The Intrinsic Alignment of Red Galaxies in DES Y1 redMaPPer Galaxy Clusters

C. Zhou,¹ A. Tong,¹ M. A. Troxel,¹ J. Blazek,² C. Lin,¹ D. Bacon,³ L. Bleem,⁴ C. Sánchez,¹⁵ C. Chang,^{5,6} M. Costanzi,^{7,8,9} J. DeRose,¹⁰ J. P. Dietrich,¹¹ A. Drlica-Wagner,^{5,12,6} D. Gruen,¹¹ R. A. Gruendl,^{13,14} B. Hoyle,¹¹ M. Jarvis,¹⁵ N. MacCrann,¹⁶ B. Mawdsley,³ T. McClintock,¹⁷ P. Melchior,¹⁸ J. Prat,^{5,6} A. Pujol,^{19,20} E. Rozo,¹⁷ E. S. Rykoff,^{21,22} S. Samuroff,² C. Sánchez,¹⁵ I. Sevilla-Noarbe,²⁸ E. Sheldon,²³ T. Shin,²⁴ D. L. Tucker,¹² T. N. Varga,^{30,31,32} B. Yanny,¹² Y. Zhang,³³ J. Zuntz,²⁹ O. Alves,³⁴ A. Amon,^{35,36} E. Bertin,^{37,38} D. Brooks,³⁹ D. L. Burke,^{21,22} M. Carrasco Kind,^{13,14} L. N. da Costa,²⁶ T. M. Davis,⁴⁰ J. De Vicente,²⁸ S. Desai,⁴¹ H. T. Diehl,¹² P. Doel,³⁹ S. Everett,⁴² I. Ferrero,⁴³ B. Flaugher,¹² J. Frieman,^{12,6} D. W. Gerdes,^{33,34} G. Gutierrez,¹² S. R. Hinton,⁴⁰ D. L. Hollowood,⁴⁴ K. Honscheid,^{45,46} D. J. James,⁴⁷ T. Jeltema,⁴⁴ K. Kuehn,^{48,49} O. Lahav,³⁹ M. Lima,^{50,26} J. L. Marshall,⁵¹ J. Mena-Fernández,²⁸ F. Menanteau,^{13,14} R. Miquel,^{52,53} A. Palmese,⁵⁴ F. Paz-Chinchón,^{13,35} A. Pieres,^{26,55} A. A. Plazas Malagón,¹⁸ A. Porredon,^{45,46,29} M. Raveri,⁵⁶ A. K. Romer,⁵⁷ E. Sanchez,²⁸ M. Smith,⁵⁸ M. Soares-Santos,³⁴ E. Suchyta,⁵⁹ M. E. C. Swanson,⁶⁰ G. Tarle,³⁴ C. To,⁴⁵ N. Weaverdyck,^{34,10} J. Weller,^{31,32} and P. Wiseman⁵⁸

(DES Collaboration)

ABSTRACT

Accepted XXX. Received YYY; in original form ZZZ

Clusters of galaxies are an important cosmological probe, sensitive to the most significant and nonlinear peaks in the cosmic density field. The weak gravitational lensing of background galaxies by foreground clusters can allow us to infer the mass of galaxy clusters. However, galaxies associated with the strong, local tidal field of the cluster can also be intrinsically aligned due to the local tidal gradient, potentially contaminating any cosmology derived from the lensing signal. We measure this intrinsic alignment in Dark Energy Survey (DES) Year 1 REDMAPPER clusters. We find evidence of a non-zero mean radial alignment of red-sequence galaxies within clusters between redshifts 0.1 and 0.7. We have also identified a significant systematic in the measured ellipticities of cluster satellite galaxies that we attribute to the extended flux profile of the central galaxy flux and other intracluster light near the center of clusters. We can correct this signal by measuring it with overlapping foreground galaxies that are not physically associated with the cluster. After correction, we attempt to fit a simple model for intrinsic alignment amplitude $(A_{\rm IA})$ to the measurement, finding $A_{\rm IA} = 0.15 \pm 0.04$, when excluding data near the edge of the cluster. We are also able to place constraints on the evolution of the alignment of the central and satellite galaxies with cluster redshift, richness, and central galaxy absolute magnitude, finding a significantly stronger alignment of the central galaxy with the cluster dark matter halo at low redshift and with higher richness and central galaxy absolute magnitude (proxies for cluster mass). This is an important demonstration of the ability of large photometric data sets like DES to provide direct constraints on the intrinsic alignment of galaxies within clusters. These measurements can inform improvements to small-scale modeling and simulation of the intrinsic alignment of galaxies to help improve the separation of the intrinsic alignment signal in weak lensing studies.

11

Key words: cosmology: observations – gravitational lensing: weak – galaxies: clusters: general

1 INTRODUCTION

In 1919, predictions from the theory of general relativity were confirmed by observing the deflection of the light by the sun (Dyson et al. 1920), which is aptly named gravitational lensing. A century after this experiment, gravitational lensing has become one of the most powerful probes in modern cosmology surveys. Weak lensing probes including galaxy-galaxy lensing, cluster lensing, and cosmic shear can effectively constrain cosmological parameters and thus reveal the growth history of structure in the universe. The recent growth in data volume from Stage III surveys such as the Dark Energy Survey (DES),¹ the Kilo-Degree Survey,² and the Hyper Suprime-Cam Survey³ has significantly lowered the statistical uncertainty in the lensing signal. This has in turn made control of small systematic

- 1 https://www.darkenergysurvey.org
- ² https://kids.strw.leidenuniv.nl
- ³ https://hsc.mtk.nao.ac.jp/ssp/

errors critical for extracting weak lensing signals from existing and 73 14 future surveys. 15 74

One major source of systematic uncertainty in weak lensing studies 75 16 is from the correlated intrinsic alignment of galaxies that contam-17 inate the shear correlations (Troxel & Ishak 2014). The intrinsic 18 alignment of galaxies is caused by a variety of physical processes 19 during structure formation Heavens et al. (2000); Croft & Metzler 20 (2000); Hirata & Seljak (2004); Bridle & King (2007); Blazek et al. 21 (2019), leading to a tendency for galaxies to physically align along 22 the gradient of the tidal field. The intrinsic alignment of galaxies 23 acts as a nuisance signal to the lensing measurement, which tends to 83 24 distort the observed shape of a galaxy tangentially to the gradient of ⁸⁴ 25 the tidal field, and it can strongly bias the weak lensing results we 26 infer (e.g., Blazek et al. (2019); Hamana et al. (2020); Asgari et al. 27 (2021); Krause et al. (2021); DES Collaboration et al. (2022)) if it 28 is improperly corrected or modeled. Isolating the intrinsic alignment 29 signal can not only improve the results we get from lensing surveys, 87 30 but also provides insights into the evolution of galaxies over time (e.g. 88 31 mergers), which would also modify the intrinsic alignment signal. 32

```
The alignment of galaxies in large-scale tidal fields has been well
33
    studied and especially for large and red galaxies, there is a consen-
34
    sus in both measurements and simulations that a non-zero alignment
35
    exists (e.g., Mandelbaum et al. (2006); Hirata et al. (2007); Joachimi
36
    et al. (2011, 2013); Chisari et al. (2015); Singh et al. (2015); Tenneti
37
                                                                            95
    et al. (2016); Samuroff et al. (2019); Fortuna et al. (2021b); Samuroff
38
                                                                            96
    et al. (2021a); Zjupa et al. (2020)). Ignoring destructive interference
39
                                                                           07
40
    via interaction or merging of galaxies and clusters, one naively ex-
    pects that the intrinsic galaxy alignment would be stronger around
41
    the strongest over-densities in the universe like galaxy clusters. There _{100}
42
    is more disagreement about the amplitude of the alignment of galax-
43
    ies within such large structures, i.e., intracluster alignments (e.g., _{102}
44
    Pereira & Kuhn (2005); Agustsson & Brainerd (2006); Faltenbacher
45
                                                                           103
    et al. (2007); Siverd et al. (2009); Hao et al. (2011); Schneider et al.
46
    (2013): Sifón et al. (2015)) with different shape measurement meth-
47
    ods leading to different conclusions. A measurement of the alignment 104
48
    of REDMAPPER clusters in the Sloan Digital Sky Survey (SDSS) data
49
    with the large-scale matter field was also performed by van Uitert &
50
```

The substantially increased physical volume (and thus the number 108 52 of clusters) probed in data sets like the Dark Energy Survey Year 1¹⁰⁹ 53 data enable an extremely powerful test of this question of intracluster ¹¹⁰ 54 alignment. In this work, we study a variety of alignment mechanisms 111 55 for red-sequence galaxies within DES Year 1 REDMAPPER clusters. ¹¹² 56 This follows an earlier work studying REDMAPPER clusters in the ¹¹³ 57 Sloan Digital Sky Survey (SDSS) data (Huang et al. 2016, 2017). ¹¹⁴ 58 We examine a similar set of alignment statistics as this earlier work, 115 59 comparing the METACALIBRATION and IM3SHAPE weak lensing shape ¹¹⁶ 60 measurement algorithms used in DES Year 1 for cosmology. In par-117 61 ticular, we are able to measure a significant non-zero signal in the ¹¹⁸ 62 metric most of interest to cosmology, the mean tangential (radial) ¹¹⁹ 63 shear. These measurements demonstrate that current and future large 120 64 photometric surveys are able to provide significant constraints on 121 65 these local alignment processes. 122 66

The paper is organized as follows. In Sec. 2 we discuss the DES 124 67 data used in this work, including the cluster and shape catalogs. We 125 68 describe the methodology used in Sec. 3, and the measurement results 126 69 in Sec. 4. In Sec. 5 we present a discussion of the interpretation of the 127 70 signal in terms of an intrinsic alignment model and the mass profiles 128 71 of the clusters. We conclude in Sec. 6. 72 129

Joachimi (2017).

51

2 DARK ENERGY SURVEY YEAR 1 DATA

The Dark Energy Survey is a six-year survey covering 5000 square degrees of the southern sky using the Dark Energy Camera (Flaugher et al. 2015) mounted on the Blanco 4m telescope in Cerro Tololo, Chile. Observations use five broadband filters g, r, i, z, Y. The first year of DES observations (Y1) lasted from August 2013 to February 2014 and covers ~40% of the total DES footprint (Drlica-Wagner et al. 2018). We use data based on several value-added catalogs built from the Y1 data: 1) the Y1A1 GOLD catalog, a high-quality photometric data set; 2) the red-sequence Matched-filter Probabilistic Percolation (REDMAPPER) cluster and member catalogs; 3) the METACALIBRATION and IM3SHAPE shape catalogs. We describe each of these in more detail in the following subsections.

2.1 GOLD Catalog

76

82

89

106

107

The Y1A1 GOLD data set (Drlica-Wagner et al. 2018) is a highquality photometric catalog that contains multi-epoch, multi-object photometric model parameters, and other ancillary information. The objects in this catalog are selected from the initial Y1A1 coadd detection catalog, which is processed by the DESDM image processing pipeline (Sevilla et al. 2011; Mohr et al. 2008, 2012). The Y1A1 GOLD catalog restricts the footprint of the objects to regions with at least one image of sufficient science quality in each filter. Several bad region masks including unphysical colors, the Large Magellanic Cloud, globular clusters, and bright stars are applied to the catalog. The final Y1A1 GOLD footprint covers ~1800 deg² with an average of three to four single-epoch images per band. The photometric accuracy is $\leq 2\%$ over the survey area. A comparison with the deeper catalog of the Canada-France-Hawaii Telescope Lensing Survey shows that the Y1A1 GOLD catalog is > 99% complete in g, r, i, z bands for magnitudes brighter than 21.5. There are approx. 137 million objects in the final Y1A1 GOLD catalog.

2.2 **REDMAPPER cluster catalog**

Matched-filter Probabilistic The red-sequence Percolation (REDMAPPER) photometric cluster finding algorithm is optimized for deep-field photometric cosmology surveys (Rykoff et al. 2014) and produces a cluster catalog identifying overdensities of red-sequence galaxies with a probabilistic assignment of these red-sequence galaxies as central/satellite members. This alogorithm has been validated using X-ray and Sunyaev-Zel'dovich (SZ) observations (Rozo et al. 2015; Saro et al. 2015; Rozo et al. 2016; Sadibekova et al. 2014; Bleem et al. 2020a; Grandis et al. 2021), and updates to the method are described in Rozo et al. (2016); Rykoff et al. (2016); McClintock et al. (2019). We briefly describe the algorithm and resulting cluster catalog below.

To identify clusters, the REDMAPPER algorithm counts the excess number of red-sequence galaxies, called the richness (λ) , within a radius $R_{\lambda} = 1.0h^{-1} \text{Mpc}(\lambda/100)^{0.2}$ that are brighter than some luminosity threshold $L_{\min}(z)$. A locally volume-limited version of the catalog is also produced, which imposes a maximum redshift on clusters such that galaxies above $L_{\min}(z)$ can be detected at 10σ . An associated redshift-dependent random catalog for both cluster catalogs is produced using a survey mask constructed to require that a cluster at redshift z at each point in the mask be masked by at most 20% by the associated galaxy footprint mask.

The algorithm centers each cluster on the most likely central galaxy, based on an iteratively-trained filter relying on galaxy brightness, cluster richness, and local density to determine the central



Figure 1. The redshift distribution of REDMAPPER cluster members used in 186 this work.

candidate probability. Each red-sequence cluster member is also as-130 190 signed an associated membership probability, which we weigh all 131 measurements by. Additional information about the quality of photo-132 metric redshifts of the clusters and cluster members can be found in 193 133 McClintock et al. (2019); Elvin-Poole et al. (2018), but over most of 194 134 the redshift range used in this paper cluster redshifts are unbiased at 135 the level of $|\Delta z| \leq 0.003$ with a median photometric redshift scatter 136 of $\sigma_z/(1+z) \approx 0.006$. For red-sequence cluster members, this is 197 137 $\sigma_z/(1+z) \approx 0.035.$ 138 198

In this work, we use a total of 7066 clusters from the DES Y1 139 199 REDMAPPER catalog (4322 in the volume-limited catalog). Within $_{200}$ 140 these clusters, there are an effective number of 399002 (105029) clus-141 ter members (central/satellite galaxies). We have performed measure-142 ments both using all clusters and only the volume-limited sample. 143 The full catalog allows us to probe a larger redshift range with higher 2011 144 statistical precision, while the volume-limited sample matches what 2002 145 has been used for cosmological inference in DES Collaboration et al. 146 (2020a). We will show results primarily from the volume-limited ²⁰³ 147 sample unless otherwise noted for cases where results are not qual-204 148 itatively similar, and using the same $\lambda > 20$ selection on richness ²⁰⁵ 149 in either case as DES Collaboration et al. (2020a), since inference 206 150 of the halo shape based on the distribution of satellite galaxies is 207 151 increasingly difficult as the number of satellite galaxies decreases. 208 152 The redshift distributions of the final samples of clusters are shown 153 in Fig. 1. 154

155 2.3 Shape Catalogs

We use a fiducial shape catalog that is calibrated with the METACALI- 211 156 BRATION method, which uses available imaging data directly without 212 157 the need for significant prior information as a function of galaxy 213 158 properties (Huff & Mandelbaum 2017; Sheldon & Huff 2017). The 214 159 METACALIBRATION implementation used in DES Y1 was described in 215 160 detail in Zuntz et al. (2018). Limitations in the DES Y1 implemen- 216 161 tation of METACALIBRATION lead to a residual mean multiplicative 217 162 shear bias estimate of $m = 0.012 \pm 0.013$, which is due primarily to 218 163 the effects of neighboring light on the shear recovery. This mean cor- 219 164 rection is applied to the measurements in this work. For IM3SHAPE, 220 165 we divide the mean shear signal by the mean of 1 + m, where m is 221 166

167

168

169

170 171

172

173

174

175

176

177

178

179

180

181

182

183

184

185

188

189

209

210

the calibration factor inferred from simulations, and for METACAL-IBRATION, we divide the mean shear signal by the mean value of $\frac{1}{2}(1+m)(\mathbf{R}_{11}+\mathbf{R}_{22})$, where *m* is the shear bias estimate above and *R* the response inferred from the METACALIBRATION process.

METACALIBRATION also allows us to account for sample selection bias effects, as described in Zuntz et al. (2018); Troxel et al. (2018), which we also include. However, we match the shape catalog to the REDMAPPER central/satellite member catalog, which introduces an additional selection that we cannot incorporate in the selection bias correction. In future work, it would be valuable to explore the impact of this selection by running the REDMAPPER selection algorithm on the photometry produced in the METACALIBRATION process similar to how we incorporate redshift selection biases in, e.g., Troxel et al. (2018). This has been measured, for example, for a generic red galaxy selection used for intrinsic alignment studies in Samuroff et al. (2019). At the current precision of the measurements in this paper, however, we expect this additional correction to be safely negligible. The METACALIBRATION catalog yields a total of 35 million objects, 262867 of which are matched to the REDMAPPER central/satellite members and used in the selection for the current analysis. We are able to match a METACALIBRATION shape measurement to 66% of **REDMAPPER** members.

We also compare measurements using the IM3SHAPE shape catalog Zuntz et al. (2018, 2013), which utilizes a simulation-based calibration and only has secure shape measurements for 39% of REDMAPPER members. This low fraction of cluster members with secure shapes for IM3SHAPE gives too low a signal-to-noise for the two-point correlation function measurements presented later in Sec. 4.4 to be useful, but it is compared to METACALIBRATION in other measurements. The IM3SHAPE catalog provides a model fit for either a bulge- or disk-like profile. We find about 80% of central galaxies better fit by a de Vaucouleurs (bulge) profile vs exponential (disk) profile, while for satellites, about 60% are better fit by an exponential profile.

3 METHODS TO INFER THE INTRINSIC ALIGNMENT OF GALAXIES IN CLUSTERS

The intrinsic alignment of galaxies in the (quasi-)linear regime is typically expressed via perturbation theory as a function of the underlying tidal field. Most cosmological studies have used a linear alignment model (Hirata & Seljak 2004; Bridle & King 2007) that uses the first-order expansion of the intrinsic shear γ^{I} (shown here up to second-order) in the linear density field:

$$\gamma^{I}(\boldsymbol{x}) = C_{1}s_{ij} + C_{2}\left(s_{ik}s_{kj} - \frac{1}{3}\delta_{ij}s^{2}\right) + C_{1\delta}(\delta s_{ij}) + C_{t}t_{ij} + \cdots,$$
(1)

where each field is evaluated at \boldsymbol{x} and summation occurs over repeated indices. The C_i parameters are then the analog to galaxy bias parameters in perturbation theory, and δ_{ij} is the Kronecker delta, δ is the density field, $s_{ij}(\boldsymbol{k}) \equiv \hat{S}_{ij}[\delta(k)]$ is the normalized Fourierspace tidal tensor, $s^2(\boldsymbol{k})$ is the tidal tensor squared, and the tensor $t_{ij} = \hat{S}_{ij}[\theta - \delta]$ involves the velocity shear. From this, one can build up all standard components of commonly used intrinsic alignment models up to second order in the density field, as described in detail in Blazek et al. (2019).

When modeling the intrinsic alignment of galaxies in strongly nonlinear environments like galaxy clusters, where perturbative models will break down, it has been proposed to use a '1-halo' model in analogy to the halo model for the matter power spectrum to describe

4 Zhou & Tong et al.

alignments internal to a single cluster halo. This has been discussed 222 by Schneider & Bridle (2010); Fortuna et al. (2021a), which outlines 223 approaches for building such a model, including tests on simula-224 tions. Previous attempts to directly measure such a signal, e.g. within 225 226 galaxy clusters, have had mixed results both in simulations and data. These fall into two categories: 1) the alignment of the cluster shape 227 with the tidal field and 2) the alignment of satellite galaxies, using 228 the cluster centers as a proxy for the peaks of the local tidal field. 229

Better measurements of the 1-halo intrinsic alignment signal are 230 231 necessary to inform and constrain such a beyond-perturbative model, however, which is the goal of this paper. While most measurement 232 attempts have focused on objects with spectroscopic redshifts, which 233 suffer from limited data volumes, we present several complementary 234 measurements of these alignments using a fully photometric galaxy 235 cluster and satellite catalog that selects red-sequence galaxies and 236 spans over 1000 deg^2 to redshift 0.7. 237

238 3.1 Orientation of the satellite galaxy distribution

We quantify the strength of the central galaxy alignment relative to 239 the orientation of the cluster satellite distribution as a proxy for the 240 dark matter halo orientation in two ways, which were also used in 241 SDSS for REDMAPPER clusters by Huang et al. (2016). First, we use 242 the position angle difference $\Delta \eta$ between the central galaxy and its 243 host cluster, and second, the central galaxy alignment angle θ_{cen} for 244 each central-satellite pair. They are both defined to lie in the range 245 $[0^{\circ}, 90^{\circ}]$, with values closer to 0° indicating stronger central galaxy 246 alignment. 247

²⁴⁸ Measuring $\Delta \eta$ requires an approximation of the overall cluster ²⁴⁹ shape from the distribution of satellite galaxies. We use 2 different ²⁵⁰ methods to determine the ellipticity and orientation of the cluster in ²⁵¹ order to measure $\Delta \eta$.

252 3.1.1 Method 1: Second moments

We follow the method used by Huang et al. (2016) to calculate the cluster ellipticity and position angle of the satellite galaxies with respect to the central galaxy. We use all satellite galaxies with $p_{\text{mem}} \ge 0.2^4$ in order to reasonably trace the shape of the cluster. We first calculate the reduced second moments of the positions of all remaining satellite galaxies in the cluster:

$$M_{xx} \equiv \frac{\sum_{i} p_{i,\text{mem}} \frac{x_{i}^{2}}{r_{i}^{2}}}{\sum_{i} p_{i,\text{mem}}}$$
(2)
$$M_{xy} \equiv \frac{\sum_{i} p_{i,\text{mem}} \frac{x_{i} y_{i}}{r_{i}^{2}}}{\sum_{i} p_{i,\text{mem}}}$$
(3)

$$M_{yy} \equiv \frac{\sum_{i} p_{i,\text{mem}}}{\sum_{i} p_{i,\text{mem}}} \qquad (4)$$

where x_i and y_i are the distances of satellite galaxy *i* from the central ²⁵⁹ galaxy in RA and Dec, respectively, and r_i is the Cartesian distance from satellite galaxy *i* to the central galaxy. We then use the Stokes parameters to define the cluster shape as follows: ²⁶⁰ ²⁶¹ ²⁶²

$$(Q,U) = \frac{1 - b^2/a^2}{1 + b^2/a^2} (\cos 2\beta, \sin 2\beta) = (M_{xx} - M_{yy}, 2M_{xy}) \quad (5)_{264}^{263}$$

 4 The choice of minimum $p_{\rm mem}$ is arbitrary, and has very little impact on 267 our results. 268



Figure 2. *Top*: Measured quantities relevant to the orientation of the central galaxy within the dark matter halo of the cluster. $\Delta \eta$ is the position angle difference between the central galaxy and the cluster halo. θ_{cen} is the alignment angle of the line connecting the central galaxy and each satellite galaxy relative to the central galaxy position angle. *Bottom*: Measured quantities relevant to the orientation of the satellite galaxies within the dark matter halo of the cluster. ϕ_{sat} is the alignment angle of the line connecting the central galaxy position angle. *Bottom*: Measured quantities relevant to the orientation of the satellite galaxies within the dark matter halo of the cluster. ϕ_{sat} is the alignment angle of the line connecting the central galaxy and each satellite galaxy relative to the satellite galaxy position angle.

where b/a is the cluster minor-to-major axis ratio and β is the cluster position angle (PA).

3.1.2 Method 2: Quadrant grid

266

Our second method for measuring cluster shapes is based on the assumption that satellite projections are distributed isotropically along a profile of 2D ellipses around the central galaxy. We place a set of orthogonal axes on the central galaxy in the plane of the sky, rotated at different angles θ relative to the central galaxy position angle, and sum the p_{mem} for all satellites in each quadrant (q).

We define the count difference in cross-pair quadrants as $m = q_1 + q_3 - q_2 - q_4$, which we can model as a function of θ . The assumption of a 2D ellipse leads to the following expression for



Figure 3. An example REDMAPPER identified cluster at z = 0.41. Overlaid in ²⁹² red is the shape of the cluster fit by Method 2. This cluster was found to have ²⁹³ e = 0.73, with a position angle 48° east-of-north and REDMAPPER radius ²⁹⁴ 0.746 Mpc. Member galaxies are identified in cyan squares to differentiate ²⁹⁵ from other projected galaxies along the line-of-sight. The brightest central ²⁹⁶ galaxy is the solid red square in the center. The model is constrained to be ²⁹⁷ centered on the REDMAPPER-identified central galaxy.



Figure 4. The jackknife correlation matrix for the full-sample $\gamma_T(R)$ measurement, discussed in Secs. 3.2 & 4.4. As expected for shot or shape noise, the covariance is strongly diagonal.

269 $m(\theta)$:

$$m(\theta) = \frac{N}{2\pi} \left[\arctan\left(\frac{\tan(\beta - \theta)}{r}\right) + 2 \arctan\left(\frac{\cot(\beta - \theta)}{r}\right) \right] \quad (6)^{317}$$

where *N* is the effective number of satellites in the cluster, β is the cluster position angle, and *r* is the minor-to-major axis ratio b/a. We fit this model to the count difference data as a function of θ assuming Poisson uncertainty and find the best-fit parameters β and *r*, which ³¹⁹ together completely describe the shape of the cluster. An example ³²⁰ cluster with the best-fit shape model over-plotted is shown in Fig. 3. ³²¹

276 3.2 Radial alignment of satellite galaxies with the cluster center

277 The tendency of satellite galaxies to align radially with their major

axis pointed toward the central galaxy is another measure of the in-

fluence of the cluster's tidal field on the orientation of galaxies within its dark matter halo. While the mechanism for this alignment, e.g., whether it is achieved over time or during the galaxies' formation, is not clear, we can place empirical constraints on this alignment at the time we observe the cluster. We can then study the evolution of the mean alignment over time at different redshifts.

One way to parameterize this alignment is similar to the observables described in the preceding section, which we will label ϕ_{sat} following Huang et al. (2017). This is the angle between the position angle of the satellite galaxy and the line connecting it to the central galaxy. This is shown in Fig. 2.

Another standard method is calculating the mean radial shape $\gamma_T(R)$

$$\gamma_T(R) = \frac{\sum_i p_{i,\text{mem}} e_{i,+}}{\sum_i p_{i,\text{mem}}}$$
(7)

via the two-point correlation function of the central galaxy positions with the ellipticity of the satellite galaxies. *R* is the projected distance separation of the satellite from the central galaxy of the cluster, *i* is some satellite galaxy in some cluster, and e_+ is the component of the ellipticity projected along a basis coinciding with the line connecting the satellite galaxy to the central galaxy of the cluster. γ_T is most relevant for contamination to the cluster lensing signal. In practice, we use TreeCorr⁵ (Jarvis et al. 2004) to perform correlation function measurements in 10 logarithmic bins of the distance between the central galaxy and the satellite galaxies. The lower bound is arbitrary, while the upper bound is the maximum radial distance to a satellite galaxy.

3.3 Estimating the covariance of measurements

299

311

315

316

323

Lacking a robust a priori theoretical model for what the measured signals should be, we cannot construct a theoretical covariance framework. Instead, we rely on a jackknife covariance estimate, iteratively removing each cluster from the sample. The covariance is then given by

$$C_{\xi}(x) = \frac{N-1}{N} \sum_{i=1}^{N} (\xi_i - \bar{\xi})^2,$$
(8)

where *N* is the number of clusters, *i* is the cluster number, and $\xi = \sum_i \xi_i / N$, for some estimator ξ . The covariances are expected to be dominated by shot or shape noise, given the small sample sizes, so we expect the jackknife approach to be sufficiently accurate. In particular, the measurement of γ_T in Sec. 4.4, which is the most substantial result in this work, is non-zero only for very small separations, where shape noise dominates the correlation function. The covariance matrix for γ_T is shown in Fig. 4.

4 MEASURED ALIGNMENT IN DES CLUSTERS

We present the results of the measurements described in the previous section. Unless otherwise noted, we will limit results to the volumelimited REDMAPPER cluster catalog for brevity, since in most cases the results are qualitatively similar and thus conclusions drawn from the data will not differ.

⁵ https://github.com/rmjarvis/TreeCorr



Figure 5. The position angle differences $(\Delta \eta)$ between the brightest central ³⁷⁴ galaxy major axis and that of the satellite galaxy distribution for the DES Y1 ³⁷⁵ galaxy clusters, as measured by the two methods described in Sec. 3.1. *Top:* ³⁷⁶ The distribution with cluster position angle inferred from the METACALIBRA- ³⁷⁷ TION (MCAL) shape catalog. *Bottom:* The distribution with cluster position ³⁷⁸ angle inferred from the im3shape (I3S) catalog. The results are generally ³⁷⁹ consistent with each other. ³⁸⁰

Alignment of central galaxy with satellite galaxy distribution

We first compare measurements of the position angle difference $\Delta \eta$, 326 weighted by the probability of satellite galaxies being a cluster mem-327 ber $p_{\rm mem}$, using the two different methods of measuring $\Delta \eta$ and two 328 386 estimates of the galaxy shape. Figure 5 shows $\Delta \eta$ for all clusters 329 in the sample, measured by Methods 1 & 2 and by both META-330 CALIBRATION (MCAL) and im3shape (I3S). In the case of random 388 331 alignment, we would expect a flat distribution with $\langle \Delta \eta \rangle = 45^{\circ}$. All 389 332 333 four results are generally consistent and show a preference for the 390 334 alignment of the central galaxy with the overall cluster shape, with 391 $\langle \Delta \eta \rangle = 35.01 \pm 0.39^{\circ}$, significantly less than 45° . 392 335

We are also able to study the dependence of this alignment on 393 336 both cluster properties (e.g., richness and redshift) and central galaxy 394 337 properties (e.g., r-band absolute magnitude M_r and g-r color), which 395 338 is shown in Fig. 6 for the volume-limited and full cluster catalogs. We 396 339 split the clusters into tertiles in each of the four quantities, and com- 397 340 pare the $\Delta \eta$ distributions. While any possible trends in the volume- 398 341 limited catalog are very weak (at most the 1σ level), we do observe 399 342 significant trends with the full cluster catalog, which has higher sta- 400 343 tistical precision and goes to much higher redshift. We find increasing 401 344

alignment of the central galaxy with the cluster shape for both higher richness clusters and brighter absolute magnitude, as expected, since both are a proxy for cluster mass. We also find a stronger tendency to align for lower redshift clusters, and while there are significant differences in bins of color, there isn't a clear trend in alignment versus color.

These results are consistent with the weak trends seen in the volume-limited sample. The trends of $\langle \Delta \eta \rangle$ for the full sample are also qualitatively similar to Huang et al. (2016), with a slightly better agreement in the low-*z* tertile selections that better matches the redshift range of the SDSS REDMAPPER clusters studied in that paper. In Huang et al. (2016) they find $\langle \Delta \eta \rangle = 35.07 \pm 0.28^{\circ}$, while we find $\langle \Delta \eta \rangle = 35.82 \pm 0.69^{\circ}$, though still extending to higher redshift than the SDSS cluster sample.

The higher volume probed by the DES data allows us to demonstrate these significant trends across redshift and magnitude for the first time. These results are consistent with a model of the intracluster alignment coalescing as the cluster evolves (at lower redshifts) and being more strongly driven in more massive clusters (larger richness and absolute magnitude). This result would be in conflict with the often-assumed scenario of large-scale alignments of galaxies being frozen in at early times as the galaxies form, and then being disrupted over time. For instance, the typical redshift scaling of analytic IA models (e.g. Hirata & Seljak (2004); Bridle & King (2007); Blazek et al. (2019)), assumes this behavior. This result, if confirmed with future studies, would provide important insight into how red galaxies align in cluster environments, and potentially with large-scale structure more generally.

4.2 Anisotropic distribution of satellite galaxies

381

382

383

384

Previous studies, including Huang et al. (2016) of REDMAPPER clusters in SDSS, have found a tendency of satellite galaxies to align along the major axis of the central galaxy. We also observe this trend, measured as the distribution of angles θ_{cen} weighted by p_{mem} between the line connecting central and satellite galaxies with the major axis of the central galaxy. This is shown in Fig. 7, where we find $\langle \theta_{cen} \rangle = 41.45 \pm 0.13^{\circ}$. The difference in the number of satellites along the major versus minor axes (slope in Fig. 7) is much less pronounced than the difference in numbers of clusters with central galaxies aligned vs anti-aligned with the cluster major axis (slope in Fig. 5), which is also consistent with what was found in SDSS REDMAPPER clusters.

4.3 Agreement between halo orientation and galaxy distribution

We have used the distribution of satellite galaxies within clusters as a proxy for the shape of the underlying dark matter halo, which is what would drive any true intrinsic alignment of the galaxies. To justify this, we compare our cluster shape measurements inferred from the galaxy distribution with the DES Y1 weak lensing convergence 'mass' map (Chang et al. 2018) to confirm the correlation between galaxy satellite distribution and the underlying dark matter halo. The region around each cluster is cut out from the mass map, rotated, and stacked so that the inferred position angle from Sec. 4.1 is aligned for all clusters. We show this result in Fig. 8, which compares the stacked convergence with original random orientations, which has a nearly isotropic shape, with the cluster stack aligned by position angle, which has a highly anisotropic shape aligned in the direction of the inferred position angle of the stacked clusters.





Figure 6. The position angle difference for clusters split into tertiles of richness, redshift, and central galaxy r-band absolute magnitude M_r and g-r color. The fractional difference of $\Delta \eta$ with respect to the middle bin is shown. Left: Results for the volume-limited catalog. There are very weak indications of trends with the four properties, but only at the 1 σ level. *Right*: Results for the full catalog, which extends to much higher redshift. There exist highly significant trends in stronger alignment of the central galaxy with the cluster shape when going to higher richness and central galaxy brightness, which are both a proxy for cluster mass. We also find a trend of stronger alignment at lower redshift. These are consistent with the weaker trends in the volume-limited catalog. We also find significant non-monotonic differences in bins of color in the full sample. Points are offset for visibility.

80

ł



Figure 7. The distribution of the alignment of satellite galaxy positions relative to the position angle of the central galaxy of the cluster (θ_{cen}). There is a slight preference for satellite galaxies to be aligned closer to the major axis of the central galaxy.

The ellipticity inferred from the stacked convergence is e = 0.33, 402 which agrees well with that inferred from the methods discussed in 403 Sec. 4.1, e = 0.35. It is important to note that we cannot isolate solely 404 405 e.g. virially bound galaxies in this process, and it is not clear that all selected cluster members are part of a virially relaxed system (see 406 Sec. 5). Thus some part of this ellipticity may be incorporating the 407 largest connected filamentary structures near the cluster node in the 408 dark matter distribution. 100

We also show in Fig. 8 the stacked convergence of clusters oriented 410 by the BCG major axis (see also, for example, Shin et al. (2018); 411 Okabe et al. (2020); Herbonnet et al. (2022)). We find this produces 412 a less elliptical stacked signal (e = 0.20) than orienting by the cluster 413 satellite galaxy distribution in the halo. This may be related to the 414 cluster satellite galaxy distribution also containing information about 415 connecting filaments, but a full understanding of this should be left 416 to a more detailed future study. 417

418 4.4 Radial alignment of satellite galaxies

In addition to the alignment of the central galaxy with the dark matter 419 halo of the cluster, satellite galaxies may also be influenced by the 420 local tidal field, causing a radial alignment of their major axes toward 421 the BCG. We find no evidence for a non-flat distribution, with mean 422 $\phi_{\text{sat}} = 44.9 \pm 0.8^{\circ}$, indicating no statistically significant mean radial 423 alignment of objects between 0° and 90° within the cluster averaged 424 425 over all distances from the center. This measurement is weighted to the outer radii of the cluster, where there are more satellite galaxies 426 and could swamp any signal closer to the center of the cluster, where 427 we expect it to exist more strongly due to the cluster halo itself. 428

We also measure the mean radial shape two-point correlation func-429 tion of REDMAPPER cluster members as a function of distance from 437 430 the cluster center $-\gamma_T(R)$, which is shown in Figs. 9 & 10, with dis- 438 431 tance from the center of the cluster both as a fraction of the cluster 439 432 size (R_{λ}) and in absolute units, respectively. We find a highly sig- 440 433 nificant radial alignment signal within about $0.1R_{\lambda}$ (or 0.1 Mpc/h) 441 434 of the cluster centers, with a total signal-to-noise S/N = 18 "Origi- 442 435 nal" in Fig. 9). In our measurements of $\gamma_T(R)$, we apply a "member 443 436



Figure 8. The stacked convergence map centered on the positions of clusters. *Top*: The stacked convergence for clusters with their original orientation on the sky. *Center*: The stacked convergence for clusters rotated with the position angle inferred from the satellite galaxy distribution oriented vertically. *Bottom*: The stacked convergence for clusters rotated with the position angle inferred from the central galaxy major axis.

boost" factor to account for the expected (weighted) fraction of cluster members in the sample that are actually foreground/background objects and thus do not contribute to the IA signal. We calculate this factor using the REDMAPPER membership probabilities p_{mem} : $B_m = \sum_i p_{mem,i} / \sum_i p_{mem,i}^2$. These probabilities are also used to weight each galaxy in the correlation function estimator,. This member boost is analogous to the boost factor typically applied to galaxygalaxy or cluster-galaxy lensing measurements to account for dilutionfrom sources physically associated with the lens.

To test the robustness of this measurement, we also show the result 446 of the $\gamma_{\times}(R)$ cross-component measurement, which is consistent 447 448 with zero, in Fig. 11. We also repeat the γ_T measurement for a sample of galaxies not physically associated with the cluster, but projected in 449 the same line of sight in front of the cluster. This should produce no 450 physical signal, as those galaxies are not affected by the potential of 451 the cluster, yet we find a sharp transition to a significant mean radial 452 alignment within about $0.05R_{\lambda}$ of the cluster center. Previously, 453 Zhang et al. (2019b) identified an intracluster light profile within 454 DES REDMAPPER clusters that is the most plausible cause of this 455 alignment of physically distant galaxies. The scale of this alignment 456 agrees fairly well with the inner-most profile model component they 457 fit, which may in fact be associated with the edge of the central galaxy 458 profile. 459

Since we can measure this contamination, and if this is the true 460 cause it should be roughly redshift independent at the precision we 461 are currently probing, we can correct the measured alignment signal 462 463 for the cluster satellite galaxies by subtracting this foreground signal, which is shown in Fig. 9 in blue. The new covariance for the measure-464 ment takes into account the uncertainties from both measurements. 465 All two-point correlation function results will be corrected by this 466 foreground signal. The final radial alignment signal we measure in 467 Figs. 9 & 10 is substantially stronger in amplitude and signal-to-noise 468 than found for the full satellite population with SDSS REDMAPPER 469 clusters in Huang et al. (2016), with a total signal-to-noise of ~ 6 . 470

Given the signal-to-noise of the measurement, we can attempt to 471 look for the evolution of the signal over redshift, shown in Fig. 12. 472 We find that the measured foreground alignment due to intracluster 473 474 light is consistent with being unchanged as a function of redshift and richness, so we correct measurements in bins of redshift or richness 475 by the foreground signal for the full cluster population, which has 476 smaller uncertainty. Given recent potential richness-dependent sys-477 tematics in optical cluster studies (DES Collaboration et al. 2020b), 478 we also consider the richness dependence of the measurement, which 479 is shown in Fig. 13. We find that the radial intrinsic alignment signal 480 has no richness dependence. However, the radial intrinsic alignment 481 signal from the satellites we observe within $0.1R_{\lambda}$ of the center of 482 the clusters does have a small indication of redshift dependence, 483 significant at approximately the 1σ level for the lowest redshift bin. 484

485 4.5 Impact of measured radial alignment within clusters on 486 cosmology

487 Given the presence of a non-zero radial alignment signal within REDMAPPER clusters, it is useful to consider if this signal could leak 488 into estimates of mean tangential shear like γ_t or $\Delta\Sigma$. In the clus-489 ter lensing measurements in McClintock et al. (2018), cosmology 490 is inferred from measurements only at (relative to this study) large 491 492 scales above 200 kpc, where the alignment signal is small. A buffer in source photometric redshift of 0.1 was also used to remove any 504 493 sources within z = 0.1 of the cluster to minimize these effects. How- 505 494 ever, due to the uncertainty in source redshifts, this leaves a non-zero 506 495 fraction of cluster members as part of the source catalog. To test any 496 impact of radial alignment leakage, we explicitly remove all clus-497 ter members from the source catalog and repeat the measurements 498 in the same bins of richness and redshift from McClintock et al. 499 (2018). We find that the impact is much smaller than the uncertainty 508 500 on the measurement expected even for DES Year 6, indicating this 509 501 intracluster intrinsic alignment can play no role in systematics of the 510 502 cluster lensing signal used for cosmological inference. This is due 511 503



Figure 9. The two-point correlation function γ_T , measuring the mean tangential shape as a function of relative satellite distance from the center of the cluster (negative values indicate radial alignment). The open points are measurements without subtracting the foreground radial alignment signal that we identify as being due to intracluster light impacting the ellipticity measurements of galaxies projected near the center of the cluster. and the solid points are the measurements after subtracting this systematic signal. Within ~0.1 R_{λ} , there is a significant radial intrinsic alignment signal. The intrinsic alignment signal is consistent with zero on scales larger than ~0.1 R_{λ} .



Figure 10. The measured γ_T signal, corrected for the impact of intracluster light on the ellipticity measurements, in bins of absolute separation. This is compared to the NFW tidal alignment model prediction with $A_{IA} = 0.15$ (red) and $A_{IA} = -0.037$ (dark blue), as well as model (light blue) with both NFW tidal alignment with $A_{IA} = 0.06$ and lensing contamination, as described in the text.

partly to the small fraction of contaminated galaxies and the signal being present most strongly only on scales smaller than those used in the cluster lensing analyses.

5 MODELING

Analytic models of intrinsic alignments typically relate the galaxy shapes to the local tidal field, often in regimes where perturbative approaches are valid (e.g. Hirata & Seljak (2004); Blazek et al. (2015, 2019). To describe the measured IA signal within REDMAPPER clus-



Figure 11. Tests of potential systematic contributions to the measured γ_T in Fig. 9. The orange dots are the cross-component γ_{\times} using cluster members. The blue dots are the γ_T signal measured using foreground galaxies around cluster centers. The cross-component should be consistent with zero at the statistical precision of this measurement, and we find that it is. Similarly, since ⁵²² the foreground galaxies are physically disassociated with the local tidal field ⁵²³ of the clusters and do not experience lensing due to the clusters, there should ⁵²⁴ also be no physical signal here. We do find evidence of correlation within ⁵²⁵ ~0.05 R_{λ} , which is most likely due to intracluster light near the center of the ⁵²⁶ cluster biasing the shape measurement of overlapping galaxies on the sky. ⁵²⁷



Figure 12. The measured mean radial alignment of satellite galaxies measured for clusters split into three bins of redshift.

ters, we must in principle include both the fully nonlinear tidal field 512 and nonlinear responses of galaxy shapes to that tidal field. Different 513 approaches have been adopted to treat these effects. A halo model for 543 514 IA (Schneider & Bridle 2010; Fortuna et al. 2021a) provides a param- 544 515 eterized description of galaxy shapes and locations within dark matter 545 516 halos. Similarly, semi-analytic models can be applied to gravity-only 546 517 simulations to populate dark matter halos with realistically aligned 547 518 galaxies (Joachimi et al. 2013; Hoffmann et al. 2022; Van Alfen et al. 548 519 2022). These approaches can be compared to both observational data 549 520 and hydrodynamic simulations (e.g. Samuroff et al. (2021b)). How- 550 521



Figure 13. The measured mean radial alignment of satellite galaxies measured for clusters split into three bins of cluster richness.

ever, such comparisons are not yet conclusive, given a combination of small signals and dependence on "sub-grid" assumptions.

In this work, we choose to use a simple nonlinear model to provide an estimate for the expected IA of red galaxies on this scale. Against this estimate, we can then explore the impact of several potential modeling complications relevant on these scales and for galaxy clusters. We believe that these insights can be incorporated into more sophisticated halo modeling in future work.

5.1 Nonlinear tidal alignment

We start with the ansatz, explored in Blazek et al. (2015), that the IA for red cluster member galaxies can be estimated as proportional to the fully nonlinear tidal field within the cluster. This model is similar in spirit to the "nonlinear linear alignment" (NLA) model often used in cosmic shear analyses Hirata & Seljak (2004); Bridle & King (2007); Samuroff et al. (2019); Johnston et al. (2019). However, rather than use the nonlinear dark matter power spectrum, which describes the overall clustering of matter, we use the cluster-matter power spectrum, $P_{\rm cm}$ to calculate the relevant tidal field correlations. As discussed in Blazek et al. (2015), the average galaxy IA, γ_{IA} can be described as the (projected) average correlation between the tracer density, in this case galaxy clusters, and the tidal field.

$$\gamma_{IA} = \frac{1}{2\Pi_{\text{max}}} \int_{-\Pi_{\text{max}}}^{\Pi_{\text{max}}} d\Pi \ \langle \delta_c | \gamma_+ \rangle, \tag{9}$$

where Π_{max} is the effective projection length. Making the Limber approximation, this expression can be related to P_{cm} :

$$\gamma_{IA} = \frac{1}{2\Pi_{\text{max}}} \frac{A_{\text{IA}}}{2\pi} \int_0^\infty d\kappa \kappa J_2(\kappa r_p) P_{\text{cm}}(\kappa), \qquad (10)$$

where A_{IA} is the IA amplitude, corresponding to the response of the galaxy shape to the tidal field, and J_i are the (cylindrical) Bessel functions. Finally, for P_{cm} , we combine a linear bias model on large scales with an NFW halo contribution Navarro et al. (1996) on small scales: $P_{cm} = b_c P_{lin} + P_{NFW}$, where P_{NFW} is the Fourier transform of the NFW profile. On the scales relevant for these intracluster measurements, the NFW contribution dominates over the linear term.

To generate the NFW profile, we use the mean cluster mass and

concentration parameters measured in McClintock et al. (2018), cor- 611 responding to $M_{200} = 10^{14.1} M_{\odot}$ and $c_{200} = 5$. We assume a flat 612 Λ CDM cosmology with $\Omega_m = 0.315$ and h = 0.67. We note that 613 our results are not sensitive to the assumed cosmological parameters, 614 within reasonable uncertainties. 615

As seen in Figure 10, the measured data after correcting for the 616 556 influence of intracluster light are consistent with this fully nonlin- 617 557 ear tidal alignment picture, but only on some scales. The positive 618 558 amplitude measurements (below ~ 200kpc/h are consistent with the 619 559 560 expected tidal alignment, while the negative points on larger scales 620 could be due to contamination from lensing or a different effect not 621 561 in our model. We discuss several possibilities below. When including 622 562 only scales near the center cluster that exhibit a coherent radial align- 623 563 ment (i.e. those with the expected IA sign), we find an IA amplitude 624 564 of $A_{\text{IA}} = 0.15 \pm 0.04$ (χ^2 /dof = 2.7). This is somewhat smaller than 625 565 most measurements of the large-scale red galaxy intrinsic alignment 626 566 amplitude, which tends to be closer to ~1-5, depending on luminosity 627 567 and details of selection. When fitting the measurements on all scales, 628 568 we find $A_{IA} = -0.04 \pm 0.02 \ (\chi^2/dof = 9.4)$. However, as reflected ₆₂₉ 569 by the poor fit, this value is mostly a coincidence of tension in mean 630 570 tangential alignment in the outer regions of the clusters and mean ra- 631 571 dial alignment in the innermost regions. Alternatively, if we include 632 572 an additional term, proportional to the "member boost" factor (de- 633 573 scribed above) which expresses the weighted fraction of non-cluster 634 574 members, we can allow for lensing contamination in the signal. With 575 this more complex model, we find $A_{IA} = 0.06 \pm 0.03 (\chi^2/dof = 7.1)$ 576 when fitting all scales. While these models behave qualitatively like 577 our measured alignment signal, only the fit ignoring the outer parts 578 of the cluster have a plausible (though still poor) χ^2 in terms of a 579 probability-to-exceed, with p = 0.02. This indicates more work is 636 580

582 5.2 Potential limitations to model interpretation

581

We now consider briefly additional effects beyond the measured 641 intracluster light that could potentially impact our interpretation of 642 the comparison of the measured IA and the NFW tidal model. We 643 leave for future work a detailed study of these effects in the context 644 of modeling IA within the one-halo and cluster regime. 645

needed to understand the measurements and potential systematics.

First, the use of the Limber approximation requires an effec- 646 588 tive line-of-sight projection length that is larger than the transverse 647 589 separation. While this assumption is typically appropriate for lens- 648 590 ing measurements as well as IA measurements that project over 649 591 80 - 100 Mpc, it is less clear that the assumption will hold within 650 592 the 1-halo cluster regime. In particular, because only probable clus- 651 593 594 ter members are selected, the projection length is roughly the same 652 size as the cluster radius. Moreover, if the IA and clustering signals 653 595 vary considerably within the cluster, the effective projection length 654 596 will also vary, as it is dominated by the locations of the observed 655 597 galaxy pairs. As indicated in Eq. 10, a changing effective projection 656 598 599 length will impact the overall normalization of the IA signal. This ef- 657 fect can be understood as follows: as the radial separation decreases, 658 600 the typical line-of-separation for the counted pairs also decreases, 659 601 significantly increasing the observed average signal. 602 660

Second, the REDMAPPER algorithm selects objects with a mem- 661 603 bership probability that by construction depends on the distance from 662 604 the cluster center and provides a weight corresponding to this prob- 663 605 ability. We use these weights to remove dilution from non cluster 664 606 members. However, if an appreciable number of galaxies are in fact 665 607 behind the cluster, this will lead to contamination from gravitational 666 608 lensing which is not included in our model, which assumes all galax- 667 609 ies are at the cluster redshift. Similarly, the membership weights 668 610

will also alter the effective line-of-sight weighting, e.g. compared to Eq. 10, and we do not take this into account.

Third, we expect the fraction of cluster members that are fully virialized to increase at smaller radii. If cluster member alignment develops as a response to the local environment during virialization, we would expect the IA signal to increase with the virialized fraction. Conversely, if IA is primarily imprinted by the large-scale tidal field at early times, we may expect the process of virialization to suppress the IA signal. It remains an open question which of these effects dominates IA, both in general and in cluster environments – see, e.g. Blazek et al. (2015); Piras et al. (2018). However, we note that even assuming a maximal impact of virialization, this would require a very significant change in virialized fraction with radius of the cluster.

Fourth, our simple ansatz, assuming a fixed linear response to the fully nonlinear field may fail to capture relevant IA physics on these scales. A scale-dependent IA response could capture some of this additional complexity.

Finally, alignments are measured with respect to an assumed cluster center. Miscentering of REDMAPPER clusters (e.g. Zhang et al. (2019a); Bleem et al. (2020b)) will lead to a suppression of the measured IA signal on the smallest scales. Because $\gtrsim 75\%$ of REDMAPPER clusters are well centered (Zhang et al. 2019a), this effect should be subdominant. However, future modeling should account for miscentering for a more precise inference of IA amplitude.

6 CONCLUSIONS

637

638

639

640

As cosmological studies seek to utilize smaller-scale information in the lensing signal, which can contribute significant additional constraining power, it will be key to form a better empirical understanding of the small-scale intrinsic alignment of galaxies. This is particularly true for cluster lensing studies, which probe the most extreme density regions of the universe. The DES Y1 photometric data set is a powerful tool for these studies, due to the large volume probed in which to identify galaxy clusters and the large number of galaxies over that volume with robust shape measurements. The DES Y1 redMaPPer cluster catalog extends to nearly z = 1, providing a wide range of redshift over which to study the evolution of the intrinsic alignment signal in galaxy clusters.

In this work, we investigate the intracluster alignment of redsequence galaxies using a variety of metrics that probe: 1) the alignment of the central galaxy with the cluster dark matter halo; 2) the mean distribution and alignment of satellite galaxies with the central galaxy; and 3) the mean radial alignment of satellite galaxies as a function of separation from the cluster center. These are compared across two shape measurement methods, METACALIBRATION and IM3SHAPE, and for the full REDMAPPER cluster sample and the volume-limited sample used for cosmological inference in DES.

We find significant trends of alignment in all measurements probed except for the mean alignment of satellite galaxies' position angles relative to the central galaxies in the full populations. We also find that our proxy for the cluster dark matter halo orientation, the distribution of satellite galaxies, agrees well with the orientation of halos inferred by the weak lensing convergence (mass). In particular, we are able to identify significant trends in the alignment of the central galaxy relative to the cluster dark matter halo orientation with increasing cluster richness and central galaxy absolute magnitude (both proxies for cluster mass) and to lower redshifts. This is consistent with an alignment mechanism that increases over time as the cluster evolves, with greater support by more massive clusters, rather than one that is fixed at cluster or galaxy formation and degrades over time with 728
 interactions and mergers. 729

We are also able to probe the mean radial alignment of cluster 730 671 satellites relative to the cluster center using the two-point correlation 731 672 function γ_T , finding a non-zero measurement below $0.2R_{\lambda}$ or 0.25_{732} 673 Mpc/h with a signal-to-noise of \sim 6 after correction for systematics in 733 674 the shape measurements due to intracluster light. Using the full range 734 675 of scales within the cluster, we find a measurement consistent with 735 676 zero, due to a tension between the mean radial alignment observed 736 677 678 in the inner regions of the clusters and a mean tangential alignment 737 in the outer parts of the clusters. We find both a larger amplitude and 738 679 higher signal-to-noise than in a previous study of this measurement 739 680 for REDMAPPER clusters in SDSS Huang et al. (2016, 2017). The 740 681 statistical power of this measurement of γ_T enables us to study its 741 682 evolution in bins of cluster properties, though we are not able to 742 683 identify any significant trends with those properties with the current 743 684 DES Year 1 data set. 744 685

The statistical power of these kinds of radial alignment measure-745 686 ments in cluster regions can enable new constraints on simulations 746 687 688 and models of small-scale intrinsic alignment behavior. We make a 747 first attempt to compare the measurement to a simple tidal intrinsic 748 689 alignment model inferred from the constraints on the NFW halo pro-749 690 file for these REDMAPPER clusters, and find an alignment amplitude 750 691 $A_{\text{IA}} = 0.15 \pm 0.04 \ (p = 0.02)$ when excluding data near the edge 751 692 of the cluster. We discuss several potential caveats with this simple 752 693 modeling approach and leave a more extensive attempt to model or 753 694 simulate the measurement to future works. 754 695

The measurements of intracluster intrinsic alignment of red-755 696 sequence galaxies presented here are just an example of the power 756 697 available in large photometric data sets like DES to study intrinsic 757 698 alignment phenomena. We have used here the first year of DES data, 758 699 which only covers one-third of the full survey area to half image 759 700 depth. We expect significant increases in statistical power for these 760 701 studies in the full DES data set and future surveys like Euclid, the 761 Vera C. Rubin Observatory Legacy Survey of Space and Time, and 703 the Roman Space Telescope. These future measurements will unlock 704 new potential for constraining small-scale astrophysics to inform 705 more robust cosmological analyses with lensing. 706 762

707 ACKNOWLEDGEMENTS

708 MT is supported by DOE Award SC0000253548. JB is supported by 767
 709 NSF Award AST-2206563.

Funding for the DES Projects has been provided by the U.S. De-710 711 partment of Energy, the U.S. National Science Foundation, the Ministry of Science and Education of Spain, the Science and Technology 712 Facilities Council of the United Kingdom, the Higher Education 773 713 Funding Council for England, the National Center for Supercomput-774 714 ing Applications at the University of Illinois at Urbana-Champaign, 775 715 716 the Kavli Institute of Cosmological Physics at the University of 776 Chicago, the Center for Cosmology and Astro-Particle Physics at 777 717 the Ohio State University, the Mitchell Institute for Fundamental 778 718 Physics and Astronomy at Texas A&M University, Financiadora de 779 719 Estudos e Projetos, Fundação Carlos Chagas Filho de Amparo à 780 720 Pesquisa do Estado do Rio de Janeiro, Conselho Nacional de Desen-721 782 volvimento Científico e Tecnológico and the Ministério da Ciência, 722 Tecnologia e Inovação, the Deutsche Forschungsgemeinschaft and 723 784 the Collaborating Institutions in the Dark Energy Survey. 724 785

The Collaborating Institutions are Argonne National Laboratory, 786
 the University of California at Santa Cruz, the University of Cam- 787
 bridge, Centro de Investigaciones Energéticas, Medioambientales y 788

Tecnológicas-Madrid, the University of Chicago, University College London, the DES-Brazil Consortium, the University of Edinburgh, the Eidgenössische Technische Hochschule (ETH) Zürich, Fermi National Accelerator Laboratory, the University of Illinois at Urbana-Champaign, the Institut de Ciències de l'Espai (IEEC/CSIC), the Institut de Física d'Altes Energies, Lawrence Berkeley National Laboratory, the Ludwig-Maximilians Universität München and the associated Excellence Cluster Universe, the University of Michigan, NFS's NOIRLab, the University of Nottingham, The Ohio State University, the University of Pennsylvania, the University of Portsmouth, SLAC National Accelerator Laboratory, Stanford University, the University of Sussex, Texas A&M University, and the OzDES Membership Consortium.

Based in part on observations at Cerro Tololo Inter-American Observatory at NSF's NOIRLab (NOIRLab Prop. ID 2012B-0001; PI: J. Frieman), which is managed by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation.

The DES data management system is supported by the National Science Foundation under Grant Numbers AST-1138766 and AST-1536171. The DES participants from Spanish institutions are partially supported by MICINN under grants ESP2017-89838, PGC2018-094773, PGC2018-102021, SEV-2016-0588, SEV-2016-0597, and MDM-2015-0509, some of which include ERDF funds from the European Union. IFAE is partially funded by the CERCA program of the Generalitat de Catalunya. Research leading to these results has received funding from the European Research Council under the European Union's Seventh Framework Program (FP7/2007-2013) including ERC grant agreements 240672, 291329, and 306478. We acknowledge support from the Brazilian Instituto Nacional de Ciência e Tecnologia (INCT) e-Universe (CNPq grant 465376/2014-2).

This manuscript has been authored by Fermi Research Alliance, LLC under Contract No. DE-AC02-07CH11359 with the U.S. Department of Energy, Office of Science, Office of High Energy Physics.

REFERENCES

763

764

765

766

- Agustsson I., Brainerd T. G., 2006, ApJ, 644, L25
- Asgari M., et al., 2021, A&A, 645, A104
- Blazek J., Vlah Z., Seljak U., 2015, J. Cosmology Astropart. Phys., 2015, 015
- Blazek J. A., MacCrann N., Troxel M. A., Fang X., 2019, Phys. Rev. D, 100, 103506
- Bleem L. E., et al., 2020a, ApJS, 247, 25
- Bleem L. E., et al., 2020b, ApJS, 247, 25
- Bridle S., King L., 2007, New Journal of Physics, 9, 444
- Chang C., et al., 2018, MNRAS, 475, 3165
- Chisari N., et al., 2015, MNRAS, 454, 2736
- C & D A C M + 1 C A 2000 A L 5
- Croft R. A. C., Metzler C. A., 2000, ApJ, 545, 561
- DES Collaboration et al., 2020a, arXiv e-prints, p. arXiv:2002.11124
- DES Collaboration et al., 2020b, Phys. Rev. D, 102, 023509
- DES Collaboration et al., 2022, Phys. Rev. D, 105, 023520
- Drlica-Wagner A., et al., 2018, ApJS, 235, 33
- Dyson F. W., Eddington A. S., Davidson C., 1920, Philosophical Transactions of the Royal Society of London. Series A, Containing Papers of a Mathematical or Physical Character, 220, 291
- Elvin-Poole J., et al., 2018, Phys. Rev. D, 98, 042006
- Faltenbacher A., Li C., Mao S., van den Bosch F. C., Yang X., Jing Y. P., Pasquali A., Mo H. J., 2007, ApJ, 662, L71
- Flaugher B., et al., 2015, Astron. J., 150, 150
- Fortuna M. C., Hoekstra H., Joachimi B., Johnston H., Chisari N. E., Georgiou C., Mahony C., 2021a, MNRAS, 501, 2983
- Fortuna M. C., et al., 2021b, A&A, 654, A76
- Grandis S., et al., 2021, MNRAS, 504, 1253

⁷⁸⁹ Hamana T., et al., 2020, PASJ, 72, 16

- Hao J., Kubo J. M., Feldmann R., Annis J., Johnston D. E., Lin H., McKay 857
 T. A., 2011, ApJ, 740, 39
- ⁷⁹² Heavens A., Refregier A., Heymans C., 2000, MNRAS, 319, 649
- ⁷⁹³ Herbonnet R., et al., 2022, MNRAS, 513, 2178
- ⁷⁹⁴ Hirata C. M., Seljak U., 2004, Phys. Rev. D, 70, 063526
- Hirata C. M., Mandelbaum R., Ishak M., Seljak U., Nichol R., Pimbblet K. A.,
 Ross N. P., Wake D., 2007, MNRAS, 381, 1197
- ⁷⁹⁷ Hoffmann K., et al., 2022, arXiv e-prints, p. arXiv:2206.14219
- Huang H.-J., Mandelbaum R., Freeman P. E., Chen Y.-C., Rozo E., Rykoff E., ⁸⁶¹
 Baxter E. J., 2016, Monthly Notices of the Royal Astronomical Society, ⁸⁶²
 463, 222–244
- Huang H.-J., Mandelbaum R., Freeman P. E., Chen Y.-C., Rozo E., Rykoff 864
 E., 2017, Monthly Notices of the Royal Astronomical Society, 474, 865
 4772–4794
- 804 Huff E., Mandelbaum R., 2017, preprint, (arXiv:1702.02600)
- ⁸⁰⁵ Jarvis M., Bernstein G., Jain B., 2004, MNRAS, 352, 338
- Joachimi B., Mandelbaum R., Abdalla F. B., Bridle S. L., 2011, A&A, 527, 468
 A26
- Joachimi B., Semboloni E., Hilbert S., Bett P. E., Hartlap J., Hoekstra H.,
 Schneider P., 2013, MNRAS, 436, 819
- ⁸¹⁰ Johnston H., et al., 2019, A&A, 624, A30
- ⁸¹¹ Krause E., et al., 2021, arXiv e-prints, p. arXiv:2105.13548
- Mandelbaum R., Hirata C. M., Ishak M., Seljak U., Brinkmann J., 2006, 874
 MNRAS, 367, 611
- ⁸¹⁴ McClintock T., et al., 2018, preprint (arXiv: 1805.00039)
- 815 McClintock T., et al., 2019, MNRAS, 482, 1352
- Mohr J. J., et al., 2008, in Observatory Operations: Strategies, Processes, and Systems II. p. 70160L, doi:10.1117/12.789550
- Mohr J. J., et al., 2012, in Radziwill N. M., Chiozzi G., eds, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series Vol. 8451, Software and Cyberinfrastructure for Astronomy II. p. 845100 (arXiv:1207.3189), doi:10.1117/12.926785
- 822 Navarro J. F., Frenk C. S., White S. D. M., 1996, ApJ, 462, 563
- ⁸²³ Okabe T., et al., 2020, MNRAS, 496, 2591
- 824 Pereira M. J., Kuhn J. R., 2005, ApJ, 627, L21
- Piras D., Joachimi B., Schäfer B. M., Bonamigo M., Hilbert S., van Uitert E., 886
 2018, MNRAS, 474, 1165
- Rozo E., Rykoff E. S., Becker M., Reddick R. M., Wechsler R. H., 2015, 888 MNRAS, 453, 38
- 829 Rozo E., et al., 2016, MNRAS, 461, 1431
- ⁸³⁰ Rykoff E. S., et al., 2014, ApJ, 785, 104
- ⁸³¹ Rykoff E. S., et al., 2016, ApJS, 224, 1
- ⁸⁹² Sadibekova T., Pierre M., Clerc N., Faccioli L., Gastaud R., Le Fevre J. P.,
 ⁸⁹³ Rozo E., Rykoff E., 2014, A&A, 571, A87
 ⁸⁹⁴ Rozo E., Rykoff E., 2014, A&A, 571, A87
- 834 Samuroff S., et al., 2019, MNRAS, 489, 5453
- Samuroff S., Mandelbaum R., Blazek J., 2021a, MNRAS, 508, 637
- Samuroff S., Mandelbaum R., Blazek J., 2021b, MNRAS, 508, 637
- 837 Saro A., et al., 2015, MNRAS, 454, 2305
- 838 Schneider M. D., Bridle S., 2010, MNRAS, 402, 2127
- 839 Schneider M. D., et al., 2013, MNRAS, 433, 2727
- 840 Sevilla I., et al., 2011, preprint, (arXiv:1109.6741)
- ⁸⁴¹ Sheldon E. S., Huff E. M., 2017, Astrophys. J., 841, 24
- Shin T.-h., Clampitt J., Jain B., Bernstein G., Neil A., Rozo E., Rykoff E., 902
 2018, Monthly Notices of the Royal Astronomical Society, 475, 2421
- 844 Sifón C., Hoekstra H., Cacciato M., Viola M., Köhlinger F., van der Burg R. 904
- ⁸⁴⁵ F. J., Sand D. J., Graham M. L., 2015, A&A, 575, A48
- Singh S., Mandelbaum R., More S., 2015, MNRAS, 450, 2195
- 847 Siverd R. J., Ryden B. S., Gaudi B. S., 2009, arXiv e-prints, p.
 848 arXiv:0903.2264
- Tenneti A., Mandelbaum R., Di Matteo T., 2016, MNRAS, 462, 2668
- ⁸⁵⁰ Troxel M. A., Ishak M., 2014, Phys. Rept., 558, 1
- ⁸⁵¹ Troxel M. A., et al., 2018, Phys. Rev. D, 98, 043528
- Van Alfen N., et al., 2022, in prep.
- ⁸⁵³ Zhang Y., et al., 2019a, MNRAS, 487, 2578
- ⁸⁵⁴ Zhang Y., et al., 2019b, ApJ, 874, 165
- 855 Zjupa J., Schäfer B. M., Hahn O., 2020, arXiv e-prints, p. arXiv:2010.07951 914

Zuntz J., Kacprzak T., Voigt L., Hirsch M., Rowe B., Bridle S., 2013, MNRAS, 434, 1604

- Zuntz J., et al., 2018, MNRAS, 481, 1149
- van Uitert E., Joachimi B., 2017, MNRAS, 468, 4502

AFFILIATIONS

867

872

873

876

877

883

884

885

890

891

895

896

897

898

899

900

901

905

906

907

908

909

911

912

913

- ¹ Department of Physics, Duke University Durham, NC 27708, USA
 ² Department of Physics, Northeastern University, Boston, MA
- 02115, USA
- ³ Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth, PO1 3FX, UK
- ⁴ Argonne National Laboratory, 9700 South Cass Avenue, Lemont, IL 60439, USA
- ⁵ Department of Astronomy and Astrophysics, University of Chicago, Chicago, IL 60637, USA
- ⁶ Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA
- ⁷ Astronomy Unit, Department of Physics, University of Trieste, via Tiepolo 11, I-34131 Trieste, Italy
- ⁸ INAF-Osservatorio Astronomico di Trieste, via G. B. Tiepolo 11, I-34143 Trieste, Italy
- ⁹ Institute for Fundamental Physics of the Universe, Via Beirut 2, 34014 Trieste, Italy
- ¹⁰ Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, CA 94720, USA
- ¹¹ University Observatory, Faculty of Physics, Ludwig-Maximilians-Universität, Scheinerstr. 1, 81679 Munich, Germany
- ¹² Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510, USA
- ¹³ Center for Astrophysical Surveys, National Center for Supercomputing Applications, 1205 West Clark St., Urbana, IL 61801, USA
- ¹⁴ Department of Astronomy, University of Illinois at Urbana-Champaign, 1002 W. Green Street, Urbana, IL 61801, USA
- ¹⁵ Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA
- ¹⁶ Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge CB3 0WA, UK
- ¹⁷ Department of Physics, University of Arizona, Tucson, AZ 85721, USA
- ¹⁸ Department of Astrophysical Sciences, Princeton University, Peyton Hall, Princeton, NJ 08544, USA
- ¹⁹ Institut d'Estudis Espacials de Catalunya (IEEC), 08034 Barcelona, Spain
- ²⁰ Institute of Space Sciences (ICE, CSIC), Campus UAB, Carrer de Can Magrans, s/n, 08193 Barcelona, Spain
- ²¹ Kavli Institute for Particle Astrophysics & Cosmology, P. O. Box 2450, Stanford University, Stanford, CA 94305, USA
- ²² SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA
- ²³ Brookhaven National Laboratory, Bldg 510, Upton, NY 11973, USA
- ²⁴ Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794, USA
- ²⁵ Instituto de Astrofisica de Canarias, E-38205 La Laguna, Tenerife, Spain
- ⁹¹⁰ ²⁶ Laboratório Interinstitucional de e-Astronomia LIneA, Rua Gal.
 - José Cristino 77, Rio de Janeiro, RJ 20921-400, Brazil
 - ²⁷ Universidad de La Laguna, Dpto. AstrofÃsica, E-38206 La Laguna, Tenerife, Spain
 - ²⁸ Centro de Investigaciones Energéticas, Medioambientales y

- 915 Tecnológicas (CIEMAT), Madrid, Spain
- ²⁹ Institute for Astronomy, University of Edinburgh, Edinburgh EH9 978
 ³¹⁷ 3HJ, UK 979
- ³⁰ Excellence Cluster Origins, Boltzmannstr. 2, 85748 Garching, 980
 ⁹¹⁹ Germany
 ⁹⁸¹
- ³¹ Max Planck Institute for Extraterrestrial Physics, Giessenbachstrasse, 85748 Garching, Germany
- ⁹²² ³² Universitäts-Sternwarte, Fakultät für Physik, Ludwig-
- Maximilians Universität München, Scheinerstr. 1, 81679 München,
 Germany
- ³³ Department of Astronomy, University of Michigan, Ann Arbor,
 MI 48109, USA
- ⁹²⁷ ³⁴ Department of Physics, University of Michigan, Ann Arbor, MI
 ⁹²⁸ 48109, USA
- ³⁵ Institute of Astronomy, University of Cambridge, Madingley
 Road, Cambridge CB3 0HA, UK
- ³⁶ Kavli Institute for Cosmology, University of Cambridge, Madin gley Road, Cambridge CB3 0HA, UK
- ³⁷ CNRS, UMR 7095, Institut d'Astrophysique de Paris, F-75014,
 Paris, France
- ³⁸ Sorbonne Universités, UPMC Univ Paris 06, UMR 7095, Institut
- ⁹³⁶ d'Astrophysique de Paris, F-75014, Paris, France
- ³⁹ Department of Physics & Astronomy, University College London,
 Gower Street, London, WC1E 6BT, UK
- ⁴⁰ School of Mathematics and Physics, University of Queensland,
 Brisbane, QLD 4072, Australia
- ⁴¹ Department of Physics, IIT Hyderabad, Kandi, Telangana 502285,
 India
- ⁴² Jet Propulsion Laboratory, California Institute of Technology,
 ⁴⁸⁰⁰ Oak Grove Dr., Pasadena, CA 91109, USA
- ⁴⁴³ Institute of Theoretical Astrophysics, University of Oslo. P.O.
 ⁹⁴⁶ Box 1029 Blindern, NO-0315 Oslo, Norway
- ⁴⁴ Santa Cruz Institute for Particle Physics, Santa Cruz, CA 95064,
 ⁹⁴⁸ USA
- ⁴⁵ Center for Cosmology and Astro-Particle Physics, The Ohio State
 University, Columbus, OH 43210, USA
- ⁴⁶ Department of Physics, The Ohio State University, Columbus,
 OH 43210, USA
- ⁴⁷ Center for Astrophysics | Harvard & Smithsonian, 60 Garden
 Street, Cambridge, MA 02138, USA
- ⁴⁸ Australian Astronomical Optics, Macquarie University, North
 ⁸⁵⁶ Ryde, NSW 2113, Australia
- ⁴⁹ Lowell Observatory, 1400 Mars Hill Rd, Flagstaff, AZ 86001,
 ⁹⁵⁸ USA
- ⁵⁰ Departamento de Física Matemática, Instituto de Física, Universidade de São Paulo, CP 66318, São Paulo, SP, 05314-970, Brazil
- ⁵¹ George P. and Cynthia Woods Mitchell Institute for Fundamental
- Physics and Astronomy, and Department of Physics and Astronomy,
- Texas A&M University, College Station, TX 77843, USA
- ⁵² Institució Catalana de Recerca i Estudis Avançats, E-08010
 Barcelona, Spain
- ⁵³ Institut de Física d'Altes Energies (IFAE), The Barcelona Institute
 of Science and Technology, Campus UAB, 08193 Bellaterra
- of Science and Technology, Campus UAB, 08193 Bellaterr
 (Barcelona) Spain
- ⁵⁴ Department of Physics, Carnegie Mellon University, Pittsburgh,
 Pennsylvania 15312, USA
- ⁵⁵ Observatório Nacional, Rua Gal. José Cristino 77, Rio de Janeiro,
 RJ 20921-400, Brazil
- ⁵⁶ Department of Physics, University of Genova and INFN, Via
 Dodecaneso 33, 16146, Genova, Italy
- ⁹⁷⁵ ⁵⁷ Department of Physics and Astronomy, Pevensey Building,
- 976 University of Sussex, Brighton, BN1 9QH, UK

⁵⁸ School of Physics and Astronomy, University of Southampton, Southampton, SO17 1BJ, UK

⁵⁹ Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831

⁶⁰ Waldorf High School, Belmont, MA 02478

977

This paper has been typeset from a $T_{\!E}\!X/{\!I\!\!\!\Delta} T_{\!E}\!X$ file prepared by the author.