## Fermi National Accelerator Laboratory

# CANVAS: C++ Objects for Easy Graphics on an Evans \& Sutherland PS390 Terminal. User's Guide 

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## 1 Introduction

The Evans and Sutherland PS390 terminal which resides in the X-Gallery HiBay area is a powerful, sophisticated graphics engine whose price/performance ratio approaches infinity because practically no one uses it. ${ }^{1}$ The reason for this lack of enthusiasm is obvious: no self-respecting scientist still of sound mind would willingly choose to read, much less assimilate, the seven-volume set of manuals that accompanies this device. The information buried in those volumes is, of course, essential for programming the PS390 to do all the sophisticated things it is capable of doing, such as creating automobiles with doors that open and close and steering wheels which move synchronously with the front tires, all at the turn of a knob. Regrettably, doing simple things, such as viewing three-dimensional magnetic fields, is no easier than doing the most complicated ones. ${ }^{2}$ There is at least one brand of third party software available for viewing data, but it requires specially formatted data files, it does not allow for data interaction, and as is usually the case with self-contained programs, it invariably does not do the one or two tasks needed for a given application. Another approach was used by Fermilab's Computing Division in writing a DI-3000 device driver for the PS390 terminal. This was a valid and useful project, but it must have been like trying to fit a square peg into a round hole. The PS390 is Phigs-like in its graphics protocols while DI-3000 is based on ACM Core, which was devised when graphics was viewed primarily as a means of drawing pictures rather than interacting with data.

The $\mathrm{C}-+$ classes described in this note comprise an attempt to provide an object-oriented approach, and if there was ever a graphics terminal naturally suited to object-oriented programming, the PS390 is it. Since a canvas is not a program but a variable to be used in programs, users can write software to suit their particular needs. By simply declaring canvas variables the application program is provided with an object which accepts data and displays it automatically. Any number of canvases can be placed anywhere on the screen, so data can be viewed in a variety of ways simultaneously. Further, the "real-time" transformation

[^0]capabilities of the PS390 are activated in one step by "connecting" its external devices, the dials and the puck, to the desired canvas. There is no need for the applications programmer to construct his own function networks, choose names for nodes, and do any of the other administrative tasks laid out in the manuals, including connecting the terminal to a host computer and initializing it. These are handled automatically by the canvases themselves, thus removing this clutter from the application program.

This User's Guide is arranged as follows. We offer in Section 2 four sample programs which illustrate the simplest usage of the canvas variables: canvas 3 d , canvas 2 d , and canvasRas. This is follwed by a description of (currently) available methods in Sections 3 and 4, the former dealing with object-orinted graphics and the latter with raster graphics. What will be described is a minimal, "bare bones" implementation which we hope will be useful to anyone who wants an easy way to explore three-dimensional data without frills. It is not our objective to attempt, single-handedly, to provide an Interviews package for the PS390. ${ }^{3}$ However, features will continue to be added slowly as needed, especially with regard to (a) locate, pick, and identify functions, (b) three-dimensional cursors, (c) ready-to-use graphics objects, such as beamLine or surface, (d) new types of derived canvases, such as stripChart, menu, or tuneDiagram, and (e) construction of a canvas4d class. For those who might want to use these variables and their methods libraries and documentation can be found in the area ALMOND: :USR\$DISK4: [MICHELOTT.PUBLIC.CANVAS].

## 2 Sample programs

The first two programs in this section were suggested by colleagues in Accelerator Division; the other 1wo had no motivation other than to illustrate the usage of canvas variables. Almost complete listings are provided, but for our purposes, it is certainly not necessary to understand all their details. We shall walk through the important highlights of each.

All of these sample programs are available to anyone who might want to play with them to see what they actually look like on the screen. Simply (i) walk up to the XGal Hi Bay Mezzanine and log into your ALMOND account using the PS390 terminal; (ii) browse through the demo names by doing
\$ DIR ALMOND::USR\$DISK4:[MICHELOTT.PUBLIC.CANVAS.DEMOS]*.DEMO;
and (iii) invoke a demo with

## \$ ©ALMOND : : USR\$DISK4:[MICHELOTT.PUBLIC.CANVAS.DEMOS]<name>.DEMO

where < name > is the name of one of the demos seen in Step (ii). Further, it is possible to make hardcopies of the PS390 display (with the exception of canvasRas images) by entering
\$ QALMOND: :USR\$DISK4:[MICHELOTT .PUBLIC.CANVAS]HARDCOPY
at VMS system level. A PostScript file named PS800.DAT will be written into your default directory.

### 2.1 Data from files

This first program merely reads three-dimensional data from a set of files and displays them in a canvas. ${ }^{4}$ Each file contained one-day temperature profiles at one of twenty-four stations around the ring. Each line

[^1]contained a (time, temperature, station) triplet, and it was desired to display these as twenty-four differentcolored curves. The names of all the data files were written into a separate file for program access.

We shall mark the important features of this program, flagged by their line numbers:
line 6: The canvas resource file, canvas.rsc, must be included before any canvas variables are declared and must have file scope, that is, it must be included outside of all "\{ ...\}" brackets (the most logical place being near the top of the file, as shown here). This header can be read from the area ALMOND : :USR $\backslash \$ D I S K 4:[M I C H E L O T T . P U B L I C . H E A D E R S]$.
line 11: A number of forms are available for declaring canvas variables. This one employs two characterstring arguments to instance pic, a three-dimensional canvas. The first argument specifies how graphics transformations are to be carried out; we shall put off its detailed explanation to Section 3.1. The second requests a parallel, rather than perspective, projection from the three-dimensional "world" of data into the screen; perspective projections are the default.
lines 13-20: This fragment of code serves the dual purpose of placing axes within the canvas and alerting it to the data ranges it can expect. Each data file contains a 24 hour temperature profile at one of the the 24 stations around the ring. We choose temperature to be the $z$-axis, while "hour" and "station" will be the other two. The array minmax indicate the minimum and maximum valses associated with each axis, while delta specifies the spacing between tic marks.
lines 22-25: Anticipating the desire to look at the data from various views, the PS390 dialbox is connected to the canvas's transformation "nodes." There are three basic data transformations which can be carried out: rotations, dilations, and translations. These statements will allow the first three dials to control rotations in three independent directions, the fourth, dilation (which is uniform in all three directions), and the last three, translations. Dial 5 is not connected to anything.
lines 8, 33: Names of the data files are contained in a separate file, whose name will appear in the command line invoking the program, as in

## \$ kissel namefile.dat

lines 37-54: These two while loops form the core of the program. The first reads the names of the data files, the second, the data. The temperature profiles are modelled as wireframes with the functions .startFrame (line 45), which initializes a wireframe, and .addToFrame (line 49), which continues it. Since transformations have already been connected, the dialbox can be used to manipulate the image as it is being draun.
line 53: It frequently happens at the end of a program that the last few data points sent to a canvas do not reach it because the Ethernet buffers have not been filled. The method .purgeBuff flushes these buffers and assures that all the data are displayed.
lines 58.61: Finally, we delay leaving the program. Upon exiting, canvas destructors are invoked, and they reset the PS390, destroying all the objects which have been created. Without the delay, this would happen before the user had a chance to examine his data. If it is desired to exit a program while leaving the objects intact - to make a hard copy of the screen, for example - then exit disgracefully with a ${ }^{-} \mathbf{Y}$.

## PROGRAM LISTING

```
#include <stddef.h> // These two statements sideline
```

\#include 〈errno.h〉 // annoying compiler warnings
// about PSECT ERRNO

```
#include <stdio.hxx>
```

\#include <stdio.hxx>
\#include "canvas.rsc"
\#include "canvas.rsc"
main ( int argNum, char *fileList[] ) {
main ( int argNum, char *fileList[] ) {
// Declaring the canvas variable ...............
// Declaring the canvas variable ...............
canvas3d pic ( "Oow", "orthographic");
canvas3d pic ( "Oow", "orthographic");
// Setting up the axis system ..................
// Setting up the axis system ..................
double delta[3];
double delta[3];
double minmax[6];
double minmax[6];
// _--- x _------ -.------ y ------
// _--- x _------ -.------ y ------
minmax[0] = 1.0. minmax[2] = 1.0i
minmax[0] = 1.0. minmax[2] = 1.0i
minmax[1] = 24.0; minmax[3] = 24.0; minmax[5] = 120.0;
minmax[1] = 24.0; minmax[3] = 24.0; minmax[5] = 120.0;
delta[0] = 1.0; delta[1] = 1.0; delta[2] = 10.0;
delta[0] = 1.0; delta[1] = 1.0; delta[2] = 10.0;
pic.makeAxes( minmax, delta);
pic.makeAxes( minmax, delta);
// Connect transformations to dials ............
// Connect transformations to dials ............
pic.connRot (1, 2, 3);
pic.connRot (1, 2, 3);
pic.connScale ( 4);
pic.connScale ( 4);
pic.connTrans (6, 7, 8 );
pic.connTrans (6, 7, 8 );
// Finally, read and display the data ..........
// Finally, read and display the data ..........
FILE *dataFile;
FILE *dataFile;
FILE *nameFile;
FILE *nameFile;
char nameOfDataFile[ 80 ];
char nameOfDataFile[ 80 ];
nameFile = fopen( fileList[1], "r");
nameFile = fopen( fileList[1], "r");
char firstPoint = 1;
char firstPoint = 1;
double time, temperature, station;
double time, temperature, station;
while ( fscanf( nameFile, "%s", nameOfDataFile ) != EOF ) {
while ( fscanf( nameFile, "%s", nameOfDataFile ) != EOF ) {
dataFile = fopen( nameDfDataFile, "r" );
dataFile = fopen( nameDfDataFile, "r" );
while ( fscanf(dataFile, "%le %le %le",
while ( fscanf(dataFile, "%le %le %le",
Etime, etemperature, estation
Etime, etemperature, estation
)
)
!= EOF
!= EOF
) {
) {
if ( firstPoint ) {
if ( firstPoint ) {
pic.startFrame( station, time, temperature );
pic.startFrame( station, time, temperature );
firstPoint = 0;
firstPoint = 0;
continue;
continue;
}
}
pic.addToFrame( station, time, temperature );
pic.addToFrame( station, time, temperature );
}

```
        }
```

```
    fclose( dataFile );
    firstPoint = 1;
    pic.purgeBuff();
    }
fclose( nameFile);
// Delaying program exit ..........................
char dummyString[ 80 ];
printf("\nPress RETURN to exit the program.\n");
gets( dummyString);
}
```


### 2.2 Eyeball curve-fitting

It frequently happens that one would like to fit to data from a parametrized family of curves, not by using automated (least squared error) methods but simply by looking at the curves and playing with the parameters until a decent fit is achieved at localized regions of interest. The program listed below enables this type of "exploratory data analysis." ${ }^{5}$
lines 16-17, 146-157: This program had an interesting problem associated with it. I wanted two twodimensional canvas variables with file scope on the screen simultaneously. However, the declarative forms employed (lines 151 and 156 ) could be used only from within a function. The solution was to declare pointers to canvases (lines 16 and 17) which are assigned values after the canvases are declared (lines 152 and 157 ). This illustrates strongly that a $C++$ class acts completely like the original variables of the language.

Locations of the canvases on the screen are specified by two arrays, $\boldsymbol{r t}$ and 2 b , which contain "normalized screen coordinates" - lying within $\pm 1-$ of the right-top and left-bottom corners. Thus the canvas it is to be centered vertically and occupy the left half of the screen, while resid will occupy the right half. (Compare lines 151 and 156 with line 11 of the preceding section.)
lines 159-165: After the canvases have been declared, translation nodes are connected to dials, as before. We are not interested in rotations for this application.
lines 172-176: The file containing $(x, y)$ coordinate pairs is read and the data stored in two arrays. Line 176 contains one of those multi-purpose statements that non- C programmers sometimes find confusing. It simultaneously (a) reads the data file, storing one pair at a time, (b) counts the number of pairs stored, and (c) terminates when the end of file is reached.
lines 178-211: Then comes a block of code which makes an initial estimate for the parameters of a gaussian model from the data's statistics. Since it is not of interest, in the context of this document, we have omitted it.
lines 213-224: As in the previous example, axes are established, one for each canvas. The vertical axis parameters are different for the two windows, since fit is to display the data themselves, while resid will contain the display of residuals from the gaussian model.

[^2]lines 227-240: Three objects are to be plotied in the two canvases: the scatterplot of $(x, y)$ coordinate pairs, the gaussian curve through those points, and the set of residuals. These are respectively given the tokens, already declared as char* variables in lines 13-15, of dataGraf, curve, and residuals. datagraf is plotted using the methods .startPts, to initialize, and .addToPts, to complete the display (lines 228-229). The methods .startFrame and .addToFrame implement the display of curve and residuals as wireframes. The colors are chosen from a template made available by canvas.rsc: BLUE, MAGENTA, RED, YELLOM, GREEN and CYAN. Other colors can be obtained by linear interpolation, as in " $0.3 *$ RED $+0.7 *$ YELLOW." The loop beginning at line 235 finishes the wireframes. Note that in addition to addToFrame, the plot of residuals makes use of a method joinToFrame (line 237). This enables residuals to be constructed from disconnected pieces, while curve is a completely connected wireframe.
lines 8, 242-249: The $C++$ class $t$ tMenu was written some time ago and is convenient for writing programs with interactive steps. Its usage should be obvious from the context.
lines 64-141: The functions absChange (lines 64ff) and relChange (lines 103ff) simply allow the user to alter the parameters of the gaussian either directly or by choosing multipliers or summands. The details are not of interest, except for lines 98 and 138: after changes are made, the two objects curve and residuals are redrawn...
lines 49-62: ... using the function reDraw (). After the old versions are erased from the canvases using .remove ( lines $51-52$ ), the new ones are put in their places: lines $53-61$ almost exactly duplicate lines $232-241$, in which these objects were originally drawn. The principal difference is that reDraw uses the pointers fitPtr and residPtr to refer to canvases.
lines 22-41: This block of code simply contains the gaussian function which is to be used as the family of curves for the fitting. The user will be able to manipulate four parameters (lines $27-30$ ) in order to achieve a "good" fit.

## PROGRAM LISTING

```
#include <stddef.h>
#include <errno.h>
#include <stdio.hxx>
#include <stream.hxx>
#include <math.hxx>
#include "canvas.rsc"
#include "[michelott.cpp.headers]menu.hxx"
#define MaxDATA 256
const double twoPi = 6.2831853072;
char* dataGraf;
char* curve;
char* residuals;
canvas2d* fitPtr;
canvas2d* residPtr;
double x[MAXDATA], y[MAXDATA];
int num;
```

```
// *****************************
```

// *****************************
//
//
// Gaussian distribution to be used in fitting
// Gaussian distribution to be used in fitting
//
//
double gsAverage = 0.0;
double gsAverage = 0.0;
double gsSigma = 1.0;
double gsSigma = 1.0;
double gsNormalization = 1.0;
double gsNormalization = 1.0;
double gsPlatform =0.0;
double gsPlatform =0.0;
double gaussian ( double u ) {
double gaussian ( double u ) {
double w;
double w;
double arg;
double arg;
arg = ( u - gsAverage ) / gsSigma;
arg = ( u - gsAverage ) / gsSigma;
arg = - 0.5 * arg * arg;
arg = - 0.5 * arg * arg;
w = exp( arg ) / ( sqrt( twoPi ) * gsSigma );
w = exp( arg ) / ( sqrt( twoPi ) * gsSigma );
w *= gsNormalization;
w *= gsNormalization;
w += gsPlatform;
w += gsPlatform;
return w;
return w;
}
}
// **************
// **************
//
//
// Manipulation routines in mainMenu
// Manipulation routines in mainMenu
//
//
void reDraw() {
void reDraw() {
int i;
int i;
fitPtr -> remove( curve );
fitPtr -> remove( curve );
residPtr -> remove( residuals );
residPtr -> remove( residuals );
curve = fitPtr > startFrame( x[0], gaussian( x[0] ), RED );
curve = fitPtr > startFrame( x[0], gaussian( x[0] ), RED );
residuals = residPtr > startFrame( x[0], 0.0, YELLOW);
residuals = residPtr > startFrame( x[0], 0.0, YELLOW);
residPtr -> addToFrame( x[0], y[0] - gaussian( x[0] ) );
residPtr -> addToFrame( x[0], y[0] - gaussian( x[0] ) );
for ( i = 1; i < num; i++ ) {
for ( i = 1; i < num; i++ ) {
fitPtr -> addToFrame ( x[i], gaussian( x[i] ) );
fitPtr -> addToFrame ( x[i], gaussian( x[i] ) );
residPtr -> joinToFrame ( x[i], 0.0 );
residPtr -> joinToFrame ( x[i], 0.0 );
residPtr -> addToFrame ( x[i], y[i] - gaussian( x[i] ) );
residPtr -> addToFrame ( x[i], y[i] - gaussian( x[i] ) );
}
}
fitPtr->purgeBuff();
fitPtr->purgeBuff();
}
}
void absChange() {
void absChange() {
int choice;
int choice;
double value;

```
double value;
```

```
6 8
.......<<<< Lines 69-93 omitted >>> ..........
94 default:
95 break;
96 }
97
98
99
100
101
102
103 void relChange() {
104 int choice;
....... <<< Lines 105-136 omitted >>> ..........
137
138 reDraw();
139 goto start;
140
141 }
142
143
144
145
146 // Declaring the canvas variables ................
147 double rt[2], lb[2];
148 // --------x ----.-------------
149 lb[0] = -1.0; lb[1] = - 0.5;
150 rt[0] = 0.0; rt[1] = 0.5;
151 canvas2d fit (rt, lb, "WWW" );
152 fitPtr = efit;
153
154
155
156
157
158
159 // Connect transformations to dials ............
160 resid.connScale ( 1, "Scale");
161
162
163
164
165
}
    resid.connTrans ( 2, 'Horiz'',
                    3, "Vert" );
    fit.connScale ( 5, "Dilation");
    fit.connTrans ( 6, "Horiz",
                                7, "Vert" );
```

```
166
167 // Reading data from the file .....
168
169 FILE* xyFile;
170
1 7 1
172
173
174
175
176 while( fscanf( xyFile, "%lf %lf", x + num, y + num) != EOF ) num++;
177
178 // Find data scales
179 double xmin = x[0];
180 double xmax = x[0];
........<<< Lines 181-209 omitted >>> ..........
212
213
214
215
216
21
218
219
220
221
222
223
224
225
226
227
228
230
231
232
233
234
235
236
237
238
```

```
210 gsSigma = sigma;
```

210 gsSigma = sigma;
211 gsNormalization = sqrt( twoPi ) * sigma * ( ymax - ymin );
211 gsNormalization = sqrt( twoPi ) * sigma * ( ymax - ymin );
229 for ( i = 1; i < num; i++ ) fit.addToPts( x[i], y[i] );
229 for ( i = 1; i < num; i++ ) fit.addToPts( x[i], y[i] );

```
    // Setting up the axis system ..................
```

    // Setting up the axis system ..................
    double delta[2], minmax[4];
    double delta[2], minmax[4];
    // _------------- x _--.-.-...-----y
    // _------------- x _--.-.-...-----y
    minmax[0] = xmin; minmax[2] = ymin;
    minmax[0] = xmin; minmax[2] = ymin;
    minmax[1] = xmax; minmax[3] = ymax;
    minmax[1] = xmax; minmax[3] = ymax;
    delta[0] = delta[1] = 1.0;
    delta[0] = delta[1] = 1.0;
    fit.makeAxes( minmax, delta);
    fit.makeAxes( minmax, delta);
                minmax[2] = - 1.5;
                minmax[2] = - 1.5;
                minmax[3] = 1.5;
                minmax[3] = 1.5;
                        delta[1] = 0.25;
                        delta[1] = 0.25;
    resid.makeAxes( minmax, delta );
    resid.makeAxes( minmax, delta );
    // Plotting the data
    // Plotting the data
    dataGraf = fit.startPts( x[0], y[0], YELLOW );
    dataGraf = fit.startPts( x[0], y[0], YELLOW );
    // Plot the initial curve
    // Plot the initial curve
    curve = fit.startFrame( x[0], gaussian( x[0] ), RED );
    curve = fit.startFrame( x[0], gaussian( x[0] ), RED );
    residuals = resid.startFrame( }x[0],0.0, YELLOW )
    residuals = resid.startFrame( }x[0],0.0, YELLOW )
            xesid.addToFrame( x[0], y[0] - gaussian( x[0] ) );
            xesid.addToFrame( x[0], y[0] - gaussian( x[0] ) );
    for ( i = 1; i < num; i++ ) {
    for ( i = 1; i < num; i++ ) {
        fit.addToFrame (x[i], gaussian( x[i] ) );
        fit.addToFrame (x[i], gaussian( x[i] ) );
        resid.joinToFrame (x[i], 0.0 );
        resid.joinToFrame (x[i], 0.0 );
        resid.addToFrame (x[i], y[i] - gaussian( x[i] ) );
    ```
        resid.addToFrame (x[i], y[i] - gaussian( x[i] ) );
```

```
239 }
240 fit.purgeBuff();
241
243
244
245
248
249
250
251
```

```
242 // Activate the menu .....
```

242 // Activate the menu .....
246 mainMenu.setItem( "Absolute change of parameters.", absChange);
246 mainMenu.setItem( "Absolute change of parameters.", absChange);
247 mainMenu.setItem( "Relative change of parameters.", relChange);
247 mainMenu.setItem( "Relative change of parameters.", relChange);

```
ttMenu mainMenu;
```

ttMenu mainMenu;
mainMenu.setPrompt( "PLAYFIT ..> ");
mainMenu.setPrompt( "PLAYFIT ..> ");
mainMenu.go();
mainMenu.go();
}

```
}
```


### 2.3 Fields

In addition to wire frames and clusters, canvases recognize vector fields as representable objects. The program below samples an electric dipole field at random points.
lines 23-38: A canvas variable is declared and customized more or less as in Section 2.1 except that "orthographic" view is not requested, which means the display will be in perspective.
lines 45-52: The method .startVF initializes the vector field display. In the loop, get FieldatPoint chooses a point randomly and calculates the field at that point. These are loaded respectively into the arrays $x$ and E. Then, .addToVF (line 51) incorporates these new samples into the diagram as they are calculated.

## PROGRAM LISTING

```
#include <stddef.h>
#include <errno.h>
#include <stdio.hxx>
#include <math.hxx>
#include "canvas.rsc"
extern double ran0( int* );
    double x[3], a[3], b[3], E[3];
    int j;
    int ranSeed = -9;
    void getFieldAtPoint();
    inline void getNextPoint() {
        for( int k = 0; k < 3; k++ ) x[k] = - 8.0 + 16.0 * (ran0( EranSeed ) );
    }
main() {
const int samples = 2500;
int i;
```

57 printf("\nPress RETURN to exit the program.\n");
5

### 2.4 Fractals

A third flavor of canvas available for immediate use is canvasRas, a two-dimensional canvas designed for pixel operations: specifically, for scanning a region in $R^{2}$ and coloring pixels according to a user-specified algorithm. This is a useful technique for creating contour plots and is indispensable if one wants to become rich and famous, especially rich, by publishing fractal images. ${ }^{6}$ The program shown below mixes a canvas 3d, in which is plotted the Lorenz attractor, with three canvasRas variables, in which are displayed various portions of the Mandelbrot set.
lines 9-10: The external function lorenz propagates an orbit obeying Lorenz's differential equation, while mandelbrot determines the RGB color code of points in $C \simeq R^{2}$ based on the number of iterates of the complex function $f(z)=z^{2}+c$ which "survive." We need not concern ourselves with their details here.
line 22: The last component of positioning arrays rtf and $\mathbf{l b b}$, which appear in instancing the threedimensional canvas lorenzCnv, specify positions for the forward and backward clipping planes. These are used in conjunction with depth cueing on the PS390: points which are "farther away" from the observer are made to appear dimmer. The first two components locate the canvas on the screen, as in lines 151 and 156 of Section 2.2.
lines 40-50: An orbit of the Lorenz equation is modelled as a wire frame beginning at the point (0,1,0). Over five thousand time steps are taken. Since the transformation nodes have been connected prior to this, in lines $35-38$, the user can manipulate the attractor while it is being constructed.
lines 81-87: Three regions of the Mandelbrot set will be displayed in raster canvases, whose declarations include arguments rt and Ib indicating where they are to be placed on the screen, exactly as with canvas 2 d and canvas3d variables. The .set $X$ and .set $Y$ functions then determine the domain in $R^{2}$ to be associated with each one, after which .scan tells the canvas to scan its domain using the RGB color-coding function named in the argument, mandelbrot.

## PROGRAM LISTING

\#include <stddef.h>
\#include <errno.h>
\#include <complex.hxx>
\#include "canvas.rsc"
// Declaring functions which generate Lorenz's attractor
// and the Mandelbrot set....................................
extern void lorenz ( double*, double*, double*);
extern void mandelbrot ( double*, double*, int*, int*, int*);
main() \{
// ++++++++++++++++++++++++++++++++++++++++++++++++++++++++
// Work begins here on the Lorenz attractor
16
${ }^{6}$ I am told that the current rate for a single fractal "project" in the advertising industry is about $\$ 150,000$. At least, this is the price charged by a fractal pioneer who has left academia to devote himself full-time to these worthwhile pursuits.
18
19
20
2 1
22
23
24
25
26

```
```

17 // Declaring the canvas variable ................

```
```

17 // Declaring the canvas variable ................

```
double rtf[3], lbb[3];
```

```
double rtf[3], lbb[3];
```




```
lbb[0] = -1.0; lbb[1] = -0.6; lbb[2] = -1.0;
```

lbb[0] = -1.0; lbb[1] = -0.6; lbb[2] = -1.0;
rtf[0] = 0.6; rtf[1] = 1.0; rtf[2] = 1.0;
rtf[0] = 0.6; rtf[1] = 1.0; rtf[2] = 1.0;
canvas3d lorenzCnv( rtf, lbb, "OwO");
canvas3d lorenzCnv( rtf, lbb, "OwO");
// Setting up the axis system
// Setting up the axis system
double deIta[3];
double deIta[3];
double minnax[6];
double minnax[6];
// --.-. x ---------y --------z
// --.-. x ---------y --------z
minmax[0] = minmax[2] = minmax[4] = - 50.0;
minmax[0] = minmax[2] = minmax[4] = - 50.0;
minmax[1] = minmax[3] = minmax[5] = 50.0;
minmax[1] = minmax[3] = minmax[5] = 50.0;
delta[0] = delta[1] = delta[2] = 5.0;
delta[0] = delta[1] = delta[2] = 5.0;
lorenzCnv.maxeAxes( minmax, delta, YELLOH );
lorenzCnv.maxeAxes( minmax, delta, YELLOH );
// Connect transformations to dials ............
// Connect transformations to dials ............
lorenzCnv.connRot ( 1, 2, 3);
lorenzCnv.connRot ( 1, 2, 3);
lorenzCnv.connScale ( 4 );
lorenzCnv.connScale ( 4 );
lorenzCnv.connTrans ( 5, 6, 7 );
lorenzCnv.connTrans ( 5, 6, 7 );
lorenzCnv.connFrom ( 8);
lorenzCnv.connFrom ( 8);
// Set initial conditions and launch the orbit .....
// Set initial conditions and launch the orbit .....
double x = 0.0;
double x = 0.0;
double y = 1.0;
double y = 1.0;
double z = 0.0;
double z = 0.0;
char* attractor;
char* attractor;
attractor = lorenzCnv.startFrame( x, y, z, RED );
attractor = lorenzCnv.startFrame( x, y, z, RED );
for ( int timeSteps = 0; timeSteps < 5500; timeSteps++ ) {
for ( int timeSteps = 0; timeSteps < 5500; timeSteps++ ) {
lorenz( \&x, \&y, zz );
lorenz( \&x, \&y, zz );
lorenzCnv.addToFrame( x, y, z );
lorenzCnv.addToFrame( x, y, z );
}
}
// ++++++++++++++++++++++++++++++++++++++++++++++++++++++++
// ++++++++++++++++++++++++++++++++++++++++++++++++++++++++
// Work begins here on the Mandelbrot sets
// Work begins here on the Mandelbrot sets
// Declare five raster canvases in which we shall scan
// Declare five raster canvases in which we shall scan
// various pieces of the Mandelbrot set.
// various pieces of the Mandelbrot set.
double rt[3][2];
double rt[3][2];
double lb[3][2];
double lb[3][2];
// _--.-----------x
// _--.-----------x
1b[0][0] = 0.6; 1b[0][1] = - 0.2;
1b[0][0] = 0.6; 1b[0][1] = - 0.2;
rt[0][0] = 1.0; rt[0][1] = 0.2;
rt[0][0] = 1.0; rt[0][1] = 0.2;
// -------------..- --------------------

```
// -------------..- --------------------
```

```
lb[1][0] = 0.6; lb[1][1] = - 1.0;
rt[1][0] = 1.0; rt[1][1] = - 0.6;
// --------------- ----.-.-------------
lb[2][0] = - 0.2; 1b[2][1] = - 1.0;
rt[2][0] = 0.2; rt[2][1] = - 0.6;
double xLo[3], xHi[3], yLo[3], yHi[3];
xLo[0] = -1.7935; xHi[0] = -1.7365;
yLo[0] = -0.0285; yHi[0] = 0.0285;
// --------------- -----------------------
xLo[1] = -0.96; }\quad\textrm{xHi[1] = -0.89;
yLo[1] = 0.23; }\quad\textrm{yHi[1]}=0.30
// --------------- ----------------------
xLo[2] = -0.94; }xHi[2] = -0.89; 
yLo[2] = 0.24; yHi[2] = 0.29;
// --.--.---------- ---...---------------
canvasRas* mandelCnv;
for ( int i = 0; i < 3 i++ ) {
    mandelCnv = new canvasRas( &(rt[i][0] ), &(lb[i][0] ) );
    mandelCnv }->\mathrm{ setX( xL.o[i], xHi[i] );
    mandelCnv -> sety( yLo[i], yHi[i] );
    mandelCnv -> scan( mandelbrot );
    }
// Delaying program exit
char dummyString[80 ];
printf("\nPress RETURN to exit the program.\n");
gets( dummyString);
}
```


## 3 Object-oriented graphics

In order to reduce the amount of space needed to list methods available to canvas variables, we have adopted a limited form for indicating options. Using this notation the line,

means that the method .mth is available both to class $A$ and to classB using one of the following argument lists:

```
( double x[3], char* z ),
( double x[3], int* y, char* }z\mathrm{ , double t), or
( double x[3], int* y, char* z, double t, int w).
```

However, ( double $x[3]$, int* $y$, char* $z$ ) would not be allowed: unless otherwise indicated, all options at the same depth go together.

### 3.1 Declarations

canvas3d::canvas3d ([char* m [, char* v ] ])
::canvas3d (double rtf[3], double lbb[3], char* m [, char* $v$ ])
canvas2d::canvas2d ( [ [ double rt[2], double lb[2], ] char* m ])

Canvas constructors are overloaded to provide various options for initializing the graphics display environment. The argument (char* m) requires some explanation. Three types of "real-time," interactive transformations are incorporated into canvases: rotations, dilations, and translations. ${ }^{7}$ The argument $m$ is a three-character string (excluding the terminating null character) which specifies the mode in which these transformations are to be carried out. For instance, rotations are carried out relative to three independent directions. If the first character in $m$ is ' $W$ ', this means that these directions are to remain fixed in space (or, in graphics terminology, in the "world"); if it is ' $O$ ' then the rotation axes remain fixed relative to the objects being rotated. In the latter case, dials connected to the rotation node of a canvas (via one of the .connRot methods discussed below) will act like yaw, pitch, and roll controls. If ' $W$ ' is specified, however, the axes of rotation will remain fixed "in space" regardless of the orientation of the objects.

A similar criterion is set up with regard to translations, which also require specification of three axes, using the third character in $m$. The middle character controls the dilation, or "scaling," operation: if ' $O$ ' is chosen, then the invariant point of the dilations remains fixed in the object; if ' $W$ ', in the world.

The argument char* $v$, if present, gives the user the option of specifying an orthographic view, rather than a perspective one: Any string not beginning with the character ' $p$ ' - such as $v=$ "orthographic" -- will select the orthographic view. This will perform parallel projection of three-dimensional data onto the screen.

If more than one canvas is declared, the arrays $\mathbf{r t}, \mathbf{l b}, \mathbf{r t f}$, and $\mathbf{l b b}$ indicate the size and position of each on the screen. The two components of $\mathbf{r t}$ and $\mathbf{l b}$ contain the relative screen coordinates of the right-top and left-bottom vertices of the canvas. Relative screen coordinates are always in the range $\pm 1$ in each direction: they indicate position as though the screen were mapped onto $\{(\boldsymbol{x}, y)||\boldsymbol{x}| \leq 1,|\boldsymbol{y}| \leq 1\}$. For example, using $\mathrm{rt}=(1,1)$ and $\mathrm{lb}=(0,0)$ will put the viewport in the upper right hand portion of the screen. If a rectangular viewport is requested, the one actually constructed will enclose the largest square that fits into this rectangle, with top right vertices matching. The three-dimensional arrays $\mathbf{r t f}$ and $\mathbf{l b b}$ are similar; their third argument indicates "depth," and sets the positions of the forward and backward clipping planes, which determine depth cueing.

Default declarations use no arguments. A canvas constructor assumes that the declared canvas will be the only one on the screen and give it maximum size. Data will appear in perspective, and depth cueing will be activated with forward and backward clipping planes set at $\pm 1$,

[^3]```
3.2 Transformations
void canvas3d::connRot (int dialX, [ char* labelX,]
                int dialY, [ char* labelY,]
    int dialZ [, char* labelZ ])
    ::connTrans (int dialX, [ char* labelX,]
        int dialY, [ char* labelY,]
        int dialZ [, char* labelZ ])
    ::connFrom (int dial [, char* label])
void canvas2d::connRot (int dial [, char* label])
    ::connTrans (int dialX, [ char* labelX,]
        int dialY [, char* labelY ])
void { canvas3d | canvas2d }::connScale( int dial [, char* label ])
```

These functions connect the transformation nodes of a canvas to the PS390's dial box so that they can be carried out interactively by turning knobs. As their names suggest, .connRot and .connTrans connect dials to a canvas's rotation and translation nodes respectively, and connScale connects a dial to dilation. The integer arguments determine the dials associated with " $x$," " $y$," and " $z$ " rotations -. or just " $z$ " rotations, in the two-dimensional case - and must lie between 1 and 8 , inclusively; the string arguments determine the labels, limited to eight characters, which will appear in the LED displays above the associated dials. If labels are not specified, defaults will be used. An input dial integer less than 1 or larger than 8 will result in no transformation capability about the axis for which the dial number was intended. This is actually useful when it is desired to select fewer than all three axes for either rotations or translations.
.connScale requires only one integer argument for selecting the dial number to be used for dilation, as the transformation is carried out uniformly in all three dimensions. It is important to remember that the origin used for the scaling tranformation is determined by the mode argument, char* $m$, used when declaring a variable of type canvas3d.

The .connFrom method, available only to canvas3d variables, allow the user to "move through" the data by changing the point of observation. Any rotation of the selected dial will result in the simulated movement of the user along the line connecting the original viewing position and the world axis system origin. If the viewing position is moved beyond the origin (the center of the display region), the data will apear to flip from front to back. ${ }^{8}$

### 3.3 Building displayable objects

char* canvas3d::startFrame (double $x$, double $y$, double $z$ [, double $c$ ]) ::startPts (double $x$, double $y$, double $z$ [, double $c]$ ) ::startVF ([ double $s$, ] double $p[3]$, double $v[3][$, double $c$ ])
void canvas3d ::addToFrame ( [ char* $n$, ] double $x$, double $y$, double $z$ ) ::joinToFrame ( $\left[\right.$ char $^{*} \mathbf{n}$, ] double $x$, double $y$, double $z$ ) ::addToPts ([ char* $n$, ] double $x$, double $y$, double $z$ )

[^4]```
    ::addToVF ([ char* n,] double p[3], double v[3])
char* canvas2d::startFrame ( double x, double y [, double c])
    ::startPts (double x, double y [, double c ])
    ::startVF ([ double s,] double p[2], double v[2] [, double c ])
void canvas2d ::addToFrame ( [char* n,] double x, double y )
    ::joinToFrame ( [ char* n,] double x, double y )
    ::addToPts ([ char* n,] double x, double y )
    ::addToVF ([ char* n,] double p[2], double v[2])
void { canvas3d | canvas2d }::makeAxes(double m[6], double d[3] [, double c ] )
```

At the time of writing, canvases support displayable objects modelled as wireframes, point sets, vector fields, or axes. Displaying data as clusters of points is accomplished through the functions .startPts and .addToPts. The first initializes the object, and the second adds members to it. .startFrame, addToFrame, and ,joinToFrame perform similar offices for wireframes. .addToFrame assumes the point given is to be attached to the frame via an edge; join ToFrame makes the edge invisible: it "lifts the pen," as it were, before moving to the new point. Thus, a wire frame need not appear connected.

The .startXXX methods return a string which is the internal name of the object being created. One application of this, the removal of an object from a canvas, was illustrated in line 51 of the Section 2.2 listing. Another is given in the methods above: Normally, after an object is started, calls are made to .addToXXX methods in order to continue its construction, as done in lines 231-239 of Section 2.2. If that process is interrupted, and another object is started, we can still return to the original one by inserting ( the token containing) the value returned by a .startXXX function as the char* $n$ argument. This is illustrated in the fragment below.

```
canvas3d zlorfik;
char* firstThing;
char* secondThing;
double }x,y,z
firstThing = zlorfik.startFrame( 0., 0., 0. );
secondThing = zlorfik.startFramo( 1., 1., 1. );
zlorfik.addToFrame( }x,y,z);// This refers automatically t
// the most recently started frame
zlorfik.addToFrame( firstThing, x, y, z );
zlorfik.joinToFrame( secondThing, 2.0*x, 2.0*y, 2.0*z );
```

Axes, built by the .makeAxes functions, are useful for orienting the observer with respect to data. The two required arguments are arrays which provide the ranges associated with each axis (double* m) and the spacing between tic marks (double* d). Their usage was illustrated in all Section 2, for example in lines 16-19 of Section 2.1. Of course, the last (two) components of double* d (double* m ) is (are) ignored by, and therefore not necessary for, canvas 2 d variables.

The optional argument double s that appears in the vector field function .startVF is a multiplicative
"scale factor" for the vectors which serves to relate the units of the vector field to those of the underlying space. Its absence is equivalent to setting $s=1$.

The argument double c refers to color. BLUE, MAGENTA, RED, YELLOW, GREEN and CYAN are automatically available as defined tokens, and can be inserted into this slot. Other hues can be obtained through interpolation, as in "0.1*GREEN + 0.9*YELLOW."

### 3.4 Miscellany

void canvas3d::setRange ( double xMin, double $x$ Max, double yMin, double yMax, double zMin, double zMax ) void canvas2d::setRange( double $x$ Min, double $x$ Max, double yMin, double yMax )
void \{ canvas3d | canvas2d \}::setRange( double m[b]) ::include (char* $n$ )
::remove( char* $n$ )
void canvas3d::connAnimate( char $g$, int $s$ )
void canvas2d::connAnimate( int s)

Besides arranging the configuration of the axes, the .makeAxes methods listed in Section 3.3 alert the canvas to the range of values it can expect. If necessary, the canvas then scales data so that all directions visually look as though they had comparable dynamic ranges. The .setRange methods provide a way of doing this without drawing axes. The argument double* $m$ is exactly the same as in Section 3.3; as before, the last two components are not needed for canvas $2 d$ variables.

After an object is created in one canvas, it can be displayed in other canvases by using the include function. Conversely, remove will remove objects from canvases, as was done in lines 51-52 of Section 2.2.
.connAnimate allows the user to activate an animated rotation about an axis of choice, determined by the argument char $g$, which should take on the values ' $x$ ', ' $y$ ', or ' $z$ '. The other argument, int $s$, controls the rotation speed: a value of 1 causes the animation to operate at a speed of about 60 degrees per second, which is the fastest available; any other value will produce a slower rotation. The animation is begun by placing the locator puck on the tablet and pressing its green button, and it is stopped by pressing the red one.

## 4 Raster Graphics

The class canvasRas, unlike its cousins, canvas 2 d and canvas 3 d , is designed for pixel operations. Specifically, it can be used to generate color-coded contour maps of functions over $R^{2}$. As was demonstrated in Section 2.4, the user specifies an arbitrarily named function

```
void func( double* x, double* y, double* r, double* g, double* b )
```

which accepts an ( $x, y$ ) coordinate pair as input and produces its red-green-blue color code as output. The values must all satisfy $0 \leq * r, * g, * b<255$. Pixel operations are not updated, so canvasRas variables should not overlap anything else appearing on the screen, including the VAX-produced messages displayed in the terminal emulator plane and the cursor.

### 4.1 Declarations

canvasRas::canvasRas([ double rt[2], double lb[2] ])

Instancing a canvasRas variable with arguments determines its position on the screen. (For example, see line 83 on page 14.) As before, It and lb contain normalized screen coordinates, lying between $\pm 1$. If the default option (no arguments) is used, then the canvas will fill the entire available area, which means that it should be the only canvas in the program.

### 4.2 Scanning the function

```
canvasRas::set X( double lo, double hi )
    ::setY(double lo, double hi )
    ::scan( RASTER_FUNC scanFunction )
```

The desired image is rendered on the screen by setting a domain in $R^{2}$ and then invoking scan. The methods .set $X$ and .set $Y$ determine the region to be scanned. Invoking .scan starts the actual data processing. The argument scanfunction is the name of the user-defined function described above. Usage was exemplified in lines 10 and 86 of Sec.2.4.

### 4.3 Miscellany

canvasRas::erase()
::fullErase()

Invoking the .erase method will clear a single raster canvas; invoking fullErase will clear all raster canvases on the screen.


[^0]:    ${ }^{1}$ An excellent Macintosh commercial was developed along these lines. Two executives are discussing how to evaluate hardware performance. One suggests that the answer lies in counting "megaflops or megahertz something like that." The other counters that an easier way is to observe which computer people use most frequently. When the first objects that the criterion is not fair because people like to use a Macintosh he receives a withering look, suggestive of severe reductions in prospects for future promotion.
    ${ }^{2}$ Perhaps this is just the negative way of saying that complicated graphics is no harder than simple graphics.

[^1]:    ${ }^{3}$ Incidentally, the fact that our class has the same name as that used by SUN graphics is purely a coincidence and is not meant to suggest any correspondence.
    ${ }^{4}$ The program in this section was suggested by Walter Kissel.

[^2]:    ${ }^{5}$ The program in this section was suggested by Crajg Moore.

[^3]:    'There is actually one more, but we'll save it for later.

[^4]:    ${ }^{8}$ This is a flaw which will be repaired eventually.

