Dark Energy Survey Year 3 Results: Cosmology from galaxy clustering and galaxy-galaxy lensing in harmonic space

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ABSTRACT

We present the joint tomographic analysis of galaxy-galaxy lensing and galaxy clustering in harmonic space, using galaxy catalogues from the first three years of observations by the Dark Energy Survey (DES Y3). We utilise the REDMAGIC and MAGLIM catalogues as lens galaxies and the METACALIBRATION catalogue as source galaxies. The measurements of angular power spectra are performed using the pseudo- C_ℓ method, and our theoretical modelling follows the fiducial analyses performed by DES Y3 in configuration space, accounting for galaxy bias, intrinsic alignments, magnification bias, shear magnification bias and photometric redshift uncertainties. We explore different approaches for scale cuts based on non-linear galaxy bias and baryonic effects contamination. Our fiducial covariance matrix is computed analytically, accounting for mask geometry in the Gaussian term, and including non-Gaussian contributions and super-sample covariance terms. To validate our harmonic space pipelines and covariance matrix, we used a suite of 1800 log-normal simulations. We also perform a series of stress tests to gauge the robustness of our harmonic space analysis. In the ACDM model, the clustering amplitude $S_8 = \sigma_8 (\Omega_m/0.3)^{0.5}$ is constrained to $S_8 = 0.704 \pm 0.029$ and $S_8 = 0.753 \pm 0.024$ (68% C.L.) for the REDMAGIC and MAGLIM catalogues, respectively. For the wCDM, the dark energy equation of state is constrained to $w = -1.28 \pm 0.29$ and $w = -1.26^{+0.34}_{-0.27}$, for REDMAGIC and MAGLIM catalogues, respectively. These results are compatible with the corresponding DES Y3 results in configuration space and pave the way for harmonic space analyses using the DES Y6 data.

Key words: (cosmology:) cosmological parameters – (cosmology:) large-scale structure of Universe – gravitational lensing: weak

1 INTRODUCTION

The accelerating expansion of the Universe, first discovered through the analysis of supernova light curves (Perlmutter et al. 1997, 1999; Riess et al. 1998), has received significant further evidence from a variety of complementary observations. These include measurements of properties of the cosmic microwave background (CMB) (Hinshaw et al. 2013; Planck Collaboration 2020; Qu et al. 2024) and the large scale structure (LSS) of the universe (see Weinberg et al. 2013 for a recent review). Analysis from these different observations have statistically converged during the recent decades upon a concordance cosmological model, the ACDM model. This model describes a spatially flat Universe composed of roughly 30% of visible and cold dark matter (CDM), and 70% dark energy. This dark energy is responsible for the accelerated expansion and is consistent with a cosmological constant (Λ), but its physical nature remains as an open problem.

Recent progress has been significant in enhancing the data quality and quantity, along with improved techniques, for extracting cosmological information from various LSS probes of cosmic acceleration. Notably, the distribution of matter traced by galaxy positions (galaxy clustering) and the weak gravitational lensing distortion it induces on the shapes of distant galaxies (cosmic shear) have proven to be powerful tools for constraining cosmological models (DES Collaboration 2018, 2022; Asgari et al. 2021; Alam et al. 2021; Dalal et al. 2023; Li et al. 2023). These techniques are considered to be amongst the key scientific drivers of current Stage-III observational programmes and will continue to be for the next generation of experiments (Ivezić et al. 2019; Laureijs et al. 2011). The Dark Energy Survey [DES¹ The Dark Energy Survey Collaboration (2005)] is the largest stage-III imaging survey today, covering almost 5000 deg² of the southern sky. One of the key cosmological results obtained from the large scale structure and weak lensing data from the first three years of observations (DES Y3) consisted of the analysis of three two-point angular correlation functions (3×2pt) arising from the clustering and gravitational shear of galaxies (DES Collaboration 2022). The final analyses using the full 6 years of data (DES Y6) are well under way.

In addition to these main results obtained from the configuration/real space angular correlation functions, complementary analyses using their Fourier/Harmonic counterpart, the two-point angular power spectra, were also conducted within DES. The angular power spectra of the data collected in the first year (DES Y1) were studied for galaxy clustering (Andrade-Oliveira et al. 2021) and cosmic shear (Camacho et al. 2022) whereas Doux et al. (2022) obtained cosmological constraints from the analysis of cosmic shear in harmonic space for DES Y3. These results add up to the ongoing generation of observations from Stage-III dark energy experiments, having as a main scientific goal a better understanding of the nature of cosmic acceleration. In the context of combined multiprobe analysis from weak gravitational lensing and galaxy clustering, the Kilo-Degree Survey (KiDS²) has released results combining its cosmic shear observations with galaxy clustering from the overlapping Baryon Oscillation Spectroscopic Survey (BOSS³) and the 2-degree Field Lensing Survey (2dFLenS⁴) in configuration space (Joachimi et al. 2021; Heymans et al. 2021). Analogously, the Hy-

³ https://www.sdss.org/surveys/boss/ ⁴ https://2dflens.swin.edu.au/

per Suprime-Cam (HSC⁵) has also cross-correlated its weak lensing signal measurements with clustering from BOSS (More et al. 2023), but based in configuration space. In a complementary way, the cosmic shear angular power spectrum was also recently measured from the three-year galaxy shear catalogue from the HSC imaging survey (Dalal et al. 2023; Li et al. 2023). A reanalysis of HSC data only, which combines the galaxy clustering and weak lensing signals in harmonic space, is currently in development (Sanchez-Cid et al. prep).

In this paper we present, for the first time within the DES, results from a combination of two angular power spectra in harmonic space, namely the two-point correlation of galaxy positions, $\langle \delta_g \delta_g \rangle$, and the cross-correlation of galaxy positions and shapes, $\langle \delta_{g} \gamma \rangle$, which we refer to as 2×2 pt. The proposed methodology is tested for internal consistency and robustness and the results are compared to the ones obtained from the configuration space analyses on the same dataset (Pandey et al. 2022; Porredon et al. 2022). For the MAGLIM sample, we present results that utilise the first four tomographic bins (employed in the fiducial results of Porredon et al. 2022), and with all six tomographic bins, and discuss the consistency of the results across these different redshift ranges. This work represents an important milestone probing the robustness of the different analyses of DES data, being a completely independent data reduction to a different set of summary statistics. The presented methodology has its own estimators, covariances and modelling, constraining the survey information in a unique way. This paves the way for a full 3×2pt analysis in harmonic space using the final DES Y6 data set, as well as for future analyses of next-generation cosmological surveys.

This paper is organised as follows. In Section 2 we review the data used, namely the two catalogues for the lens galaxies, RED-MAGIC (Pandey et al. 2022) and MAGLIM (Porredon et al. 2021), and the METACALIBRATION catalogue for the source galaxies (Gatti & Sheldon et al., 2021). In this section, we also describe the generation of log-normal simulations used to validate the estimated covariance matrix and assess the accuracy of our cosmological analysis pipeline. Section 3 describes the theoretical modelling of the angular power spectra, accounting for galaxy bias, intrinsic alignments, magnification bias, shear magnification bias and photometric redshift uncertainties. Scale cuts are devised to mitigate small-scale uncertainties and a likelihood analysis is presented and tested against simulated data vectors. Our results for ACDM and wCDM models are presented in Section 4 along with internal consistency and robustness tests, and our conclusions are summarised in Section 5.

2 DATA

The DES is a photometric galaxy survey that imaged about onefourth of the southern sky in five optical filters: g, r, i, z, and Y, collecting data from more than 500 million galaxies. Using the Dark Energy Camera (DECam) on the Blanco telescope at the Cerro Tololo Inter-American Observatory (CTIO) in Chile, DES completed its observations in January 2019 after 6 years of operations. In this paper, we utilise data from the initial three-year observation period (Y3), spanning August 2013 to February 2016.

¹ http://www.darkenergysurvey.org/

² http://kids.strw.leidenuniv.nl/

⁵ https://www.naoj.org/Projects/HSC/

DES Y3 Harmonic Space 2×2*pt* 3

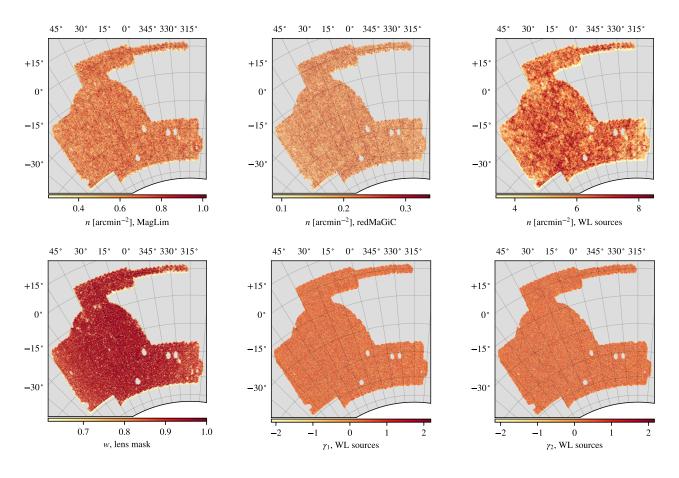


Figure 1. The maps of the different DES Y3 catalogues used in this work. Top: the number densities of the full REDMAGIC, MAGLIM and METACALIBRATION samples, without tomographic selection. Bottom left: The covered fraction of the sky common to all samples, used as the mask for the lens samples. Bottom middle and right: the two components of shear ellipticities in the METACALIBRATION sample.

2.1 DES Y3 catalogues

The DES Y3 photometric data set resulted in a catalogue encompassing nearly 390 million objects over an area of 4946 deg² of the sky, with a depth reaching a signal-to-noise ratio of approximately 10 for extended objects up to an AB system magnitude in the *i* band of approximately 23. Its detailed selection is referred to as the GoLD catalogue, and is described in detail in Sevilla-Noarbe et al. (2021). To mitigate the influence of astrophysical foregrounds and known data processing artefacts on subsequent cosmological analyses, additional masking was implemented. This process resulted in a final catalogue encompassing a reduced area of 4143 deg². This dataset was used to further select two distinct lens samples and one source sample of galaxies. The source sample serves as the background population for weak lensing analysis, while the lens samples are employed for both weak lensing, as foreground population, and galaxy clustering analyses.

The first lens sample used in the DES Y3 analyses was constructed using the REDMAGIC algorithm (outlined in Rozo et al. 2016). This algorithm is specifically designed to identify luminous red galaxies (LRGs) with minimal uncertainties in their photometric redshifts. It achieves this by leveraging the well-established magnitude-colour-redshift relationship exhibited by red-sequence galaxies. The resulting selection on the DES Y3 data, the so-called REDMAGIC sample, consists of 2.6 million galaxies, which are divided into five tomographic bins described in Table 1. The full

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REDMAGIC catalogue's angular density is depicted in the uppercentral panel of Figure 1. The redshift distribution of each bin is shown in Figure 2. For more details about the REDMAGIC algorithm, the REDMAGIC sample, and its comparison with other samples we refer the reader to Rozo & Rykoff et al., (2016) and Pandey et al. (2022), respectively.

The second, and fiducial, lens sample used for the DES Y3 analyses, the so-called MAGLIM sample, was optimised in Porredon et al. (2021) to maximise its constraining power for combined galaxy clustering and galaxy-galaxy lensing. MAGLIM is a magnitude-limited sample defined by a magnitude cut in the *i*-band that is linearly dependent on the photometric redshift, which allows including more galaxies at higher redshift. The photometric redshift estimation for the MAGLIM sample used the Directional Neighborhood Fitting (DNF) algorithm (De Vicente et al. 2016). In order to remove stellar contamination from binary stars and other bright objects, the MAGLIM selection applies a further lower magnitude cut of *i* > 17.5. The resultant sample, comprising 10.7 million galaxies, is divided into the six tomographic bins detailed in Table 1^6 and comprises a wider redshift distribution and 3.5 times more galaxies compared to the REDMAGIC sample, resulting in tighter

⁶ We note bin edges in Table 1 are slightly modified from Porredon et al. (2021) and shown in Figure 2 to improve the photometric redshift calibration (see Porredon et al. (2022) for further discussion).

cosmological parameter constraints (Porredon et al. 2022). The angular density of the full MAGLIM catalogue is shown on the top-left panel of Figure 1.

Statistically significant correlations were found between the galaxy number density of both the REDMAGIC and MAGLIM lens samples and various observational survey properties. Such correlation imprints a non-cosmological bias into the galaxy clustering signal for the lens samples. We account for those biases by applying weights to each galaxy corresponding to the inverse of the estimated angular selection function. The computation and validation of these weights, for both lens samples, is described in Rodríguez-Monroy et al. (2022).

Finally, we used as source sample the DES Y3 weak lensing shape catalogue (Gatti & Sheldon et al., 2021). The source shapes are measured using the METACALIBRATION method (Sheldon 2014; Sheldon & Huff 2017; Huff & Mandelbaum 2017). This method offers a self-calibrating approach to correct for biases in the galaxy shear estimation. This is achieved by applying an iterative process where a single elliptical Gaussian model is fitted to artificially sheared replicas of each galaxy. This procedure results in the construction of a shear response matrix, denoted as $R = R_{\gamma} + R_S$, which encapsulates two distinct components: R_{γ} representing the response of the shape estimator and R_S representing the response of object selection. The calibrated shear measurements are then obtained by multiplying the estimated galaxy ellipticities by the inverse of this matrix (Gatti & Sheldon et al., 2021).

For the DES Y3 shape catalogue, the METACALIBRATION method improves the accuracy of galaxy shape measurements over its DES Y1 counterpart (Zuntz et al. 2018) by incorporating per galaxy inverse variance weights based on signal-to-noise ratio and size (Gatti & Sheldon et al., 2021), better astrometric methods (Sevilla-Noarbe et al. 2021), and better point-spread function (PSF) estimation (Jarvis et al. 2021). On top of that, shear biases sourced by object blending, not taken into account by METACALIBRATION, were calibrated using image simulations in MacCrann et al. (2022). The resultant shape catalogue comprises 100.2 million galaxies covering the same area as the lens catalogues. This translates to an effective angular galaxy density of 5.59 arcmin⁻², as defined by Heymans et al. (2013). Furthermore, the catalogue exhibits an effective shape noise $\sigma_e = 0.261$ per ellipticity component. The catalogue is further subdivided into four tomographic bins, selecting in photometric redshift estimates that rely on the Self-Organizing Map Photometric Redshift (SOMPZ) method as described by Myles, Alarcon et al. (2021), each possessing a normalised redshift distribution as illustrated in Figure 2 and properties detailed in Table 2.

2.2 Log-normal realisations

In order to validate our covariance matrix and parameter inference pipeline, we rely on the simulation of a large ensemble of lognormal random fields. The log-normal distribution has been used in a broad range of applications for modelling cosmic fields (Coles & Jones 1991). Their efficacy has been demonstrated in approximating the 1-point probability density function (PDF) of weak lensing convergence/shear (Hilbert et al. 2011; Xavier et al. 2016) and the distribution of late-time matter density contrast fields (Friedrich et al. 2018; Gruen et al. 2018). In the context of DES, Clerkin et al. (2017) further validated the log-normal distribution assumption using Science Verification data for the convergence field. More recently, Friedrich et al. (2021) employed it to compute and validate covariance matrices for the full combination of weak lensing and

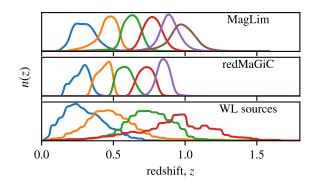


Figure 2. Normalised redshift distributions for the DES Y3 lens and source catalogues. Each panel corresponds to a sample and each curve corresponds to a tomographic bin selection.

Table 1. The DES Y3 lens samples specifications used in this work. This table shows the photometric redshift selection, total number of galaxies selected, $(N_{\rm gal})$, effective angular number density of galaxies in arcmin⁻², $(n_{\rm eff})$, and magnification bias, $(C_{\rm g})$, as measured in Elvin-Poole, MacCrann et al. (2023). The survey property systematic weights have been accounted for in the effective angular number density following Equation (5).

redshift bin	Ngal	<i>n</i> _{eff}	$C_{ m g}$				
REDMAGIC lens sample							
$0.15 < z_{\rm ph} < 0.35$	330 243	0.022	1.3134				
$0.35 < z_{\rm ph} < 0.50$	571 551	0.038	-0.5179				
$0.50 < z_{\rm ph} < 0.65$	872 611	0.058	0.3372				
$0.65 < z_{\rm ph} < 0.80$	442 302	0.029	2.2515				
$0.80 < z_{\rm ph} < 0.90$	377 329	0.025	1.9667				
Мас	MAGLIM lens sample						
$0.20 < z_{\rm ph} < 0.40$	2 236 473	0.150	1.2143				
$0.40 < z_{\rm ph} < 0.55$	1 599 500	0.107	1.1486				
$0.55 < z_{\rm ph} < 0.70$	1 627 413	0.109	1.8759				
$0.70 < z_{\rm ph} < 0.85$	2 175 184	0.146	1.9694				
$0.85 < z_{\rm ph} < 0.95$	1 583 686	0.106	1.7805				
$0.95 < z_{\rm ph} < 1.05$	1 494 250	0.100	2.4789				

galaxy clustering correlation functions, the $3 \times 2pt$ data vector in the configuration space of DES Y3.

In this work we use the implementation of the Full-sky lognormal Astro-fields Simulation Kit (FLASK; Xavier et al. 2016) to generate a suite of 1800 log-normal realisations of our data vector.

The FLASK requires a set of angular power spectra as its primary input. These spectra must include the auto- and cross-correlations of all the desired cosmic fields, simulated as HEALPIX maps. We generate them using the theoretical framework presented in Section 3.1 at the fiducial REDMAGIC + METACALIBRATION cosmology of Table 3. A more detailed description of the parameters of Table 3 is found in Section 3.1 and the power spectra

Table 2. The DES Y3 source sample properties. Similar to Table 1, this table shows the photometric redshift selection, the effective galaxy number density, $(n_{\rm eff})$ in arcmin⁻², the shape-noise per-component, (σ_e) and the mean shear response, $(\langle R_{\gamma} \rangle)$, and the mean selection response, $(\langle R_{\gamma} \rangle)$.

redshift bin	$n_{\rm eff}$	σ_e	$\langle R_{\gamma} \rangle$	$\langle R_S \rangle$
$0.0 < z_{\rm ph} < 0.36$	1.476	0.243	0.7636	0.0046
$0.36 < z_{\rm ph} < 0.63$	1.479	0.262	0.7182	0.0083
$0.63 < z_{\rm ph} < 0.87$	1.484	0.259	0.6887	0.0126
$0.87 < z_{\rm ph} < 2.0$	1.461	0.301	0.6154	0.0145

measurements in the suite of log-normal realisations are presented in Appendix B.

2.3 Angular power spectra measurements

We estimate angular power spectra of galaxy clustering (GCL) and galaxy-galaxy lensing (GGL) using the so-called pseudo- C_{ℓ} (PCL) or MASTER method (Peebles 1973; Hivon et al. 2002; Brown et al. 2005), as implemented in the NAMASTER code⁷ (Alonso et al. 2019).

We commence by constructing weighted tomographic cosmic shear maps as

$$\vec{\gamma}_p = \frac{\sum_{i \in p} v_i^{(\gamma)} \hat{\vec{\gamma}}_i}{\sum_{i \in p} v_i^{(\gamma)}},\tag{1}$$

where the index *i* runs over galaxies in the catalogue, index *p* runs over pixels in map, $\hat{\gamma}_i = (\hat{\gamma}_{1,i}, \hat{\gamma}_{2,i})$ is the calibrated galaxy shear and $v_i^{(\gamma)}$ its associated weight.

Analogously, tomographic galaxy over-density maps are given by

$$\delta_{p} = \frac{N_{p} \sum_{p'} w_{p'}^{(\delta)}}{w_{p}^{(\delta)} \sum_{p'} N_{p'}} - 1$$
(2)

where $N_p = \sum_{i \in p} v_i^{(\delta)}$ gives the number of galaxies at a given pixel p, with v_i the weight associated with the *i*-th galaxy as given by the systematics weights (see Section 2). When working with simulated log-normal realisations, we assume $v_i = 1$. Whereas, $w_p^{(\delta)}$ gives the effective fraction of the area covered by the survey at pixel p.

In addition to the cosmic shear and galaxy clustering signal maps, the pseudo- C_{ℓ} method relies on the use of an angular window function, also known as the mask. Such a mask encodes the information of the partial-sky coverage of the observed signal and is used to deconvolve this effect on the estimated bandpowers. For the cosmic shear maps, we use the inverse-variance weighting scheme as presented in Nicola et al. (2021), and construct tomographic mask maps as

$$w_p^{(\gamma)} = \sum_{i \in p} v_i^{(\gamma)}.$$
(3)

We note this approach assigns the weighted number of galaxies map

as mask, thus there are different masks for each source tomographic bin.

The discrete nature of galaxies introduces a shot-noise contribution to the auto-correlation spectra. We estimate this noise analytically, as specified below, and subsequently, we subtract it from our power spectrum estimates. For the case of galaxy clustering we assume this noise to be Poissonian, and estimate it analytically for the pseudo-spectra following Alonso et al. (2019), Nicola et al. (2020), and García-García et al. (2021) as

$$\tilde{N}_{\ell}^{(\delta)} = \left(\frac{\sum_{p} w_{p}^{(\delta)}}{N_{\text{pix}}}\right) \frac{1}{n_{\text{eff}}},\tag{4}$$

where N_{pix} is the total number of pixels in our maps. We note that this noise is constant over all multipoles. For HEALP1x-based pixelization, this is given in terms of the HEALP1x resolution parameter (Górski et al. 2005), N_{side} as $N_{\text{pix}} = 12N_{\text{side}}^2$. Note the first term in parentheses is the mean of the mask on the sphere. The second term is the Poissonian noise in terms of the effective mean angular number density, n_{eff} , when accounting for the galaxy weights, v_i^{δ} , as

$$n_{\rm eff} = \frac{\left(\sum_{i} v_i^{(\delta)}\right)^2}{\Omega_{\rm pix} \sum_{p} w_p^{(\delta)} \sum_{i} \left(v_i^{(\delta)}\right)^2},\tag{5}$$

where Ω_{pix} is the area of each HEALP1x pixel at the given resolution.

For the case of cosmic shear, the pseudo-spectra noise is computed following Nicola et al. (2020) as

$$\tilde{N}_{\ell>2}^{(\gamma)} = \Omega_{\text{pix}} \frac{\sum_{p} \sum_{i \in p} \left(v_i^{(\gamma)} \right)^2 \sigma_{e,i}^2}{N_{\text{pix}}},$$
(6)

where $\sigma_{e,i}^2 = (\hat{\gamma}_{1,i}^2 + \hat{\gamma}_{2,i}^2)/2$ is the RMS noise per galaxy for a given shape estimator.

Finally, the different pseudo-spectra are binned into bandpowers. The chosen bandpowers are a set of 32 square-root-spaced bins within the multipole interval $\ell = [8, 2048]$. The angular power spectra measurements for galaxy clustering C_{ℓ}^{gg} and galaxy-galaxy lensing C_{ℓ}^{gE} using the REDMAGIC and MAGLIM lens samples are shown in Figures 3 and 4, along with the theory prediction calculated at the Λ CDM best-fit values. For MAGLIM, we use one prediction considering only the first four tomographic bins (green) and another using all six bins (purple). The residual plots comparing the measurements to these predictions are shown below for each redshift combination. The measurements of the 1800 log-normal realisations can be found in Appendix B.

3 METHODOLOGY

3.1 Theoretical modelling

Our theoretical framework for modelling the angular power spectra draws upon the formalism presented in Krause et al. (2021).

We calculated the galaxy clustering angular power spectra using the full non-Limber approach detailed in Section III.B of Krause et al. (2021),

$$C_{ij}^{gg}(\ell) = \frac{2}{\pi} \int_0^\infty \frac{\mathrm{d}k}{k} \, k^3 P_{\mathrm{NL}}(k) \Delta^i_{\delta_g}(k,\ell) \Delta^j_{\delta_g}(k,\ell),\tag{7}$$

⁷ github.com/LSSTDESC/NaMaster

Table 3. The parameters used in the present analyses. We show the fiducial values used for the construction of the log-normal realisations and the prior probability distributions used for the Bayesian parameter inference. Priors for the REDMAGIC + METACALIBRATION analysis follow the ones described in Pandey et al. (2022) while the priors for the MAGLIM + METACALIBRATION are the same as in Porredon et al. (2022). Uniform priors are described by $\mathcal{U}(x, y)$, with x and y denoting the prior edges, and Gaussian priors are represented by $\mathcal{N}(\mu, \sigma)$, with μ and σ being the mean and standard deviation. The dark energy equation of state w is fixed at -1 for Λ CDM chains, while for wCDM it varies following the indicated uniform prior. The main analyses were performed only with linear galaxy bias in their modelling; the non-linear galaxy bias parameters were used in some additional runs (see Section 3.2 and 4.3).

	Cos	smology		Intrinsic Alignments	\$
Parameters	Fiducial values	Priors	Parameters	Fiducial values	Priors
Ω_m	0.3	$\mathcal{U}(0.1, 0.9)$	a_1	0.7	U(-5.0, 5.0)
h_0	0.69	$\mathcal{U}(0.55, 0.91)$	a_2	-1.36	U(-5.0, 5.0)
Ω_b	0.048	$\mathcal{U}(0.03, 0.07)$	α_1	-1.7	U(-5.0, 5.0)
n _s	0.97	$\mathcal{U}(0.87, 1.07)$	α_2	-2.5	U(-5.0, 5.0)
$A_{s}10^{9}$	2.19	$\mathcal{U}(0.5, 5.0)$	b_{TA}	1.0	$\mathcal{U}(0.0, 2.0)$
$\Omega_{\nu}h^2$	0.00083	$\mathcal{U}(0.0006, 0.00644)$	z_0	0.62	Fixed
w	-1	ACDM: fixed wCDM: $\mathcal{U}(-2, -0.33)$			

REDMAGIC + METACALIBRATION			MAGLIM + METACALIBRATION			
Parameters	Fiducial values	Priors	Parameters	Fiducial values	Priors	
Linear galax	y bias		Linear galax	y bias		
b_i	1.7, 1.7, 1.7, 2.0, 2.0	$\mathcal{U}(0.8, 3.0)$	b_i	1.5, 1.8, 1.8, 1.9, 2.3, 2.3	$\mathcal{U}(0.8, 3.0)$	
Non-linear g	alaxy bias		Non-linear g	alaxy bias		
$b_1^i \sigma_8$	1.42, 1.42, 1.42, 1.68, 1.68	U(0.67, 2.52)	$b_1^i\sigma_8$	1.43, 1.43, 1.43, 1.69, 1.69, 1.69	$\mathcal{U}(0.67, 3.0)$	
$b_2^i \sigma_8$	0.16, 0.16, 0.16, 0.35, 0.35	U(-3.5, 3.5)	$b_2^i \sigma_8$	0.16, 0.16, 0.16, 0.36, 0.36, 0.36	$\mathcal{U}(-4.2, 4.2)$	
Shear calibra	ation		Shear calibra	ıtion		
m^1	-0.0063	$\mathcal{N}(-0.0063, 0.0091)$	m^1	-0.006	N(-0.006, 0.008	
m^2	-0.0198	$\mathcal{N}(-0.0198, 0.0078)$	m^2	-0.010	N(-0.010, 0.013	
m^3	-0.0241	$\mathcal{N}(-0.0241, 0.0076)$	m^3	-0.026	$\mathcal{N}(-0.026, 0.009)$	
m^4	-0.0369	N(-0.0369, 0.0076)	m^4	-0.032	N(-0.032, 0.012)	
Source photo)- <i>z</i>		Source photo)-Z		
Δz_s^1	0.0	N(0.0, 0.018)	Δz_s^1	0.0	$\mathcal{N}(0.0, 0.018)$	
Δz_s^2	0.0	N(0.0, 0.015)	Δz_s^2	0.0	N(0.0, 0.013)	
$\Delta z_s^2 \\ \Delta z_s^3$	0.0	N(0.0, 0.011)	Δz_s^3	0.0	$\mathcal{N}(0.0, 0.006)$	
Δz_s^4	0.0	<i>N</i> (0.0, 0.017)	Δz_s^4	0.0	$\mathcal{N}(0.0, 0.013)$	
Lens photo-2	7		Lens photo-2	z shift		
Δz_l^1	0.006	$\mathcal{N}(0.006, 0.004)$	Δz_l^1	-0.009	N(-0.009, 0.007	
Δz_I^2	0.001	<i>N</i> (0.001, 0.003)	Δz_l^2	-0.035	N(-0.035, 0.011	
Δz_I^3	0.004	$\mathcal{N}(0.004, 0.003)$	Δz_l^3	-0.005	N(-0.005, 0.006	
$\begin{array}{l} \Delta z_l^2 \\ \Delta z_l^3 \\ \Delta z_l^4 \\ \Delta z_l^5 \end{array}$	-0.002	$\mathcal{N}(-0.002, 0.005)$	Δz_l^4	-0.007	N(-0.007, 0.006	
Δz_1^5	-0.007	$\mathcal{N}(-0.007, 0.01)$	Δz_l^5	0.002	N(0.002, 0.007)	
-	-	-	Δz_l^6	0.002	$\mathcal{N}(0.002, 0.008)$	
Lens photo-:	z stretch		Lens photo-2	z stretch		
σz_l^1	1.0	Fixed	σz_l^1	0.975	$\mathcal{N}(0.975, 0.062)$	
σz_l^2	1.0	Fixed	σz_l^2	1.306	N(1.306, 0.093)	
σz_l^1 σz_l^2 σz_l^3 σz_l^4 σz_l^5	1.0	Fixed	σz_I^3	0.870	N(0.870, 0.054)	
σz_l^4	1.0	Fixed	σz_l^4	0.918	N(0.918, 0.051)	
σz_l^5	1.23	N(1.23, 0.054)	$\sigma z_l^4 \\ \sigma z_l^5 \\ \sigma z_l^6$	1.080	$\mathcal{N}(1.080, 0.067)$	
-	-	-	σz_l^6	0.845	$\mathcal{N}(0.845, 0.073)$	

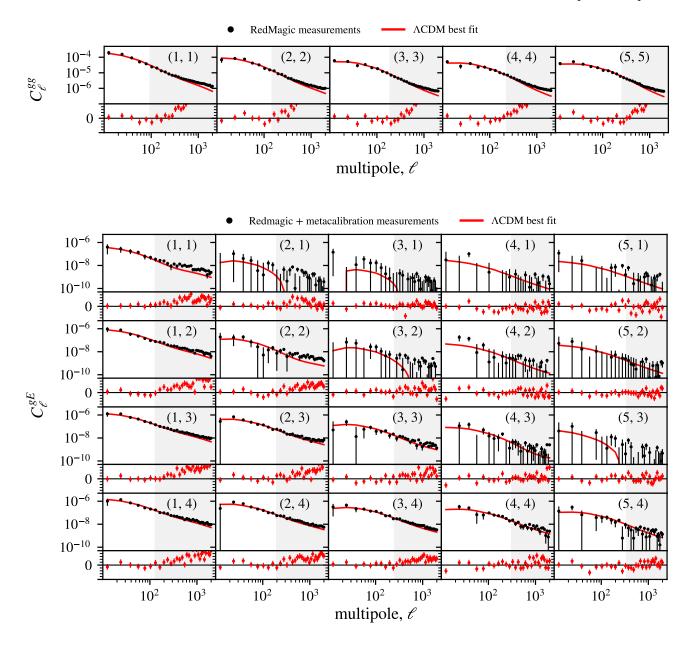


Figure 3. Angular power spectrum measurements of galaxy clustering (C_{ℓ}^{gg}) and galaxy-galaxy lensing (C_{ℓ}^{gE}) from the DES Y3 REDMAGIC and METACALI-BRATION catalogues, along side with theoretical prediction calculated at the Λ CDM best-fit values. Residual plots compare measurements with the theoretical prediction.

where the kernel accounts for linear density growth (D), redshiftspace distortions (RSD) and lensing magnification (μ) , $\Delta_{\delta_g}^i(k, \ell) = \Delta_D^i(k, \ell) + \Delta_{RSD}^i(k, \ell) + \Delta_{\mu}^i(k, \ell)$. The specific form of each term is provided by Krause et al. (2021) and Fang et al. (2020b). Numerical integrations were performed using the FFTLog algorithm (Hamilton 2000) as implemented by Fang et al. (2020b).

The galaxy-galaxy lensing spectra, on the other hand, were evaluated under the Limber approximation,

$$C_{ij}^{gE}(\ell) = \int d\chi \frac{q_{\delta_g}^i(\chi) q_{\gamma}^J(\chi)}{\chi^2} P_{\rm NL}\left(k = \frac{\ell + 0.5}{\chi}, z(\chi)\right).$$
(8)

In both Equations (7) and (8), we refer to δ_g as the *lens galaxy sample* overdensity field and γ as the *source galaxy sample* shear field and

i, *j* run over tomographic redshift bins for the corresponding galaxy sample.

Furthermore, Equations (7) and (8) can be understood as projections of the nonlinear total matter power spectrum, $P_{\rm NL}(k, z)$, computed using CAMB (Lewis et al. 2000) and HALOFIT (Takahashi et al. 2012), by specific radial kernels per tomographic bin along the comoving distance χ or redshift z. These kernels encode the response to the large-scale structure of the different probes at different scales and are given by

$$q_{\delta_g}^i(\chi) = b^i(k, z(\chi)) n_{\delta_g}^i(z(\chi)) \frac{\mathrm{d}z}{\mathrm{d}\chi},\tag{9}$$

$$q_{\gamma}^{i}(\chi) = \frac{3H_{0}^{2}\Omega_{\rm m}}{2c^{2}} \frac{\chi}{a(\chi)} \int_{\chi}^{\infty} \mathrm{d}\chi' n_{\gamma}^{i}\left(z(\chi')\right) \frac{\mathrm{d}z}{\mathrm{d}\chi'} \frac{\chi'-\chi}{\chi'},\qquad(10)$$

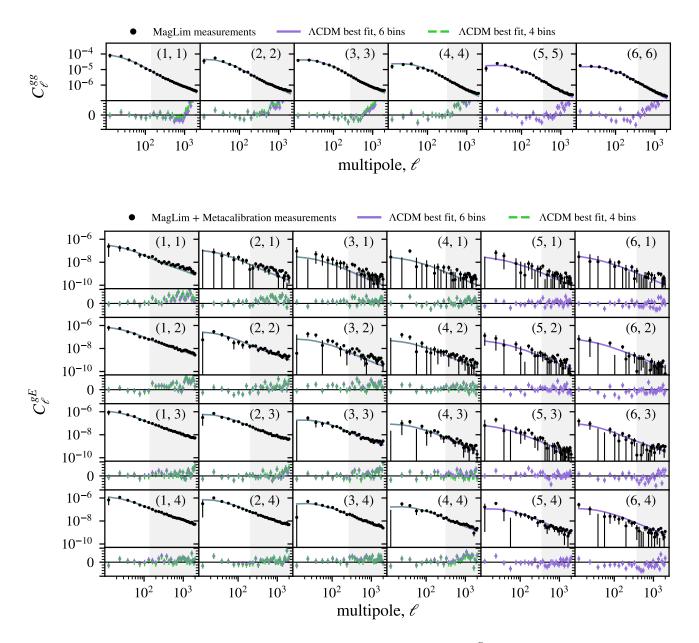


Figure 4. Angular power spectrum measurements of galaxy clustering (C_{ℓ}^{gg}) and galaxy-galaxy lensing (C_{ℓ}^{gE}) from the DES Y3 MAGLM and METACALI-BRATION catalogues, alongside with theoretical prediction calculated at the ACDM best-fit values from the analysis using all six tomographic lenses (solid, purple line) and only the first four bins (dashed, green line). Residual plots compare measurements with the theoretical prediction from the six-bin (purple markers) and four-bin (green points) analysis. The indexes (z_i, z_j) in each subplot indicate the redshift bin combination. For GGL, z_i and z_j refer to the bin of the lens and source, respectively.

where H_0 is the Hubble's constant, Ω_m the matter density, $a(\chi)$ the scale factor corresponding to the comoving distance χ , b(k, z) the scale-dependent galaxy bias, and $n^i_{\delta_g/\gamma}(z)$ the normalised redshift distributions of the lens/source galaxies in the tomographic bin *i*.

We consider two models for the galaxy bias b(k, z). The first, and fiducial choice, is a linear bias model where $b(k, z) = b^i$ is a constant free parameter for each tomographic bin *i*. The second one is a nonlinear biasing model presented by Saito et al. (2014) and Pandey et al. (2022), consisting of a perturbative galaxy bias model to third order in the density field with four parameters: b_{1}^{i} (linear bias), b_{2}^{i} (local quadratic bias), $b_{s^2}^{i}$ (tidal quadratic bias) and b_{3nl}^{i} (third-order non-local bias). Following Pandey et al. (2022) and Porredon et al. (2022), we fix the bias parameters $b_{s^2}^i$ and b_{3nl}^i to their co-evolution value of $b_{s^2}^i = -4(b^i - 1)/7$ and $b_{3nl}^i = b^i - 1$ (Saito et al. 2014), making the total number of free parameters for this bias model two per tomographic bin *i*. We further note that for this second model, the power spectra from HALOFIT is not used. Instead, different kernels for each bias term are computed from the linear power spectrum, following Saito et al. (2014) and Pandey et al. (2022).

To account for the contribution to the observed galaxy shapes caused by the gravitational tidal field, the so-called intrinsic alignment (IA) effect, we adopt the tidal alignment tidal torquing (TATT) model of Blazek et al. (2019). The TATT model has five parameters: a_1 and α_1 characterise the amplitude and redshift dependence of the tidal alignment; a_2 and α_2 characterise the amplitude and redshift dependence of the tidal torquing effect and b_{TA} accounts for the fact that our measurement is weighted by the observed galaxy counts. Following Pandey et al. (2022) and Porredon et al. (2022) we will also compare our results using a simpler IA model, the nonlinear alignment (NLA) model of Bridle & King (2007). The NLA model is equivalent to the TATT model in the limit where $a_2, \alpha_2, b_{TA} \rightarrow 0$, thus having two free parameters.

Foreground structure can distort the observed lens galaxy properties due to gravitational lensing magnification effects. Such distortions are commonly known as lens magnification, and impact both the apparent position and the distribution of light received from individual galaxy images. We model the effect of lens magnification following Krause et al. (2021) and Elvin-Poole, MacCrann et al. (2023) by modifying the lens galaxy overdensity kernel, Equation (9), as

$$q^{i}_{\delta_{g}}(\chi) \to q^{i}_{\delta_{g}}(\chi)(1 + C^{i}_{g}\kappa^{i}_{g}), \tag{11}$$

where κ_g^i is the tomographic convergence field, as defined in Krause et al. (2021) and Elvin-Poole, MacCrann et al. (2023), and C_g^i are the magnification bias coefficients. We fix the values of C_g^i to the ones estimated by Elvin-Poole, MacCrann et al. (2023) as listed in Table 1.

To account for possible residual uncertainty in both lens and source galaxies redshift distributions, we introduce shift parameters, Δz^{i} , when modelling the redshift distributions,

$$n^{i}(z) \to n^{i}(z - \Delta_{z}^{i}).$$
⁽¹²⁾

For the lens sample, motivated by Cawthon et al. (2022) and Porredon et al. (2022) we additionally introduce stretch parameters (σ_z^i), as

$$n^{i}(z) \rightarrow \frac{n^{i}}{\sigma_{z}^{i}} \left(\frac{z - \langle z \rangle}{\sigma_{z}^{i}} + \langle z \rangle - \Delta_{z}^{i} \right),$$
 (13)

where $\langle z \rangle$ is the mean redshift of the *i*-th tomographic bin.

To account for possible residual uncertainty in the shear calibration, we introduce multiplicative factors to the shear kernel, Equation (10), as

$$q^{i}_{\gamma}(\chi) \to (1+m^{i})q^{i}_{\gamma}(\chi) \tag{14}$$

where m^i is the shear calibration bias for source bin *i*.

Finally, the theoretical angular power spectrum is binned into bandpowers. This is done by filtering the predictions with a set of bandpower windows, $\mathcal{F}_{q\ell}^{ab}$, consistent with the pseudo- C_{ℓ} approach we follow for the data estimates (see Section 2.3). Thus the final model for a bandpower, $\ell \in q$, is computed as

$$\mathbf{C}_{(i,j)}(q) = \sum_{\ell \in q} \mathcal{F}_{q\ell}^{(i,j)} \mathbf{C}_{(i,j)}(\ell)$$
(15)

where (i, j) represents the tomographic redshift bin pair, and a vector notation, $\mathbf{C} = (C^{gg}, C^{gE}, C^{gB})$, is required to account for the E/B-mode decomposition of the shear field. We refer the reader to Alonso et al. (2019) for the detailed expressions for the bandpower windows and details about the E/B-mode decomposition.

All the different pieces for the modelling presented above are integrated as modules in the $COSMOSIS^8$ framework (Zuntz et al.

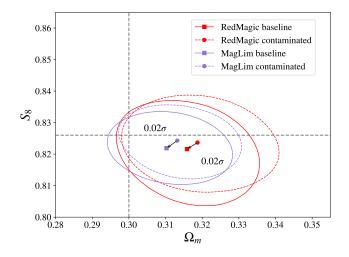


Figure 5. 2-dimensional posterior of S_8 and Ω_m for REDMAGIC and MAGLIM baseline and contaminated data vectors under the extended (8, 6) Mpc/*h* scale cut, both analysed with linear bias and HALOFIT model. The ellipses represent $0.3 \sigma_{2D}$ contours around their best-fit values marked in the centre. The arrows and numbers show the distance between the best-fit of baseline and contaminated chains.

2015) in an analogous way to what was done for the configurationspace analysis presented in Porredon et al. (2022) and Pandey et al. (2022).

The complete set of parameters of the theoretical modelling is summarised in Table 3, including their fiducial values and priors. For Λ CDM analyses, we sample over the matter density Ω_m , the Hubble parameter h_0 , the amplitude of primordial scalar density fluctuations A_s , the spectral index n_s , the baryonic density Ω_b , and the massive neutrino density Ω_v . The equation of state of dark energy *w* is set as a free parameter in the *w*CDM analyses. Following the DES standard, we quote our results in terms of the clustering amplitude, defined as

$$S_8 \equiv \sigma_8 \left(\frac{\Omega_m}{0.3}\right)^{0.5},\tag{16}$$

where σ_8 is the amplitude of mass fluctuations on 8 Mpc/*h* scale in linear theory.

3.2 Scale cuts

Due to the fact that the chosen theoretical modelling is not a complete astrophysical modelling – lacking known effects that appear in smaller, non-linear scales such as baryonic dynamics and higher order non-linear galaxy bias – using the full range of scales in this analysis would result in inaccurate results. For that reason, finding the scales for which our modelling correctly predicts the physics involved is a crucial part of this work.

In order to find this range of scales, we test our pipeline with two simulated data vectors. One represents our fiducial modelling, while the other includes additional modelling for non-linear galaxy bias and baryons, the dominant non-linear effects of galaxy clustering and GGL. From now on, they will be referred to as baseline and contaminated data vectors, respectively. The non-linear galaxy bias were modelled by including contributions from the local quadratic bias b_2^i for every photo-*z* bin of lenses *i* (see Section 3.1). Their fiducial values are the same ones from (Pandey et al. 2022) and (Porredon et al. 2022), and can be found in Table 3. The impact

⁸ https://github.com/joezuntz/cosmosis

of the baryonic physics were modelled using hydrodynamic simulations with strong AGN feedback. In particular, we use the AGN simulation (van Daalen et al. 2011) from the OverWhelmingly Large Simulations project (OWLS) suite (Schaye et al. 2010). Following the approach of the DES Y3 methods paper (Krause et al. 2021), we expect a valid scale cut to satisfy the criteria of $0.3\sigma_{2D}$ of compatibility in the $S_8 \times \Omega_m$ plane of posteriors, calculated at the best-fit values from both data vectors.

The galaxy-galaxy lensing signal in configuration space is inherently non-local. This means the predicted signal at a given source-lens separation depends on the modelling of all scales within that separation, including non-linear small scales. Several approaches have emerged to address the non-locality of the configuration space galaxy-galaxy lensing signal (Baldauf et al. 2010; MacCrann et al. 2020; Park et al. 2021), see Prat et al. (2023) for a recent comparison of different approaches. In this work, we do not implement any additional methodology to circumvent non-localities in GGL. In harmonic space, the modelling of a given scale does not exhibit explicit dependence on smaller scales. Nevertheless, we try to be extra careful about the scales we are including in the analysis. We present two approaches: the conservative and extended scale cuts. For both, we made sure that the baseline and contaminated data vectors have a compatibility well under the $0.3\sigma_{2D}$ criterion. We evaluated compatibility using our standard pipeline with the priors of Table 3. To remain conservative and apply more stringent tests to the models considered, we did not perform nuisance parameter marginalisation, following the prescription in Krause et al. (2021). The results are summarised in Figure 5. The ellipses represent the marginalised $0.3\sigma_{2D}$ contours of the baseline and contaminated data vectors under the extended scale cut, and the difference between the peaks of these posteriors are denoted by the arrows.

To select these scale cuts, we first defined a minimum physical distance R_{\min} that is associated to a maximum comoving Fourier mode $k_{\max} = 1/R_{\min}$. The maximum multipole ℓ_{\max} can then be extracted for every redshift bin of lenses by the following relation:

$$\ell_{\max} = k_{\max} \,\chi(\langle z_i \rangle) \tag{17}$$

where $\langle z_i \rangle = \left(\int z n_i(z) dz \right) / \left(\int n_i(z) dz \right)$ is the mean redshift for the *i*th tomographic set of lenses and χ is the comoving distance assuming the fiducial cosmology of the analysis (see Table 3). This means that GGL combinations sharing the same lenses also share the same ℓ_{max} .

From this relation come our two sets of scale cuts: the *conservative* approach using $R_{\min}^{\text{gcl}} = 8 \text{ Mpc}/h$ and $R_{\min}^{\text{ggl}} = 12 \text{ Mpc}/h$ for clustering and GGL respectively; and the *extended* approach, that goes to lower scales in GGL with $R_{\min}^{\text{ggl}} = 6 \text{ Mpc}/h$. Both methodologies follow the criteria from DES configuration space analyses. The R_{\min}^{ggl} reference in the conservative approach is the same as the one in DES Collaboration (2018), when the GGL data also did not receive special modelling for its non-localities. On the other hand, the minimum physical scale of $R_{\min}^{\text{ggl}} = 6 \text{ Mpc}/h$ was chosen in (DES Collaboration 2022; Prat et al. 2022; Pandey et al. 2022), when those non-localities were modelled using the point-mass marginalisation technique. Appendix E summarises the maximum multipoles associated with each one of these minimum distances for clustering and GGL.

3.3 Likelihood

We assume our power spectra measurements follow a multivariate Gaussian likelihood distribution with a fixed covariance matrix,

$$-2\ln \mathcal{L} (\mathbf{D} \mid \Theta, M) = \chi^2 = [\mathbf{D} - \mathbf{d}(\Theta)] \cdot \mathbf{C}^{-1} \cdot [\mathbf{D} - \mathbf{d}(\Theta)], \quad (18)$$

where $\mathbf{d}(\Theta)$ is the theoretical prediction for our data vector, constructed by stacking the power spectra bandpowers for both probes, GCL and GGL, given the parameters Θ as described in Section 3, and assuming a model *M*.

The corresponding measured data vector, **D**, is also constructed by stacking the measured power spectra bandpowers for both probes over the different pair combinations of tomographic bins considered, accounting for scale cuts (see Sections 2.3 and 3.2). We note that including shear ratios (SR) measurements is out of the scope of this work. The SR methodology, as described by Sánchez & Prat et al., (2022), consists in taking the ratios of two GGL measurements that share the same lens tomographic bin. Under the limit that the lens distribution is sufficiently thin, this ratio loses its dependency on the power spectra and, thus, results in a geometrical measurement of the lensing system. One can then use the SR from the small scales measurements of GGL, which would be discarded after the scale cut, to increase the constraining power of the analysis by improving the constraints of the systematics and nuisance parameters of the model. These measurements were incorporated at the likelihood level in other DES Y3 works (DES Collaboration 2022; Pandey et al. 2022; Porredon et al. 2022; Doux et al. 2022). The methods to measure and apply shear ratios to harmonic space analyses are currently under development and will be implemented in future projects using DES Y6 data.

Finally, **C** is the joint covariance of galaxy clustering and galaxy-galaxy lensing power spectra. It is analytically decomposed into Gaussian and non-Gaussian components arising from the cosmic shear and galaxy overdensity fields. The Gaussian contribution is computed using NAMASTER to account for binning and mode coupling coming from partial sky coverage with the improved narrow-kernel approximation (iNKA) developed by García-García et al. (2021), as optimised by Nicola et al. (2021). We also account for the noise contribution to the covariance in the Gaussian term, using the analytical estimate from Equations (4) and (6) as described in Nicola et al. (2021). For this, we rely on the iNKA implementation of the general covariance calculator interface to be used for the Vera C. Rubin Observatory's Legacy Survey of Space and Time (LSST⁹) Dark Energy Science Collaboration (DESC) LSST Dark Energy Science Collaboration (2012), TJPCov¹⁰.

The non-Gaussian contribution comprises two components: i) the connected four-point covariance (cNG), arising from the joint cosmic shear and galaxy clustering trispectra; and ii) the super-sample covariance (SSC), which accounts for correlations between Fourier modes used in the analysis and super-survey modes (Takada & Hu 2013). The computation of both components utilises the implementation provided by COSMOLIKE (Krause & Eifler 2017; Fang et al. 2020a). This follows the methodology outlined in Krause et al. (2021), which in turn draws upon formulae established in the works of Takada & Jain (2009) and Schaan et al. (2014). We simplify the treatment of partial sky coverage and binning for the non-Gaussian contribution by scaling it with the observed fraction of the sky, f_{sky} and computing it on the grid of points defined by the effective multipole of each bandpower considered.

A sample covariance was also computed from a set of 1800 log-normal simulations, and its comparison with our theoretical

⁹ https://www.lsst.org/lsst

¹⁰ https://github.com/LSSTDESC/TJPCov

covariance is discussed in Section 3.4. The right-hand panel of Figure 6 shows both covariances side by side, while the left-hand panel shows the ratio of their diagonal. The compatibility between them is discussed in Section 3.4.

As discussed in Friedrich et al. (2021), calculating covariance matrices at a set of values considerably different from the best-fit values of the analysis can have a meaningful impact on the likelihood contours. For that reason, the results on data shown in Section 4 were run twice, where in the second run the covariance was recalculated at the best-fit values of the first iteration. Appendix A discusses the impact of updating the covariance in our main analyses.

The likelihood (Equation (18)) is related to the posterior distributions of the parameters via the Bayes' theorem:

$$P(\Theta|\mathbf{D}, M) \propto \mathcal{L}(\mathbf{D}|\Theta, M) \Pi(\Theta|M), \tag{19}$$

where $\Pi(\Theta|M)$ is the prior probability distribution given a model M. The parameters constraints are reported by the mean of their marginalised posterior distributions and the 68% confidence limits (C.L.) relative to this mean as error bars. The constraining power of different analyses are compared through the 2D Figure of Merit, defined as FoM_{Θ_1,Θ_2} = (det Cov(Θ_1,Θ_2))^{-1/2}, while the distance between their constraints is calculated as the difference between their best-fit values in terms of σ_{2D} , the marginalised 68% C.L. on the $S_8 \times \Omega_m$ plane. The parameter inference was performed with the PolyChord sampler (Handley et al. 2015a; Handley et al. 2015b).

3.4 Validations on simulated data

Before any work on data was done, all the aspects of the pipeline were extensively tested using simulated data vectors and covariances, to make sure that the developed methodology would not rely on biased expectations for the real measurements. A set of 1800 independent log-normal realisations generated by the code FLASK (Xavier et al. 2016) were produced for this purpose (Section 2.2). The measurements of the angular power spectra of this set are discussed in Appendix B.

The simulated covariance is a sample covariance matrix calculated out of this set of log-normal realisations. The right-hand panel of Figure 6 shows the analytical and sample covariance side by side. In the left-hand panel, we compare the diagonal terms of both covariances, finding a good agreement in the valid range of scales after performing the scale cuts (non-shaded areas). The largest deviations occur at large scales - more specifically, at the first and second bandpowers - where the sample covariance has error bars around $\sim 10\%$ larger than the analytical for most combinations. We assessed the compatibility between our analytical and sample covariance by verifying their impact on cosmological constraints. Running the pipeline on our baseline data vector with the sample covariance and the final, analytical covariance for the REDMAGIC analysis showed an excellent agreement, resulting in a difference lower than $0.01\sigma_{2D}$. The marginalised constraints are shown in the first (sample cov.) and second (theoretical cov.) rows of Figure 7.

One can notice that, despite the baseline angular power spectra being a noiseless, simulated data vector, the constraints found are not centred at their fiducial values – although they are still consistent within 1σ . This deviation can be attributed to the so-called prior projection effects. In this particular analysis, the projection of the Ω_{ν} prior is the main source of this effect (see Krause et al. 2021 for more discussions on that). This statement is illustrated by the constraints shown in the third row of Figure 7, where we run the pipeline on the same baseline data vector but with this parameter fixed, resulting in a much smaller deviation. This happens because Ω_{ν} is prior dominated and its true value is set close to the boundary of the flat prior, which allows the peak of the likelihood to shift in the direction of its degeneracies.

For the remaining two rows of Figure 7, we perform some more pipeline tests with the sample covariance but using the average of all 1800 log-normal realisations (mock average) and a single, arbitrary realisation (single mock) as data vectors. As expected, we see that the constraints obtained by the mock average case are consistent with the baseline ones, and that the single mock constraints are compatible with the true values within 1σ .

Finally, taking advantage of the single mock data vector, we also check the goodness-of-fit compatibility between our analytical and sample covariance. After running the pipeline on the single mock with the sample covariance matrix, we obtained $\chi_F^2 = 182$ at the best-fit parameters for the extended scale cut, with 227 - 30 = 197 degrees of freedom (reduced $\chi_F^2 = 0.92$), while the same test using our theoretical matrix resulted in $\chi_T^2 = 208$ (reduced $\chi_T^2 = 1.05$).

This χ^2 difference, $\Delta \chi^2_{T-F} = 11$, can be compared with analytical approximations for its expected value and variance (see Section 7 in Andrade-Oliveira et al. 2021 and Fang et al. 2020a):

$$E[\Delta \chi_{T-F}^{2}] = \operatorname{Tr}(\mathbf{C}_{T}^{-1}\mathbf{C}_{F}) - N_{D},$$

$$\operatorname{Var}[\Delta \chi_{T-F}^{2}] = 2N_{D} + 2\operatorname{Tr}(\mathbf{C}_{T}^{-1}\mathbf{C}_{F}\mathbf{C}_{T}^{-1}\mathbf{C}_{F}) - 4\operatorname{Tr}(\mathbf{C}_{T}^{-1}\mathbf{C}_{F}),$$

$$(21)$$

where Tr represents the trace operator, C_T and C_F are the theoretical and the sample covariance from FLASK, respectively, and N_D is the number of degrees of freedom. These give us the estimation $E[\Delta \chi^2_{T-F}] = 9.11 \pm 9.00$, within a 1 σ agreement with what was previously calculated for the particular realisation.

4 RESULTS

After all the processes described in Section 3 to validate our methodology with simulated data vectors and covariance, the analysis pipeline was applied to the real data. Due to the fact that the DES Y3 catalogues are public already, no specific blinding method was applied. That being said, as described in Section 3, every step of the pipeline had been previously tested and validated using simulations so that measurements of the catalogues and the main cosmological chains had to be run only once.

The main results of this work are presented in this Section. First, the constraints for Λ CDM (Section 4.1) and wCDM (Section 4.2) modelling are shown and discussed alongside the main results from Pandey et al. (2022) and Porredon et al. (2022). Table 4 summarises the constraints obtained, as well as the gain in constraining power in the 1D marginalised posteriors of Ω_m , S_8 and w, and the agreement between harmonic and configuration space chains in the $S_8 \times \Omega_m$ 2D plane. In Appendix C we discuss the goodness-of-fit of these results. Subsequently, a series of internal consistency and robustness tests are discussed (Section 4.3).

As discussed in Section 3.3, after running the pipeline on data once, we recalculated the theoretical covariance at its best-fit values and ran the pipeline again with the updated covariance. Although the results of all these first iteration chains had a satisfactory goodness-of-fit, the runs for MAGLIM using all six photometric bins of lenses resulted in a p-value very close to the 0.01 requirement on goodness-of-fit used in the DES Y3 unblinding process (see Table C1). This worst fit for the six-bin case after updating the covariance also happened in Porredon et al. (2022), where they localised the

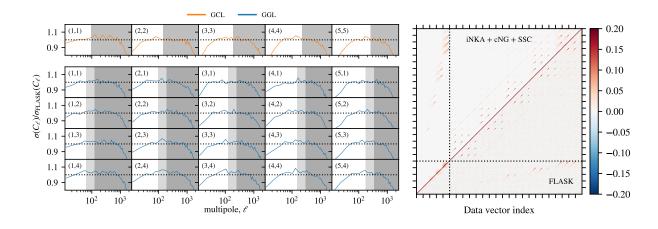


Figure 6. The analytical covariance matrix used in this work is computed using TJPCov, NAMASTER, and COSMOLIKE. Left: Comparison of the error bars estimated from log-normal realisations with the fiducial ones. We show the galaxy clustering (GCL) and galaxy-galaxy lensing (GGL) separately and the indexes (z_i, z_j) in each subplot indicate the redshift bin combination. For GGL, z_i and z_j refer to the bin of the lens and source, respectively. Right: The full correlation matrix, from the log-normal realisations in the lower triangle, and the full analytical model including Gaussian (iNKA) and non-Gaussian (nNG + SSC) contributions in the upper triangle (note the normalisation in the range -0.2 to 0.2).

Table 4. 68% C.L. marginalised cosmological constraints in ACDM and wCDM using the combination of DES Y3 galaxy clustering and galaxy-galaxy lensing measurements (2×2pt) in harmonic space (HS). In parenthesis after the constraints are the improvements of the error bars when compared to the configuration space (CS) results from Pandey et al. (2022) and Porredon et al. (2022). Last column shows the agreement, calculated as described in Section 3.3.

REDMAGIC model	Scale cut	Ω_m	S_8	σ_8	w	HS-CS agreement
ЛСDМ	(8,6) Mpc/h	0.325 ± 0.040 (-19%)	0.704 ± 0.029 (+2%)	$0.681^{+0.045}_{-0.072}$	-	$1.03\sigma_{ m 2D}$
ΛCDM	(8,12) Mpc/h	$0.328 \pm 0.041 \; (-22\%)$	$0.690 \pm 0.034 \; (-15\%)$	$0.665^{+0.041}_{-0.071}$	-	$0.29\sigma_{ m 2D}$
wCDM	(8,6) Mpc/h	$0.301^{+0.037}_{-0.048} \ (+7\%)$	$0.682^{+0.025}_{-0.039}\ (0\%)$	$0.685^{+0.042}_{-0.052}$	-1.28 ± 0.29 (+8%)	$0.95\sigma_{ m 2D}$
MAGLIM model	Scale cut	Ω_m	S_8	σ_8	W	HS-CS agreement
ACDM, 6 bins	(8,6) Mpc/h	$0.307^{+0.027}_{-0.037}$ (+14%)	0.753 ± 0.024 (+29%)	0.748 ± 0.054	-	$0.9\sigma_{ m 2D}$
ACDM, 6 bins	(8,12) Mpc/h	$0.315^{+0.028}_{-0.042} \ (+9\%)$	$0.739 \pm 0.033 \ (+3\%)$	0.726 ± 0.061	-	$1.27\sigma_{ m 2D}$
wCDM, 6 bins	(8,6) Mpc/h	$0.302 \pm 0.036 \; (+17\%)$	$0.759 \pm 0.032 \ (+20\%)$	0.760 ± 0.051	$-1.01^{+0.24}_{-0.18}\;(+2\%)$	$0.35\sigma_{ m 2D}$
ΛCDM, 4 bins	(8,6) Mpc/h	$0.324^{+0.032}_{-0.047}$ (-7%)	0.779 ± 0.028 (+18%)	0.754 ± 0.064	-	$0.02\sigma_{ m 2D}$
ΛCDM, 4 bins	(8,12) Mpc/h	$0.330^{+0.038}_{-0.043} \ (-9\%)$	$0.761 \pm 0.035 \; (-3\%)$	$0.731^{+0.058}_{-0.076}$	-	$0.14\sigma_{2D}$
wCDM, 4 bins	(8,6) Mpc/h	$0.321^{+0.040}_{-0.047}\ (+17\%)$	$0.745 \pm 0.039 \ (+24\%)$	$0.726^{+0.057}_{-0.067}$	$-1.26^{+0.34}_{-0.27}\ (+7\%)$	0.42 $\sigma_{ m 2D}$

problem to be related to the last two redshift bins. Combining this with the fact that the best-fit values found for the six-bin case are considerably more sensitive to the covariance update, as discussed in Appendix A, we decided to quote the four-bin MAGLIM results as the fiducial ones for this work. For completeness, however, the results found using all six bins of MAGLIM are still shown in this Section.

We note that there are other DES works that performed cosmological analyses using all six bins of MAGLIM in configuration space. In Giannini et al. (2023) an alternative calibration for the MAGLIM redshift distributions was presented, and in Elvin-Poole, MacCrann et al. (2023) the impact of the magnification bias was studied. We further note the results shown in these analyses are consistent with both the fiducial configuration space analysis (Porredon et al. 2022) and the present work.

4.1 ΛCDM

The constraints derived from the harmonic space (HS) pipeline developed for this study, using galaxy clustering and galaxy-galaxy lensing measurements in ACDM analyses, are presented in Figure 8 for REDMAGIC (left-hand panel) and MAGLIM (right-hand panel; HS contours in the lower triangle include all six tomographic bins, while only the first four are included in the upper triangle) samples. The results for the DES Y3 2×2pt configuration space analyses (Pandey et al. 2022; Porredon et al. 2022) are also shown for comparison.

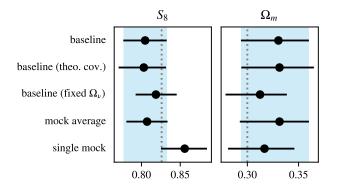


Figure 7. Comparison of marginalised constraints of REDMAGIC-like analyses between a fiducial, noiseless data vector (baseline), and data vectors constructed from the mean over the 1800 log-normal realisations (mock average) and a single realisation (single mock). First two rows: constraints of the baseline data vector with the sample covariance and the final theoretical covariance used in the REDMAGIC analysis. Third row: constraint of the baseline data vector with the sample covariance, but fixing the value of Ω_{ν} . Forth and fifth rows: constraints of the mock average and single mock data vectors with the sample covariance. The vertical dotted lines represent the fiducial values used to construct both the noiseless data vector and the lognormal realisations. Shaded vertical regions are the 68% C.L. marginalised regions from the constraints in the first row.

It is important to emphasise that even though the harmonic space scale cuts were based on the same physical scale threshold as the real space ones, that does not mean both analyses were performed using the exact same information. Furthermore, these configuration space curves use their fiducial analysis choice, which includes shear ratios measurements. As mentioned in Section 3.3, the harmonic space curves do not include shear ratios. The marginalised posterior probability distributions for Ω_m , S_8 and σ_8 are summarised in Table 4.

From Figure 8, one can immediately notice that the RED-MAGIC constraints point to lower values of S_8 , both in harmonic and configuration space. This is properly discussed in (Pandey et al. 2022), where they found a bias in the galaxy selection of the fiducial sample of REDMAGIC. This issue was responsible for the best-fit values of the galaxy bias b_i from the clustering part of the data vector to be systematically higher than the galaxy-galaxy lensing part, thus implying that the phenomenological parameter $X_{\text{lens}}^i = b_{\text{GGL}}^i / b_{\text{GCL}}^i$, often referenced as "de-correlation", would not be equal to 1 as predicted from local biasing models. In fact, they found $X_{\text{lens}} = 0.9 \pm 0.03$ for the fiducial REDMAGIC catalogue when using a single de-correlation parameter for all redshift bins a 3.5 σ deviation from 1. They were able to trace back the source of this de-correlation to be associated with the goodness-of-fit threshold $\chi^2_{\rm RM}$ for a galaxy to be classified as part of the REDMAGIC sample in the procedure described in (Rozo et al. 2016). Creating a new REDMAGIC sample with a broader χ^2_{RM} was enough to recover X_{lens} compatible with 1.

In this work we only perform analyses using the fiducial RED-MAGIC sample. Although the harmonic space constraints of this sample also point to lower values of S_8 when compared to MAGLIM results, we notice that these constraints are not as low as the one found in configuration space, resulting in a tension of $3.01\sigma_{2D}$ and $2.01\sigma_{2D}$ between REDMAGIC and MAGLIM four and six bins in HS, respectively, under the extended scale cut. The de-correlation parameter X_{lens} for the REDMAGIC fiducial sample in harmonic space is consistent with what was found in configuration space, although slightly more compatible with 1 due to the higher S_8 , as indicates Figure 9. In order to compare the X_{lens} constraints from HS and CS, we followed the prescription in Pandey et al. (2022), where the cosmological parameters were fixed at the DES Y1 best-fit values (DES Collaboration 2018).

From Figure 8 and Table 4 we can see that the harmonic space results using the extended scale cut (shaded curves) have tighter constraints for the clustering amplitude S_8 in all three analyses (REDMAGIC and MAGLIM four and six bins) when compared to the configuration space ones (black lines). On the other hand, while we do find tighter constraints for matter energy density Ω_m in the four and six bins analyses of MAGLIM, the constraining power of REDMAGIC for this parameter is weaker in harmonic space. The Λ CDM 4 and six bins analyses of MAGLIM had an improvement in FoM of 64% and 14% for our extended scale cut, while REDMAGIC had a decrease of -15%.

The level of agreement between the harmonic and configuration space results can be quantified on the $S_8 \times \Omega_m$ plane, as shown in the last column of Table 4. For all Λ CDM cases we see deviations lower than 1σ , except for the 1.03 σ and 1.27 σ found for REDMAGIC with the extended and MAGLIM six bins with the conservative scale cut, which are still statistically compatible with the configuration space results. In particular, the MAGLIM results with four redshift bins shows a strong agreement with CS results (0.02 σ_{2D} and 0.14 σ_{2D}).

The marginalised posteriors of the galaxy bias under the extended scale cut are shown in Figures 10 and 11. We find an overall good compatibility between the harmonic and configuration space constraints. The REDMAGIC HS results systematically show a small tail towards lower values of b_i , making the constraints slightly looser than in CS. For MAGLIM, on the other hand, the results for the four bins analysis reproduce well what was found in CS, while the six bins run shows an expected increase in the constraining power. Appendix D shows the 1D marginalised posteriors of all parameters, along with their priors and their CS counterparts. A discussion about the goodness-of-fit of all these runs can be found in Appendix C.

4.2 wCDM

Similarly to what was presented in Section 4.1, the harmonic space results of the analogous chains but considering the *w*CDM cosmological model and our extended scale cut are shown in Figure 12 (again, bottom triangle includes all six tomographic bins of MAGLIM, while the upper triangle includes only the first four bins). The HS constraints are represented by the shaded contours, and we also included their respective counterpart results in CS following the fiducial choices of Pandey et al. (2022) and Porredon et al. (2022) (black and grey lines).

The constraints derived for Ω_m , S_8 , σ_8 , and w can be seen in Table 4, which also shows the agreement between harmonic and configuration space results in the $S_8 \times \Omega_m$ plane. All wCDM results in HS are compatible with CS under $1\sigma_{2D}$. However, we note that the REDMAGIC and MAGLIM four bins constraints are very consistent with each other and are compatible with w = -1 within 1σ .

4.3 Internal consistency and robustness tests

A series of additional tests on data was performed to investigate the internal consistency of the data vectors and the robustness of our modelling. The results of those tests are summarised in Figure 13 for REDMAGIC (left) and MAGLIM (right).

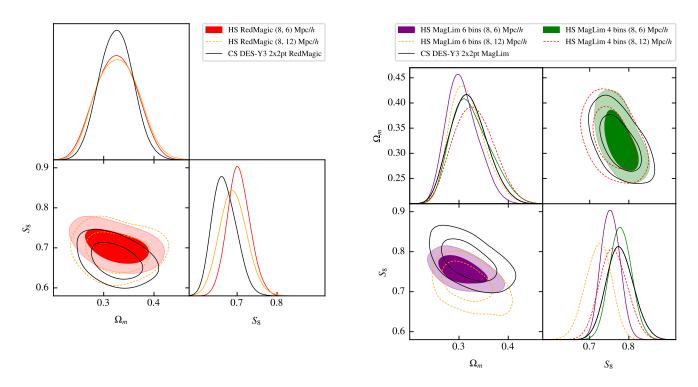


Figure 8. marginalised constraints on S_8 and Ω_m in Λ CDM from galaxy clustering and galaxy-galaxy lensing joint analyses. Left: Harmonic (HS) and configuration space (CS) REDMAGIC constraints. Right: Harmonic and configuration space MAGLIM constraints. Configuration space curves are the main results from Pandey et al. (2022) and Porredon et al. (2022), which includes shear ratio measurements in their analysis and 4 tomographic bins of lenses for MAGLIM.

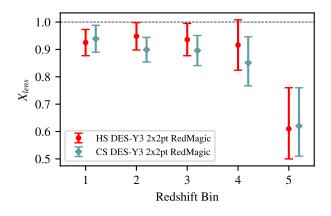


Figure 9. Constraints on the de-correlation parameter X_{lens} for each tomographic redshift bin of the fiducial REDMAGIC sample. Harmonic space results (HS) are represented by the red, circle markers, while the green, diamond markers represents configuration space (CS) from Pandey et al. (2022).

The first set of tests (second quadrant in Figure 13) consists in additional runs changing the structure of the data vectors. The *small scales only* test restricts the analysis to physical scales smaller than the threshold of 30 Mpc/*h* (same threshold used in Pandey et al. (2022) and Porredon et al. (2022)), while *large scales only* restricts the analysis to scales larger than this limit. The other consistency tests are chains removing the information from one tomographic bin of lenses at a time.

The second set of tests (third quadrant in Figure 13) corresponds to the following changes in the theoretical modelling:

• NLA: variation of the intrinsic alignment model, setting parameters a_2 , η_2 and b_{TA} to zero.

• Fixed neutrinos: the mass range of neutrinos modelling is fixed at its lower boundary.

• Non-linear bias: the modelling also includes the non-linear galaxy bias effect, following the parameters in Table 3.

• wCDM: changes the dark energy parametrization.

The respective results in configuration space for each internal consistency and robustness test are also shown in Figure 13, all following their main analyses choices of including shear ratios and four bins of lenses for MAGLIM (green diamond marker).

Overall, these series of tests show that harmonic space analyses respond well to changes in the data vector and in the theoretical modelling. One can see that the large scales only results have much bigger error bars for S_8 than its configuration space counterpart. This is probably due to the fact that the S_8 information comes mainly from large multipoles ℓ , which is also the reason why the extended scale cut gives tighter constraints for S_8 over the conservative, but does not improve Ω_m (see Figure 8). Moreover, the limit of 30 Mpc/*h* used to define small and large scales did not separate evenly the number of points in each group. Because of that, the large scales test had 1 - 4 less points than the small scales test for each combination.

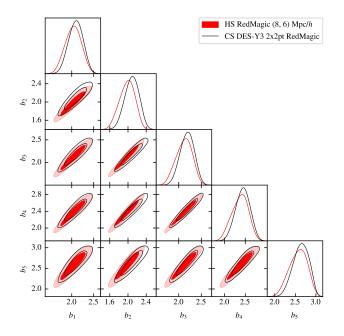


Figure 10. Marginalised posteriors of the linear galaxy bias found in the REDMAGIC analysis. The red, shaded contours are the HS results under the extended scale cut, and the black contours are the CS results from Pandey et al. (2022).

5 CONCLUSIONS

This work presents the harmonic space joint analysis of galaxy clustering and galaxy-galaxy lensing using the DES Y3 data. We performed two independent analyses using the REDMAGIC and MAGLIM catalogues for lens galaxies. In both, the source galaxies came from the METACALIBRATION catalogue.

In order to compare these analyses with their counterparts in configuration space, the theoretical modelling and prior choice followed the ones described in Pandey et al. (2022) and Porredon et al. (2022), although the overall methodology was designed around the harmonic case. In particular, our main results have an optimised scale cut for harmonic space and include two versions of the MAGLIM analysis: using only the first four tomographic bins of lenses and using all six bins.

We describe our data and measurements in Section 2. The estimators used to measure the angular power spectra followed the PCL/MASTER method (Hivon et al. 2002), implemented via the NAMASTER code (Alonso et al. 2019). The entire measurement and analysis pipelines were first rigorously tested using a large set of log-normal realisations. The same set of realisations and contaminated versions of the baseline data vector with non-linear galaxy bias and baryonic effects were used to select and validate our scale cuts and theoretical covariance. We presented two sets of scale cuts: the conservative ($R_{min}^{gcl} = 8 \text{ Mpc}/h$ and $R_{min}^{ggl} = 12 \text{ Mpc}/h$) and extended ($R_{min}^{gcl} = 8 \text{ Mpc}/h$ and $R_{min}^{ggl} = 12 \text{ Mpc}/h$) approaches. For our fiducial MAGLIM analysis (first four tomographic bins

For our fiducial MAGLIM analysis (first four tomographic bins of lenses and the extended scale cut) in the Λ CDM modelling, we found a clustering amplitude of $S_8 = 0.779 \pm 0.028$ and a matter energy density of $\Omega_m = 0.324^{+0.032}_{-0.047}$, corresponding to a constraining power increase of 14% in the $S_8 \times \Omega_m$ plane compared to the main results in Porredon et al. (2022). The same analysis but using all six tomographic bins resulted in $S_8 = 0.753 \pm 0.024$ and $\Omega_m = 0.307^{+0.027}_{-0.037}$, representing 64% increase in constraining

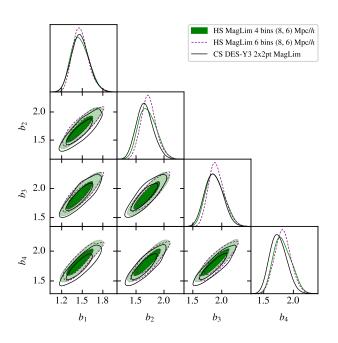


Figure 11. Marginalised posteriors of the linear galaxy bias found in the MAGLIM analysis. The green, shaded contours are the HS results under the extended scale cut and using the first four bins of the sample, while the purple, dashed curves are the constraints from using all six bins of MAGLIM. The black contours are the CS results from Porredon et al. (2022).

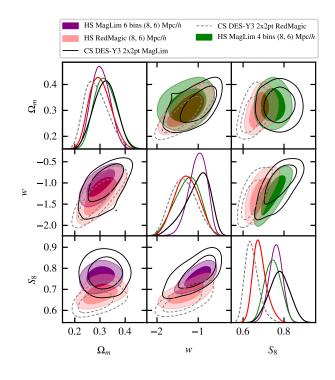


Figure 12. marginalised constraints on w, S_8 and Ω_m in wCDM from galaxy clustering and galaxy-galaxy lensing joint analyses. Purple and red shaded contours represent the harmonic space (HS) chains under the (8,6) Mpc/*h* scale cut respectively. Solid and dashed contours represent the configuration space (CS) wCDM results from Pandey et al. (2022) and Porredon et al. (2022), which includes shear ratio measurements in their analysis and 4 tomographic bins of lenses for MAGLIM.

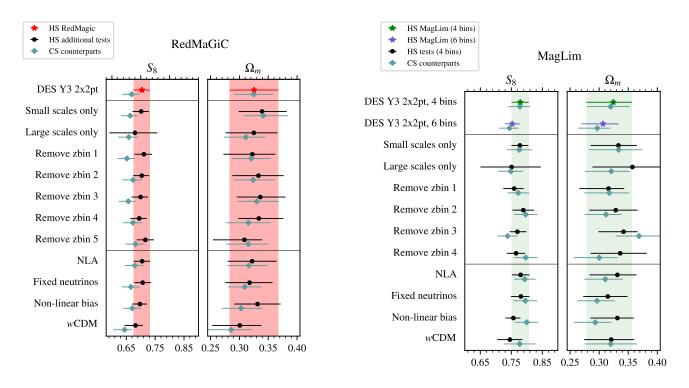


Figure 13. Internal consistency and robustness tests for the galaxy clustering and galaxy-galaxy lensing joint analyses for the extended scale cut. Left: REDMAGIC DES Y3 2×2pt (red star) in harmonic space (HS), additional tests in HS (black circles) and their configuration space (CS) counterparts (green diamonds) from Pandey et al. (2022). Right: MAGLIM DES Y3 2×2pt (purple star) in HS, additional tests in HS (black circles) and their CS counterparts (green diamonds) from Porredon et al. (2022). All CS tests include shear ratio measurements and use 4 tomographic bins of lenses for MAGLIM, except where otherwise is mentioned. From top to bottom of both figures: first quadrant demarcates main results; second quadrant, internal consistency tests; and third quadrant, tests for the model robustness.

power. It is worth noting, however, that the six-bin analysis exhibited the poorest goodness-of-fit and the greatest impact on the cosmological constraints following the update of the covariance, as detailed in Appendices A and C. Their respective results for a *w*CDM modelling was $S_8 = 0.745 \pm 0.039$, $\Omega_m = 0.321^{+0.040}_{-0.047}$ and $w = -1.26^{+0.34}_{-0.27}$ for the four-bin analysis, and $S_8 = 0.759 \pm 0.032$, $\Omega_m = 0.302 \pm 0.036$ and $w = -1.01^{+0.24}_{-0.18}$ for the six-bin.

For REDMAGIC with the (8,6) Mpc/h scale cut, on the other hand, our Λ CDM results were $S_8 = 0.704 \pm 0.029$ and $\Omega_m = 0.325 \pm 0.040$, representing a 15% decrease in the constraining power when compared to the main results in Pandey et al. (2022). Interestingly, however, the harmonic chains for REDMAGIC prefer slightly higher values of S_8 .

The goodness-of-fit of all analyses are discussed in Appendix C and the 1D marginalised posteriors of each parameter are shown along side with their priors and configuration space counterparts in Appendix D.

Additional tests were made and presented in Section 4.3 to check the internal consistency of our data vectors and the robustness of the theoretical modelling. The tests had a very consistent agreement with our DES Y3 $2\times$ 2pt results for REDMAGIC and MAGLIM, as Figure 13 summarises.

This work is the first publication of the Dark Energy Survey collaboration to describe a methodology for galaxy-galaxy lensing in the harmonic space, paving the path for a $3 \times 2pt$ analysis in harmonic space for DES Y6, a project already under development. To do so, other than combining the present work with the one

developed for the DES Y3 cosmic shear in harmonic space (Doux et al. 2022) and incorporating the Y6 guidelines being currently developed for the $3\times2pt$ in configuration space, there are additional procedures to be worked on.

We expect the methodology presented in this work to pave the way for and incentivise future harmonic space analyses of significantly larger datasets from next generation Stage-IV imaging programmes, such as those anticipated from LSST Ivezić et al. (2019) and Euclid (Laureijs et al. 2011).

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REFERENCES

- Alam S., et al. 2021, Phys. Rev. D, 103, 083533
- Alonso D., et al. 2019, MNRAS, 484, 4127
- Andrade-Oliveira F., et al. 2021, Monthly Notices of the Royal Astronomical Society, 505, 5714
- Asgari M., et al. 2021, A&A, 645, A104
- Baldauf T., et al. 2010, Phys. Rev. D, 81, 063531
- Blazek J. A., et al. 2019, Phys. Rev. D, 100, 103506
- Bridle S., King L., 2007, New Journal of Physics, 9, 444
- Brown M. L., Castro P. G., Taylor A. N., 2005, MNRAS, 360, 1262
- Camacho H., et al. 2022, MNRAS, 516, 5799
- Cawthon R., et al. 2022, MNRAS, 513, 5517
- Clerkin L., et al. 2017, MNRAS, 466, 1444
- Coles P., Jones B., 1991, MNRAS, 248, 1
- DES Collaboration 2018, Physical Review D, 98

- DES Collaboration 2022, Physical Review D, 105
- Dalal R., et al. 2023, Phys. Rev. D, 108, 123519
- De Vicente J., Sánchez E., Sevilla-Noarbe I., 2016, MNRAS, 459, 3078
- Doux C., et al. 2022, Monthly Notices of the Royal Astronomical Society, 515, 1942
- Elvin-Poole J., MacCrann N., et al., 2023, MNRAS, 523, 3649
- Fang X., Eifler T., Krause E., 2020a, MNRAS, 497, 2699
- Fang X., et al. 2020b, J. Cosmology Astropart. Phys., 2020, 010
- Feroz F., Hobson M. P., 2008, Monthly Notices of the Royal Astronomical Society, 384, 449–463
- Feroz F., Hobson M. P., Bridges M., 2009, Monthly Notices of the Royal Astronomical Society, 398, 1601–1614
- Feroz F., et al. 2019, The Open Journal of Astrophysics, 2
- Friedrich O., et al. 2018, Phys. Rev. D, 98, 023508
- Friedrich O., et al. 2021, Monthly Notices of the Royal Astronomical Society, 508, 3125–3165
- García-García C., et al. 2021, J. Cosmology Astropart. Phys., 2021, 030
- Gatti M., et al. 2021, MNRAS, 504, 4312
- Giannini G., et al. 2023, Monthly Notices of the Royal Astronomical Society, 527, 2010–2036
- Górski K. M., et al. 2005, ApJ, 622, 759
- Gruen D., et al. 2018, Phys. Rev. D, 98, 023507
- Hamilton A. J. S., 2000, MNRAS, 312, 257
- Handley W. J., Hobson M. P., Lasenby A. N., 2015a, Monthly Notices of the Royal Astronomical Society: Letters, 450, L61–L65
- Handley W. J., Hobson M. P., Lasenby A. N., 2015b, MNRAS, 453, 4384
- Harris C. R., et al. 2020, Nature, 585, 357-362
- Heymans C., et al. 2013, MNRAS, 432, 2433
- Heymans C., et al. 2021, A&A, 646, A140
- Hilbert S., Hartlap J., Schneider P., 2011, A&A, 536, A85
- Hinshaw G., et al. 2013, ApJS, 208, 19
- Hivon E., et al. 2002, ApJ, 567, 2
- Howlett C., et al. 2012, J. Cosmology Astropart. Phys., 1204, 027
- Huff E., Mandelbaum R., 2017, arXiv e-prints, p. arXiv:1702.02600
- Hunter J. D., 2007, Computing in Science Engineering, 9, 90
- Ivezić Ž., et al. 2019, ApJ, 873, 111
- Jarvis M., Bernstein G., Jain B., 2004, Monthly Notices of the Royal Astronomical Society, 352, 338–352
- Jarvis M., et al. 2021, MNRAS, 501, 1282
- Joachimi B., et al. 2021, A&A, 646, A129
- Krause E., Eifler T., 2017, Monthly Notices of the Royal Astronomical Society, 470, 2100–2112
- Krause E., et al. 2021, arXiv e-prints, p. arXiv:2105.13548
- LSST Dark Energy Science Collaboration 2012, arXiv e-prints, p. arXiv:1211.0310
- Laureijs R., et al. 2011, arXiv e-prints, p. arXiv:1110.3193
- Lewis A., 2019, GetDist: a Python package for analysing Monte Carlo samples (arXiv:1910.13970)
- Lewis A., Bridle S., 2002, Phys. Rev. D, 66, 103511
- Lewis A., Challinor A., Lasenby A., 2000, ApJ, 538, 473
- Li X., et al. 2023, Phys. Rev. D, 108, 123518
- MacCrann N., et al. 2020, MNRAS, 491, 5498
- MacCrann N., et al. 2022, MNRAS, 509, 3371
- More S., et al. 2023, Phys. Rev. D, 108, 123520
- Myles J., Alarcon A., et al., 2021, MNRAS, 505, 4249
- Nicola A., et al. 2020, J. Cosmology Astropart. Phys., 2020, 044
- Nicola A., et al. 2021, J. Cosmology Astropart. Phys., 2021, 067
- Pandey S., et al. 2022, Phys. Rev. D, 106, 043520
- Park Y., Rozo E., Krause E., 2021, Phys. Rev. Lett., 126, 021301
- Peebles P. J. E., 1973, ApJ, 185, 413
- Perlmutter S., et al. 1997, ApJ, 483, 565
- Perlmutter S., et al. 1999, ApJ, 517, 565
- Planck Collaboration 2020, A&A, 641, A6
- Porredon A., et al. 2021, Phys. Rev. D, 103, 043503
- Porredon A., et al. 2022, Phys. Rev. D, 106, 103530
- Prat J., et al. 2022, Physical Review D, 105 Prat J., et al. 2023, MNRAS, 522, 412
- Qu F. J., et al. 2024, ApJ, 962, 112

- Riess A. G., et al. 1998, AJ, 116, 1009
- Rodríguez-Monroy M., et al. 2022, MNRAS, 511, 2665
- Rozo E., et al. 2016, MNRAS, 461, 1431
- Saito S., et al. 2014, Phys. Rev. D, 90, 123522

Sanchez-Cid D., et al. in prep.

- Sánchez C., et al. 2022, Phys. Rev. D, 105, 083529
- Schaan E., Takada M., Spergel D. N., 2014, Phys. Rev. D, 90, 123523
- Schaye J., et al. 2010, MNRAS, 402, 1536
- Sevilla-Noarbe I., et al. 2021, ApJS, 254, 24
- Sheldon E. S., 2014, MNRAS, 444, L25
- Sheldon E. S., Huff E. M., 2017, ApJ, 841, 24
- Takada M., Hu W., 2013, Physical Review D, 87
- Takada M., Jain B., 2009, MNRAS, 395, 2065
- Takahashi R., et al. 2012, ApJ, 761, 152
- The Dark Energy Survey Collaboration 2005, arXiv e-prints, pp astroph/0510346
- Virtanen P., et al. 2020, Nature Methods, 17, 261
- Weinberg D. H., et al. 2013, Phys. Rep., 530, 87
- Xavier H. S., Abdalla F. B., Joachimi B., 2016, MNRAS, 459, 3693
- Zuntz J., et al. 2015, Astronomy and Computing, 12, 45-59
- Zuntz J., et al. 2018, MNRAS, 481, 1149
- van Daalen M. P., et al. 2011, MNRAS, 415, 3649

APPENDIX A: IMPACT OF COVARIANCE UPDATE

The choice of cosmological parameters employed to calculate the analytical covariance matrix within a Bayesian framework can introduce a bias into the inferred parameter constraints if these parameters deviate significantly from the recovered values (see Friedrich et al. 2021 and references therein). To mitigate bias, the protocol adopted in this and other DES studies involves re-running the analysis with the covariance matrix updated to the best-fit values obtained from the previous iteration.

Figure A1 illustrates the effect of covariance updates on the Λ CDM analyses when applying the extended scale cut. The second iteration of the covariance causes a low impact for REDMAGIC $(0.01\sigma_{2D})$ and MAGLIM four bins $(0.04\sigma_{2D})$ in the $S_8 \times \Omega_m$ plane. For MAGLIM six bins, however, we see a greater impact, although still under $0.3\sigma_{2D}$. We tested updating one more time the covariance for MAGLIM six bins, but it did not result in a convergence as good as the others. As mentioned in 4, the better convergence of the covariance and the goodness-of-fit (detailed in Appendix C) were the reasons to choose the four bins configuration as the fiducial MAGLIM results of the present work.

APPENDIX B: MEASUREMENTS ON THE LOG-NORMAL SIMULATIONS

The pipeline developed to measure the angular power spectra from the DES catalogues was first validated using a set of 1800 lognormal, REDMAGIC-like realisations. These realisations were generated using the FLASK code (Xavier et al. 2016), as detailed in Section 2.2.

Figure B1 presents the measurements of galaxy clustering (top panels) and galaxy-galaxy lensing (bottom panels). It displays the mean of all realisations (solid, blue line) and the associated standard deviation (shaded, blue regions). The simulated power spectra, assumed to be noiseless, used as input for generating the realisations are shown as the dashed black lines (see Table 3 for the fiducial parameters). Across all tomographic combinations of power spectra, the simulated signal is faithfully reproduced by the mean of the

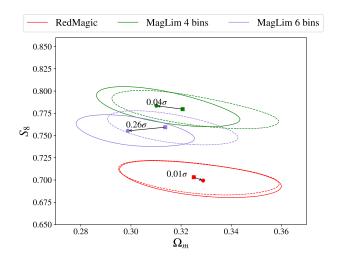


Figure A1. The impact on the $S_8 \times \Omega_m$ plane of updating the covariance for the different cases considered for the 2 × 2pt analysis in harmonic space. All cases assume the extended scale cut and Λ CDM modelling. The square marker and dashed ellipses represent the best-fit value and $0.3 \sigma_{2D}$ contour for the analyses using the original covariances (calculated at fiducial values of Table 3). The circle marker and solid curves represent the analyses using the updated covariance (recalculated at the best-fit values of the previous run).

realisations well within its standard deviation. This demonstrates the internal consistency of the measurement pipeline.

The same set of measurements on log-normal realisations was further used in the validation of the analytical covariance matrix and the analysis pipeline, as detailed in Section 3.4.

APPENDIX C: GOODNESS-OF-FIT

In this section, we summarise and discuss the goodness-of-fit for all the Λ CDM and wCDM presented in Sections 4.1 and 4.2. As described in Section 3.3 and Appendix A, the pipeline was run twice: the first iteration used the original covariance matrix, calculated at the fiducial values listed in Table 3; and the second, for each case, used an updated covariance matrix calculated at the corresponding first iteration best-fit values. Table C1 summarises the goodness-offit information for both iterations of each analysis. It is important to consider that the presented reduced χ^2 does not incorporate the informative priors. Consequently, its actual value is likely to be lower, particularly for the simulations employing the conservative scale cut with fewer data points. Appendix D presents the marginalised Λ CDM posteriors alongside the priors for each parameter.

In particular, for the MAGLIM analyses employing all six bins of the sample, the update in the covariance matrix parameters leads to a significant increase in the χ^2 . This effect, while less pronounced, mirrors the one already observed in the corresponding configuration space analysis, as described in Appendix B of Porredon et al. (2022). Figure 4 displays the residual plots of the Λ CDM best-fit predictions against the angular power spectra measurements.

APPENDIX D: FULL MARGINALISED POSTERIORS

We show all the marginalised 1D posteriors for the full parameter space of our fiducial Λ CDM analysis in Figures D1 and D2 for

REDMAGIC and MAGLIM, respectively. For comparison, the configuration space counterparts from Pandey et al. (2022) and Porredon et al. (2022) are also shown as well as their common prior distributions as computed by the apriori sampler¹¹ of CosmoSiS.

We find no statistically significant constraints on the nuisance parameters, including photometric redshift biases and stretches, and cosmic shear calibration biases, beyond those imposed by the priors.

APPENDIX E: SCALE CUTS IN MULTIPOLE SPACE

In this appendix, we present the effective maximum multipoles, ℓ_{max} , associated with the different scale cut schemes discussed in Section 3.2. Table E1 present summarises the different values for the different power spectra considered.

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¹¹ https://cosmosis.readthedocs.io/en/latest/reference/
samplers/apriori.html

Table C1. The goodness-of-fit for different configurations of the 2×2pt analysis in harmonic space. The first column displays the cosmological model and the number of tomographic bins of lenses for the cases using the MAGLIM sample. The second column shows the scale cut used: either *extended* (8, 6) Mpc/*h* or *conservative* (8, 12) Mpc/*h*. The covariance iteration column tells which version of the covariance was used: either original (calculated at the fiducial parameters shown in Table 3 or recalculated at best-fit values). The last five columns are: the number of total free parameters, the number of data points in the data vector after scale cuts, the χ^2 at best-fit values, the reduced χ^2 assuming the number of degrees of freedom (DoF) as number data points in the data vector minus the total number of parameters constrained, and the corresponding *p*-value.

REDMAGIC model	Scale cut	Cov. iteration	Total params.	data points	χ^2	$\frac{\chi^2}{\text{DoF}}$	<i>p</i> -value
ЛСDM	Extended	Updated	30	227	187	0.95	0.68
ΛCDM	Conservative	Updated	30	159	128	0.99	0.51
wCDM	Extended	Updated	31	227	190	0.96	0.63
АСДМ	Extended	Original	30	227	206	1.05	0.32
ΛCDM	Conservative	Original	30	159	137	1.07	0.28
wCDM	Extended	Original	31	227	210	1.09	0.18
MAGLIM model	Scale cut	Cov. iteration	Total params.	data points	χ^2	$\frac{\chi^2}{\text{DoF}}$	<i>p</i> -value
ACDM, 6 bins	Extended	Updated	37	295	314	1.22	0.01
ACDM, 6 bins	Conservative	Updated	37	207	230	1.35	0.001
wCDM, 6 bins	Extended	Updated	38	295	304	1.17	0.03
Λ CDM, 4 bins	Extended	Updated	31	178	146	0.99	0.51
Λ CDM, 4 bins	Conservative	Updated	31	122	108	1.18	0.09
wCDM, 4 bins	Extended	Updated	32	178	154	1.05	0.31
ACDM, 6 bins	Extended	Original	37	295	242	0.94	0.75
ACDM, 6 bins	Conservative	Original	37	207	178	1.05	0.32
wCDM, 6 bins	Extended	Original	38	295	244	0.95	0.73
ΛCDM, 4 bins	Extended	Original	31	178	135	0.92	0.77
Λ CDM, 4 bins	Conservative	Original	31	122	94	1.03	0.40
wCDM, 4 bins	Extended	Original	32	178	143	0.98	0.56

Table E1. Scale cuts used for the analyses. The maximum multipoles included were calculated from a certain minimum physical distance R_{\min} , which is converted to ℓ_{\max} via Equation (17) for every photo-*z* bin of lenses. This means that GGL combinations sharing the same lenses also share the same ℓ_{\max} . From this we derived our two sets of scale cuts. The conservative scale cut uses $R_{\min} = (8, 12) \text{ Mpc}/h$ respectively for GCL and GGL, following the approach in (DES Collaboration 2018). The extended scale cut, which is our fiducial choice, is derived from $R_{\min} = (8, 6) \text{ Mpc}/h$.

	REDMAG	GIC + METACALII	BRATION	MagLim + METACALIBRATION			
	GCL GGL GGL		GCL	GGL	GGL		
	$R_{\min} = 8 \mathrm{Mpc}/h$	$R_{\min} = 6 \mathrm{Mpc}/h$	$R_{\min} = 12 \mathrm{Mpc}/h$	$R_{\min} = 8 \mathrm{Mpc}/h$	$R_{\min} = 6 \mathrm{Mpc}/h$	$R_{\min} = 12 \mathrm{Mpc}/h$	
Lens 1	$\ell_{\rm max} = 94$	$\ell_{\rm max} = 126$	$\ell_{\rm max} = 63$	$\ell_{\rm max} = 105$	$\ell_{\rm max} = 139$	$\ell_{\rm max} = 70$	
Lens 2	$\ell_{max} = 144$	$\ell_{\rm max} = 193$	$\ell_{\rm max} = 96$	$\ell_{\rm max} = 154$	$\ell_{\rm max} = 204$	$\ell_{\rm max} = 103$	
Lens 3	$\ell_{\rm max} = 187$	$\ell_{\rm max} = 250$	$\ell_{\rm max} = 125$	$\ell_{\rm max} = 199$	$\ell_{\rm max} = 264$	$\ell_{\rm max} = 133$	
Lens 4	$\ell_{max} = 226$	$\ell_{\rm max} = 302$	$\ell_{\rm max} = 151$	$\ell_{\rm max} = 237$	$\ell_{\rm max} = 315$	$\ell_{\rm max} = 158$	
Lens 5	$\ell_{\rm max} = 255$	$\ell_{\rm max} = 340$	$\ell_{\rm max} = 170$	$\ell_{\rm max} = 265$	$\ell_{\rm max} = 353$	$\ell_{\rm max} = 177$	
Lens 6	-	-	-	$\ell_{\rm max} = 283$	$\ell_{\rm max} = 376$	$\ell_{\rm max} = 189$	

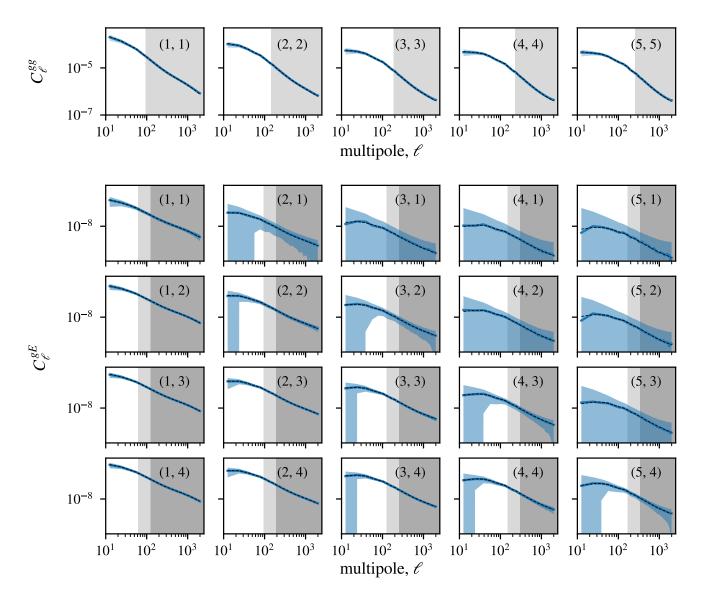


Figure B1. The angular power spectrum measurements for the set of 1800 log-normal realisations. Top panel: average of the galaxy clustering measurements C_{ℓ}^{gg} (solid line) and their standard deviation (blue, shaded area). The grey shaded area represents the scale cut based on the minimum physical scale $R_{min}^{gcl} = 8$ Mpc/*h*. Bottom panel: average of the galaxy-galaxy lensing (GGL) measurements C_{ℓ}^{gE} (solid line) and their standard deviation (blue, shaded area). The grey shaded area represents the scale cut based on the minimum physical scale $R_{min}^{ggl} = 6$ Mpc/*h* (light grey) and $R_{min}^{ggl} = 12$ Mpc/*h* (dark grey). The indexes (z_i, z_j) in each subplot indicate the redshift bin combination. For GGL, z_i and z_j refer to the bin of the lens and source, respectively. The black dashed curves show the input power spectra used to generate the log-normal realisations.

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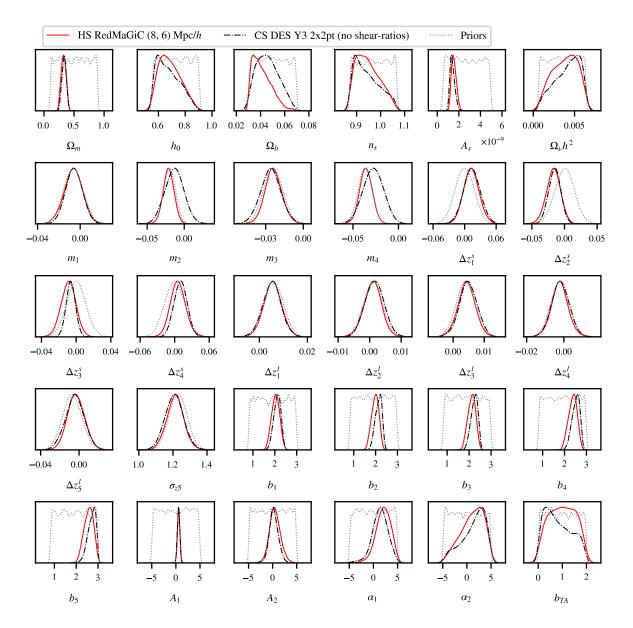


Figure D1. The full marginalised 1D posterior distributions for the fiducial harmonic space analysis of the REDMAGIC dataset (red). The fiducial DES Y3 configuration space analysis counterpart is also shown (black) for comparison as well as the input priors common to both analyses (grey). The prior distributions were sampled using the apriori sampler of CosmoSiS.

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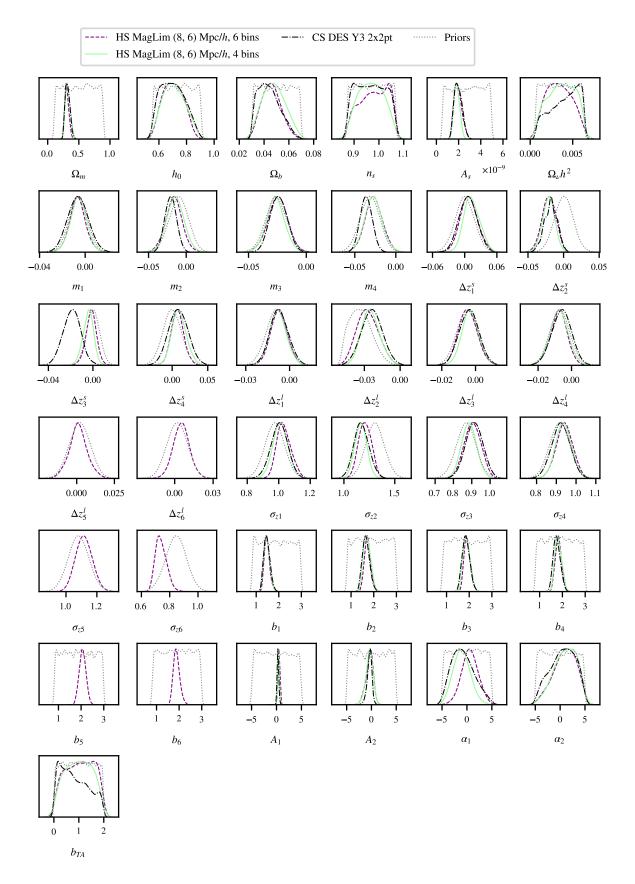


Figure D2. The full marginalised 1D posterior distributions for the fiducial harmonic space analysis of the MAGLIM dataset using 4 (purple) and 6 (green) tomographic bins of lenses. The DES Y3 configuration space analysis without shear ratios counterpart is also shown (black) for comparison as well as the input priors common to both analyses (grey). The prior distributions were sampled using the apriori sampler of COSMOSIS.

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