



Global Analysis of Neutrino Oscillation

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Acknowledgment:

**A. Bandyopadhyay, S. Choubey,
S.T. Petcov, D.P.Roy**

Plan of Talk

Two flavour oscillation analysis

 Solar +KamLAND – constraints on $\Delta m_{\odot}^2$ and $\sin^2 \theta_{\odot}$

 Atmospheric+K2K – constraints on Δm_{atm}^2 and $\sin^2 \theta_{atm}$

Three flavour oscillation analysis

 solar+KL+chooz+atmospheric+K2K - constraints on θ_{13} ,
 $\Delta m_{\odot}^2 / \Delta m_{atm}^2$

Sterile Neutrinos – LSND ✕

Summary and Future Goals

ν Oscillation: experimental evidences ...

- Atmospheric Neutrino data from SuperKamiokande
- Solar Neutrino Data from Homestake, SAGE, Gallex, GNO, Kamiokande, SuperKamiokande, SNO (Phase-I, Phase-II)
- Data from Long baseline accelerator based experiment K2K
- Long baseline reactor experiment KamLAND
- Accelerator based oscillation experiment LSND
 - not confirmed by Karmen
 - Miniboone will provide independent check

Global Analysis — Ingredients ...

Experimental Data

- statistical error
- systematic errors and their correlations

Theoretical Predictions

- the fluxes and their uncertainties
- the interaction cross-sections and their uncertainties
- the oscillation probabilities (depends on the density profile of the propagating medium Δm^2 , θ , E_ν )

 rate = flux $\times$ cross – section $\times$ probability

Minimisation of χ_{global}^2

- covariance method
- pull method

Fogli et al., 2002

Frequentist method

Creminelli, Signorelli, Strumia

Bayesian Analysis

M.V.Grazzali and C. Giunti

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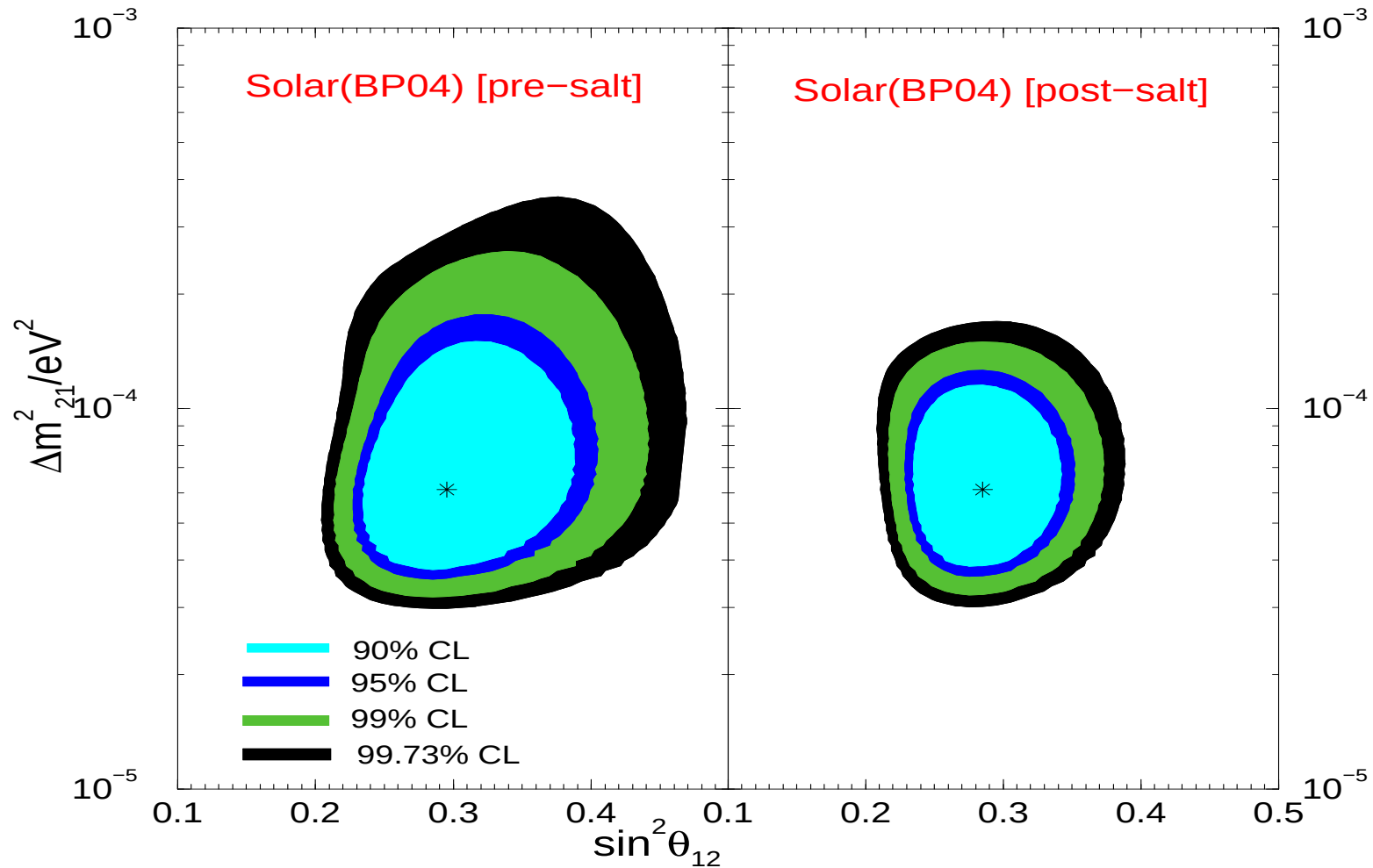
Best-fit values of parameters Δm^2 , $\sin^2 \theta$...

Solar Neutrino Oscillation Parameters:two flavour analysis

Allowed area from global Solar Data . . . $\nu_e - \nu_{\text{active}}$

■ Solar Neutrino Oscillation Parameters : $\Delta m_{\odot}^2 \equiv \Delta m_{21}^2$, $\theta_{\odot} \equiv \theta_{12}$

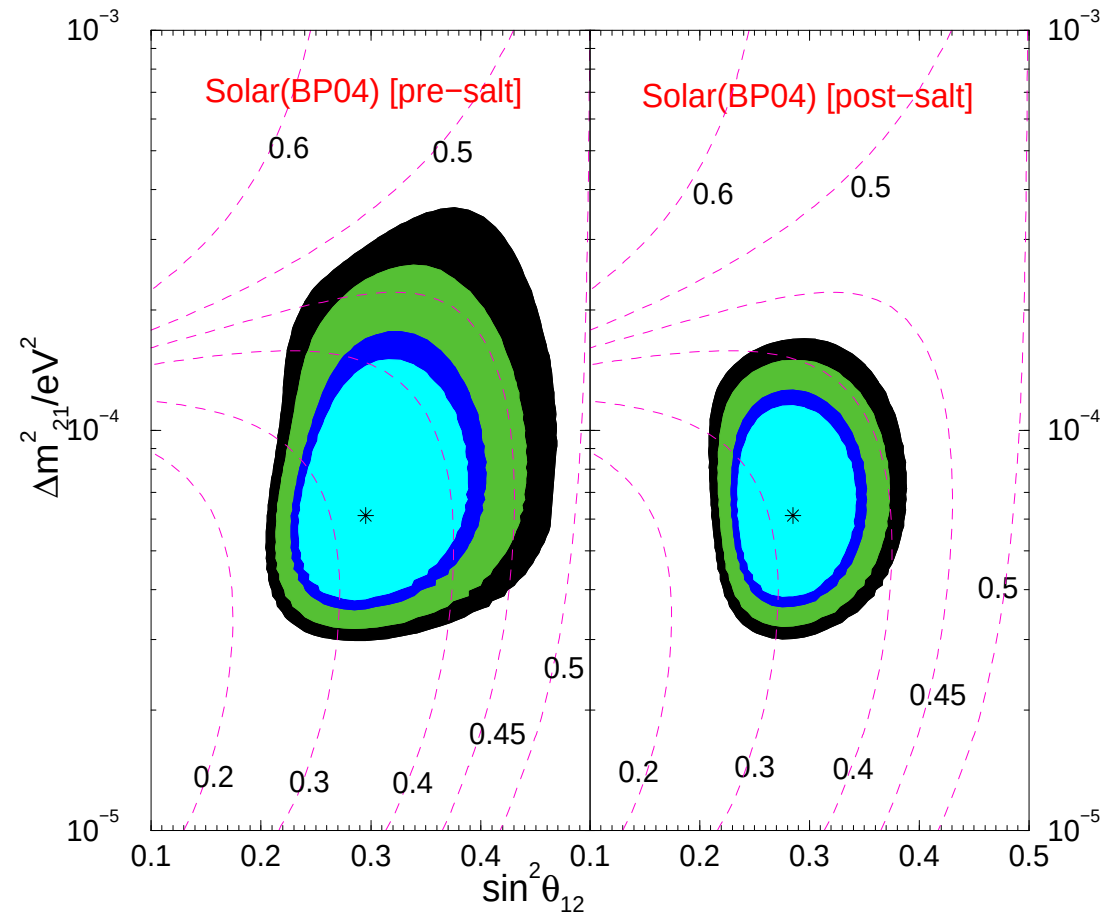
■ BP04 fluxes, 8B flux normalisation free



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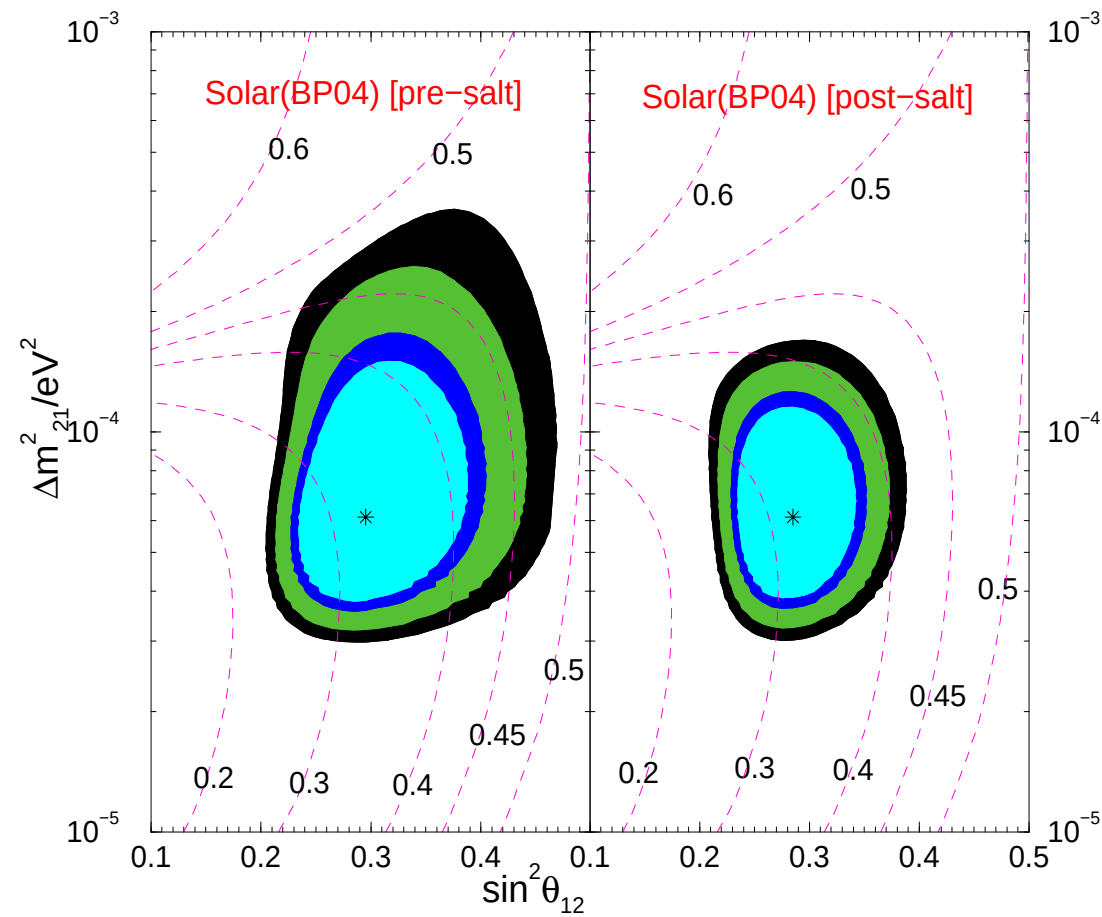
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● Best fit

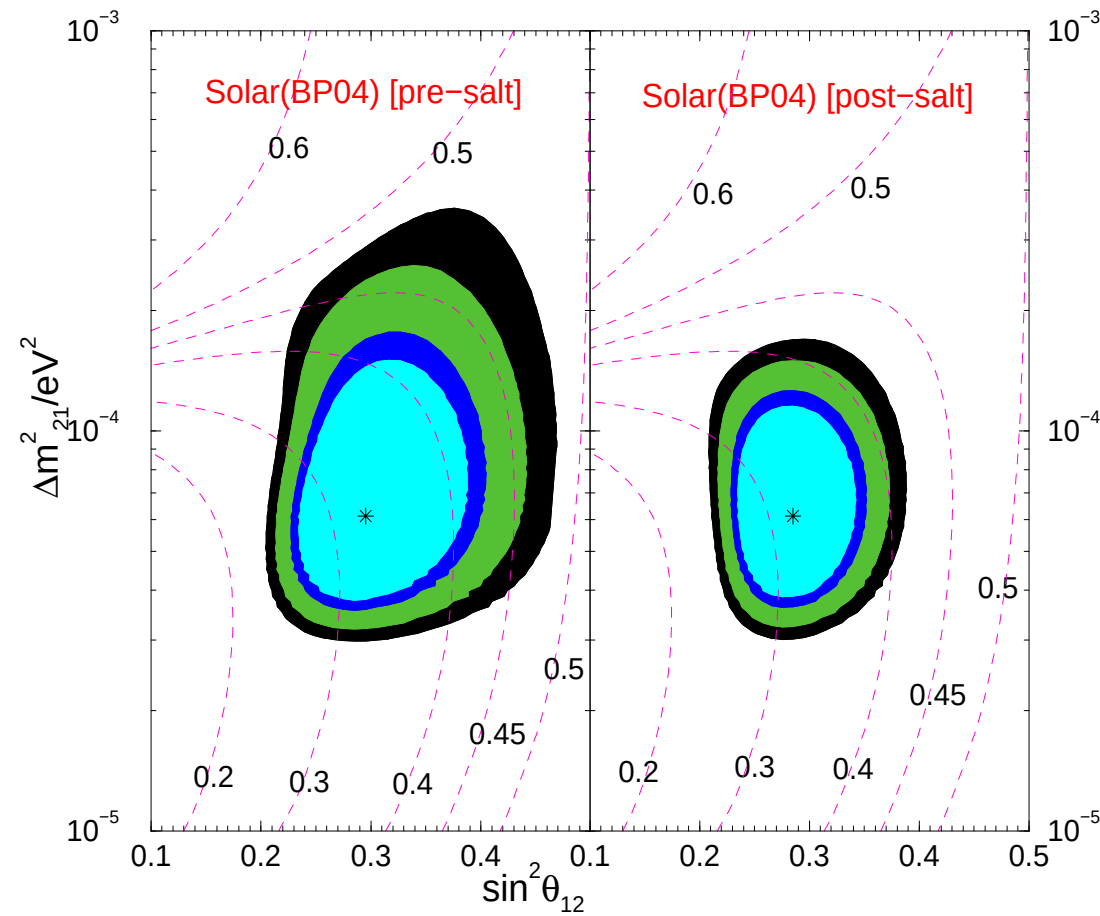
$$\Delta m_{21}^2 = 6.06 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{12} = 0.29 \quad f_B = 0.89$$

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● 99% C.L. range

$$\Delta m_{21}^2 = (3.1 - 25.7) \times 10^{-5} \text{eV}^2$$

$$\sin^2 \theta_{12} = 0.21 - 0.44$$

.... (before salt)

$$\Delta m_{21}^2 = (3.2 - 14.8) \times 10^{-5} \text{eV}^2$$

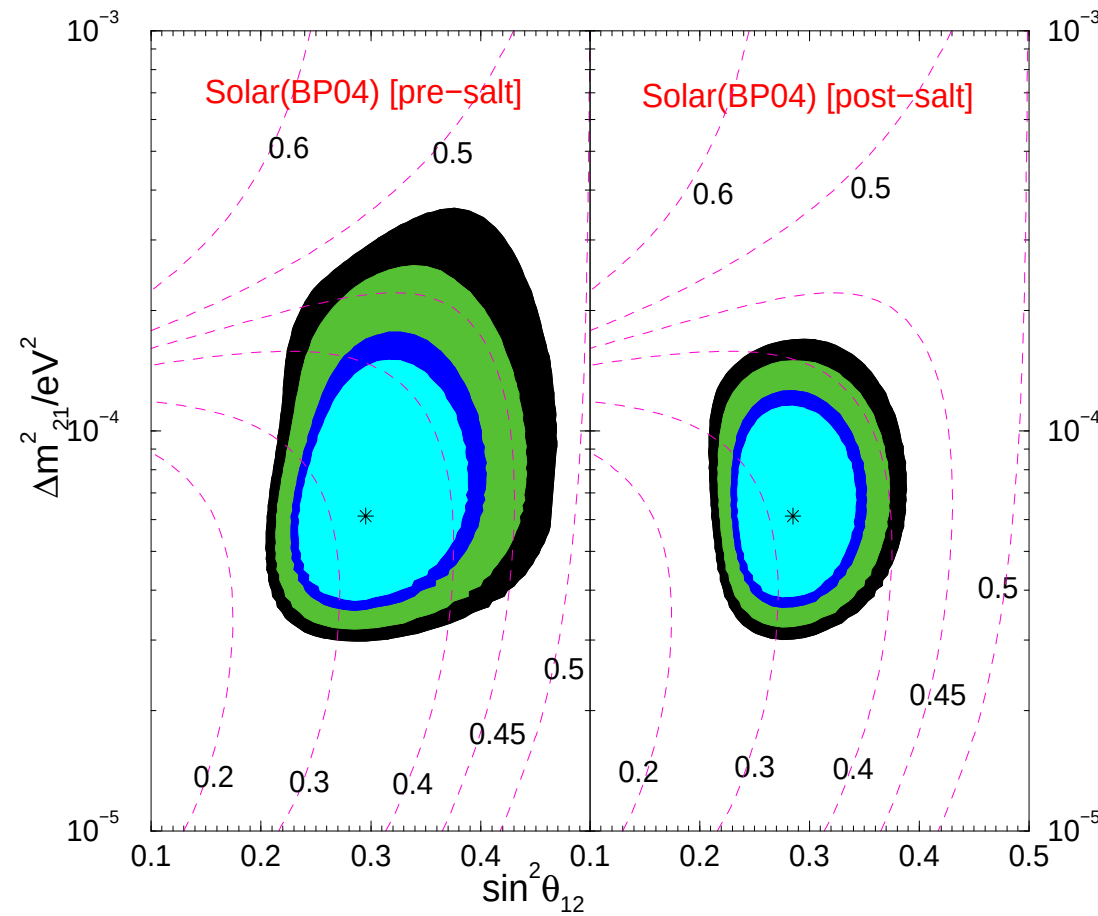
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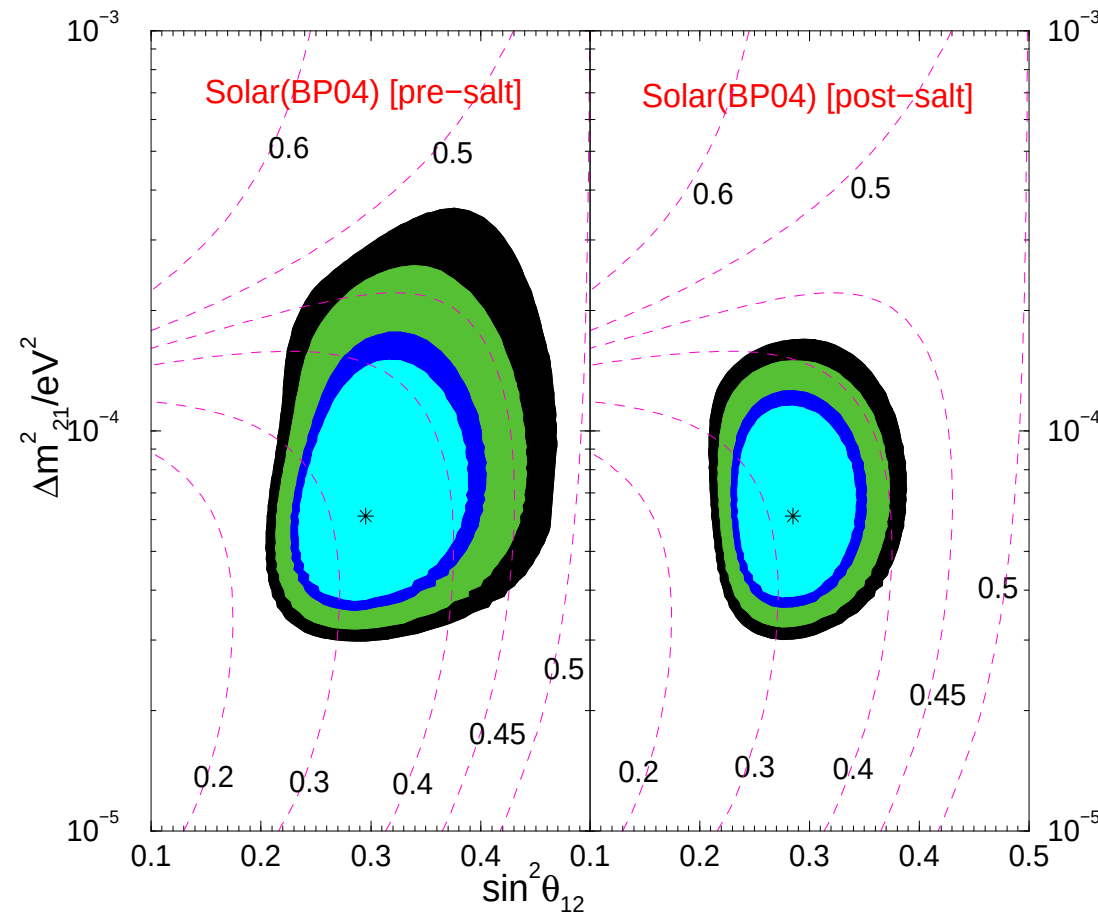
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 Upper limit on Δm_{21}^2 and $\sin^2 \theta_{12}$ tightens with salt data

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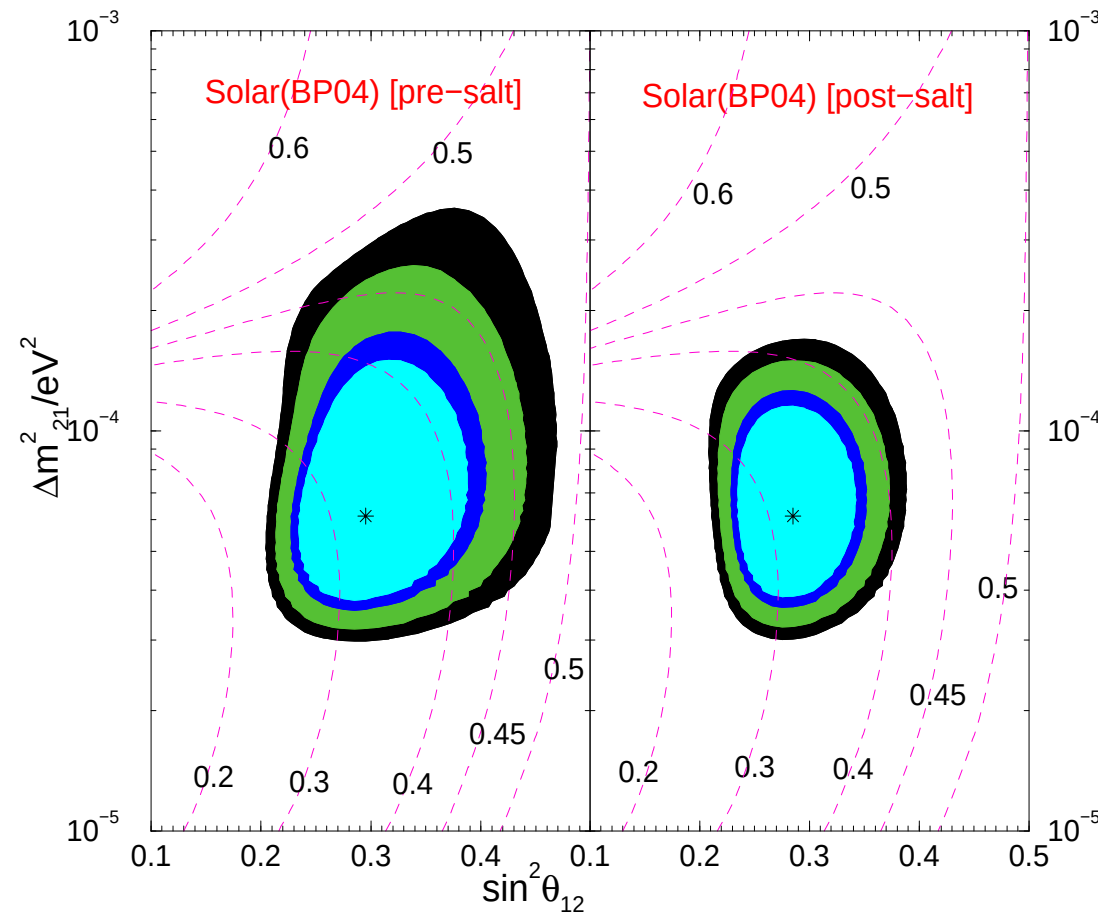
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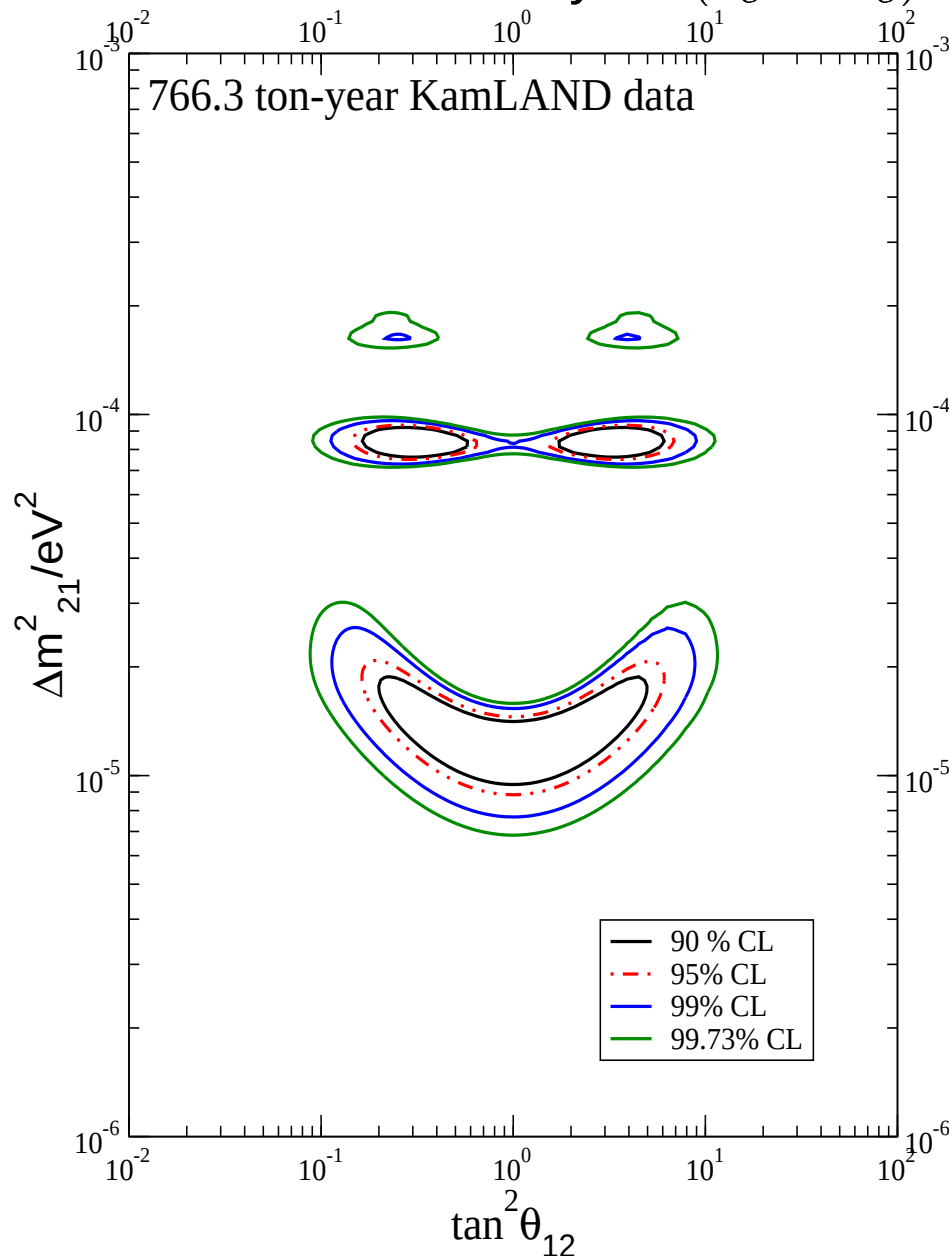
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 Upper limit on Δm_{21}^2 and $\sin^2 \theta_{12}$ tightens with salt data

 No significant change due to BP04

Allowed area from KamLAND spectra

Survival Probability : $P(\bar{\nu}_e \leftrightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E_\nu} \right)$



sensitive to **LMA** region
(assuming CPT conservation)

higher Δm^2 regions **reduce**
in size with new KamLAND data

● New Best fit

$$\Delta m^2_{\odot} = 8.3 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{\odot} = 0.44$$

KL collaboration, 2004

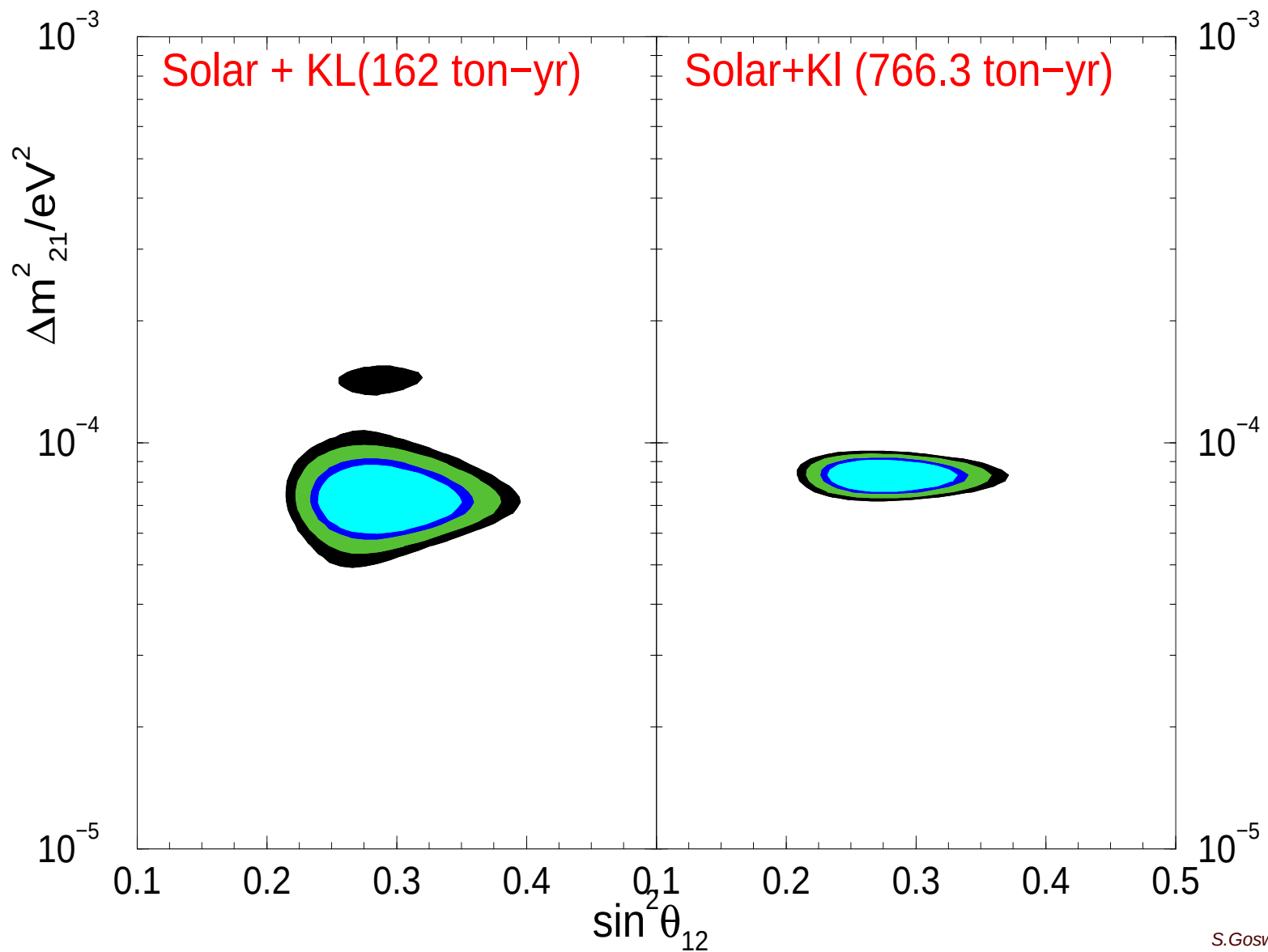
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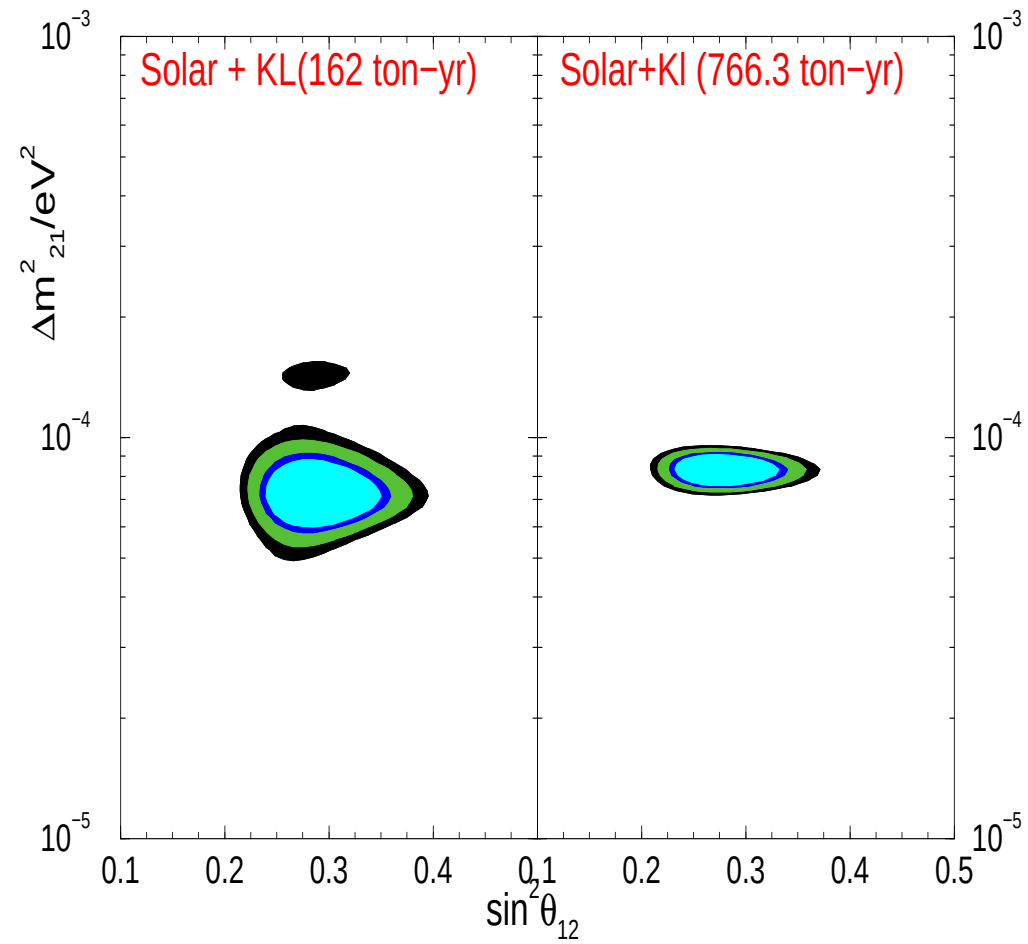
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Bandyopadhyay et. al. 2004

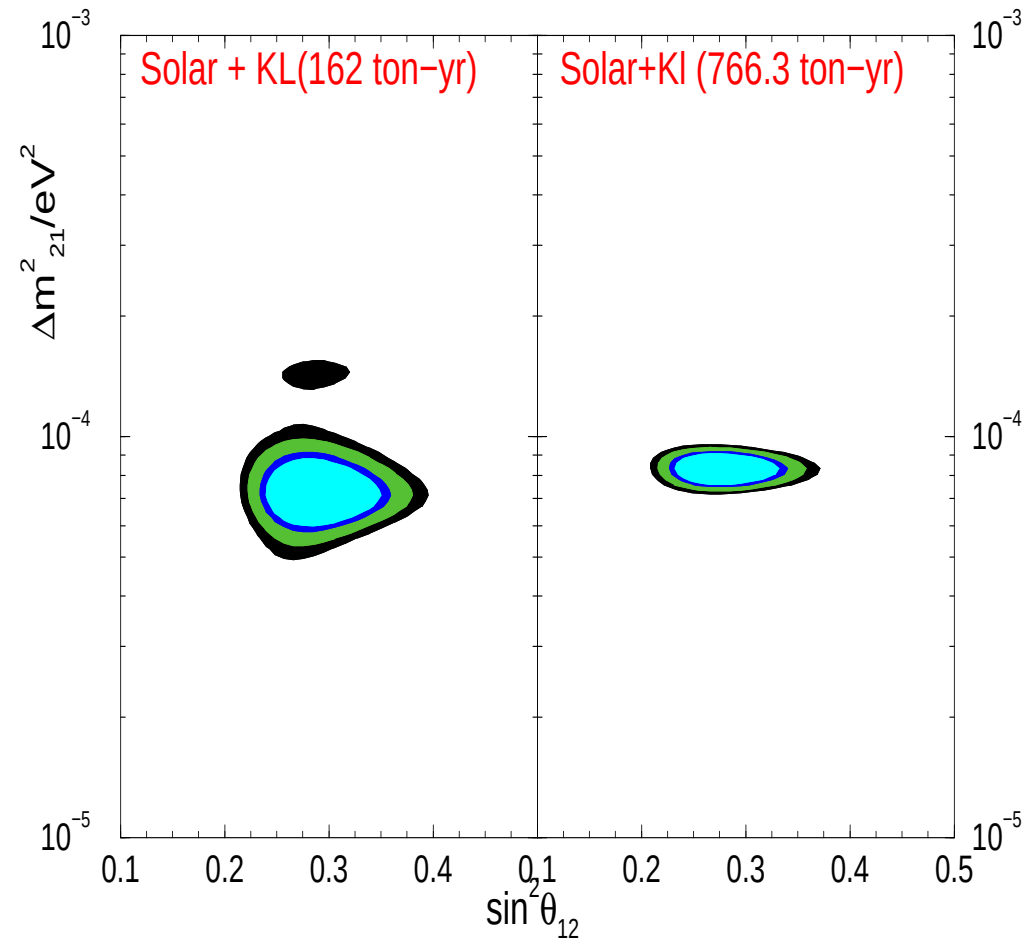
Allowed area from Solar+KamLAND ...



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● Best fit (KL 162Ty)

$$\Delta m_{21}^2 = 7.2 \times 10^{-5} \text{eV}^2$$

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● New Best fit (KL 766.3Ty)

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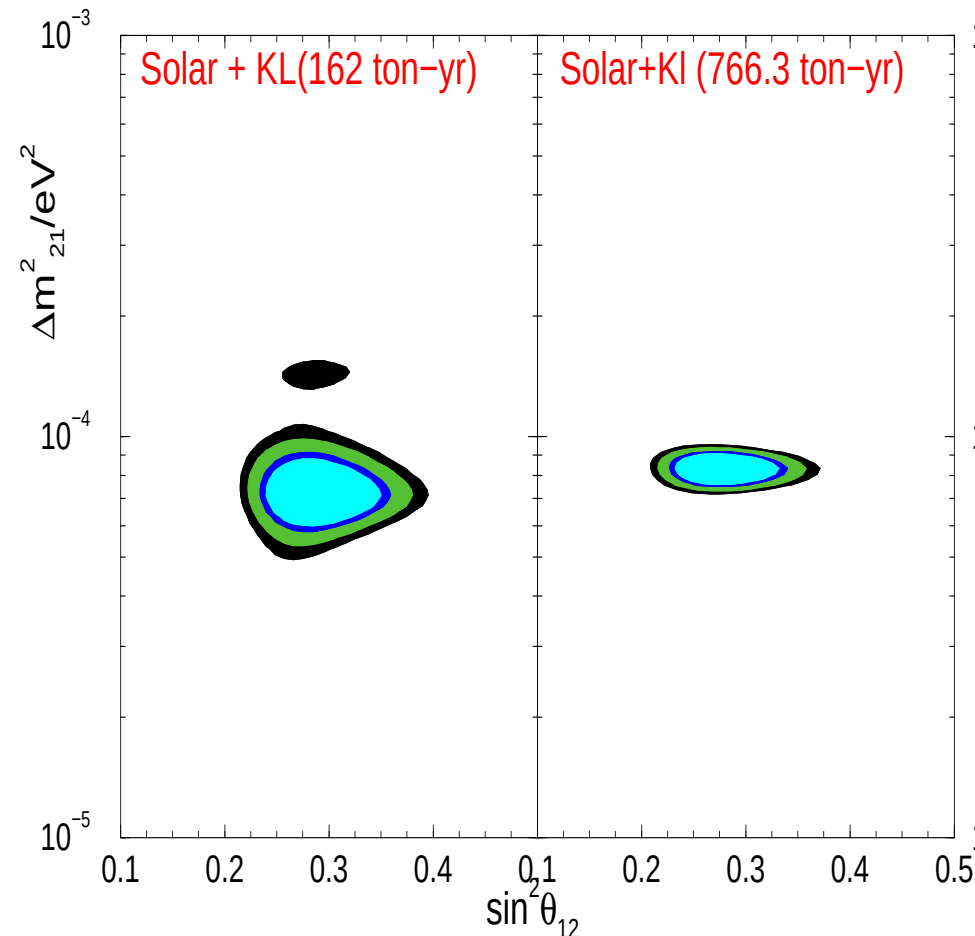
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KamLAND collaboration 2004

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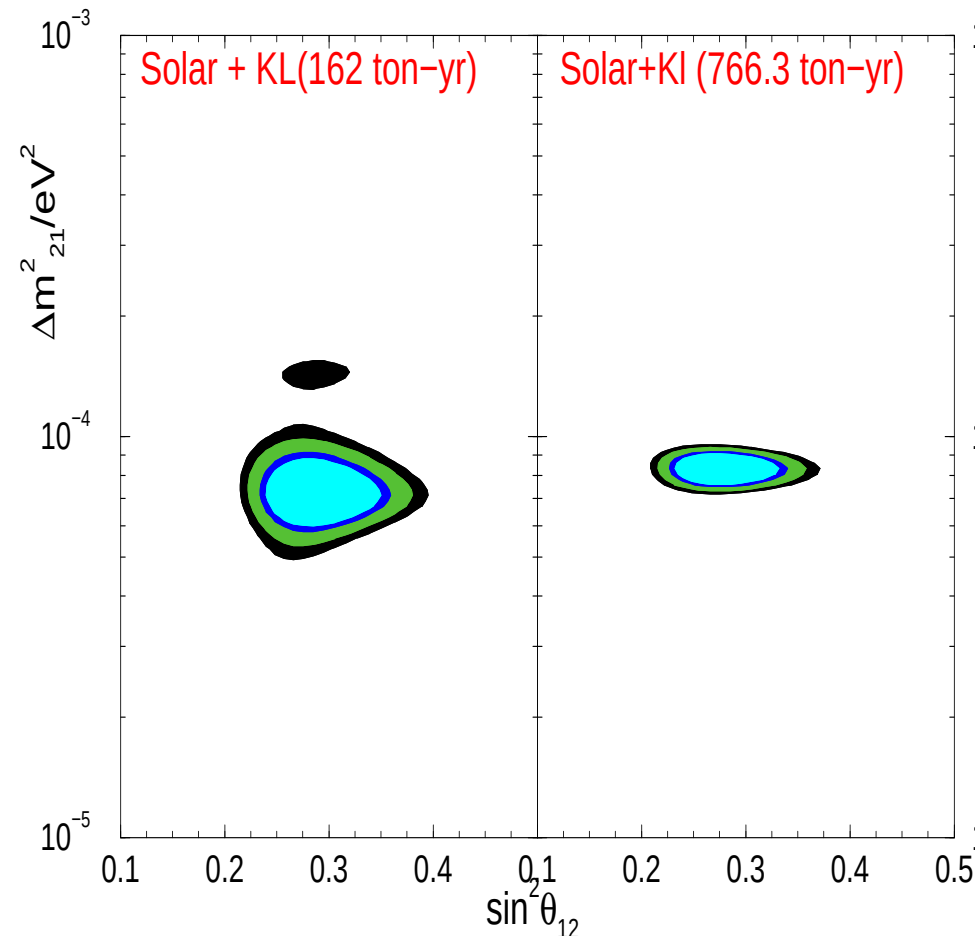
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The **high-LMA** region is **excluded** at more than **3σ**

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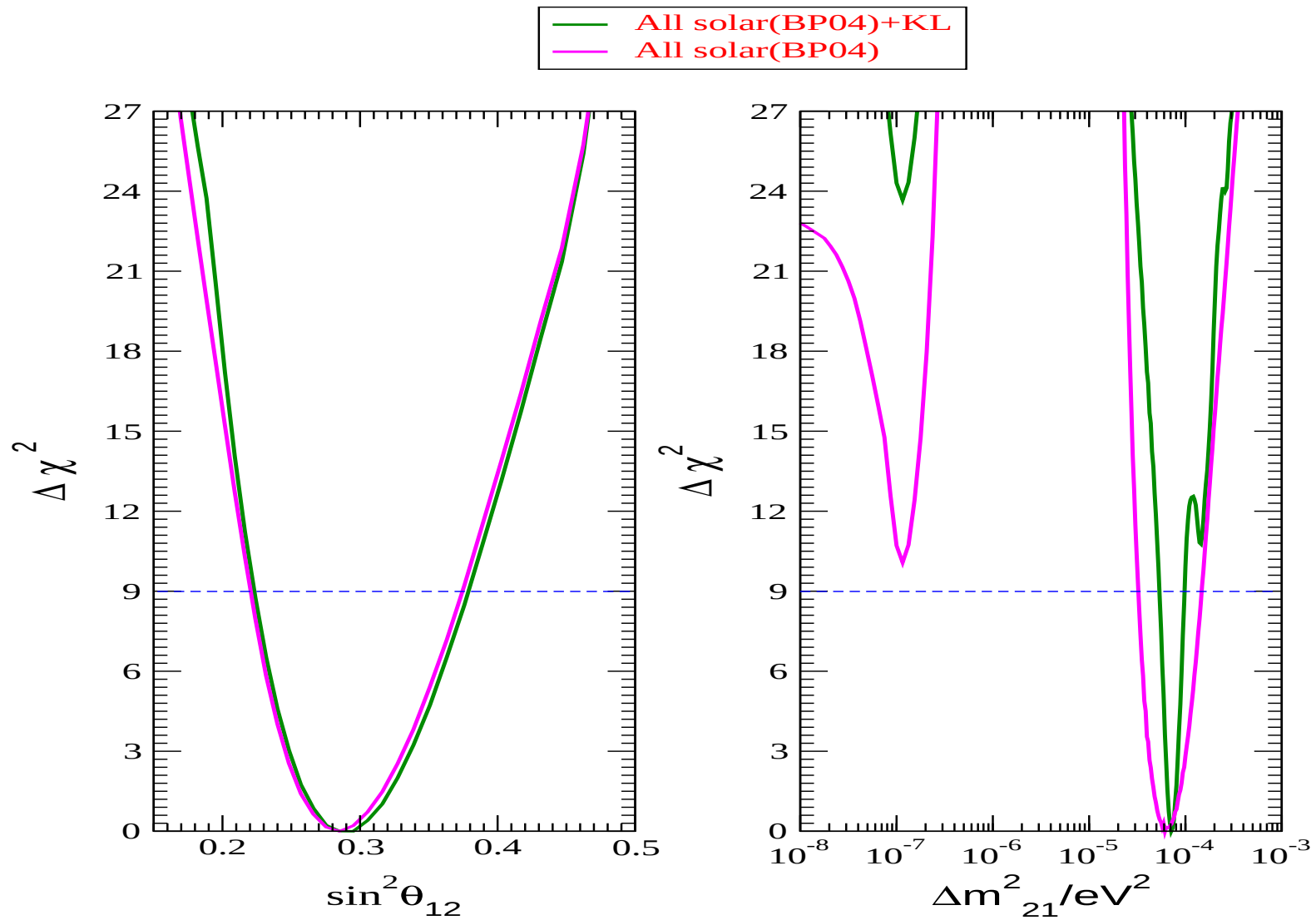
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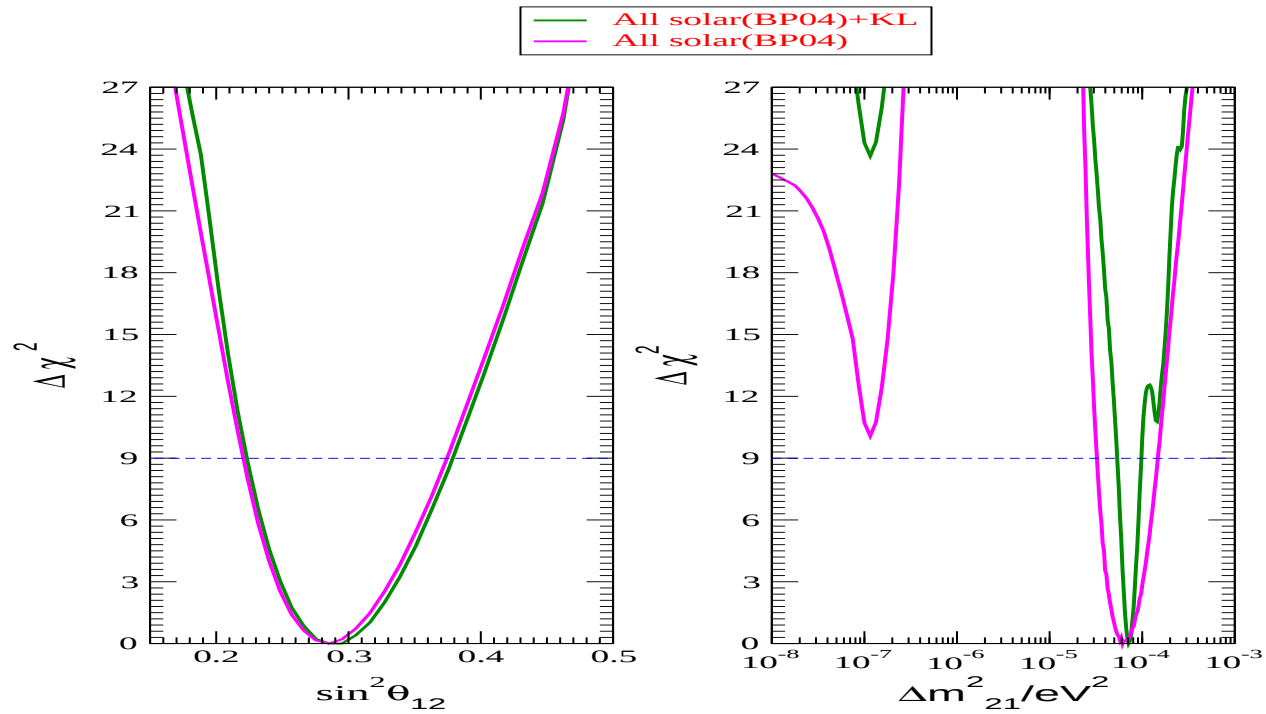
● The **high-LMA** region is **excluded** at more than **3σ**

● Solar data disallows $\theta > \pi/4$ (**Dark-Side**) solutions $\Rightarrow \Delta m_{21}^2 > 0$

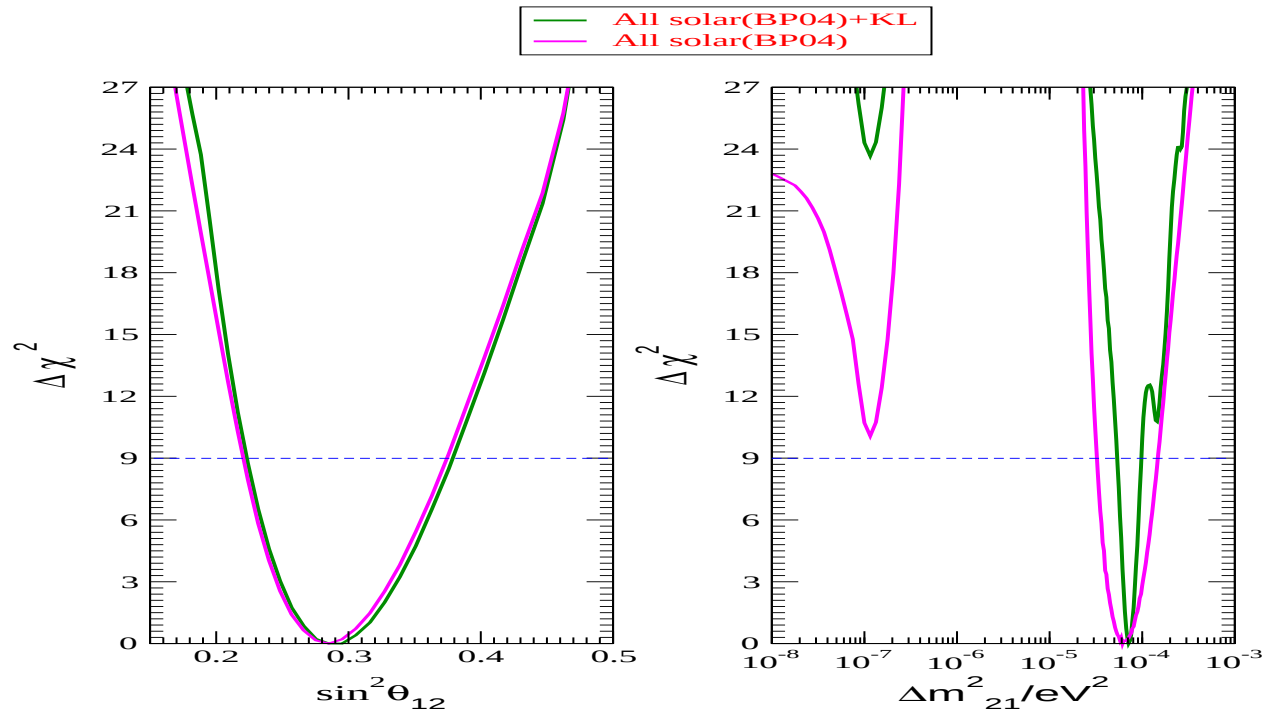
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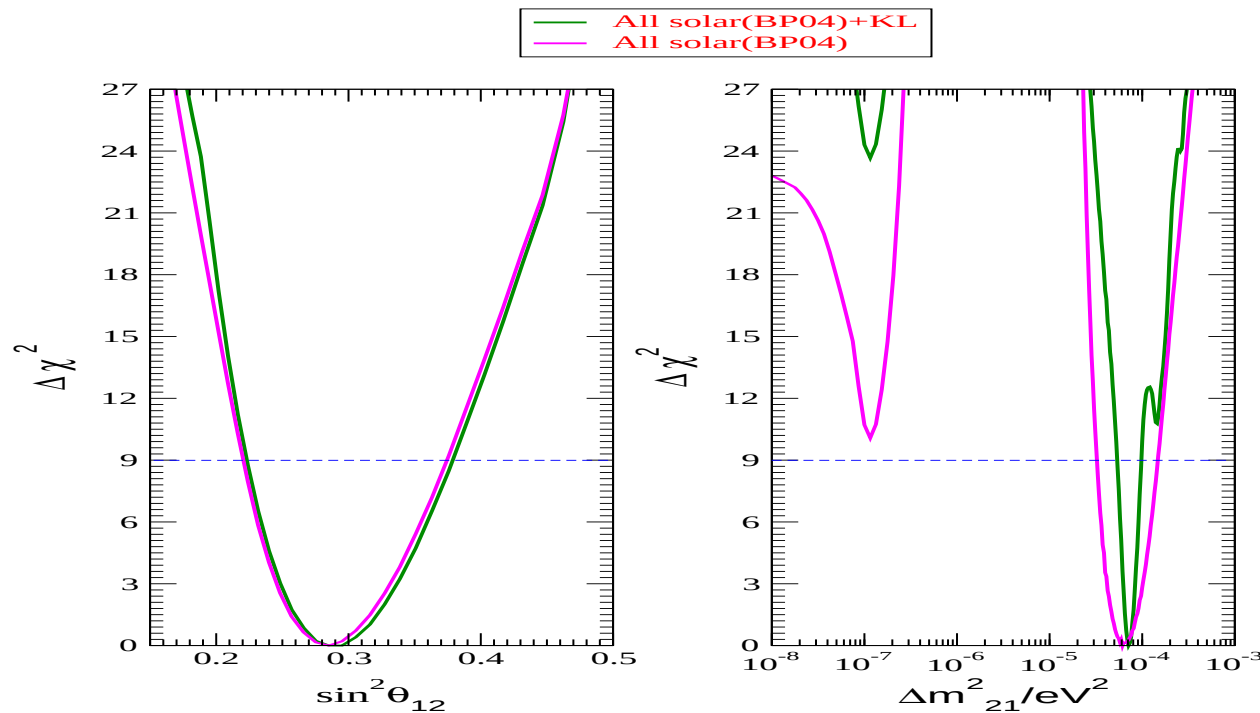


Allowed area from Solar+KamLAND ...



Δm^2_{21} further constrained by KamLAND

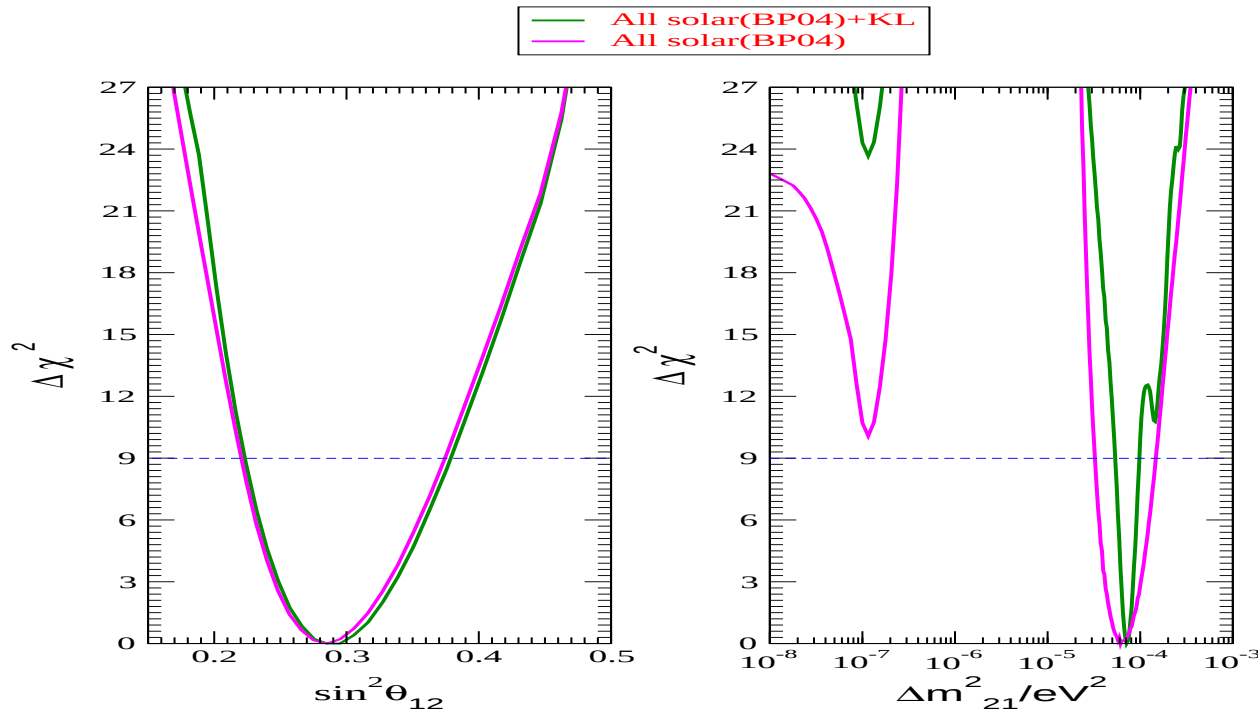
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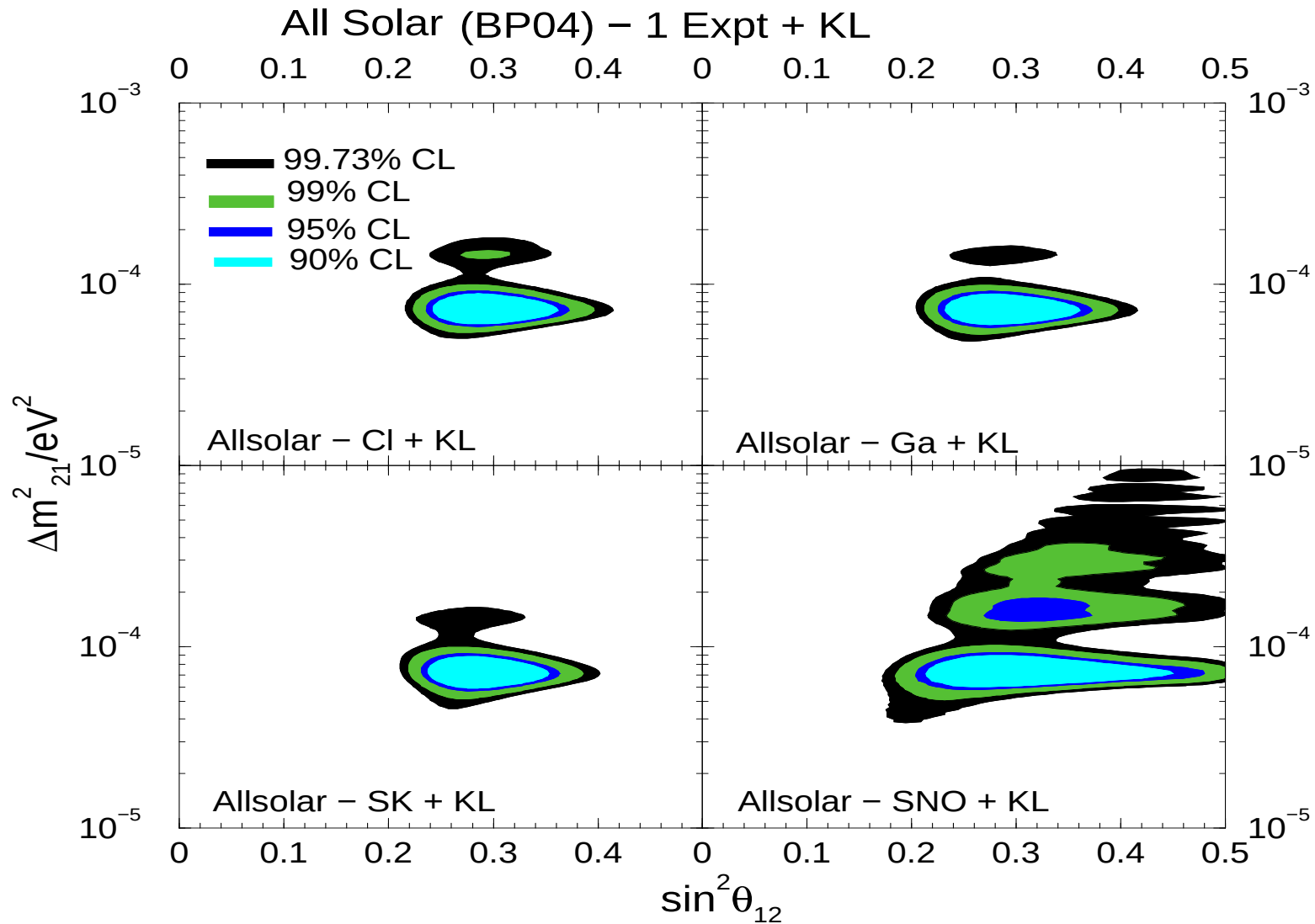
 $\sin^2\theta_{12}$ not constrained any further

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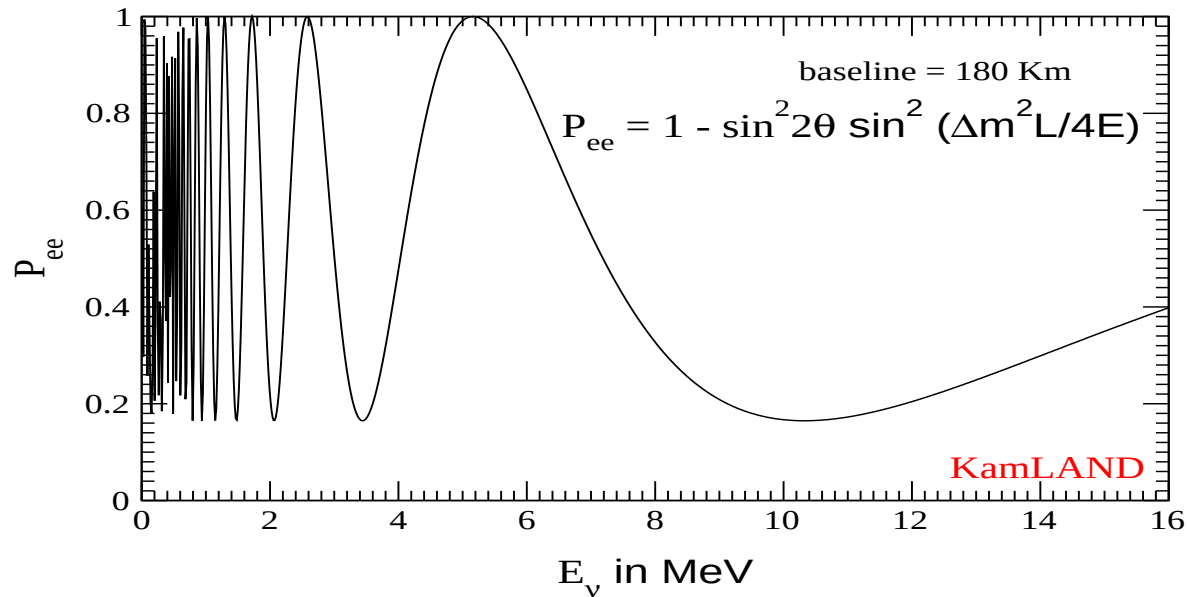
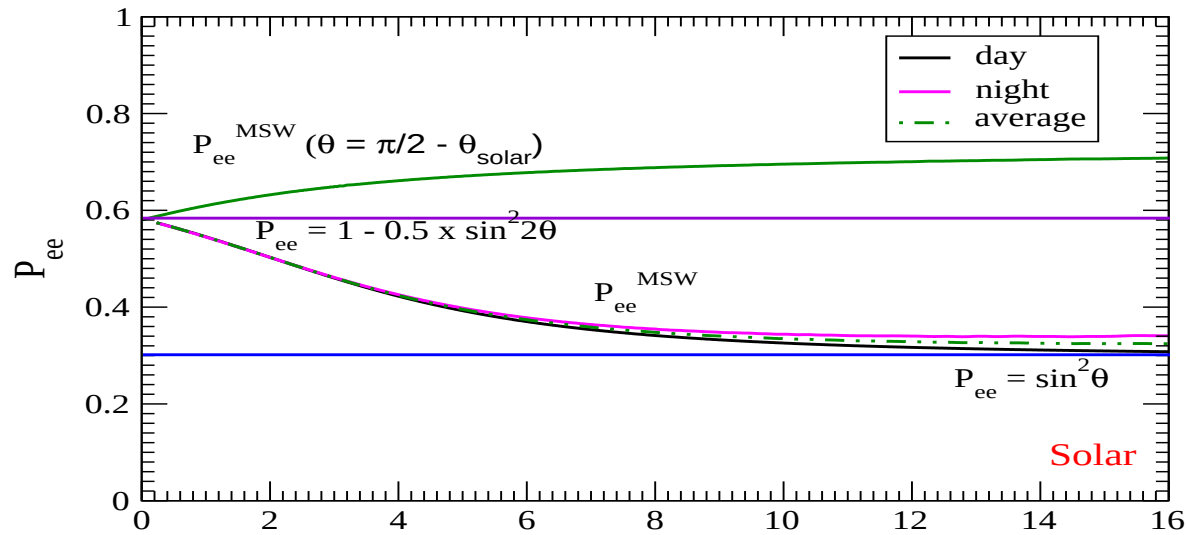
- Δm_{21}^2 further constrained by KamLAND
- $\sin^2\theta_{12}$ not constrained any further
- LOW solution is disfavoured at more than 3σ by only solar data and at about 5σ by solar+KL data
- Maximal mixing is disfavoured at more than 5σ

Impact of each solar experiment . . .



SNO instrumental in disfavouring maximal mixing, Dark side and higher Δm^2 solutions

Survival Probabilities for solar and KamLAND



On the precision of $\nu_{\odot}$ oscillation parameters

 6%(5%) total error for future SNO NC(CC) data

$$\text{spread} = \frac{a_{max} - a_{min}}{a_{max} + a_{min}} \times 100 \%$$

Data set used	Range* of $\Delta m_{21}^2 \times 10^{-5} \text{ eV}^2$	spread in Δm_{21}^2	Range* of $\sin^2 \theta_{12}$	spread in $\sin^2 \theta_{12}$
only sol	3.2 - 14.9	65%	0.22 – 0.37	25%
sol+162 Ty KL	5.2 - 9.8	31%	0.22 – 0.37	25%
sol+ 766.3 Ty KL	7.3 - 9.4	13%	0.22 – 0.36	24%
future sol+1.3 kTy KL	6.7 - 7.8	8%	0.24 – 0.34	17%

* 99% C.L.

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 KamLAND has tremendous sensitivity to Δm_{21}^2

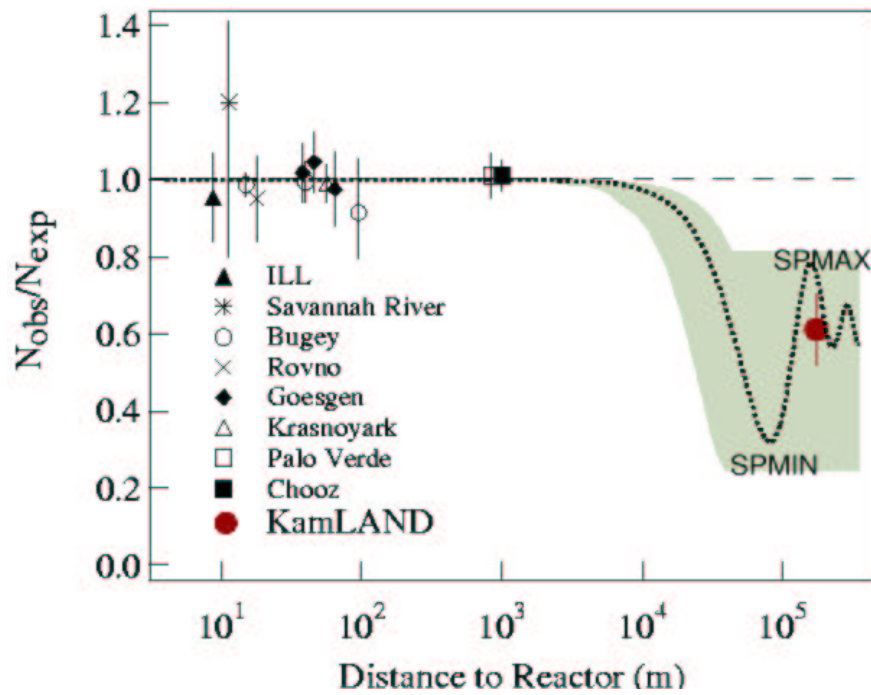
 Does not constrain θ_{12} much better than the current set of solar experiments

Still closer look at KamLAND sensitivity

■ $P_{ee} = 1 - \sin^2 2\theta \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right)$

■ $\sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right) \rightarrow 1 \Rightarrow \text{SPMIN}, \quad \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right) \rightarrow 0 \Rightarrow \text{SPMAX}$

■ **SPMIN** best for $\sin^2 \theta_\odot$ for $\sin^2 \theta_\odot \lesssim 0.37$



Best-Fit: $\sin^2 \theta_\odot = 0.3$

Range: $0.22 < \sin^2 \theta_\odot < 0.37$

■ KamLAND is at **SPMAX**

■ The θ_{12} sensitivity gets smothered

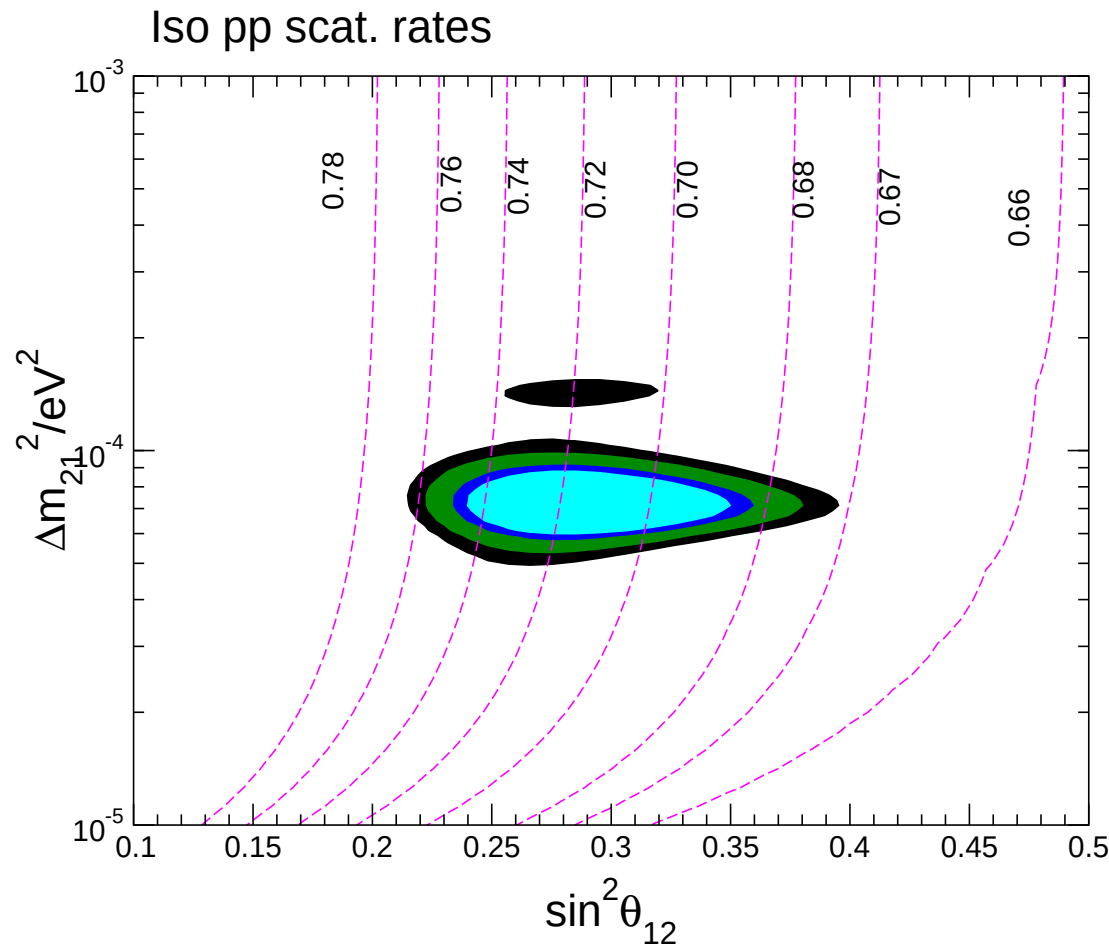
■ KamLAND is not at best position for θ_{12}

■ **SPMIN** comes at $L \sim 70 \text{ km}$ for low-LMA

■ Reactor Experiment at $L \sim 70 \text{ km}$

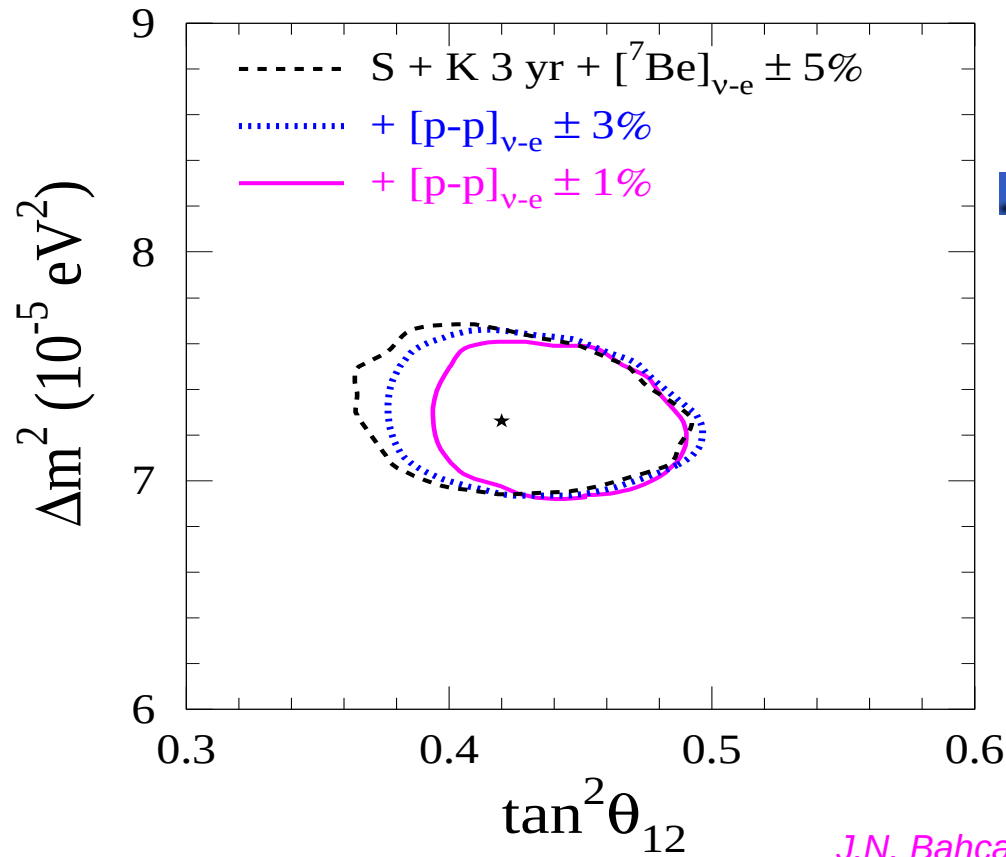
(KamLAND Collaboration, hep-ex/0212021)

Potential of LowNU experiments for $\theta_{\odot}$



-  The pp flux is known with 1% accuracy from Standard Solar Models ($^8B \sim 20\%$, $^7Be \sim 10\%$)
-  Can pin down θ_{12} if experimental errors are low

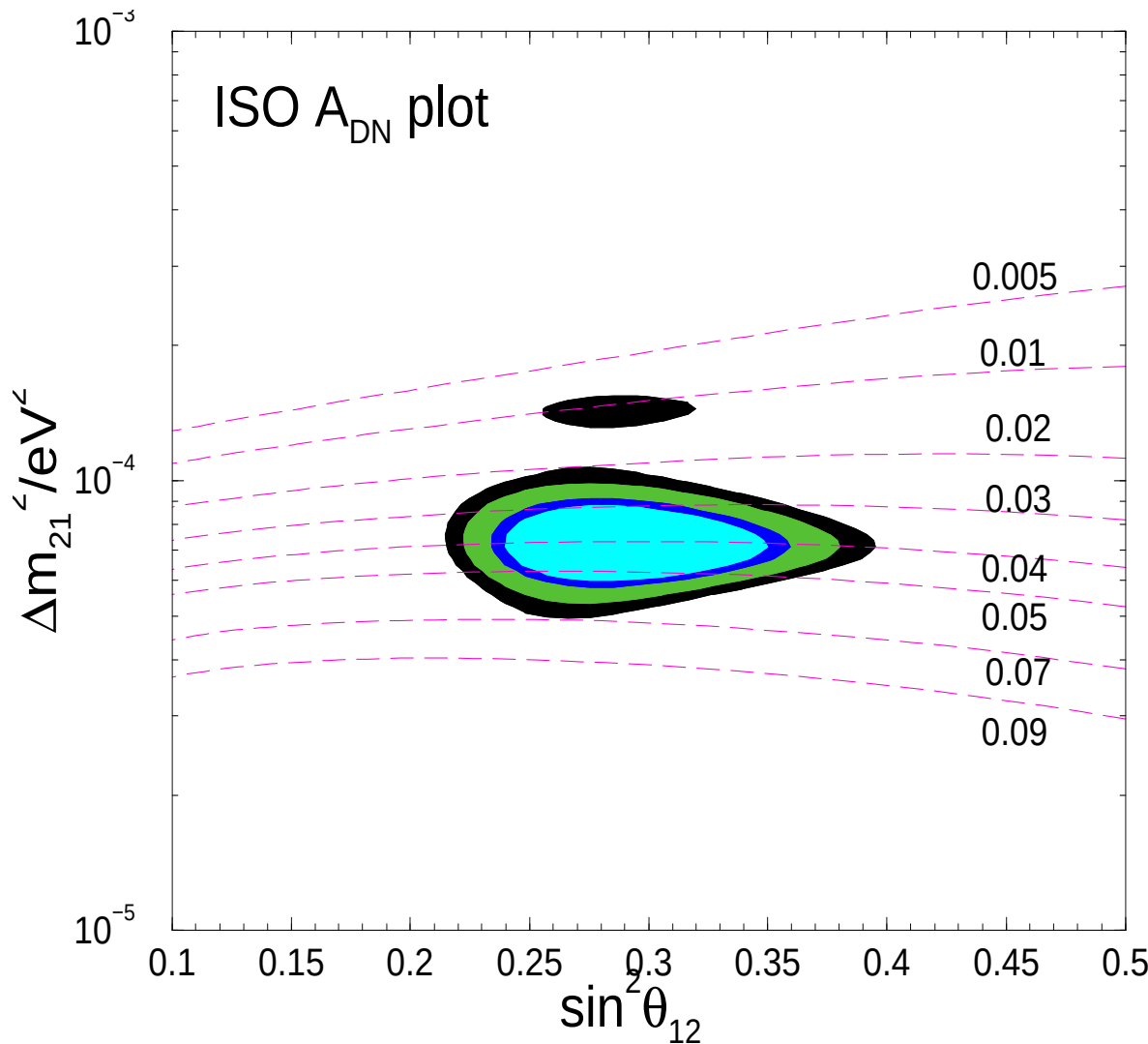
Potential of LowNU experiments for $\theta_{\odot}$



Precision in θ_{12} increases with reduced error in pp flux measurement

J.N. Bahcall and C. Pena-Garay, hep-ph/0305159

Potential of day/night asymmetry for Δm_{21}^2



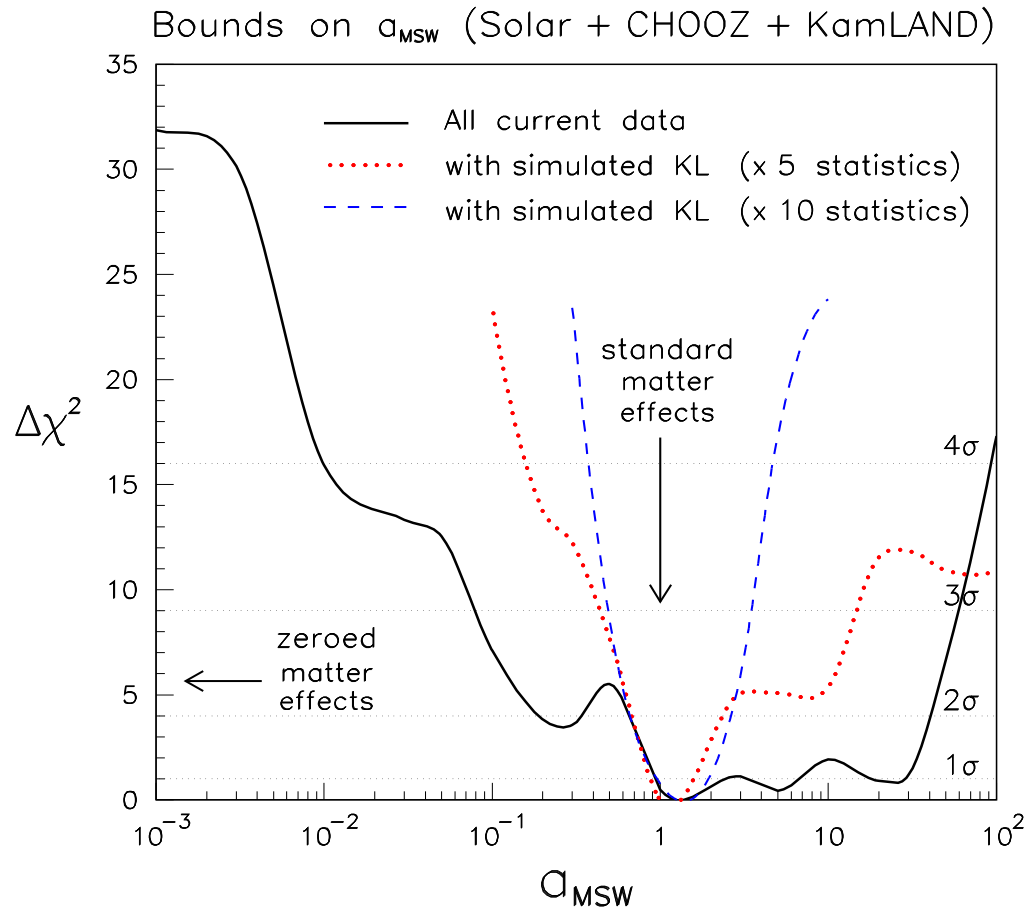
$$A_{D/N} = 2 \frac{N - D}{N + D}.$$

Maris, Petcov
de. Hollanda, Smrinov
Blennow, Ohlsson, Snellman
Bandyopadhyay et al.

$A_{DN}^{SNO} = 0.04$, 3σ range: 0.02-0.07, (low-LMA)

$A_{DN}^{SNO} \approx 0.01$, 3σ range: 0.009-0.014, (high-LMA).

Evidence for MSW effect in Sun ...



$$V_{\text{MSW}} = \sqrt{2}G_F n_e$$
$$V_{\text{MSW}} \rightarrow \alpha_{\text{MSW}} \cdot V$$



"No MSW" rejected
at several σ

Fogli et al. 2003



Increased statistics from KL can put stronger constraints

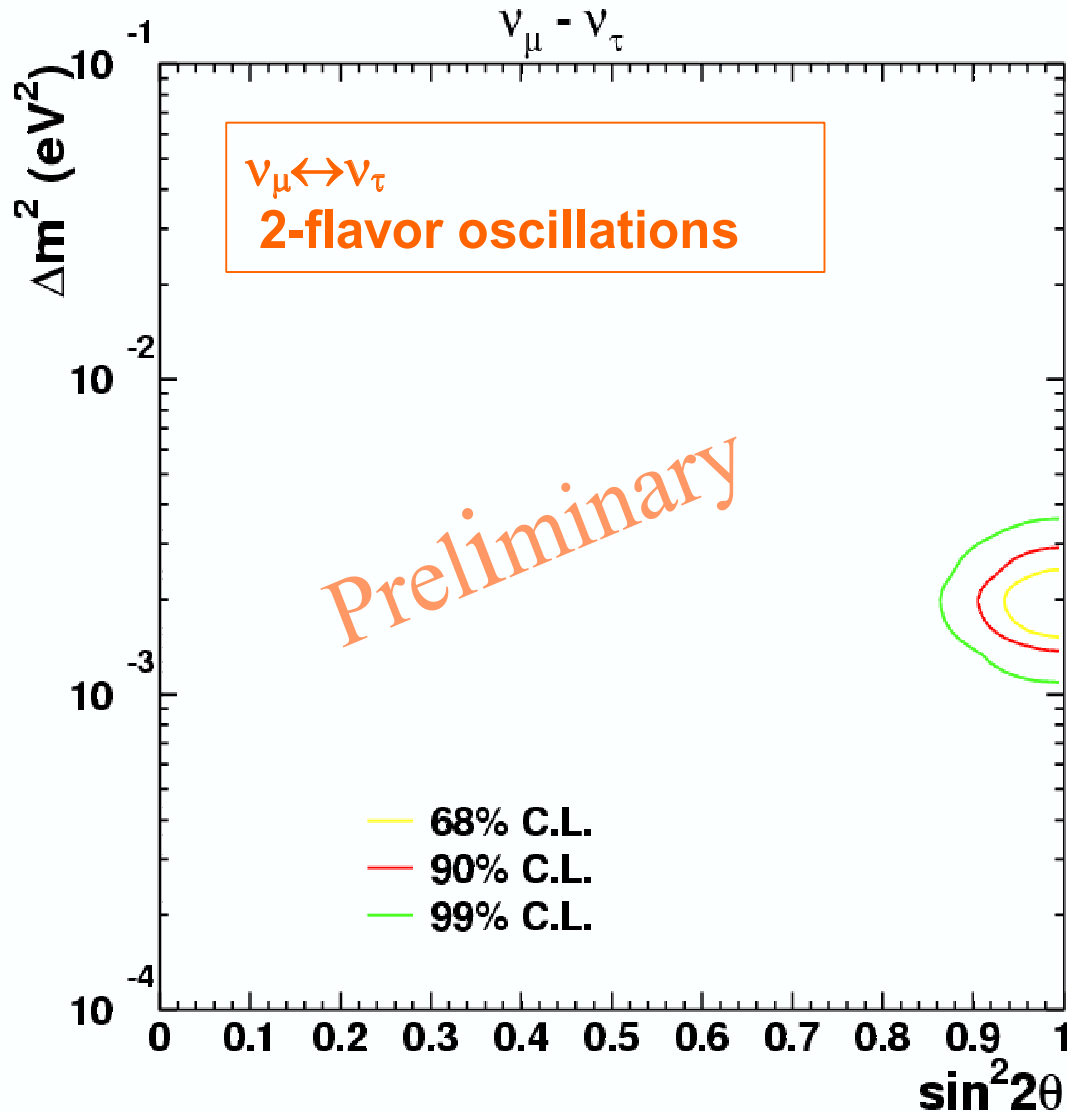


More precise test of **MSW** and "new" physics beyond MSW

Atmospheric Neutrino Oscillation Parameters: two flavour analysis of SK +K2K data

Oscillation Analysis Results

(FC + PC + UP- μ)



C.Saji NOON2004

- **Best fit:**
 $\sin^2 2\theta = 1.0$
 $\Delta m^2 = 2.0 \times 10^{-3} \text{ eV}^2$
 $\chi^2 = 170.8/170 \text{ dof}$
- **90% C.L. region:**
 $\sin^2 2\theta > 0.90$
 $1.3 < \Delta m^2 < 3.0 \times 10^{-3} \text{ eV}^2$

Best-fit $\Rightarrow 2.1 \times 10^{-3} \text{ eV}^2$

E. Kearns, Neutrino 2004

Analysis of SK Atmospheric Data

- Analysis of SuperKamiokande data by two groups * confirm this downward shift of Δm_{atm}^2
- Three-Dimensional Honda Atmospheric Fluxes
- Normalisation to SK Monte Carlo to include the effect of revised efficiencies and cross-sections
- Pull approach for systematic uncertainties
 - provides useful information on the role of systematic uncertainties on the best-fit rates.

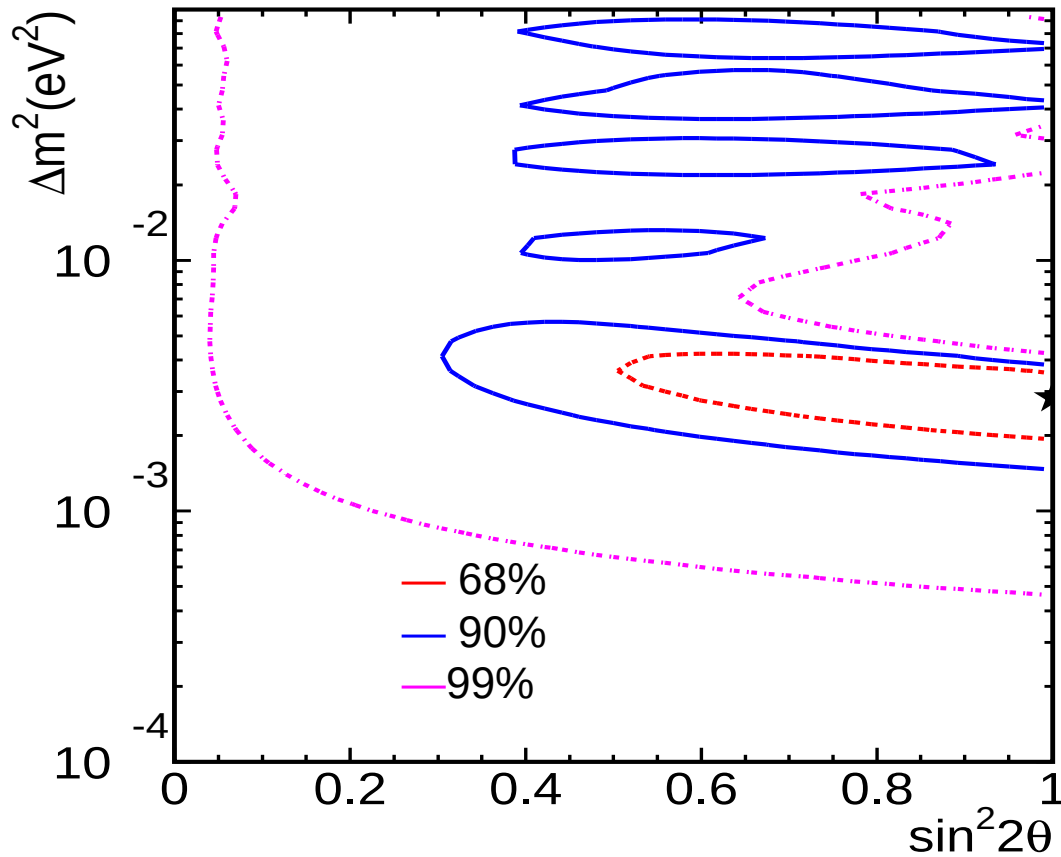
**Maltoni et al., hep-ph/0405172*

**Gonzalez-Garcia et al., hep-ph/0404085*

Allowed area from K2K Experiment

● $P_{\mu\mu} = 1 - \sin^2 2\theta_{atm} \sin^2 \left(\frac{\Delta m_{atm}^2 L}{4E} \right)$

● $L \sim 250 \text{ km}, E_\nu \sim 1.3 \text{ GeV}$

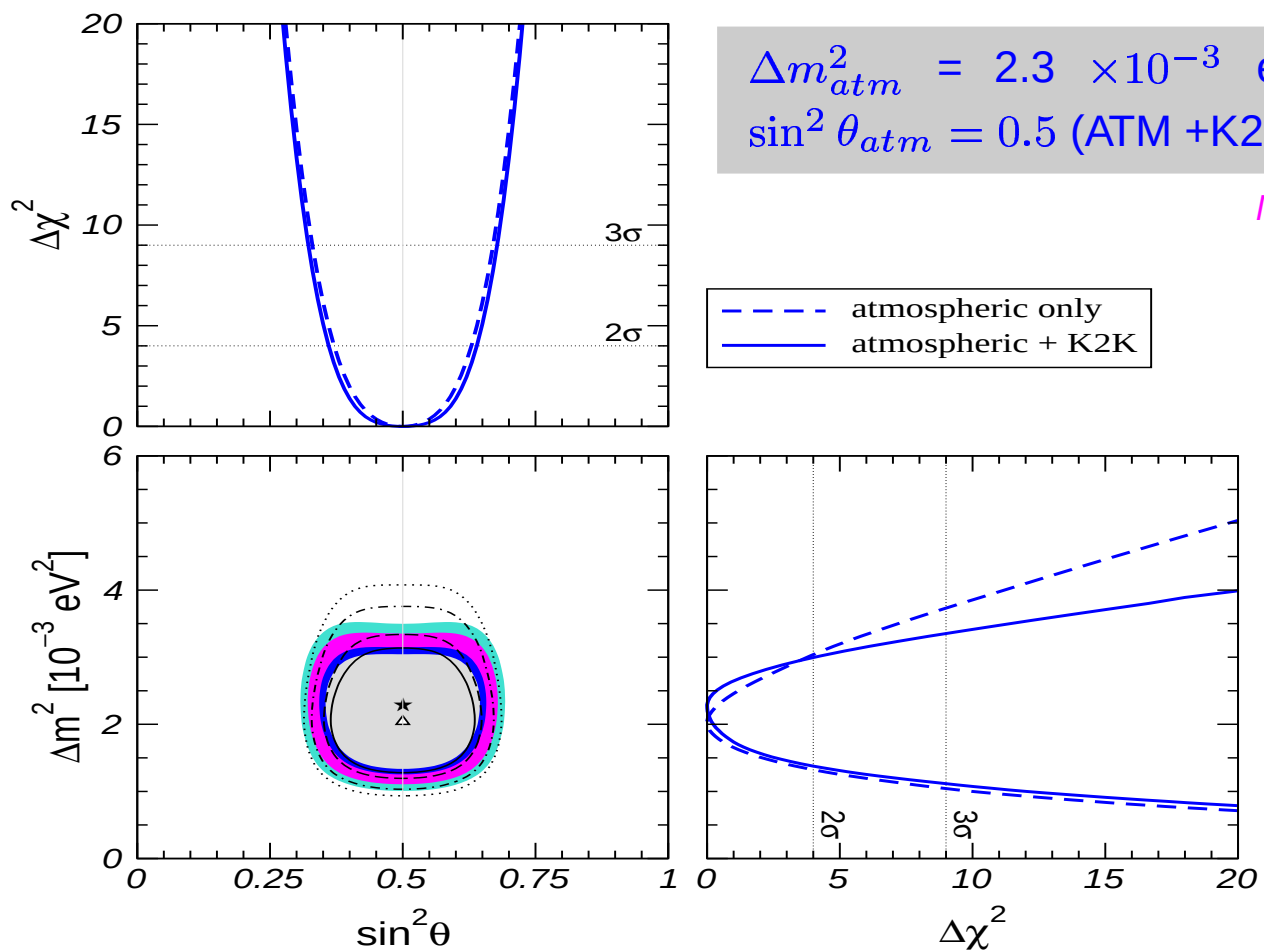


● Best-fit

$$\Delta m_{atm}^2 = 2.8 \times 10^{-3} \text{ eV}^2$$
$$\sin^2 2\theta_{atm} = 1.0$$

K2K collaboration, 2003

Allowed parameters from SK+K2K analysis



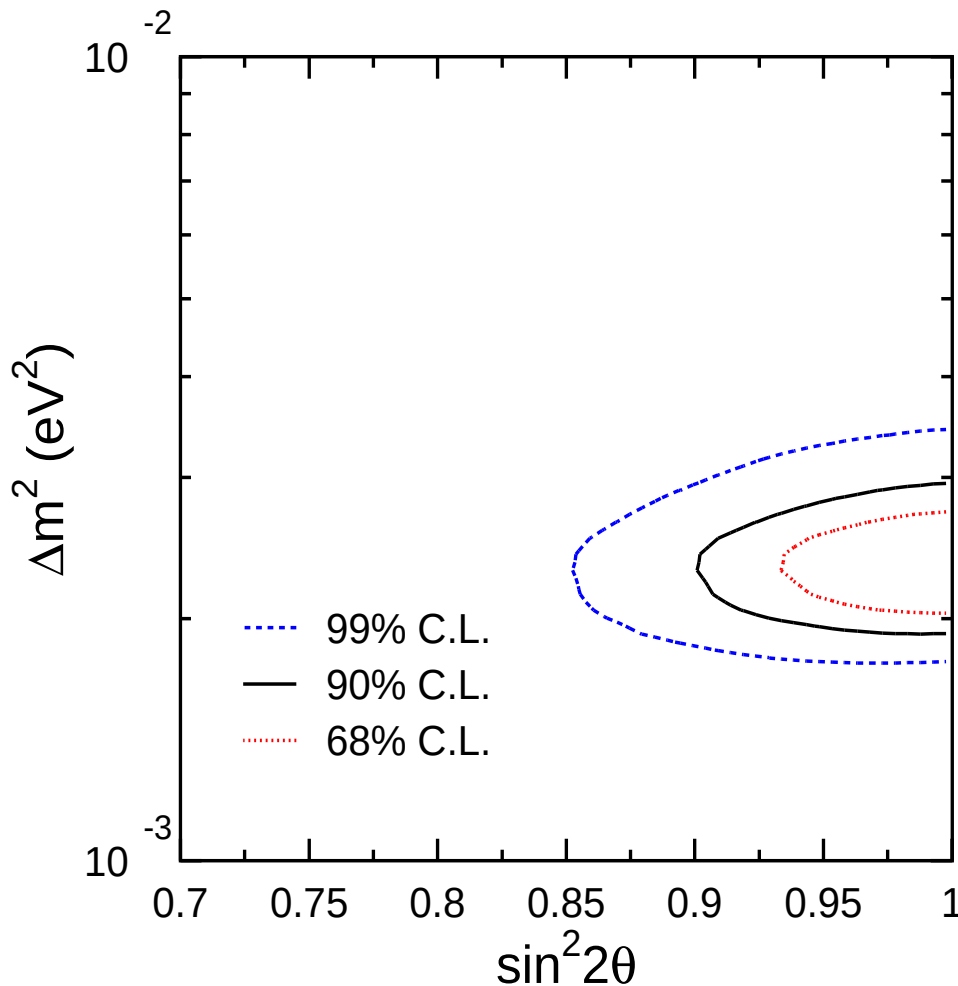
$$\Delta m_{atm}^2 = 2.3 \times 10^{-3} \text{ eV}^2,$$

$$\sin^2 \theta_{atm} = 0.5 \text{ (ATM + K2K)}$$

Maltoni et al., hep-ph/0405172

- Higher Δm^2 values are constrained by K2K
- K2K data does not constrain θ_{atm} any better

Allowed area from SK L/E data . . .



● Best-fit

$$\Delta m_{atm}^2 = 2.4 \times 10^{-3} \text{ eV}^2,$$

$$\sin^2 2\theta_{atm} = 1.0 \text{ (SK L/E)}$$

● 90% C.L. range

$$\Delta m_{atm}^2 = 1.9 - 3.0 \times 10^{-3} \text{ eV}^2,$$

$$\sin^2 2\theta_{atm} > 0.9 \text{ (SK L/E)}$$

spread in $\Delta m_{atm}^2 = 22\%$

● 90% C.L. range

$$\Delta m_{atm}^2 = 1.3 - 3.0 \times 10^{-3} \text{ eV}^2,$$

$$\sin^2 2\theta_{atm} > 0.9 \text{ (SK Zenith)}$$

spread in $\Delta m_{atm}^2 = 39\%$

Improved precision in Δm_{atm}^2 with L/E data

Range of $\sin^2 \theta_{atm}$ unchanged $\rightarrow \delta(\sin^2 2\theta_{23}) \sim 5\%$

Y. Ashie et al. SK collaboration, hep-ex/0404034

Precision of atmospheric neutrino oscillation parameters

- $\delta(\sin^2 \theta_{23}) \sim 32\% \Rightarrow \sin^2 \theta_{23}$ precision is worse than $\sin^2 2\theta_{23}$ precision near maximal mixing
- $\delta(\sin^2 2\theta_{23}) = \sqrt{(\text{exposure})} \Rightarrow$ more statistics from SK
 - $\delta(\sin^2 \theta_{23}) \sim 22\%$ in SK 20 years at 90% C.L..
- Increased statistics in L/E data can improve $\delta(\Delta m_{32}^2)$
 - $\delta(\Delta m_{32}^2) \sim 10\%$ in SK 20 years at 90% C.L..
- Effect sensitive to the true Δm_{32}^2 chosen ($\Delta m_{32}^2 = 2.5 \times 10^{-3} \text{ eV}^2$)

T.Kajita, Talk in NOON2004

Precision of atmospheric neutrino oscillation parameters

■ Large Magnetized Iron (30-100 kT) calorimeters have very **good**
L/E resolution

■ excellent muon track and charge identification

■ $\sim 5\%$ energy resolution

■ MONOLITH was first proposed for GranSasso

MONOLITH proposal, <http://castore.mi.infn.it/~monolith>

■ INO : currently planned for location in India

$\delta(\Delta m^2) \sim 10\%$ for 150 kTy ~ 5 yrs of INO

(at $\Delta m_{atm}^2 \sim 3.0 \times 10^{-3} \text{ eV}^2$) ➡

<http://www.imsc.res.in/~ino>

■ Longbaseline, Superbeam ...

Three Flavour Oscillation

Two mass squared differences

$$\Delta m_{21}^2 = \Delta m_{\odot}^2, \quad \Delta m_{31}^2 = \Delta m_{CHOOZ}^2 \simeq \Delta m_{atm}^2 = \Delta m_{32}^2$$

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Three mixing Angles

$U = R_{23}R_{13}R_{12} =$

$$\begin{pmatrix} c_{13}c_{12} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - s_{23}s_{13}c_{12} & c_{23}c_{12} - s_{23}s_{13}s_{12} & s_{23}c_{13} \\ s_{23}s_{12} - s_{13}c_{23}c_{12} & -s_{23}c_{12} - s_{13}s_{12}c_{23} & c_{23}c_{13} \end{pmatrix}$$

Three Flavour Oscillation

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- $\Delta m_{21}^2 \ll \Delta m_{32}^2$

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Three mixing Angles

$\Delta m_{21}^2 \ll \Delta m_{32}^2$

 Atmospheric probabilities depend on $\Delta m_{32}^2, \theta_{13}, \theta_{23}$

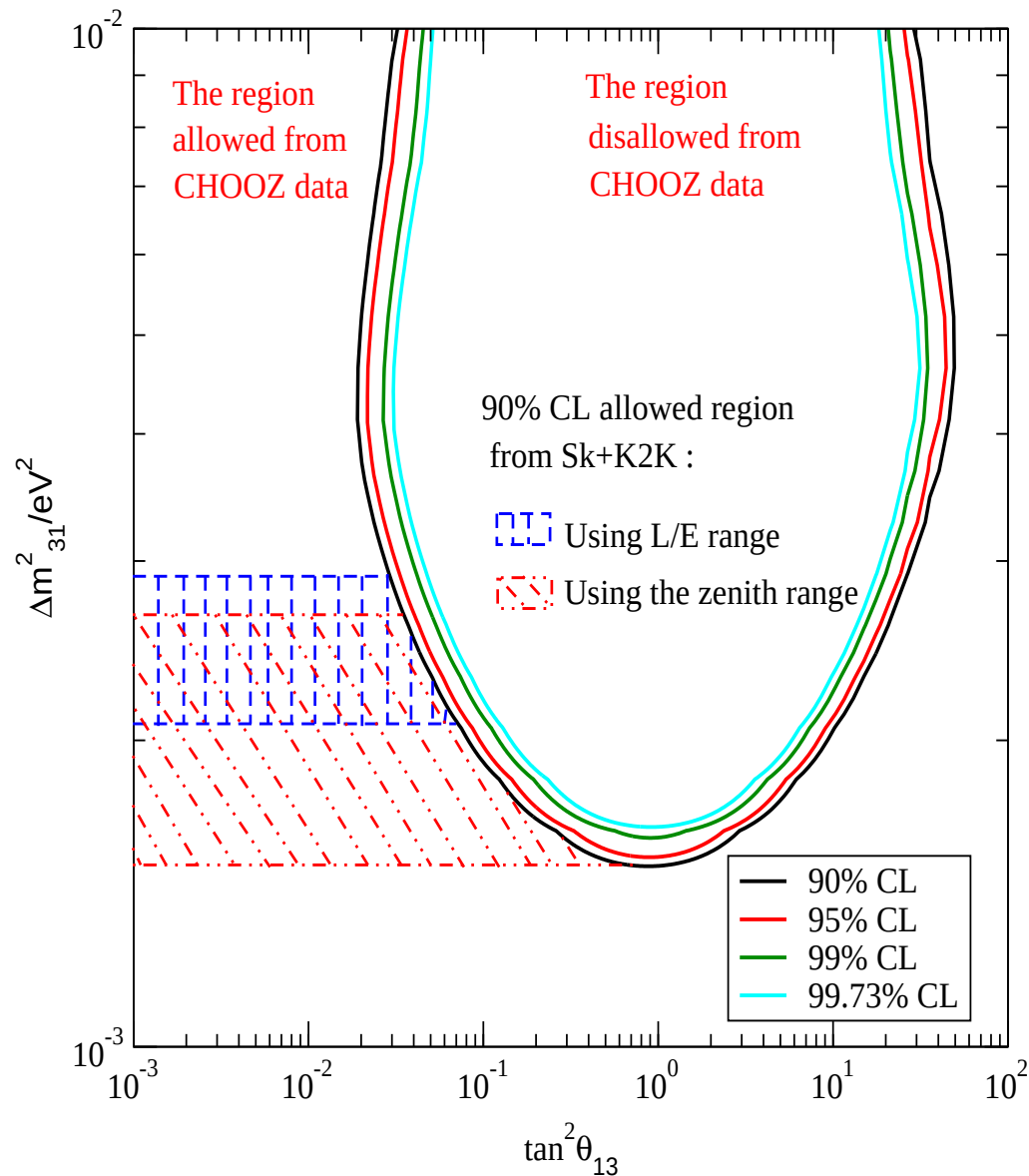
 Solar neutrino probabilities depend on $\Delta m_{21}^2, \theta_{12}, \theta_{13}$

 CP violation phases can be neglected

 $\theta_{13} = 0 \Rightarrow$ solar and atmospheric neutrinos decouple

 CHOOZ probability depends on $\Delta m_{31}^2, \theta_{13}$

Allowed area from CHOOZ

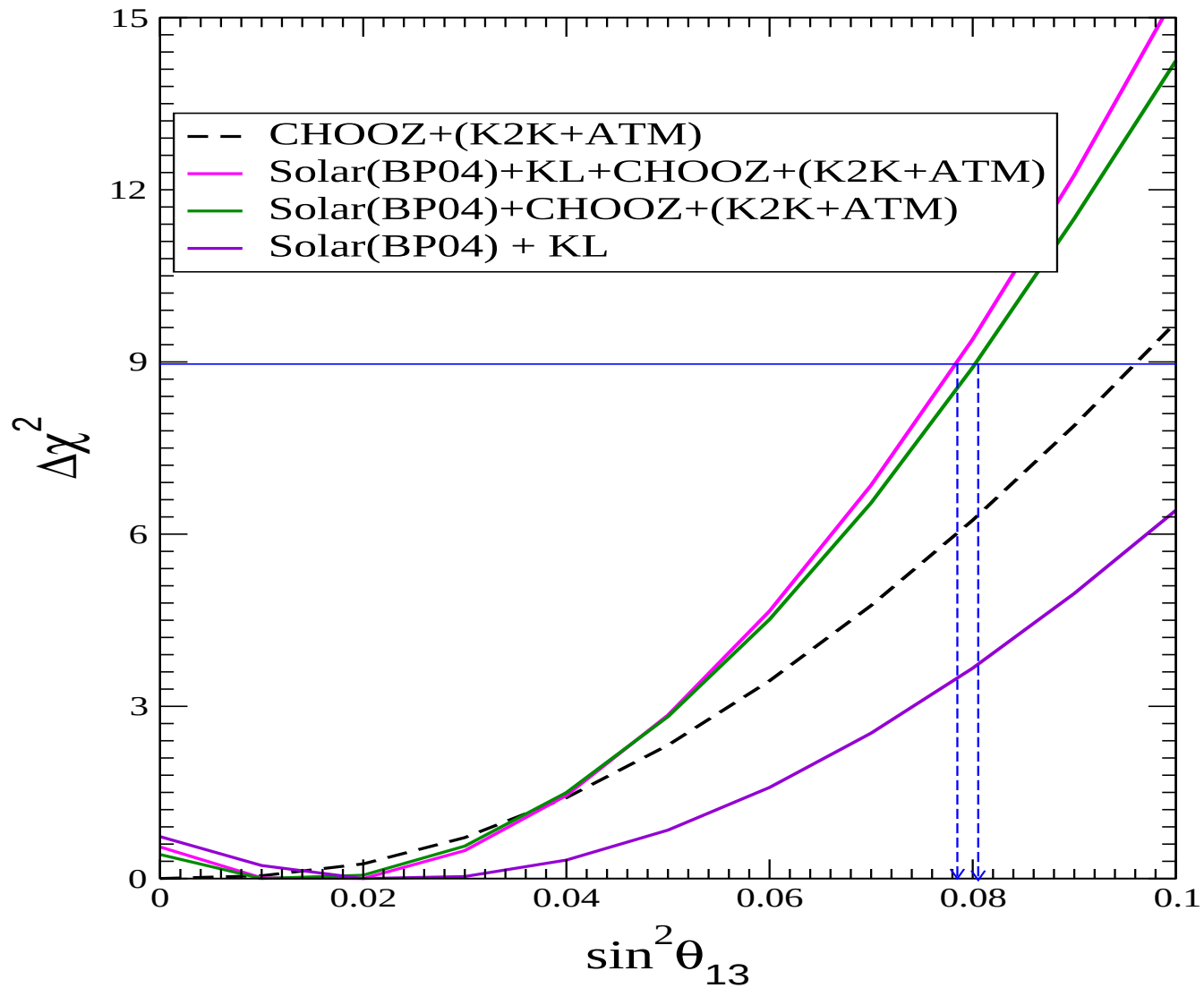


CHOOZ/PaloVarde → bound on θ_{13} from non-observation of $\bar{\nu}_e$ disappearance

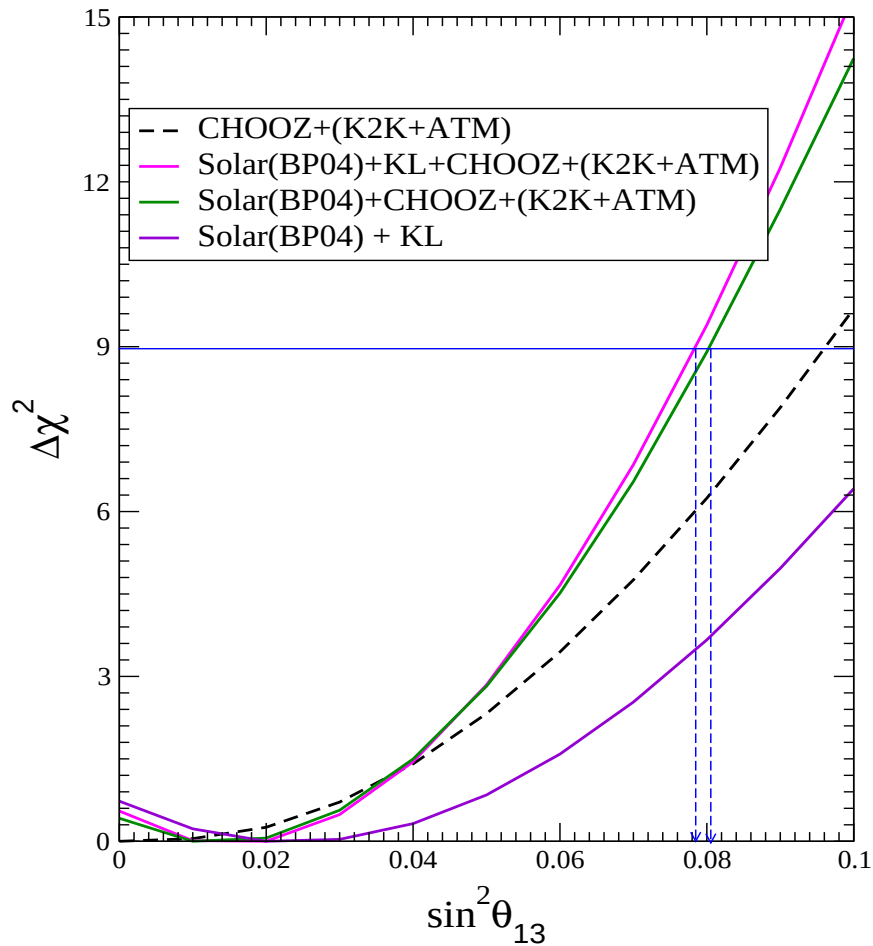
The θ_{13} bound from CHOOZ depends on Δm^2_{31}

Stronger bounds for higher Δm^2_{31}

Bounds on $\sin^2 \theta_{13}$



Bounds on $\sin^2 \theta_{13}$



3σ Bounds ($\Delta\chi^2 = 9$)

- Assuming the Δm_{32}^2 range from SK+K2K analysis

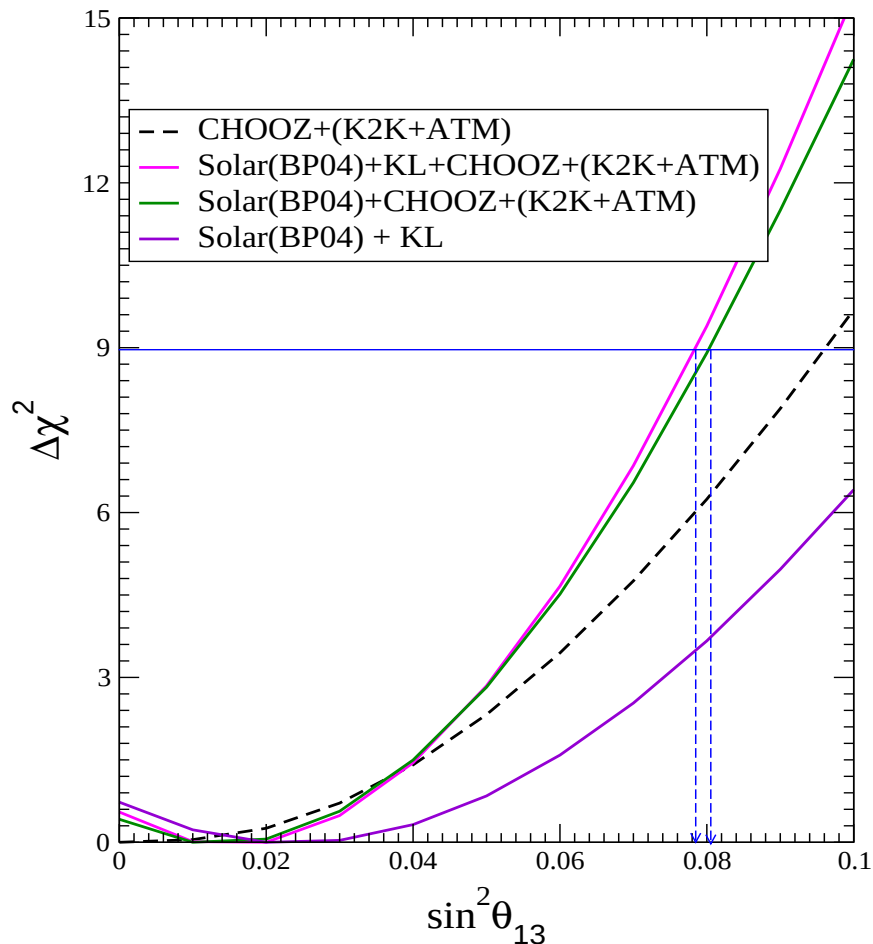
$$\sin^2 \theta_{13} < 0.096 \quad (\text{CHOOZ+ ATM+K2K})$$

$$\sin^2 \theta_{13} < 0.077 \quad (\text{Sol+CHOOZ+ ATM+K2K})$$

$$\sin^2 \theta_{13} < 0.074 \quad (\text{all data})$$

Bandyopadhyay et al., 2003

Bounds on $\sin^2 \theta_{13}$



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Bandyopadhyay et al., 2003

- Assuming the SK zenith analysis

$$\sin^2 \theta_{13} < 0.067 \quad (\text{all data})$$

Fogli et al., 2003

- Assuming SK L/E analysis

$$\sin^2 \theta_{13} < 0.05 \quad (\text{all data})$$

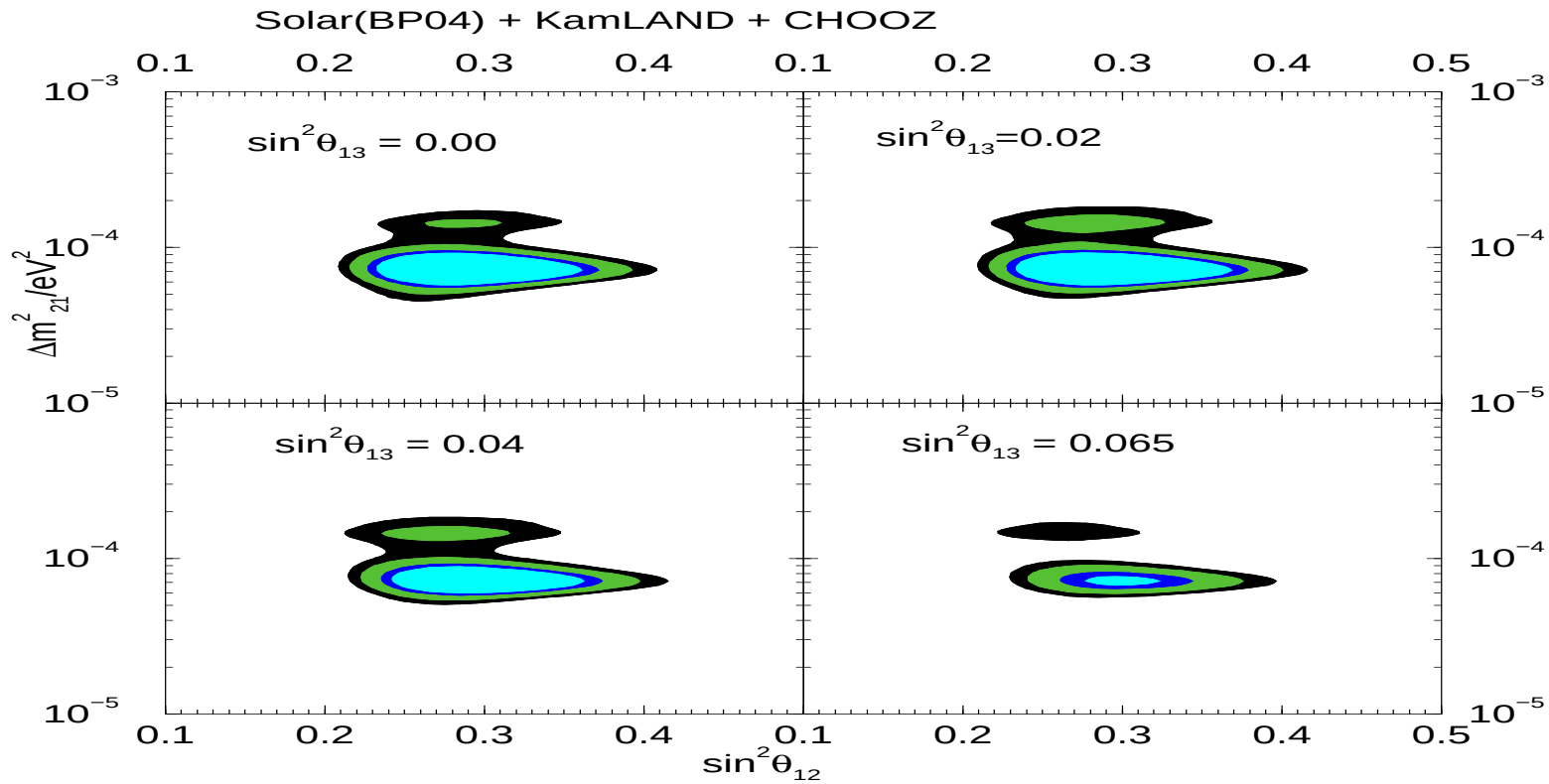
Fogli, Lisi, Marrone, Palazzo, 2004

- SK zenith+K2K+solar+reactor analysis

$$\sin^2 \theta_{13} < 0.061 \quad (\text{all data})$$

Maltoni et al., 2004

Effect of $\sin^2 \theta_{13}$ on Solar Parameters

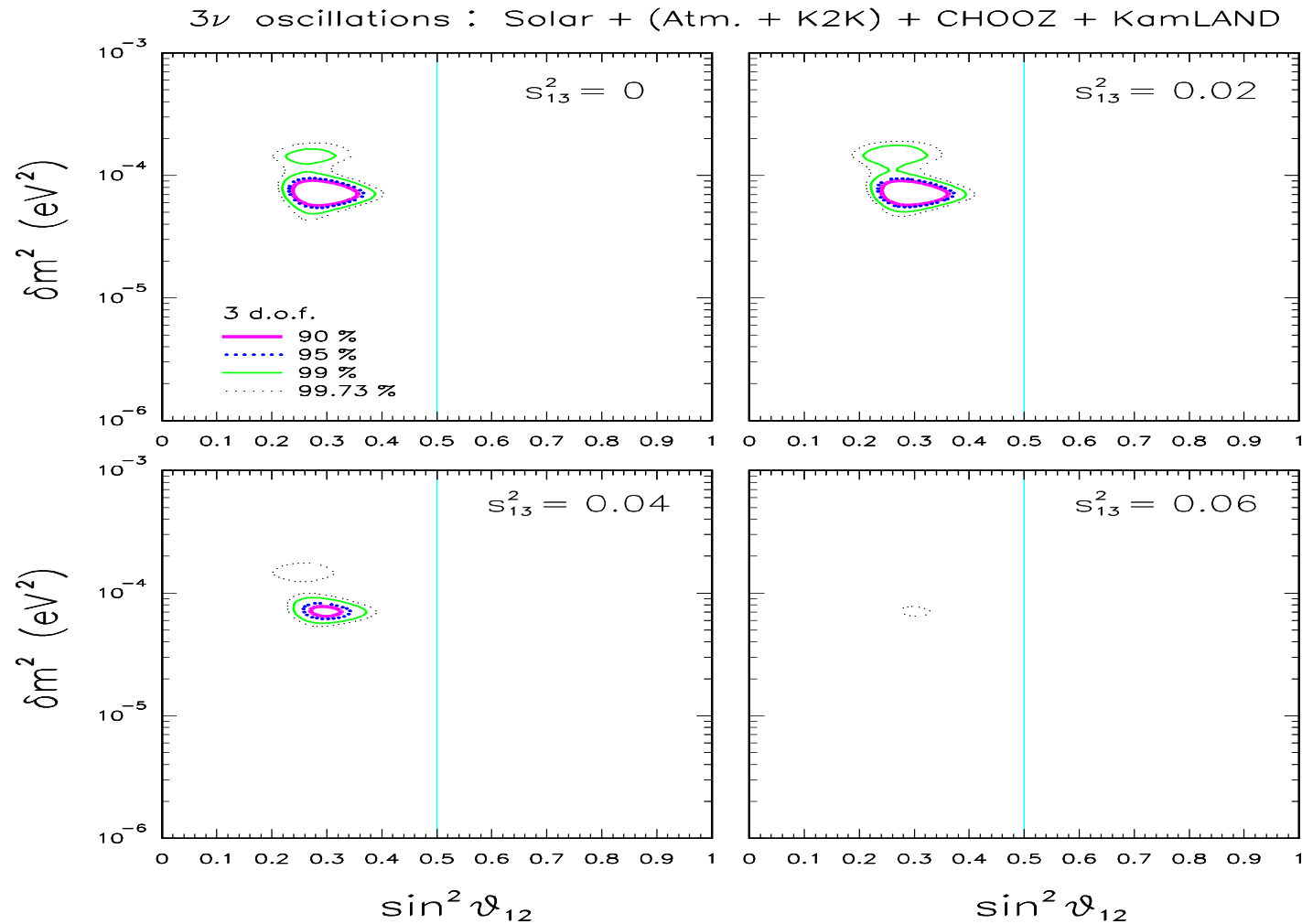


 **Solar:** $P_{ee} \approx \cos^4 \theta_{13} \sin^2 \theta_{12}$

 **KamLAND** $P_{ee} = \cos^4 \theta_{13} \left(1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m^2_{21} L}{4 E_\nu} \right)$

 **CHOOZ** $P_{ee} = \left(1 - \sin^2 2\theta_{13} \sin^2 \frac{\Delta m^2_{31} L}{4 E_\nu} \right)$

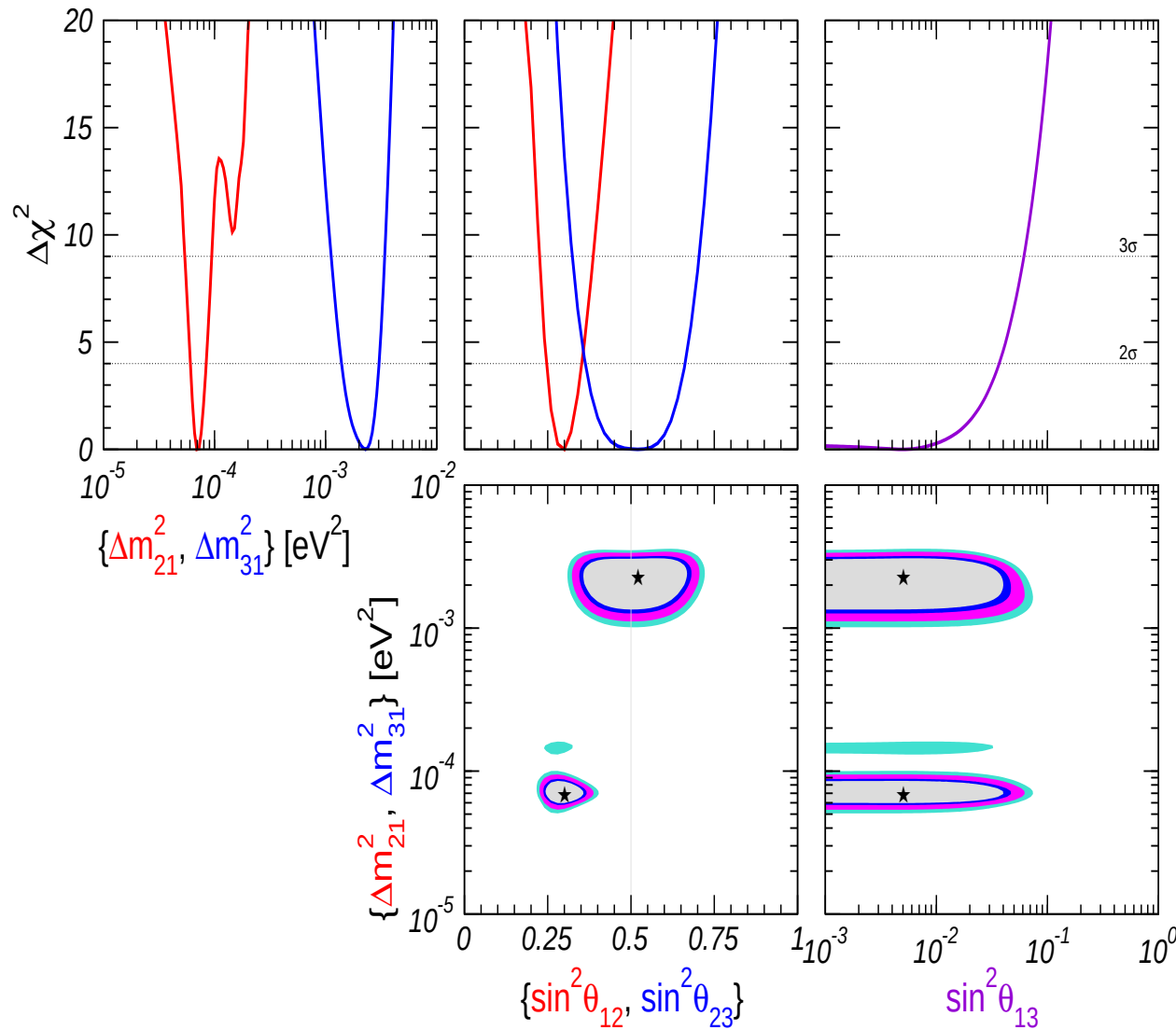
Effect of $\sin^2 \theta_{13}$ on Solar Parameters



Using the SK likelihood function of $\Delta m_{32}^2, \sin^2 \theta_{23}$ from the SK L/E analysis by graphical reduction

Fogli, Lisi, Marrone, Palazzo, 2004

Three generation parameters

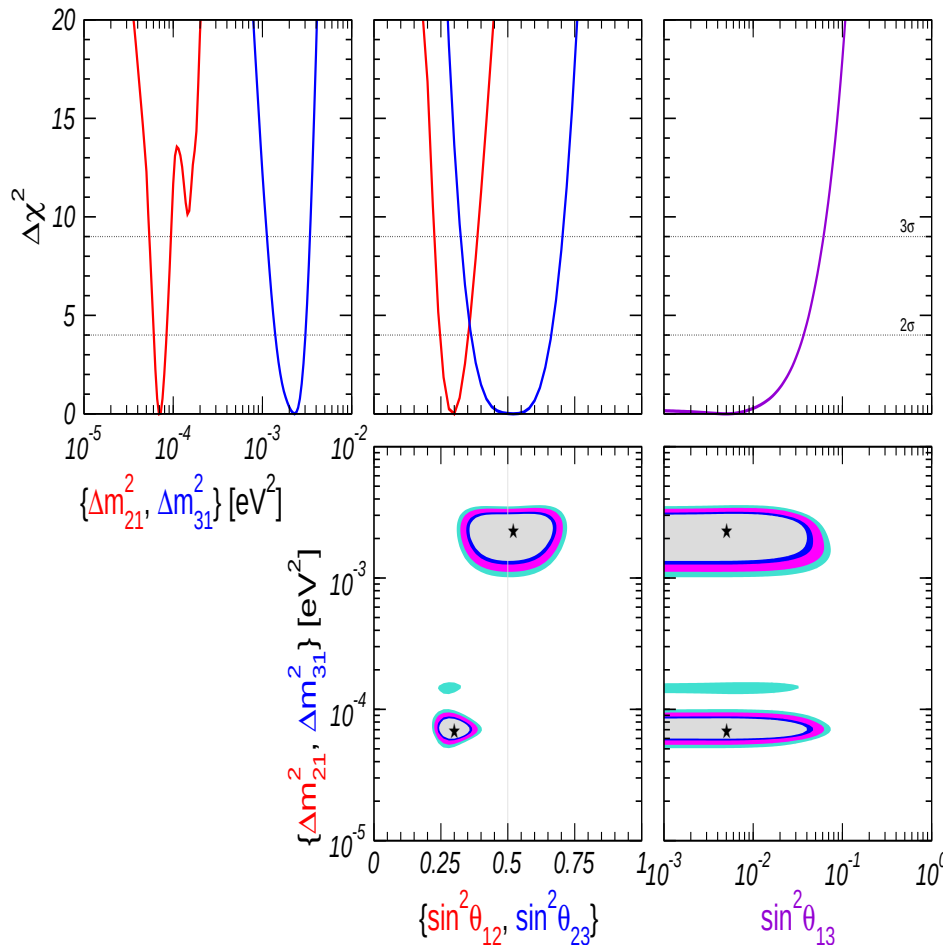


Maltoni et al., 2004



Minimised w.r.t undisplayed parameters

Three generation parameters



• 3σ range: 3-flavour analysis

$$\Delta m_{31}^2 = 1.1 - 3.4 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{23} = 0.32 - 0.7$$

$$\Delta m_{21}^2 = 5.4 - 9.4 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{12} = 0.23 - 0.39$$

• 3σ range: 2-flavour analysis

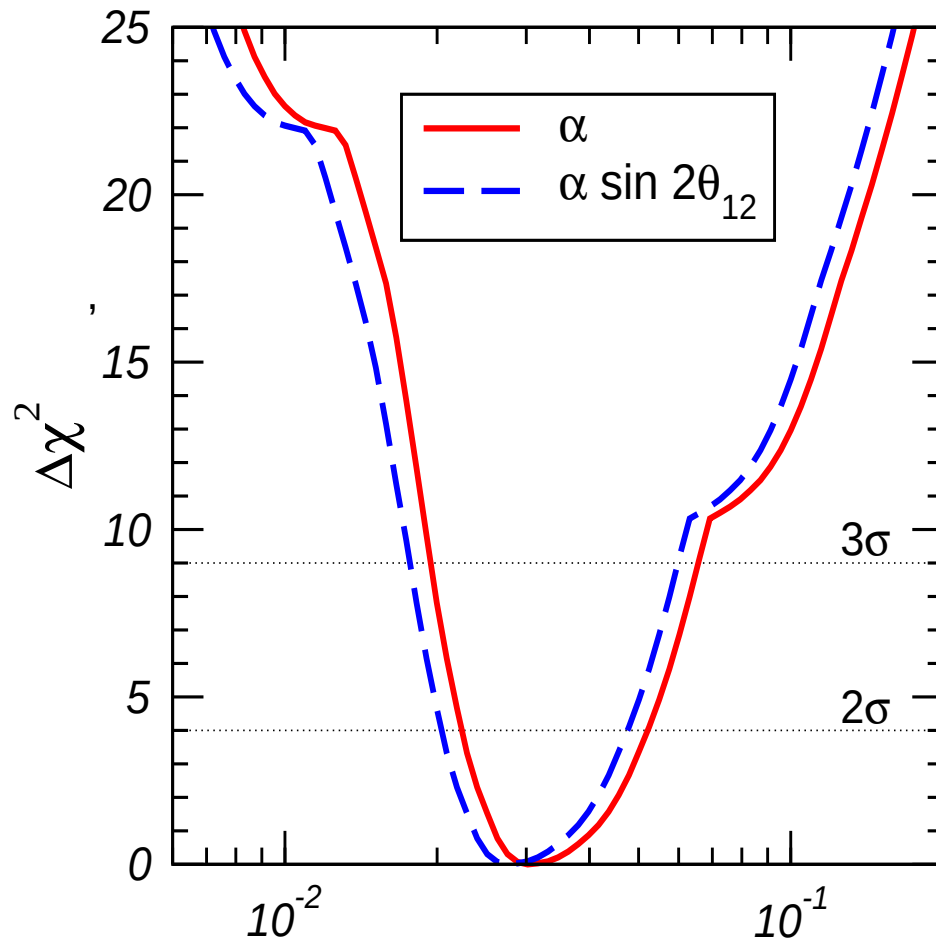
$$\Delta m_{31}^2 = 1.1 - 3.4 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{23} = 0.32 - 0.68$$

$$\Delta m_{21}^2 = 5.4 - 9.4 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{12} = 0.23 - 0.39$$

Bound on $\Delta m_{21}^2 / \Delta m_{31}^2$



● $\alpha = \Delta m_{21}^2 / \Delta m_{31}^2 \Rightarrow$ the hierarchy parameter associated with subleading oscillations

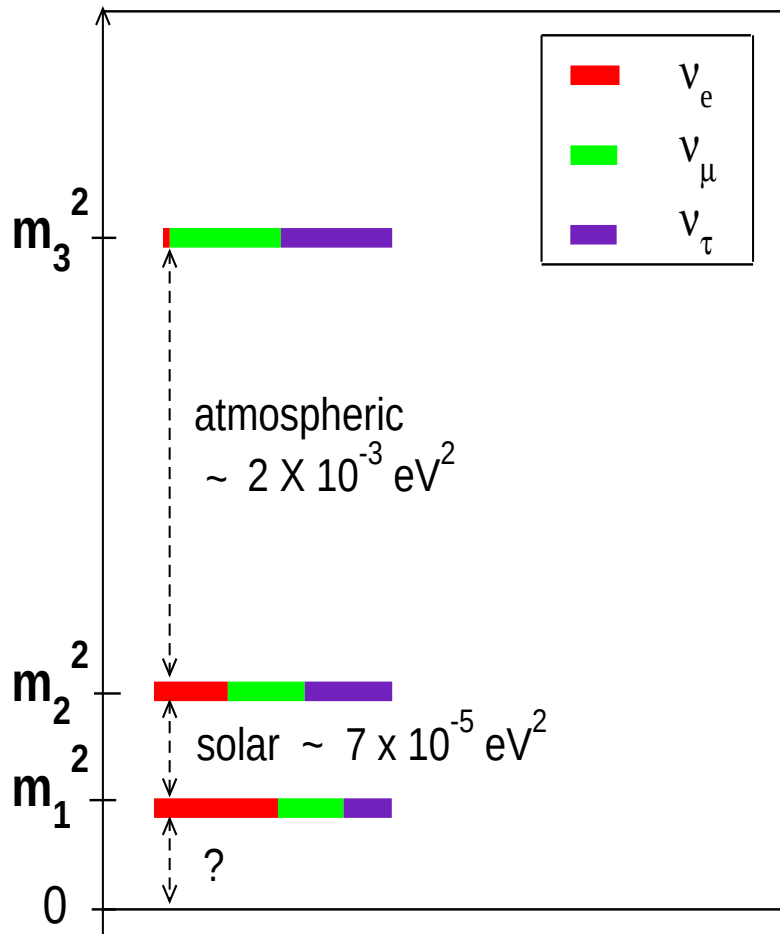
● Best-fit

$$\alpha = 0.03$$

$$\alpha \sin 2\theta_{12} = 0.028$$

Maltoni et al. 2004

Three neutrino oscillation parameters



• Best-fit

$$\Delta m_{21}^2 = 7.1 \times 10^{-5} \text{ eV}^2, \quad \sin^2 \theta_{12} = 0.29$$

$$\Delta m_{32}^2 = 2.4 \times 10^{-3} \text{ eV}^2, \quad \sin^2 \theta_{23} = 0.5, \quad \sin^2 \theta_{13} = 0.01$$

Fogli, Lisi, Marrone, Palazzo, 2004

$$U = \begin{pmatrix} 0.84 & 0.54 & 0.1 \\ -0.44 & 0.56 & 0.71 \\ 0.32 & -0.63 & 0.71 \end{pmatrix}$$

 Δm_{32}^2 can be positive or negative

 $\Delta m_{21}^2 > 0$ (from solar data)

Summary-Current status

Solar+KamLAND

- MSW effect in sun is confirmed.
- Salt phase data from SNO further restricts $\Delta m_{\odot}^2$ and $\sin^2 \theta_{\odot}$
- Solar + new KamLAND data favours **low-LMA**
- Best-fit $\Delta m_{\odot}^2 = 8.3 \times 10^{-5} \text{ eV}^2$, $\sin^2 \theta_{\odot} = 0.28$
- **high-LMA** disallowed at more than 3σ
- **Maximal mixing** disfavoured at more than 5σ
- Solar Neutrino physics enters precision era

Atmospheric+K2K

- Analysis of SK zenith angle data gives $\Delta m_{atm}^2 \sim 2.1 \times 10^{-3} \text{ eV}^2$, $\sin^2 \theta_{atm} = 0.5$
- K2K constrains the higher Δm^2 part
- The L/E data gives $\Delta m_{atm}^2 = 2.4 \times 10^{-3} \text{ eV}^2$, $\sin^2 \theta_{atm} = 0.5$
- Increased precision in Δm_{atm}^2 with L/E data

Summary -Current status

Three Generation Analysis

- Solar,KamLAND ,atmospheric,K2K,CHOOZ data compatible
- The bound on θ_{13} is sensitive to the allowed Δm_{32}^2 range and $\sin^2 \theta_{13} < 0.05 - 0.07$
- Best fit value of $\Delta m_{21}^2 / \Delta m_{31}^2 = 0.03$
- The two generation allowed parameter regions are stable

Future goals

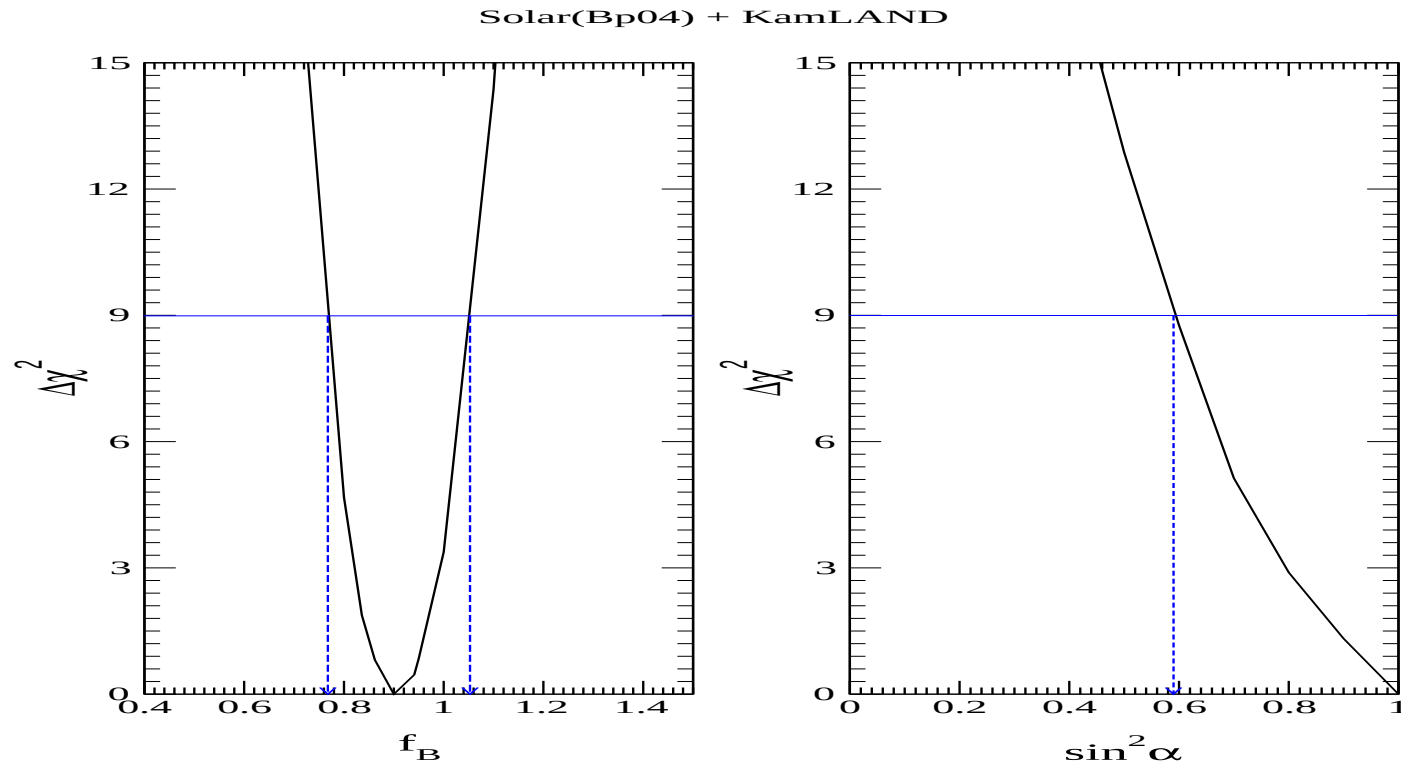
- Improve the **precision** of parameters we already know
- Obtain some measure of smallness of θ_{13}
- Determine the **sign of Δm_{32}^2**
- Search for **CP violation** in the lepton sector;
- **Sbleading effects** in solar and atmospheric neutrinos
 - **Sterile neutrinos, discrete symmetries, Nonstandard Interactions . . .**

Future goals

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 - **Sterile** neutrinos, **discrete symmetries**, **Nonstandard Interactions** . . .

Thanks to T.Kajita, E. Lisi, M. Maltoni for disucssions

Sterile component in solar ν_e flux



$$\nu_e \rightarrow \sin \alpha \nu_a + \cos \alpha \nu_s$$

$$\sin^2 \alpha = 1, \text{ pure } \nu_e \rightarrow \nu_a$$

$$\sin^2 \alpha = 0, \text{ pure } \nu_e \rightarrow \nu_s$$

- Best-fit $\sin^2 \alpha = 1.0$
- sterile fraction $\cos^2 \alpha < 0.41$ at 3σ

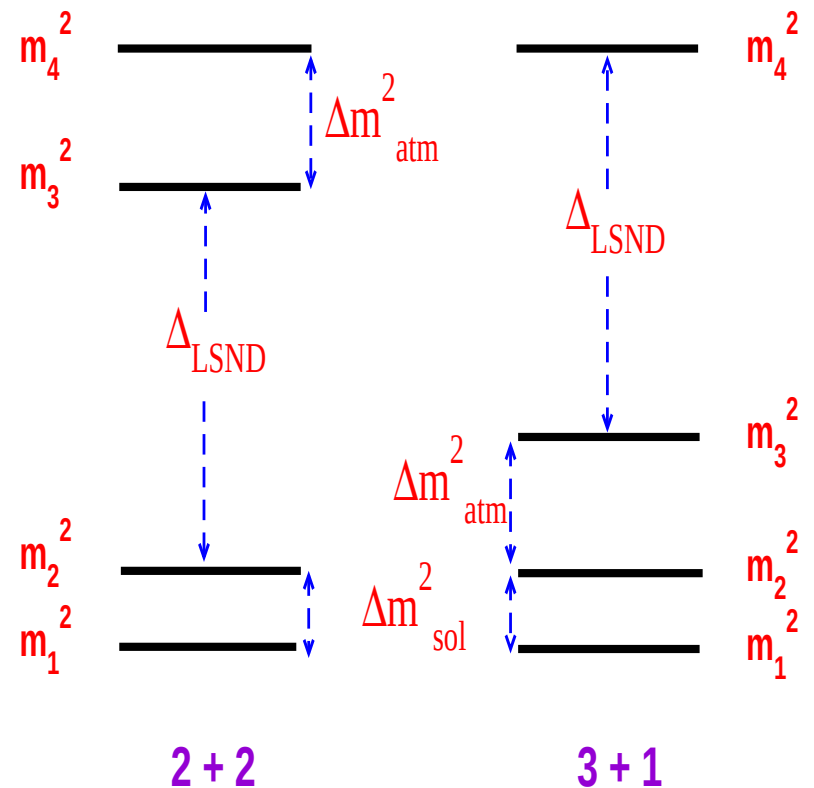
Accommodating LSND

● Adding extra sterile neutrinos

● CPT violation

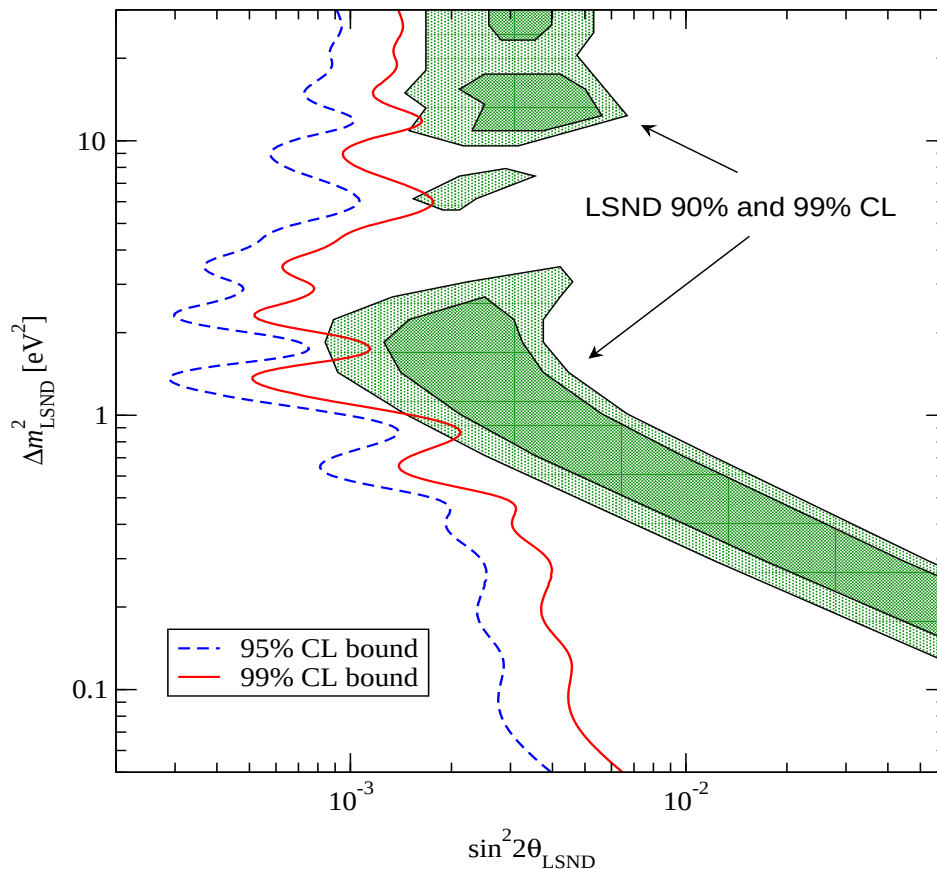
One additional sterile neutrino

- 6 mixing angles
- two possible mass schemes



One additional sterile neutrino: 3+1 vs 2+2

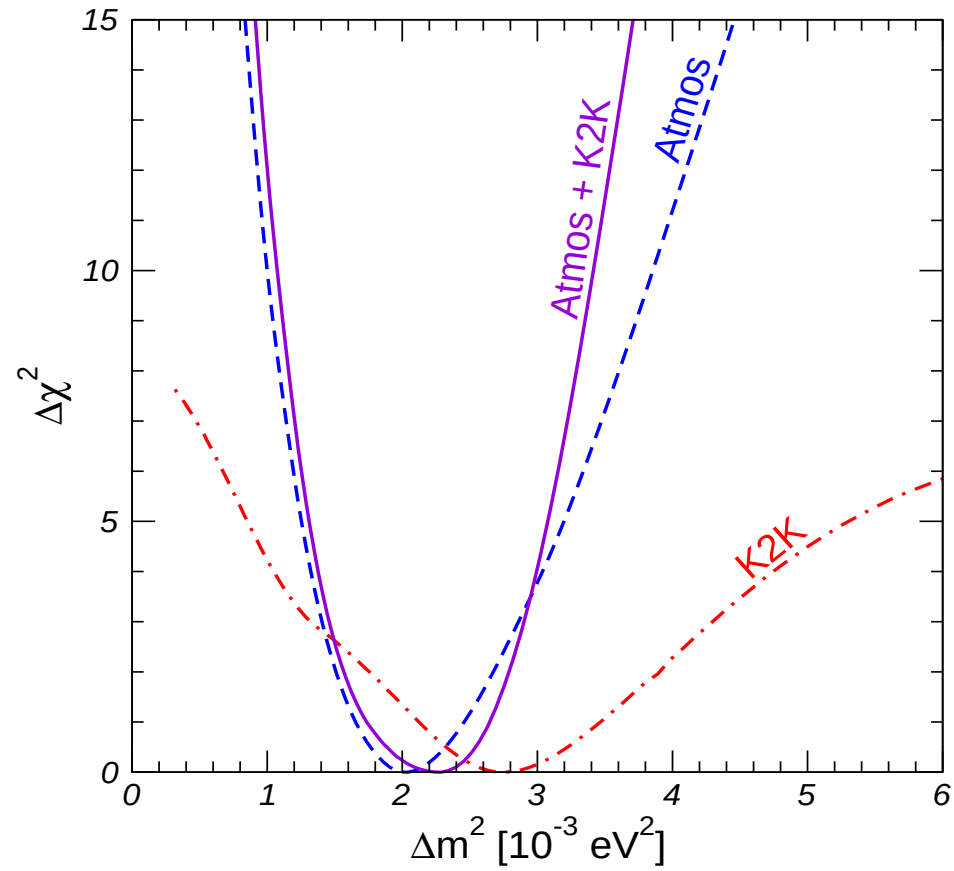
- 3+1 disfavoured from SBL accelerator and reactor experiments
Karmen+Bugey+CDHS+NOMAD



- Two small areas consistent at 99% C.L.
- 2+2 disfavored irrespective of LSND
is confirmed or not
—oscillation to almost pure sterile state is disfavoured in both solar and atmospheric

M. Maltoni *et al.*, [hep-ph/0209368](#)

Effect of K2K on Δm_{atm}^2



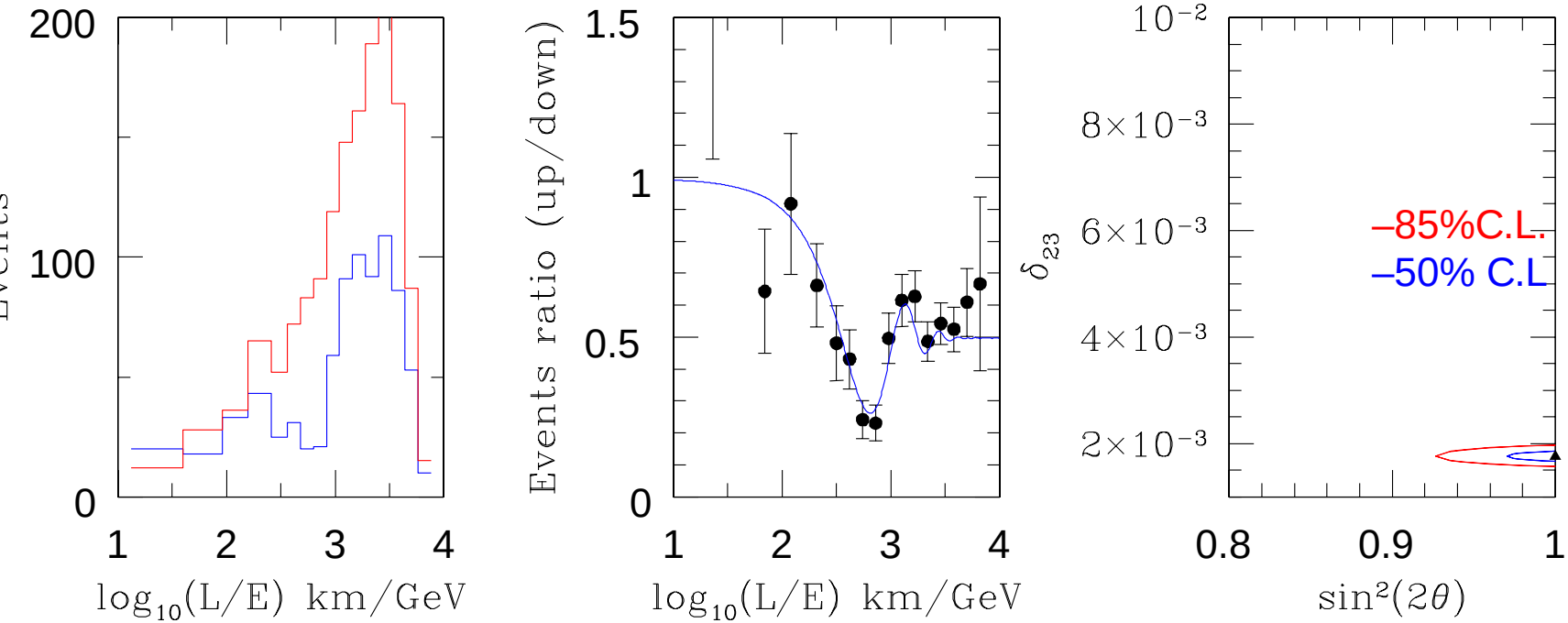
Maltoni et al



$$\delta = 2 \times 10^{-3} \text{ eV}^2$$

INO:Preliminary

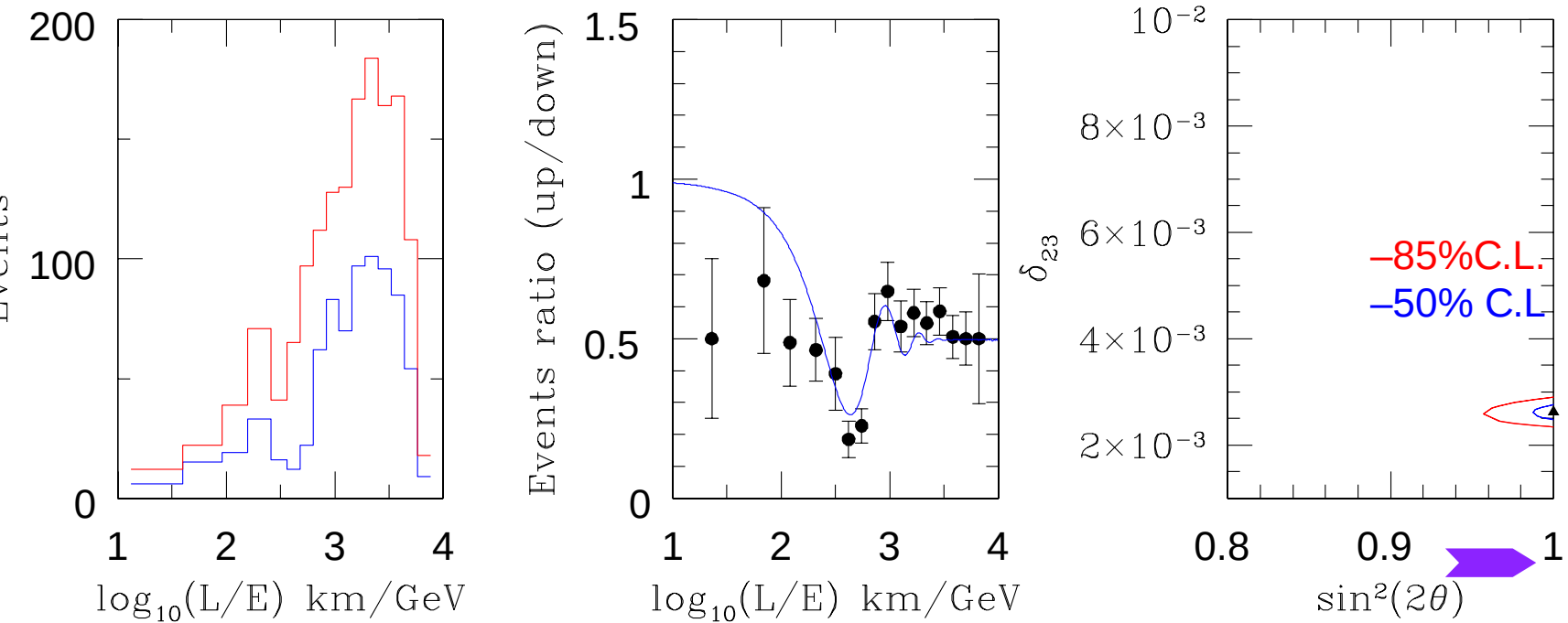
$$\delta_{23} = 2 \times 10^{-3} \text{ eV}^2; \sin^2 2\theta = 1$$



$$\delta = 3 \times 10^{-3} \text{ eV}^2$$

INO:Preliminary

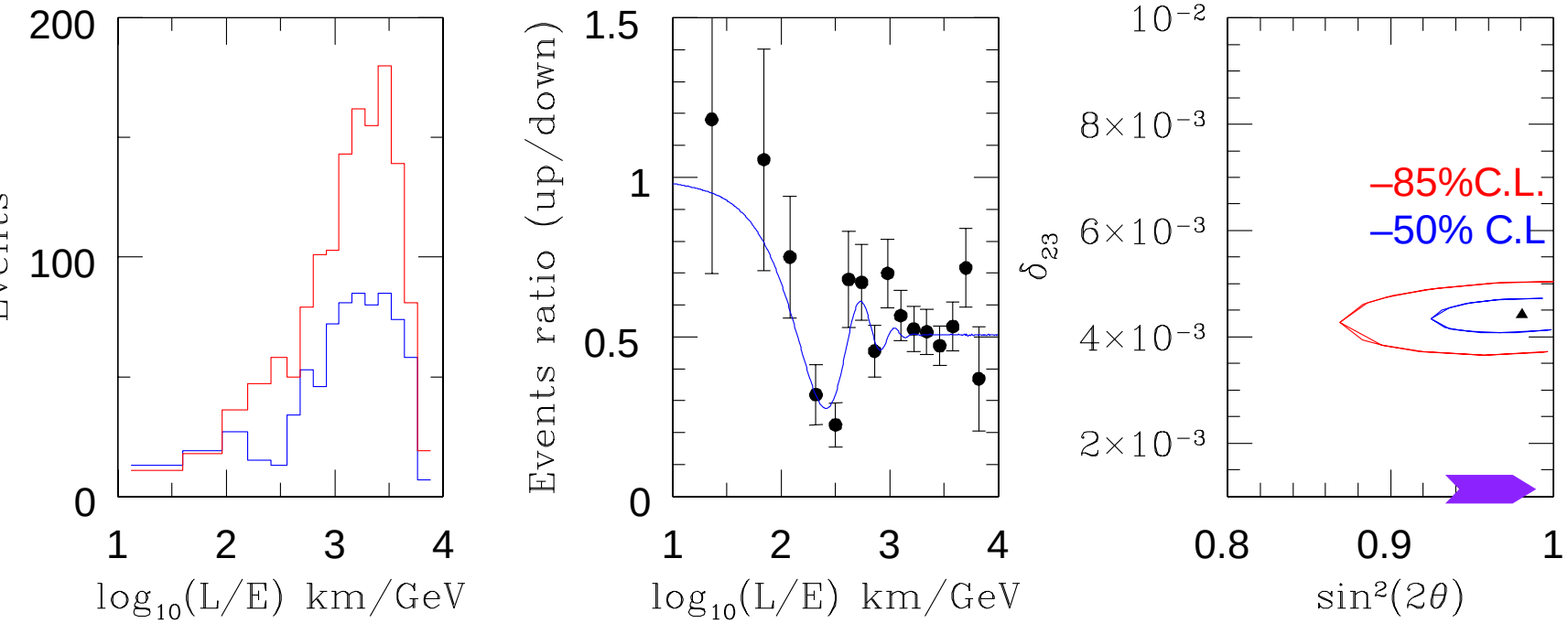
$$\delta_{23}=3\text{e-3 eV}^2; \sin^2 2\theta=1$$



$$\delta = 5 \times 10^{-3} \text{ eV}^2$$

INO:Preliminary

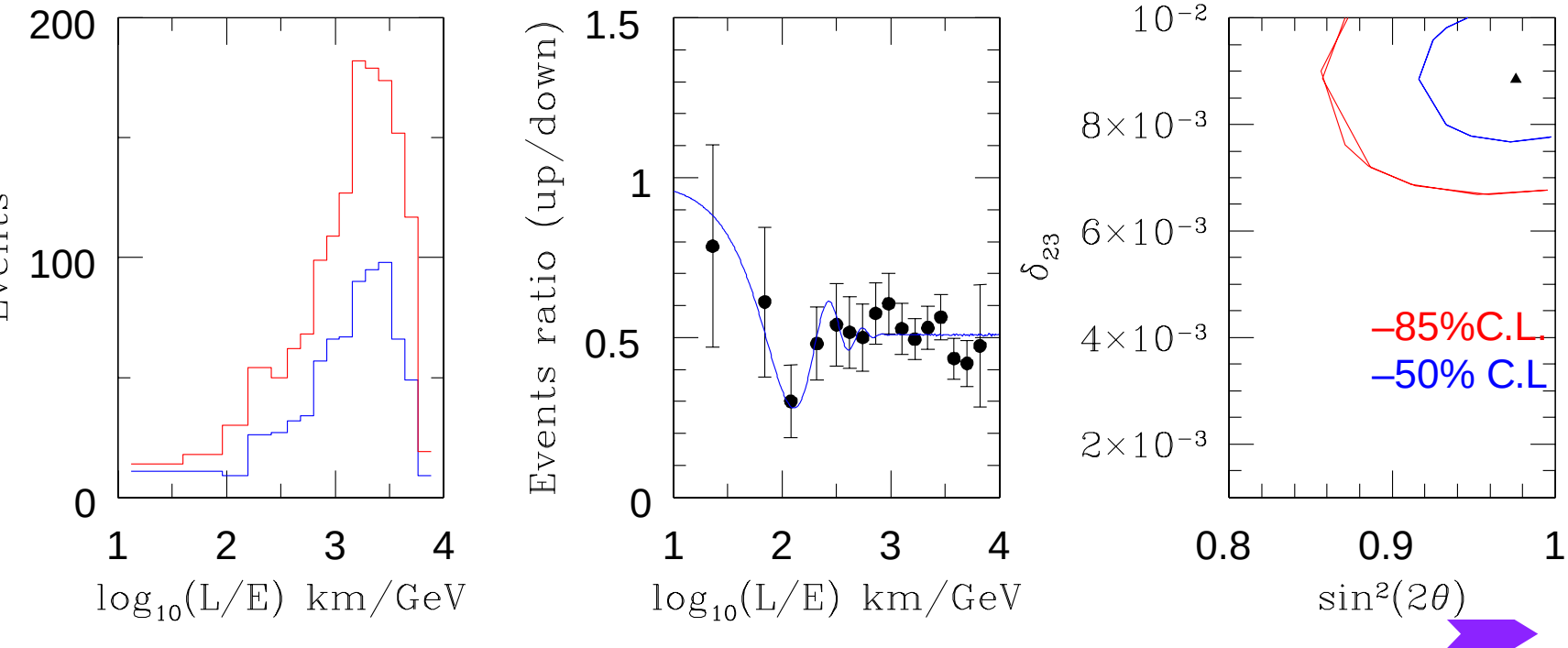
$$\delta_{23} = 5 \times 10^{-3} \text{ eV}^2; \sin^2 2\theta = 1$$



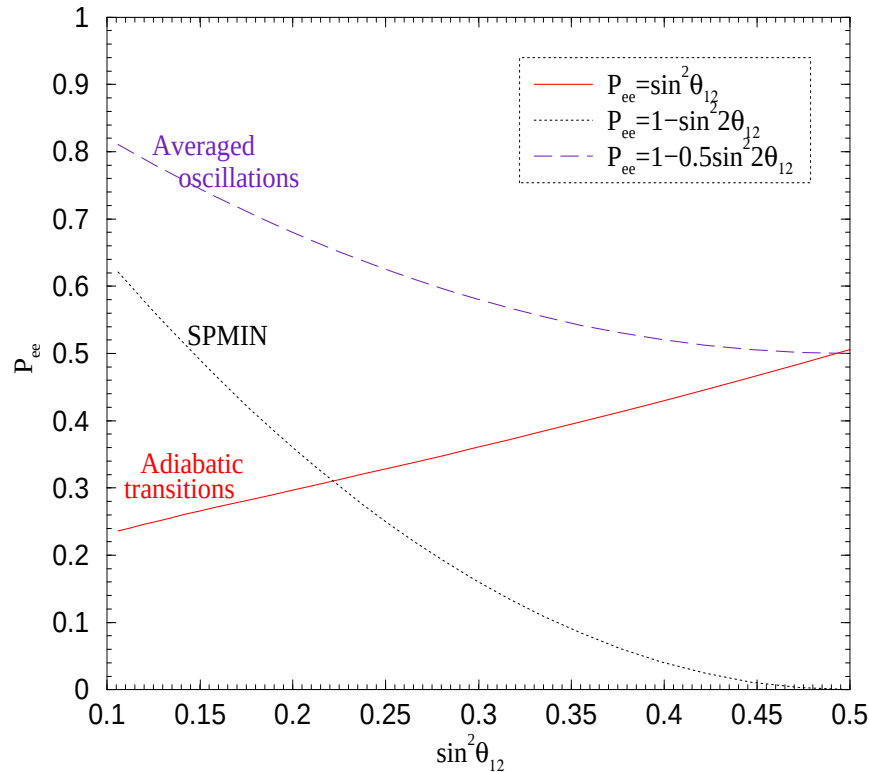
$$\delta = 8 \times 10^{-3} \text{ eV}^2$$

INO:Preliminary

$$\delta_{23} = 8 \times 10^{-3} \text{ eV}^2; \sin^2 2\theta = 1$$



Sensitivity of $\sin^2 \theta_\odot$



$$(\Delta \sin^2 \theta_\odot)_{AD} \sim \Delta P_{ee}; \quad \text{good if}$$

$$(\Delta \sin^2 \theta_\odot)_{AV} \sim \frac{\Delta P_{ee}}{-2 \cos 2\theta_\odot}; \quad \text{better if}$$

$$(\Delta \sin^2 \theta_\odot)_{spmin} \sim \frac{\Delta P_{ee}}{-4 \cos 2\theta_\odot}; \quad \text{best if}$$

For 8B neutrinos undergoing matter enhanced resonance

$$P_{ee}^{AD} \approx \sin^2 \theta_\odot \quad \text{LMA(AD)}$$

For VO $\Rightarrow \sin^2(\Delta m_\odot^2 L/E) = 1/2$

$$P_{ee}^{AV} = 1 - \frac{1}{2} \sin^2 2\theta_\odot$$

Averaged Oscillations(AV)

For VO $\Rightarrow \sin^2(\Delta m_\odot^2 L/E) = 1$

$$P_{ee}^{SPMIN} = 1 - \sin^2 2\theta_\odot$$

Survival Prob. MINima(SPMIN)

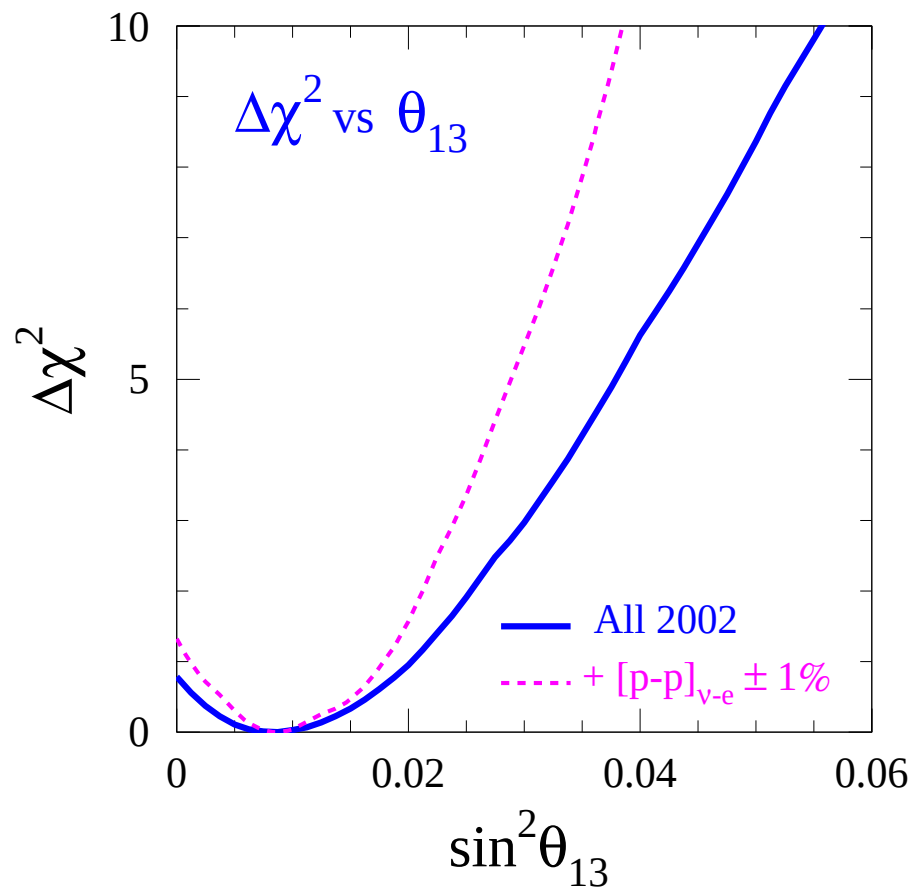
$$\sin^2 \theta_\odot \sim 0.5$$

$$\cos 2\theta \gtrsim 0.5 (\sin^2 \theta_\odot \lesssim 0.25)$$

$$\cos 2\theta_\odot \gtrsim 0.25 (\sin^2 \theta_\odot \lesssim 0.375) \quad \Rightarrow$$

Future precision of three neutrino oscillation parameters

 θ_{13} from solar



J.N. Bahcall and C. Pena-Garay, hep-ph/0305159

 Reactors, Superbeams... 

Future precision of three neutrino oscillation parameters

-  θ_{13} , θ_{23} , sign of Δ_{23} from observation of earth matter effects in atmospheric neutrinos
-  Detectors with charge identification capability
-  MINOS, INO....

Palomarez-Ruiz, Petcov, 2004