



Demonstrating the Potential of Adaptive LMS Filtering on FPGA-Based Qubit Control Platforms for Improved Qubit Readout in 2D and 3D Quantum Processing Units

IEEE Quantum Week 2024: QCE24 Submission 416

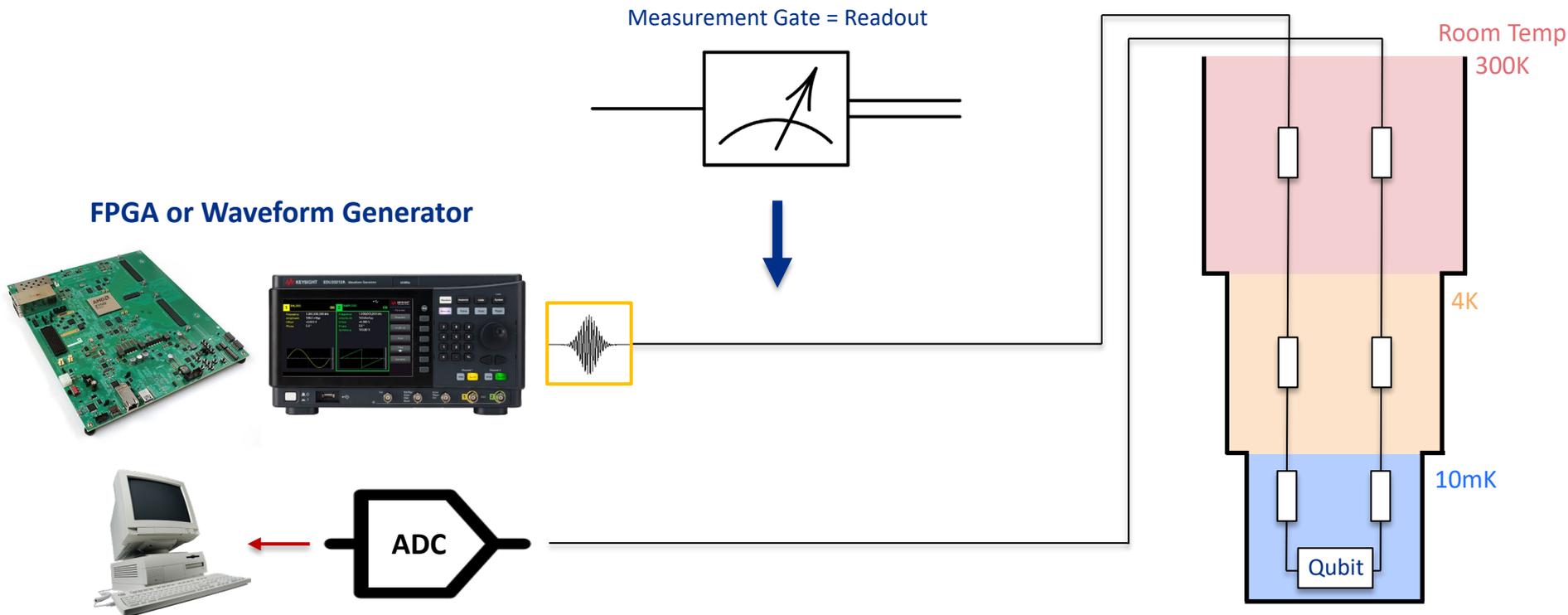
Presenter: Hans Johnson

Authors: Hans Johnson, Nicholas Bornman, Taeyoon Kim, David Van Zanten, Silvia Zorzetti, Jafar Saniie

Introduction

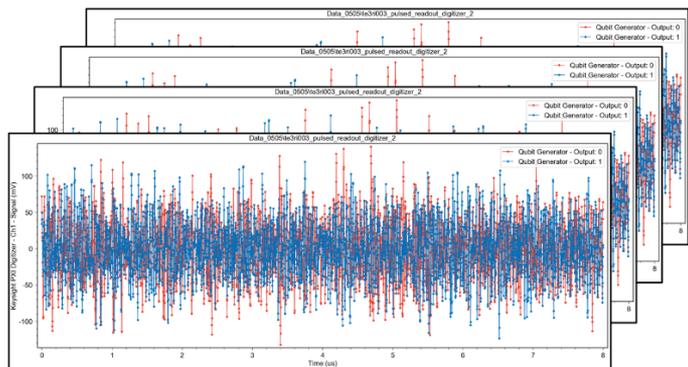
(Least Means Squared)

- Goal: **Improving Qubit Readout Through Adaptive LMS Filtering!**



Current Methodology

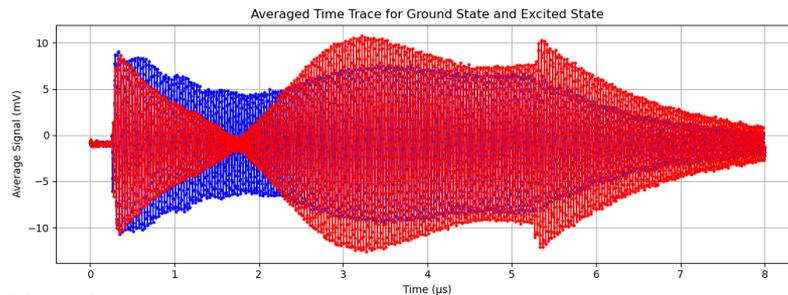
- **Readout pulses are very noisy!**
- The current method to average readout pulses in post processing for qubit readout works for smaller systems. **However, this has limitations as qubit systems scale up.**



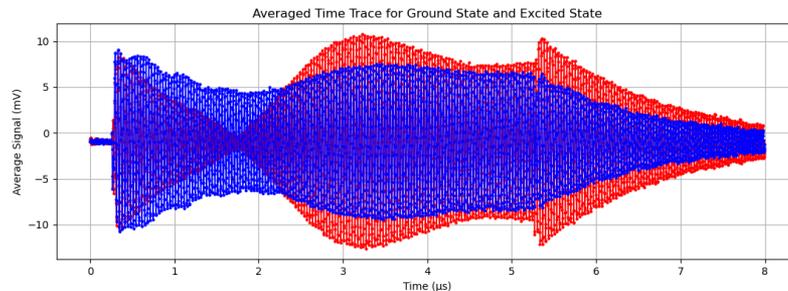
Phase Sweep @ ~6.3 GHz for single-shot time trace readout



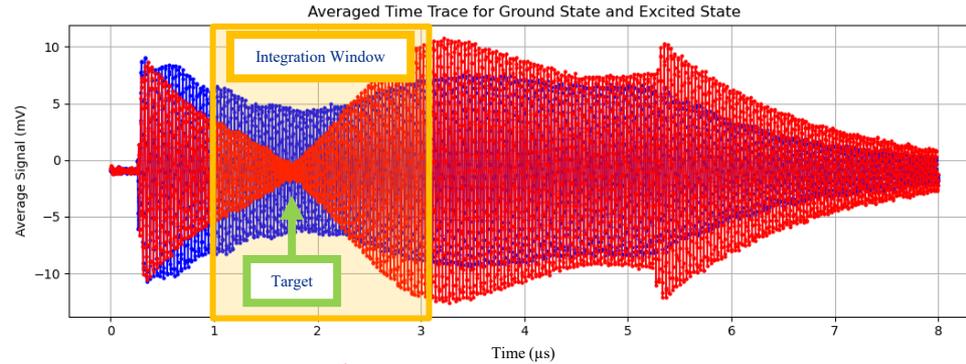
100,000 averages



Ground State
Excited State



Qubit Calibration



Ground State
Excited State

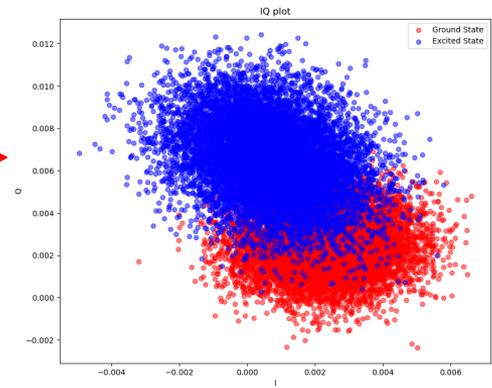
Extract I,Q from signal

Input signal from digitizer : $s[n] = A \cos(\Omega_{IF}n + \phi)$
 Qubit state information is encoded in A, ϕ .
 We need to extract A, ϕ (equivalently $I = A \cos(\phi), Q = A \sin(\phi)$)

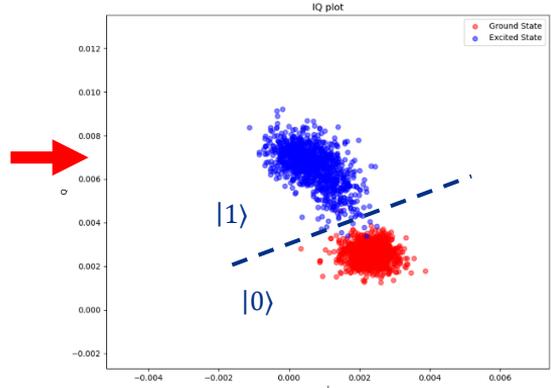
$$\sum_n s[n] e^{-i\Omega_{IF}n} = \sum_n A \cos(\Omega_{IF}n + \phi) (\cos(\Omega_{IF}n) - i \sin(\Omega_{IF}n))$$

$$= I + i Q + (\text{averaged to zero})$$

1 dot = 10 traces



1 dot = 100 traces



Why Filter Readout Signals?

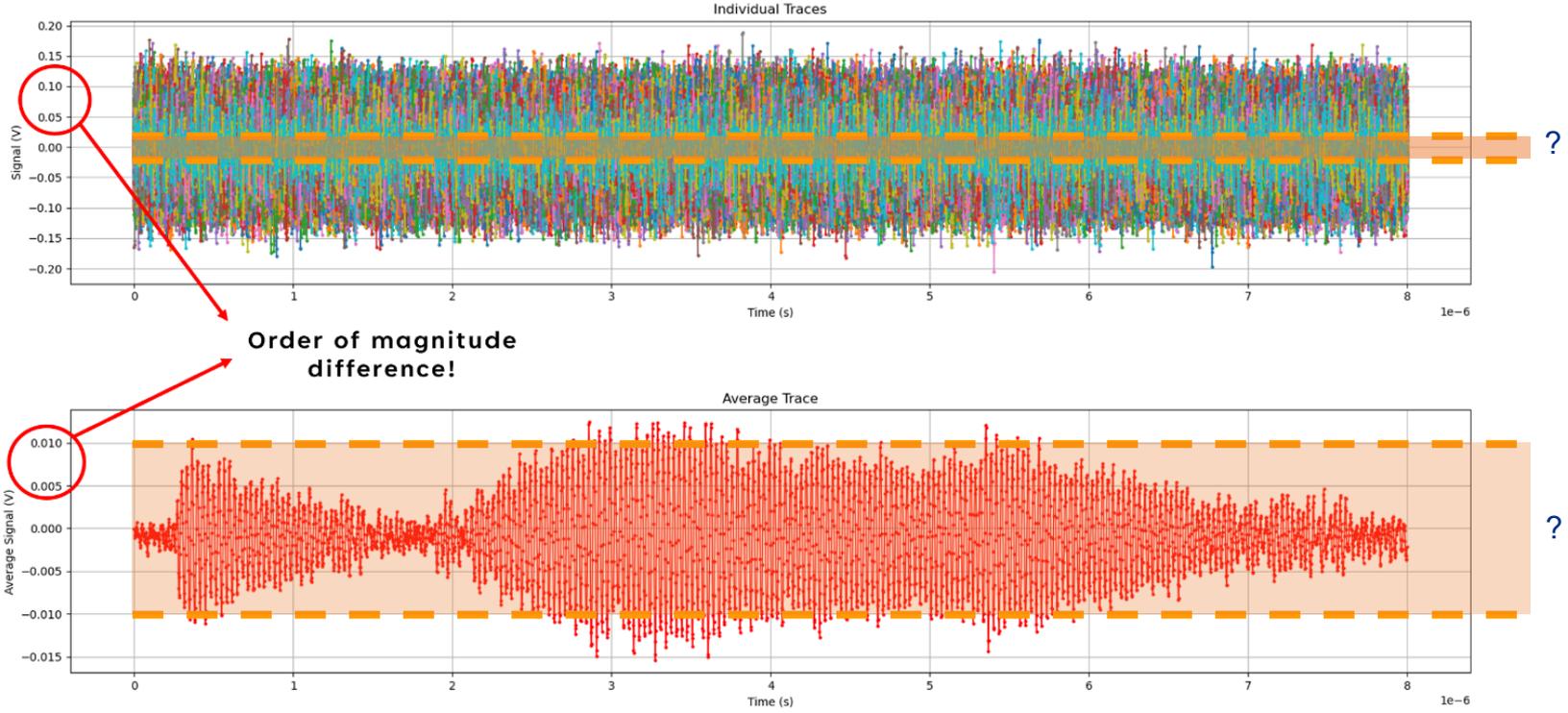
1. Filtered signals = faster convergence to the **center of mass** for the IQ plots.
 - By filtering readout signals on a pulse-by-pulse basis, we reduce the noise in each individual trace before averaging.
 - We can achieve the same level of discrimination with fewer traces or achieve better readout fidelity with the same number of traces.

Larger qubit systems = frequency-multiplexing = increased readout crosstalk...

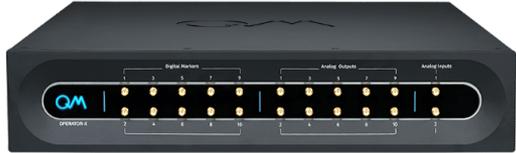
Therefore, faster calibrations are important for larger qubit systems

2. Enables us to have a new diagnostic tool for quantum system environment and noise monitoring.
 - Result of using an adaptive filter... more on this later!

Why an LMS Filter?

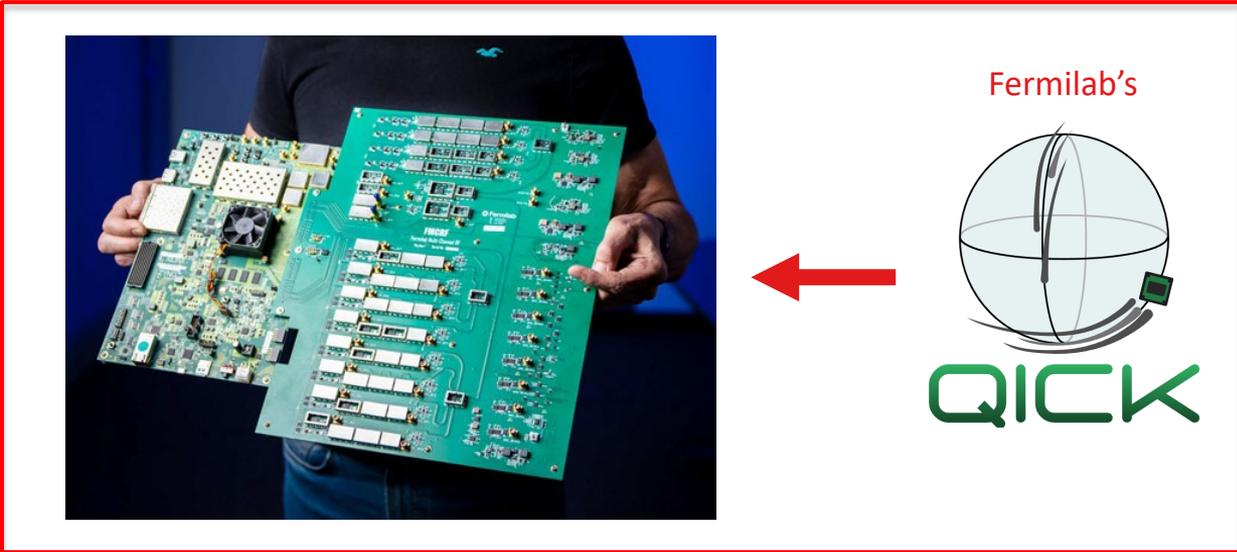


Commercial Solutions



Open-Source Solutions on FPGA

Lawrence Berkeley
National Lab's
QubiC



Fermilab's



FPGA Quantum Controller

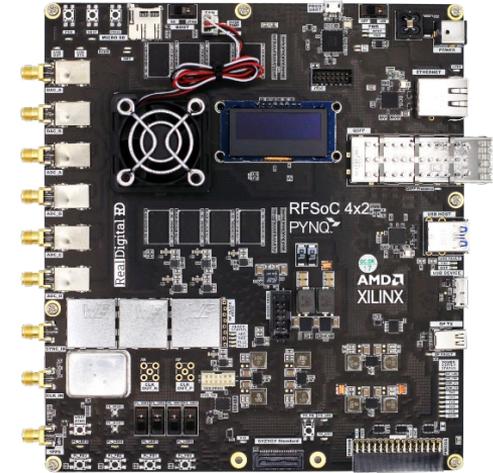
ZCU111



ZCU216



RFSoc 4x2



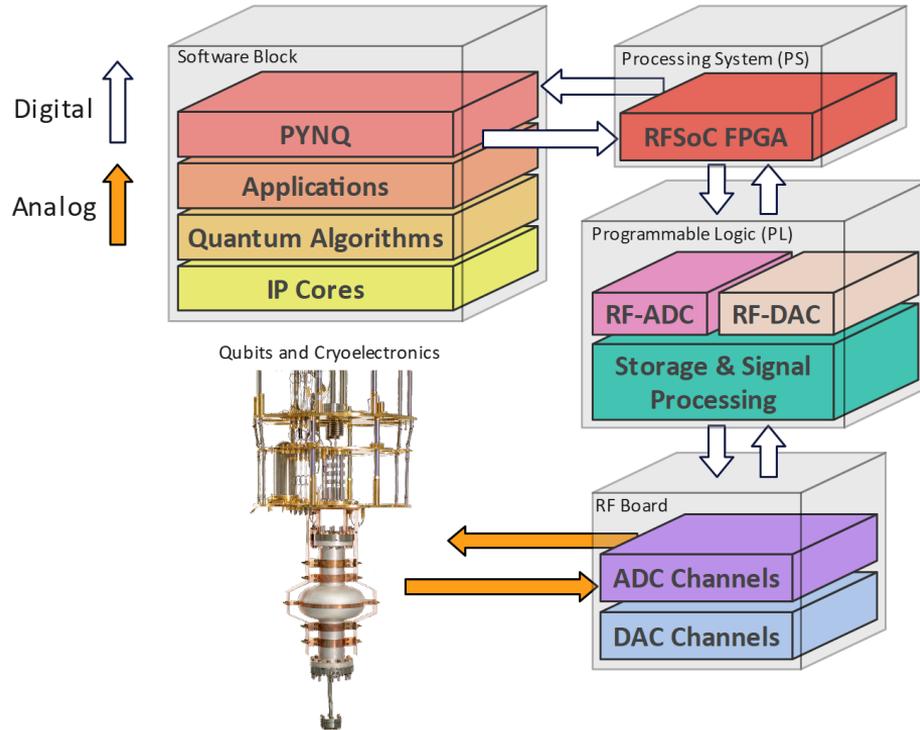
- Gen 1
- Max Control Pulse carrier frequency = 6 GHz
- Eight 14-bit DACs @ 6.5 GSPS
- Eight 12-bit ADCs @ 4.096 GSPS

- Gen 3
- Max Control Pulse carrier frequency = 10 GHz
 - Can push to 12-13 GHz
- Sixteen 14-bit DACs @ 9.85 GSPS
- Sixteen 14-bit ADCs @ 2.5 GSPS
 - Can be combined for 5.0 GSPS

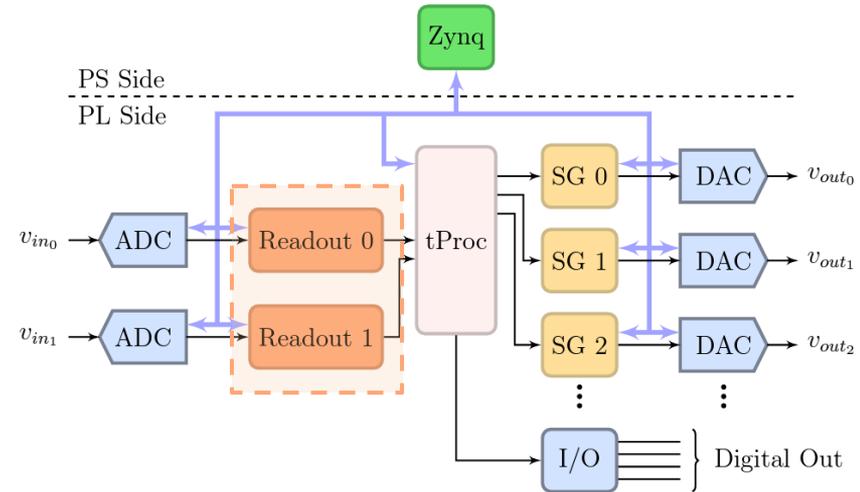
- Gen 3
- Max Control Pulse carrier frequency = 10 GHz
 - Can push to 12-13 GHz
- Two 14-bit DACs @ 9.85 GSPS
- Four 14-bit ADCs @ 5.0 GSPS

Firmware and Readout Chain Overview

Block Diagram of System

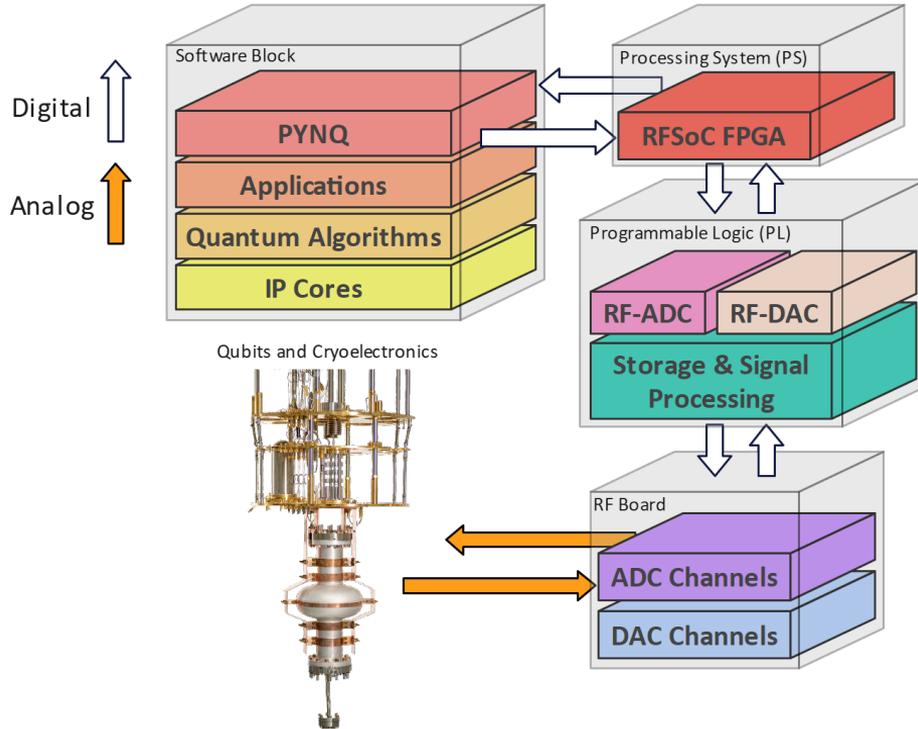


Block Diagram of QICK Firmware

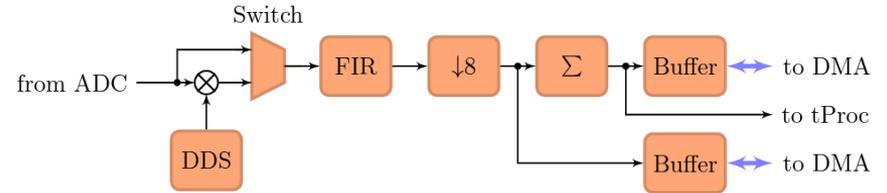


Firmware and Readout Chain Overview

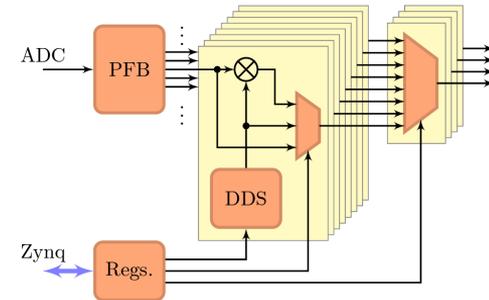
Block Diagram of System



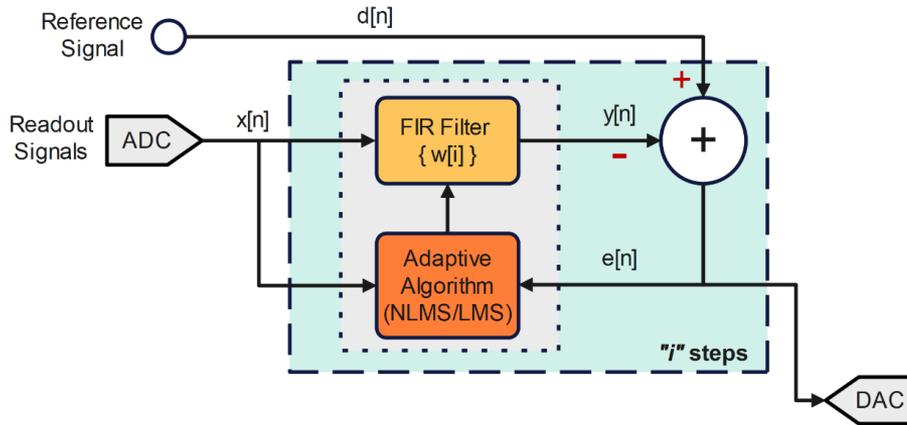
QICK Readout Chain (v1)



QICK Readout Chain (v2 = multiplexed)



LMS Filter



- n : Sample index
- i : Tap index within the filter's impulse response
- $x[n]$: Noisy input signal
- $d[n]$: Desired/reference signal
- $w[i]$: Weights = adjustable weights of LMS
- $y[n]$: Output signal (estimated signal or noise estimation) at time index $[n]$
- $e[n]$: error signal (difference between desired and output signals) at time index $[n]$
- μ : Learning rate of LMS algorithm
- N : number of taps in the filter, dictating the number of past input samples used by the filter

$$w[i + 1] = w[i] + \mu * e[n] * x[n - i] \quad (1)$$

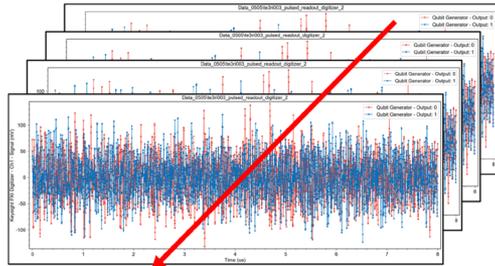
$$y[n] = \sum_{i=0}^{N-1} w[i] * x[n - i] \quad (2)$$

$$e[n] = d[n] - y[n] \quad (3)$$

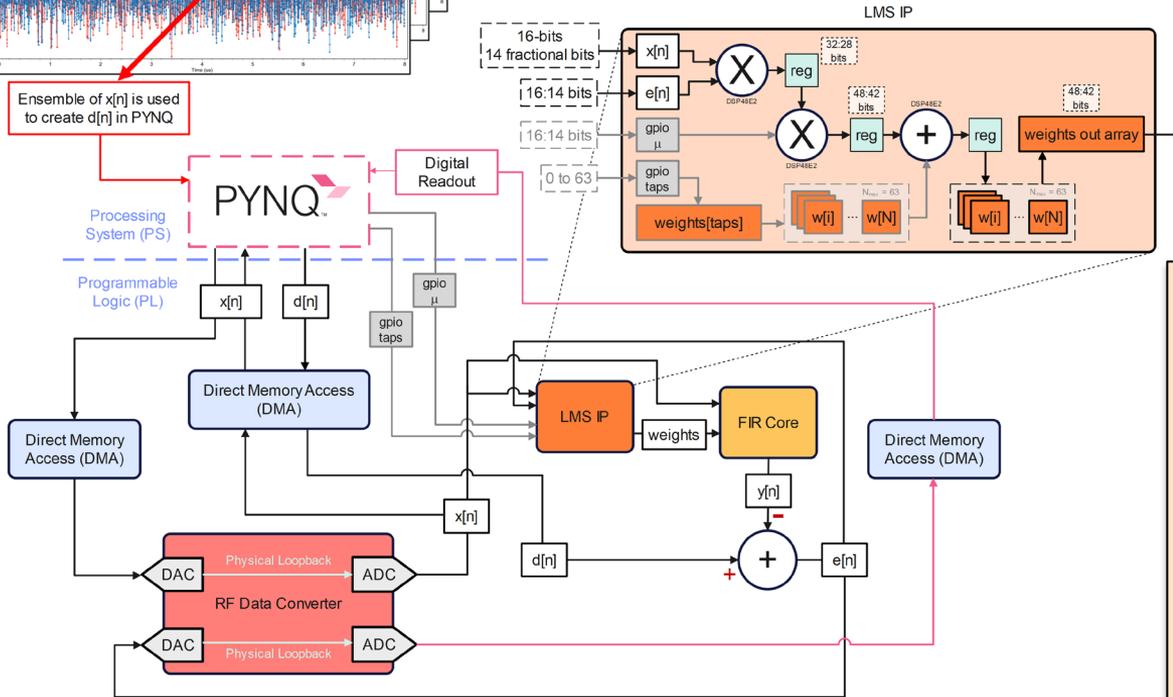
LMS Demo

Equation (4)

- The purpose of the demo was to prove the efficacy of the LMS algorithm on FPGA.



Ensemble of $x[n]$ is used to create $d[n]$ in PYNQ



$$w[i + 1] = w[i] + \mu * e[n] * x[n - i] \quad (1)$$

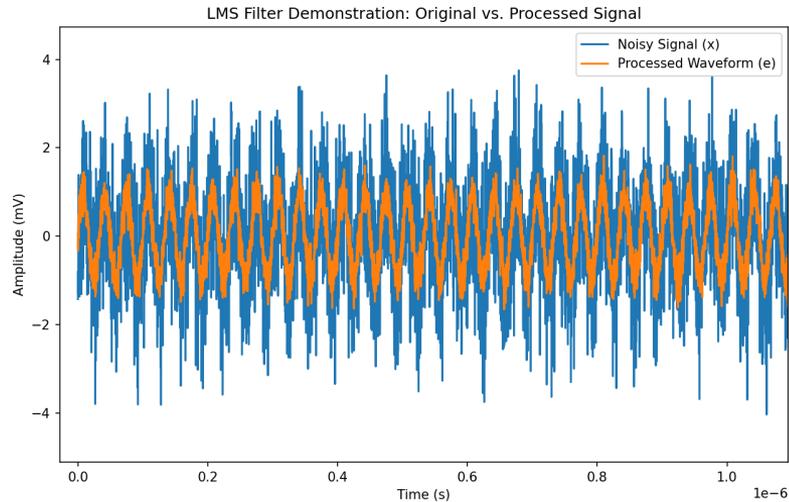
$$y[n] = \sum_{i=0}^{N-1} w[i] * x[n - i] \quad (2)$$

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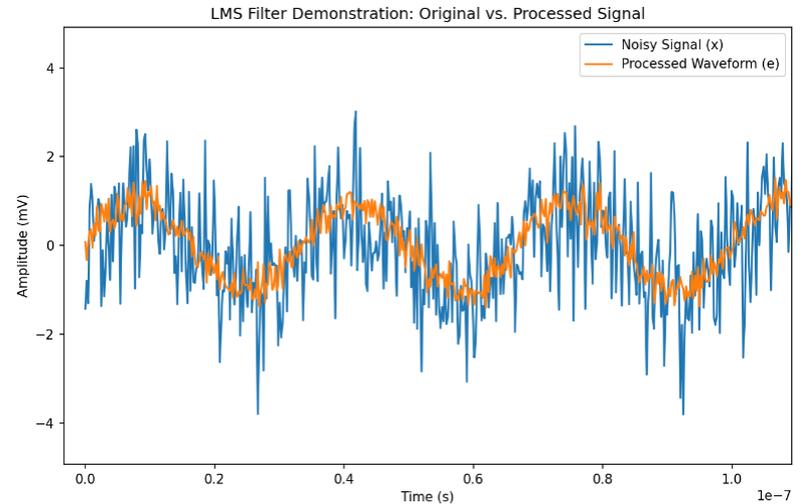
$$d_{new}[n] = \frac{(d_{old}[n] * i) + x_{new}[n]}{i + 1} \quad (4)$$

Results: LMS Filter Demonstration on FPGA

- 30 MHz, 8 μs pulse with white-noise standard deviation of 1
- Learning rate = 0.0006
- Taps = 64
- Filter was allowed to execute over 10 pulses
- 10th pulse/iteration for both 'x' and 'e' are shown



1 μs
window

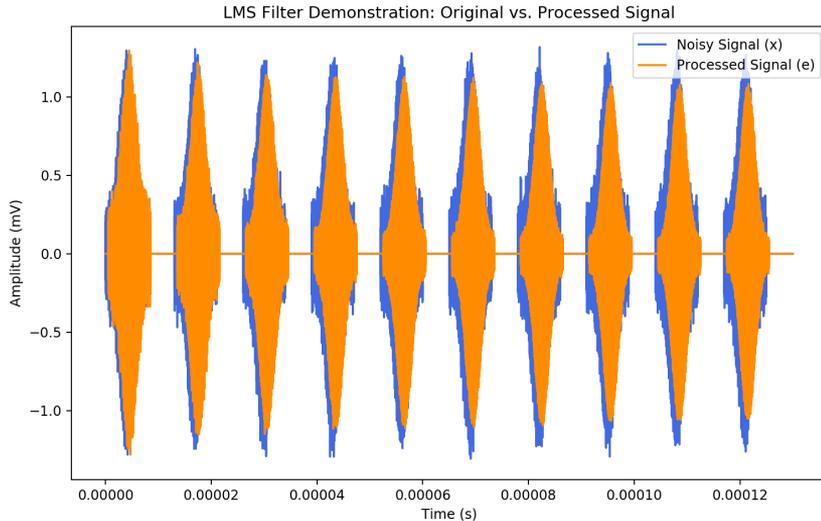


0.1 μs
window

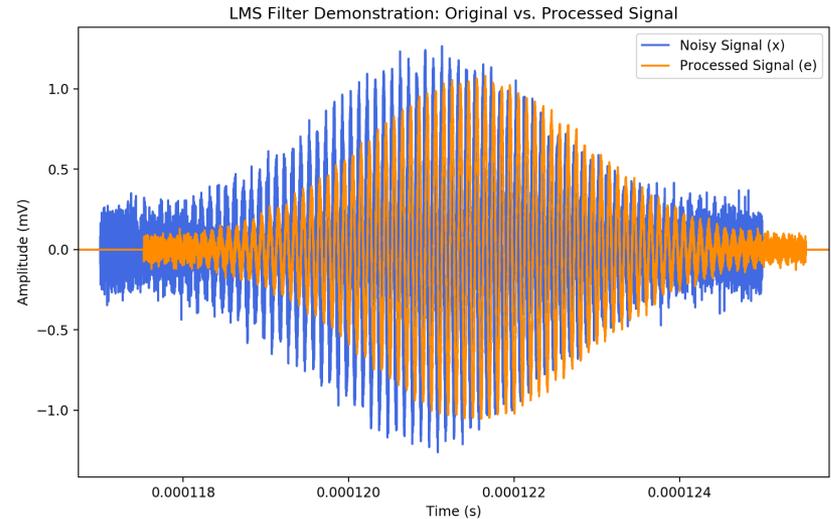
Results: LMS Filter Demonstration on FPGA

- 30 MHz, 8 μ s gaussian chirp with white-noise standard deviation of 1, 5 μ s in between pulses
- Learning rate = 0.0006
- Taps = 64
- Filter was allowed to execute over 10 pulses

Latency = 527.66 ns*
Took 15-20 minutes to load

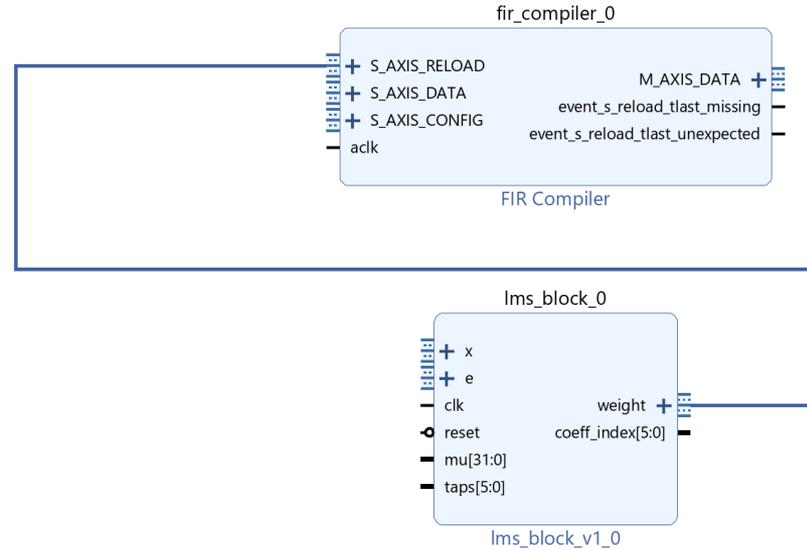
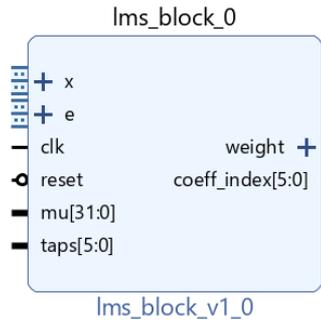


130 μ s
window



13 μ s window
(pulse 10)

Packaged Logic Blocks



- Packaged logic block containing weight update LMS algorithm

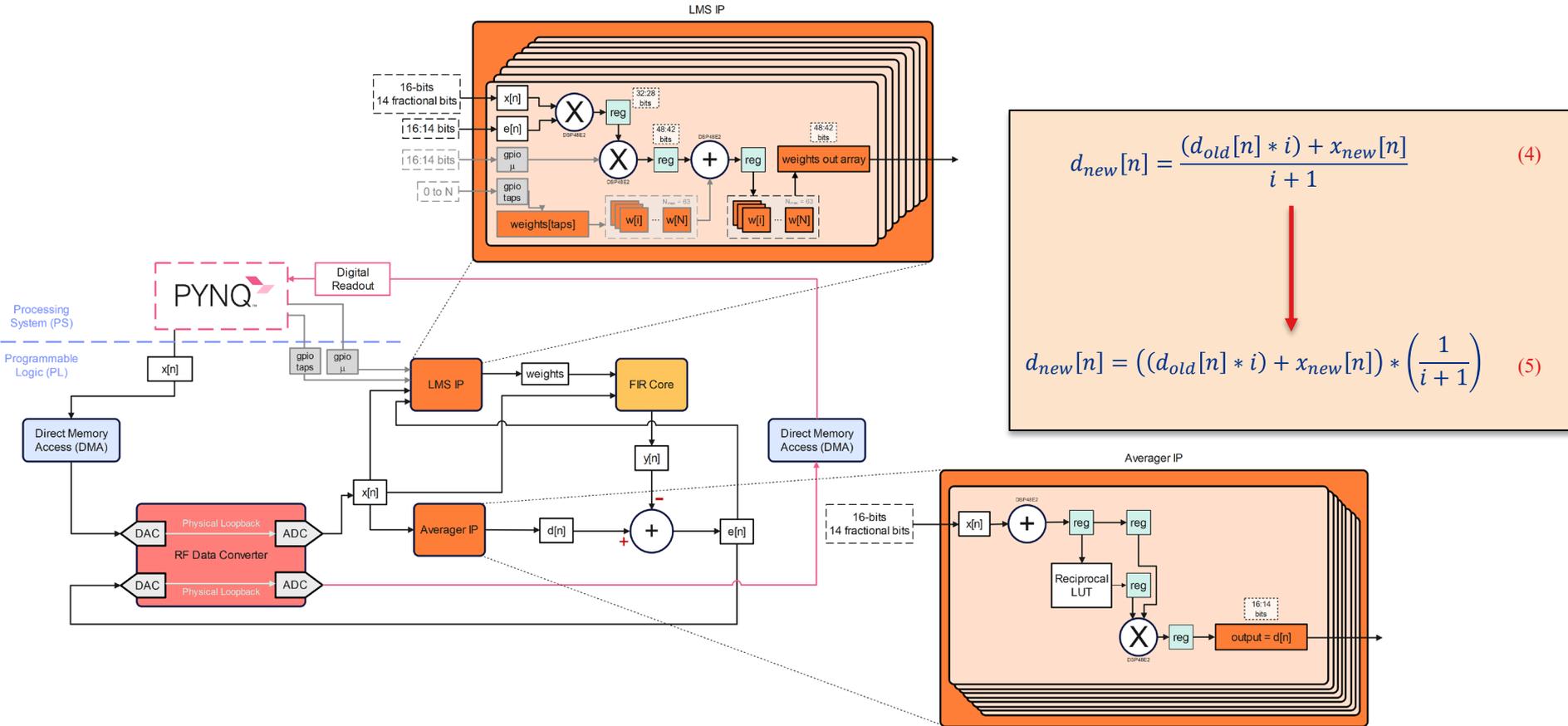
- LMS logic block sends updated weights to FIR compiler

LMS Demo Hardware Resources

TABLE 3.1: RESOURCE UTILIZATION FOR LMS DEMO ON RFSOC 4x2

Resource	Utilization	Available	Utilization (%)
<i>LUT</i>	21,964	425,280	5.16%
<i>LUTRAM</i>	3,529	213,600	1.65%
<i>FF</i>	33,992	850,560	4.00%
<i>BRAM</i>	133	1080	12.31%
<i>DSP</i>	10	42,732	0.23%
<i>BUFG</i>	7	696	1.01%
<i>MMCM</i>	1	8	12.5%

LMS Demo: Current Work



Research Objectives & Future Work

- 1. Develop an Adaptive LMS Filter:** Implement an adaptive Least Mean Squares (LMS) filter on an RFSoc FPGA-based control board to dynamically fine-tune the readout signals of qubits.
- 2. Integrate and Tune the Filter with the QICK Platform:** Deploy the adaptive filter onto the open-source Quantum Instrumentation Control Kit (QICK) platform to enhance its capabilities for quantum experiments.
- 3. Evaluate and Enhance Qubit Readout Fidelity:** Evaluate the performance of the adaptive filter in comparison to the current methodology of ensemble averaging and timing to demonstrate its efficiency and effectiveness in improving readout signal clarity.
- 4. Characterize the Noise Profile:** Utilize the adaptive LMS filter to conduct a detailed analysis and characterization of the noise affecting readout signals in both 2D and 3D QPU experiments.

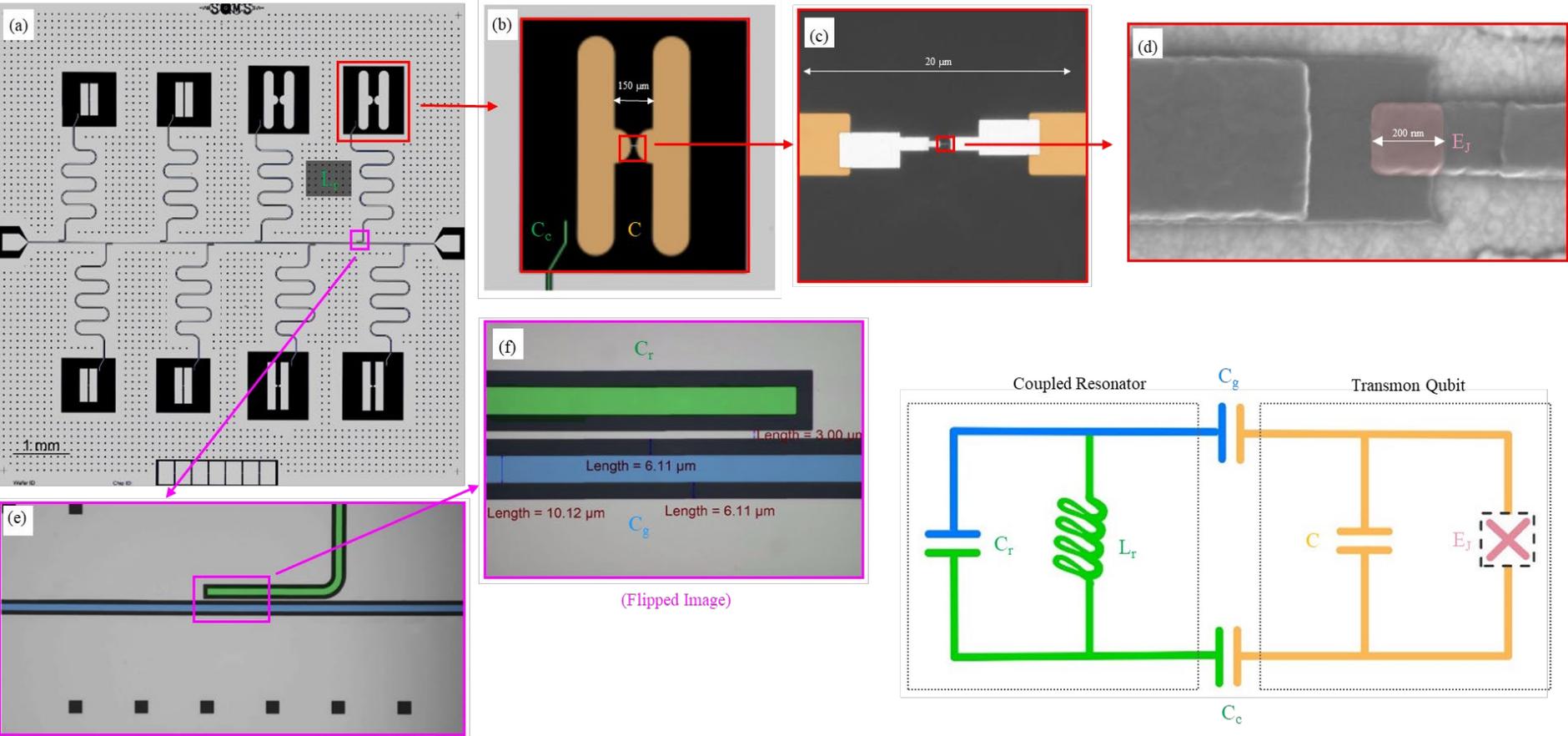
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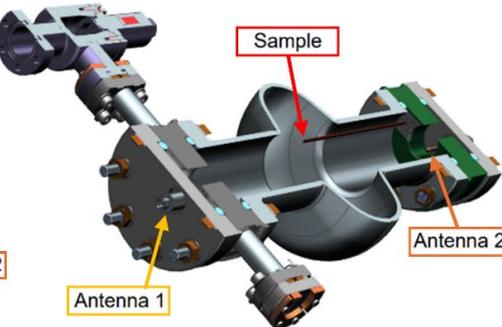
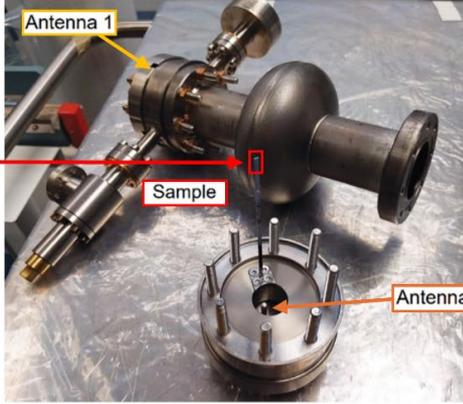
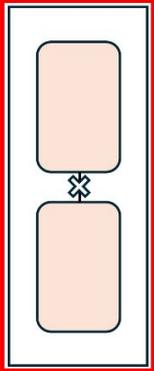
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2D QPU Platform



3D QPU Platform

- **3D QPU** = Superconducting qubits with SRF Cavities



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Characteristic Equations of Noise

- These equations are general equations for the noise power spectral density derived to fit the context of readout signals
- As the main effect of this research is to improve the Signal-to-Noise Ratio (SNR), the equations for SNR can give us insight as to what the sources of noise are

Fourier Transform

$$S(\omega) = 2 \int_{-\infty}^{+\infty} d(t-t') \frac{e^{i(\omega-\omega')(t-t')}}{2\pi} [\langle I(t)I(t') \rangle - \langle I(t) \rangle \langle I(t') \rangle] \quad (6)$$

Contribution from all time differences
Autocorrelation function

$$SNR(\omega) = \frac{P_{signal}(\omega)}{S(\omega)} \quad (7)$$

$$SNR(t) = \frac{I_{signal}^2(t)}{\sigma_I^2(t)} \quad (8)$$



$$P_{signal}(\omega) = |F\{I_{signal}(t)\}|^2 \quad (9)$$

$$P_{signal}(t) = I_{signal}^2(t) \quad (10)$$

Conclusion

- Foundational work is complete, implementation is underway
- Results will be significantly contributing to multi-qubit experiments when complete
 - Latency needs to be measured properly for new LMS filter on hardware, and new design needs more tests before integrating with QICK!



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Thank You!



Follow us on social media @sqmscenter



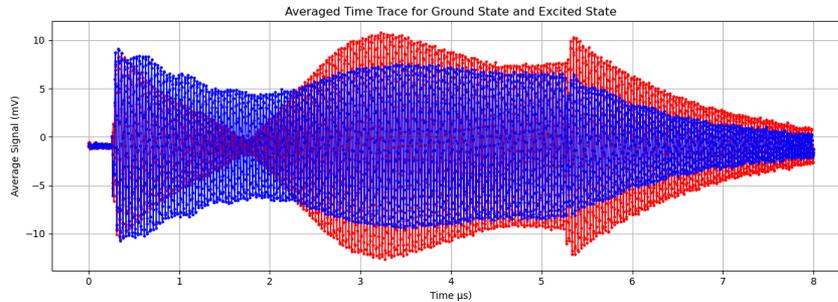
Twitter



Instagram

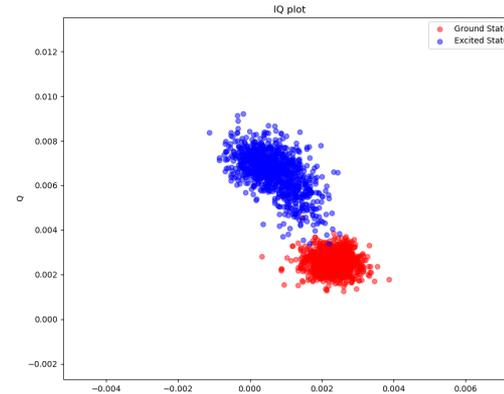
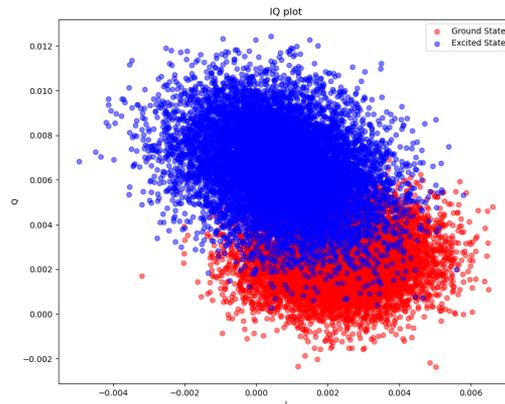
Backup Slides

Effect of LMS Filter on Readout calibration



Get this result in
<100,000 traces

Achieve this in the same
number of averages!

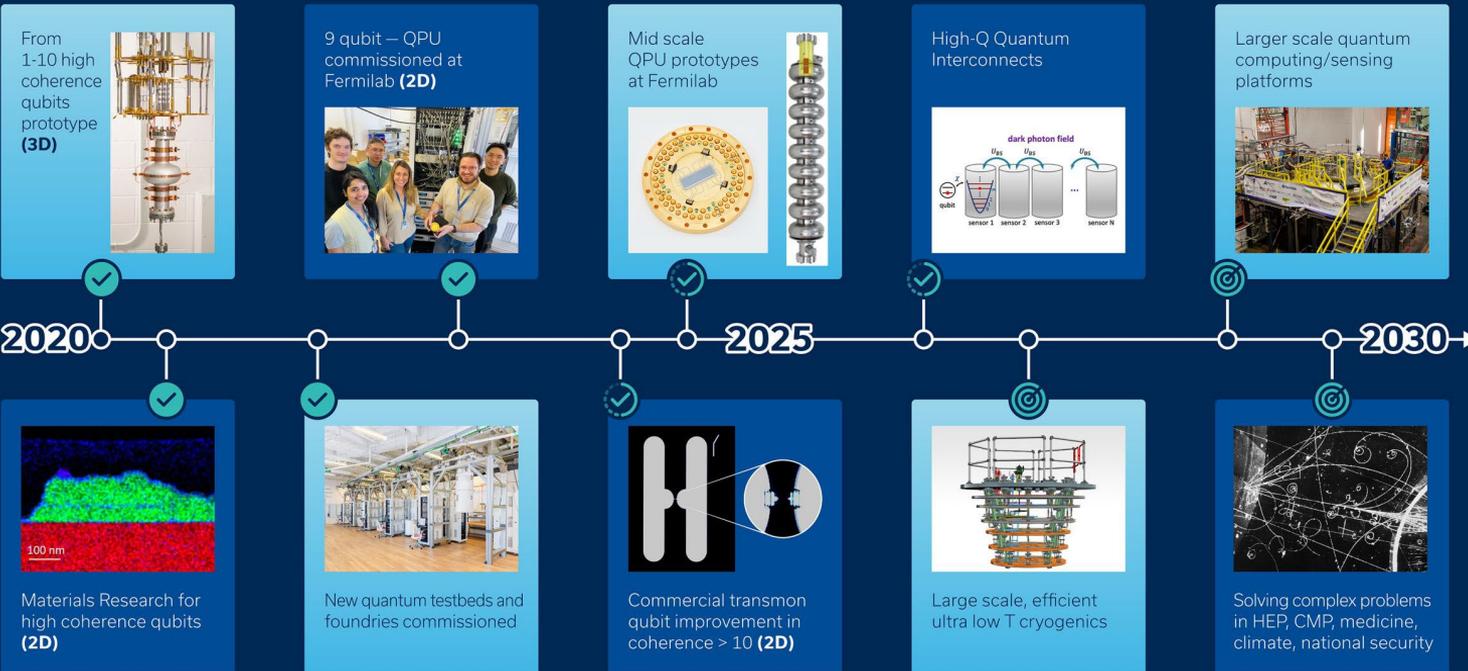


Best Superconducting Coherence Times

TABLE 2.1: BEST 2D SINGLE QUBIT COHERENCE TIMES

<i>Group</i>	T_1 (μs)	<i>Freq. (GHz)</i>	<i>Substrate</i>	<i>Primary Material</i>	<i>Year</i>	<i>Ref.</i>
<i>SQMS/Rigetti</i>	~600	4 – 6	Sapphire	Ta/Nb, dry etch	2024	[4]
<i>SQMS</i>	451	4.5 – 5	Sapphire	Ta/Nb, dry etch	2023	[4] (preprint)
<i>Yu (China)</i>	503	3.8 – 4.7	Sapphire	Ta, dry etch	2022	[58]
<i>IBM</i>	340	~ 4	Silicon	Nb, wet etch	2021	[87]
<i>Houck/Princeton</i>	360	3.1 – 5.5	Sapphire	Ta, wet etch	2021	[57]
<i>IBM</i>	234	3.808	Silicon	Al, dry etch	2021	[88]
<i>Schuster</i>	126	4.749	Sapphire	Nb, Fl etch	2021	[89]
<i>Rigetti</i>	133	3.8 – 4.2	Silicon	Nb	2019	[90]

Transmon Qubit Timeline - SQMS



SQMS Center 10 year roadmap

- Complete
- In-progress
- Future tech

FPGA Controls

- Single RFSoc FPGA is used for controller of 2D qubits.
- 3D QPU uses benchtop control stack for now due to power limitations on ZCU216

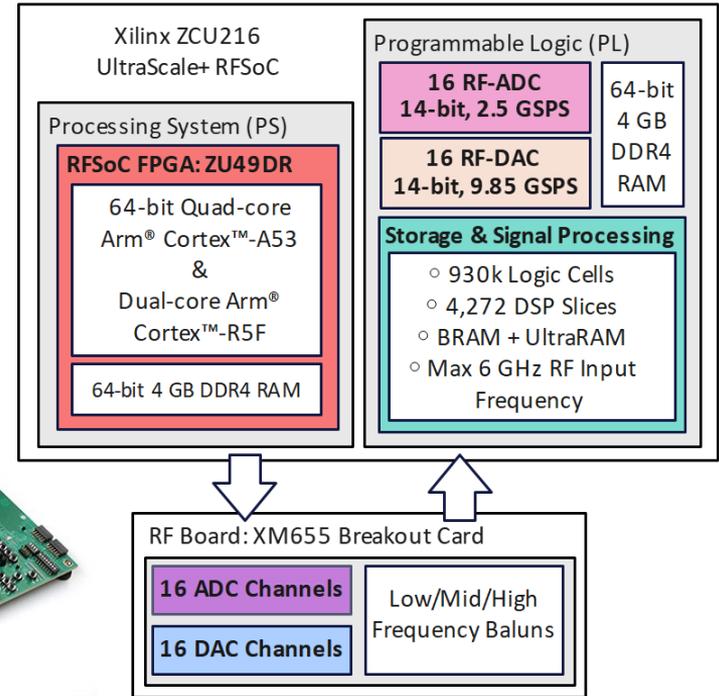
1. Xilinx ZCU111 RFSoc UltraScale+ FPGA (*Gen 1*)
2. Xilinx RFSoc 4x2 UltraScale + FPGA (*Gen 3*)
3. **Xilinx ZCU216 RFSoc UltraScale+ FPGA (*Gen 3*)**

- XM655 Breakout Card or custom card
- 16 RF-ADC: 14-bit, 2.5 GSa/s (interleaved)
- 16 RF-DAC: 14-bit, 9.85 GSa/s

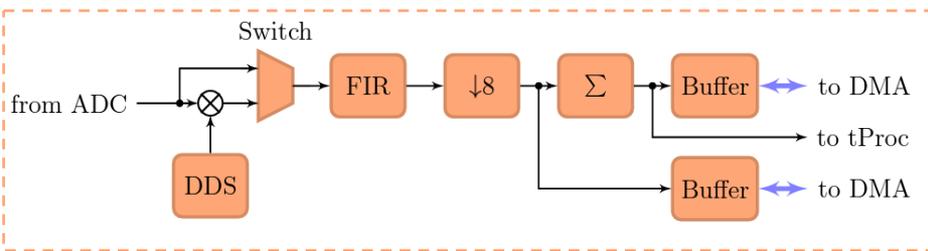
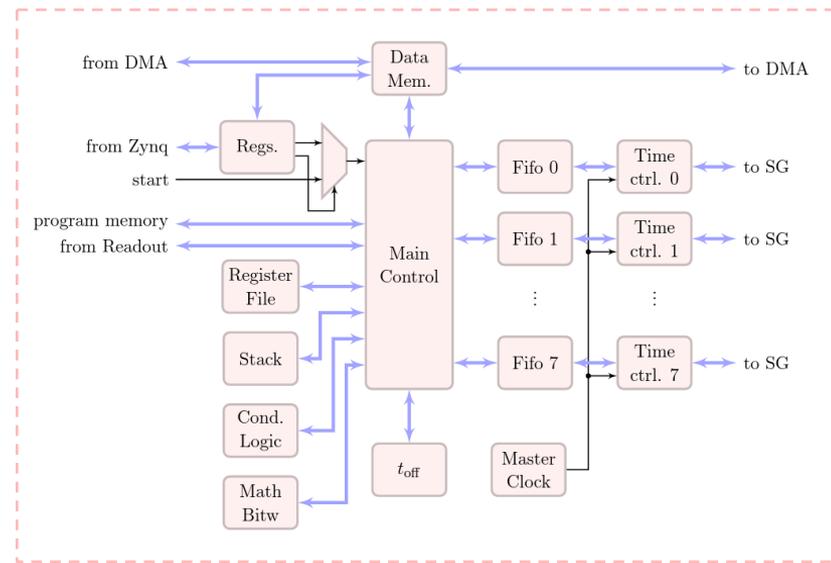
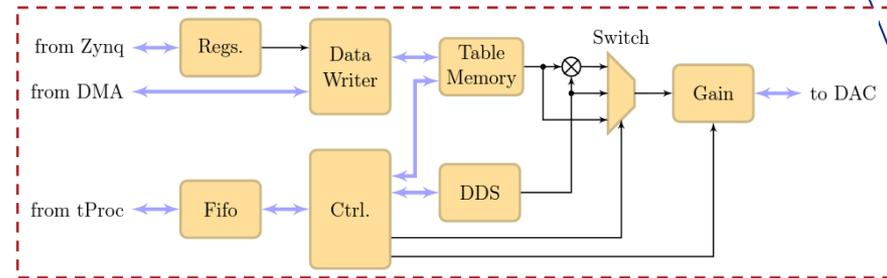
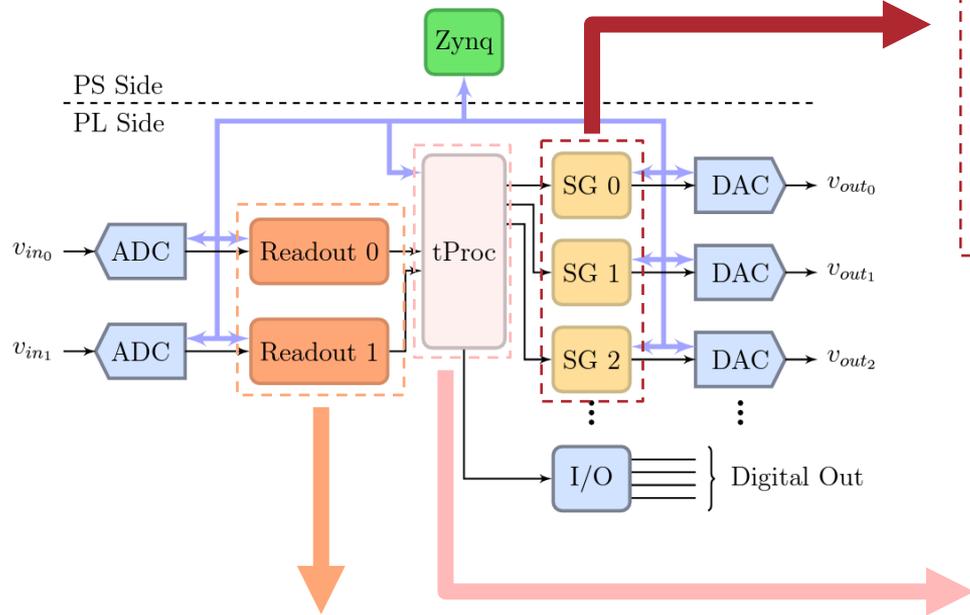
- Quantum Instru (**QICK**)



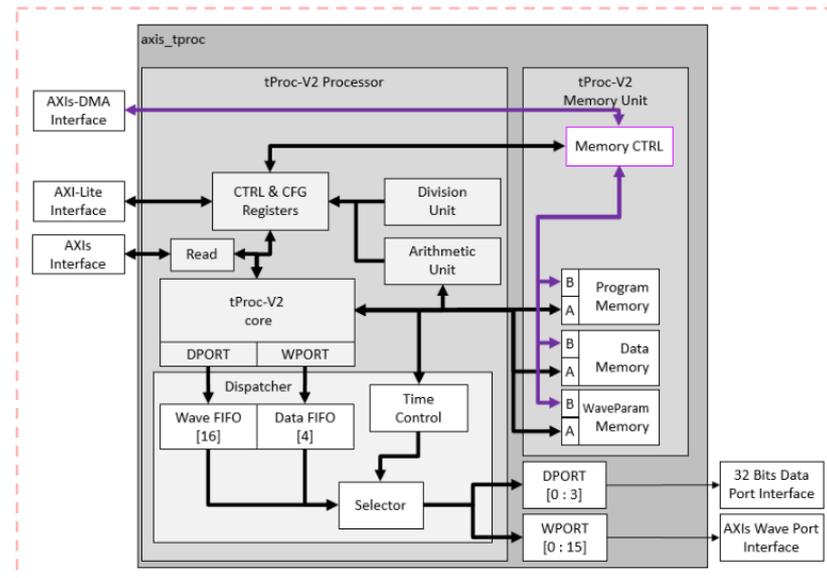
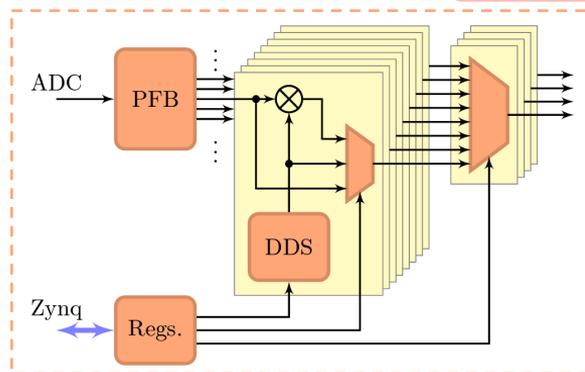
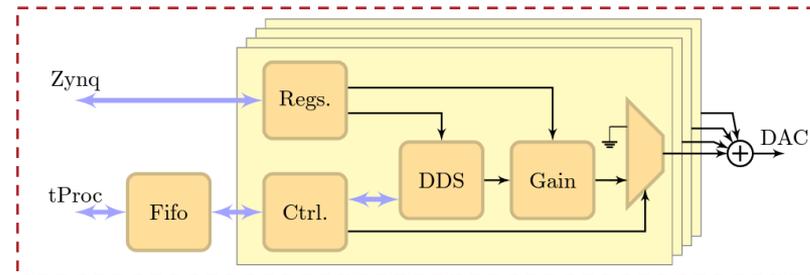
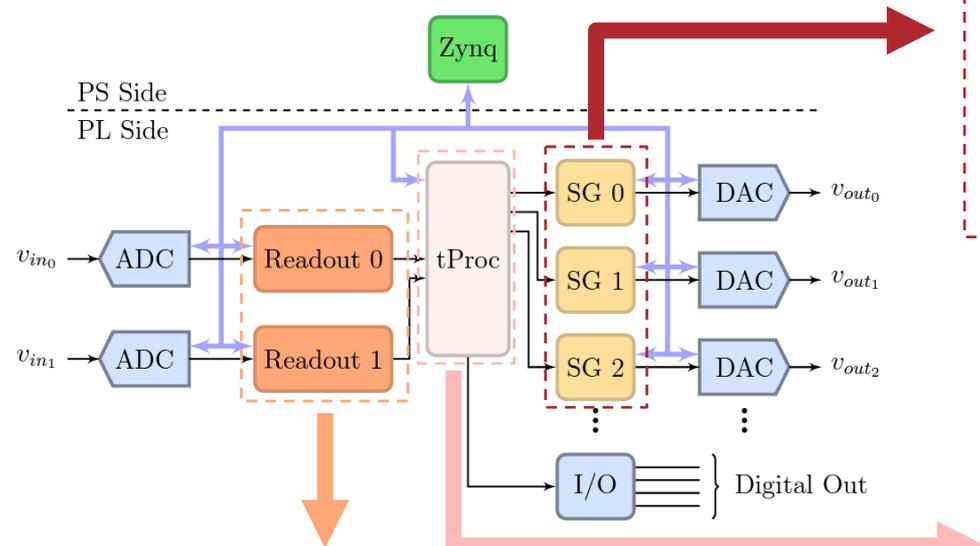
Control Kit



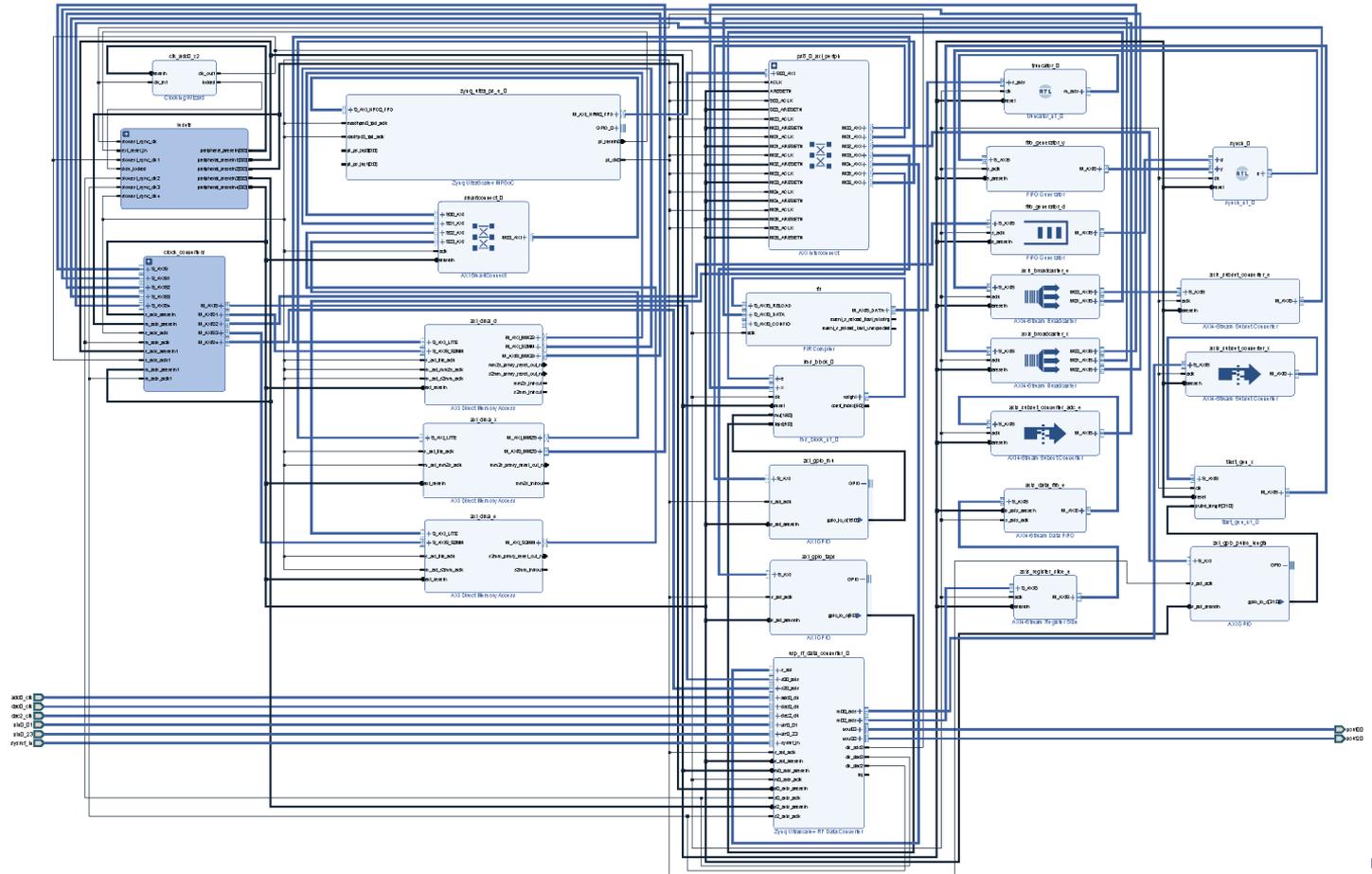
QICK Firmware v1



QICK Firmware v2



LMS Demo Block Design



Qubit Characterization Experiment

- Qubit calibration and measurement on QICK
- This is a standard process for determining the ground/excited state for a qubit, and then determining T_1 and T_2 measurements for a qubit
- The goal is to do this with the LMS filter active and then compare results!

