Constraints on metastable superheavy dark matter coupled to sterile neutrinos with the Pierre Auger Observatory

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Dark matter particles could be superheavy, provided their lifetime is much longer than the age of the universe. Using the sensitivity of the Pierre Auger Observatory to ultra-high energy neutrinos and photons, we constrain a specifc extension of the Standard Model of particle physics that meets the lifetime requirement for a superheavy particle by coupling it to a sector of ultra-light sterile neutrinos. Our results show that, for a typical dark coupling constant of 0.1, the mixing angle θ_m between active and sterile neutrinos must satisfy, roughly, $\theta_m \lesssim 1.5 \times 10^{-6} (M_X/10^9 \text{ GeV})^{-2}$ for a mass M_X of the dark-matter particle between 10⁸ and 10¹¹ GeV.

Despite its countless successes, the Standard Model (SM) of particle physics is known to be incomplete. Missing elements include, among others, dark matter (DM) and neutrino masses.

A minimal extension to the SM is to add right-handed neutrinos inert to SM interactions ("sterile" neutrinos) that mix with left-handed ones active under weak interactions ("active" neutrinos) via the Brout–Englert–Higgs mechanism. Sub-eV mass eigenvalues result from mixing angles made sufficiently small by highly-enough massive sterile neutrinos (seesaw mechanism [1, 2]). Other extensions may use additional sterile neu-

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trinos, as their number is in general largely under-constrained. This is the case of the extension presented in [3], considered in this study as a beyond-standard-model (BSM) benchmark. In this model, which includes DM and neutrino masses, a second sterile neutrino is assumed to render metastable a superheavy particle referred to as X with mass M_X and lifetime τ_X , the decay products of which can leave unique signatures in the data of the Pierre Auger Observatory [4].

A superheavy particle that is metastable attracts particular attention if it is to be a viable DM candidate. The constraints imposed on τ_X are indeed demanding: $\tau_X \ge 10^{22}$ yr, see e.g. [5–11] for recent estimates in various channels. Compliance with these constraints indeed calls for adjusting a reduced coupling constant α_X down to a tiny level and, simultaneously, the multiplicity of the fnal state to a large value [12, 13]. This is in general challenging for theoretical constructions, unless the decay rules are based on non-perturbative effects [14, 15]. In the BSM benchmark [3], however, the lifetime does not resort to such a fine tuning. The DM particle X interacts only with sub-eV and superheavy (10^{12−14} GeV) sterile neutrinos, of masses m_N and M_N respectively, via Yukawa couplings y_m and y_M . In the mass-eigenstate basis, neutrinos are then quasi-active or quasi-sterile, depending on the mixture of active and sterile neutrinos governed by a small mixing angle $\theta_m \simeq \sqrt{2} y_m v / m_v$, with v the electroweak scale and m_v the mass of the known neutrinos. To leading order in y_m , quasi-active neutrinos are produced from quasi-sterile ones subsequent to the decay of X. Consequently, the coupling y_m controls the dominant decay channels and allows for trading a factor $(M_X/M_P)^2$ (with M_P the Planck mass) for a $(m_\nu \theta_m/v)^2$ one in the decay width of X . This trading enables the reduction of the width by a factor ~ $10^{-25} \theta_m^2$ for a benchmark value $M_X = 10^9$ GeV, leading to the required lifetimes well beyond the age of the universe.

Ultra-high energy (UHE) neutrinos and photons are expected to emerge from the cascade of the X decay. In this Letter, we use the sensitivity of the Pierre Auger Observatory to such neutrinos and photons to impose constraints on the active-sterile neutrino mixing angle θ_m for DM masses $M_X \geq 10^8$ GeV. After recalling the main features of the Observatory that enable the detection of neutrinos and photons, we present the main decay channels of the X particle. We then calculate the number of neutrinos and photons expected to be observed at the Observatory as a function of θ_m and M_X . Their non-observation allows us to constrain θ_m for $M_X \ge 10^8$ GeV. In a last section, we comment on the complementary bounds obtained on M_X from DM abundance and on θ_m from cosmological observations.

The Pierre Auger Observatory is the largest ground-based observatory that exploits extensive air showers to study UHE cosmic rays [4]. Several detection techniques are combined. A surface of $3{,}000\,\mathrm{km^2}$ is covered with a ground array of particle detectors separated by 1,500 m surrounded by fuorescence detectors spread over four sites. This baseline confguration is complemented with low-energy enhancements: a frst nested array of 24 km² with particle detectors separated by 750 m and overlooked by three additional fuorescence telescopes with an elevated field of view, and a second one of 1.14 km^2 with detectors separated by 433 m, some of them on top of buried scintillation modules used to measure the number of highenergy muons. The fuorescence detectors provide, during moonless nights, direct observation of the longitudinal shower profle, which allows for the measurement of the energy and the primary-mass sensitive depth of the shower maximum, X_{max} . On the other hand, the ground-level and underground detectors sample the shower particles with a permanent duty cycle. Although showers are observed at a fxed slice in depth with this technique, their longitudinal development is embedded in the signals detected.

Neutrinos of all favors can be distinguished from nuclei through showers developing deeply in the atmosphere at large zenith angles (down-going detection mode) [16], while tau neutrinos can undergo charged-current interactions and produce a τ lepton in the crust of the Earth that eventually decays in the atmosphere, inducing an upward-going shower (Earthskimming detection mode) [17]. In both cases, neutrinos can be identifed at the Observatory with signals in the groundlevel particle detectors that are spread over time, by contrast to narrow ones expected from the much more abundant nucleiinduced showers at large zenith angles [18–20]. Photoninduced showers have also distinct salient features [21, 22]. Their frst interactions are of electromagnetic nature, and the transfer of energy to the hadron/muon channel is reduced with respect to the bulk of hadron-induced showers. This results in a lower number of secondary muons. Additionally, as the development of photon showers is delayed by the typically small multiplicity of electromagnetic interactions, their X_{max} is deeper in the atmosphere than for showers initiated by hadrons.

Based on these characteristics, a number of analyses have been designed to make the most of the sensitivity of the diferent detectors of the Observatory to neutrinos above $\simeq 10^8$ GeV [23] and to photons above 5×10^7 GeV [24–27]. The non-observation of point sources and difuse fuxes allowed the derivation of upper bounds that constrain various models very efectively. In the following, we draw constraints on the BSM benchmark [3] from these non-observations.

In the BSM benchmark [3], the DM candidate is a pseudoscalar particle X coupled to the sterile neutrinos sector alone. The interaction can be represented diagrammatically as

with q the four-momentum of X, and γ the Dirac matrices. Sterile neutrinos, which are right-handed, are denoted as N . Two types of Majorana sterile neutrinos are actually introduced. The first type, N_M , corresponds to the right-handed neutrino of the seesaw mechanism, with a superheavy mass M_N . The second type, N_m , with mass m_N , is necessary

to allow the X particle to decay in an electroweak channel. In the basis of interaction eigenstates, the couplings between sterile neutrinos, active neutrinos and SM Higgs isospinor scalar fields through Yukawa parameters y_m and y_M give rise, after symmetry breakdown, to Dirac masses $m_{N_m}^{\rm D} = y_m v / \sqrt{2}$ and $m_{N_M}^{\rm D} = y_M v / \sqrt{2}$. Assuming the hierarchy $m_N < m_{N_M}^D \ll M_N$, the three mass eigenstates associated to the eigenvalues (m_1, m_2, m_3) are well approximated by the following mixing between v_L (active neutrinos), N_M and N_m (and their conjugate partners with superscripts c):

$$
\nu_1 \simeq (N_m + N_m{}^c) + \theta_m (\nu_L + \nu_L{}^c), \tag{2}
$$

$$
\nu_2 \simeq (\nu_L + \nu_L^c) - \theta_m (N_m + N_m^c), \tag{3}
$$

$$
v_3 \simeq N_M, \tag{4}
$$

with the mixing angle θ_m , assumed to be $\ll 1$, defined as $\theta_m \simeq y_m v / \sqrt{2}(m_1 + m_2)$. For small mixings, the first (second) mass eigenstate v_1 (v_2) is almost the light sterile (active) neutrino with a small admixture of the active (sterile) one, and that the third mass eigenstate v_3 is almost the superheavy sterile neutrino. Note that to avoid complications that would be irrelevant to the question of DM, the favor couplings in the active neutrino sector are considered diagonal in this study. The three mass eigenvalues read as

$$
m_1 \simeq m_N, \tag{5}
$$

$$
m_2 \simeq y_m^2 v^2 / 2M_N, \t\t(6)
$$

$$
m_3 \simeq M_N. \tag{7}
$$

The third eigenstate v_3 appears to decouple from the two other states. While the superheavy particle N_M is essential to provide the mass to the active neutrino through a mixing angle $\theta_M = y_M v/2M_N$ identical to that of the standard seesaw mechanism $[1, 2]$, we shall ignore ν_3 hereafter. From the constraints on SM neutrino masses $\sum m_{\nu} \leq 0.12$ eV inferred from cosmological observations [28], we use hereafter $m_2 \approx 0.04$ eV as a benchmark. As for m_1 , following [3], we use $m_1 = 10^{-4}$ eV to fix the ideas; we shall see below that as long as $m_1 \ll m_2$, results are not sensitive to the specific choice. That $m_1 \ll m_2$ is required for the lifetime of X to be much larger than the age of the universe.

To leading order in θ_m , the interaction described by Eqn. 1 gives rise, in the basis of mass eigenstates, to the two-body decay $X \to \nu_1 \nu_1$. However, in the relevant parameter space such that $m_1 \ll m_2 \ll m_e \ll m_Z \ll M_X$, the total width Γ^X is dominated by three-body channels stemming from the diagram depicted in Eqn. 1 and the interaction between active/sterile neutrinos and the Higgs isodoublet with Yukawa coupling $y_m \simeq \sqrt{2} \theta_m m_2/v$. The channel $X \to h v_1 v_2$, diagrammatically represented as

gives the most important contribution to the width [3]:

$$
\Gamma_{h\nu_1\nu_2}^X = \frac{\alpha_X^2 \theta_m^2}{192\pi^3} \left(\frac{M_X}{M_P}\right)^2 \left(\frac{m_2}{v}\right)^2 M_X.
$$
 (9)

Due to the structure of the interaction depicted in Eqn. 1, a factor $(M_X/M_P)^2$ expected from dimensional arguments [12] is traded for a factor $(m_2/v)^2$.

Although subdominant, there are two other three-body decay channels of interest, namely $X \to Z \nu_1 \nu_2$ and $X \to W \nu_1 e$ with respective widths

$$
\Gamma_{Z\nu_1\nu_2}^X = \frac{\alpha_X^2 g^2 \theta_m^2}{798\pi^3 \cos^2 \theta_W} \left(\frac{M_X}{M_P}\right)^2 \left(\frac{m_2}{m_Z}\right)^2 M_X, \quad (10)
$$

$$
\Gamma_{W_{V_1e}}^X = \frac{\alpha_X^2 g^2 \theta_m^2}{768\pi^3} \left(\frac{M_X}{M_P}\right)^2 \left(\frac{m_1}{m_W}\right)^2 M_X,\tag{11}
$$

with g the weak-isospin gauge constant and $\theta_{\rm W}$ the Weinberg angle. These two widths share the same structure as $\Gamma_{h\nu_1\nu_2}^X$ modulo smaller numerical factors.

UHE neutrinos and photons are expected as byproducts of the decay of any particle with a mass much larger than the electroweak scale. Ultimately, they result from splitting-particle efects due to soft or collinear (real) radiative corrections enhanced by large logarithmic factors at high scale. The probability that a particle a at a scale μ_a fragments to produce a particle b at a scale μ_b carrying a fraction x of the initial energy is described by a fragmentation function (FF) $D_a^b(x; \mu_a, \mu_b)$. The FFs are evolved starting from measurements at the electroweak scale up to the energy scale M_X . In the QCD sector, the evolution is governed by DGLAP equations to account for the splitting function that describes the emission of parton k by parton j . The resulting prompt spectra of photons and neutrinos have been derived in [29] and in several subsequent studies. Similarly, electroweak cascading can be described by evolution equations valid for a spontaneously broken theory [30]. Seminal works of [29, 31, 32] in the QCD sector and of [33] in the electroweak one have provided the calculation of the FFs to derive the prompt fux of high-energy secondaries from the decay of a particle at high scale. We use hereafter the up-to-date HDMSpectra tool [34] to calculate the energy spectra of UHE neutrinos and photons from the decay of the X particle in the $X \to h\nu_1\nu_2$, $X \to Z\nu_1\nu_2$ and $X \to W\nu_1 e$ channels.

The number of neutrinos $n_v(E)$ expected to be observed above an energy threshold E results from the integration over the sky of the directional exposure $\mathcal{E}_v(E, \mathbf{n})$ of the Observatory and of the fux of neutrinos emitted isotropically in proportion to the DM density accumulated in galaxy halos [35]:

$$
n_{\nu}(E) = \iint_{\geq E} d\mathbf{n} \, dE' \frac{\mathcal{E}_{\nu}(E', \mathbf{n})}{4\pi M_X} \left[\frac{d\Gamma_{\nu}(E')}{dE'} \int ds \, \rho(\mathbf{x}_{\odot} + s\mathbf{n}) + \Omega_{X}\rho_{c} \int dz \, \frac{e^{-S_{\nu}(E', z)}}{(1+z)H(z)} \frac{d\Gamma_{\nu}(E^*)}{dE'} \right]_{E^* = (1+z)E'} \Bigg]. \tag{12}
$$

The frst contribution is from the Milky Way halo, in which the DM energy density is parameterized by a profle function $\rho(\mathbf{x})$. **x** \circ is the position of the Solar system in the Galaxy, *s* is the distance from \mathbf{x}_{\odot} to the emission point, and $\mathbf{n} \equiv \mathbf{n}(\ell, b)$ is a unit vector on the sphere pointing to the longitude ℓ and latitude b , in Galactic coordinates. There are uncertainties in the determination of the galactic-halo profle. We use here the traditional NFW profle as a reference [36],

$$
\rho_{\rm DM}(R) = \frac{\rho_s}{(R/R_s)(1+R/R_s)^2},\tag{13}
$$

where R is the distance to the Galactic center, $R_s = 24$ kpc, and ρ_s is fixed by the DM density in the solar neighborhood, namely $\rho_{\odot} = 0.44 \,\text{GeV} \,\text{cm}^{-3}$ [37]. To quantify the systematics stemming from the uncertainties on this profle, we repeat the analysis using other ones [38–40]. The second contribution in Eqn. 12, which is obtained by integration over redshift z and which amounts to about 10% of the frst one, is from all other galaxies. ρ_c is the critical energy density, Ω_X is the DM abundance, $S_{\nu}(E, z)$ is the neutrino opacity of the universe as calculated in [41], and the Hubble rate $H(z)$ depends on that observed today, H_0 , and on the total matter abundance, $\Omega_{\rm m}$, through $H(z) = H_0 \sqrt{\Omega_{\rm m} (1+z)^3 + (1-\Omega_{\rm m})}$. In both contributions, the particle X decays into a (SM) daughter particle whose FF leads to neutrinos. Thus, the diferential decay width into neutrinos, $d\Gamma_{\nu}/dE$, results from the convolution of the differential decay width of X to I with the FF of I into neutrinos. For a single favor, it reads as

$$
\frac{d\Gamma_{\nu}}{dE} = \frac{2}{\Gamma^X} \sum_{I} \int_{x}^{1} \frac{dy}{y} \frac{d\Gamma_{I}^X(y)}{dy} D_{I}^{\nu} \left(\frac{x}{y}, \frac{M_X}{2}, 0\right), \tag{14}
$$

with $x = 2E_v/M_x$. In the $h v_1 v_2$ channel, the differential decay width reads as

$$
\frac{d\Gamma_{\nu}^{X \to h\nu_1\nu_2}(y)}{dy} = 3\Gamma_{h\nu_1\nu_2}^X y^2
$$
 (15)

for neutrino fnal states, while it reads as

$$
\frac{d\Gamma_h^{X \to h\nu_1\nu_2}(y)}{dy} = 6\Gamma_{h\nu_1\nu_2}^X y(1-y)
$$
 (16)

for Higgs fnal states [3]. Similar expressions hold in the cases of the Zv_1v_2 and Wv_1e channels, with the corresponding decay widths. Finally, the differential widths entering into Eqn. 14

Figure 1. Energy spectrum of neutrinos and photons from the decay of the pseudo-scalar particle X within the BSM benchmark [3] ($M_X =$ 10^{10} GeV).

account for all detectable flavors for the $v_{2\alpha}$ species, where an explicit flavor index α is re-introduced. In the down-going detection mode, the three favors contribute explicitly as

$$
\frac{d\Gamma_{\nu_2,all}}{dE} = \frac{2}{\Gamma^X} \int_x^1 \frac{dy}{y} \left[\sum_{\alpha} \left(\frac{d\Gamma_h^{X \to h}(y)}{dy} D_h^{\nu_{2\alpha}} \left(\frac{x}{y} \right) \right) \right. \\
\left. + \frac{d\Gamma_Z^{X \to Z}(y)}{dy} D_Z^{\nu_{2\alpha}} \left(\frac{x}{y} \right) + 2 \frac{d\Gamma_W^{X \to W}(y)}{dy} D_W^{\nu_{2\alpha}} \left(\frac{x}{y} \right) \right) \\
+ \sum_{\alpha,\beta} \left(\frac{d\Gamma_V^{X \to h}(y)}{dy} D_{\nu_{2\beta}}^{\nu_{2\alpha}} \left(\frac{x}{y} \right) + \frac{d\Gamma_V^{X \to Z}(y)}{dy} D_{\nu_{2\beta}}^{\nu_{2\alpha}} \left(\frac{x}{y} \right) \right) \\
+ \sum_{\alpha} 2 \frac{d\Gamma_V^{X \to W}(y)}{dy} D_e^{\nu_{2\alpha}} \left(\frac{x}{y} \right) \right], \quad (17)
$$

with flavor indices α and β . Additionally, the non-zero probability for neutrinos in the fnal state for "no-splitting" leads to an extra contribution

$$
D_{\nu_{2\alpha}}^{\nu_{2\alpha}}\left(\frac{x}{y},\frac{M_X}{2},0\right) \simeq \xi \,\delta\left(\frac{x}{y}-1\right),\tag{18}
$$

with $\zeta = 0.13$. The contribution to the Earth-skimming detection mode is obtained similarly, considering only the τ favor. Besides, the diferential decay width into photons is also calculated following the same procedure, with proper FFs. Note that the expected photon fuxes to be compared to the fux limits are almost-entirely determined by the contribution of the Milky Way halo (due to their attenuation over inter-galactic scales). The resulting energy spectra are shown in Fig. 1 for $M_X = 10^{10}$ GeV. The high-energy enhancements are shaped by the non-zero probabilities for splitting a few times only at high scales.

Constraints in the planes (τ_X, M_X) *and* (θ_m, M_X) *can* be derived from the non-observation of neutrinos at the Observatory. First, 90% C.L. lower limits on the lifetime τ_X are obtained by setting, for a specific value of M_X , $n_V(E)$ or $n_{\gamma}(E)$ to the 90% C.L. upper-limit numbers corresponding to the number of background-event candidates in the absence of signal [42, 43]. More details about the upper-limit numbers for each specifc analysis searching for neutrinos or photons are provided in the supplemental material. Subsequently, a scan in M_X is carried out. It leads to a curve in the plane (τ_X, M_X) that pertains to the energy threshold E considered. By repeating the procedure for several thresholds, a set of curves is obtained, refecting the sensitivity of a specifc energy threshold to some range of mass M_X . The union of the excluded regions fnally provides the constraints in the (τ_X, M_X) plane. Results are shown in Fig. 2 (top panel); lifetimes within the cross-hatched region are excluded. The region in full red pertains to a particular value of a Yukawa coupling $\lambda_{N_m} = 10^{-5}$, the meaning of which will be explained below. To illustrate the contribution from each secondary at our disposal, we show as the dotted the contribution to the constraints stemming from neutrinos alone; an analysis of the IceCube exposure dedicated to the benchmark-scenario decay channels would likely provide better sensitivity for exploring masses $M_X \le 10^{8.5}$ GeV. The lower limit on τ_X is then transformed into an upper limit on θ_m using the expressions of the total width of the particle X . Results are shown in the bottom panel for separate values of α_X : color-coded regions pertain to $\lambda_{N_m} = 10^{-5}$ while their extension (in cross-hatched) would require smaller values of λ_{N_m} . Systematic uncertainties on θ_m constraints amount overall to $\simeq \pm 15\%$; they are dominated by those on the neutrino exposure [23]. The restricted ranges of M_X for different α_X values come from the requirements not to overclose the universe with DM, while the exclusion hatched band comes from not altering the expansion history of the universe with the presence of ultra-light species such as sterile neutrinos N_m . We now briefly explain how these constraints are obtained.

In addition to its couplings to the DM sector and to the SM one through the Higgs isodoublet, the sterile neutrino N_m is also coupled to an infationary sector in the BSM benchmark [3]. This coupling, governed by a unique Yukawa parameter $\lambda_{N_{\rm{m}}}$ for every v_1 neutrinos, yields to a "radiative" production of X via a diagram similar to that depicted in Eqn. 8 (substituting X by the inflaton Φ in the initial state, and h and v_2 by X and v_1 in the final states). Such a mechanism leads to a direct production of DM during the reheating period that can be sufficient, in general, to match the right amount of DM observed today [44]. In the BSM benchmark [3], values for λ_{N_m} are then required to range preferentially around 10⁻⁵. To infer the DM density n_X produced mainly during the reheating epoch, we also consider the minimal setup of gravitational production of X particles through the annihilation of SM (inflaton) particles as in [45] (as in [46]). In these conditions, X particles can be produced as long as the collision rate of particles is larger than the expansion rate H and/or as long as the inflaton field oscillates. By contrast, n_X is prohibitively low to allow any thermal equilibrium for DM. The collision term in the Boltzmann equation is then approximated as a source term

Figure 2. *Top*: Constraints on τ_X as a function of M_X for a value of the couplings of sterile neutrinos with the inflationary sector $\lambda_{N_m} = 10^{-5}$. The dotted line illustrates the constraints stemming from neutrino secondaries alone. *Bottom*: Constraints on θ_m as a function of M_X for three different values of the coupling constant α_X , still for λ_{N_m} = 10⁻⁵. The hatched-red region $\theta_m \ge 9 \times 10^{-4}$ is excluded from the constraint on ΔN_{eff} (see text).

only. Overall, the Boltzmann equation reads as

$$
\frac{dn_X(t)}{dt} + 3H(t)n_X(t) = \sum_i \overline{n}_i^2(t)\gamma_i + \overline{n}_\phi(t)\Gamma_{X\nu_1\nu_1}.\tag{19}
$$

Here, the sum on the right hand side represents the contributions from the SM and infationary sectors. Using, on the one hand, the evolution of the SM-matter and infaton densities derived in [47] and [46] respectively, and, on the other hand, the $SM+SM \rightarrow X+X$ and $\Phi + \Phi \rightarrow X+X$ reaction rates γ_i derived in [48] and [46] respectively, the present-day relic abundance of DM can then be related, using Eqn. 19 in the same way as in [15], to the mass M_X , the Hubble rate at the end of inflation H_{inf} , and the reheating efficiency ϵ quantifying the duration of the reheating period ($\epsilon = 1$ for an instantaneous reheating) [45]. As a result, viable couples of values for (H_{inf}, M_X) scale as $H_{\text{inf}} \propto M_X^2$ up to a maximum value for M_X , which depend on ϵ and α_X . This scaling is a consequence of the domination of the radiative-production process over the gravitational one as long as the allowed values of H_{inf} are too small for a given M_X value to generate significant particle production by gravitational interactions. For larger masses, the contribution from gravitational interactions added to the radiative production of X leads to an overproduction of DM that overcloses the universe, and there is thus no longer solution. This explains why the color-coded regions extend up to some maximum values of M_X in Fig. 2, for a benchmark value of $\lambda_{N_m} = 10^{-5}$. To the right of the regions shown in cross-hatched, λ_{N_m} would need to be smaller.

Another constraint on θ_m stems from the upper bound on the departure from 3 of the effective number of neutrino degrees of freedom N_{eff} , $\Delta N_{\text{eff}} = N_{\text{eff}} - 3$, inferred from cosmological observations. From Friedmann equation, the Hubble parameter is governed by the energy-density content, which, during the radiation-dominated epoch, receives contributions from all relativistic species such as photons, active neutrinos and possible sterile ones. A significant value of ΔN_{eff} would thus change the dynamics of the expansion during the radiation era and thus impact on the cosmological microwave background measurements as well as on the big bang nucleosynthesis. Therefore, the 95%-confidence-level current limits on $\Delta N_{\text{eff}} < 0.3$ [49] provide constraints on the temperature T_{v_1} of v_1 neutrinos:

$$
\Delta N_{\text{eff}} = \frac{3}{2} \left(\frac{T_{\nu_1}}{T_{\nu_2}} \right)^4 < 0.3. \tag{20}
$$

This relationship is valid at any time before the radiation era started, in particular at the time each neutrino species decoupled from the thermal bath when the expansion rate became larger than the interaction rate R_{ν_i} of the species ν_i . Given that the ratio H/R_{v_i} scales as $(T/T_{\star v_i})^3$ [50] (denoting as $T_{\star v_i}$ the decoupling temperature of v_i), and given that the neutral-current-interaction rate of the v_1 species is that of v_2 but reduced by θ_m^2 , the relation $T_{\star \nu_1} = \theta_m^{-2/3} T_{\star \nu_2}$ holds. As soon as T dropped below $T_{\star v_1}$, the temperature of the freely expanding v_1 species fell as $T_{v_1} = (a_{\star 1}/a)T_{\star v_1}$ (with $a_{\star 1}$ the scale factor at the time of the decoupling of the v_1 species). At temperatures $T < T_{\star v_1}$, other particles that are still in thermal equilibrium, such as electrons and positrons, annihilate once T becomes smaller than their mass and thus heat the rest of the relativistic species (photons) relative to the neutrinos. Entropy conservation in this "freeze-out" then gives rise to the relationship

$$
\left(\frac{T_{\nu_1}(T_{\star\nu_2})}{T_{\star\nu_2}}\right)^3 = \frac{N_{\star 2}}{N_{\star 1}},\tag{21}
$$

with $N_{\star i}$ the number of degrees of freedom at $a = a_{\star i}$. Combining Eqn. 20 and Eqn. 21 with $N_{\star 2} = 43/4$ (accounting for two photon polarization states, three species of neutrinos and three of anti-neutrinos, and electrons and positrons each with two spin states) and $T_{\star v_2} = 2$ MeV [50], we obtain that $N_{\star 1} \geq 35.95$ and thus, using [51] to convert N into a temperature, the following bound on θ_m ,

$$
\theta_m \le \left(\frac{T_{\star v_2}}{T_{\star v_1}}\right)^{3/2} \simeq \left(\frac{2 \text{ MeV}}{215 \text{ MeV}}\right)^{3/2} \simeq 9 \times 10^{-4}.\tag{22}
$$

This bound is shown as the cross-hatched band in Fig. 2.¹

In conclusion, we have shown that the data of the Pierre Auger Observatory provide stringent constraints on the angle θ_m mixing sub-eV sterile and active neutrinos in the context of an extension to the SM that couples the sterile neutrinos to a superheavy DM candidate [3]. For a typical dark coupling constant of 0.1, the mixing angle θ_m must satisfy, roughly, $\theta_m \lesssim 1.5 \times 10^{-6} (M_X/10^9 \text{ GeV})^{-2}$ for a mass M_X of the darkmatter particle between 10^8 and 10^{11} GeV. Future sensitivity to the effective number of neutrino degrees of freedom ΔN_{eff} from cosmological observations will be complementary, as they will probe θ_m below 10^{-3} independent of the mass M_X . In particular, a value of ΔN_{eff} departing significantly from 3 would call for sterile neutrinos and would fx the range of the mixing angle θ_m . Our constraints would then be decisive in determining whether the new physics thus revealed in the neutrino sector is intimately related to that of superheavy DM.

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¹ Once translated in terms of effective sterile neutrino mass and ΔN_{eff} (see e.g. [52]), the constraints on neutrino mass-squared diference between eigenstates and on mixing angles between mass and favour eigenstates inferred from neutrino-oscillation experiments are within the dark red band.

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SUPPLEMENTAL MATERIAL

We provide in this supplemental material a few summary plots and data related to the sensitivity of the Observatory to neutrinos and photons. All needed data can be found on www.auger.org.

The calculation of the exposure to neutrinos involves folding the detection efficiencies with the area of the $3,000 \text{ km}^2$ ground array projected onto the direction perpendicular to the arrival direction of the neutrino. In the down-going detection mode,

Directional exposure to Earth-skimming neutrinos at 10¹⁸ eV

Figure 3. Directional exposure of the Pierre Auger Observatory in Galactic coordinates to neutrinos at 10¹⁸ eV. *Top*: Down-going channel, sensitive to all favors. *Bottom*: Earth-skimming channel, sensitive to v_{τ} flavor only.

the directional exposure in equatorial coordinates reads as

$$
\mathcal{E}_{\nu}^{\text{DG}}(E,\delta) = \iiint dX d\mathbf{x} dt \cos \theta \epsilon_{i,c}(E,\theta,\varphi,X,\mathbf{x}) \sigma_c m_p^{-1},
$$
\n(23)

where the relationships relating local angles and time to equatorial angles are implicitly used, and where the integrations run over the depth at which the neutrino interaction can take place, the detector area and the time over the search period. The detection efficiency, $\epsilon_{i,c}$, depends on neutrino flavor *i*, the type of interaction c (charged current or neutral current), neutrino energy E, zenith θ and azimuth φ angles, the point of impact of the shower core on the ground **x**, and the depth in the atmosphere X measured along the shower axis at which the neutrino is forced to interact in the simulations. The term $\sigma_c m_{\rm p}^{-1} dX$, with m_p the mass of a proton and σ_c the neutrino-nucleon cross-section, represents the probability of neutrino-nucleon interactions along a depth dX expressed in $g \text{ cm}^{-2}$. The result is illustrated in the top panel of Fig. 3 at $E = 10^{18}$ eV in Galactic coordinates. The zero-exposure region in the Northern hemisphere refects the absence of sensitivity to showers beyond 90° in zenith angle given the Earth latitude of $\simeq -39.25^\circ$ of the Observatory, while that in the Southern hemisphere refects the minimum zenith angle of the analysis (75◦ here). In the bottom panel, the directional exposure is shown in the case of the Earth-skimming detection mode. In that case, the calculation is more involved. The efficiency ϵ_{ES} depends on the energy of the emerging τ leptons E_{τ} , the position of the signal pattern on the ground, the zenith and azimuth angles, and the altitude h_{dec} of the decay point of the τ above ground. ϵ_{ES} is averaged over the decay channels of the τ with their corresponding branching ratios and is subsequently folded with the projected area of the detector, with the diferential probability $p_{\text{exit}}(E, \theta, E_{\tau}) = dp_{\text{exit}}/dE_{\tau}$ of a τ emerging from the Earth with energy E_{τ} , as well as with the differential probability $p_{\text{dec}}(E_{\tau}, \theta, h_{\text{dec}}) = dp_{\text{dec}}/dh_{\text{dec}}$ that the τ decays at an altitude h_{dec} . The directional exposure is then

$$
\mathcal{E}_{\nu_{\tau}}^{\text{ES}}(E,\delta) = \iiint dx dE_{\tau} dh_{\text{dec}} dt |\cos \theta| \epsilon_{\text{ES}} p_{\text{exit}} p_{\text{dec}}.
$$
 (24)

The sky map shown in Fig. 3 (bottom panel) reflects that in local coordinates, the integrand of Eqn. 24 is non-zero in a narrow zenithal range of a few degrees only just below the horizon.

Table I. Upper limits on the number of photon candidates for each energy threshold.

$E(10^{18} \text{ eV})$	$n_{\gamma}(E)$
0.05	2.44
0.08	2.44
0.12	2.44
0.20	2.44
0.30	2.44
0.50	2.44
1.00	23.38
2.00	9.53
3.00	3.43
5.00	2.59
10.0	24.00
20.0	4.36
40.0	2.44

In the case of photons, the directional exposure is obtained through the time and area integration of the detection efficiency ϵ_{γ} and selection efficiency κ_{γ} projected onto the direction perpendicular to the arrival direction of the photon,

$$
\mathcal{E}_{\gamma}(E,\delta,\alpha) = \iint \mathrm{d}\mathbf{x} \mathrm{d}t \cos \theta \epsilon_{\gamma}(E,\theta,\mathbf{x},t) \kappa_{\gamma}(E,\theta). \tag{25}
$$

Four diferent analyses, difering in the detector used, have been developed to cover the wide energy range probed at the Observatory. In particular, two of these analyses beneft from a direct estimate of the depth of shower maximum by the fuorescence detector as one of the discriminating variables. The use of the fuorescence-detector datasets introduces for these analyses an explicit dependence in time for ϵ_{γ} due to the limited duty cycle on moonless nights that propagates into a small dependence in right ascension α for \mathcal{E}_{γ} . In addition to the detection efficiency, the κ_{γ} factor accounts for the dependencies of the selection process aimed at separating hadronicinduced showers from photon-induced ones. By contrast to the neutrino case, searches for photons are not backgroundfree and, for some of the energy thresholds explored, there is an irreducible small number of charged cosmic-ray events that resemble photon events despite the selection process. The values used for $n_{\gamma}(E)$ result from the upper limits on the number of candidates accounting for this irreducible background; they are listed in Table I. For illustration, we show in Fig. 4 an example of directional exposure to photons at 10^{17} eV (top panel) and at 10^{19} eV (bottom panel). The former is built on the 1.14 km^2 array with a separation of detectors of 433 m optimized to study the range of energies around 10^{17} eV, while the latter on the $3,000 \text{ km}^2$ one, optimized for higher energies. This explains the large increase of exposure observed at high energies.

Figure 4. Directional exposure of the Pierre Auger Observatory in Galactic coordinates to photons at 10^{17} eV (*top*) and $10^{19.5}$ eV (*bottom*).