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DESI 2024: Constraints on Physics-Focused Aspects of Dark Energy using  
DESI DR1 BAO Data

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# DESI 2024: Constraints on Physics-Focused Aspects of Dark Energy using DESI DR1 BAO Data

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**Abstract.** Baryon acoustic oscillation data from the first year of the Dark Energy Spectroscopic Instrument (DESI) provide near percent-level precision of cosmic distances in seven bins over the redshift range  $z = 0.1\text{--}4.2$ . We use this data, together with other distance probes, to constrain the cosmic expansion history using some well-motivated physical classes of dark energy. In particular, we explore three physics-focused behaviors of dark energy from the equation of state and energy density perspectives: the thawing class (matching many simple quintessence potentials), emergent class (where dark energy comes into being recently, as in phase transition models), and mirage class (where phenomenologically the distance to CMB last scattering is close to that from a cosmological constant  $\Lambda$  despite dark energy). All three classes fit the data at least as well as  $\Lambda$ CDM, and indeed can improve on it by  $\Delta\chi^2 \approx -5$  to  $-17$  for the combination of DESI BAO with CMB and supernova data, while having one more parameter. The mirage class does essentially as well as  $w_0w_a$ CDM while having one less parameter. These classes of dynamical behaviors highlight worthwhile avenues for further exploration into the nature of dark energy.

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## 1 Introduction

Cosmic distances and the cosmic expansion rate contain information on the matter and energy contents of the universe. Redshift surveys can measure these at many epochs in cosmic history and so are especially valuable in separating the contributions and studying their evolution. In particular, a central question in cosmology is the nature of cosmic acceleration: does it originate from a cosmological constant  $\Lambda$  or a dynamically evolving dark energy?

Dark energy can be explored through the use of particular models, general parametrizations, or in a model-independent manner. In the absence of a fundamental theory pointing to a compelling model, and for robustness, many analyses take one of the latter two routes. The standard parametrization for the dark energy equation of state  $w(a) = w_0 + w_a(1 - a)$  originated from exact solutions of the dark energy physical dynamics and has been demonstrated to be accurate to  $\sim 0.1\%$  [1, 2] in matching distances and expansion rates over a wide array of models. Results for  $w_0w_a$ CDM cosmology using DESI data are presented in [3]. Model-independent or at least model-agnostic approaches, e.g. Crossing Statistics, Gaussian Processes, values in redshift bins, etc., are investigated in [4] and forthcoming works for DESI data.

Here, we take a middle path, with general parametrizations informed by physics properties. Thus we do not use specific models, but are focused by the physics into classes of dynamical evolution. One perspective is to address the evolution in terms of the dark energy equation of state, specifically the thawing class, and another in terms of the dark energy density, specifically where dark energy arises quickly, whether through a phase transition or

a rapid growth ( $w \ll -1$ ). A third class is the mirage class [5], where an apparent  $w = -1$  when forced to a constant value actually hides dynamics. These are chosen because previous data pointed to these physical properties as compatible with observations, at least as well as the cosmological constant, and they describe broad classes of characteristic behavior, rather than a single model.

New, highly precise data have become available from Data Release 1 of the DESI baryon acoustic oscillations (DESI BAO) measurements. The data are discussed in detail in [3, 6, 7]. Here we investigate their implications for the dark energy physics, using the physics-focused classes above. Section 2 describes the physics-focused classes for the dark energy equation of state and density. In Section 3 we review the DESI distance data in seven redshift ranges, as well as other data sets used in combination. Constraints on cosmology and the physics implications are discussed in Section 4, with conclusions in Section 5.

## 2 Physics-focused classes

The current data, including DESI BAO, favors dynamical dark energy over a simple cosmological constant at various levels of significance when different data set combinations are used, as shown in [3]. This motivates consideration of a wide variety of dark energy behaviors.

However, there is no compelling physics-based theory for dark energy differing from  $\Lambda$ , so one tends to adopt a more phenomenological approach. Here, we want to retain physics to a significant extent and use classes of dark energy properties consistent with the data, and that are more general than specific models.

Dark energy properties enter the measurements through their impact on cosmic distances (we do not here consider growth probes of large scale structures). This follows from the Friedmann equations, and we can write the dark energy influence as (assuming a spatially flat universe)

$$\frac{H^2(z)}{H_0^2} = \Omega_{m,0}(1+z)^3 + \Omega_{r,0}(1+z)^4 + (1 - \Omega_{m,0} - \Omega_{r,0}) f_{\text{DE}}(z) , \quad (2.1)$$

where  $\Omega_{m,0}$  and  $\Omega_{r,0}$  are the present fractions of the critical energy density in matter and radiation respectively, and  $f_{\text{DE}}(z)$  describes the dark energy density evolution. The dark energy equation of state, or pressure to energy density ratio, then comes from the continuity equation as

$$w(z) = -1 + \frac{1}{3} \frac{d \ln f_{\text{DE}}(z)}{d \ln(1+z)} . \quad (2.2)$$

For example,

$$w(a) = w_0 + w_a(1-a) \quad \Leftrightarrow \quad f_{\text{DE}}(a) = a^{-3(1+w_0+w_a)} e^{-3w_a(1-a)} , \quad (2.3)$$

where the scale factor  $a = 1/(1+z)$ . The key then is seeing how physics informs the dark energy density  $f_{\text{DE}}(z)$  or equation of state  $w(a)$ . We assume throughout that the dark energy fluid sound speed  $c_s^2 = 1$ .

### 2.1 Dark Energy Equation of State: Thawing Physics

While writing the dark energy equation of state as  $w(a) = w_0 + w_a(1-a)$  [1, 8] has been shown to be highly accurate for a wide variety of models [1, 2], the physics does not actually

predict that any *arbitrary* combination of  $w_0$  and  $w_a$  is equally valid. Basic physics – evolution of the dark energy field through the long history of radiation and matter domination in the presence of Hubble friction – calls out two regions of the phase space as preferred, known as the thawing and freezing regions [9]. Other regions of the phase space arise only due to extraordinary circumstances, e.g. fine tuning, noncanonical kinetic structure, or non-gravitational interactions. The freezing region, with  $w_a > 0$ , tends not to be compatible with observations; indeed DESI BAO plus other probes disfavors it at  $\sim 3\sigma$  [3]. Thus we focus on exploring the thawing physics class.

Thawing physics arises because, during the long cosmic history, the Hubble friction was high enough to overcome dark energy dynamics, causing it to act like a cosmological constant. Only recently, as the Hubble expansion rate declined sufficiently, was dark energy released to allow dynamics (“thawed”). This describes a broad variety of particle physics models for dark energy, including pseudo-Nambu-Goldstone bosons (PNGB [10]; e.g. axions), the linear potential [11] with its shift symmetry shielding against quantum corrections, and many monomial potentials (e.g. the standard quadratic  $V \sim m^2\phi^2$  and quartic  $V \sim \lambda\phi^4$ ).

One of the great virtues of the  $w_0$ – $w_a$  parametrization is that it acts as a calibration relation for the physics. Not only are the thawing fields in the same class, but  $w_0$ – $w_a$  calibrates their evolution  $w(a)$ , bringing their phase space tracks in  $w$ – $w'$  into a universal relation [2]:

$$w_a \approx -1.58(1 + w_0) . \quad (2.4)$$

(The coefficient  $-1.58$  comes from fits to the dynamics in [2], e.g. see Eq. (1) of [12].)

Another approach to thawing dynamics is to account for the Hubble friction freeze in the past plus an algebraic factor describing the thawing, roughly related to the ratio of the frozen dark energy density to the matter density,  $\sim a^3$ . Again, these are general characteristics of the thawing class as a whole, and so not model dependent in the usual sense. Following [12, 13] we have

$$1 + w(a) = (1 + w_0) a^3 \left( \frac{3}{1 + 2a^3} \right)^{2/3} . \quad (2.5)$$

Note that both the calibration and algebraic forms have simply one parameter more than  $\Lambda$ CDM. They have also both been demonstrated to have accuracy better than 0.1% in matching distances  $d(z)$  and Hubble expansion rates  $H(z)$  of the exact physics [12]. Describing the thawing class by either the calibration or algebraic forms gives virtually identical results (see Fig. 7 in Appendix A), adding support for the model-independent nature of the analysis.

## 2.2 Dark Energy Density: Emergent Physics

In contrast to the previous subsection, we now consider the dark energy density, rather than the equation of state, and a rapid emergence or transition rather than a slow thaw. In this class of physical behavior, dark energy is negligible (or vanishes) above moderate redshift (say  $z \approx 2$ ) but its energy density quickly grows at lower redshift (implying  $w < -1$ ) before leveling off to a constant in the future (and so  $w \rightarrow -1$ ). Physical examples of this behavior include phase transitions such as vacuum metamorphosis [14, 15] and dark energy as a critical phenomena [16, 17]. The density of dark energy as a critical phenomenon can behave similarly to the magnetization of the Ising model and effectively emerges at a particular time (redshift) corresponding to the critical temperature in the model [17].

Phenomenological Emergent Dark Energy (PEDE) model [18, 19] has been introduced as a zero freedom dark energy model where dark energy has no effective presence in the past

and effectively emerges in the late Universe. The model was generalised as Generalised Emergent Dark Energy (GEDE) [20], to include both PEDE and  $\Lambda$  as two limits of the parametric form and to include a larger class of emergent dark energy behaviors.

The evolution of the energy density in GEDE is given by [20, 21]

$$f_{\text{DE}}(z) = \frac{1 - \tanh\left(\Delta \times \log_{10}\left(\frac{1+z}{1+z_t}\right)\right)}{1 + \tanh\left(\Delta \times \log_{10}(1+z_t)\right)}, \quad (2.6)$$

where  $\Delta$  is a free parameter, determining the steepness of the transition, and  $z_t$  is a derived quantity determined by solving  $\rho_m(z_t) = \rho_{\text{DE}}(z_t)$ . The corresponding equation of state for GEDE is

$$w(z) = -1 - \frac{\Delta}{3 \ln(10)} \left[ 1 + \tanh\left(\Delta \log_{10}\left(\frac{1+z}{1+z_t}\right)\right) \right]. \quad (2.7)$$

Note that  $f_{\text{DE}}(z)$  goes from much less than one for  $z \gg z_t$  to one today to a finite value greater than one in the future (de Sitter state), while  $w(z)$  goes from  $-1 - 2\Delta/(3 \ln 10)$  at  $z \gg z_t$  to  $-1$  in the future.

### 2.3 Dark Energy: Mirage Physics

Another, more phenomenological class is that of mirage dark energy [5]. This originated as a way to match the CMB distance to last scattering from  $\Lambda$ CDM but for some evolving dark energy equation of state  $w(a)$ . More generally, it will appear to yield a constant  $w = -1$  for data combinations with a pivot point, or greatest sensitivity to dark energy equation of state, around  $a \approx 0.7$ . The condition becomes

$$w_a = -3.66(1 + w_0). \quad (2.8)$$

(The coefficient  $-3.66$  comes from Eqs. (1) and (3) of [5] and varies by a couple percent over the range  $\Omega_{m,0} \in [0.25, 0.35]$ .)

Interestingly, DESI BAO DR1 gives a confidence contour in the  $w_0$ - $w_a$  plane that follows this closely, and indeed delivers a  $w \approx -1$  fit when assuming  $w = \text{const}$  (e.g. see Fig. 5 of [3]). We emphasize, however, as demonstrated in this article and [4], that this does not actually mean that  $w = \text{const}$ . That may merely be a mirage, even for quite rapidly evolving  $w(a)$ . Note furthermore that since mirage models match the CMB distance, they will also generally closely match the growth of structure (within general relativity), as the mirage holds for this as well (see [22] and Fig. 6 of [5] for demonstration).

As to the physical mechanism behind the mirage, this is less clear. Such a crossing of  $w(a) = -1$  is a hallmark of perhaps a combination of multiple scalar fields, interactions, or modified gravity generally involving noncanonical kinetic terms and possibly braiding of the scalar and tensor degrees of freedom. Rapid emergence of the dark energy density (i.e. strongly negative  $w_a$  and hence  $w(a) \ll -1$  at early redshifts) however is not a generic characteristic of such mechanisms, and if taken at face value could point more to a phase transition mechanism. Many of those, however, such as vacuum metamorphosis [14], tend toward a de Sitter ( $w = -1$ ) state not  $w_0 > -1$ . It is not clear what reasonable physics would contain both a rapid emergence in density and a crossing of  $w(a) = -1$ . (Speculatively, one could imagine the scalar field responsible for the phase transition having a negative potential or some interaction that would cause crossing of  $w(a) = -1$ .)

**Table 1.** Parameters and priors used in the analysis with our modified version of the Boltzmann solver `class`. All of the priors are uniform in the ranges specified below.

	parameter	prior/value
<b>background-only</b>	$\Omega_{m,0}$	$\mathcal{U}[0.01, 0.99]$
	$H_0 r_d$ [km s <sup>-1</sup> ]	$\mathcal{U}[1000, 100000]$
<b>CMB</b>	$\omega_{\text{cdm}} \equiv \Omega_{\text{cdm}} h^2$	$\mathcal{U}[0.001, 0.99]$
	$\omega_{\text{b}} \equiv \Omega_{\text{b}} h^2$	$\mathcal{U}[0.005, 0.1]$
	$\ln(10^{10} A_s)$	$\mathcal{U}[1.61, 3.91]$
	$n_s$	$\mathcal{U}[0.8, 1.2]$
	$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	$\mathcal{U}[20, 100]$
	$\tau$	$\mathcal{U}[0.01, 0.8]$
<b>Thawing/Mirage</b>	$w_0$	$\mathcal{U}[-3, 1]$
<b>GEDE</b>	$\Delta$	$\mathcal{U}[-3, 10]$
$w_0 w_a$	$w_0$	$\mathcal{U}[-3, 1]$
	$w_a$	$\mathcal{U}[-3, 2]$

### 3 Data and Methodology

The cosmological probes and specific data sets used in our analysis are:

- **Baryon Acoustic Oscillations (BAO):** We use the compilation of compressed distance quantities  $D_M/r_d$ ,  $D_H/r_d$ , and  $D_V/r_d$  from the first year data release of the Dark Energy Spectroscopic Instrument [23–27], where  $D_M$  is the transverse comoving distance,  $D_H$  the Hubble distance,  $D_V$  their isotropic average, and  $r_d$  is the sound horizon at the baryon drag epoch. This dataset, abbreviated as “DESI BAO”, spans seven redshift bins from  $z = 0.3$  to  $z = 2.33$  [6]. We refer the reader to [3, 6, 7, 27–30] for further details.
- **Supernovae Ia (SNe Ia):** We combine with supernova data from three sets, one at a time: “PantheonPlus”, a compilation of 1550 supernovae spanning a redshift range from 0.01 to 2.26 [31], “Union3”, containing 2087 SNe Ia processed through the Unity 1.5 pipeline based on Bayesian Hierarchical Modelling [32], and “DES-SN5YR”, a compilation of 194 low-redshift SNe Ia ( $0.025 < z < 0.1$ ) and 1635 photometrically classified SNe Ia covering the range  $0.1 < z < 1.3$  [33].
- **Cosmic Microwave Background (CMB):** We also include temperature and polarization measurements of the CMB from the Planck satellite [34]. In particular, we use the high- $\ell$  TTTEEE likelihood (`planck_2018_highl_plik.TTTEEE`), together with low- $\ell$  TT (`planck_2018_lowl.TT`) and low- $\ell$  EE (`planck_2018_lowl.EE`) [35], as implemented in `cobaya` [36]. Additionally, we include CMB lensing measurements from the combination of NPIPE PR4 from Planck [37] and the Atacama Cosmology Telescope (ACT DR6) [38, 39] using importance sampling. When using the combined Planck+ACT lensing likelihood, we use `accurate_lensing:1` and `delta_l_max:800` options to match CAMB precision settings as recommended by ACT.

In our analysis, we utilize Markov Chain Monte Carlo (MCMC) sampling to explore the parameter space using the Metropolis-Hastings algorithm [40, 41] as implemented in

cobaya [36]. To facilitate efficient sampling of the CMB Planck likelihoods, we employ the “fast-dragging” scheme [42]. We have adopted priors similar to [3], as presented in Table 1, and have modified the Boltzmann solver `class` [43, 44] incorporating a generalized equation of state for dark energy for the theoretical prediction of observables. We switched to the `Recfast` option for recombination as it does not assume anything about the equation of state. We assume three neutrino species with  $\sum m_\nu = 0.06$  eV and  $N_{\text{eff}} = 3.044$ . For the supernovae likelihoods (PantheonPlus, Union3, and DES-SN5YR), we analytically marginalize over the absolute magnitude  $M_B$ . For clarity of presentation, in the main text figures we use PantheonPlus but list constraints from each supernova set in the tables and show their contours in Appendix B.

## 4 Results and Discussions

We present the results for each class in turn, showing the cosmological parameter joint posteriors and the reconstructed dark energy equation of state  $w(z)$  and energy density  $f_{\text{DE}}(z)$  for various combinations of data sets.

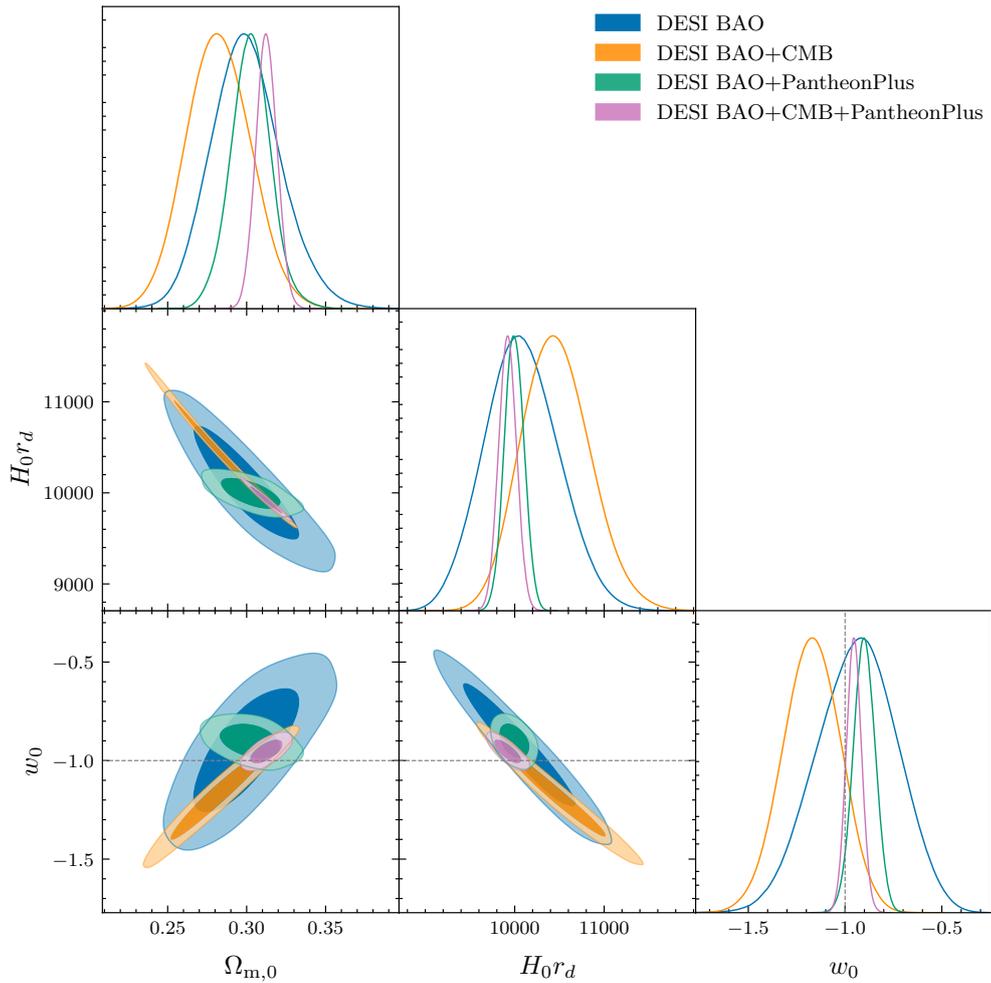
### 4.1 Thawing

Figure 1 shows the joint parameter constraints for the thawing class. The dashed black line corresponds to  $\Lambda$ CDM ( $w_0 = -1$ ). In the first few rows of Table 2, we report the marginalized constraints on some of the relevant cosmological parameters and for various data combinations. The addition of CMB data to DESI BAO significantly reduces the uncertainty in  $w_0$ , shifting its value to  $< -1$ , which also results in  $w_a > 0$ . However, combining DESI BAO with PantheonPlus yields  $w_0 > -1$ . A combination of all three datasets provides even tighter constraints, with posteriors peaking at  $w_0 \gtrsim -1$ , hence  $w_a < 0$ . Using either of the other two supernova datasets instead somewhat strengthens  $w_0 > -1$ . Figure 2 illustrates the behaviors for the equation of state  $w(z)$  and energy density evolution  $f_{\text{DE}}(z)$ .

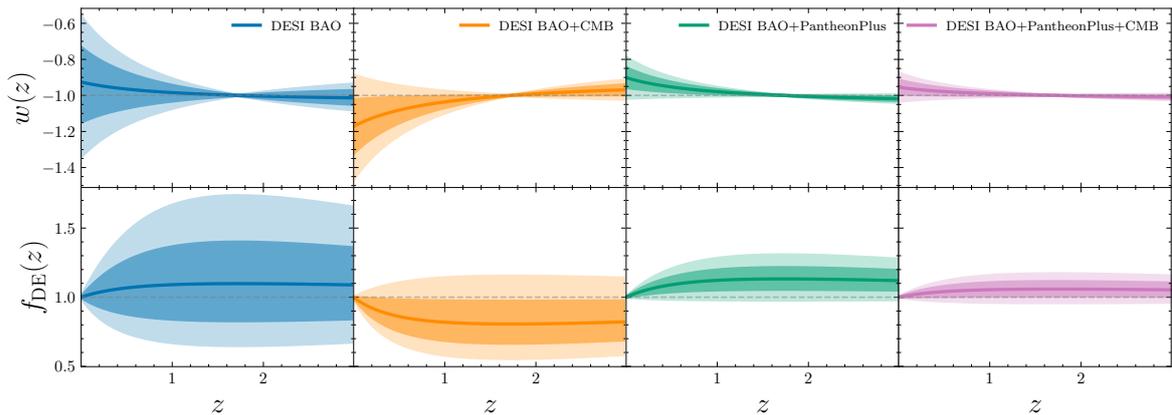
We emphasize that the relations  $w_a(w_0)$  for both the thawing and mirage classes are designed to replicate *observations*, i.e. distances and Hubble parameters to  $\sim 0.1\%$ , not the actual  $w(z)$  for a specific model within the class, and hence do not need to have  $w(z \gg 1) \rightarrow -1$ , say. Indeed  $w(z)$  can appear to cross  $-1$  even if it actually doesn’t, yet still fit the observations exquisitely – this is well known: see Table 1 of [12] and Fig. 14 of [45] for a PNGB model, [46] for a hilltop model, etc. However, for  $|w_a| \gtrsim 1$  such unreal crossings of  $w(z) = -1$  tend to be in conflict with the CMB distance to last scattering, and such strong crossings tend in fact to be real.

### 4.2 Generalized Emergent Dark Energy

The GEDE analysis proceeds similarly, with Fig. 3 showing its constraints on parameters, using the same datasets. When considering DESI BAO alone, the dataset is broadly consistent with  $\Delta = 0$ , corresponding to  $\Lambda$ CDM. However, when combined with CMB,  $\Delta$  peaks at a positive value ( $\Delta \simeq 1$ , corresponding to PEDE [18]), indicating that dark energy emerges at late times. Adding PantheonPlus, GEDE prefers a negative value of  $\Delta$ , which corresponds to the injection of energy at earlier redshifts. However, combining all three datasets results in a peak near  $\Delta = 0$ , indicating that dark energy density remains roughly constant throughout evolution and that GEDE is not preferred over  $\Lambda$ CDM. Note that the model-agnostic reconstructions of dark energy in [4] do seem to indicate a sharp emergence of dark energy in the recent past. The issue is that GEDE sharply emerges, but asymptotes to  $w = -1$  rather

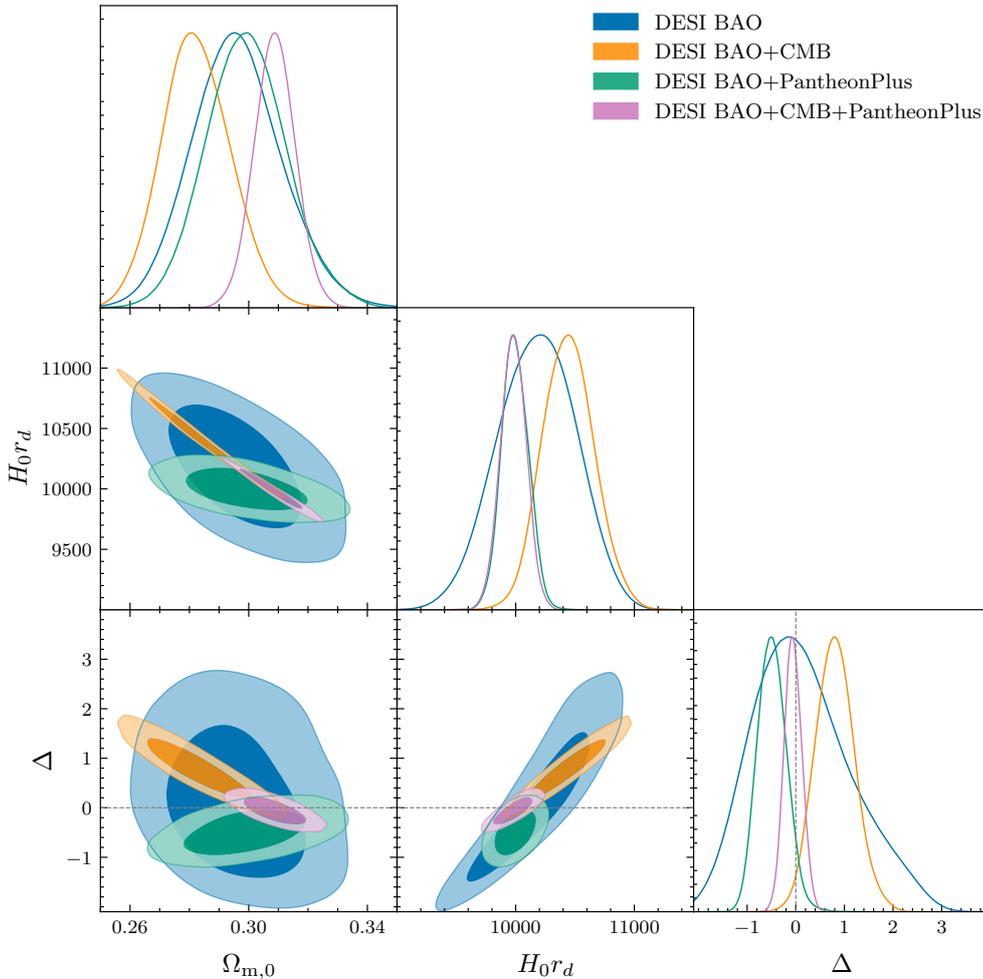


**Figure 1.** Marginalized constraints within the thawing class of dark energy described by Eq. (2.4), from different combinations of data sets.



**Figure 2.** Marginalized constraints on the dark energy equation of state  $w(z)$  and energy density  $f_{\text{DE}}(z)$  for the thawing class, parametrized by Eq. (2.4).

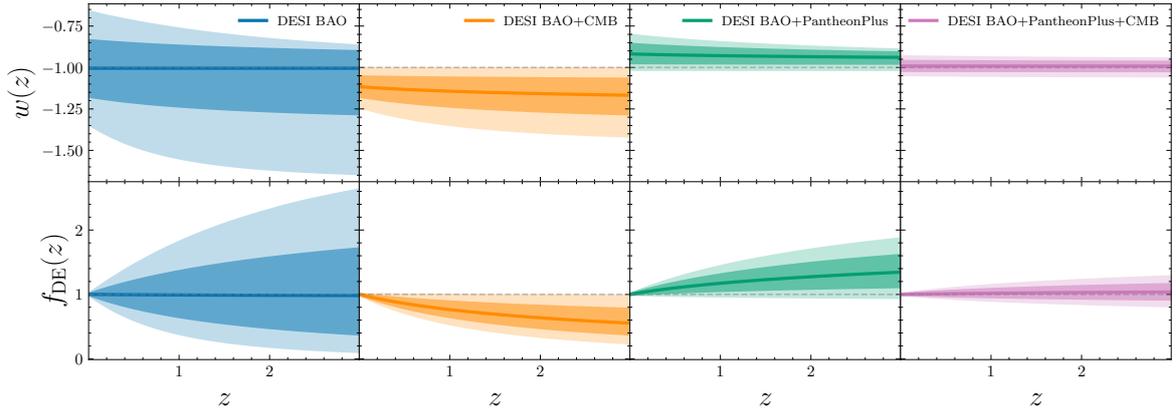
than crossing it. Increasing  $\Delta$  fits the  $z \approx 1$  data better than  $\Lambda$ CDM but the  $z \lesssim 0.5$  data prefers  $w > -1$  and so GEDE is worse than  $\Lambda$ CDM there, resulting in GEDE “mellowing” to approach  $\Lambda$ CDM behavior (and so, as we will see, not having a particularly advantageous goodness of fit). If there were an emergent model that also crossed  $w = -1$  then this might provide a superior fit to data, but physics motivation for such behavior is not obvious. Figure 4 exhibits the uncertainty bands for the reconstructed equation of state  $w(z)$  and energy density evolution  $f_{\text{DE}}(z)$ .



**Figure 3.** Marginalized constraints within the Generalized Emergent Dark Energy (GEDE) class described by Eq. (2.6).

### 4.3 Mirage

The mirage class has cosmological parameter constraints illustrated in Fig. 5. Again, the preference is pulled off  $\Lambda$ CDM (which is a member of this class, where the mirage is real). A best fit of  $w_0 \approx -0.8$ , and hence  $w_a \approx -0.7$ , is quite consistent with DESI BAO data, including in combination with other data sets such as CMB and supernovae. One can make  $w_0$  even less negative (and hence  $w_a$  more negative), i.e. strengthen the mirage, if one compensates by decreasing the late time dark energy density (increasing  $\Omega_{\text{m},0}$ ), as seen in Fig. 5.



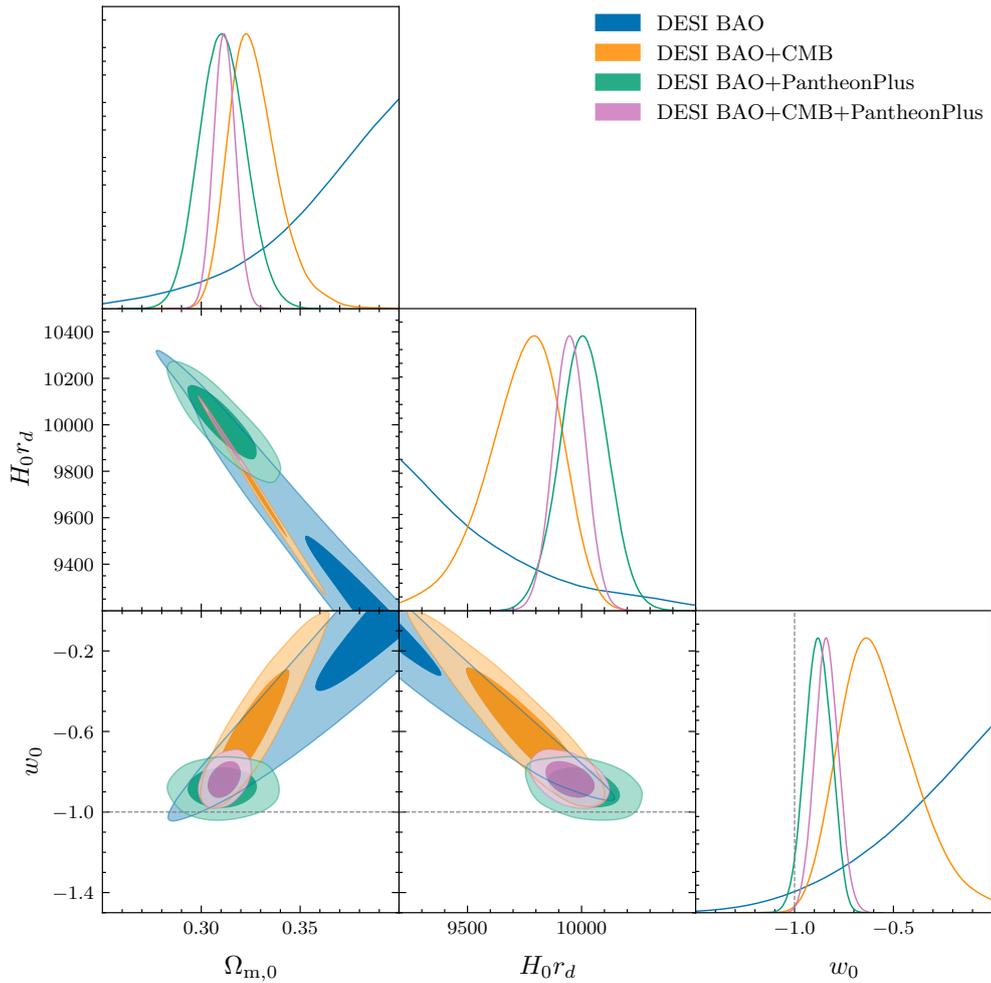
**Figure 4.** Marginalized constraints on the dark energy equation of state  $w(z)$  and energy density  $f_{\text{DE}}(z)$  for the GEDE model, parametrized by Eq. (2.6).

At earlier times, the strongly negative  $w_a$  implies a strongly negative  $w(a)$ , and hence very little dark energy density, before rapidly increasing in energy density while crossing  $w(a) = -1$ . This effectively is acting like GEDE at higher redshift and the thawing class at lower redshift. In Figure 6, we show the reconstructed equation of state  $w(z)$ , crossing the  $w = -1$  threshold near  $z \approx 0.4$ , along with the corresponding evolution of energy density  $f_{\text{DE}}(z)$ ; these results agree with the DESI results in [3, 4].

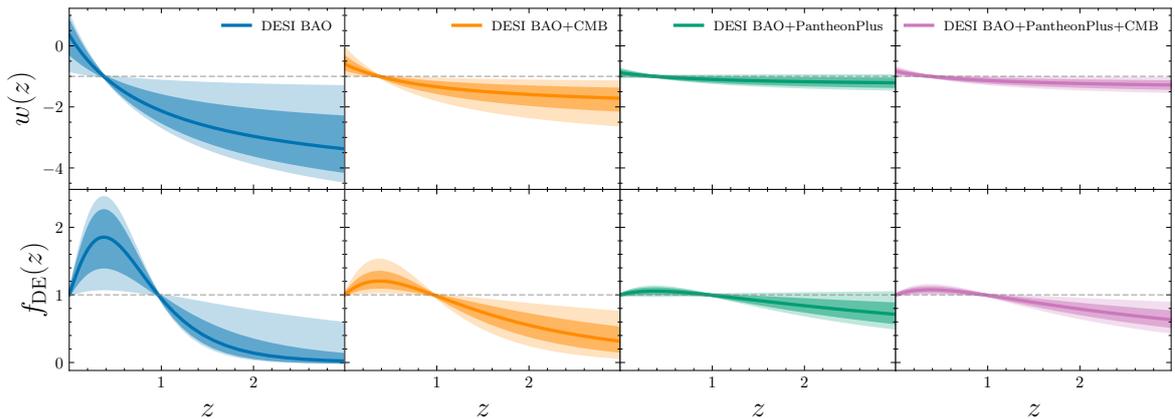
#### 4.4 Comparison and Discussion

Table 2 summarizes the constraints on relevant cosmological parameters. One general aspect to note is that the clustering amplitude parameter  $S_8$  has a rather consistent and reasonable value for all three classes (note that no direct galaxy clustering growth data is used, only BAO). When combining all three cosmological probes, the values of  $H_0$  and  $\Omega_m$  are also quite consistent both across classes and regardless of which supernova dataset is included. For the thawing class,  $w_0$  is pulled somewhat off  $\Lambda$ . For GEDE,  $\Delta$  is mostly consistent with zero (hence  $\Lambda$ ). The mirage class is where the strongest deviation from  $\Lambda$  is seen, and as we discuss next is where the goodness of fit is best as well. Consistency between a class and  $\Lambda$ CDM should be viewed not through the 1D confidence intervals, however, but through the joint parameter constraints and the  $\Delta\chi^2$  quantification.

Table 3 presents how the three classes compare to each other, relative to  $\Lambda$ CDM, and  $w_0w_a$ CDM in goodness of fit ( $\Delta\chi^2$ ), for various combinations of datasets. Here, we report  $\Delta\chi_{\text{MAP}}^2$ , the difference between the maximum a posteriori of the model and the maximum of the posterior fixing  $w_0 = -1$  or  $\Delta = 0$  (i.e. to the cosmological constant case). Note that the three classes have one more parameter than  $\Lambda$ CDM and one less than  $w_0w_a$ CDM. The first general result of interest is that all three classes have better  $\chi^2$  than  $\Lambda$ CDM. They do have one more parameter but in the combination of all three cosmological probes, the improvement is notably more than one. Note that  $w_0w_a$ CDM has a significantly better  $\chi^2$  than  $\Lambda$ CDM, even taking into account its two more parameters, as discussed in [3]. However, the  $\chi^2$  for the physics-focused classes are often close to the  $w_0w_a$ CDM values, while having one less parameter. This is especially true for the mirage class, while the thawing class and GEDE appear to be less favored. As thawing and mirage are subsets of  $w_0w_a$ CDM, their  $\chi^2$  cannot go below that of  $w_0w_a$ ; for the case of fitting DESI BAO data alone, this appears not to hold



**Figure 5.** Marginalized constraints within the mirage class of dark energy described by Eq. (2.8).



**Figure 6.** Marginalized constraints on the equation of state  $w(z)$  for the mirage class, parametrized by Eq. (2.8).

**Table 2.** Constraints on the relevant cosmological parameters

Model/Dataset	$H_0[\text{km s}^{-1} \text{Mpc}^{-1}]$	$\Omega_{\text{m},0}$	$w_0$	$\Delta$	$S_8$
<b>Thawing</b>					
DESI BAO+CMB	$71.0^{+2.4}_{-2.8}$	$0.282 \pm 0.020$	$-1.17 \pm 0.15$	–	$0.812 \pm 0.011$
DESI BAO+CMB+Union3	$66.55 \pm 0.95$	$0.3195 \pm 0.0094$	$-0.906 \pm 0.060$	–	$0.8223 \pm 0.0094$
DESI BAO+CMB+DES-SN5YR	$66.49 \pm 0.61$	$0.3200 \pm 0.0065$	$-0.902 \pm 0.038$	–	$0.8224 \pm 0.0091$
DESI BAO+CMB+PantheonPlus	$67.31 \pm 0.66$	$0.3125 \pm 0.0067$	$-0.954 \pm 0.040$	–	$0.8208 \pm 0.0092$
<b>GEDE</b>					
DESI BAO+CMB	$71.0 \pm 1.5$	$0.282 \pm 0.012$	–	$0.81 \pm 0.40$	$0.8156 \pm 0.0092$
DESI BAO+CMB+Union3	$67.6^{+1.0}_{-0.93}$	$0.3096 \pm 0.0089$	–	$-0.08 \pm 0.25$	$0.8199 \pm 0.0092$
DESI BAO+CMB+DES-SN5YR	$66.80 \pm 0.69$	$0.3166 \pm 0.0066$	–	$-0.28 \pm 0.17$	$0.8207 \pm 0.0091$
DESI BAO+CMB+PantheonPlus	$67.73 \pm 0.74$	$0.3088 \pm 0.0070$	–	$-0.06 \pm 0.18$	$0.8198 \pm 0.0093$
<b>Mirage</b>					
DESI BAO+CMB	$66.2^{+1.3}_{-0.79}$	$0.3271^{+0.0093}_{-0.015}$	$-0.56^{+0.15}_{-0.23}$	–	$0.842 \pm 0.013$
DESI BAO+CMB+Union3	$66.67 \pm 0.59$	$0.3217 \pm 0.0072$	$-0.657^{+0.096}_{-0.11}$	–	$0.838 \pm 0.010$
DESI BAO+CMB+DES-SN5YR	$67.10 \pm 0.44$	$0.3169 \pm 0.0056$	$-0.742 \pm 0.066$	–	$0.8332 \pm 0.0091$
DESI BAO+CMB+PantheonPlus	$67.55 \pm 0.43$	$0.3117 \pm 0.0055$	$-0.837 \pm 0.060$	–	$0.8272 \pm 0.0092$

for the mirage class, but this is due to the limited prior range of  $-3 < w_a < 2$  (also used for  $w_0 w_a$  in [3]) – see the extended degeneracies in Fig. 5. When combining DESI BAO with other data this influence of the prior no longer matters.

The promising  $\Delta\chi_{\text{MAP}}^2$  for the mirage class led us to conduct additional nested-sampling runs using the `PolyChord` sampler [47] to calculate the Bayesian evidence using the `anesthetic` package [48]. We report the Bayes factors of  $|\ln B_{21}| = 2.8$  (0.65), 4.2 (2.4), and 6.4 (2.8) in favor of the mirage class (compared to  $w_0 w_a$ CDM) over  $\Lambda$ CDM for the DESI+CMB with PantheonPlus, Union3, and DES-SN5YR data combinations, respectively. These findings suggest a moderate preference for the mirage class over  $\Lambda$ CDM by the PantheonPlus combination and a strong preference by the Union3 and DES-SN5YR on a Jeffreys’ scale [49, 50].

**Table 3.**  $\Delta\chi_{\text{MAP}}^2 \equiv \chi_{\text{model}}^2 - \chi_{\Lambda\text{CDM}}^2$  values for the different models and data combinations. The minimum  $\chi^2$  values were obtained using `iminuit` [51] and `Py-BOBYQA` [52, 53] minimizer. Note that all data combinations include DESI BAO.

Data	$\Delta\chi_{\text{Thawing}}^2$	$\Delta\chi_{\text{GEDE}}^2$	$\Delta\chi_{\text{Mirage}}^2$	$\Delta\chi_{w_0 w_a}^2$
DESI BAO	–0.2	–0.04	–5.0	–3.8
+CMB	–0.6	–5.7	–7.6	–8.9
+PantheonPlus	–3.2	–3.0	–3.5	–3.5
+Union3	–6.3	–5.2	–8.7	–8.9
+DES-SN5YR	–8.8	–7.7	–10.7	–11.1
+CMB+PantheonPlus	–0.6	–1.7	–9.0	–9.6
+CMB+Union3	–3.0	–3.2	–15.2	–15.6
+CMB+DES-SN5YR	–5.0	–4.8	–17.7	–18.3

## 5 Conclusion

Physics-focused classes can give insight into the nature of dynamical dark energy. Using DESI BAO data combined with different state-of-the-art supernovae compilations (PantheonPlus, Union3, DES-SN5YR) and CMB (Planck and ACT) observations, our main result indicates a preference for evolving dark energy rather than a cosmological constant. This behavior can be very well captured by the mirage class, evolving from  $w < -1$  and low energy density at  $z \gtrsim 1$  to  $w > -1$  more recently. Note that this also gives a hump in the dark energy density at  $z \approx 0.3\text{--}0.5$ , in agreement with our previous model-agnostic findings [4]. The mirage class of dark energy models has a comparable  $\Delta\chi^2$  with that of the  $w_0w_a$ CDM model, while having one less degree of freedom.

The mirage class combines the emergence of dark energy density, perhaps indicative of a phase transition, with the recent evolution of  $w(a)$  to less negative values than the cosmological constant of the thawing class. With DESI+SNe Ia, consistently across the three supernova sets, all three classes have better fits than  $\Lambda$ CDM and come close to  $w_0w_a$ CDM (which has one more parameter). Neither thawing nor GEDE have a strong advantage for DESI+CMB, however, and the combination of all three cosmology probes gives a clear advantage to the mirage class over the other two (which are still better fits than  $\Lambda$ CDM). This preference is reflected in the Bayes factor, showing a moderate to strong preference (depending on the SNe Ia dataset considered) for the Mirage class over  $\Lambda$ CDM. However, the significance of the Bayesian evidences have to be interpreted cautiously [54, 55]. We leave a detailed model-selection analysis for future works.

Other cosmology parameters such as  $H_0r_d$ ,  $\Omega_m$ , and  $S_8$  remain near  $\Lambda$ CDM values when using any of the three classes with the full dataset combination. Together with model independent analyses, such physics-focused classes provide important clues to the physical properties we should seek in dark energy models, beyond the “blank slate” characterization of  $w_0\text{--}w_a$ .

The dark energy properties indicated by the data – consistent with [3, 4] – are rapid evolution from  $w(a \ll 1) \ll -1$  across  $w = -1$  to more recent  $w(a \approx 1) > -1$ , and hence emergent dark energy density at modest redshift while at low redshift an energy density bump together with a slowing down of recent cosmic acceleration (see e.g. the  $q(z)$  reconstruction in [4]). These characteristics do not generally exist simultaneously in the usual dark energy models. Phase transition-type behavior does not generally give  $w$  evolving away from  $\Lambda$  today, and the thawing class evolving away from  $\Lambda$  today does not generally give  $w < -1$ , let alone  $w \ll -1$ , in the past.

If the data and its analysis hold, then we are facing a more complicated dark energy sector than generally treated, possibly involving multiple components or involving special nonlinearities in the action (modified gravity or couplings). Fortunately, further data is imminent, with more DESI BAO data, as well as DESI measurements of redshift space distortions and peculiar velocities that can test cosmic growth and gravity.

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[57], `scipy` [58] and `matplotlib` [59]. This work was supported by the high-performance computing cluster Seondeok at the Korea Astronomy and Space Science Institute. A.S. would like to acknowledge the support by National Research Foundation of Korea 2021M3F7A1082056, and the support of the Korea Institute for Advanced Study (KIAS) grant funded by the government of Korea.

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The DESI collaboration is honored to be permitted to conduct scientific research on Iolkam Du’ag (Kitt Peak), a mountain with particular significance to the Tohono O’odham Nation.

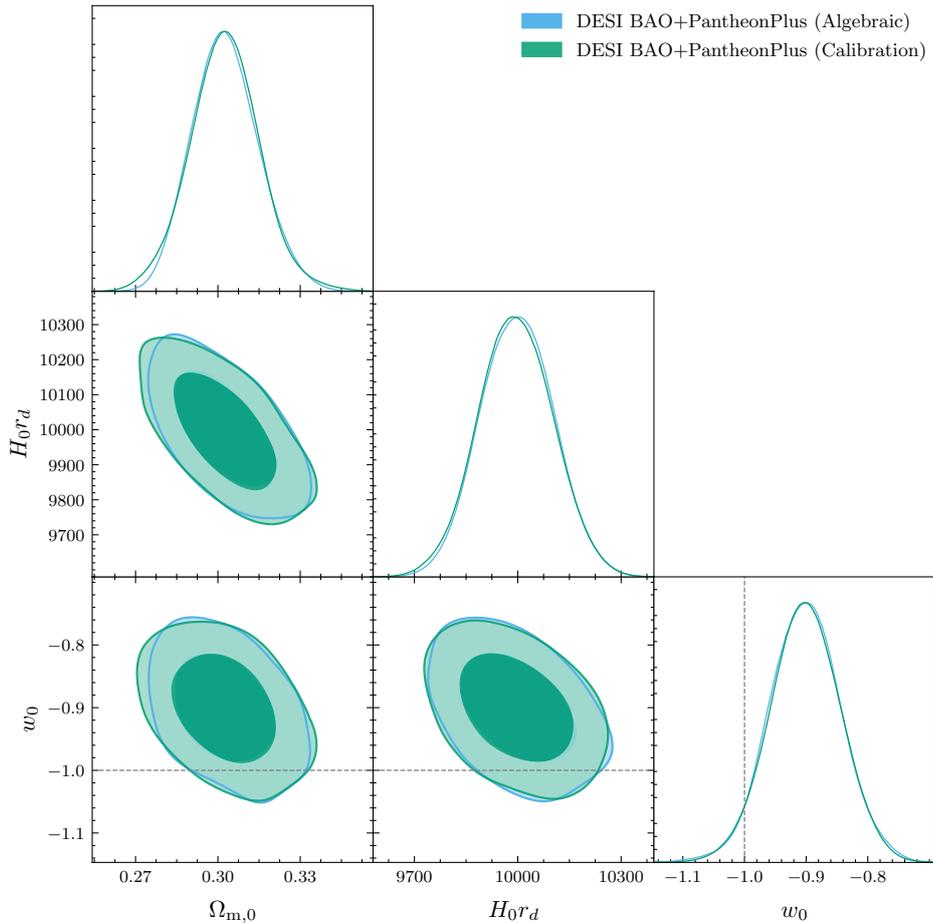
## Data Availability

The data used in this analysis will be made public along the Data Release 1 (details in <https://data.desi.lbl.gov/doc/releases/>).

## A Thawing Class: Calibration vs Algebraic Forms

The thawing class encompasses rich physics, including pseudo-Nambu Goldstone bosons (PNGB axions), the shift symmetric linear potential, and the classic  $\phi^2$  and  $\phi^4$  potentials. The calibration Eq. (2.4) and algebraic Eq. (2.5) forms were shown to accurately describe the exact numerical solutions for observables to  $\sim 0.1\%$  (e.g. Table 1 of [12], and [2]). The former emphasizes the calibration, i.e. model independent, aspects of the physics, and the latter the dynamical evolution flow, but each captures the essential physics and Figure 7 confirms that the two forms give nearly identical results. The specific numbers quoted in this work use the calibration form.

Note that while the algebraic form Eq. (2.5) does not cross  $w = -1$  while the calibration form Eq. (2.4) does, they both describe the *observations* nearly identically, with excellent accuracy. Thus not every  $w(a)$  that crosses  $-1$  indicates a physical crossing of  $-1$ ; the forms are designed to describe the observations, not  $w(a)$  itself, as emphasized in Section 4.1. However, for  $w_0$  too far from  $-1$ , i.e.  $|w_a|$  large enough, such apparent crossings will not fit certain observations like the distance to CMB last scattering, and so  $|w_a| \gtrsim 1$  often does point to a real crossing of  $-1$  by  $w(a)$ .



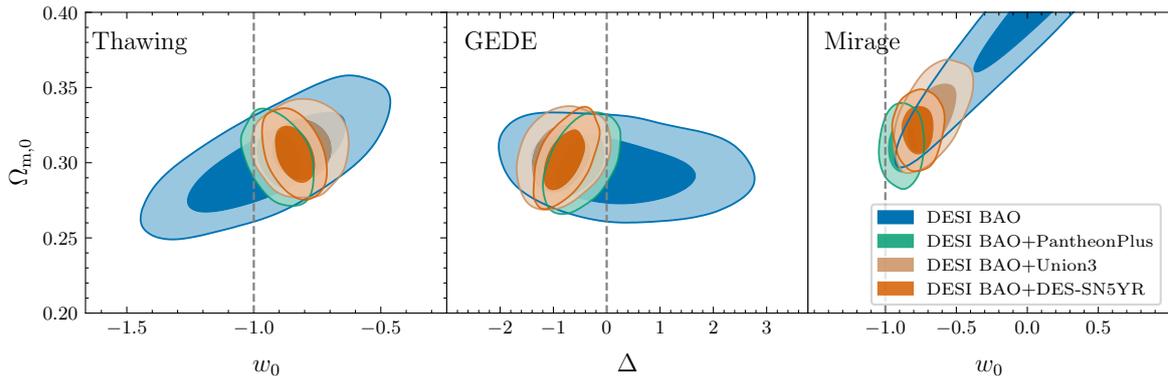
**Figure 7.** Comparison of the calibration Eq. (2.4) vs algebraic Eq. (2.5) parametrizations of the thawing class of dark energy, using DESI BAO+PantheonPlus.

## B Supernova Data Comparison

The figures in the main section of the paper use PantheonPlus as the supernova dataset for clarity of presentation by limiting the number of contours. Tables 2 and 4 list the parameter constraints for each supernova dataset in turn. Here, Figure 8 presents the joint confidence contours using DESI BAO in combination with each supernova set in turn. The results are quite consistent between each supernova dataset and a similar trend can also be seen in Figure 6 of [3] for  $w_0w_a$ CDM.

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**Figure 8.** Marginalized posterior distributions using DESI BAO and each supernova dataset. The vertical dashed line indicates  $\Lambda$ CDM.

**Table 4.** Constraints on the relevant cosmological parameters for DESI BAO and DESI BAO+SNe Ia datasets.

Model/dataset	$\Omega_{m,0}$	$H_0 r_d$ [km s $^{-1}$ ]	$w_0$	$\Delta$
<b>Thawing</b>				
DESI BAO	$0.300^{+0.020}_{-0.023}$	$10080 \pm 410$	$-0.94 \pm 0.20$	–
DESI BAO+PantheonPlus	$0.303 \pm 0.013$	$9994 \pm 110$	$-0.901 \pm 0.057$	–
DESI BAO+Union3	$0.309 \pm 0.013$	$9835 \pm 140$	$-0.811^{+0.079}_{-0.070}$	–
DESI BAO+DES-SN5YR	$0.306 \pm 0.012$	$9890 \pm 100$	$-0.840 \pm 0.052$	–
<b>GEDE</b>				
DESI BAO	$0.296^{+0.014}_{-0.016}$	$10170 \pm 330$	–	$0.12^{+0.81}_{-1.2}$
DESI BAO+PantheonPlus	$0.299 \pm 0.013$	$9993 \pm 110$	–	$-0.49^{+0.27}_{-0.32}$
DESI BAO+Union3	$0.303 \pm 0.014$	$9845 \pm 140$	–	$-0.86^{+0.30}_{-0.40}$
DESI BAO+DES-SN5YR	$0.302 \pm 0.014$	$9871 \pm 99$	–	$-0.80^{+0.24}_{-0.27}$
<b>Mirage</b>				
DESI BAO	$0.430^{+0.066}_{-0.044}$	$8813^{+300}_{-630}$	$> 0.078$	–
DESI BAO+PantheonPlus	$0.311 \pm 0.012$	$10010 \pm 100$	$-0.880 \pm 0.065$	–
DESI BAO+Union3	$0.331 \pm 0.015$	$9768 \pm 150$	$-0.67 \pm 0.11$	–
DESI BAO+DES-SN5YR	$0.322 \pm 0.011$	$9875 \pm 99$	$-0.770 \pm 0.073$	–

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