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The Hierarchical Growth of Bright Central Galaxies and Intracluster Light as Traced by the Magnitude Gap

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ABSTRACT

Using a sample of 2800 galaxy clusters identified in the Dark Energy Survey across the redshift range 0.20 < z < 0.60, we characterize the hierarchical assembly of Bright Central Galaxies (BCGs) and the surrounding intracluster light (ICL). To quantify hierarchical formation we use the stellar mass - halo mass (SMHM) relation for the BCG+ICL system and incorporate the magnitude gap (M14), the difference in brightness between the BCG (measured within 30 kpc) and 4th brightest cluster member galaxy within $0.5 R_{200,c}$. The inclusion of M14, which traces BCG hierarchical growth, increases the slope and decreases the intrinsic scatter in the SMHM relation, highlighting that it is a latent variable within the BCG+ICL SMHM relation. Moreover, the correlation with M14 decreases at large radii from the BCG's centre. However, the stellar light within the BCG+ICL transition region (30 kpc - 80 kpc) most strongly correlates with the dark matter halo mass and has a statistically significant correlation with M14. As the light in the transition region and M14 are independent measurements, the transition region may grow as a result of the BCG's hierarchical two-phase formation. Additionally, as M14 and ICL result from hierarchical growth, we use a stacked sample and find that clusters with large M14 values are characterized by larger ICL and BCG+ICL fractions, which illustrates that the merger processes that build the BCG stellar mass also grow the ICL. Furthermore, this may suggest that M14 combined with the ICL fraction can be used as a method to identify dynamically relaxed clusters.

1 INTRODUCTION

Bright Central Galaxies (BCGs) are massive, radially extended, elliptical galaxies located near the centre of their host cluster's dark matter halo. BCGs grow hierarchically, by merging with smaller galaxies over time (e.g., De Lucia & Blaizot 2007; Oser et al. 2010; van Dokkum et al. 2010). The combination of hierarchical formation and central location results in a correlation between the properties of the BCG and the cluster's dark matter halo (Jones & Forman 1984; Rhee & Latour 1991; Lin & Mohr 2004; Lauer et al. 2014). This galaxy-halo connection provides key information in characterizing the formation history of these massive galaxies.

Observations, simulations, and semi-analytic models (Croton et al. 2006; De Lucia & Blaizot 2007; Guo et al. 2011; Tonini et al. 2012; Shankar et al. 2015) suggest that BCGs grow as a result of a two-phase formation (Oser et al. 2010; van Dokkum et al. 2010). At high redshift (z > 2) a dense core ($r <\approx 10$ kpc), which contains $\approx 25\%$ of the stellar mass is formed via in-situ star formation. At

z < 2, the outer envelope grows hierarchically as a result of major and minor mergers. This outer envelope extends to the faint and diffuse halo of intracluster light (ICL; Zwicky 1933, 1951) that is observed around BCGs. Indeed, the presence of ICL can be used to differentiate BCGs from similarly massive non-central galaxies. Therefore, it is unsurprising that prior works have suggested that at least part of the ICL forms due to the BCG's hierarchical assembly process (e.g., Murante et al. 2007; Golden-Marx et al. 2023).

Due to the faint and diffuse nature of the ICL, deep, high resolution photometry with a large field-of-view is needed to accurately characterize the ICL. Using such observations, individual clusters have measurements of the ICL that extend out to hundreds of kiloparsecs from the BCG (e.g., Kluge et al. 2020; Montes et al. 2021; Montes & Trujillo 2022; Golden-Marx et al. 2023; Kluge et al. 2024). However, these observations can be enhanced by stacking the ICL signal surrounding many BCGs. Doing so, prior analyses have found that the ICL extends as far out as Mpc scales (Zibetti et al. 2005; Zhang et al. 2019c; Chen et al. 2022; Zhang et al. 2024). Although the ICL can be measured out to large radii, it is observationally challenging to distinguish the light associated with the BCG and that of the ICL.

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Therefore, we do not disentangle the BCG and ICL; instead, we focus on the BCG+ICL system and use fixed radial apertures to define our measurements, as introduced in Pillepich et al. (2018). In this analysis, we define similar radial regimes as Zhang et al. (2024); the BCG refers to the inner 30 kpc, the BCG+ICL transition regime is 30 kpc - 80 kpc, and the ICL is the light beyond 80 kpc.

The stellar mass-halo mass (SMHM) relation is a commonly used observational formalism to quantify the galaxy-halo connection for galaxy clusters $(\log_{10}(M_{halo}/(M_{\odot}/h)) \ge 14.0)$ due to its low intrinsic scatter, σ_{int} , in stellar mass at fixed halo mass, which observations and simulations measure as ≈ 0.15 dex (e.g., Zu & Mandelbaum 2015; Pillepich et al. 2018; Kravtsov et al. 2018; Golden-Marx & Miller 2018). In logarithmic scale, this is a linear relation, which directly compares the stellar mass of the BCG to the total mass of the cluster with the form: $\log_{10}(M_*) \propto \text{slope} \times \log_{10}(M_{halo})$. Moreover, measurements of the SMHM relation's parameters, such as the slope and σ_{int} provide insight into BCG growth and evolution (Gu et al. 2016; Golden-Marx & Miller 2019; Golden-Marx et al. 2023).

As a result of the two-phase growth, information about the BCG's recent stellar mass growth is contained within the BCG's outer envelope and ICL (Oser et al. 2010; van Dokkum et al. 2010). It follows that measurements of the SMHM relation in both observations and semi-analytic models have found that the slope increases in progressively larger radii (Moster et al. 2018; Golden-Marx & Miller 2019). Moreover, Golden-Marx et al. (2023) extended this analysis to the ICL and found that the SMHM relation's slope increases to an asymptote at ~100 kpc. Moreover, recent work found that the underlying halo mass is more strongly correlated with the light from the outer envelopes (50 kpc-100 kpc (Huang et al. 2022) or 30 kpc - 50 kpc (Golden-Marx et al. 2023)) than the light from the BCG's core. Thus, the ICL is imprinted with information about recent mergers, which strengthens the correlation with the underlying halo mass.

Accounting for latent variables, which ideally increase the slope and decrease σ_{int} also strengthens statistical correlations. One observational measurement inherently tied to BCG hierarchical growth is the magnitude gap, the difference in r-band magnitude between the BCG and 4th brightest cluster member within half the radius enclosing 200 times the critical density of the Universe $(R_{200,c})$ (Dariush et al. 2010), referred to as M14 throughout this analysis. N-body simulations found that BCG stellar mass linearly increases with the number of progenitor galaxies (Solanes et al. 2016). Thus, as BCGs grow hierarchically, they increase in stellar mass and brightness, while the satellite galaxies remain fixed or merge with the BCG. Therefore, BCG growth increases M14 yielding the correlation between M14 and BCG stellar mass (Harrison et al. 2012; Golden-Marx & Miller 2018, 2019; Golden-Marx et al. 2022). Thus, M14 traces the BCG's hierarchical assembly (Golden-Marx & Miller 2018) and acts as an indicator of the BCG's dominance over other cluster member galaxies, similar to the Bautz-Morgan classification (Bautz & Morgan 1970). Additionally, Vitorelli et al. (2018) found that clusters with larger magnitude gaps, defined using the 2nd brightest galaxy (M12), are more concentrated and likely formed earlier, suggesting that the magnitude gap traces cluster formation.

Based on Golden-Marx & Miller (2018), M14 is a statistical latent parameter within the cluster SMHM relation, as it increases the slope and decreases σ_{int} by as much as 50% (Golden-Marx & Miller 2018, 2019; Golden-Marx et al. 2022). Moreover, reducing σ_{int} , tightens the constraints on the slope, which allowed for the detection of redshift evolution of the SMHM relation's parameters (Golden-Marx & Miller 2019; Golden-Marx et al. 2022). We also note that the M14 correlation holds if M12 is used (Golden-Marx & Miller 2018). We use M14 because it yields a stronger correlation with early formation (Dariush et al. 2010). Moreover, the variance in the selection of the 4th brightest galaxy (and thus its magnitude) is less susceptible to large uncertainty due to foreground or background interloper galaxies, cluster mergers with multiple central galaxies, or recently infalling bright galaxies.

The ICL and M14 result from BCG hierarchical assembly. However, it remains unclear how these parameters are related. The ICL is a direct measurement of the diffuse light that surrounds the BCG and can be used as a fossil tracer of the BCGs assembly history, while M14 is a measure of the BCGs hierarchical assembly within the cluster environment. Therefore, in this paper we present measurements of the correlation of the BCG+ICL stellar content with halo mass and M14 (an extension of the work presented by Golden-Marx et al. (2023)) to determine for the first time how these parameters correlate in the context of BCG hierarchical assembly and the SMHM relation. For this analysis, we use the Dark Energy Survey (DES; DES Collaboration 2005) Y6 sample of clusters, currently the only statistically large (> 1000) sample of clusters that such measurements of the ICL can be taken within the redshift range 0.2 < z < 0.6.

The remainder of this paper is outlined as follows. In Section 2, we define our observational sample, the DES Y3 redMaPPer cluster sample and DES Y6 data, and the data reduction methods. In Section 3, we present the measurements of the stellar mass content of the BCG+ICL system, halo mass, and M14. In Section 4, we describe the hierarchical Bayesian model used to measure the parameters of the SMHM relation. In Section 5, we present our analysis of the SMHM relation for the BCG+ICL system. In Section 6, we discuss the correlation between M14 and ICL, including the ICL fraction. Finally, we conclude in Section 7.

In this analysis, we assume a flat Λ CDM universe, with Ω_M =0.30, Ω_{Λ} =0.70, H₀=100 *h* km/s/Mpc with *h*=0.7.

2 DATA

2.1 DES Y6 data

The Dark Energy Survey (DES) is a wide-area multi-band photometric sky survey covering $\approx 5,000$ square degrees across five photometric wavebands (g, r, i, z, Y) taken using the Victor M. Blanco 4-m telescope beginning with Science Verification in 2012 and ending in 2019 with the Year 6 observations. The DES Year 6 data, which includes all prior DES data releases, features several layers of singleepoch images combined to create deep photometry that allow us to capture low surface brightness features. DECam, the imager used for DES, features a large 2.2 degree field-of-view, a 570 megapixel camera constructed using a CCD mosaic, and a low-noise electronic readout system (Flaugher et al. 2015). These properties make DE-CAM ideal for studying faint and extended diffuse sources, including the ICL, in the optical from the ground in a single field-of-view.

The data used throughout this analysis, both the source catalogs and the images, come from the DES Y6 co-addition (this includes publicly released data from DES Data Release 2 (Abbott et al. 2021)). The DESY6 images are deeper than the Y3 versions and provide a more uniform co-add with an improved background subtraction. Since this work focuses on the diffuse ICL, these improvements, which include the improved masking of faint galaxies located spatially near/within the ICL, are key. Such faint galaxies can unintentionally be treated as part of the ICL, thus, these improvements enhance our ability to accurately measure the contribution from the ICL by strengthening our ability to delineate between the diffuse light and total light within the cluster, which includes all cluster member galaxies and the ICL. The improvements seen in the final images presented in Abbott et al. (2021) take advantage of additional exposures and tilings that cover the entire DES footprint. For these images, a single-epoch background subtraction is performed, instead of a "global" Swarp (Bertin 2010) background subtraction. Like in Golden-Marx et al. (2023) and Zhang et al. (2024) the science images are an average of the *riz* photometry. Moreover, the DESY6 photometry allows for a fainter detection threshold (5 σ) than what was used in previous data releases (10 σ).

2.2 redMaPPer Cluster Sample

In this analysis, we use the DES Y3 redMaPPer cluster catalog version 6.5.22+2, based on DES Year 3 Gold photometric data (Sevilla-Noarbe et al. 2021). This version of the redMaPPer cluster catalogue contains over 21,000 galaxy clusters with a redMaPPer defined richness, λ , greater than 20, which corresponds to a halo mass lower limit of $10^{14.1}$ M_{\odot} (McClintock et al. 2019). Moreover, we take advantage of redMaPPer's membership catalogue which provides the probability (Pmem) and DES r-band model magnitude of each cluster member, to measure M14 and central galaxy probability (P_{Cen}), for BCG identification. We note that redMaPPer selects a luminous cluster galaxy located nearest to the centre of the cluster's gravitational potential well and provides the information for the five most probable central candidates per cluster. We assume that the most likely central galaxy candidate is the BCG. Based on multi-wavelength measurements, this selection has been shown to be correct with an $\sim 80\%$ frequency (Saro et al. 2015; Zhang et al. 2019a; Bleem et al. 2020).

2.3 Measuring the ICL

The BCG and ICL profiles used in this analysis are data products derived as part of Zhang et al. (2024), which uses a similar methodology as Zhang et al. (2019c), Sampaio-Santos et al. (2021), Golden-Marx et al. (2022), and Golden-Marx et al. (2023). Below, we briefly summarize the methodology used in Zhang et al. (2024).

• We analyse only clusters in the redshift range 0.2 < z < 0.6, which reduces the number of redMaPPer ($\lambda > 20$) clusters from 21092 to 15654.

• The BCGs were selected as the most probable central galaxy provided by redMaPPer. The impact of using all BCGs regardless of redMaPPer P_{Cen} is discussed in the Appendix.

• Using these BCGs, the DES database was queried to select images within a 0.15 deg \times 0.15 deg region centred on the BCG. These individual images were combined (using mean pixel values) to create the final coadd image centred on the BCG. The images used throughout this analysis have not had a local sky background subtraction (measured either with Source Extractor (Bertin & Arnouts 1996) or Swarp (Bertin 2010)) applied. Instead, these images underwent a global background subtraction process (estimated across the whole Field-of-View, about 2.5 deg² for single exposure images; Bernstein et al. 2017). This background subtraction is done because local background regions often include the ICL, which results in an underestimation of the light in the BCG+ICL outer profiles (e.g., von der Linden et al. 2007; Golden-Marx & Miller 2018).

• To prevent contamination of our BCG+ICL light profiles from bright foreground stars and galaxies, clusters with BCGs near such objects were removed, reducing the number of available clusters in our sample to 7042.

• Using the BCG as the centre, all objects covering a 0.2 deg \times 0.2 deg region surrounding the BCG in the DES database were

identified. We acknowledge that miscentring exists in redMaPPer (see Zhang et al. (2019a)). However, this is not corrected for in the reduction process. As shown in the Appendix, when we look at high and low probability centrals, we find no evidence that it impacts the parameters of the SMHM relation as shown in Tables A1 and A2.

• Elliptical masks, with a semi-major axis of 3.5 $R_{\rm Kron}$ (Kron 1980), were placed around all galaxies above a selected masking limit, excluding the BCG, allowing for the measurement of a BCG+ICL profile. The masking limit is a *z*-band magnitude limit, based on the cluster's photometric redshift, of 0.2*L**, where *L** is the characteristic luminosity of a cluster red galaxy luminosity function measurement (Zhang et al. 2019b).

• Using the BCG as the central point, the surface brightness profiles (mean values) of the unmasked regions for each galaxy cluster, representative of the BCG+ICL light profile, were measured in circular radial annuli. We note that using simulations, Brough et al. (2024) find no statistical difference between measurements of the ICL done using circular and elliptical annular profiles. These measurements are the surface brightness radial profile for each cluster, which contain light from the cluster's BCG and ICL as well as some background light. Masked regions are excluded from the measurement process.

• The surface brightness measurements described in the previous step also contain residual background light and contributions from unmasked foreground and background objects. For each radial surface brightness measurement, we take their values at the radial range beyond 500 kpc as the "background" value, and subtract this "background" value from the corresponding measurements. The robustness of this background measurement was discussed in the Appendix of Golden-Marx et al. (2023).

• Lastly, we remind the reader that unlike Zhang et al. (2019c), Sampaio-Santos et al. (2021), and Zhang et al. (2024), we do not stack the measurements of the ICL on a secondary cluster property such as richness. Instead, we only combine images of the same cluster to create a deeper photometric image.

3 THE OBSERVABLE MEASUREMENTS FOR CONSTRUCTING THE SMHM RELATION

3.1 BCG Stellar Mass

The stellar mass is estimated in the same manner as in Golden-Marx et al. (2023), so we summarize the method. For each cluster, using the BCG+ICL system's light profile (see Section 2.3) we measure the apparent magnitude within a given radial aperture by integrating the light profile between the selected inner and outer radii in the DES i-band. In this analysis we use the following apertures: 0-30 kpc, 0-80 kpc, 0-150 kpc, 0-225 kpc, 0-300 kpc, 30-80 kpc, 80-150 kpc, 150-225 kpc, 225-300 kpc.

Using the selected aperture magnitudes, we use the EzGal (Mancone & Gonzalez 2012) SED modelling software to estimate the stellar mass. For EzGal, we assume a passive spectral model, as DES photometry prevents us from statistically constraining additional star formation parameters such as burst times and formation epochs. For converting magnitude to stellar mass, we assume the same parameters as Golden-Marx & Miller (2019), Golden-Marx et al. (2022), and Golden-Marx et al. (2023); a Bruzual & Charlot (2003) stellar population synthesis model, a Salpeter (1955) Initial Mass Funtion (IMF), a formation redshift of z = 4.9, and a metallicity of 0.008 (66% Z_{\odot}). These parameters were selected to minimize the χ^2 statistic between the measured and EzGal modeled photometry. Following Golden-Marx et al. (2022) and Golden-Marx et al. (2023), we assume a subsolar metallicity for each BCG+ICL system since observations find that the metallicity of early type galaxies decreases radially outward (McDermid et al. 2015) and light from the ICL has been characterized as having a subsolar metallicity (Montes & Trujillo 2018). Additionally, we note that our stellar mass estimate is independent of our choice of formation redshift and that changing the Salpeter (1955) IMF to a Chabrier (2003) IMF uniformly lowers our stellar mass estimates by ≈ 0.25 dex. Thus, the SMHM relation's amplitude is the only SMHM parameter impacted.

Since our Bayesian infrastructure relies on an estimate of measurement uncertainty, we assume the same uncertainty in stellar mass, 0.06 dex, as in Golden-Marx et al. (2022) and Golden-Marx et al. (2023). This is likely a lower limit on the estimated uncertainty in stellar mass, in particular when we incorporate the ICL. If a larger uncertainty is required, this only changes σ_{int} . The remaining parameters are consistent. While our MCMC analysis measures σ_{int} , a detected change of σ_{int} with radius may reflect our underestimation of the uncertainty in the stellar mass at large radii.

3.2 DES Cluster Richnesses and Halo Masses

Unlike in Golden-Marx et al. (2023), which used the DES-ACT overlap sample (Hilton et al. 2021) and SZ-estimated halo masses, for the DES clusters, we use redMaPPer richness, λ . This richness is converted to halo mass using the DES Year 1 calibrated mass-richness relation (McClintock et al. 2019), given by Equation 1,

$$M_{\rm halo}/(h^{-1}M_{\odot}) = 10^{14.344} (\lambda/40)^{1.356} (\frac{1+z_{\rm red}}{1+0.35})^{-0.30}$$
(1)

where M_{halo} refers to M_{200m} , z_{red} is the redMaPPer photometric redshift and λ is the redMaPPer richness. We note that the McClintock et al. (2019) mass-richness relations has an intrinsic scatter associated with the halo mass at fixed richness. While not shown in Equation 1, we account for this scatter in our Bayesian MCMC analysis, as discussed in Section 4. Although we are using the DES Y3 redMaPPer catalogue a preliminary analysis of the DES-redMaPPer Y3 mass-richness relationship is consistent with the Y1 analysis.

We note that a bias has been found in the weak lensing calibration of the McClintock et al. (2019) mass-richness relation. The halo masses are biased ≈ 0.1 dex low, with the $\lambda < 30$ clusters most strongly impacted (Abbott et al. 2020; Costanzi et al. 2021). For this analysis, if only the low- λ clusters have halo masses that are biased low, this bias would result in a value of the slope that is also biased low and may also impact the offset parameter. Since this would be a uniform bias across each aperture measurement of the SMHM relation, the bias would not affect our ability to characterize how incorporating ICL and M14 change the SMHM relation and thus would not impact the conclusions of this analysis.

Here, we treat the uncertainty in the mass-richness relation as a fixed value identical to what was found for the SDSS and DES redMaPPer clusters in Golden-Marx & Miller (2019) and Golden-Marx et al. (2022) because these measurements come from the same algorithm. We remind the reader that our chosen value, 0.087 dex, was determined in Golden-Marx & Miller (2019) from a joint analysis where the parameters for the SMHM relation were simultaneously determined for a sample with halo masses estimated by richness and the caustic phase-space technique. This scatter in halo mass at fixed richness corresponds to 0.20 in a natural log scale, which is in excellent agreement with Rozo et al. (2015), which measures a value between 0.17-0.21.

3.3 Magnitude Gap (M14)

M14 is defined uniformly throughout this paper, regardless of our choice of BCG+ICL aperture stellar mass. For the DES-redMaPPer clusters we identify cluster members as those with $P_{\text{mem}} \ge 0.9$. This is a less restrictive than Golden-Marx & Miller (2019) and Golden-Marx et al. (2022) since we do not match to the C4 catalog (Miller et al. 2005). This P_{mem} choice optimizes the number of clusters in our sample and only reduces the sample from 7042 to 6903 clusters. When we did this analysis with a threshold of $P_{\text{mem}} \ge 0.8$ our results were consistent.

We define M14 following Dariush et al. (2010) as the difference in the *r*-band apparent model magnitude of the 4th brightest cluster member (with $P_{\text{mem}} \ge 0.9$) within $0.5R_{200,c}$ and the BCG's inner 30 kpc *r*-band apparent magnitude. We estimate $R_{200,c}$ for redMaP-Per clusters using the following equations from Rykoff et al. (2014):

$$R_{200,c} \approx 1.5 R_c(\lambda) \tag{2}$$

where λ is the redMaPPer richness, and R_c is the redMaPPer cutoff radius, given by Equation 3:

$$R_c(\lambda) = 1.0h^{-1}(\lambda/100)^{0.2} \text{Mpc.}$$
(3)

Since we use DES data, we estimate the M14 uncertainty in the same manner as in Golden-Marx et al. (2022) and assume a value of 0.31. While this value may be an upper limit due to our lower P_{mem} criterion (as opposed to $P_{\text{mem}} > 0.984$ used in Golden-Marx et al. (2022)) this is unlikely to change our results as our Bayesian analysis is robust to moderate changes in the M14 uncertainty. For example, if we increase the M14 uncertainty to 0.5, our values remain in agreement.

4 THE STATISTICAL MODELLING OF THE SMHM RELATION

We measure the parameters of the SMHM relation using a similar hierarchical Bayesian MCMC approach to what is described in Golden-Marx & Miller (2019) and Golden-Marx et al. (2023). We quantify the SMHM relation using Equation (4), when M14 is incorporated

$$\log_{10}(M_*/M_{\odot}) = N(\alpha + \beta \times \log_{10}(M_{halo}/M_{\odot}) + \gamma \times (M14), \sigma_{int}^2)$$
(4)

and Equation 5, when it is not

$$\log_{10}(M_*/M_{\odot}) = N(\alpha + \beta \times \log_{10}(M_{\text{halo}}/M_{\odot}), \sigma_{\text{int}}^2)$$
(5)

where α is the mathematical offset, β is the slope of the SMHM relation, γ is the M14 parameter, and σ_{int} is the intrinsic scatter in stellar mass at fixed M_{halo} . This is a nested model, if γ =0, Equation 4 reverts to Equation 5. The only differences between the model used in this analysis and those in Golden-Marx & Miller (2019) and Golden-Marx et al. (2023) are that we do not account for redshift evolution and we include γ , respectively.

A Bayesian formalism works by convolving prior information associated with a selected model with the likelihood of the observations given that model, to yield the posterior distribution for the non-nuisance parameters in our model. To determine the posterior distributions for each SMHM parameter, our MCMC model generates values for the observed aperture stellar masses, richness-estimated halo masses, and M14s at each step in our likelihood analysis, which are directly compared to the observed measurements.

We model the \log_{10} BCG stellar masses (y), \log_{10} halo masses

(x), and M14 values (z) as normal distributions with mean values (locations) taken from our measurements. The standard deviations associated with each value is taken from measurement uncertainties, described in Section 3 (σ_{x0} , σ_{y0} , σ_{z0}) as well as a stochastic component from a beta function, $\beta(0.5, 100)$ (Golden-Marx & Miller 2018), which allows for additional uncertainty on the observational errors. These errors are treated statistically in the Bayesian model as free nuisance parameters σ_x , σ_y , and σ_z . Additionally, as done in Golden-Marx & Miller (2019), Golden-Marx et al. (2022), and Golden-Marx et al. (2023), we reduce the covariance between α and β by subtracting off the median values of the upper and lower limits in $\log_{10}(M_*/M_{\odot})$ and $\log_{10}(M_{halo}/M_{\odot})$, 11.3 and 14.55 respectively. For consistency we subtract off the median stellar mass measured within 0-30 kpc in each aperture bin.

Due to the lack of detected evolution in the stellar mass of the ICL found in Golden-Marx et al. (2023) and Zhang et al. (2024),

 $p(\alpha, \beta, \gamma, \sigma_{\text{int}}, x_i, \sigma_{y_i}, \sigma_{x_i}, \sigma_{z,i} | x, y, z) \propto$

and the results from Golden-Marx et al. (2022), which find that the majority of the evolution in the parameters of the SMHM relation (when including M14) occurs in the redshift range z < 0.25, much of which is below the redshift range we observe, we do not allow for the parameters of the SMHM relation to vary with redshift.

The parameters of the SMHM relation are given in Table 1, where each i^{th} cluster is a component in the summed log likelihood and the terms marked 0i are representative of the observed data.

Additionally, we reiterate that this is a nested Bayesian model, which allows for γ to equal 0. Thus any statistically significant non-zero γ is real and signifies that including M14 improves the fit to the measured data. If a correlation between M14 and stellar mass did not exist in our data or added additional noise, we would not detect a statistically significant γ parameter. This discussion is expanded in Table A3 in the Appendix.

$$\underbrace{\sum_{i} P(y_{0i}|\alpha,\beta,\sigma_{y_{i}},\sigma_{\text{int}},x_{i},z_{i}) P(x_{0i}|x_{i},\sigma_{x_{i}}) P(z_{0i}|z_{i},\sigma_{z_{i}}) \times}_{\text{likelihood}}_{\text{likelihood}}$$

$$\underbrace{p(x_{i}) p(\sigma_{x_{i}}) p(\sigma_{y_{i}}) p(\sigma_{x_{i}}) p(\alpha) p(\beta) p(\gamma) p(\sigma_{\text{int}})}_{\text{likelihood}}$$
(6)

priors

5 THE OBSERVED SMHM RELATION

As discussed in Section 1, many recent analyses have focused on the connection between the ICL and the cluster's dark matter halo. Recent observations (e.g., Montes & Trujillo 2019) suggest the light distribution of the ICL may trace the halo's dark matter distribution. Moreover, prior results have identified statistically significant correlations between the stellar mass contained within the ICL and the cluster's halo mass (e.g., Sampaio-Santos et al. 2021; Huang et al. 2022; Golden-Marx et al. 2023). As presented in Golden-Marx et al. (2023), accounting for the ICL increases the slope, β , of the SMHM relation by 0.1-0.15. Thus, as a result of BCG+ICL hierarchical growth, the larger slope is measured because ICL, due to recent growth, is more correlated with the dark matter halo mass. Here, for the first time, we analyse the correlation between M14 and the ICL and investigate both quantitatively and qualitatively the impact of incorporating the ICL and M14 into the SMHM relation.

Our observational sample consists of all redMaPPer clusters (λ > 20) in the redshift range 0.2 < z < 0.6 with at least 4 high probability member galaxies ($P_{mem} > 0.90$). We remove a large fraction of clusters that as a result of masking of either bright stars or nearby galaxies, we are unable to measure the BCG+ICL profile, reducing our sample size to 2929. Lastly, we remove those clusters that we were unable to measure the light out to 300 kpc leaving our final analysis sample as 2788 cluster. These criteria are summarized in Table 2.

5.1 The BCG+ICL+M14 SMHM relation

First, we address the entire BCG+ICL profile and how the SMHM relation varies as we increase the outer radius. Specifically, we use the

0-30 kpc, 0-80 kpc, 0-150 kpc, 0-225 kpc, and 0-300 kpc apertures as shown in Figure 1. We note that the ICL is defined as incorporating all light beyond the transition region (r > 80 kpc). However, as we were unsure of whether M14 continues to correlate with BCG+ICL stellar mass out to the full extent of the ICL, we divide the ICL into multiple apertures.

Figure 1 visualizes the stellar mass within the selected aperture plotted against the halo mass for each annulus, colour coded by M14. In each subplot, we overplot three lines, which are representative of the median of one-third of the data sorted by M14. The median M14 values are 0.90 (dark blue), 1.50 (green) and 2.10 (yellow). In the final subplot, we overlay the posterior distribution from our MCMC analysis for samples representative of the upper and lower M14 values to illustrate our fitting.

To quantify the impact of including the ICL and M14 on the parameters of the SMHM relation, we present the values of the posterior distribution (both for when M14 is and is not incorporated) in Table 3. For consistency, we see that the results in the radial range of 0 < R < 30 kpc are in excellent agreement with the results presented in Golden-Marx & Miller (2019) and Golden-Marx et al. (2022). Moreover, these SMHM relation parameters are within 1σ of the values of β and σ_{int} measured in Golden-Marx et al. (2023) (due to the different median subtraction values, we can't compare α), which shows our results are not biased by the use of richness-inferred halo masses as opposed to SZ-estimated halo masses.

In terms of including M14, Figure 2 directly compares how β and σ_{int} vary with outer radius when M14 is (blue) and is not (red) incorporated. Across each aperture, we see clear trends such that the incorporation of M14 increases β by $\approx 0.10-0.15$ matching prior results (Golden-Marx & Miller 2018, 2019; Golden-Marx et al. 2022). Moreover, β reaches an asymptote at a radii of 150 kpc, in strong

We express the entire posterior as:



Figure 1. The data used to measure the SMHM relation including the BCG's core. In each sub-figure, we plot the BCG stellar mass against the halo mass. The outer radius used to measure the stellar mass is measured to progressively larger radii from 30 kpc to 300 kpc. The solid lines are representative of the median values of three M14 bins, each containing one-third of the data. In the last sub-figure, we overlay the SMHM relation posterior distribution for a value of M14 = 0.5 and M14 = 2.5. Moreover, in each sub-figure, the colour is the M14 value of the data shown. As we include light from larger radii, we see that the M14-stellar mass stratification becomes noisier, though continues to persist.

Table 1. Bayesian Analysis Parameters for the DES Sample

Symbol	Description	Prior
α	The offset of the SMHM relation	U(-20,20)
β	The high-mass power law slope	Linear Regression Prior
γ	The stretch parameter which describes the stellar mass - M14 stratification	Linear Regression Prior
$\sigma_{ m int}$	The uncertainty in the intrinsic stellar mass at fixed M_{200m}	$\mathcal{U}(0.0, 0.5)$
Уi	The underlying distribution in stellar mass	Deterministic (inferred from Equation 4)
x_i	The underlying M_{200m} distribution	$N(14.11, 0.21^2)$
Zi	The underlying M14 distribution	$N(1.74, 0.66^2)$
$\sigma_{y_{0i}}$	The uncertainty between the observed stellar mass and intrinsic stellar mass distribution	0.06 dex
$\sigma_{x_{0i}}$	The uncertainty associated with $\log_{10}(M_{200m})$	0.087 dex
$\sigma_{z_{0i}}$	The uncertainty between the underlying and observed M14 distribution	0.31 dex

Table 2. Sample Selection

Criteria	Number of Clusters
$\lambda > 20$ redMaPPer sample	21092
0.2 < z < 0.6	15654
No nearby bright foreground objects	7042
$4 P_{\text{mem}} > 0.9 \text{ members}$	6903
ICL unimpacated by masking of nearby galaxies	2929
Can measure ICL profile out to 300 kpc	2788

agreement with the trends found in Golden-Marx & Miller (2019) and Golden-Marx et al. (2023). Additionally, the inclusion of the ICL increases β by 0.1-0.15 as found in Golden-Marx et al. (2023) (a similar increase to what is found by including M14). As in Golden-Marx & Miller (2019), the value β asymptotes at is significantly higher when M14 is accounted for, by approximately 0.1.

The change of σ_{int} is more nuanced. When M14 is incorporated we find that σ_{int} decreases, in agreement with the trends for the BCG (Golden-Marx & Miller 2018, 2019; Golden-Marx et al. 2022). Interestingly, the decrease in σ_{int} that results from the inclusion of M14, is reduced from 0.04 dex to 0.02 dex as we extend our measurement to larger radii, which may reflect that M14 is more strongly correlated with the light in the inner portion of the total BCG+ICL profile, as investigated in Section 5.2.

Additionally, although Figure 2 does not present the γ measurements, the values given in Table 3 are all greater than 13σ from 0. Thus, the M14-stellar mass correlation persists out to 300 kpc. However, γ decreases as we progress to larger radii, which can be seen by the separation between the solid lines shown in Figure 1.

The presence of a non-zero γ along with the reduction in σ_{int} and increase in β allow us to conclude that M14 is a latent parameter when the SMHM relation is measured out to the ICL. For further verification, we randomly reassign the M14 values. If a non-zero value is measured for γ , this would suggest an intrinsic, non-physical, correlation between these parameters. However, as shown in Table A3, for each bin, the shuffled γ value is equivalent to 0. Moreover, the values of α , β , and σ_{int} are in excellent agreement between the versions with the randomly assigned M14 (Table A3) and when M14 is not incorporated (Table 3). Thus, any change in parameter measurements results solely from a correlation between the BCG+ICL stellar mass and M14. Going forward, we include M14 in all measurements discussed in this analysis (though we provide the posteriors when M14 is not accounted for in Tables 3, A1, and A2).

5.2 Comparing the SMHM relation of the BCG to the SMHM relation of outskirts

Although the correlation between the stellar mass and the halo mass increases as the BCG+ICL light profile is extended outward, as discussed in Golden-Marx et al. (2023) and Huang et al. (2022), the strongest correlation between stellar mass and halo mass has been measured when the core of the BCG is excluded. Here, we investigate the inclusion of M14 and use 5 non-overlapping radial apertures, 0-30 kpc, 30 kpc-80 kpc (representative of the ICL transition region (Zhang et al. 2024)), 80 kpc-150 kpc, 150 kpc-225 kpc, 225 kpc-300 kpc. We note that the data set used in this part of the analysis is a slightly different sample as what was used in Section 5.1 because we require that the aperture have a non-zero stellar mass in each of the 5 apertures, so there are some where we can measure a non-zero total light profile (starting from the core), but not an individual aperture mass (i.e., there are some clusters where the data may not be deep enough to allow for measurements of the large outer apertures).

In Figure 3, we plot the the data used to measure the SMHM relation, the stellar mass vs. the halo mass coloured using M14. Although the stellar mass range contained within each aperture varies, we fix the y-axis, to highlight the changing value. In each subplot, we overlay the median values of stellar mass and halo mass for the three previously defined M14 bins. The stellar mass-M14 correlation persists strongly in both the 0-30 kpc and 30 kpc-80 kpc apertures. Beyond this aperture, both the overall distribution and any trend with M14 becomes dominated by the noise, as demonstrated by the solid lines which begin to overlap.

We visually compare how using the core of the BCG impacts the β , γ , and σ_{int} parameters in Figure 4. For β , we measure the steepest slope in the radial range 30-80 kpc. This slope that is almost 0.07 (15%) steeper than any version measured when the light from the core of the BCG is used, which supports that the light contained within the ICL is strongly correlated with the cluster's halo mass. Moreover, this is similar to the result found in Golden-Marx et al. (2023) that the slope is peaked in the radial aperture of 30 kpc-50 kpc and also agrees with results presented in Huang et al. (2022) that find the strongest correlation with halo mass using the radial range of 50 kpc - 100 kpc. Additionally, we note that the light from the outskirts (beyond 150 kpc) is almost as strongly correlated with the dark matter halo mass as the BCG's core, though with a significantly larger scatter.

The trend measured for σ_{int} is nearly identical to what is found in Golden-Marx et al. (2023), where σ_{int} is significantly lower when the light from the core of the BCG is included. Since BCG cores can be treated as a standard candle (e.g., Lauer et al. 2007), this is

Table 3. Posterior Distribution Results

Data	Inner Radius	Outer Radius	α	β	γ	$\sigma_{ m int}$
Core	0	30	0.170 ± 0.008	0.249 ± 0.018	_	0.136 ± 0.002
Core	0	80	0.325 ± 0.009	0.321 ± 0.020	-	0.147 ± 0.002
Core	0	150	0.422 ± 0.009	0.357 ± 0.020	-	0.155 ± 0.002
Core	0	225	0.499 ± 0.011	0.391 ± 0.024	_	0.180 ± 0.003
Core	0	300	0.561 ± 0.012	0.405 ± 0.027	-	0.208 ± 0.003
Core	0	30	-0.001 ± 0.008	0.398 ± 0.016	0.152 ± 0.004	0.092 ± 0.002
Core	0	80	0.153 ± 0.008	0.464 ± 0.017	0.153 ± 0.004	0.103 ± 0.002
Core	0	150	0.274 ± 0.010	0.488 ± 0.019	0.134 ± 0.004	0.123 ± 0.002
Core	0	225	0.375 ± 0.011	0.500 ± 0.021	0.112 ± 0.005	0.162 ± 0.003
Core	0	300	0.456 ± 0.014	0.495 ± 0.027	0.094 ± 0.007	0.197 ± 0.003
No Core	0	30	0.177 ± 0.009	0.262 ± 0.020	_	0.136 ± 0.003
No Core	30	80	-0.207 ± 0.013	0.431 ± 0.031	_	0.211 ± 0.004
No Core	80	150	-0.262 ± 0.014	0.351 ± 0.032	_	0.221 ± 0.004
No Core	150	225	-0.250 ± 0.016	0.281 ± 0.037	_	0.262 ± 0.004
No Core	225	300	-0.274 ± 0.020	0.252 ± 0.047	-	0.334 ± 0.006
No Core	0	30	0.006 ± 0.008	0.408 ± 0.017	0.154 ± 0.004	0.087 ± 0.003
No Core	30	80	-0.364 ± 0.015	0.565 ± 0.029	0.142 ± 0.007	0.187 ± 0.004
No Core	80	150	-0.314 ± 0.017	0.389 ± 0.033	0.044 ± 0.009	0.219 ± 0.004
No Core	150	225	-0.273 ± 0.020	0.306 ± 0.038	0.023 ± 0.010	0.262 ± 0.004
No Core	225	300	-0.281 ± 0.023	0.229 ± 0.045	0.021 ± 0.011	0.300 ± 0.005

unsurprising. However, we remind the reader that our estimate for σ_{int} is an upper limit because we assume the same uncertainty on the stellar mass for each of the radial bins, calibrated for the BCG 0-30 kpc region. If we are underestimating the uncertainty in the stellar mass of the ICL, then we we would be overestimating σ_{int} .

Lastly, the most interesting and surprising result comes from γ , which is statistically more than 5 σ from 0 for the 0-30 kpc, 30 kpc-80 kpc, and 80 kpc-150 kpc apertures. This means that the stellar mass-M14 correlation persists out to 150 kpc, though its strength decreases drastically beyond 80 kpc. Moreover, the value of γ is statistically equivalent in the BCG's core and the BCG+ICL transition region (30 kpc-80 kpc). Since M14 is independent of the light from this radial regime, this may offer further support that the light in the transition region is also growing as a result of BCG hierarchical assembly. Additionally, we note that at large radii (r > 150 kpc), we detect no correlation between stellar mass and M14, which may lead to the decrease in γ measured when the BCG's core is included and shows that for that dataset , the correlation between M14 and stellar mass is coming from the inner region (between 0-80 kpc or 0-150 kpc) of the BCG+ICL system.

6 PHYSICAL MEANING OF THE CORRELATION BETWEEN THE MAGNITUDE GAP AND THE ICL

6.1 The SMHM Relation

Figures 1 and 3 illustrate the connection between M14 and the ICL as inferred from the SMHM relation. Table 3 and Figure 4 quantify that the ICL and M14 correlate, such that for certain radial bins, the inclusion of M14 yields a tighter SMHM relation. However, as shown in Figure 4, the strength of this correlation weakens as we extend the ICL out to larger apertures and stops being statistically significant at radii beyond 150 kpc.

Figure 4 and Table 3 also highlight that the strength of the correlation between the BCG+ICL light/stellar mass and M14 is within 1*σ* for the 0-30 kpc, 0-80 kpc, and 30 kpc - 80 kpc apertures. Moreover, both when the core is and is not included, *γ* declines at radii beyond 80 kpc. While the *γ* parameters are similar, the radial range that features the strongest correlation between the stellar mass and the underlying halo mass is the BCG+ICL transition region (30 kpc - 80 kpc). Although this aperture does not have the lowest *σ*_{int}, the value (*σ*_{int} = 0.187) is in agreement with the values assumed when M14 is not incorporated (~ 0.15). Therefore, from a statistical standpoint, there is a trade-off between the lower *σ*_{int} when the core is included and the higher *β* when it is not. Additionally, we note that the inclusion of M14 decreases *σ*_{int} by 0.034 dex and increases *β* by 0.13, in the transition region, which is the largest change in both parameters for one of the unique apertures when incorporating M14 into the SMHM relation.

We remind the reader that the stellar mass measured between 30 kpc-80 kpc and M14 are independent. Thus, this strong γ parameter informs the BCG+ICL system's formation. Following the results of Golden-Marx & Miller (2018), M14 can be thought of as a tracer for hierarchical growth, such that clusters with larger M14 values are more evolved and possibly older systems. Thus, the presence of such a strong M14 stratification in the BCG+ICL transition region suggests that the hierarchical growth of the BCG is not confined to the core, but rather extends to the BCG+ICL transition regime. Moreover, it is plausible that a greater fraction of the stellar mass growth from this hierarchical merging is deposited within the transition region, which may lead to the strong correlation. Assuming this scenario, the BCG+ICL transition region then grows predominately through the major/minor mergers of the BCG, while the ICL may grow through tidal stripping of satellite galaxies (as shown by the detected colour gradient (e.g., Montes & Trujillo 2018; DeMaio et al. 2018; Contini et al. 2019; Golden-Marx et al. 2023)). Moreover, because we use radial apertures to separate the ICL and BCG, it is possible that due to projection effects, the correlation with the ICL is even stronger as some fraction of the ICL is contained inside 30 kpc.

Although redshift evolution is beyond the scope of this analysis, we present an alternative formation scenario. Golden-Marx et al.



Figure 2. We compare the inferred parameter values from the posterior distributions for β and σ_{int} when M14 is (blue) and is not (red) incorporated. The dashed horizontal lines represent the radial range over which the measurement is made, while the solid vertical lines represent the 1 σ uncertainty in our measurement. M14 is a latent parameter out to large radii in the SMHM relation because β increases and σ_{int} decreases.

(2022) find the stellar mass contained within the core of the BCG is constant over this redshift range. Thus, Golden-Marx et al. (2022) posit that the growth must be occurring at larger radial apertures, possibly within the ICL. However, this growth was not detected in Golden-Marx et al. (2023), though that analysis focused on the 50 kpc - 300 kpc aperture (and did not account for M14), which may have washed out any evolution signal due to the increase in noise. Thus, the correlation with M14 may suggest recent growth is not occurring in the far outskirts of the ICL, but rather in the BCG+ICL transition region, as Zhang et al. (2024) find preliminary evidence for.

6.2 The ICL Fraction vs. Magnitude Gap

Along with the correlation between the ICL and M14 highlighted via the SMHM relation, we measure the ICL fraction as a function of M14 since both parameters have been posited to correlate with the dynamical state of the cluster. We measure three unique ICL fractions defined by the following equations.

ICL Fraction<sub>30 =
$$\frac{\text{Lum}_{\text{ICL}}(30 < r < 150)}{\text{Lum}_{\text{ICL}+\text{Sat}}(30 < r < 150)}$$
(7)</sub>

Equation 7 is the ratio of the ICL light to the total light within the cluster (ICL + satellite galaxies, excluding the BCG) measured between 30 kpc and 150 kpc.

$$BCG + ICL Fraction_{0 < r < 150} = \frac{Lum_{BCG+ICL}(0 < r < 150)}{Lum_{BCG+ICL+Sat}(0 < r < 150)}$$
(8)

Equation 8 compares the BCG+ICL light to the total light of the cluster measured within 150 kpc.

ICL Fraction<sub>0 =
$$\frac{\text{Lum}_{\text{ICL}}(30 < r < 150)}{\text{Lum}_{\text{BCG+ICL+Sat}}(0 < r < 150)}$$
 (9)</sub>

Equation 9 compares the ICL light to the total light in the cluster within 150 kpc.

For this portion of the analysis, we stack the measurements of the ICL in 5 M14 bins (20% quintiles), and then measure the mean ICL fraction and M14 in each bin. For this analysis, we do not further bin the data by halo mass as Zhang et al. (2024), using the same ICL measurements, detect no correlation between ICL fraction and richness. Moreover, we note that there is no correlation between M14 and halo mass in our measurements.

As shown in Figure 5, we for the first time using observations find that clusters characterized by a large M14 have significantly larger ICL fractions. Each ICL fraction increases by between 50-75% when comparing low M14 (M14 < 1.0) and high M14 (M14 > 2.0) clusters. As a result of hierarchical merging, we expect a fraction of stars will be ejected into the ICL while another fraction will increase the BCG stellar mass. Thus, the M14 and ICL fraction correlation directly results from BCG hierarchical assembly. Therefore, it follows the increase in the fraction as a function of M14 is much larger when the BCG's light is included (comparing the middle and lower panels), as the BCG's stellar mass increases due to hierarchical assembly. Moreover, following the interpretation of M14 from Golden-Marx & Miller (2018) and M12 from Vitorelli et al. (2018) - clusters with larger M14 values form earlier and have had more time to evolve - we posit that this may mean that clusters characterized by larger ICL fractions are dynamically older and that as clusters evolve, the BCG+ICL system (and as a result M14 and ICL fraction) grows. Additionally, though not shown, similar to Zhang et al. (2024), we find that the ICL fraction is dependent on aperture and decreases as the ICL is extended out to 300 kpc

Previous work by Jiménez-Teja et al. (2018), Dupke et al. (2022), and Jiménez-Teja et al. (2024) have found that the ICL fraction has an inverse correlation with the dynamical state of the cluster, such that relaxed clusters are characterized by low ICL fractions, while merging clusters are characterized by larger ICL fractions. Moreover, studying fossil group galaxies, Zarattini et al. (2015) suggest that systems characterized by larger M12 values are dynamically relaxed. Additionally, in cosmological hydrodynamic simulations Yoo et al. (2024) find that clusters with larger M12 values are more relaxed. Furthermore, Yoo et al. (2024) also find a strong correlation between M12 and BCG+ICL fraction, similar to what is shown in the middle panel of Figure 5. Although we use M14, as shown in Golden-Marx & Miller (2018), there is no statistical difference between these



Figure 3. The data used to measure the SMHM relation within unique non-overlapping apertures. In each sub-figure, we plot the stellar mass against the halo mass. The inner and outer radius used to measure the stellar mass progressively increases from 0-30 kpc to 225 kpc - 300 kpc. As we look at light from the ICL, we no longer see a correlation between M14 and stellar mass at fixed halo mass. The solid lines represent the median values of three M14 bins containing one-third of the data each. In the last subfigure, we overlay the posterior distribution for a value of M14 = 0.5 and M14=2.5 in the 30 kpc < R < 80 kpc aperture.





Figure 4. We compare the inferred median values derived from the posterior distribution for β , γ , and σ_{int} when the core of the BCG is (blue) and is not (orange) incorporated. The dashed horizontal lines show the radial range where which measurement is made, while the solid vertical lines are the 1σ measurement uncertainty. We see that the strongest correlations (in terms of β , γ , and σ_{int}) occur in the radial range 30-80 kpc, which is shaded in light red, and that the correlation with M14 becomes weaker when looking at only light beyond 150 kpc.

Figure 5. Using stacked measurements of the ICL in 5 M14 bins (20% quintiles), we compare the ICL fraction to M14. The upper panel is a measure of the ICL fraction in the radial range 30 kpc < R < 150 kpc given by Equation 7. The middle panel represents the BCG+ICL fraction measured within 150 kpc given by Equation 8. The lower panel represence the ICL fraction measured within 150 kpc given by Equation 9. The errorbars are representative of a boostrap uncertainty from 100,000 draws.

parameters due to the measurement uncertainty. Thus, the results shown in Figure 5 are in excellent agreement with the simulations from Yoo et al. (2024). Lastly, recent observational work by Casas et al. (2024) also find that applying a high M14 criteria (M14 > 1.25) better identifies dynamically relaxed clusters.

This literature comparison is not a perfect. Jiménez-Teja et al. (2018), Dupke et al. (2022), and Jiménez-Teja et al. (2024) use Xray measurements, measure the ICL using CICLE (e.g., Jiménez-Teja et al. 2018), and do not estimate the ICL fraction within a fixed aperture, Zarattini et al. (2015) focus on lower halo mass fossil galaxies, Yoo et al. (2024) use simulations the majority of which are galaxy groups, and Casas et al. (2024) also analyze an X-ray sample and do not consider the ICL. However, the excellent agreement with the simulations from Yoo et al. (2024) suggests that both ICL fraction and M14 may correlate with dynamical state such that larger M14 values and higher ICL fractions are typical of dynamically relaxed systems. However, given this contradiction to results from Jiménez-Teja et al. (2018), Dupke et al. (2022), and Jiménez-Teja et al. (2024) we posit two alternatives. First, X-ray relaxation measurements are made on large cluster scale observations. However, M14 depends only on the cluster's central region. Therefore, it is possible that while M14 traces the hierarchical assembly of the BCG, it is unrelated to the cluster's overall dynamical state because it is characteristic of just the mergers within the core. Second, Zhang et al. (2024) find that the ICL fraction is dependent on the choice of radial aperture, and thus it is possible that the measurements from Jiménez-Teja et al. (2018), Dupke et al. (2022), and Jiménez-Teja et al. (2024) are not directly comparable to our own. However, further investigation, using simulations and consistent ICL measurement methods and definitions are required to gain greater insight into this apparent discrepancy.

7 CONCLUSION

In this work, our analysis focuses on characterizing how the ICL and M14 are related using the SMHM relation as both measurements are related to BCG hierarchical assembly. We use DES Year 6 data to characterize the SMHM relation over the redshift range 0.2 < z < 0.6. Throughout the analysis we treat the BCG and ICL as a linked system using radial cuts to define certain regions. We summarize the primary results of this analysis as follows.

• When the BCG+ICL stellar mass is measured from the core out to progressively larger apertures, γ , the correlation between stellar mass and M14 at fixed halo mass is non-zero out to large radii. Using our Bayesian infrastructure, we find that the inclusion of M14 increases β by 0.1-0.15 and decreases σ_{int} by 0.01-0.04 dex (depending on the choice of aperture). Thus, M14 is a latent variable in the SMHM relation. However, the impact of M14 decreases at larger radii.

• When measuring the SMHM relation in unique, nonoverlapping apertures, we find that the strongest correlation between stellar mass and halo mass is in the 30 kpc - 80 kpc bin. This result follows from the "two-phase" formation of BCGs and agrees with results from Huang et al. (2022) and Golden-Marx et al. (2023). Moreover, β increases by 30% with the inclusion of M14.

• When using unique apertures, the stellar mass - M14 correlation is statistically significant in the 0-30 kpc, 30 kpc - 80 kpc, and 80 kpc - 150 kpc apertures. γ decreases significantly beyond 80 kpc. Most importantly, γ is equivalent in the 0-30 kpc, 0-80 kpc, and 30 kpc -80 kpc apertures. Since M14 contains no information about the light in the 30 kpc - 80 kpc aperture, this correlation highlights that the stellar mass in this region likely grows as a result of BCG hierarchical assembly. Thus, it is plausible that the BCG+ICL transition region grows as a result of mergers, while the outer ICL grows through processes such as tidal stripping.

• We for the first time observationally measure a strong correlation between the mean ICL fraction and M14 value such that clusters characterized by a larger M14 (M14 > 2.0) have ICL fractions that are more than 50% higher than clusters with a small M14 (M14 < 1.0). As M14 grows as a result of mergers, this correlation follows from BCG hierarchical assembly.

Going forward, there remain many research questions we aim to explore to improve our observational understanding and characterisation of the BCG+ICL. In particular, understanding how the BCG+ICL stellar mass and radial distribution evolves with redshift. In future analysis using the Euclid Mission (as demonstrated by Kluge et al. (2024)) and the Rubin Observatory's LSST, we plan to extend this type of analysis out to higher redshifts $(z \approx 1.5)$) to investigate the formation and evolution of the BCG+ICL system and how its correlation with halo mass evolves. Moreover, given the correlation between M14 and ICL fraction, we suggest that characterizing large M14 systems in Euclid and LSST, or targetting them with JWST, may provide information about the earliest appearances of the ICL. Additionally, we aim to determine whether the correlation between M14 and BCG stellar mass persists out to high redshift and whether this is intrinsic (i.e., is it in place prior to ex-situ growth) or results entirely from hierarchical formation.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

APPENDIX A: VERIFICATION TESTS

In Tables A1 and A2, we present the posterior distributions when we divide our sample into two subsets based on the redMaPPer central galaxy probability (P_{Cen}). We use two samples with $P_{Cen} < 0.60$ (Table A1) and $P_{Cen} > 0.99$ (Table A2). When comparing these posterior distributions to those presented in Table 3, we see that all measurements are consistent within 1 σ . This provides additional evidence that our results are not biased by miscentring or incorrect BCG identification, as BCGs with low P_{Cen} are more likely to be miscentred or misidentified as the BCG.

In Table A3, we present the posterior distributions when M14 is randomly assigned, removing any existing correlation between M14 and aperture stellar mass. For each version, we find that γ is equivalent to 0 and that the measured posteriors are in excellent agreement with the values provided in Table 3 when M14 is not accounted for. The discrepancy between the shuffled results (Table A3) and those of the real data (Table 3) along with the nested nature of our MCMC model further highlight that M14 is indeed a latent parameter, the correlation between aperture stellar mass and M14 is real, and including M14 yields a better fit to the underlying observational data.

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Table A1. Posterior Distribution Results PCen < 60°	%
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Data	Inner Radius	Outer Radius	α	β	γ	$\sigma_{ m int}$
Core	0	30	0.178 ± 0.024	0.260 ± 0.053	_	0.136 ± 0.006
Core	0	80	0.323 ± 0.026	0.308 ± 0.057	-	0.143 ± 0.007
Core	0	150	0.434 ± 0.027	0.360 ± 0.059	-	0.150 ± 0.007
Core	0	225	0.527 ± 0.031	0.425 ± 0.069	-	0.177 ± 0.008
Core	0	300	0.596 ± 0.036	0.449 ± 0.079	-	0.204 ± 0.009
Core	0	30	0.023 ± 0.023	0.426 ± 0.046	0.146 ± 0.011	0.095 ± 0.006
Core	0	80	0.181 ± 0.026	0.460 ± 0.052	0.133 ± 0.013	0.111 ± 0.007
Core	0	150	0.312 ± 0.029	0.489 ± 0.056	0.112 ± 0.014	0.129 ± 0.007
Core	0	225	0.421 ± 0.035	0.511 ± 0.069	0.091 ± 0.017	0.166 ± 0.008
Core	0	300	0.533 ± 0.043	0.511 ± 0.083	0.057 ± 0.021	0.201 ± 0.009
No Core	0	30	0.180 ± 0.027	0.264 ± 0.061	-	0.137 ± 0.007
No Core	30	80	-0.208 ± 0.037	0.406 ± 0.084	-	0.206 ± 0.010
No Core	80	150	-0.224 ± 0.043	0.419 ± 0.097	-	0.231 ± 0.011
No Core	150	225	-0.175 ± 0.049	0.455 ± 0.111	-	0.273 ± 0.013
No Core	225	300	-0.190 ± 0.063	0.440 ± 0.143	-	0.352 ± 0.016
No Core	0	30	0.021 ± 0.027	0.412 ± 0.052	0.146 ± 0.013	0.096 ± 0.007
No Core	30	80	-0.319 ± 0.045	0.506 ± 0.087	0.101 ± 0.022	0.195 ± 0.010
No Core	80	150	-0.261 ± 0.052	0.435 ± 0.099	0.029 ± 0.026	0.230 ± 0.011
No Core	150	225	-0.179 ± 0.060	0.465 ± 0.116	0.005 ± 0.030	0.272 ± 0.013
No Core	225	300	-0.204 ± 0.069	0.336 ± 0.132	0.005 ± 0.035	0.316 ± 0.015

Table A2. Posterior Distribution Results PCen > 99%

Data	Inner Radius	Outer Radius	α	β	γ	$\sigma_{ m int}$
Core	0	30	0.183 ± 0.014	0.285 ± 0.032	_	0.133 ± 0.004
Core	0	80	0.333 ± 0.015	0.349 ± 0.035	_	0.146 ± 0.004
Core	0	150	0.424 ± 0.016	0.375 ± 0.036	-	0.155 ± 0.005
Core	0	225	0.503 ± 0.018	0.412 ± 0.041	-	0.176 ± 0.005
Core	0	300	0.577 ± 0.020	0.450 ± 0.046	-	0.199 ± 0.006
Core	0	30	-0.015 ± 0.014	0.396 ± 0.027	0.157 ± 0.007	0.091 ± 0.004
Core	0	80	0.141 ± 0.016	0.472 ± 0.029	0.159 ± 0.008	0.099 ± 0.005
Core	0	150	0.259 ± 0.017	0.487 ± 0.032	0.139 ± 0.009	0.120 ± 0.005
Core	0	225	0.362 ± 0.021	0.504 ± 0.039	0.117 ± 0.010	0.156 ± 0.005
Core	0	300	0.462 ± 0.024	0.526 ± 0.045	0.094 ± 0.012	0.188 ± 0.006
No Core	0	30	0.189 ± 0.015	0.283 ± 0.036	_	0.134 ± 0.005
No Core	30	80	-0.201 ± 0.023	0.463 ± 0.055	-	0.213 ± 0.007
No Core	80	150	-0.259 ± 0.023	0.398 ± 0.055	-	0.214 ± 0.007
No Core	150	225	-0.257 ± 0.027	0.319 ± 0.066	-	0.256 ± 0.008
No Core	225	300	-0.276 ± 0.034	0.295 ± 0.083	-	0.329 ± 0.010
No Core	0	30	0.005 ± 0.016	0.387 ± 0.029	0.149 ± 0.008	0.090 ± 0.005
No Core	30	80	-0.388 ± 0.027	0.578 ± 0.051	0.153 ± 0.014	0.186 ± 0.007
No Core	80	150	-0.316 ± 0.030	0.425 ± 0.056	0.045 ± 0.016	0.212 ± 0.007
No Core	150	225	-0.259 ± 0.035	0.318 ± 0.066	0.001 ± 0.018	0.255 ± 0.008
No Core	225	300	-0.247 ± 0.039	0.270 ± 0.075	0.001 ± 0.021	0.285 ± 0.009

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Table A3. Posterior Distribution Results Shuffled

Data	Inner Radius	Outer Radius	α	β	γ	$\sigma_{ m int}$
Core	0	30	0.167 ± 0.011	0.257 ± 0.018	0.002 ± 0.004	0.139 ± 0.002
Core	0	80	0.321 ± 0.012	0.318 ± 0.020	0.002 ± 0.005	0.147 ± 0.002
Core	0	150	0.427 ± 0.012	0.358 ± 0.021	-0.002 ± 0.005	0.155 ± 0.002
Core	0	225	0.503 ± 0.014	0.393 ± 0.024	-0.002 ± 0.006	0.180 ± 0.003
Core	0	300	0.561 ± 0.017	0.398 ± 0.028	-0.001 ± 0.007	0.210 ± 0.003
No Core	0	30	0.175 ± 0.013	0.263 ± 0.021	0.001 ± 0.005	0.136 ± 0.003
No Core	30	80	-0.210 ± 0.019	0.424 ± 0.031	0.000 ± 0.008	0.212 ± 0.004
No Core	80	150	-0.255 ± 0.019	0.351 ± 0.032	-0.004 ± 0.008	0.221 ± 0.004
No Core	150	225	-0.238 ± 0.023	0.275 ± 0.038	-0.009 ± 0.009	0.263 ± 0.005
No Core	225	300	-0.249 ± 0.027	0.208 ± 0.043	-0.005 ± 0.011	0.300 ± 0.005

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