# Discovering Strong Gravitational Lenses in the Dark Energy Survey with Interactive Machine Learning and Crowd-sourced Inspection with Space Warps

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#### ABSTRACT

We conduct a search for strong gravitational lenses in the Dark Energy Survey (DES) Year 6 imaging data. We implement a pre-trained Vision Transformer (ViT) for our machine learning (ML) architecture and adopt Interactive Machine Learning to construct a training sample with multiple classes to address common types of false positives. Our ML model reduces ~236 million DES cutout images to 22,564 targets of interest, including ~85% of previously reported galaxy-galaxy lens candidates discovered in DES. These targets were visually inspected by citizen scientists, who ruled out ~90% as false positives. Of the remaining 2,618 candidates, 149 were expert-classified as 'definite' lenses and 516 as 'probable' lenses, with 147 of these candidates being newly identified. Additionally, we trained a second ViT to find double-source plane lens systems, finding at least one double-source system. Our main ViT excels at identifying galaxy-galaxy lenses, consistently assigning high scores to candidates. This selection is an order of magnitude higher in purity than previous convolutional neural network-based lens searches and demonstrates the feasibility of applying our methodology for discovering large samples of lenses in future surveys.

Keywords: Gravitational lensing: strong - methods: machine learning

1. INTRODUCTION

Gravitational lensing occurs when an astronomical source is located behind a massive foreground object such as a galaxy, galaxy group, or cluster of galaxies. If the source is sufficiently close to the line of sight between the observer and the lensing object, its light can be deflected by the gravitational potential of the foreground object, producing multiple magnified images of the source. If the source is a galaxy these images appear as extended arcs, whereas if the source is intrinsically small, such as a quasar, we see multiple magnified point source images.

In galaxy-scale strong gravitational lenses, systems in which the deflector is a single galaxy, the observables are primarily sensitive to the mass distribution of the lensing galaxy. Most massive galaxies in the universe are elliptical galaxies, so strong lensing can be utilized to study the structure (baryonic and dark matter profiles) and evolution of these galaxies (Shajib et al. 2024). Strong gravitational lensing is also sensitive to the underlying cosmological parameters of our Universe (Pascale et al. 2024; Kelly et al. 2023; Birrer et al. 2020; Shajib et al. 2020a; Wong et al. 2019). A population of ~10,000 galaxy-galaxy gravitational lenses can provide competitive constraints on the dark energy equation of state parameters (Li et al. 2023). Strong gravitational lenses with two sources at different redshifts (doublesource plane lenses, hereafter DSPLs) are particularly useful for cosmology (Linder 2016; Collett et al. 2012) since the ratio of Einstein radii is only mildly sensitive to the mass profile of the deflector, the dominant systematic in strong lensing analyses. With only one system Collett & Auger (2014) improved the equation of state of dark energy w from Planck by 30%.

The initial discoveries of strong gravitational lenses were mostly serendipitous (e.g., Walsh et al. (1979)). The first dedicated searches for strong lenses involved manually inspecting large numbers of images from smallarea surveys applying modest selection criteria, resulting in the identification of hundreds of lenses (e.g., More et al. (2011); Newton et al. (2009); Faure et al. (2008); Jackson (2008); Moustakas et al. (2007); Fassnacht et al. (2006, 2004)). However, this method is impractical for wide-field surveys, necessitating the development of automated detection techniques. Early automated methods primarily targeted lenses with multiple wellseparated images or distinctive elongated and curved arcs (e.g., Gavazzi et al. (2014); More et al. (2012); Alard (2006)). Since then, additional automated search techniques have been developed. For instance, algorithms such as 'Blue Near Anything' and 'Red Near Anything' focus on identifying strong lensing systems with lensed sources of the corresponding color (O'Donnell et al. 2022; Diehl et al. 2017). While these automatic techniques have proven effective, they still require substantial visual inspection to confirm candidates. Other strong lensing search methods leverage crowdsourced visual inspection of large volumes of images, resulting in candidate samples with high purity and completeness (Marshall et al. 2016a; More et al. 2016).

Current state-of-the-art search methods involve the application of machine learning (ML) techniques, which have been successfully used in various fields of astrophysics (Huertas-Company & Lanusse 2023). Among these, Convolutional Neural Networks (CNNs), a class of deep learning algorithms suited to identify patterns and features in images, have shown significant promise. Metcalf et al. (2019) compared different strong lensing search methodologies and found that CNN-based techniques consistently outperform previous methods, significantly reducing the presence of false positives. Numerous studies have applied these techniques to wide-field imaging surveys, identifying thousands of strong lenses (e.g., Storfer et al. (2023); Zaborowski et al. (2023); Rojas et al. (2022); Shu et al. (2022); Huang et al. (2021); Cañameras et al. (2020); Huang et al. (2020); Li et al. (2020); Jacobs et al. (2019a,b); Petrillo et al. (2019)). However, despite reaching excellent performance on developed testing samples, the results on real data are very different, usually exhibiting low true-positive rates of  $\sim 1\%$  or less. This discrepancy may stem from training samples that lack the realism and diversity of actual data.

Recently, a novel machine-learning technique known as the transformer encoder (Vaswani et al. 2023) has been adapted to image classification tasks. This technique has shown superior performance compared to traditional CNN techniques on many image classification datasets like ImageNet, CIFAR-10 and CIFAR-100 (Dosovitskiy et al. 2021). Thuruthipilly et al. (2024) integrated a transformer encoder in their strong lens search methodology and applied it to data from the Kilo-Degree Survey (KiDS), reporting a true-positive rate of 0.5%. Grespan et al. (2024) adopted the ML architectures of the previous work and fine-tuned them to real KiDS data, after applying them to ~5 million galaxies from KiDS, they select a sample of ~51,000 systems for visual inspection and report a final sample of 231 candidates. Similar to previous searches, they encountered the common issue of an extremely low true-positive rate of less than 1%, which reflects the current state-of-theart performance.

Currently, the sample of strong lensing candidates consists of tens of thousands of systems (Vernardos et al. in prep), but with upcoming astronomical surveys such as Euclid and the Legacy Survey of Space and Time (LSST), this number is expected to increase to  $10^5 - 10^6$  (Barroso et al. 2024; Collett 2015). For the much rarer DSPLs the picture is similar: A handful are currently known (e.g., O'Donnell et al. (2022); Shajib et al. (2020b); Diehl et al. (2017); Tanaka et al. (2016); Gavazzi et al. (2008)) but  $\mathcal{O}(10^3)$  and  $\mathcal{O}(10^2)$  DSPLs are expected to be found in Euclid (Sharma et al. 2023) and LSST (The LSST Dark Energy Science Collaboration et al. 2021), respectively. The main challenge for these surveys will be finding strong lenses and DSPLs amongst the billions of non-lenses that they will predominantly observe.

In the near future, astronomical surveys will generate a massive amount of data, making it essential to develop search methods with higher true-positive rates. Without new methods, an implausible amount of human time would be needed to visually inspect ML-selected strong lensing candidates. Our work has two main goals: (1) identifying strong gravitational lenses in the Dark Energy Survey (DES) and (2) developing a methodology that can better handle the demands of upcoming wide-field astronomical surveys. To achieve this, we choose the Vision Transformer (Subsection 2.3) as our machine learning architecture and adopt Interactive Machine Learning (IML) to create a more comprehensive training sample (Subsection 2.2). Additionally, we conduct two independent strong lensing (SL) searches: one to find strong lenses in general and another one to target DSPLs. We implement an independent search for DSPL because DSPLs can exhibit very different morphology from single source lenses (Collett & Bacon 2015), and ML searches designed for single-plane lenses often struggle to identify them. In one study comparing different lens searches, Metcalf et al. (2019) found that all automated searches failed to identify a compound lens in their data. Only expert visual inspection correctly identified the DSPL.

This paper is structured as follows: In Section 2, we summarize the methodology adopted in this work. Subsection 2.1 describes the DES dataset, 2.2 outlines how our training sample is constructed, Subsection 2.3 summarizes the architecture of the Vision Transformer, and Subsection 2.4 covers the training process and the ML model's performance on a testing sample and known catalogs of strong lenses. Section 3 presents the results from the ML search, along with two rounds of visual inspection: one involving citizen scientists on the platform Zooniverse, and the other with strong lensing experts. Finally, in Section 5, we discuss the significance of these results and summarize our conclusions.

# 2. METHODOLOGY

Applying machine learning to detect strong gravitational lenses represents a standard vision classification task. The initial step in this process is constructing a training sample. Given the limited number of known lenses, simulations of strong lenses are employed as positive examples within training datasets. Conversely, negative examples are typically extracted from real data obtained from astronomical surveys.

In this section, we outline our methodology and it is organized as follows: Subsection 2.1 describes the DES cutout images used in this work for training and applying our ML algorithms. Subsection 2.2 details the construction of our ML dataset for training, validating, and testing. Subsection 2.3 provides an overview of the Vision Transformer's architecture and Subsection 2.4 delineates the training process and discusses the ML model's performance.

#### 2.1. The Dark Energy Survey Dataset

The Dark Energy Survey utilizes the Dark Energy Camera (DECam) (Flaugher et al. 2015) on the 4-meter Victor M. Blanco Telescope at the Cerro Tololo Inter-American Observatory in Chile. DES mostly makes use of five photometric filters (g, r, i, z, and Y) that collectively cover the range ~398-1065 nm. The latest DES public data release (DR2) encompasses the total six years of DES operations (DES Y6), covering approximately 5,000 square degrees of the southern sky and cataloging roughly 691 million distinct astronomical objects (DES Collaboration et al. 2021). This data release has a median point-spread function Full Width at Half Maximum (FWHM) of q = 1.11, r = 0.95, i = 0.88, z = 0.83" and Y = 0.90". The median coadded catalog depth for a 1.95" diameter aperture at signal-to-noise ratio = 10 is g = 24.7, r = 24.4, i = 23.8, z = 23.1, and Y = 21.7 mag.

In this work, we use g-, r-, and i-band 45x45 pixel (~12"x12") cutouts of the Y6 coadded images to construct our training sample and apply our machine learning algorithms. The image sample for ML application is created by selecting objects from the Y6 catalogs that are likely to be galaxies, which are identified by applying a cut on the morphological star/galaxy classifier of EXT\_COADD > 1 (DES Collaboration et al. 2021). Additionally, we apply a magnitude cut, selecting objects with i-band AB magnitudes between 15 and 23.5. We highlight that in contrast to many previous SL searches, we do not apply color selection cuts. The resulting sample has an approximate size of 236 million cutout images. Section 2.4 describes how the images are pre-processed for the ML model.

Certain kinds of astronomical objects with features that may resemble strong gravitational lensing frequently appear as false positives in SL searches. Examples include spiral galaxies, ring galaxies, edge-on galaxies with close neighbors, etc. Some of these kinds of objects are more abundant in the universe than others, e.g. ring galaxies are much rarer than spiral galaxies. Consolidating all such potential false positives into a single negative training class risks under-representing less common types. This under-representation can hinder the ML model's ability to learn the distinctive features of each object type, reducing its effectiveness in distinguishing them from genuine strong lenses. To mitigate this issue, we designed our machine learning searches as multi-class image classification tasks, with specific training classes tailored to address these different types of common false positives.

The training sample was constructed implementing Interactive Machine Learning (IML), a form of humanin-the-loop ML methodology characterized by close interaction between the ML model and the developer. In IML, both entities exert comparable levels of control over the learning process. In this iterative approach, the performance of a trained model is evaluated, and the developer provides feedback by modifying either the training sample or the ML model's features (Amershi et al. 2014). By enabling humans to tailor input based on the model's current deficiencies, IML facilitates ML models to have predictions that better align with the developer's goals (Jiang et al. 2018).

We implement IML by starting with two basic training classes for our primary search: positive (lens) and negative (not lens). When applying this initial trained model to real Y6 DES imaging data, an enormous quantity of images were incorrectly classified into the positive class exhibiting a true positive rate  $\ll 1\%$ . A large fraction of these false positive cases were spiral galaxies and small and faint elliptical galaxies. As a consequence, we created a new training class for spiral galaxies and added faint elliptical galaxies to our initial negative class. We iterated this process several times and created a total of nine distinct training classes for the main search. These training classes were also included in the dataset for the DSPL search, supplemented by two additional classes: the target of this search (DSPLs) and an additional common type of false positive of this search. All training classes are described in detail in subsections 2.2.1 and 2.2.2. Both training samples are similar in size, and in the DSPL search, single-plane strong lenses are part of a different training class than DSPLs. Figure 1 showcases example images for each training class. Additionally,

Tables 1 and 2 show the entire composition of the ML dataset for the main and DSPL search, respectively.

**Table 1.** Distribution of classes in the ML dataset for the main search, with the dataset divided into 70% for training, 15% for validation, and 15% for testing. Subsections 2.2.1 and 2.2.2 describe the training classes.

Class	Number of Images
Single	14,000
Ring	1,700
SDSS Spirals	1,500
DES Spirals	2,000
Smooth	1,500
Companions	1,000
Artifacts	2,090
Crowded	1,400
Red Spheroids	15,000
Total	40,190

**Table 2.** Distribution of classes in the ML dataset for the DSPL search, with the dataset divided into 70% for training, 15% for validation, and 15% for testing. Subsections 2.2.1 and 2.2.2 describe the training classes.

Class	Number of Images
Double	8,000
Single	8,000
Ring	$1,\!600$
SDSS Spirals	1,500
DES Spirals	2,000
Smooth	1,250
Companions	1,000
Artifacts	2,090
Crowded	1,400
Red Spheroids	15,000
Diffuse	1,100
Total	42,940

While most examples in the negative training classes were sourced from previously published morphological catalogs of galaxies, approximately 8,000 examples were added through visual inspection of images that the ML model initially misclassified as positive. These examples were selected after manually reviewing tens of thousands of images, which required a significant time investment. However, by applying this ML model to the DES dataset, this work provides tens to hundreds of thousands of objects reliably categorized into each of our



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Figure 1. Examples of the classification classes in our ML Dataset. This figure illustrates 5 example images from each of the 11 different training classes in our dataset. The examples demonstrate the distinct features within each class. Classes include 'Single' (Single-plane simulations), 'Double' (DSPL simulations), 'Ring' (ring galaxies), 'SDSS Spirals' and 'DES Spirals' (spiral galaxies found in the respective survey), 'Smooth' (diffuse, extended galaxies), 'Companions' (central galaxies with adjacent companions), 'Artifacts' (imaging anomalies), 'Crowded' (densely populated regions), 'Red Spheroids' (predominantly elliptical galaxies), and 'Diffuse' (interstellar clouds of gas and dust). Each cutout measures  $\sim 12 \times 12$  arcseconds.

training classes, facilitating the creation of future training samples. Furthermore, recent efforts to refine galaxy morphology catalogs, such as Walmsley et al. (2023), will further reduce the need for extensive human involvement in the construction of training datasets.

# 2.2.1. Simulated Positive Training Classes

'Single' is the positive class of our main search, while 'Double' is the positive class for the DSPL search. Both classes are populated with simulations featuring real DES images of the lensing galaxies, overlaid pixel by pixel with images of simulated lensed sources. The lensing galaxies are selected randomly from a DES catalog created with the redMaGiC algorithm (Rozo et al. 2016) that targets luminous red galaxies (LRGs), which tend to be massive elliptical galaxies. We consider only the  $\sim 50,000$  galaxies with available spectroscopic redshifts, which are measured by external spectroscopic surveys as described in Rozo et al. (2016). For this reason, the representation of deflectors with redshifts greater than 0.75 is limited (see Figure 3), and this methodology is not expected to achieve a high completion rate for such systems. Additionally, we exclude galaxies with redshifts below 0.15 due to them being too large and bright for our cutout size. After choosing a lensing galaxy, we superpose simulated lensed sources into the image of the deflector galaxy, as shown in Figure 2. Finally, we randomly rotate and reflect the final image to augment this class with non-repeating simulations.



Figure 2. Creation of simulations for the 'Single' class. Left: Images of luminous red galaxies randomly selected from the DES redMaGiC catalog (Rozo et al. 2016). Right: The same images overlaid with simulated strongly lensed sources. Simulation properties are constrained to ensure obvious strong lensing features. Each cutout measures  $\sim 12 \times 12$  arcseconds.

Through the adoption of IML, we observed a significant improvement in the performance of the ML model when utilizing simulations featuring clear strong lensing features. Consequently, we adopted simulation properties that produce bright and large lensed source images. Although the resulting simulations may not resemble realistic examples of strong lenses, this does not pose a problem in the context of a search as long as the selection function of the ML model is taken into account in population-level analyses of strong lenses. The use of IML likely tunes this methodology to preferentially identify strong gravitational lenses with large Einstein radii and bright lensed images.

The simulation of gravitationally lensed sources is generated using Lenstronomy (Birrer et al. 2021; Birrer & Amara 2018). The mass distribution of the lensing galaxy is assumed to be a Singular Isothermal Ellipsoid (SIE) profile, a simple mass profile capable of fitting most strong lenses. This mass profile requires as input parameters the velocity dispersion of the galaxy (attribute proportional to its mass), its position (assumed to be in the center of the cutout), and its ellipticity. The values of the velocity dispersion are drawn from a uniform distribution spanning the range 300-650 km/s. For the ellipticity, we choose the orientation angle to be within 40 degrees of the galaxy's visible orientation angle, this is because the semi-major axis of the galaxy could be misaligned with respect to the orientation angle of the dark matter halo hosting it. The axis ratio of the ellipticity is allowed to vary uniformly between 0.001 and 1.

The redshift of the lensing galaxy is drawn from the sample of spectroscopic redshifts included in the red-MaGiC catalog (Rozo et al. 2016). For the 'Single' class, the redshifts of the deflector galaxy and the source follow the distributions shown in the top panel of Figure 3, with the constraint that the source redshift is at least 0.2 higher than the lensing galaxy's redshift.

The intrinsic light distribution of the source, prior to lensing, is modeled by a Sérsic light profile (Sérsic 1963). The eccentricity parameters, and surface brightness value at the half-light radius and the half-light radius for each photometric band are derived from measured properties of galaxies in the DES Y6 catalog with similar redshift values (DES Collaboration et al. 2021). The Sérsic index is randomly drawn from a uniform distribution between 0.3 and 4. In addition, we choose a random source position inside the region that produces multiple images with a total magnification higher than 3. The seeing of the simulated image in each photometric band is modeled by a Gaussian function with its FWHM determined using the DES Y6 survey condition maps for sky areas near the deflector galaxy. This Gaussian approximation is sufficient for our analysis, as it captures the dominant effects of seeing while maintaining consistency with the observational conditions.



Figure 3. Redshift distributions used for our strong gravitational lensing simulations. Top panel: 'Single' class, ensuring the source redshift is at least 0.2 larger than the lensing galaxy's redshift. Bottom panel: 'Double' class, ensuring the first source redshift is at least 0.2 larger than the lensing galaxy's redshift, and the second source redshift is at least 0.1 larger than the first source's redshift.

To make simulations with pronounced lensed arcs, we boost the brightness of the source by two magnitudes, similar to the adjustment made by Rojas et al. (2022)and Jacobs et al. (2019b). Additionally, we set constraints on simulation properties like the apparent magnitude of the lensed source, and source image position (correlated to the Einstein radius). The distribution of Einstein radii of these simulations is shown in the top panel of Figure 4. Additionally, we define and constrain the values of two properties: 'contrast' and 'size comparison'. Contrast measures the brightness of the source relative to the lensing galaxy within the pixels occupied by the source. Size comparison estimates the potential overlap between the source images and the lensing galaxy as the ratio between the Einstein radius and the radius of a circle around the lensing galaxy's barycenter that contains half of its flux in the q band.



**Figure 4.** Einstein radii distributions used for our strong gravitational lensing simulations. Top panel: 'Single' class. Bottom panel: 'Double' class.

In relation to the DSPL search, we are particularly interested in finding systems where the intermediate source galaxy is much less massive than the foreground lensing galaxy. This is because in this case lens modeling, the main systematic in strong lensing analyses, is much easier to determine. For this reason, we produce the 'Double' simulations by generating two independent 'Single' simulations with sources at different redshifts using the same lensing galaxy. Then, we overlay the image of the lensing galaxy with the simulations of both sources. Both 'Single' simulations are required to pass the constraints described in the previous paragraph. The redshifts of the lensing galaxy and the sources follow the distributions shown in the bottom panel of Figure 3, with the constraints that the first source redshift is at least 0.2 higher than the lensing galaxy's redshift and the second source redshift is at least 0.1 higher than the first source redshift. To ensure that the lensed features from each source are distinguishable and clear, we define and constrain the values of two new simulation properties. One of these constraints avoids simulations where the sources have colors that

are too similar: we calculate the difference between the color indices g-i and g-r for the sources, and require that the sum of the absolute differences be at least 0.3  $(|(g-i)_2 - (g-i)_1| + |(g-r)_2 - (g-r)_1| \ge 0.3)$ . The other constraint discourages sources with similar Einstein radii by requiring a minimum absolute difference of 0.5" in image separation between the values of both source simulations. The distribution of Einstein radii of these simulations is shown in the bottom panel of Figure 4.

#### 2.2.2. Negative Training Classes

As described in Section 2.2, our negative training sample was constructed employing an IML approach. We began with a basic negative training sample consisting solely of LRGs and gradually increased its complexity to enhance the ML model's performance on the DES dataset. While several training classes were populated using published morphological catalogs of galaxies, the majority were populated through the manual labeling of images that our ML models had incorrectly classified as either 'Single' or 'Double' with high probability.

Our main search uses the following negative training classes: Ring, Smooth, Companions, SDSS Spirals, DES Spirals, Crowded, Artifacts, and Red Spheroids. All of these classes have a degree of subjectivity and are best understood by referring again to Figure 1. In summary, the 'Ring' class consists of images showcasing ring galaxies, while 'Smooth' denotes galaxies with a diffuse and extended appearance. 'Companions' refer to images featuring a central galaxy with an adjacent edge-on or diffuse galaxy. 'SDSS Spirals' and 'DES Spirals' encompass mostly spiral galaxies originally identified within their respective astronomical surveys. These two classes were not combined because 'DES Spirals' could not be filtered to include only face-on spiral galaxies, which are more challenging to distinguish from strong lenses, whereas 'SDSS Spirals' was specifically constructed to include only face-on spirals. 'Crowded' images capture densely populated regions. 'Artifacts' represent images displaying imaging anomalies stemming from instrumental effects, processing errors, or transient phenomena. 'Red Spheroids' comprises a diverse collection of images predominantly featuring elliptical galaxies.

The DSPL search includes two additional negative training classes: Single (single plane lenses) and Diffuse. 'Diffuse' images feature cloud-like, diffuse structures, often representing fields observed through the extended structure of a low-redshift galaxy. This class was added to this search because the initial DSPL ML model frequently misclassified such objects as 'Double'.

We populate some training classes with the SDSS morphological catalog presented in Domínguez Sánchez et al. (2018), which comprises ~42,000 galaxies also identified in DES. From these  $\sim 42,000$  galaxies, we select face-on spiral galaxies and classify them as either Ring (46 instances) or SDSS Spiral (317 instances). Both sets were augmented by applying rotations and reflections to increase their size to 100 and 1,100, respectively. Additionally, we select images with a high probability of displaying merging objects, augment this sample from 219 to 400, and add the resulting images to the SDSS Spiral class. The augmentation limits were chosen to increase sample size while avoiding over-representation and potential overfitting. Finally, we randomly select 2,000 galaxies likely to be round and add them to the Red Spheroid training class.

We populate more training classes with the morphological catalog presented by Cheng et al. (2021), which contains over 20 million galaxies detected within the DES footprint, along with a probability measure for each galaxy being elliptical rather than spiral. From this catalog, we select a sample of 2,000 galaxies likely to be spiral. Given the significant fraction of edge-on galaxies in this subset, we create the 'DES Spirals' class for them. This approach ensures that the class 'SDSS Spirals', allows the ML model to better distinguish the features of face-on spiral arms from lensing arclets. In addition, we add to the 'Red Spheroids' class 2,500 highly probable elliptical galaxies (p > 0.9) and 2,000 moderately probable elliptical galaxies (p > 0.6), excluding previously selected objects.

The 'Red Spheroids' class also includes 5,000 randomly selected redMaGiC galaxies (Rozo et al. 2016) that we use as lensing galaxies in our simulations. Additionally, this class comprises 3,500 images that were classified by an early-trained ML model as having an extremely low probability of being strong lenses.

Approximately 40% of the 'Artifact' class consists of images selected using columns from the Y6 GOLD table (Bechtol et al. in prep), which identify bright foreground objects or regions with missing data.

The remaining images in the training set were selected through manual inspection and labeling of images incorrectly classified as 'Single' or 'Double' during the IML process. The distribution of labeled images across the different categories is as follows: 1,600 for 'Ring', 1,500 for 'Smooth', 1,000 for 'Companions', 1,400 for 'Crowded', 1,290 for 'Artifacts', and 1,100 for 'Diffuse'.

## 2.3. The Vision Transformer

The machine learning model used for both searches is the Vision Transformer (ViT) (Dosovitskiy et al. 2021). We briefly describe the model's architecture here and refer the reader to the original paper for full details. Figure 5 provides a visual representation of the ViT architecture. First, the input image is divided into smaller, non-overlapping image sections called patches, with each patch projected onto a one-dimensional vector. Position embedding vectors are then added to these vectors to encode the position of each patch within the sequence. The resulting vectors, called 'embedded patches', are then input into the Transformer Encoder, which consists of multiple stacked layers. The final element in the architecture is a Multilayer Perceptron (MLP) head that assigns the input image to one of the predefined categories for the classification task.

The Transformer Encoder was introduced in Vaswani et al. (2023) and is based on the self-attention mechanism, here represented by multi-head attention (MHA) blocks. The goal of the self-attention mechanism is to produce output vectors that are 'context-aware' of the entire sequence. This is done by calculating them as a weighted sum of the input values using three matrices, whose components are learned during training. A multi-head attention block performs multiple attention functions in parallel and at the end, the output of each function is concatenated into a single vector. The final element in the Transformer Encoder is an MLP that acts as a classification head.

A key difference between transformers and conventional CNNs is their approach to image analysis. In CNNs, early layers focus on small, localized regions of an image, with each subsequent layer integrating information from progressively larger areas. In contrast, the Vision Transformer (ViT) processes the entire image from the initial transformer block. This allows the network to capture patterns across distant patches and identify global features early in the training process.

Since self-attention layers are global and lack the builtin assumptions about local patterns that CNNs have, they do not generalize well when trained on limited data. However, we can overcome this disadvantage by pre-training a ViT model on a large dataset and then fine-tuning it to our classification task, this is known as 'transfer-learning' (Pan & Yang 2010). By using the learned features and weights of the pre-training process as a starting point, the amount of data and computational resources required for training is reduced and the performance of the model usually increases. When ViT is pre-trained on large datasets, it can perform the same or better than state-of-the-art CNN models (like BiT and Noisy Student) (Dosovitskiy et al. 2021).

In this work, we implemented the ViT model with the least number of parameters (ViT-Base, with 86 mil-



Figure 5. Architecture of the Vision Transformer (ViT) (Dosovitskiy et al. 2021). The input image is divided into fixed-size image sections, which are linearly embedded and combined with position embeddings. These embeddings are then processed by a Transformer Encoder which applies multiple self-attention mechanisms. The output is finally fed into a classification head to predict the input image's class based on the training categories.

lion parameters) and adopted a 16x16 pixel patch size. These choices reduce the computational resources required for training while maintaining high performance. Our ML model is pre-trained on ImageNet-21k (Deng et al. 2009), which contains 14 million images and 21 thousand classes. Pre-training enables the model to learn general image features from a diverse dataset, providing a strong foundation that improves performance and reduces the data requirements for fine-tuning on our specific task. The model with its pre-trained weights is implemented using the Python library PyTorch Image Models (*Timm*) (Wightman 2019). For the fine-tuning process, we add a single MLP layer at the end of the architecture to classify images according to the defined classes for our task.

### 2.4. Training and Performance

The ML datasets used for both searches are divided into three subsets: 70% for training, 15% for validation, and 15% for testing. Before being fed into the ML model, the images are resized to 224 x 224 pixels, as required by the pre-trained model available in the *Timm* Python package (Wightman 2019). The resizing is performed using the Resize function from the torchvision.transforms package, which employs bilinear interpolation. Additionally, the images are normalized to the mean values [0.485, 0.456, 0.406] and standard deviations [0.229, 0.224, 0.225] for the g-, r-, and i-bands, respectively. These values are used because the ML model was pre-trained on the ImageNet dataset, and these images were pre-processed using these specific mean and standard deviation values. During training, we minimize cross-entropy loss and stop training once the accuracy on the validation set fails to improve for more than three epochs. Training accuracy reflects the ML model's performance on the data it learned from, while validation accuracy provides an indication of how well the ML model generalizes to unseen data, helping to prevent overfitting. The ML model for the main search achieved training and validation accuracies of 95.5% and 95.6%, respectively, while the DSPL model achieved training and validation accuracies of 95.2% and 93.9%. We trained both ML models on the Open Science Pool (OSG 2015) platform, utilizing a GPU to accelerate the process from a few days to nearly four hours.

### 2.5. Performance on the testing sample

We achieve classification accuracies of 95.2% and 93.9% on the testing samples for the main search and the DSPL search, respectively. Additionally, we assess the model's ability to distinguish between the positive class and any of the negative classes, yielding accuracies of 99.5% for the main search and 99% for the DSPL search. To further assess performance, we use a Receiver Operating Characteristic (ROC) curve, which illustrates an ML model's performance as a binary classifier as the discrimination threshold is adjusted. Figure 6 presents the exceptional ROC curve for the main model, where all negative classes are treated as a unified class.

Another performance metric for binary classifiers is the area under the ROC curve (AUC), which ranges from 0 (indicating a perfectly incorrect classifier) to 1 (indicating a perfect classifier), with a value of 0.5 representing random guessing. Both ML models demonstrate



Figure 6. Receiver Operating Characteristic (ROC) curve illustrating the performance of the main machine learning model on its testing sample. The pink star indicates the probability threshold chosen for application to the Dark Energy Survey dataset.

exceptional performance on their respective testing samples, achieving AUC values of ~1. While many previous ML strong lensing search studies have also reported near-perfect performance on their testing sets, the performance on real data differed significantly. Given that training, testing, and validation were conducted solely on simulated lenses and our negative sets are unambiguous, we should not anticipate achieving near-perfect performance on the actual DES data. This discrepancy highlights the importance of not overemphasizing model performance based solely on results from constructed testing sets.

# 2.6. Performance on known SL candidate catalogs

We use two catalogs of SL *candidates* identified in DES to evaluate the performance of our main ML model. The Jacobs et al. (2019a,b) sample consists of 511 mostly galaxy-scale candidates discovered using CNN-based methods. The O'Donnell et al. (2022) catalog contains 247 mainly cluster-scale candidates identified through non-ML algorithms. For this analysis, we visually inspect these candidates and exclude systems with lensing features outside our cutout images, resulting in 457 candidates from the Jacobs catalog and 140 from the O'Donnell catalog.

The ML model's output for an input image is a vector with components corresponding to the number of training classes, where each component, ranging from 0 to 1, represents the probability of the image belonging to that class. By classifying images into the class with the highest assigned probability, the model successfully recovers 85.6% of candidates from the Jacobs sample and 70% from the O'Donnell sample. Given that neither the Jacobs nor the O'Donnell samples are completely pure, it is not surprising that many of their candidates are missed. Additionally, the lower recovery of the O'Donnell sample is probably due to group-scale lenses having more complex morphologies that are not represented in our training sample.

To provide a qualitative assessment of the ML model's performance, Figure 7 displays a collection of candidates that were not recovered. Each image title indicates the class to which it was classified, the model-assigned probability of being 'Single', and an expert-assigned grade (0-3) or rank (0-10) from the Jacobs and O'Donnell samples respectively, reflecting the likelihood of being a strong lens. While Jacobs et al. (2019a,b) required a grade of 2 to qualify as a candidate, O'Donnell et al. (2022)'s rank cut was set at 3. Most of the candidates not recovered by the main ML model lack definite signs of strong lensing or seem to be group-scale lenses.

Without spectroscopic confirmation, it is not possible to determine whether our ML model fails to identify real lenses or correctly rejects false positives in the Jacobs and O'Donnell catalogs. Additionally, the Jacobs search was performed on a previous DES data release significantly shallower than DES Y6. Visual inspection suggests that many of the missed candidates are likely not true lenses, although some may be lenses that our classifier has overlooked. Nonetheless, most of the missed candidates remain ambiguous even after expert visual inspection.

#### 3. RESULTS

We applied both ML models to the sample of  $\sim 236$ million DES cutout images and selected all images exceeding a threshold of 0.75 and 0.5 for the main and DSPL search, respectively. The output was then visually inspected by citizen scientists through a Space Warps<sup>1</sup> project on the Zooniverse<sup>2</sup> platform. Subsequent expert inspection was conducted on the resulting images. In Section 3.1, we describe the application of ML to the DES dataset. Sections 3.2 and 3.3 detail the setup and results of the citizen science inspection. Section 3.4 covers the expert visual inspection process and the classification of our final sample of candidates. Finally, in Section 3.5, we present the best DSPL candidates identified. Figure 8 provides an overview of our selection workflow, illustrating the filtering of 230 million images to 1,328 SL candidates and 8 DSPL candidates. This figure includes the number of candidates that have been reported as strong lensing candidates in the SLED

<sup>&</sup>lt;sup>1</sup> www.spacewarps.org

<sup>&</sup>lt;sup>2</sup> www.zooniverse.org



Figure 7. Examples of strong lensing candidates (O'Donnell et al. 2022; Jacobs et al. 2019a,b) not retrieved by the main ML model. Each image title indicates the assigned class, the model's probability of being 'Single' (single-plane strong lens), and the expert-assigned 'grade' or 'rank' (0-3 for Jacobs, 0-10 for O'Donnell). Most unrecovered candidates lack definite strong lensing signs (with lower 'grades' from Jacobs et al. (2019a,b)) or group-scale strong lensing candidates. Each cutout measures ~12×12 arcseconds.

database (Vernardos et al. in prep), without doing any cuts on the reported expert score or on the astronomical survey where they were identified.

## 3.1. Machine Learning

We processed the ~230 million DES cutout images with both ML models on the FermiGrid<sup>3</sup>, and through parallelization, both applications took around three days to complete. For the main search sample, we selected images with a 'Single' ML score of 0.75 or higher. For the DSPL search sample, we selected images with a 'Double' ML score of 0.5 or higher. The 'Single' probability threshold was chosen to obtain a reasonable number of candidates for visual inspection while still aiming to attenuate the presence of false positives. For the DSPL search, a much lower threshold was chosen as the focus in this case is to find true-positives. A significant fraction of the selected images contained the same SL candidates, albeit centered on different objects. We removed duplicated images and manually add 40 SL candidates visually identified during the IML process. This led us to a final sample of 20,636 'Single' candidates and 2,538 'Double' candidates, with 610 candidates in the intersection of both sets.

## 3.2. Visual Inspection by Citizens

The 22,564 candidates from both searches were visually inspected by citizen scientists as a Space Warps (Marshall et al. 2016a; More et al. 2016) project, which ran from October 17th to November 3rd, 2023. During this period, 731 users participated with a median of 34 classifications. Each lens candidate was presented in four different 'filters' or color balance PNG settings, which highlight different features in the images. Participants were asked to mark any strong lensing features they recognized in the image. The four PNG filters and the task instructions are shown in Figure 9.

In addition to our candidates, which we refer to as 'test subjects', we included 2,451 'training subjects', comprised of 1,152 non-lenses, 444 known candidate lenses, and 855 simulated lenses. These known candidate lenses are extracted from the samples published in Jacobs et al. (2019a,b) and O'Donnell et al. (2022), and did not include systems with strong lensing features outside our cutout images. We use the training subjects to provide active training to citizens during the classification task, providing live feedback indicating whether the classification was correct or incorrect after each classification was made. In addition, these classifications are used to calculate the users' success or skill in classifying lenses and non-lenses.

This method is summarised here, but readers are directed to Marshall et al. (2016a) for a complete description. The posterior probability  $P_{k+1}(L) \equiv P(L|\{C_{U_0}, ..., C_{U_k}\})$  for a given training subject, having received k + 1 classifications  $\{C_{U_0}, ..., C_{U_k}\}$  from users  $\{U_0, ..., U_k\}$  is given by:

$$P_{k+1}(L) = \frac{P(C_{U_k}|L) \cdot P_k(L)}{P(C_{U_k}|L) \cdot P_k(L) + P(C_{U_k}|\hat{L}) \cdot P_k(\hat{L})} \quad (1)$$

where the classifications are either 'Lens' ('L') or 'Non-Lens' (' $\hat{L}$ '). The skill of each user is given by their responses to the training subjects they have seen, e.g,  $P(C_{U_k} = L'|L) \approx N_{\cdot L'}/N_L$  is the ratio of the number of lens training subjects,  $N_{\cdot L'}$ , that the user has correctly classified as a lens to the total number of lenses they have seen,  $N_L$ . In this manner, higher skill users can

<sup>&</sup>lt;sup>3</sup> https://www.fnal.gov/pub/science/computing/grid.html



Figure 8. Summary of our selection workflow, illustrating the reduction from 230 million images to 1,328 SL candidates and 8 DSPL candidates. Both ML models were applied to the DES cutout images, and those exceeding a chosen threshold were inspected by citizen scientists. The highest-scoring images were then reviewed by experts. The number at the bottom of each block represents the number of subjects reported in the SLED database as SL candidates including all reported scores and candidates identified in other surveys. We report 1,328 strong lensing candidates and 8 potential DSPL candidates.



Figure 9. Screenshot from the Space Warps citizen science project on Zooniverse. Participants were shown each candidate in four distinct PNG filters designed to highlight different image features and were asked to place at least one mark in the image if strong lensing features were recognized.

cause more significant changes in the posterior probability, while a user who mis-classified the training subjects 50% of the time (i.e. random classification) would not change the subject score at all.

All subjects were assigned an initial score of  $P_0(L) = 5 \times 10^{-4}$  (the prior), based on the frequency of strong lensing in the galaxy population. These scores were processed via the Space Warps Analysis Pipeline (SWAP, Marshall et al. (2016b)). If users reached a consensus on any test subject after at least 5 classifications such that its score was  $p < 1 \times 10^{-5}$  the subject was 'retired' i.e.

no longer shown on the platform. This is to maximise efficiency as the bulk of the task is to remove unlikely candidates. Test subjects with  $p > 1 \times 10^{-5}$  remained in the classification stream until 30 classifications had been made. Training subjects were not retired.

## 3.3. Results of Visual Inspection

The citizen scientists skill distribution is shown in Figure 10. The vast majority of classifiers were in the 'Astute' quadrant of user skill, indicating that they could correctly identify the majority of training subjects, both lenses and non-lenses. The training subjects



Figure 10. A plot of the user skills, based on their performance on a training set. The user skill is defined as the fraction of correctly classified training subjects of each type, e.g the probability a user will classify a training subject as being a lens, given that it is indeed a lens, P(`Lens'|Lens), and vice versa. The size of each datapoint is scaled by the number of classifications made by the user. The vast majority of users correctly identified most of the lenses and nonlenses they were shown.

were accurately classified: most non-lenses received low scores, while most lenses (both simulated and real) received high scores. Furthermore, the majority of highconfidence real lens candidates also received a high score from the citizens.

Out of the 22,564 test subjects that were inspected by citizens, 2,502 received a score  $p > 1 \times 10^{-5}$  and were subsequently inspected by SL experts.

The Zooniverse platform allows users to engage in discussion boards about specific subjects, tag subjects with relevant labels (such as 'lens', 'possible', 'double'), and save them to personal collections. During the process of classifying subjects, reviewing discussions, and examining various tags, JG saved 'interesting' subjects into different collections. 104 of these subjects had received scores  $p < 1 \times 10^{-5}$  and were manually added to the pool of candidates to be inspected by SL experts.

# 3.4. Expert Grading of Candidates

Experts inspected the 2,502 subjects that received a score  $p > 1 \times 10^{-5}$  from citizens, along with 500 lowerscoring subjects randomly chosen for calibration purposes, and 104 candidates manually added by JG (as described in section 3.3). The group of experts consisted of eight individuals: JAB, GC, PH, JG, MM, TL, KR, and SS. The inspection task was performed using the software Visapp (More et al. 2016). Each subject was displayed in the same four PNG settings we used in the visual inspection by citizens. Experts assigned a grade to each subject as follows:

- 0: Very unlikely (< 1%),
- 1: Probably not a lens (2 50%),
- 2: Probable lens (50 90%),
- 3: Certain lens (> 90%).

Additionally, we asked the experts to type the word 'double' in the Visapp comment box if they believed a subject could be a DSPL candidate.

We calibrated the scores from the experts and report this as the 'expert score'. Figure 11 displays the distribution of these values across the sample (not including the 500 random subjects). We use the following thresholds on the expert score for classifying our final 1,328 strong lensing candidates into categories A, B, and C:

- A: 2.25 < Score (149 subjects, with 141 reported in the SLED database),
- B: 1.25 < Score < 2.25 (516 subjects, with 377 reported in the SLED database),
- C: 0.75 < Score < 1.25 (663 subjects, with 243 reported in the SLED database),



Figure 11. Distribution of the calibrated expert scores for the 2,502 subjects with citizen scores exceeding  $10^{-5}$ , and the 104 subjects manually added by JG after reviewing Zooniverse discussion boards, tags, and personal collections.

The A category contains primarily 'definite' lenses, with all 149 subjects displayed in Figures 12 and 13. Each subject in this category was scored a 2 or 3 by at least six of our seven experts, and at least two experts rated them a 3. Category B includes mostly 'probable' lenses, with a subset of subjects shown in Figure 14. Most subjects in this category received a score of 2 or 3 from at least three experts. Category C comprises 'maybe' lenses, which are less likely but could still be true positives. A subset of these subjects is shown in Figure 15. Each subject in this category was scored a 2 or 3 by at least one expert and exhibited a relatively high variation between the highest and lowest scores given by the experts.

#### 3.5. Double source plane lens candidates

Out of the 2,502 subjects experts inspected, 44 received a 'double' comment from at least one expert. This sample includes DESJ0610-5559, a multiple-source gravitational lens found previously in Diehl et al. (2017) and O'Donnell et al. (2022). All clear multiple-source candidates in both Diehl et al. (2017) and O'Donnell et al. (2022) are cluster-scale systems, and given that our cutout size is not optimized for this scale, we only recovered one of them. JG reviewed the subset of 44 subjects to identify the most compelling galaxy-scale DSPL candidates, removing cluster-scale multiple-source lenses from consideration. Figure 16 presents the top 8 DSPL candidates with their respective expert scores across various PNG settings and bands. Notably, all these candidates were identified by the main ML model, with two (DESJ001314-560839 and DESJ012258-022705) also being selected by the DSPL model. Most of the candidates are probably at least single-plane lenses (in our A and B categories), which is also suggested by the observation that all candidates, except for DESJ012258-022705, have already been reported in the SLED database. DESJ035242-382544 is almost certainly a double-source strong lens, though spectroscopic data is needed to confirm whether the sources are on different planes. The remaining candidates exhibit characteristics indicative of potential DSPLs, but higher-resolution imaging and spectroscopic confirmation are required for definitive identification.

# 4. GENERATION OF AN ENSEMBLE CLASSIFIER

Given classification scores were available for two different classifiers, the Vision Transformer and the Space Warps visual inspection, we tested whether an ensemble (combining the information from each individual classifier) would provide improved classification overall. With the arrival of wide-area surveys such as LSST, Euclid, and Roman wide-area surveys, the time-cost of expert grading of large numbers of high-scoring candidates will be significant but can be reduced by constructing the best possible performing classifier.

We generated an ensemble classifier via the 'Isotonic Regression' method, the best-performing method studied in Holloway et al. (2024). We split the expert-graded sample equally into a calibration and test set. For the purpose of calibration, we defined a 'true lens' as one receiving a grade  $G \geq 1.25$ . We calibrated the scores of the Vision Transformer and citizen science project via Isotonic Regression using the calibration set to produce probabilities a given object was a lens; this process maps a given classifier score (e.g. a score of 0.9 from the Vision Transformer) to the average expert grade that subjects with that score receive (calculated via Isotonic Regression). We note due to our definition of a true lens in this case the 'probabilities' are with respect to a system being an A or B grade; in the future a spectroscopic calibration set could be used to provide true probabilities of a lensing system. The probabilities determined from each classifier,  $\{P_c\} = \{P_{SW}, P_{VT}\}$  are then combined via Bayes Theorem (see Holloway et al. (2024) for a full derivation):

$$P_{Ens}(L|\{P_c\}) = \frac{N_{NL} \cdot \prod_c P_c}{N_{NL} \cdot \prod_c P_c + N_L \cdot \prod_c (1 - P_c)} \quad (2)$$

where  $N_L$  and  $N_{\hat{L}}$  refer to the number of lenses (i.e. grade A+B) and non-lenses (including low confidence candidates in the C category) in the calibration set respectively.

Validation of this calibration was made on the distinct test set, which is shown in Figure 17; a third 'validation' set commonly used in machine learning was not required here as the Isotonic Regression method had no free parameters. We then combined the calibrated probabilities for each subject from the vision transformer and citizen science search, assuming the two classifiers were independent (Holloway et al. 2024). The ROC and purity-completeness curves of the individual and ensemble classifiers are shown in Figure 18. We find the Citizen Science classifier typically provides greater completeness than the Vision Transformer, however the latter can provide a more complete sample when requiring high purity. We find our ensemble of just two classifiers can provide the best of both worlds, providing a performance at least as good as the best classifier for a given false positive rate (or purity). The ensemble classifier is dominated by the Citizen Science classifications at low purity ( $\leq 60\%$ ), while both classifiers play a significant role for higher purity thresholds. For future surveys this would reduce the number of systems required to be inspected; the ensemble classifier can provide lower false positive rates than the individual classifiers, and the calibration can be used to accurately predict the lens likelihood for each system in a dataset without them all being inspected.

## 5. DISCUSSION AND CONCLUSIONS

The main goal of this work was to develop an ML search methodology for strong gravitational lenses that



Figure 12. Page 1 of the strong lensing candidates in our A category (expert score > 2.25 out of 3). Eight of the candidates in this category have not been reported in the SLED database and are highlighted in blue in this figure. Each image shows the candidate's coordinates and expert score, with each cutout measuring  $\sim 12 \times 12$  arcseconds.

DESJ051314-523020	DESJ000451-010318	DESJ041644-552500	DESJ042048-563046	DESJ004109-004349	DESJ031638-223633	DESJ031127-423219	DESJ012753-453233
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2.55	2.55	2.55	2.54	2.53	2.53	2.53	2.53
DESJ014655-092959	DESJ004144-233905	DESJ020611-372938	DESJ053804-473513	DESJ012431-520703	DESJ013026-152012	DESJ034130-513045	DESJ014908-313738
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251	250	250	250	2.48	2.45	245	2.44
DESI055734-415950	DESI014134-404033	DESI000816-323714	DESI020954-354757	DESI225403-405549	DESI034311-282840	DESI034744-245431	DESI003119-642037
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2.43	2.43	2.42	2.42	2.42	2.42	2.42	2.41
DESJ044747-304630	DESJ011842-015013	DE5J035649-240841	DESJ235717-571025	DESJ011646-243702	DESJ013822-284408	DESJ212251-005949	DESJ022148-042042
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2.41	2.39	2.39	2.39	2.39	2.38	2.38	2.38
DESJ014433-114209	DESJ054735-600442	DESJ050849-214430	DESJ011758-052717	DESJ013322-125201	DESJ032125-153003	DESJ024328-214202	DESJ015737-122138
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2.38	2.37	2.37	2.37	2.37	2.34	2.32	2.31
DESJ054848-421254	DESJ004150-515750	DESJ013050-160008	DESJ001110-323704	DESJ035510-183134	DESJ023906-204718	DESJ024857-605403	DESJ032711-324634
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2.30	2.30	2.30	2.29	2.29	2.29	2.29	2.29
DESJ062415-470942	DESJ203911-545942	DESJ024809-395548	DESJ011408-361313	DESJ052700-185805	DESJ011756-242824	DESJ030639-273626	DESJ044805-580721
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2.29	2.28	2.28	2.28	2.28	2.27	2.27	2.27
DESJ010606-310437	DESJ211005-563930	DESJ035337-402417	DESJ025052-552411	DESJ060443-414837	DESJ022140-021020	DESJ021744-215834	DESJ003104-440300
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2.27	2.27	2.27	2.27	2.27	2.26	2.26	2.26
DESJ022809-125252	DESJ012025-182001	DESJ041112-541320	DESJ224434-590910	DESJ060239-465307			
Sector Sector				100000			
10 CA.				Sec. 1987			
				10 M			
7.76	2.26	2.26	2.26	2.25			
2.20	2.20	2.20	2.20	2.2.3			

Figure 13. Page 2 of the strong lensing candidates in our A category (expert score > 2.25 out of 3). Eight of the candidates in this category have not been reported in the SLED database and are highlighted in blue in this figure. Each image shows the candidate's coordinates and expert score, with each cutout measuring  $\sim 12 \times 12$  arcseconds.

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Figure 14. Collage of 56 random strong lensing candidates in our B category (1.25 < expert score < 2.25, out of 3). Candidates not reported in the SLED database are highlighted in blue. This category contains 516 subjects. Each image shows the candidate's coordinates and expert score, with each cutout measuring ~12×12 arcseconds.

can better handle the demands of the upcoming era of big data by producing samples of candidates with higher true-positive rates (TPR). We developed two ML models: one to find strong lenses in general and another to target DSPLs. We designed both searches as multi-class classification tasks, where we created specific training classes to address different types of potential false positives. We implemented a pre-trained Vision Transformer model as our ML architecture and adopted an Interactive Machine Learning approach to iteratively build and increase the complexity of our training sample.

Figure 8 summarizes our results. We applied both ML models to  $\sim 230$  million DES cutout images, selecting the

top 20,636 images from the main model and 2,538 from the DSPL model, with 610 images overlapping between the two samples. The selected images were visually inspected by citizen scientists, and the top 2,502 were further reviewed by experts, along with 104 images manually added by JG, as described in 3.3. Out of these, 1,328 received an expert score higher than 0.75 out of 3, and 149 of these are grade-A candidates according to our expert scores. Figures 12 and 13 show all candidates in the A category. Figures 14 and 15 present a random collection of candidates in the B and C categories, respectively. The 8 most promising galaxy-scale DSPL candidates are shown in Figure 16.



Figure 15. Collage of 56 random strong lensing candidates in our C category (0.75 < expert score < 1.25, out of 3). Candidates not reported in the SLED database are highlighted in blue. This category contains 663 subjects. Each image shows the candidate's coordinates and expert score, with each cutout measuring ~12×12 arcseconds.

Figure 19 presents a selection of 32 images that are scored highly by the main ML model ( $\geq 0.998$ ) and are rejected by the experts. The majority of these images exhibit features very similar to strong lensing. A significant fraction of them appear to depict merging galaxies and blue curved or elongated objects around a red galaxy, objects that are not well represented in our training sample. Future ML algorithms could be improved by including more of these types of systems in the training data or potentially by incorporating physics-based priors into the learning process.

To investigate the recovery rate of our methodology, we use four catalogs of strong lensing *candidates* that have been identified in DES previously (O'Donnell et al. 2022; Rojas et al. 2022; Diehl et al. 2017; Jacobs et al. 2019a,b). Results are summarized in Table 3. For the samples from Diehl and O'Donnell, we only consider systems with an Einstein radius lower than or equal to 6" and a rank of 5 or higher out of 10, where 3 was the minimal rank to be considered a candidate in both works. Additionally, for the Jacobs sample, we do not consider systems with arc-lets outside our cutout images. For low-confidence candidates in Rojas, and all pre-selected candidates in Diehl, O'Donnell, and Jacobs, the main ML model alone recovers 52%, 58%, 72% and 81% of the samples, respectively. The low recovery rate



Figure 16. The eight most promising galaxy-scale DSPL candidates from the 44 subjects identified by at least one expert as potential DSPLs. Each sub-figure's title includes the candidate's coordinates and expert score. The first two images of each candidate are composites of the g-, r-, and i-band cutouts. Each cutout measures  $\sim 12 \times 12$  arcseconds.



Figure 17. Validation of the calibration curves generated via isotonic regression, performed on a separate test set. The x-axis shows the calibrated probability, while the y-axis shows the fraction of objects with that assigned probability which are indeed lenses. A perfect calibration curve would therefore lie along the y = x line (solid black). The error bars have been calculated via bootstrapping.



Figure 18. Receiver operating characteristic (ROC) and purity-completeness curves for the individual and ensemble classifiers. The black point indicates the Space Warps threshold  $p = 1 \times 10^{-5}$ , marking the point where expert grading moved from all subjects to a random subsample. The curve segments have been weighted to account for this difference. The dashed line indicates the ROC expected from a random classifier (note the left-hand x-axis is logarithmic).



Figure 19. Collection of 44 images that received very high scores from our main ML model ( $\geq 0.998$ ) but were rated low by the experts. These are challenging cases with features very similar to strong lensing, most of which appear to be galaxy mergers. The text box on the bottom right of each image is its expert score. Each cutout measures ~12×12 arcseconds.

for these Rojas candidates is expected as these are ambiguous systems without prominent lensing features or counter-images. The highest recovery rate is for the Jacobs sample, which is composed mostly of galaxy-scale SL candidates. In comparison, we noticed a lower recovery for Diehl and O'Donnell, which could be due to these samples containing group-scale candidates. Next, we consider only the high-confidence candidates from Rojas, and the candidates that pass the thresholds grade > 2.3 out of 3 and rank > 7 out of 10 from Jacobs, and Diehl and O'Donnell, respectively. We calculate a recovery of 76%, 87%, 88%, and 90% for the high-confidence candidates in O'Donnell, Diehl, Rojas and Jacobs, respectively. This proves that our ML model is successful in identifying galaxy-scale lenses with clear lensing features.

The '(%)' column of 'Citizen Scientist (CS) Recovered' in Table 3 considers only the systems that were recovered by the ML model and not the total pre-selected sample. Thus, this column offers an estimate of ~88.5% for the completion rate of Citizen Scientists. When taking into account the selection by the main ViT model and the citizens' inspection, we calculate a recovery of 51%, 62%, 71% and 81% of the Diehl, O'Donnell, Jacobs, and Rojas high-confidence samples, respectively.

We also investigated how many of our final highconfidence candidates were reported in the previous four catalogs of strong lensing candidates (O'Donnell et al. 2022; Rojas et al. 2022; Diehl et al. 2017; Jacobs et al. 2019a,b). We calculate that the Diehl, O'Donnell, Jacobs and Rojas samples contain 10%, 10%, 39% and 23% of our candidates in categories A and B. Considering only the candidates in our A category, we calculate that the Diehl, O'Donnell, Jacobs, and Rojas samples contain 20%, 23%, 63% and 40% of these candidates, respectively. This highlights the relatively high completion achieved by our methodology.

Among our 228 candidates that received an expert score higher than 2, 71 were not reported by Jacobs or Rojas. Of these, 40 did not pass either of their color selection cuts. By not applying color cuts, we discovered  $\sim 20\%$  more candidates but at the cost of analyzing  $\sim 30$  times more data.

The TPR that an ML model can achieve depends on the chosen score threshold, which determines the number of images to be inspected. Figure 20 shows the number of images past a probability threshold that needs to be inspected (x-axis) to recover a certain number of candidates (y-axis). To recover 100 of the 149 subjects in our A category, we would need to inspect 830 images, representing a TPR of 12.1%. A similar TPR of 12.8% is reached to recover 400 of the 655 subjects with expert scores higher than 1.25. Discovering 600 of these would require inspection of 15,310 images (TPR of 3.9%). These TPR estimates are much higher than previous searches, demonstrating the viability of our methodology for discovering tens of thousands of lenses in Euclid and LSST.

## DATA AVAILABILITY

As part of this publication, we are making the following data products publicly available:

**Table 3.** Recovery statistics of our methodology for different strong lensing candidate catalogs identified in the Dark Energy Survey. Rojas's A and B samples are high and low-confident strong lensing candidates, respectively.

SL Catalog	Total	Pre-selected	ML Recovered		ered CS Recovered		ML+CS Recovered
			Count	(%)	Count	(%)	(%)
Diehl et al. (2017)	376	129	75	58.1	66	88.0	51.2
O'Donnell et al. (2022)	252	94	68	72.3	58	85.3	61.7
Jacobs et al. (2019a,b)	511	457	371	81.2	329	88.7	72.0
Rojas et al. (2022) (A)	90	90	79	87.8	73	92.4	81.1
Rojas et al. (2022) (B)	315	315	164	52.1	127	77.5	40.3

Acronym definitions: ML = Machine Learning; CS = Citizen Science. The '%' of 'CS Recovered' is the percentage that citizens recovered from the sample selected by ML. 'ML+CS' is the workflow of applying visual inspection by CS to the output of ML.



Figure 20. Relationship between the number of images with ML scores exceeding a specified threshold (x-axis) and the number of good candidates among these images (y-axis). Candidates are separated by expert score thresholds. This figure illustrates the true-positive rate that can be achieved by our main ML model.

- A dataset containing ~236 million scores from our main ML model (Gonzalez et al. 2025). This includes the coordinates of the systems and the complete probability vector for the different training classes. This dataset is highly valuable for constructing training samples in future strong lensing searches. The dataset is hosted on Zenodo and can be accessed here.
- Expert Scores: ~2,600 coordinates and expert scores of all subjects inspected by our experts.
- Ensemble Scores: ~20,600 coordinates and ensemble scores for all subjects inspected by citizen scientists.

We extend our gratitude to the Zooniverse developers for their invaluable work in preparing and maintaining the platform, which was instrumental in facilitating this project. We also thank the citizen scientists for their vital contributions without which this project would be impossible. A full list of citizen scientists contributing to the classifications is given at the end of The Team section of our Zooniverse project.

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Contribution statement: JG designed this project, implemented the Vision Transformer architecture, created and labeled the training sample, led the execution of the project and wrote this publication. JG, KB, SB, RM, ADW, JHO, and EZ contributed to producing the cutout images subsequently analyzed by the machine learning models. JG, PH, and AV prepared and ran the Space Warps visual inspection project on Zooniverse. PH and AV analyzed the results from the platform. PH also generated the ensemble classifier using machine learning and citizen science scores. TC contributed to the writing and organization of this publication. KB provided guidance and advice throughout the execution of the project. AV, PM, AM, Space Warps PIs, offered feedback on the design of the citizen science visual inspection project, the image display settings, and the final ranking of candidates. JG, PH, AV, TL, CM, EMB and SB interacted with the citizens on 'Talk' responding to comments and helping citizens. JG, PH, JAB, GC, MM, TL, KR, and SS participated as experts in the second round of visual inspection. SB and TD served on the internal review committee for this publication, providing valuable feedback on the presentation of this work. SB and BN, co-conveners of the Strong Lensing group in DES, provided feedback on the execution of the project. The remaining authors contributed to this paper in various capacities, including the construction of DECam and other data collection instruments, data processing and calibration, developing broadly used methods, codes, and simulations, running pipelines and validation tests, and supporting the scientific analysis.

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### APPENDIX

In this section, we present Table 5, which summarizes key information about the strong lensing candidates in the A category. Additionally, we provide a complete table with this information for all subjects inspected by

our experts, available in a machine-readable format accompanying this publication.

**Table 5.** Strong lensing candidates in our A category. Ordered by increasing RA. ID is the 'COADD\_OBJECT\_ID', a unique object id for the object within the Y6 DES data release.

Name	ID	RA	DEC	Exp. score	References
DESJ000316-334804	1032630238	0.818284	-33.801233	2.68	Jacobs et al. (2019a,b)
DESJ000451-010318	1040460697	1.21556	-1.055098	2.55	Diehl et al. (2017); Jaelani et al. (2020); Rojas et al. (2022)
DESJ000816-323714	1040688993	2.067008	-32.620741	2.42	Khramtsov et al. (2019); Storfer et al. (2023)
DESJ001110-323704	1046194283	2.793084	-32.617921	2.29	This work
DESJ001542-463611	1054556683	3.928374	-46.603077	3.0	Jacobs et al. (2019a); Rojas et al. (2022)
DESJ002510-494626	1065068829	6.294487	-49.774042	2.72	O'Donnell et al. (2022); Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)
DESJ003104-440300	1075990880	7.770369	-44.050078	2.26	Diehl et al. (2017); Rojas et al. (2022)
DESJ003119-642037	1080776069	7.832104	-64.343818	2.41	Jacobs et al. (2019a)
DESJ003507-252658	1079483541	8.7806	-25.449639	2.83	Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ003727-413150	1083587736	9.362854	-41.530574	2.55	Diehl et al. (2017); Jacobs et al. (2019a); Rojas et al. (2022)
DESJ004109-004349	1088494058	10.287583	-0.730289	2.53	Jacobs et al. (2019a); Huang et al. (2020)
DESJ004144-233905	1093364977	10.434067	-23.651545	2.5	Huang et al. (2021)
DESJ004150-515750	1091516325	10.461274	-51.963971	2.3	Stein et al. (2022); Storfer et al. (2023)
DESJ004257-371858	1093259184	10.738893	-37.31623	2.71	Jacobs et al. (2019a)
DESJ004958+022714	1102641485	12.493282	2.454043	2.74	Stein et al. (2022); Storfer et al. (2023)
DESJ005736-484814	1120481923	14.403741	-48.803999	2.68	Diehl et al. (2017); O'Donnell et al. (2022)
DESJ005948-244220	1122534660	14.952536	-24.705638	2.58	Huang et al. $(2021)$
DESJ010519+014456	1135365822	16.331889	1.749025	2.87	Jacobs et al. (2019a); Huang et al. (2020)
DESJ010606-310437	1133540843	16.525913	-31.077073	2.27	Li et al. (2020); Huang et al. (2021); O'Donnell et al. (2022)
DESJ010659-443201	1136639478	16.746433	-44.533746	2.84	Jacobs et al. (2019a); Rojas et al. (2022)
DESJ010704-312840	1139453426	16.770516	-31.478048	2.83	Li et al. (2020); Huang et al. (2021); O'Donnell et al. (2022)
DESJ011333-381312	1147504166	18.389683	-38.220225	2.57	Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)
DESJ011408-361313	1151529929	18.534964	-36.220442	2.28	Jacobs et al. (2019a)
DESJ011646-243702	1153333586	19.194995	-24.61728	2.39	Jacobs et al. (2019a); Rojas et al. (2022)
DESJ011756-242824	1154333895	19.48702	-24.473544	2.27	Jacobs et al. (2019a)
DESJ011758-052717	1159257785	19.494912	-5.45495	2.37	Jacobs et al. (2019a); Huang et al. (2020); Rojas et al. (2022)
DESJ011842-615613	1162332513	19.677498	-61.937023	2.39	Jacobs et al. (2019a); Storfer et al. (2023)

Name	ID	$\mathbf{R}\mathbf{A}$	DEC	Exp. score	References
DESJ012025-182001	1164169304	20.107368	-18.333831	2.26	Jacobs et al. (2019a,b)
DESJ012042-514353	1163516688	20.176065	-51.731425	3.0	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020); Rojas et al. (2022)
DESJ012431-520703	1170335487	21.130103	-52.117501	2.48	Jacobs et al. (2019a)
DESJ012533-414217	1172896430	21.389999	-41.704998	2.83	Diehl et al. (2017); Jacobs et al. (2019a)
DESJ012611-131642	1173896612	21.549582	-13.278375	2.85	Jacobs et al. (2019a)
DESJ012753-453233	1178407449	21.971634	-45.542754	2.53	Jacobs et al. (2019a)
DESJ012933-150634	1176674664	22.388727	-15.109646	2.59	Huang et al. (2021); Rojas et al. (2022)
DESJ013002-374457	1179738251	22.512071	-37.749394	2.83	Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022); Storfer et al. (2023)
DESJ013026-152012	1177839322	22.610422	-15.336928	2.46	Jacobs et al. (2019a); Huang et al. (2020); Rojas et al. (2022); Storfer et al. (2023)
DESJ013050-160008	1178164184	22.710647	-16.002424	2.3	Jacobs et al. (2019a); Huang et al. (2020)
DESJ013322-125201	1300215437	23.342167	-12.867052	2.37	Jacobs et al. (2019a)
DESJ013354-643412	1186271916	23.47771	-64.57026	2.86	Jacobs et al. (2019a); O'Donnell et al. (2022)
DESJ013522-423223	1305035224	23.845168	-42.539875	2.56	Diehl et al. (2017); Jacobs et al. (2019a); Rojas et al. (2022)
DESJ013542-203335	1301081250	23.928359	-20.559886	2.25	Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ013822-284408	1309246601	24.595731	-28.735568	2.38	Jacobs et al. (2019a); Huang et al. (2021); O'Donnell et al. (2022); Ro- jas et al. (2022)
DESJ014134-404033	1307017630	25.391709	-40.675957	2.43	Jacobs et al. (2019a)
DESJ014234-164817	1301526898	25.64572	-16.804905	3.0	Jacobs et al. (2019a)
DESJ014252-183115	1620013669	25.720342	-18.521055	2.87	Jacobs et al. (2019a,b); Rojas et al. (2022)
DESJ014326-085021	1194748640	25.862212	-8.839277	2.68	Jacobs et al. (2019a,b); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ014433-114209	1195735476	26.138987	-11.70261	2.38	Jacobs et al. (2019a); Huang et al. (2020); Rojas et al. (2022)
DESJ014546-354127	1196484135	26.44499	-35.690953	2.87	Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ014556+040228	1194195904	26.484828	4.041358	2.59	Jacobs et al. (2019a); Huang et al. (2020); Rojas et al. (2022)
DESJ014655-092959	1311861257	26.731673	-9.499843	2.51	This work
DESJ014839-442555	1205436665	27.16306	-44.43212	2.68	Stein et al. (2022)
DESJ014908-313738	1200974180	27.283341	-31.627336	2.44	Jacobs et al. (2019a); Li et al. (2021)
DESJ015225-570359	1207637405	28.108001	-57.066558	2.68	Storfer et al. (2023)
DESJ015737-122138	1223104292	29.404393	-12.36064	2.31	Huang et al. (2021)
DESJ015824-003959	1224505431	29.603206	-0.666636	2.7	Jacobs et al. (2019a); Huang et al. (2020); O'Donnell et al. (2022); Shu et al. (2022)
DESJ020107-155117	1225062343	30.283231	-15.854756	2.61	Jacobs et al. (2019a); Huang et al. (2020); Rojas et al. (2022)
DESJ020134-603640	1227758667	30.392541	-60.611218	2.83	Stein et al. (2022)

Name	ID	RA	DEC	Exp. score	References
DESJ020144-273942	1229530106	30.436133	-27.661776	2.87	Jacobs et al. (2019a); Huang et al. (2021)
DESJ020304-233802	1235391858	30.766741	-23.634049	2.83	Jacobs et al. (2019a,b); Cañameras et al. (2020); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ020505-403830	1621099632	31.27143	-40.641747	2.83	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020); Rojas et al. (2022)
DESJ020526-353947	1234418937	31.358766	-35.66318	3.0	Jacobs et al. (2019a); Li et al. (2021); O'Donnell et al. (2022)
DESJ020611-372938	1240229572	31.547501	-37.494102	2.5	Stein et al. (2022); Storfer et al. (2023)
DESJ020706-272644	1243683190	31.777784	-27.445807	3.0	Jacobs et al. (2019a); Huang et al. (2021); Li et al. (2021); O'Donnell et al. (2022)
DESJ020954-354757	1248376493	32.477616	-35.79924	2.42	This work
DESJ021100-193810	1247965442	32.752503	-19.63615	2.6	Cañameras et al. (2020)
DESJ021514-290925	1255097893	33.809596	-29.157161	2.85	Jacobs et al. (2019a); Khramtsov et al. (2019); Huang et al. (2021)
DESJ021744-215834	1260779971	34.43687	-21.976185	2.26	Storfer et al. (2023)
DESJ022140-021020	1272147895	35.417247	-2.172297	2.26	Sonnenfeld et al. (2018); Jacobs et al. (2019a); Cañameras et al. (2021); Shu et al. (2022)
DESJ022148-642642	1264873479	35.453169	-64.445139	2.38	Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)
DESJ022310-224817	1270874866	35.794587	-22.804847	2.7	Huang et al. (2021); Rojas et al. (2022)
DESJ022809-125252	1282567543	37.03776	-12.881181	2.26	Jacobs et al. (2019a); Huang et al. (2020)
DESJ022930-290816	1286124138	37.379004	-29.137926	2.58	Jacobs et al. (2019a)
DESJ023249-032326	1287909989	38.207791	-3.390566	3.0	Diehl et al. (2017); Jacobs et al. (2019a); Huang et al. (2020); Jae- lani et al. (2020); Cañameras et al. (2021); Shu et al. (2022)
DESJ023341-344759	1294274501	38.422054	-34.79983	2.87	Li et al. (2021); Stein et al. (2022)
DESJ023906-204718	1321063152	39.776981	-20.788368	2.29	Jacobs et al. (2019a)
DESJ024328-214202	1326680132	40.866699	-21.700556	2.32	Jacobs et al. (2019a)
DESJ024604-060739	1331836609	41.520481	-6.12752	2.68	Huang et al. $(2020)$
DESJ024809-395548	1334070236	42.039764	-39.930101	2.28	Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022); Storfer et al. (2023)
DESJ024857-605403	1335051094	42.240122	-60.900967	2.29	Jacobs et al. (2019a)
DESJ025052-552411	1342755111	42.717888	-55.403254	2.27	Jacobs et al. (2019a); Rojas et al. (2022)
DESJ025623-270718	1358779892	44.097386	-27.121845	3.0	Jacobs et al. (2019a)
DESJ030639-273626	1368575074	46.665437	-27.607478	2.27	Petrillo et al. (2019); Huang et al. (2021)
DESJ031127-423219	1380201297	47.863261	-42.538645	2.53	Jacobs et al. (2019a); O'Donnell et al. (2022)
DESJ031638-223633	1441805121	49.161822	-22.609255	2.53	Jacobs et al. (2019a); Rojas et al. (2022)
DESJ031904-492143	1445784294	49.768511	-49.362018	2.25	Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)

Name	ID	$\mathbf{R}\mathbf{A}$	DEC	Exp. score	References
DESJ031906-273941	1444249631	49.778598	-27.66145	2.58	Huang et al. (2021)
DESJ031941-173404	1447194025	49.922007	-17.567922	2.83	Jacobs et al. (2019a)
DESJ032125-153003	1449752819	50.356635	-15.501013	2.34	Jacobs et al. (2019a)
DESJ032216-523440	1385113597	50.568423	-52.577903	2.87	Diehl et al. (2017); Jacobs et a (2019a); Nord et al. (2020); Roja et al. (2022)
DESJ032449-102053	1382896242	51.205155	-10.348143	2.72	Cañameras et al. (2020); Huan et al. (2021)
DESJ032711-324634	1386748971	51.797337	-32.776162	2.29	Jacobs et al. (2019a,b); Rojas et a (2022)
DESJ033056-522815	1395105474	52.734562	-52.47084	2.7	This work
DESJ033143-612315	1397305017	52.932554	-61.3875	2.56	Rojas et al. (2022); Stein et a (2022); Storfer et al. (2023)
DESJ033717-315213	1400483784	54.321876	-31.870435	3.0	Jacobs et al. (2019a); Rojas et a (2022)
DESJ034130-513045	1410370257	55.378418	-51.51253	2.45	Diehl et al. (2017); Jacobs et a (2019a); O'Donnell et al. (2022) Rojas et al. (2022)
DESJ034311-282840	1409295264	55.797722	-28.477789	2.42	Huang et al. (2021); ?); ?
DESJ034435-444744	1413196615	56.146233	-44.795611	2.83	Jacobs et al. (2019a)
DESJ034744-245431	1414531628	56.935597	-24.908735	2.42	Jacobs et al. (2019a,b); Rojas et a (2022)
DESJ035242-382544	1425127607	58.17678	-38.429166	3.0	Jacobs et al. (2019a); O'Donne et al. (2022); Rojas et al. (2022)
DESJ035337-402417	1423677815	58.405967	-40.404958	2.27	Diehl et al. (2017); Rojas et a (2022)
DESJ035346-170639	1423965682	58.442713	-17.110922	2.83	Jacobs et al. (2019a); Cañamera et al. (2020)
DESJ035418-160952	1425763095	58.576161	-16.164526	2.87	Jacobs et al. (2019a,b); Rojas et a (2022)
DESJ035510-183134	1427368966	58.792571	-18.52621	2.29	Huang et al. $(2021)$
DESJ035649-240841	1429256248	59.204423	-24.144758	2.39	Jacobs et al. (2019a); O'Donne et al. (2022); Rojas et al. (2022)
DESJ035713-475652	1432852433	59.306552	-47.948003	2.72	This work
DESJ040624-264624	1453825350	61.601641	-26.773339	3.0	Jacobs et al. (2019a)
DESJ040715-571303	1458095582	61.815154	-57.217543	2.83	Jacobs et al. (2019a); Storfer et a (2023)
DESJ040822-532714	1454069093	62.094448	-53.453918	2.83	Diehl et al. (2017); Rojas et a (2022)
DESJ041112-541320	1462051999	62.802003	-54.222443	2.26	Rojas et al. (2022)
DESJ041242-264632	1616630786	63.178811	-26.775662	2.87	Jacobs et al. (2019a)
DESJ041644-552500	1466200592	64.186786	-55.416745	2.55	Diehl et al. (2017); Jacobs et a (2019a); O'Donnell et al. (2022)
DESJ041809-545734	1466401262	64.541216	-54.959696	2.59	Diehl et al. (2017); Jacobs et a (2019a); Nord et al. (2020); Roj et al. (2022)
DESJ042048-563046	1468847242	65.201028	-56.51302	2.54	Storfer et al. (2023)
DESJ042218-213245	1470342587	65.575916	-21.546111	2.85	Jacobs et al. (2019a,b); Rojas et a (2022)
DESJ042723-290743	1481457559	66.848597	-29.128656	2.83	This work
DESJ043303-271423	1491366260	68.26478	-27.239827	3.0	Jacobs et al. (2019a)
DESJ043806-322852	1493630017	69.525777	-32.481174	2.69	Jacobs et al. (2019a)

Name	ID	RA	DEC	Exp. score	References
DESJ044747-304630	1505802492	71.94812	-30.775079	2.41	This work
DESJ044805-580721	1505900316	72.022081	-58.122569	2.27	Diehl et al. (2017); Jacobs et al. (2019a); Rojas et al. (2022)
DESJ045008-571519	1510652342	72.536758	-57.255536	3.0	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020)
DESJ045352-502234	1516572409	73.470762	-50.376362	2.56	Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)
DESJ045951-304324	1523439802	74.964266	-30.723591	2.55	Huang et al. (2021); Rojas et al. (2022)
DESJ050849-214430	1536678003	77.205297	-21.741881	2.37	Jacobs et al. (2019a,b)
DESJ051314-523020	1538255919	78.3096	-52.505683	2.55	Rojas et al. (2022); Storfer et al. (2023)
DESJ051325-305035	1540902420	78.356147	-30.843306	3.0	Huang et al. (2021); O'Donnell et al. (2022)
DESJ052700-185805	1559106390	81.753525	-18.96833	2.28	This work
DESJ053804-473513	1569046306	84.51926	-47.587146	2.5	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020); Rojas et al. (2022)
DESJ054735-600442	1584250649	86.897808	-60.078518	2.37	Diehl et al. (2017); Rojas et al. (2022)
DESJ054848-421254	1588997152	87.200728	-42.215103	2.3	Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)
DESJ055734-415950	1591517201	89.393433	-41.997283	2.43	Jacobs et al. (2019a); Storfer et al. (2023)
DESJ060239-465307	1601363180	90.662686	-46.885496	2.25	Diehl et al. $(2017)$
DESJ060246-452443	1597714254	90.695238	-45.411976	2.87	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020)
DESJ060443-414837	1599167680	91.180479	-41.810311	2.27	Storfer et al. (2023)
DESJ060653-585843	1604164262	91.721436	-58.978777	2.87	Rojas et al. (2022); Stein et al. (2022); Storfer et al. (2023)
DESJ062415-470942	1610316947	96.065874	-47.161667	2.29	Jacobs et al. (2019a,b); Rojas et al. (2022)
DESJ203911-545942	895557306	309.797344	-54.995216	2.28	Diehl et al. (2017); Jacobs et al. (2019a); Rojas et al. (2022)
DESJ211005-563930	909363984	317.522564	-56.658496	2.27	Diehl et al. (2017); Jacobs et al. (2019a)
DESJ211627-594701	913936319	319.113845	-59.783864	2.87	Jacobs et al. (2019a)
DESJ212251-005949	918844670	320.716645	-0.997037	2.38	Diehl et al. (2017); O'Donnell et al. (2022)
DESJ212427-612510	919882930	321.113269	-61.419484	3.0	O'Donnell et al. (2022); Storfer et al. (2023)
DESJ213054-485714	925546537	322.727846	-48.954092	2.56	Stein et al. $(2022)$
DESJ221912-434835	958711616	334.801696	-43.809809	2.83	Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ224434-590910	974192911	341.144978	-59.152836	2.26	Stein et al. (2022); Storfer et al. (2023)
DESJ225403-405549	981794120	343.512752	-40.930347	2.42	Diehl et al. (2017); Jacobs et al. (2019a); Rojas et al. (2022)
DESJ230521-000211	995519978	346.34027	-0.036597	2.86	Wong et al. (2018); Jacobs et al. (2019a); Cañameras et al. (2021); Shu et al. (2022)
DESJ232128-463049	1005730815	350.368333	-46.513736	2.83	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020); Rojas et al. (2022)

Name	ID	RA	DEC	Exp. score	References
DESJ233459-640407	1015482810	353.746734	-64.068626	3.0	Jacobs et al. (2019a); Rojas et al. (2022)
DESJ233551-515217	1015396778	353.966419	-51.871635	2.68	Diehl et al. (2017); Jacobs et al. (2019a); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ234930-511339	1027961497	357.375315	-51.22754	3.0	Diehl et al. (2017); Jacobs et al. (2019a); Nord et al. (2020); O'Donnell et al. (2022); Rojas et al. (2022)
DESJ235717-571025	1031154124	359.323497	-57.173869	2.39	Jacobs et al. (2019a)
DESJ235848-612558	1033271849	359.700322	-61.433041	2.83	Huang et al. (2021); O'Donnell et al. (2022)

## REFERENCES

- Alard, C. 2006, Automated detection of gravitational arcs. https://arxiv.org/abs/astro-ph/0606757
- Amershi, S., Cakmak, M., Knox, W. B., & Kulesza, T. 2014, AI Magazine, 35, 105,

doi: 10.1609/aimag.v35i4.2513

- Barroso, J. A. A., O'Riordan, C. M., Clément, B., et al. 2024, Euclid: The Early Release Observations Lens Search Experiment. https://arxiv.org/abs/2408.06217
- Birrer, S., & Amara, A. 2018, Lenstronomy: multi-purpose gravitational lens modelling software package, doi: https://doi.org/10.1016/j.dark.2018.11.002

Birrer, S., Shajib, A. J., Galan, A., et al. 2020, Astronomy & amp; Astrophysics, 643, A165, doi: 10.1051/0004-6361/202038861

- Birrer, S., Shajib, A. J., Gilman, D., et al. 2021, Journal of Open Source Software, 6, 3283, doi: 10.21105/joss.03283
- Cañameras, R., Schuldt, S., Suyu, S. H., et al. 2020, A&A, 644, A163, doi: 10.1051/0004-6361/202038219
- Cañameras, R., Schuldt, S., Shu, Y., et al. 2021, A&A, 653, L6, doi: 10.1051/0004-6361/202141758
- Cañameras, R., Schuldt, S., Suyu, S. H., et al. 2020, A&A, 644, A163, doi: 10.1051/0004-6361/202038219
- Cheng, T.-Y., Conselice, C. J., Aragón-Salamanca, A., et al. 2021, Monthly Notices of the Royal Astronomical Society, 507, 4425–4444, doi: 10.1093/mnras/stab2142
- Collett, T. E. 2015, The Astrophysical Journal, 811, 20, doi: 10.1088/0004-637X/811/1/20
- Collett, T. E., & Auger, M. W. 2014, Monthly Notices of the Royal Astronomical Society, 443, 969–976, doi: 10.1093/mnras/stu1190
- Collett, T. E., Auger, M. W., Belokurov, V., Marshall, P. J., & Hall, A. C. 2012, Monthly Notices of the Royal Astronomical Society, 424, 2864–2875, doi: 10.1111/j.1365-2966.2012.21424.x

- Collett, T. E., & Bacon, D. J. 2015, Monthly Notices of the Royal Astronomical Society, 456, 2210–2220, doi: 10.1093/mnras/stv2791
- Deng, J., Dong, W., Socher, R., et al. 2009, in 2009 IEEE Conference on Computer Vision and Pattern Recognition, 248–255, doi: 10.1109/CVPR.2009.5206848
- DES Collaboration, Abbott, T. M. C., Adamów, M., et al. 2021, The Astrophysical Journal Supplement Series, 255, 20, doi: 10.3847/1538-4365/ac00b3
- Diehl, H. T., Buckley-Geer, E. J., Lindgren, K. A., et al. 2017, The Astrophysical Journal Supplement Series, 232, 15, doi: 10.3847/1538-4365/aa8667
- Diehl, H. T., Buckley-Geer, E. J., Lindgren, K. A., et al. 2017, ApJS, 232, 15, doi: 10.3847/1538-4365/aa8667
- Domínguez Sánchez, H., Huertas-Company, M., Bernardi, M., Tuccillo, D., & Fischer, J. L. 2018, Monthly Notices of the Royal Astronomical Society, 476, 3661–3676, doi: 10.1093/mnras/sty338
- Dosovitskiy, A., Beyer, L., Kolesnikov, A., et al. 2021, An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale. https://arxiv.org/abs/2010.11929
- Fassnacht, C. D., Moustakas, L. A., Casertano, S., et al. 2004, The Astrophysical Journal, 600, L155, doi: 10.1086/379004
- Fassnacht, C. D., McKean, J. P., Koopmans, L. V. E., et al. 2006, The Astrophysical Journal, 651, 667, doi: 10.1086/507623
- Faure, C., Kneib, J.-P., Covone, G., et al. 2008, The Astrophysical Journal Supplement Series, 176, 19, doi: 10.1086/526426
- Flaugher, B., Diehl, H. T., Honscheid, K., et al. 2015, The Astronomical Journal, 150, 150, doi: 10.1088/0004-6256/150/5/150

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Gavazzi, R., Marshall, P. J., Treu, T., & Sonnenfeld, A. 2014, The Astrophysical Journal, 785, 144, doi: 10.1088/0004-637X/785/2/144

Gavazzi, R., Treu, T., Koopmans, L. V. E., et al. 2008, The Astrophysical Journal, 677, 1046, doi: 10.1086/529541

Gonzalez, J., Holloway, P., Collett, T., et al. 2025, Strong Lensing Search: 236 Million Multiclass ML Scores, Zenodo, doi: 10.5281/zenodo.14588719

Grespan, M., Thuruthipilly, H., Pollo, A., et al. 2024, Astronomy & amp; Astrophysics, 688, A34, doi: 10.1051/0004-6361/202449929

Holloway, P., Marshall, P. J., Verma, A., et al. 2024, MNRAS, 530, 1297, doi: 10.1093/mnras/stae875

Huang, X., Storfer, C., Ravi, V., et al. 2020, The Astrophysical Journal, 894, 78, doi: 10.3847/1538-4357/ab7ffb

Huang, X., Storfer, C., Ravi, V., et al. 2020, ApJ, 894, 78, doi: 10.3847/1538-4357/ab7ffb

Huang, X., Storfer, C., Gu, A., et al. 2021, The Astrophysical Journal, 909, 27, doi: 10.3847/1538-4357/abd62b

Huang, X., Storfer, C., Gu, A., et al. 2021, ApJ, 909, 27, doi: 10.3847/1538-4357/abd62b

Huertas-Company, M., & Lanusse, F. 2023, Publications of the Astronomical Society of Australia, 40, doi: 10.1017/pasa.2022.55

Jackson, N. 2008, Monthly Notices of the Royal Astronomical Society, 389, 1311, doi: 10.1111/j.1365-2966.2008.13629.x

Jacobs, C., Collett, T., Glazebrook, K., et al. 2019a, The Astrophysical Journal Supplement Series, 243, 17, doi: 10.3847/1538-4365/ab26b6

—. 2019b, Monthly Notices of the Royal Astronomical Society, 484, 5330, doi: 10.1093/mnras/stz272

Jacobs, C., Collett, T., Glazebrook, K., et al. 2019a, ApJS, 243, 17, doi: 10.3847/1538-4365/ab26b6

-. 2019b, MNRAS, 484, 5330, doi: 10.1093/mnras/stz272

Jaelani, A. T., More, A., Oguri, M., et al. 2020, MNRAS, 495, 1291, doi: 10.1093/mnras/staa1062

Jiang, L., Liu, S., & Chen, C. 2018, Recent Research Advances on Interactive Machine Learning. https://arxiv.org/abs/1811.04548

Kelly, P. L., Rodney, S., Treu, T., et al. 2023, Science, 380, doi: 10.1126/science.abh1322

Khramtsov, V., Sergeyev, A., Spiniello, C., et al. 2019, A&A, 632, A56, doi: 10.1051/0004-6361/201936006

Li, R., Napolitano, N. R., Tortora, C., et al. 2020, The Astrophysical Journal, 899, 30, doi: 10.3847/1538-4357/ab9dfa Li, R., Napolitano, N. R., Tortora, C., et al. 2020, ApJ, 899, 30, doi: 10.3847/1538-4357/ab9dfa Li, R., Napolitano, N. R., Spiniello, C., et al. 2021, ApJ, 923, 16, doi: 10.3847/1538-4357/ac2df0 Li, T., Collett, T. E., Krawczyk, C. M., & Enzi, W. 2023, Cosmology from Large Populations of Galaxy-Galaxy Strong Gravitational Lenses. https://arxiv.org/abs/2307.09271 Linder, E. V. 2016, Physical Review D, 94, doi: 10.1103/physrevd.94.083510 Marshall, P. J., Verma, A., More, A., et al. 2016a, MNRAS, 455, 1171, doi: 10.1093/mnras/stv2009 —. 2016b, MNRAS, 455, 1171, doi: 10.1093/mnras/stv2009 Metcalf, R. B., Meneghetti, M., Avestruz, C., et al. 2019, A&A, 625, A119, doi: 10.1051/0004-6361/201832797 More, A., Cabanac, R., More, S., et al. 2012, The Astrophysical Journal, 749, 38, doi: 10.1088/0004-637X/749/1/38 More, A., Jahnke, K., More, S., et al. 2011, The Astrophysical Journal, 734, 69, doi: 10.1088/0004-637X/734/1/69 More, A., Verma, A., Marshall, P. J., et al. 2016, MNRAS, 455, 1191, doi: 10.1093/mnras/stv1965 Moustakas, L. A., Marshall, P., Newman, J. A., et al. 2007, The Astrophysical Journal, 660, L31, doi: 10.1086/517930 Newton, E. R., Marshall, P. J., & Treu, T. 2009, The Astrophysical Journal, 696, 1125, doi: 10.1088/0004-637X/696/2/1125 Nord, B., Buckley-Geer, E., Lin, H., et al. 2020, MNRAS, 494, 1308, doi: 10.1093/mnras/staa200 O'Donnell, J. H., Wilkinson, R. D., Diehl, H. T., et al. 2022, ApJS, 259, 27, doi: 10.3847/1538-4365/ac470b OSG. 2006, OSPool, OSG, doi: 10.21231/906P-4D78 —. 2015, Open Science Data Federation, OSG, doi: 10.21231/0KVZ-VE57 O'Donnell, J. H., Wilkinson, R. D., Diehl, H. T., et al. 2022, The Astrophysical Journal Supplement Series, 259, 27, doi: 10.3847/1538-4365/ac470b Pan, S. J., & Yang, Q. 2010, IEEE Transactions on Knowledge and Data Engineering, 22, 1345, doi: 10.1109/TKDE.2009.191 Pascale, M., Frye, B. L., Pierel, J. D. R., et al. 2024, SN H0pe: The First Measurement of  $H_0$  from a Multiply-Imaged Type Ia Supernova, Discovered by JWST. https://arxiv.org/abs/2403.18902

Petrillo, C. E., Tortora, C., Vernardos, G., et al. 2019, Monthly Notices of the Royal Astronomical Society, 484, 3879, doi: 10.1093/mnras/stz189

Petrillo, C. E., Tortora, C., Vernardos, G., et al. 2019, MNRAS, 484, 3879, doi: 10.1093/mnras/stz189 Pordes, R., Petravick, D., Kramer, B., et al. 2007, in 78, Vol. 78, J. Phys. Conf. Ser., 012057, doi: 10.1088/1742-6596/78/1/012057

- Rojas, K., Savary, E., Clément, B., et al. 2022, A&A, 668, A73, doi: 10.1051/0004-6361/202142119
- Rojas, K., Savary, E., Clément, B., et al. 2022, A&A, 668, A73, doi: 10.1051/0004-6361/202142119

Rozo, E., Rykoff, E. S., Abate, A., et al. 2016, Monthly Notices of the Royal Astronomical Society, 461, 1431, doi: 10.1093/mnras/stw1281

Sérsic, J. 1963, Boletín de la Asociación Argentina de Astronomía

Sfiligoi, I., Bradley, D. C., Holzman, B., et al. 2009, in 2, Vol. 2, 2009 WRI World Congress on Computer Science and Information Engineering, 428–432, doi: 10.1109/CSIE.2009.950

- Shajib, A. J., Birrer, S., Treu, T., et al. 2020a, Monthly Notices of the Royal Astronomical Society, 494, 6072, doi: 10.1093/mnras/staa828
- —. 2020b, Monthly Notices of the Royal Astronomical Society, 494, 6072, doi: 10.1093/mnras/staa828
- Shajib, A. J., Vernardos, G., Collett, T. E., et al. 2024, Strong Lensing by Galaxies. https://arxiv.org/abs/2210.10790

Sharma, D., Collett, T. E., & Linder, E. V. 2023, Journal of Cosmology and Astroparticle Physics, 2023, 001, doi: 10.1088/1475-7516/2023/04/001

- Shu, Y., Cañameras, R., Schuldt, S., et al. 2022, A&A, 662, A4, doi: 10.1051/0004-6361/202243203
- Shu, Y., Cañameras, R., Schuldt, S., et al. 2022, A&A, 662, A4, doi: 10.1051/0004-6361/202243203
- Sonnenfeld, A., Chan, J. H. H., Shu, Y., et al. 2018, PASJ, 70, S29, doi: 10.1093/pasj/psx062

Stein, G., Blaum, J., Harrington, P., Medan, T., & Lukić, Z. 2022, ApJ, 932, 107, doi: 10.3847/1538-4357/ac6d63

Storfer, C., Huang, X., Gu, A., et al. 2023, New Strong Gravitational Lenses from the DESI Legacy Imaging Surveys Data Release 9. https://arxiv.org/abs/2206.02764

Tanaka, M., Wong, K. C., More, A., et al. 2016, The Astrophysical Journal Letters, 826, L19, doi: 10.3847/2041-8205/826/2/L19

The LSST Dark Energy Science Collaboration, Mandelbaum, R., Eifler, T., et al. 2021, The LSST Dark Energy Science Collaboration (DESC) Science Requirements Document. https://arxiv.org/abs/1809.01669

- Thuruthipilly, H., Grespan, M., & Zadrożny, A. 2024, in AIP Conference Proceedings (AIP Publishing), doi: 10.1063/5.0203317
- Vaswani, A., Shazeer, N., Parmar, N., et al. 2023, Attention Is All You Need. https://arxiv.org/abs/1706.03762

Walmsley, M., Géron, T., Kruk, S., et al. 2023, Galaxy Zoo DESI: Detailed Morphology Measurements for 8.7M Galaxies in the DESI Legacy Imaging Surveys. https://arxiv.org/abs/2309.11425

Walsh, D., Carswell, R. F., & Weymann, R. J. 1979, Nature, 279, 381, doi: 10.1038/279381a0

Wightman, R. 2019, PyTorch Image Models, https://github.com/rwightman/pytorch-image-models, GitHub, doi: 10.5281/zenodo.4414861

Wong, K. C., Sonnenfeld, A., Chan, J. H. H., et al. 2018, ApJ, 867, 107, doi: 10.3847/1538-4357/aae381

Wong, K. C., Suyu, S. H., Chen, G. C.-F., et al. 2019, Monthly Notices of the Royal Astronomical Society, 498, 1420–1439, doi: 10.1093/mnras/stz3094

Zaborowski, E. A., Drlica-Wagner, A., Ashmead, F., et al. 2023, The Astrophysical Journal, 954, 68, doi: 10.3847/1538-4357/ace4ba