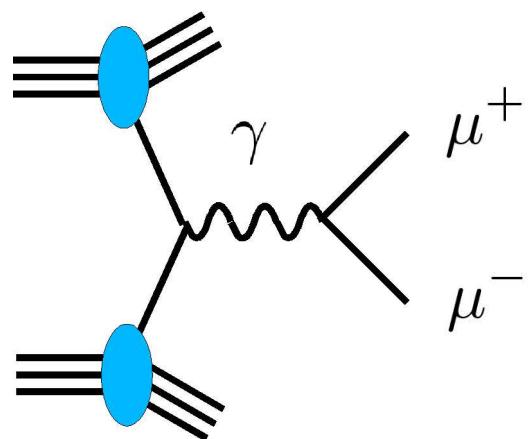
Three-loop kernel generates asymmetry

$$\langle x(s-\bar{s}) \rangle \approx -5 \times 10^{-4} \text{ @ } Q^2 20 \text{ GeV}^2$$

S. Catani, D. de Florian, G. Rodrigo,  
W. Vogelsang; Phys.Rev.Lett. 93 (2004) 152003

# Fixed Target

## Drell-Yan



## Fixed Target Drell-Yan

FNAL-E866/NuSea Collaboration (J.C. Webb et al.)

AIP Conf.Proc.549:532-535,2002 A1

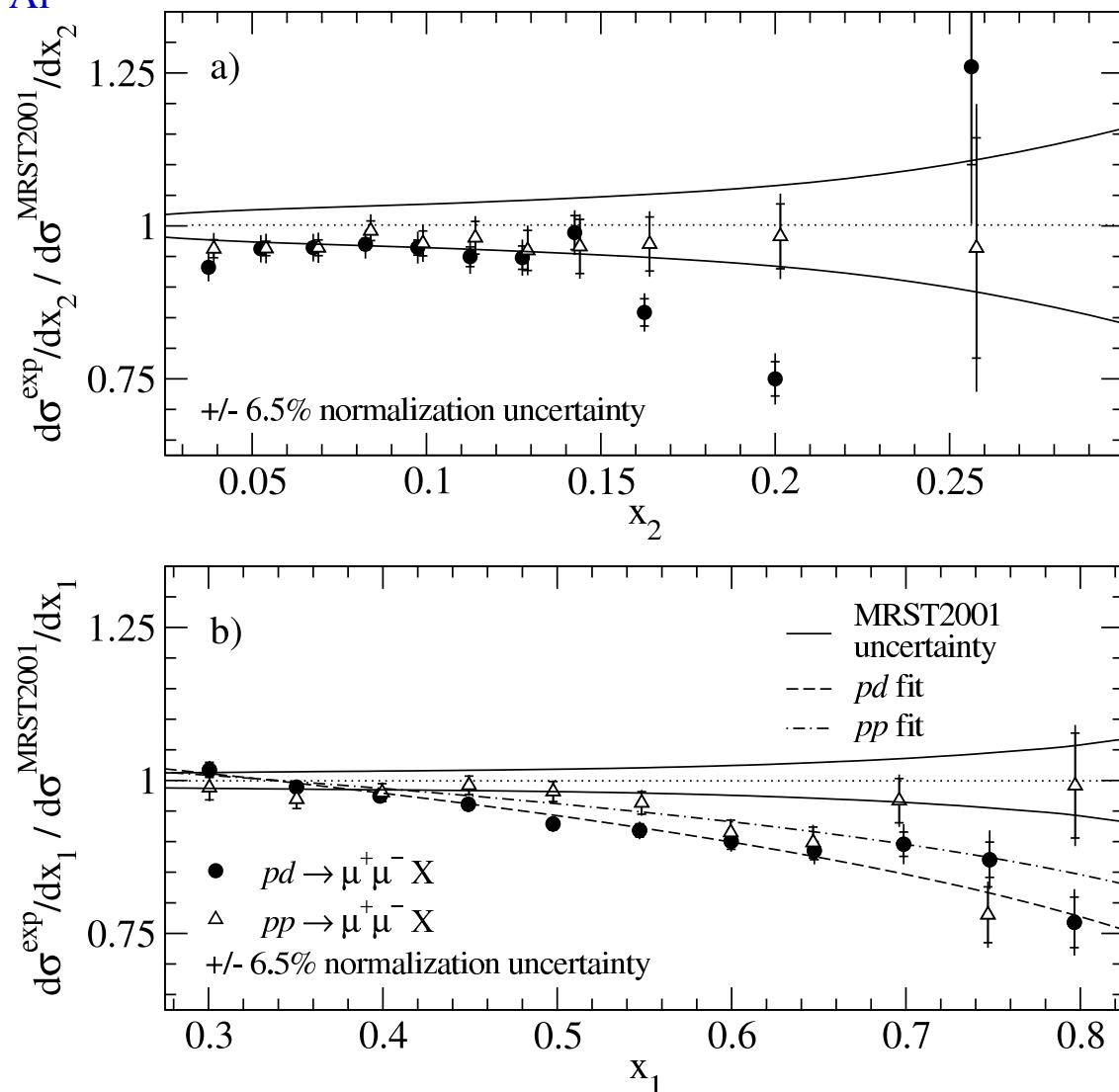
Theory is  
uncomfortably  
high at large-x

Implications for  
valence...

Radiative  
Corrections  
in progress

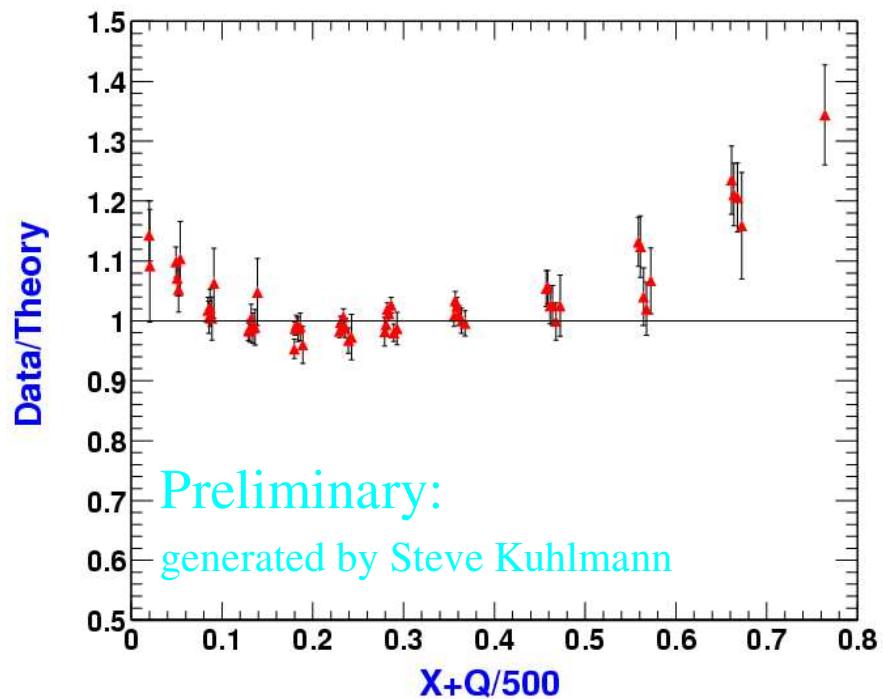
The radiative corrections change both the normalization of the data w/respect to the theory, and the slope vs x1. The pp data are consistent with MRST w/in errors. The pd aren't.

*Constrains  $\bar{d}/\bar{u}$*

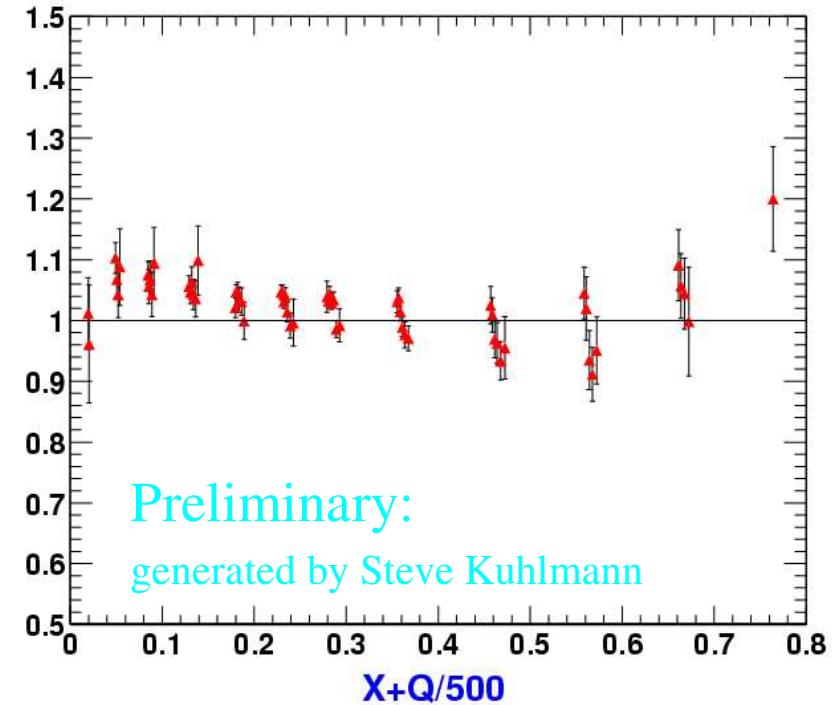


# *Heavy Quark Effects*

## Effect of Fully Massive Calculation

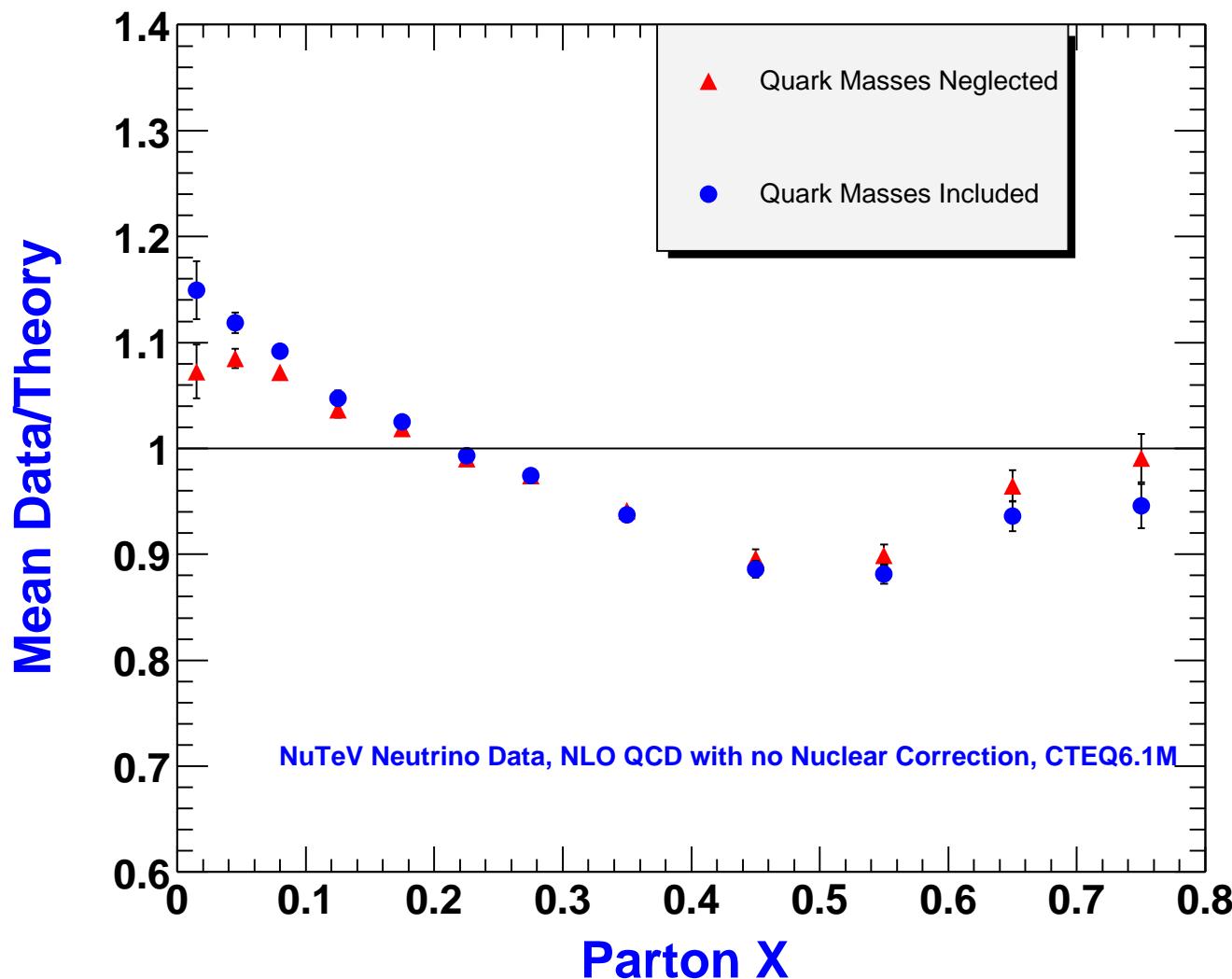


NuTeV F2, evaluated with zero mass NLO QCD, CTEQ6.1M PDFs, and EMC nuclear correction



NuTeV F2, evaluated with S-ACOT heavy quark scheme, CTEQ6.1M PDFs, and EMC nuclear correction

## Effect of Fully Massive Calculation



Minimal effect for this kinematic range with inclusive quantity  
Does make a difference for specific observables

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