

$\nu$ 2000  
Sudbury  
June 18, 2000

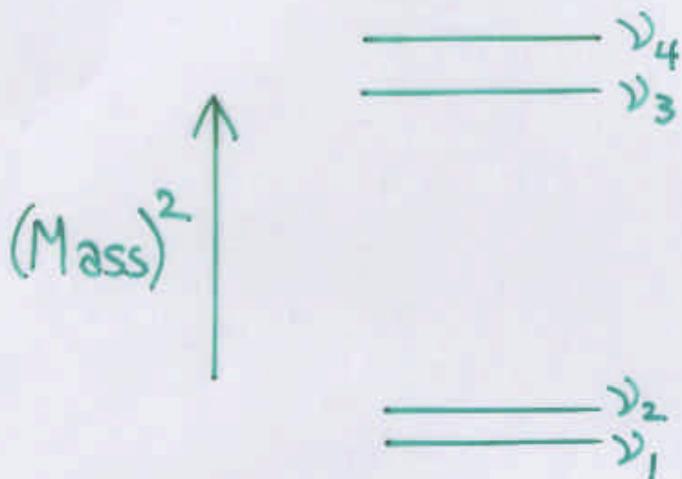
Neutrino Properties  
Boris Kayser

# NEUTRINO PROPERTIES

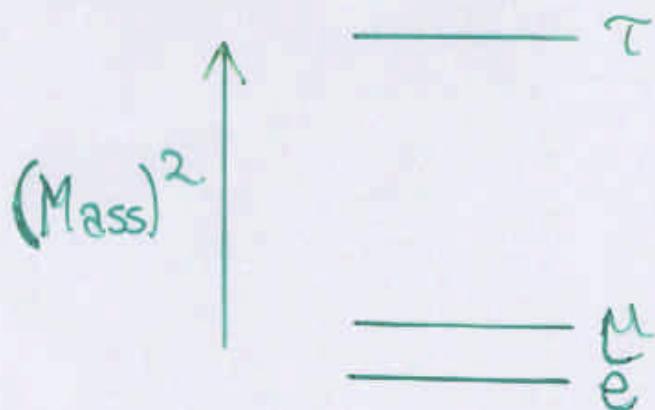
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Neutrinos almost certainly have masses and mix.

There is some spectrum of three or more neutrino mass eigenstates  $\nu_m$ :

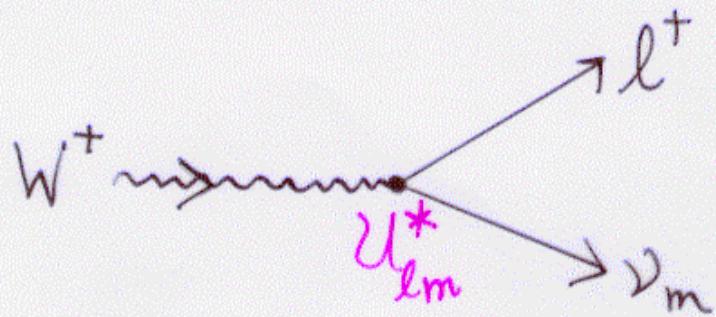


This is the neutrino analogue of the spectrum of charged-lepton mass eigenstates  $l = e, \mu$ , and  $\tau$ :



2)

Mixing means that the weak interaction couples a given charged lepton of definite mass,  $l$ , to more than one neutrino of definite mass,  $\nu_m$ .



$U$  is the Maki-Nakagawa-Sakata leptonic mixing matrix.

The neutrino state produced in association with a specific charged lepton  $l$  is

$$|\nu_l\rangle = \sum_m U_{lm}^* |\nu_m\rangle$$

$\uparrow$  Neutrino of flavor  $l$

$\uparrow$  Neutrino of mass  $M_m$

If there are, say, four neutrino mass eigenstates, then one linear combination of them,

$$|\nu_{\text{sterile}}\rangle = \sum_m U_{sm}^* |\nu_m\rangle,$$

has no normal weak couplings.

Having discovered that neutrinos have masses and mix —

### What Would We Like To Learn?

- How many neutrino flavors, active and sterile, are there? Equivalently, how many neutrino mass eigenstates are there?
- What are the masses,  $M_m$ , of the mass eigenstates,  $\nu_m$ ?  
 (Oscillation experiments can measure only  
 mass splittings  $\delta M_{mm'}^2 \equiv M_m^2 - M_{m'}^2$ .)

4)

- Are the neutrinos of definite mass—
  - \* Majorana particles ( $\bar{\nu}_m = \nu_m$ ),  
or
  - \* Dirac particles ( $\bar{\nu}_m \neq \nu_m$ ) ?
- What are the elements  $U_{\ell m}$  of the leptonic mixing matrix?
- Does the behavior of neutrinos, in oscillation and other contexts, violate CP invariance?
- What are the electromagnetic properties of neutrinos? What are their dipole moments?
- What are the lifetimes of the neutrinos?

# What is Known Now About These Questions, and How Will We Learn More?

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## How Many Neutrinos Are There?

Most people believe that if  $\nu_0$ ,  $\nu_{\text{Atmos}}$ , and  $\nu_{\text{LSND}}$  all oscillate, then there are more than 3 neutrinos:

3 neutrinos can fit  $\nu_0$ ,  $\nu_{\text{Atmos}}$  and  $\nu_{\text{LSND}}$ :

Teshima, Sakai, Inagaki

Thun & McKee

Barenboim & Scheck

Ohlsson & Snellman

Haug, Faessler, Vergados

No they can't:

Giunti

With only 3 neutrino mass eigenstates,

$$\sum \delta M^2 = (M_3^2 - M_2^2) + (M_2^2 - M_1^2) + (M_1^2 - M_3^2) = 0.$$

But -

### Oscillating Neutrinos

Solar  
Atmospheric  
LSND

	Required $ \delta M^2 $ (eV $^2$ )
Solar	$10^{-10}$ or $10^{-5}$
Atmospheric	$10^{-3}$
LSND	1
	$\sum \delta M^2 \neq 0$

∴ Must add a 4<sup>th</sup> mass eigenstate.

Since  $Z \rightarrow \nu_e \bar{\nu}_e$  yields only 3 distinct neutrinos of definite flavor, the 4 flavor eigenstates corresponding to the 4 mass eigenstates must be -

$\nu_e, \nu_\mu, \nu_\tau, \nu_{\text{sterile}}$ .

Solar + Atmospheric + LSND Oscillations  
 $\Rightarrow$  A new breed of neutrino.

## II How Much Do the Mass Eigenstates Weigh?

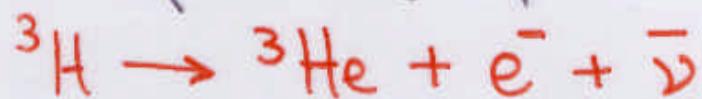
Oscillation experiments yield only  $(\text{mass})^2$  splittings:

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$$\text{Amp}(\nu_e \rightarrow \nu_{e'}) = \sum_m U_{em}^* U_{e'm'} e^{-i M_m^2 \frac{L}{2E}}$$

Suggested relative  $(\text{mass})^2$  spectra: Smirnov

Studies of the  $\beta^-$  energy spectrum in



may not be able to gain sensitivity to

$$M_m \lesssim 1 \text{ eV} . \quad (\text{Otten})$$

There may be a mass eigenstate that weighs this much.

If the LSND oscillation is genuine, there is at least one neutrino  $\nu_H$  with mass

$$M_H \geq \sqrt{\delta M_{\text{LSND}}^2} \gtrsim \sqrt{0.2 \text{ eV}^2} \approx 0.4 \text{ eV}.$$

8]

$$\text{BR}({}^3\text{H} \rightarrow {}^3\text{He} + \bar{e}^- + \bar{\nu}_H) \sim |U_{eH}|^2$$

may be large or small. \*

If the LSND oscillation is not genuine, the heaviest mass eigenstate may have a mass no larger than

$$\sqrt{\delta M_{\text{Atmos}}^2} \sim \sqrt{4 \times 10^{-3} \text{ eV}^2} \sim 0.06 \text{ eV}.$$

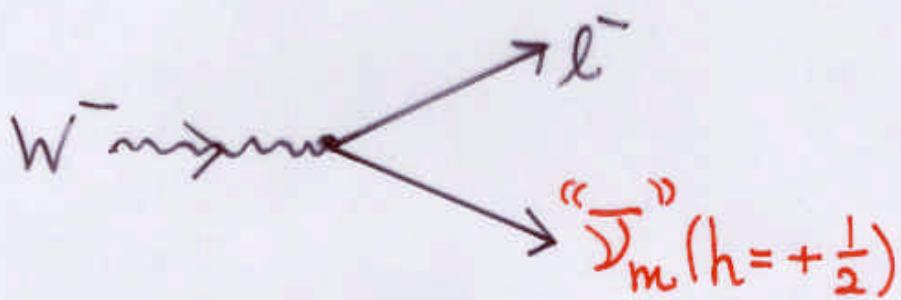
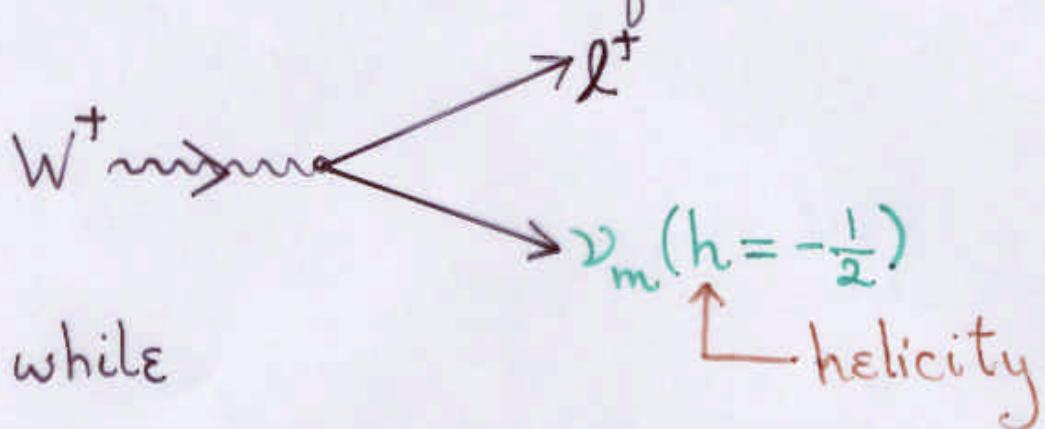
It is important to study tritium decay, but is there a more sensitive probe of absolute masses??

Neutrinoless double beta decay can perhaps shed light on neutrino masses, as we shall see.

\* Studies of supernova neutrinos may be able to probe  $\sim$  few eV masses of neutrinos strongly coupled to  $\mu$  or  $\tau$ . (Beacom, Boyd, Mezzacappa)

Does  $\bar{\nu}_m = \nu_m$ ?

What does this question mean?



Is helicity the only difference between  $\nu_m (h = -)$  and  $\bar{\nu}_m (h = +)$ ?

Would a  $\bar{\nu}_m (h = +)$  become a  $\nu_m (h = -)$  if we could somehow reverse its helicity?

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If so, then

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$$\bar{\nu}_m(h) = \nu_m(h).$$

Majorana  
neutrino

However,  $\bar{\nu}_m(h=+)$  and  $\nu_m(h=-)$  may differ by a conserved quantum number (usually the lepton number L), in addition to having opposite helicity.

If they do have this added difference, then

$$\bar{\nu}_m(h) \neq \nu_m(h).$$

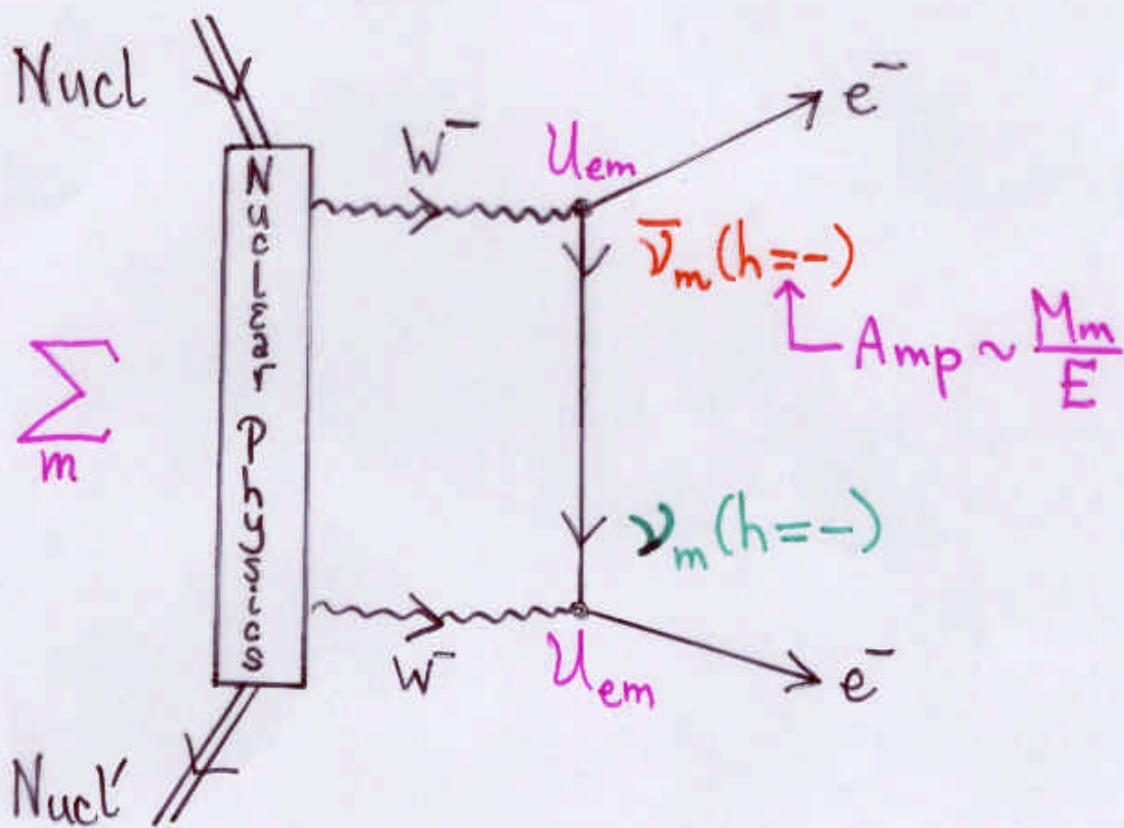
Dirac  
neutrino

The "see-saw" explanation of why neutrinos are so light predicts that they are Majorana particles.

(Gell-Mann, Ramond, Slansky  
Yanagida  
Mohapatra, Senjanovic)

To try to show that neutrinos are Majorana particles, look for neutrinoless double beta decay ( $\beta\beta_{0\nu}$ ):

$$\text{Nucl} \rightarrow \text{Nucl}' + 2\bar{e}^-.$$



Iff  $\bar{\nu}_m(h) = \nu_m(h)$ ,

$$\text{Amp}[\beta\beta_{0\nu}] = \underbrace{\left( \sum_m M_m U_{em}^2 \right)}_{M_{\beta\beta}} \times (\text{Nuclear Factor}).$$

12) Can we distinguish between Majorana  
and Dirac neutrinos via -

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Probability

$$P[\bar{\nu}_e(\text{RH}) \rightarrow \bar{\nu}_e(\text{RH})] = P[\nu_e(\text{LH}) \rightarrow \nu_e(\text{LH})] \quad \text{Majorana}$$

but

$$P[\bar{\nu}_e(\text{RH}) \rightarrow \bar{\nu}_e(\text{RH})] \neq P[\nu_e(\text{LH}) \rightarrow \nu_e(\text{LH})] \quad \text{Dirac}$$

in a constant magnetic field ?

(Balaji & Grimus)

### 3) What Are the Mixing Matrix Elements $U_{\ell m}$ ?

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With  $L$  = distance a neutrino travels,  
and  $E$  = neutrino energy,  
the oscillation probability is

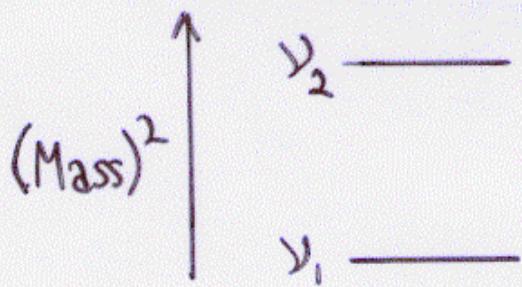
$$\begin{aligned} P(\overleftarrow{\nu}_e \rightarrow \overleftarrow{\nu}_{e'}) &= \\ &= \delta_{\ell\ell'} - 4 \sum_{m>m'} \text{Re}(U_{\ell m}^* U_{\ell' m} U_{\ell m'} U_{\ell' m'}^*) \sin^2(\delta M_{mm'}^2 \frac{L}{4E}) \\ &\quad \pm 2 \sum_{m>m'} \text{Im}(U_{\ell m}^* U_{\ell' m} U_{\ell m'} U_{\ell' m'}^*) \sin(\delta M_{mm'}^2 \frac{L}{2E}) \end{aligned}$$

Complex phases in  $U$  can lead to CP.

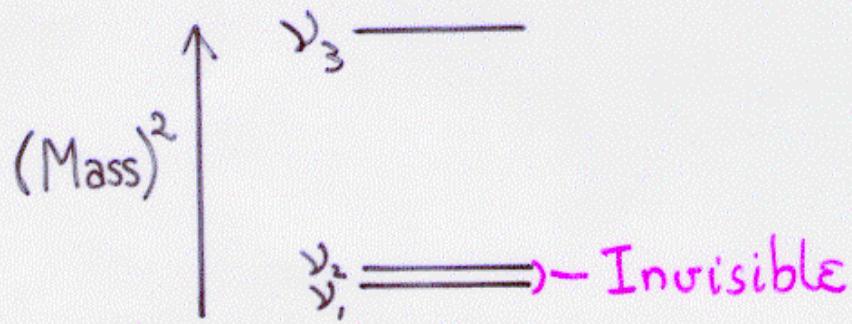
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# Oscillation involving only 2 neutrinos

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or effectively 2 neutrinos



depends only on the sizes of the  $U_{\ell m}$ .

Sizes  $|U_{\ell m}|$  can be determined this way.

Phases of combinations of  $U$  elements  
could be determined from the  $\mathcal{CP}$  asymmetries

$$\Delta_{\mathcal{CP}}(ll') \equiv P(\nu_e \rightarrow \nu_{e'}) - P(\bar{\nu}_e \rightarrow \bar{\nu}_{e'}).$$

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# Possible CP Phases in U

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Number of Neutrinos	Universal	Majorana ( $\bar{\nu}_m = \nu_m$ )
2	0	1
3	1	2
4	3	3

Why extra phases when  $\bar{\nu}_m = \nu_m$ ?

Because then

$$\text{Charge conjugate } (\bar{\nu}_m) \equiv \gamma_2 \nu_m^* = \nu_m,$$

so phases cannot be removed from U by phase-redefining  $\nu_m$ .

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$\mathcal{CP}$ Phases	Affect $\rightarrow$ Oscillation	Affect $\beta\beta_{0\nu}$
Universal	Yes	No
Majorana	No	Yes

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If there are only 3 neutrinos, then,  
 with  $P(\nu_e \rightarrow \nu_{e'}) - P(\bar{\nu}_e \rightarrow \bar{\nu}_{e'}) \equiv \Delta_{CP}(ll')$ ,

$$\begin{aligned}\Delta_{CP}(e\mu) &= \Delta_{CP}(\mu\tau) = \Delta_{CP}(\tau e) \\ &= 16 JS_{12}S_{23}S_{31},\end{aligned}$$

where

$$J \equiv \text{Im} (U_{e1} U_{e2}^* U_{\mu 1}^* U_{\mu 2}),$$

and

$$S_{mm'} \equiv \sin \left[ 1.27 \delta M_{mm'}^2 (\text{eV}^2) \frac{L (\text{km})}{E (\text{GeV})} \right].$$

Life is simple, but hard.

7) Authors who have discussed  $\beta\beta$ :  
Arafune & Sato; Bernabeu; Dick, Freund,  
Lindner, Romanino; Fisher, B.K., McFarland;  
Gago, Pleitez, Funchal; Schubert;  
Many Others.

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### What Can $\beta\beta_{0\nu}$ Teach Us?

From a measured  $\tau_{\beta\beta_{0\nu}}$  and a calculated nuclear matrix element, we would know

$$M_{\beta\beta} \equiv \sum_m M_m U_{em}^2$$

$M_{\beta\beta}$  is a different combination of neutrino masses than those measured in neutrino oscillation.

$M_{\beta\beta}$  could test mass spectra suggested by oscillation.

$|M_{\beta\beta}| \gtrsim 0.03 \text{ eV}$  would exclude:

- The 3-neutrino mass hierarchy
- The 4-neutrino spectrum with light  $\nu_e$

In the 4-neutrino spectrum with heavy  $\nu_e$ ,

$$|M_{\beta\beta}| = \sqrt{\delta M_{\text{LSND}}^2} \sqrt{1 - \sin^2 2\theta_0 \sin^2 \alpha_{\text{CP}}},$$

where

$\theta_0$  = the mixing angle for  $\nu_0$  oscillation,  
and

$\alpha_{\text{CP}}$  = a Majorana ~~CP~~ phase in U.

(Barger, Whisnant; Bilenky, Giunti, Grimus,  
B.K., Petcov; Klapdor-Kleingrothaus, Päs,  
Smirnov)

# What Are the Magnetic and Electric Dipole Moments of Neutrinos?

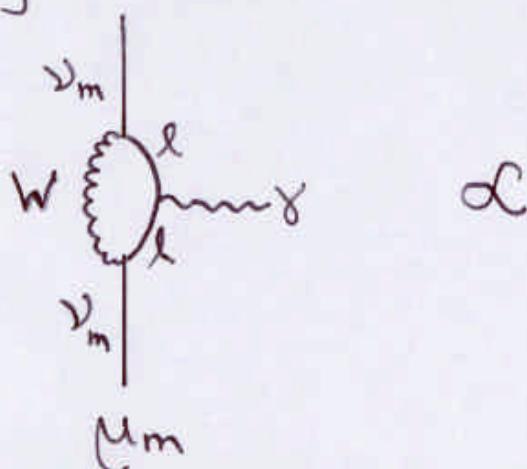
$$\text{Moment}[\bar{\nu}_m] \underset{\text{CPT}}{=} -\text{Moment}[\nu_m]$$

∴ If  $\bar{\nu}_m = \nu_m$ , Moment = 0.

Only Dirac neutrinos can have non-transition dipole moments.

Both Majorana and Dirac neutrinos can have transition moments.

In simple extensions of the Standard Model, neutrino magnetic dipole moments  $\mu_m$  are tiny because



$\mathcal{L}$



$$\mu_m = 3.2 \times 10^{-19} M_m(\text{eV}) \mu_{\text{Bohr}}$$

(Lee & Shrock; Fujikawa & Shrock)

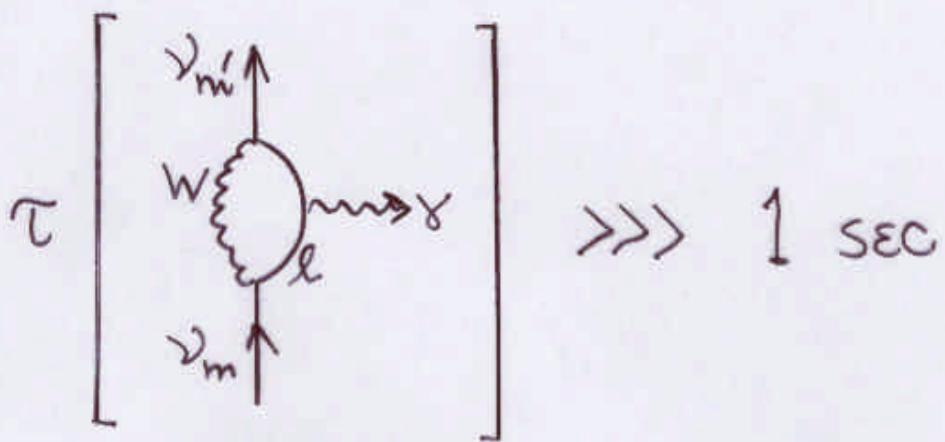
Electric dipole moments must violate CP too.

There are models with much bigger moments.

One can look for neutrino magnetic moment contributions to  $\nu$ -e scattering, using reactor neutrinos or solar neutrinos.

↑ Beacom & Vogel

# What Are the Neutrino Lifetimes?



Exotic decay modes may yield shorter lifetimes.  
 (Pakvasa; B.K. & Mohapatra)

If some neutrino  $\nu_m$  decays rapidly ( $\tau < 1 \text{ sec}$ ) then the atmospheric neutrino data, usually explained in terms of  $\nu_\mu \rightarrow \nu_\tau$  oscillation, can be equally well explained in terms of neutrino decay.

(Barger, Learned, Lipari, Lusignoli; Pakvasa, Weiler)

## Conclusion

We are just beginning to learn-

- How many neutrinos there are
- How much they weigh
- Their nature
- Their interactions

In neutrino physics, interesting years lie ahead.

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