

WIN2021

University of Minnesota, USA

June, 2021

Virtual Conference

QED radiative corrections
to charged-current neutrino-nucleon
elastic scattering
for accelerator neutrino experiments

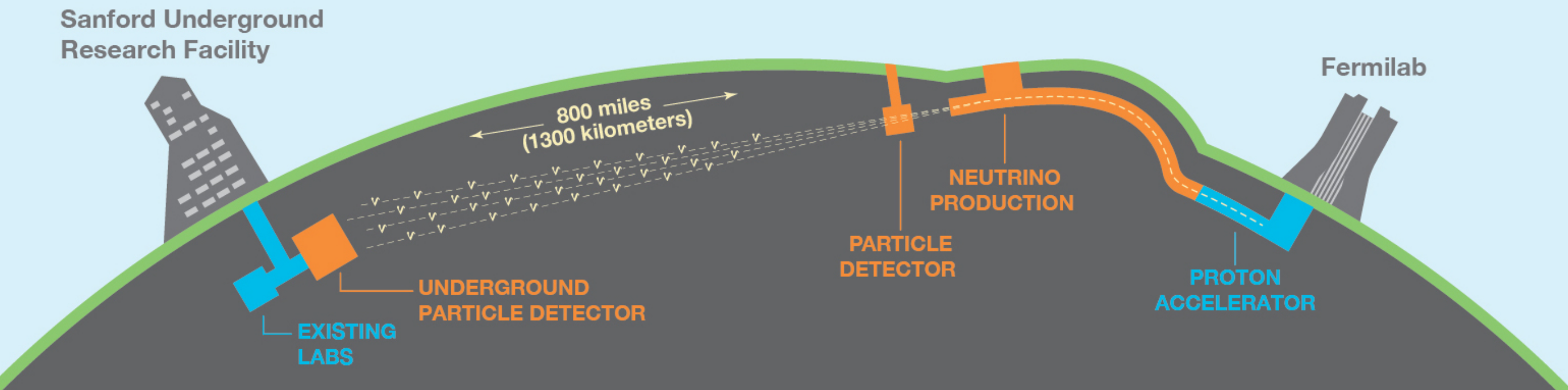


Oleksandr Tomalak

O.T., Qing Chen, Richard J. Hill and Kevin S. McFarland, arXiv: 2105.07939

Neutrino experiments

- **DUNE** and Hyper-K: leading-edge ν science experiments

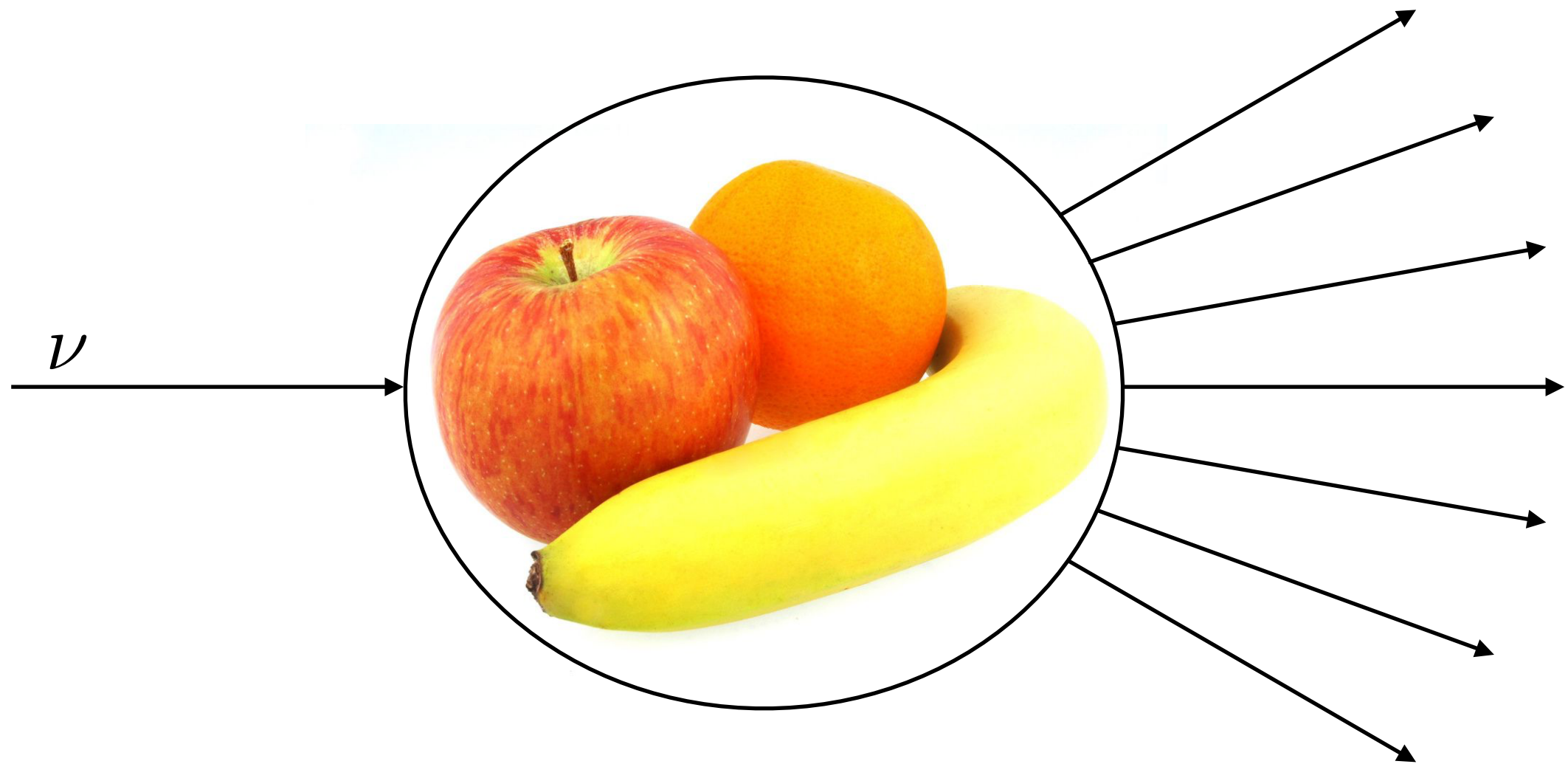


- measurement of ν_μ disappearance and ν_e appearance

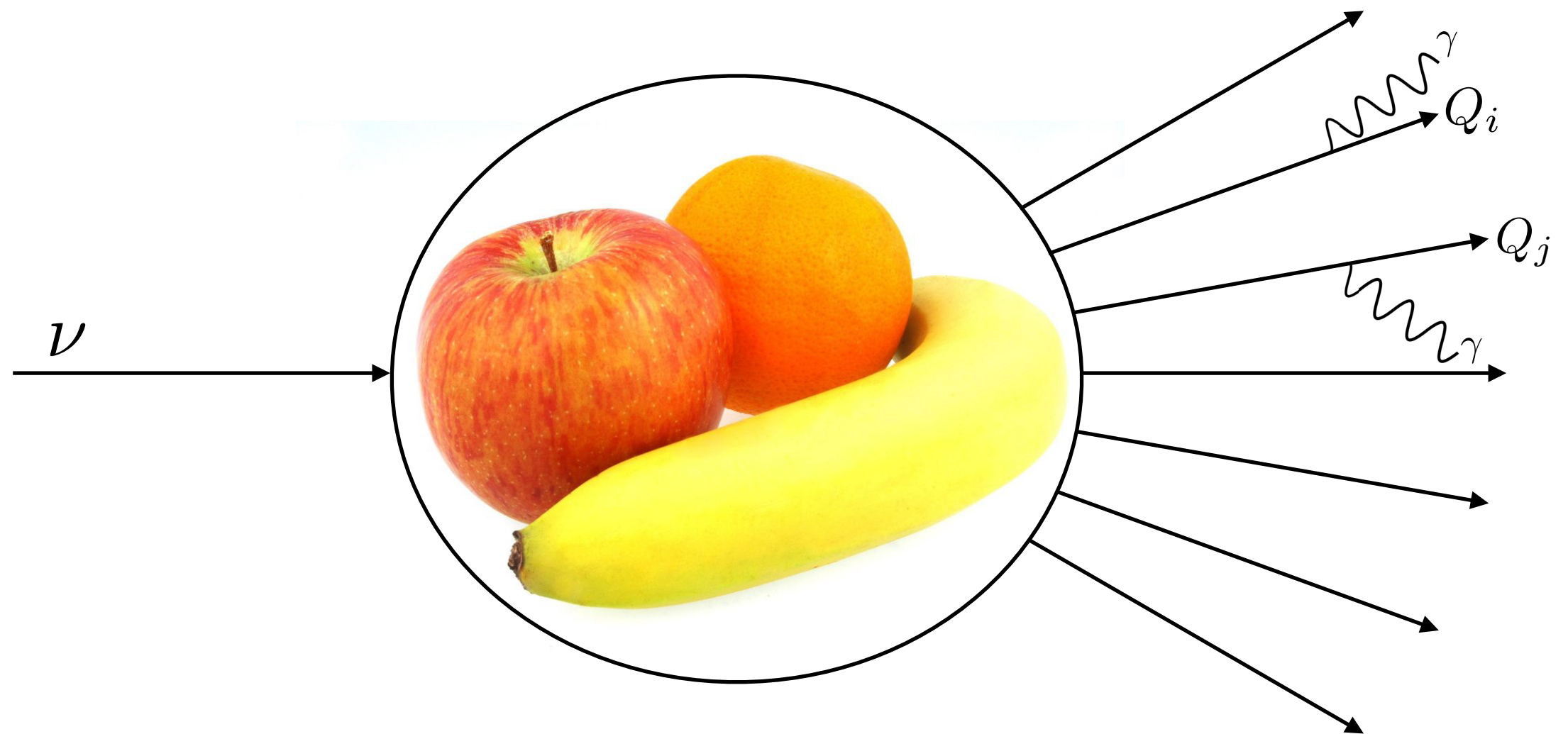
$$N_\nu \sim \int dE_\nu \Phi_\nu(E_\nu) \times \sigma(E_\nu) \times R(E_\nu, E_\nu^{\text{rec}})$$

- near detector: determine flux and cross sections

Neutrino interactions

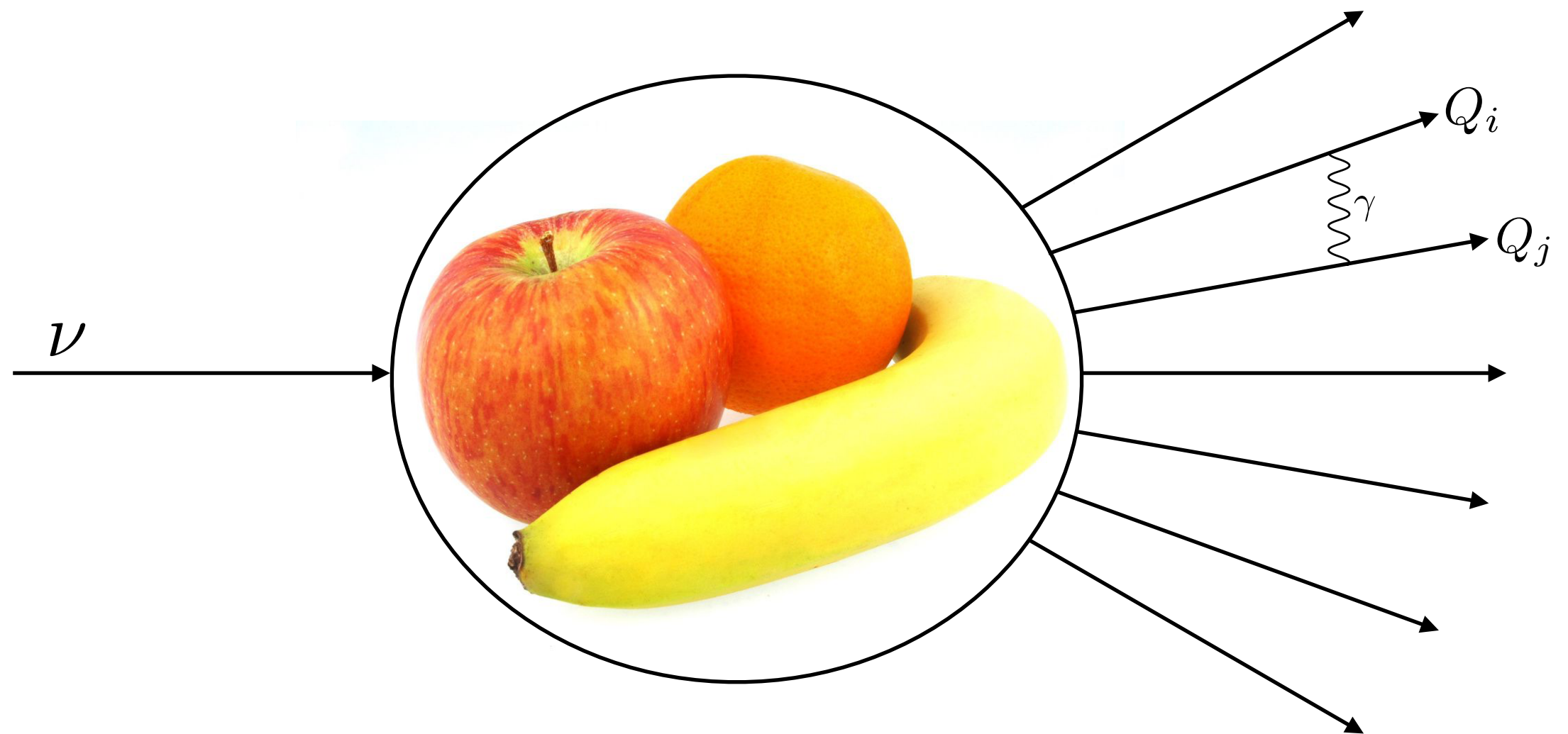


QED corrections



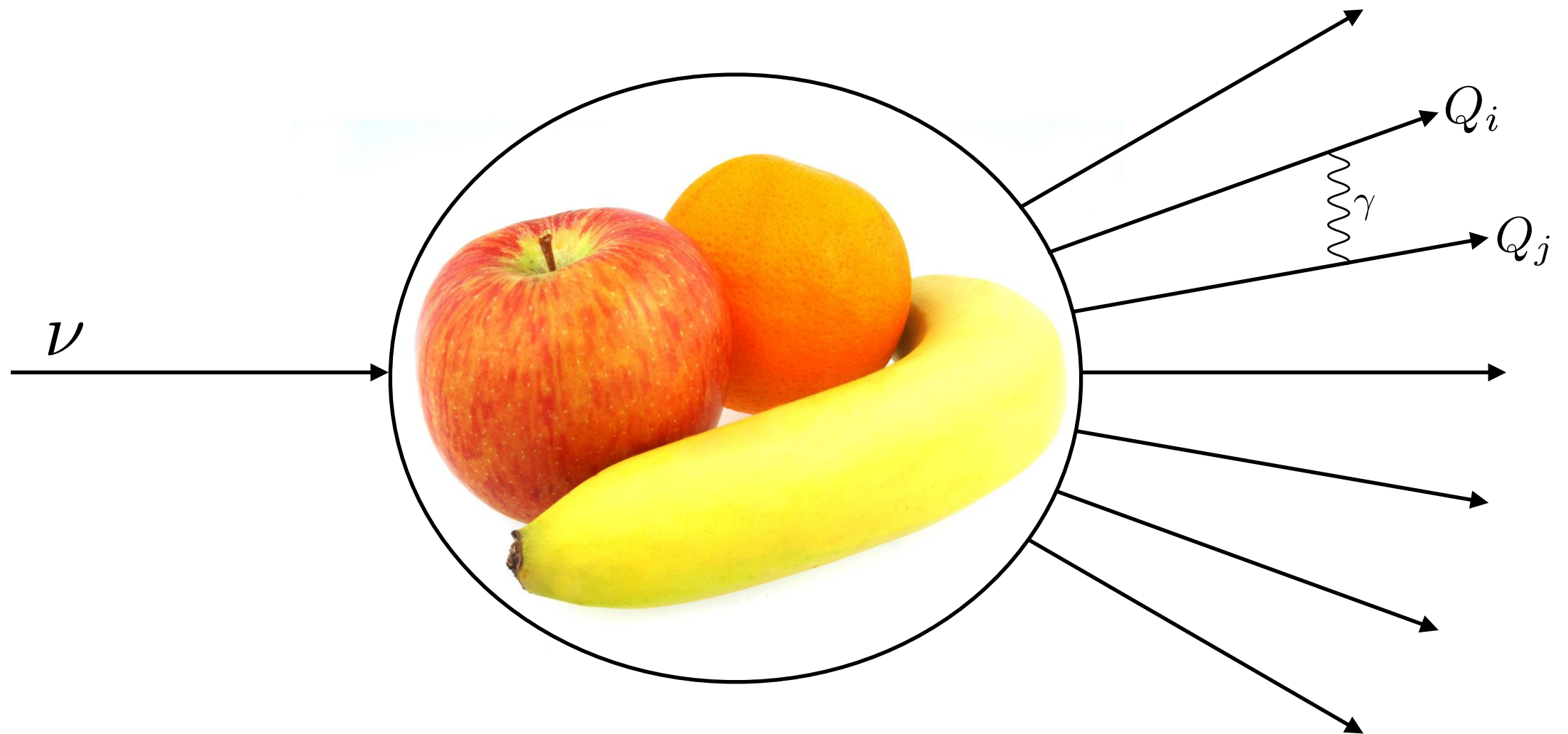
- all charged particles couple to real and virtual photons

QED corrections



- all charged particles couple to real and virtual photons

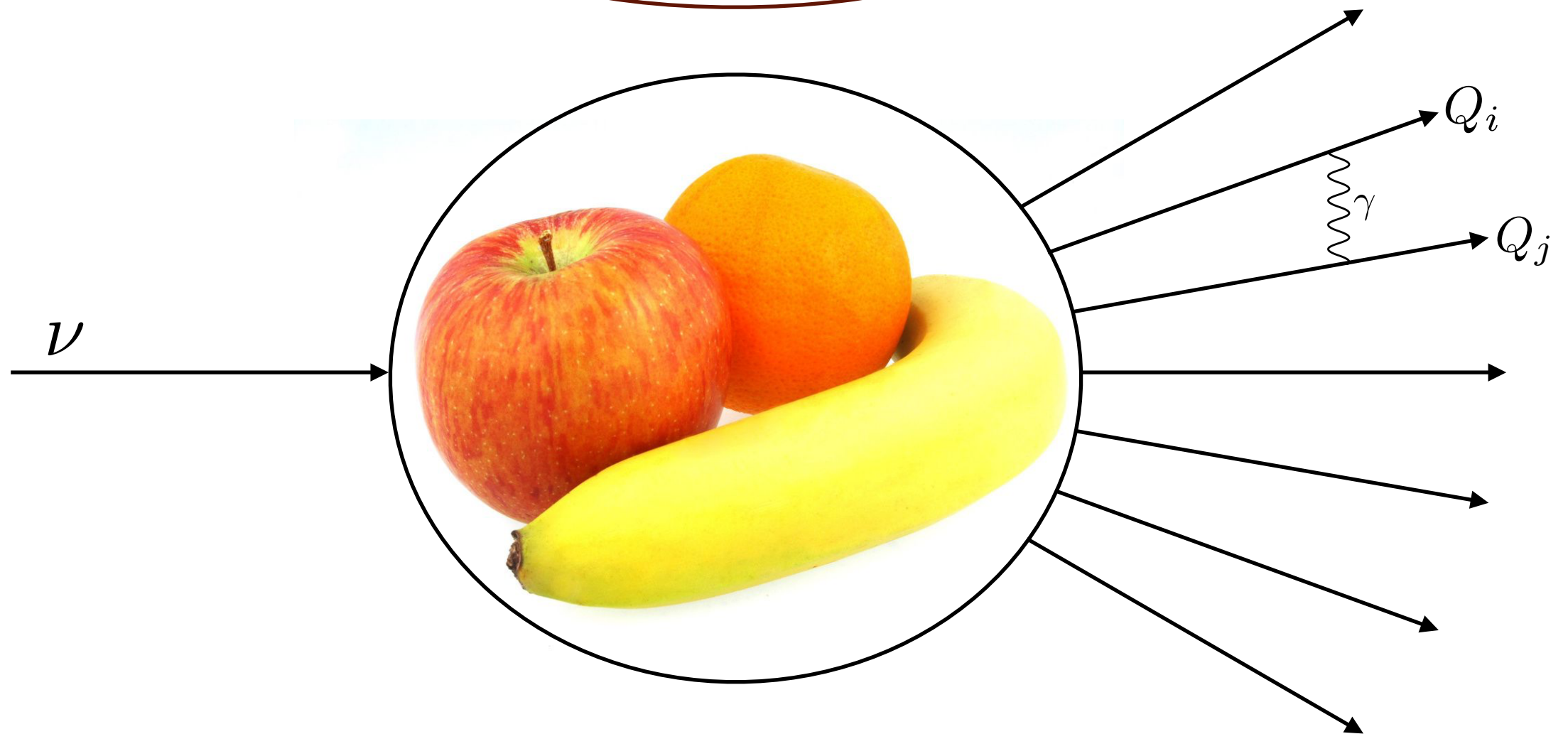
QED corrections



- $\frac{\alpha}{\pi} \sim 0.2 \%$ suppression by electromagnetic coupling constant

QED corrections

$$m_e \ll m_\mu \ll E_\nu$$

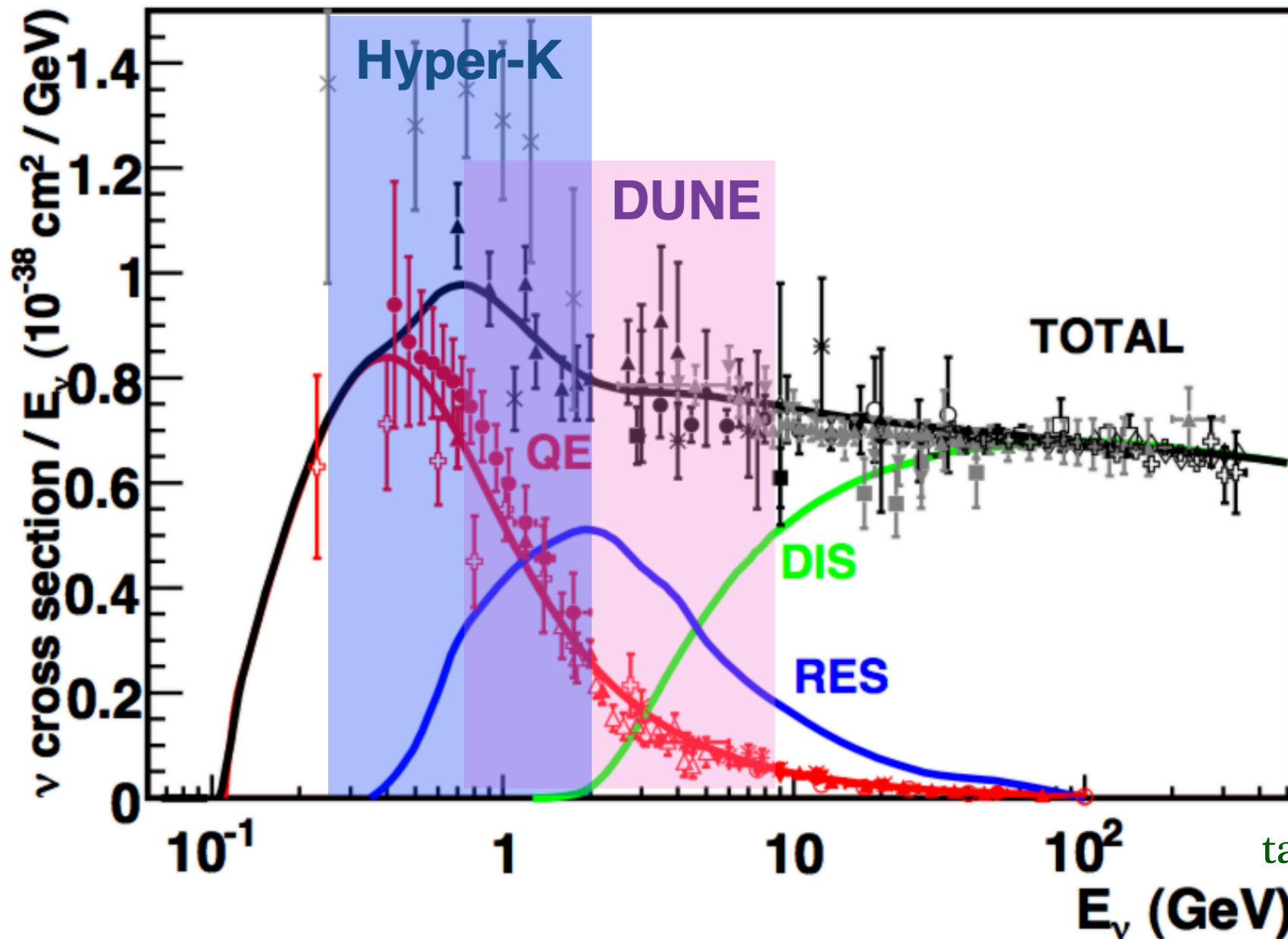


$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \ln \frac{E_\nu}{m_e} \sim 6 - 10 \text{ or } \ln^2 \frac{E_\nu}{m_e} \sim 36 - 100$$

- scale separation: large flavor-dependent logarithms for GeV energy

CCQE. Why should we care?

- neutrino-nucleus cross sections and future accelerator-based fluxes

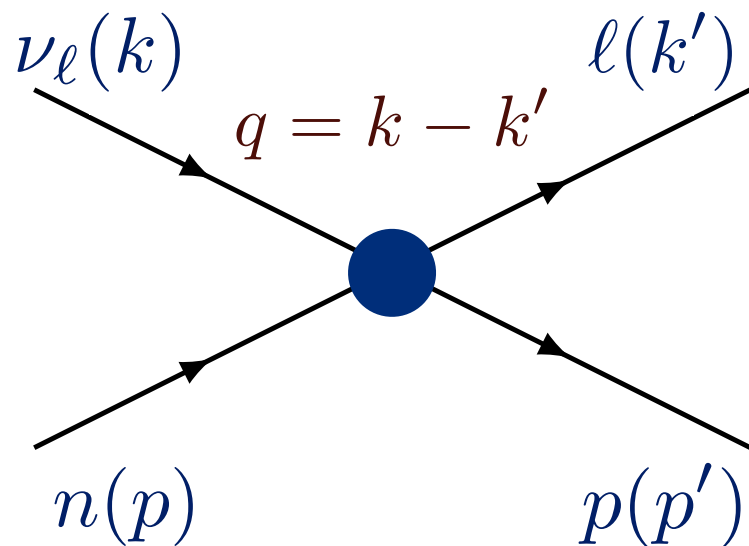


Formaggio
and Zeller
(2013)

Noemi Rocco
talk at Neutrino 2020

- basic process: bulk of events at Hyper-K and DUNE
- best channel for reconstruction of neutrino energy

Scattering on free nucleon



neutrino energy

$$E_\nu$$

momentum transfer

$$Q^2 = -q^2$$

contact interaction at GeV energies

- assuming isospin symmetry, nucleon current:

$$\Gamma^\mu(Q^2) = \langle p | \bar{u} (\gamma^\mu - \gamma^\mu \gamma_5) d | n \rangle$$

$$\Gamma^\mu(Q^2) = \gamma^\mu F_D^V(Q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2M} F_P^V(Q^2) + \gamma^\mu \gamma_5 F_A(Q^2) + \frac{q^\mu}{M} \gamma_5 F_P(Q^2)$$

form factors: isovector Dirac and Pauli axial and pseudoscalar

$$F_{D,P}^V = F_{D,P}^p - F_{D,P}^n$$

tree-level amplitude

$$T = \frac{G_F V_{ud}}{\sqrt{2}} (\bar{\ell}(k') \gamma_\mu (1 - \gamma_5) \nu_\ell(k)) (\bar{p}(p') \Gamma^\mu(Q^2) n(p))$$

Radiative corrections

- large kinematic logarithms enhance radiative corrections

$$\frac{\alpha}{\pi} \sim 0.2 \% \quad \text{multiplied by} \quad \ln \frac{E_\nu}{m_e} \sim 6 - 10$$

- cross sections with electron flavor are subject to large corrections

- phase-space restrictions enhance radiative corrections

$$\frac{\alpha}{\pi} \sim 0.2 \% \quad \text{multiplied by} \quad \ln^2 \frac{E_\nu}{m_e} \sim 36 - 100$$

$$E_\gamma < \Delta E \quad \text{soft photons} \quad 2 \ln \frac{E_\nu}{m_e} \ln \frac{\Delta E}{m_e} \sim 35 - 60$$

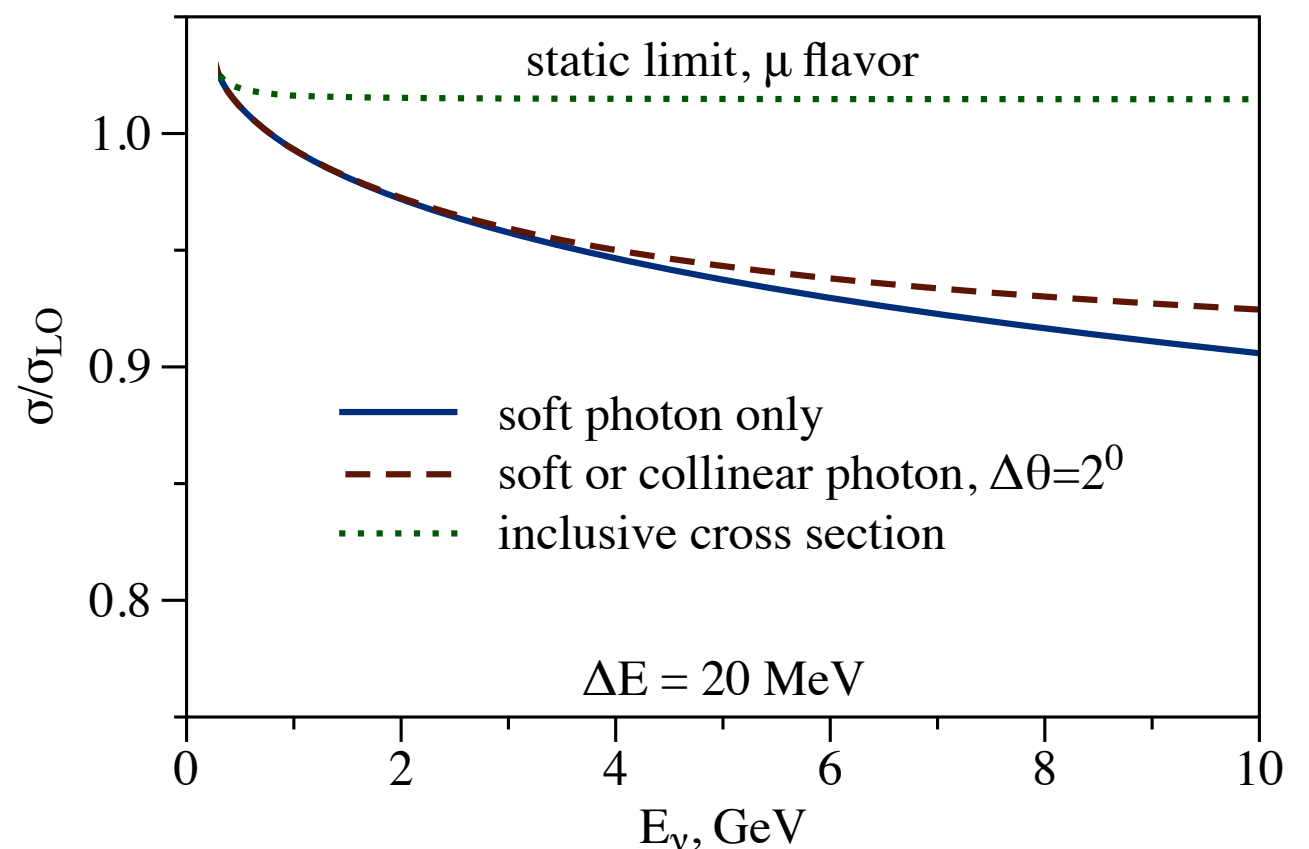
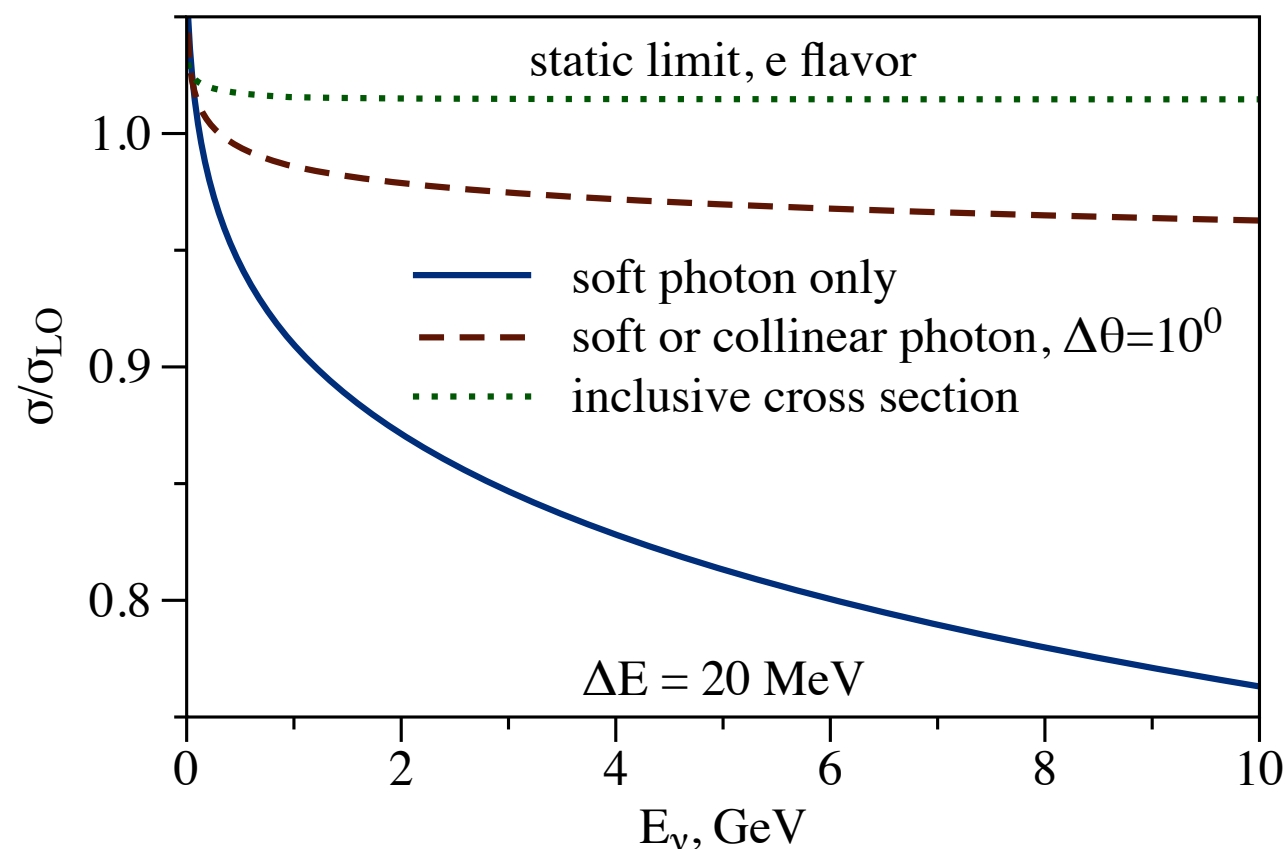
smaller collinear logarithms

- crucial dependence on detector details

- radiative corrections crucial for %-level oscillation program

Static nucleon limit

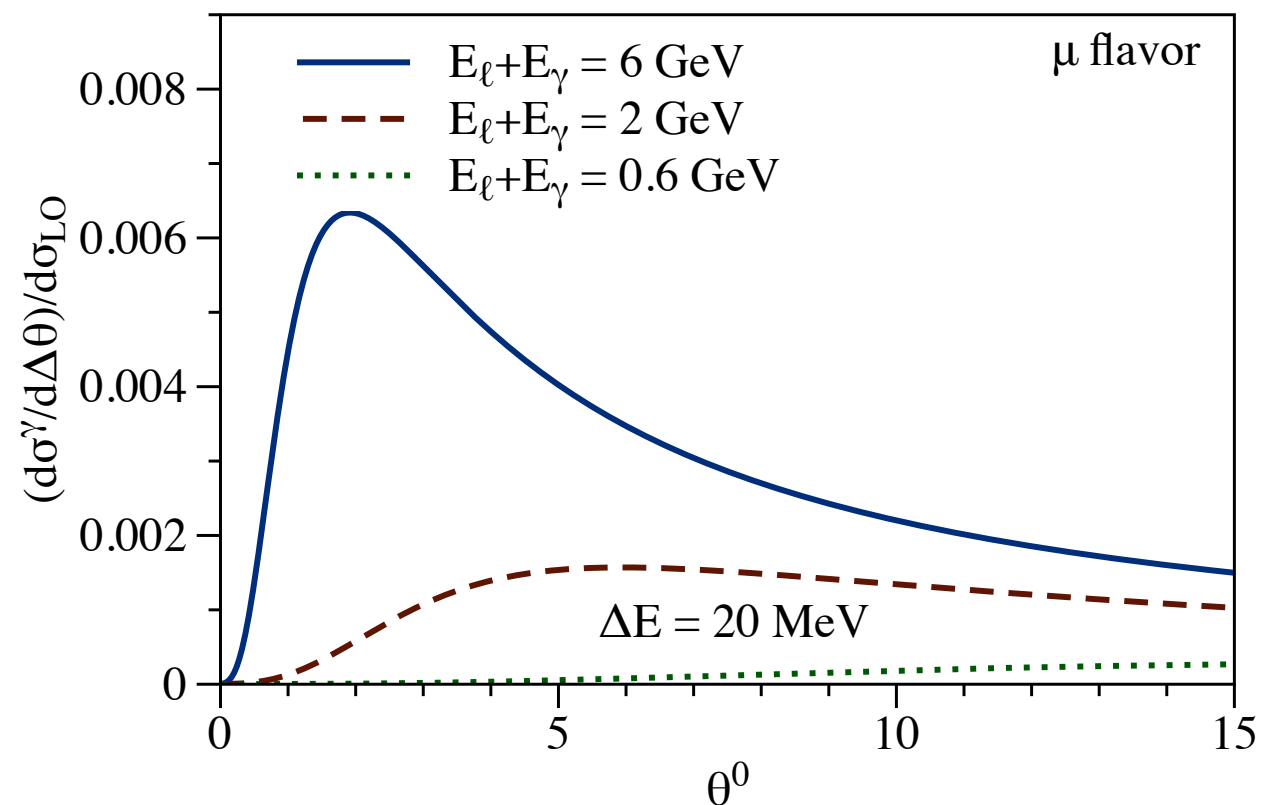
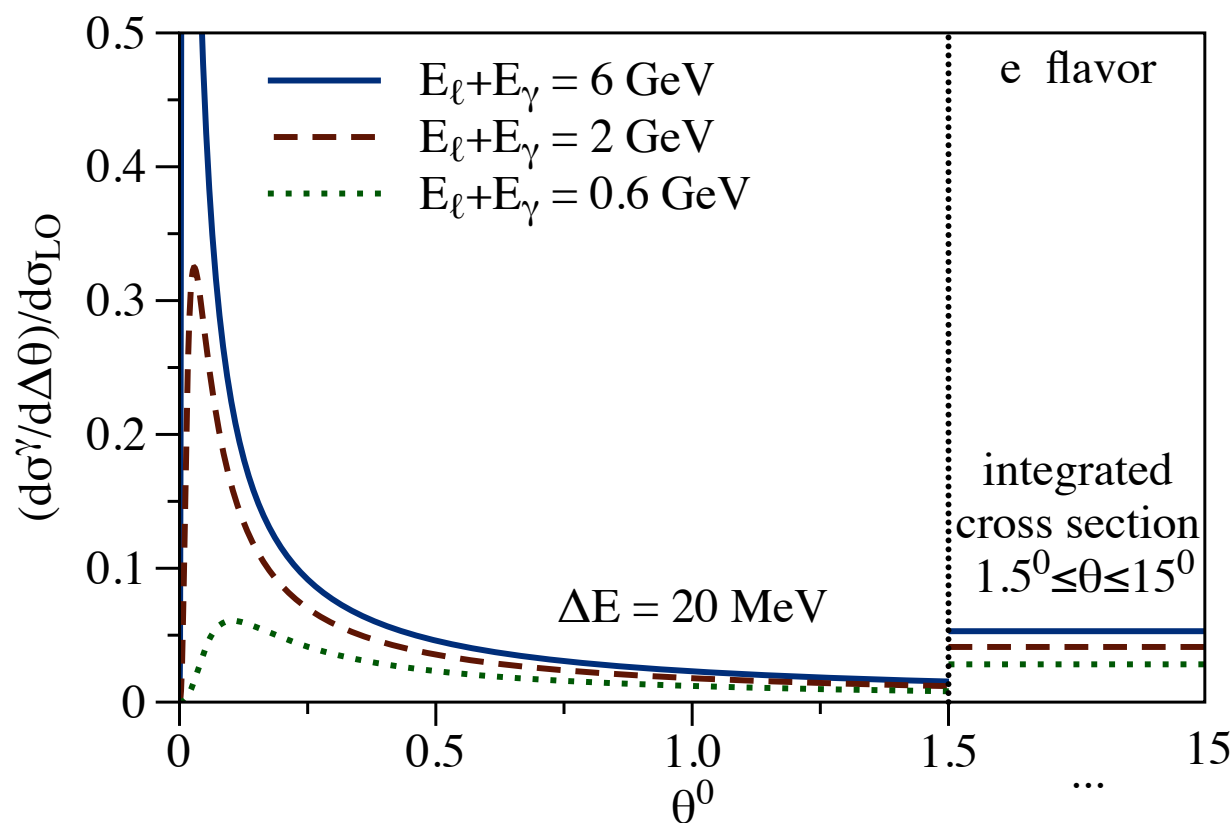
- formal limit of infinitely heavy nucleus $m_\ell \ll E_\ell \ll M$
- provides correct soft and collinear logarithms
- soft-photon energy < 20 MeV, jet size: 10° for electron and 2° for muon



- flavor-dependent effect, same for $\nu_\ell n \rightarrow \ell^- p$ vs $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- collinear observable: cancellation of virtual vs real logs
- inclusive observables ($+\gamma$): few % level, flavor independent

Electron vs muon jets

- factorization for radiation of collinear photons
- cone angle is defined to lepton direction
- photons of energy > 20 MeV, fixed energy in the cone



- flavor-dependent effect, same for $\nu_\ell n \rightarrow \ell^- p$ vs $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- forward-peaked radiation for electron flavor
- negligible radiation for muons with shifted peak position

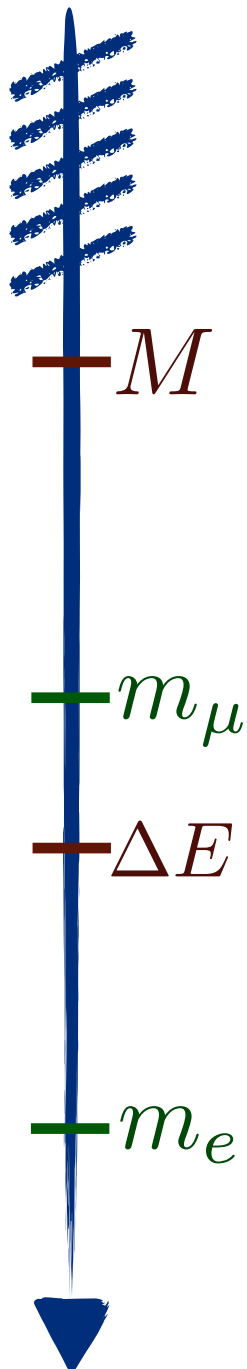
Factorization approach

- cross section is given by **factorization formula**

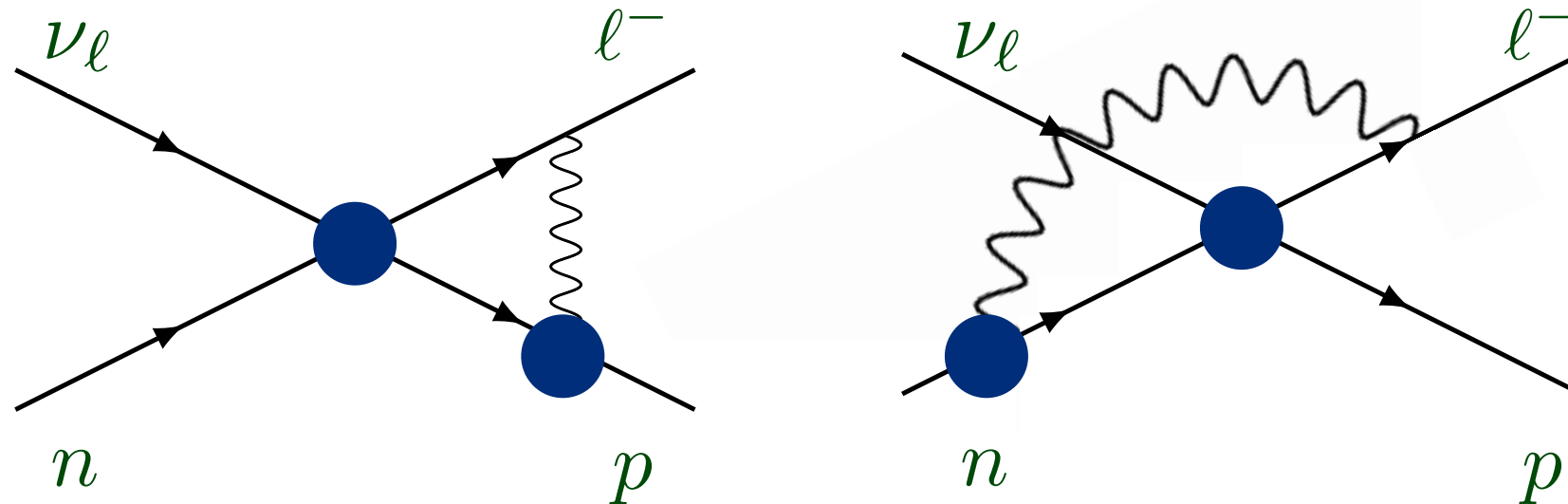
$$d\sigma \sim S \left(\frac{\Delta E}{\mu} \right) J \left(\frac{m_\ell}{\mu} \right) H \left(\frac{M}{\mu} \right)$$

- determine **hard function** at hard scale by matching experiment or hadronic model to the theory with heavy nucleon

- **soft and collinear functions** are evaluated **perturbatively**



Hadronic model at GeV scale




- exchange of photon between the charged lepton and nucleons
- assume **onshell form** for each interaction with dipole form factors
discussed for neutrino-nucleon scattering: Graczyk (2013)
- add **self energy** for charged particles
- reproduce soft and collinear regions of SCET

- best determination of hard function

Factorization approach

- cross section is given by **factorization formula**

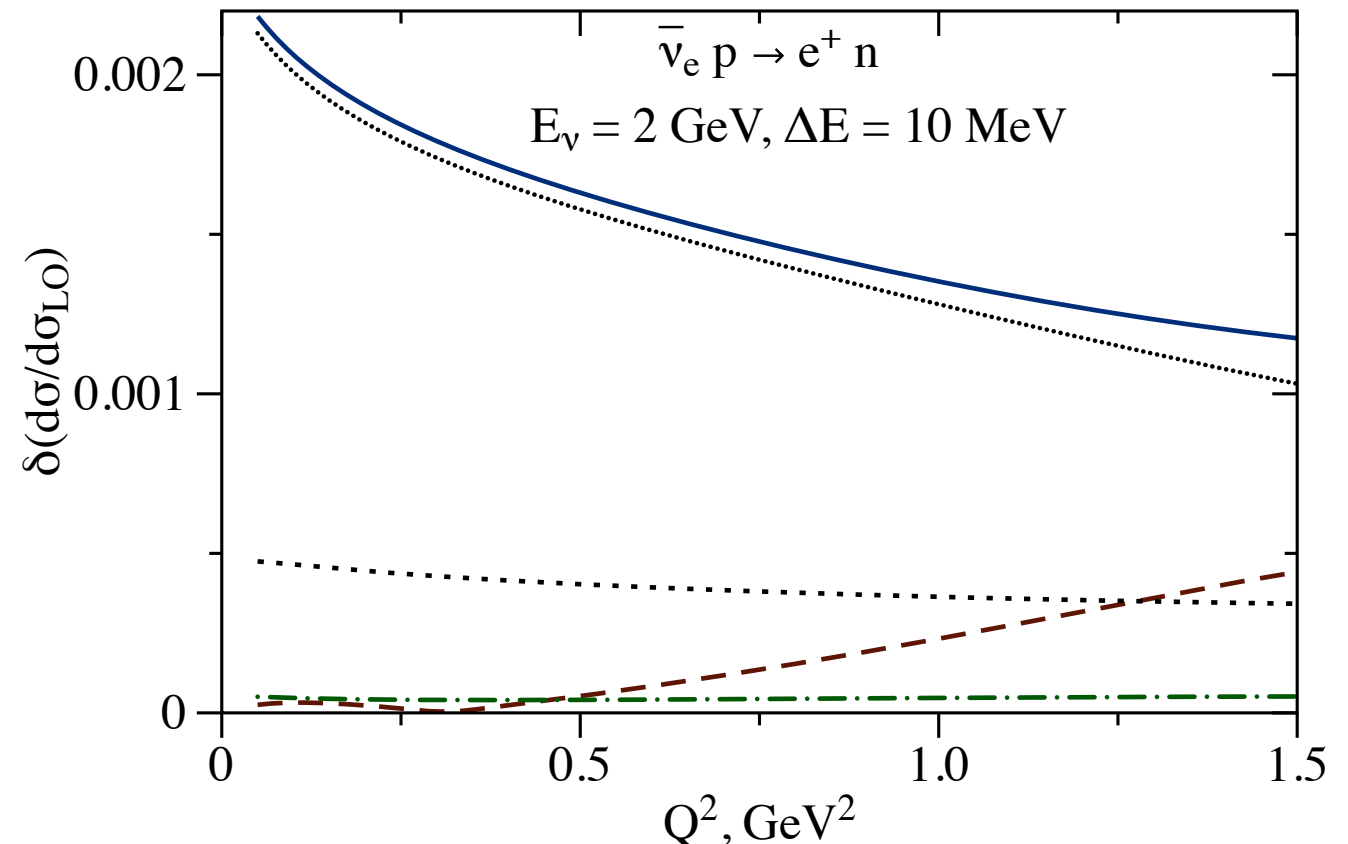
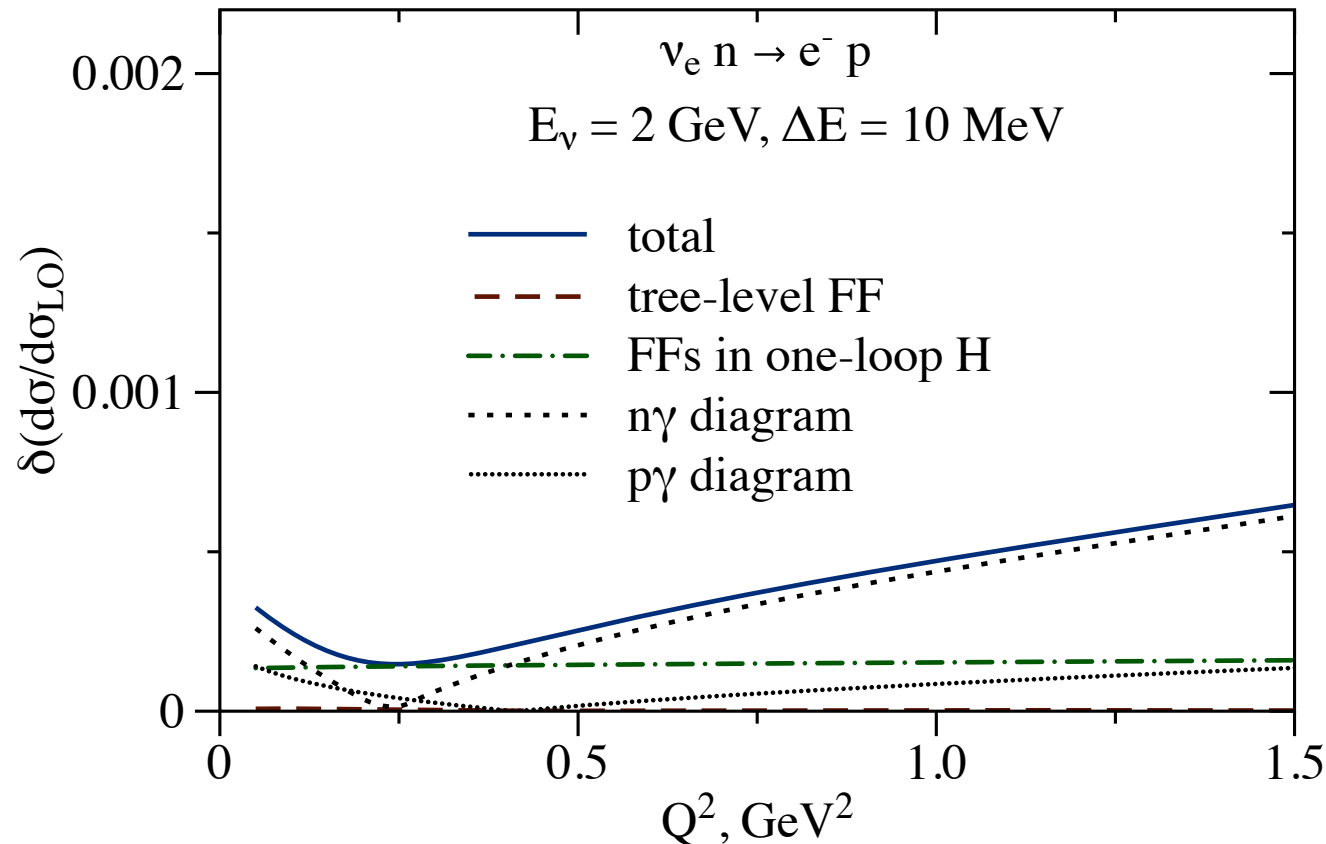
$$d\sigma \sim S \left(\frac{\Delta E}{\mu} \right) J \left(\frac{m_\ell}{\mu} \right) H \left(\frac{M}{\mu} \right)$$

- 
- determine **hard function** at hard scale by matching experiment or hadronic model to the theory with heavy nucleon
 - **RGE evolution** of the hard function to scales $\Delta E, m_\ell$
 - **soft and collinear functions** are evaluated **perturbatively**
 - calculate cross section at low energies accounting for **all large logs**
ep scattering with soft radiation only: Richard J. Hill (2016)

- **soft and collinear functions** determined **analytically**
- **hard function** describes physics at GeV energies

Error budget

- uncertainties from hard function



Meyer, Betancourt, Gran and Hill (2016)

- nucleon form factors

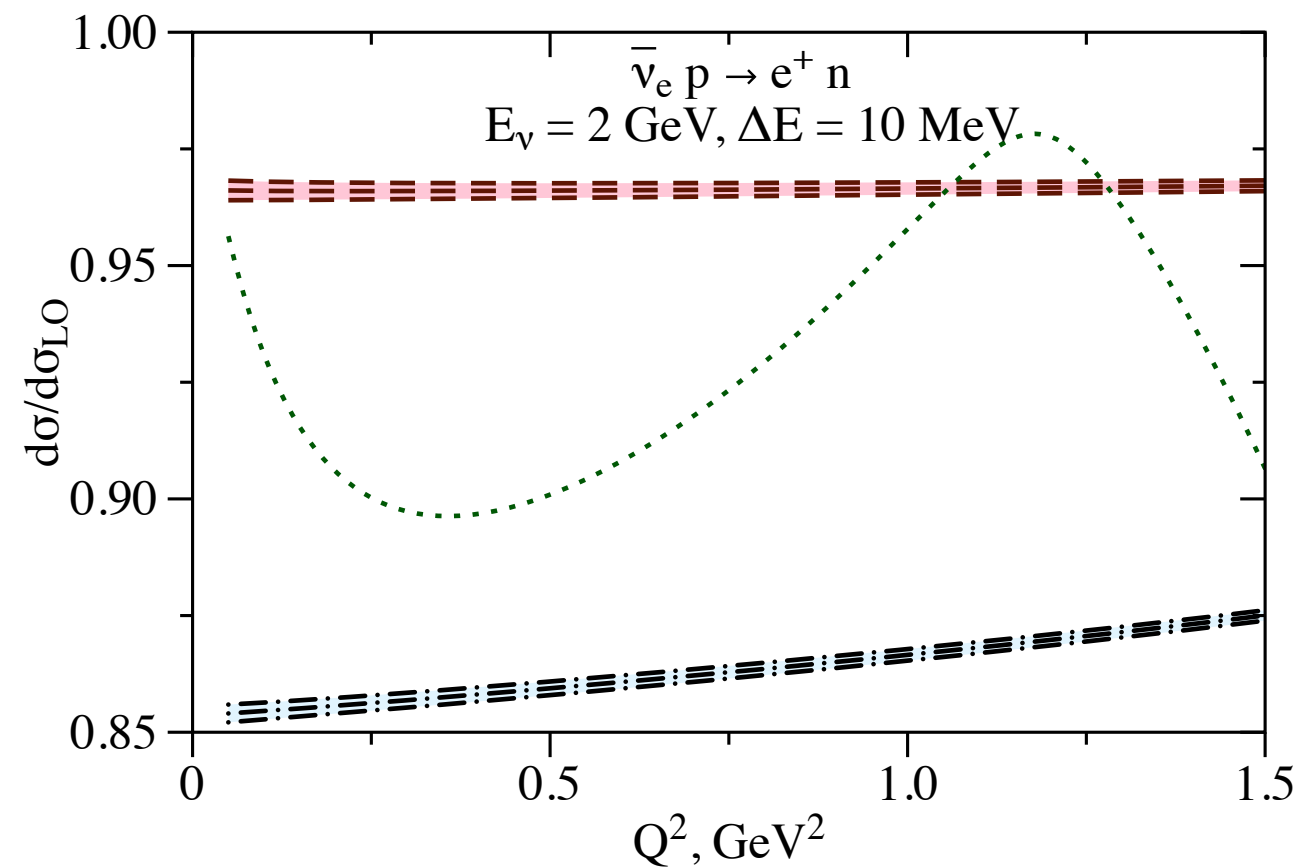
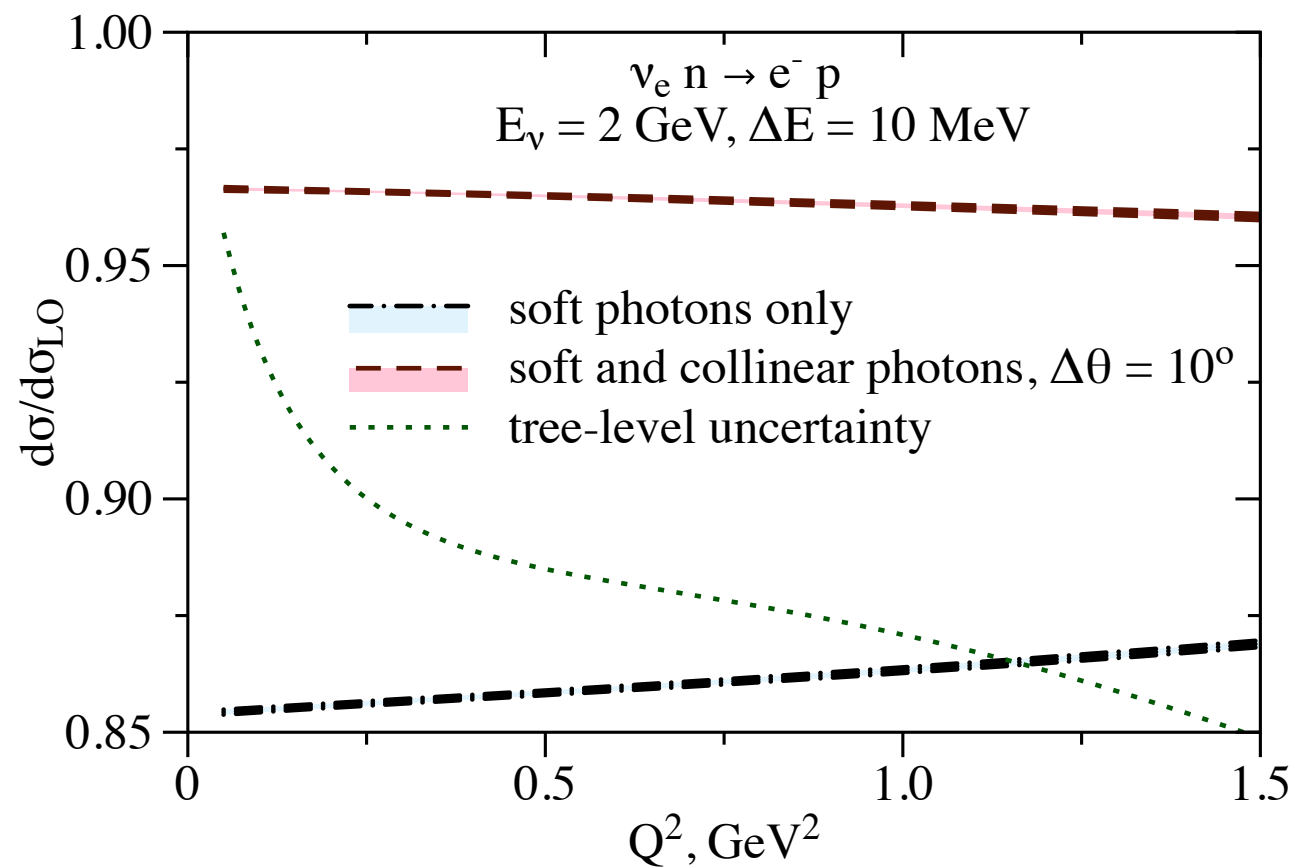
Kaushik Borah, Gabriel Lee, Richard J. Hill and O.T. (2020)

- add perturbative uncertainty by variation of scale

- uncertainty of permille level for the ratio to LO result

Cross section. Electron flavor

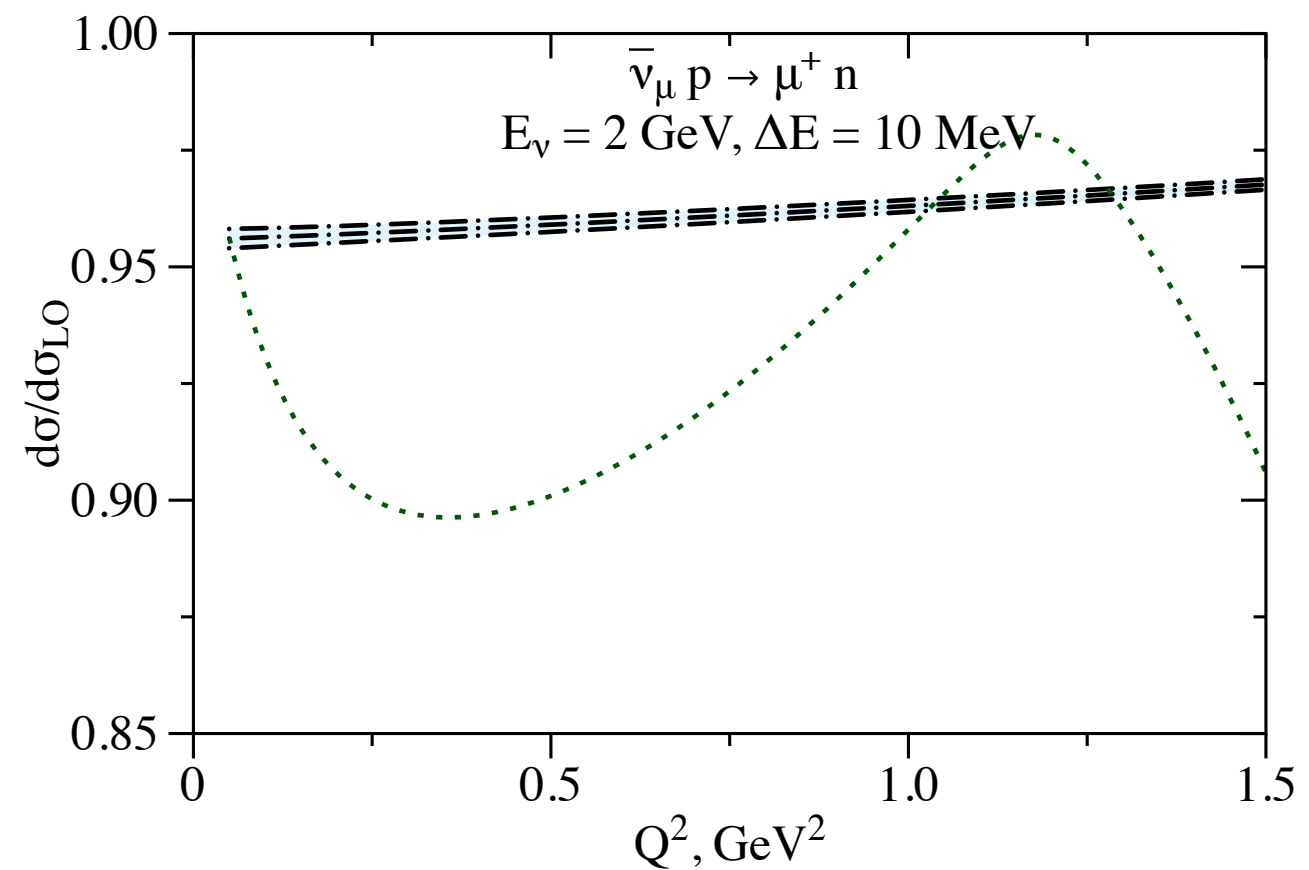
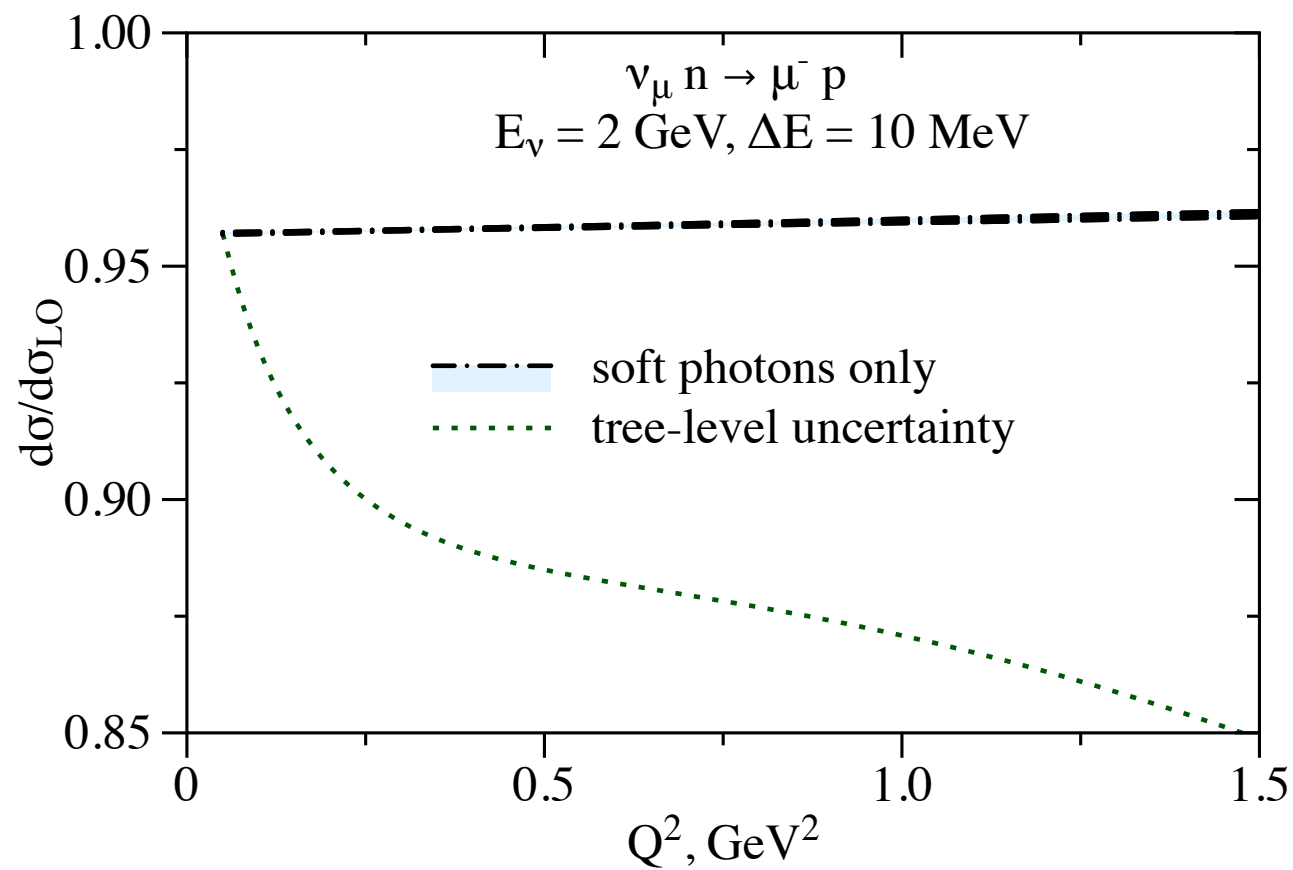
- exclusive observables



- ratio to LO: cancellation of uncertainty from hard function

Cross section. Muon flavor

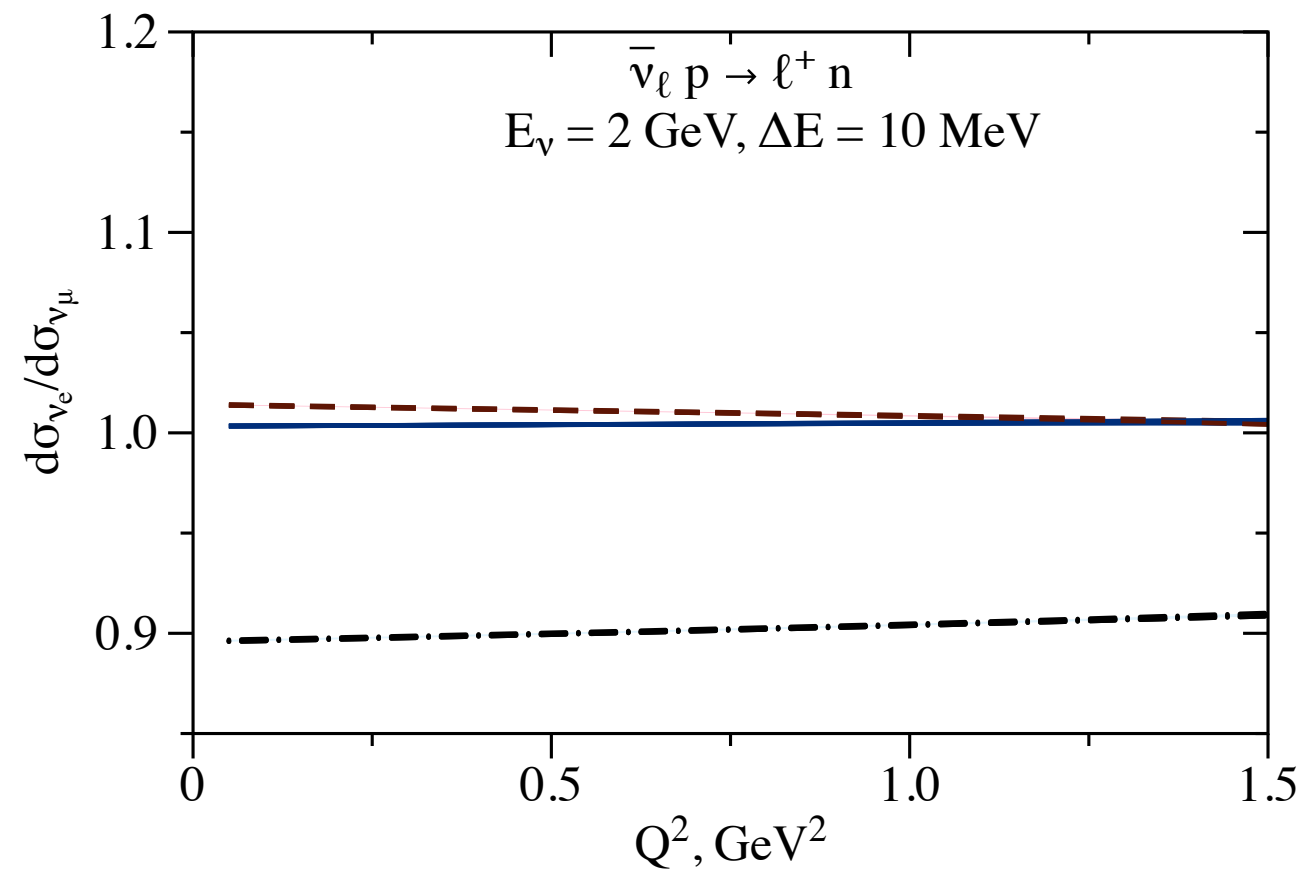
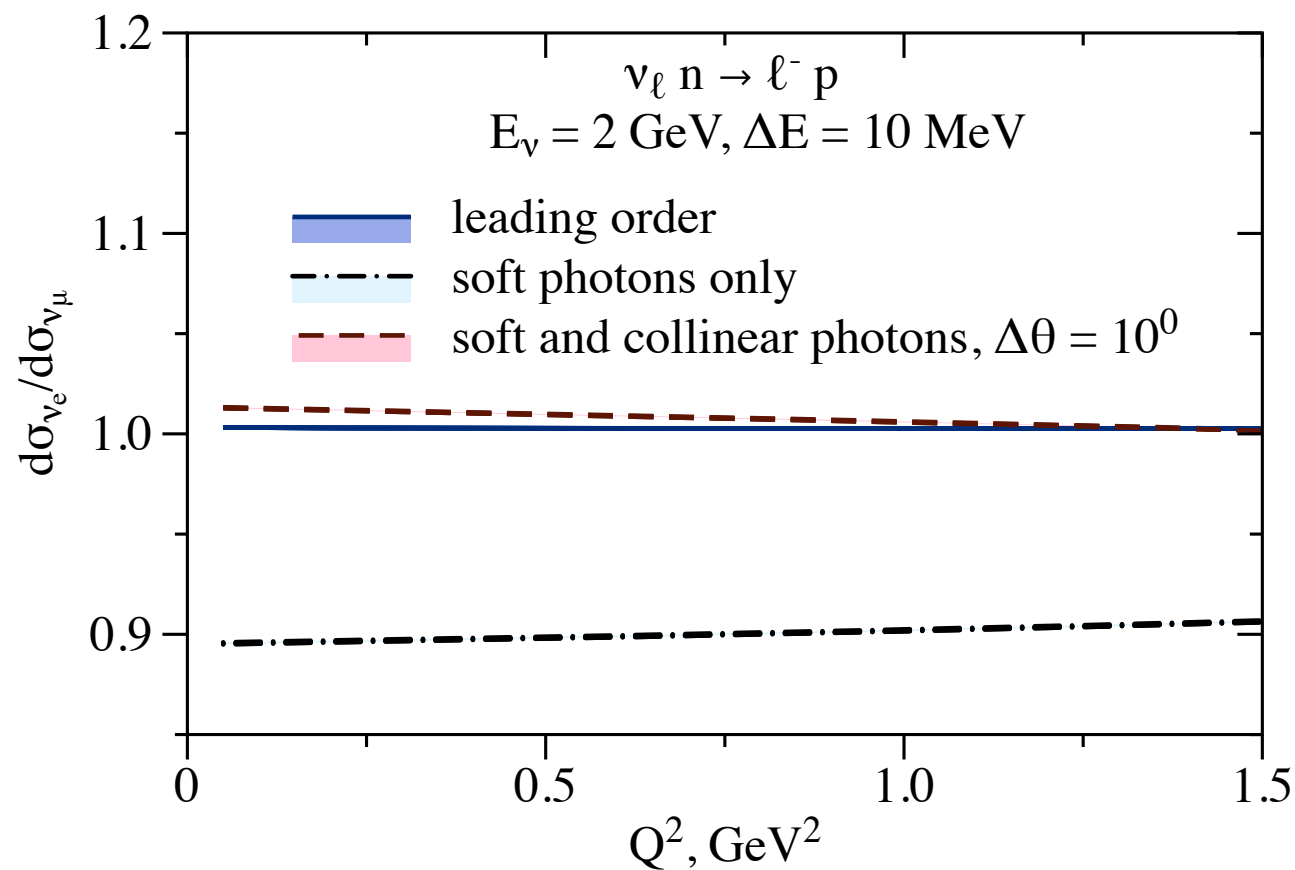
- exclusive observables



- ratio to LO: cancellation of uncertainty from hard function

Electron/muon ratio

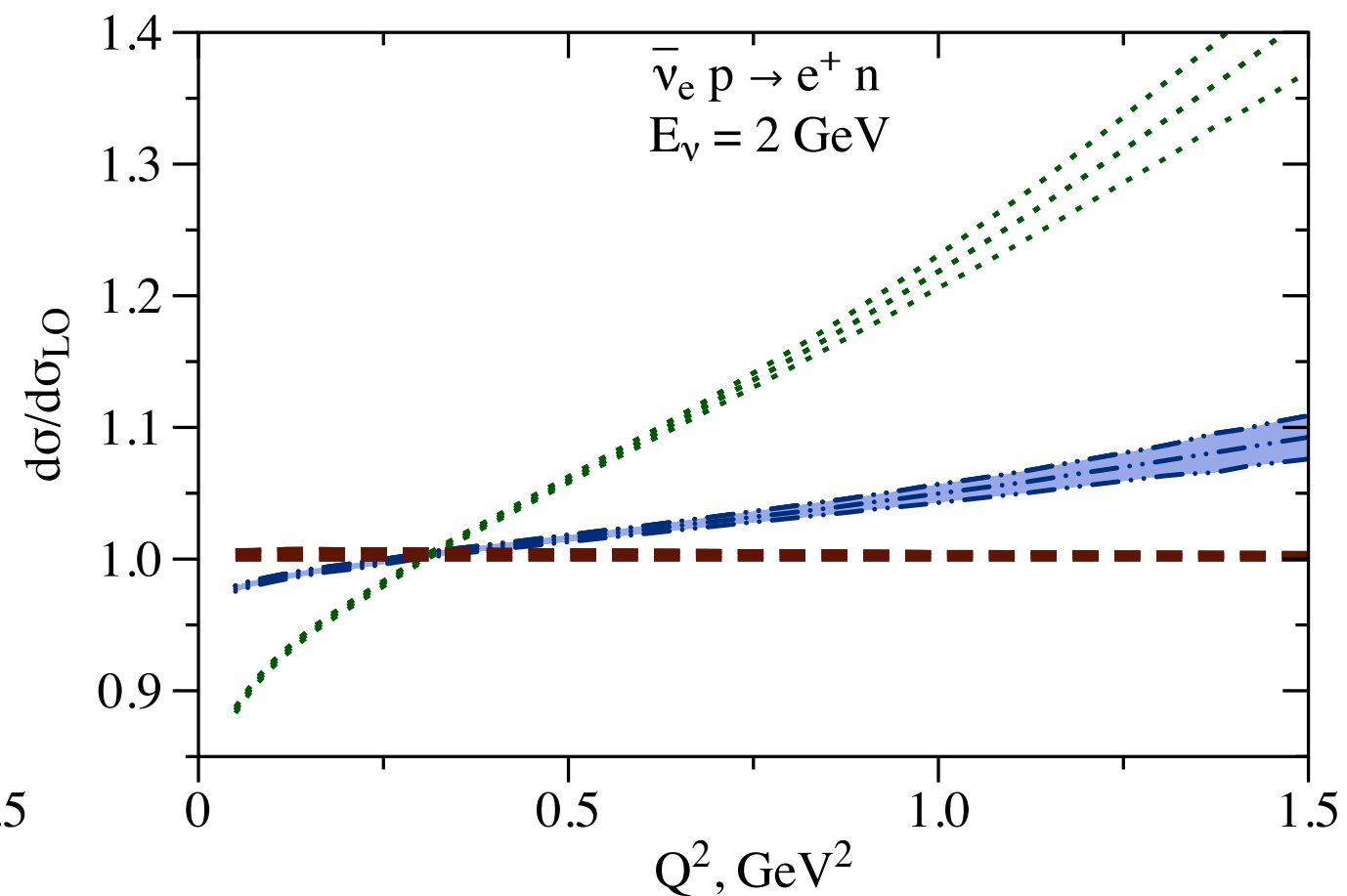
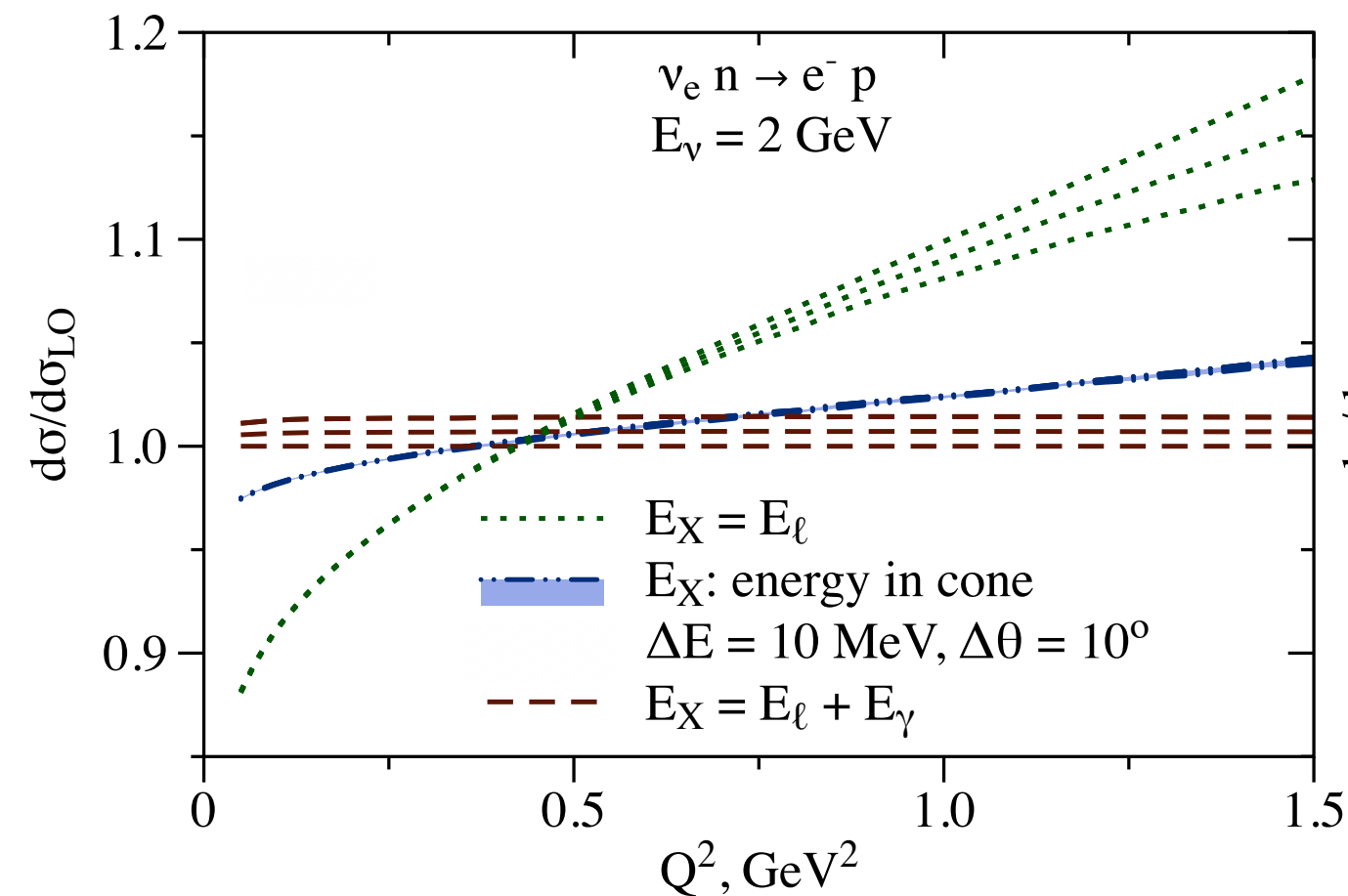
- exclusive observables



- small uncertainty: hard function does not depend on mass

Cross section. Electron flavor

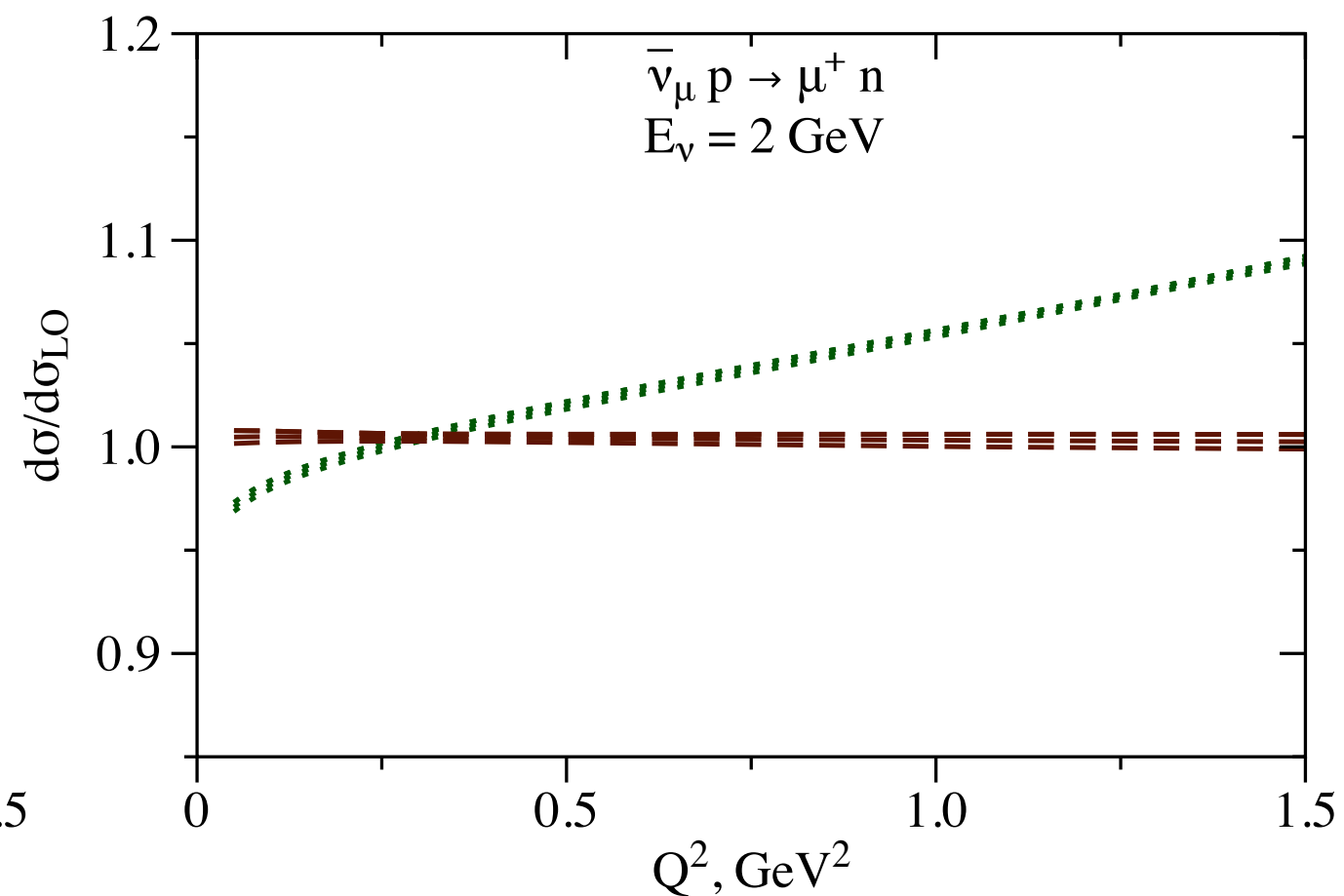
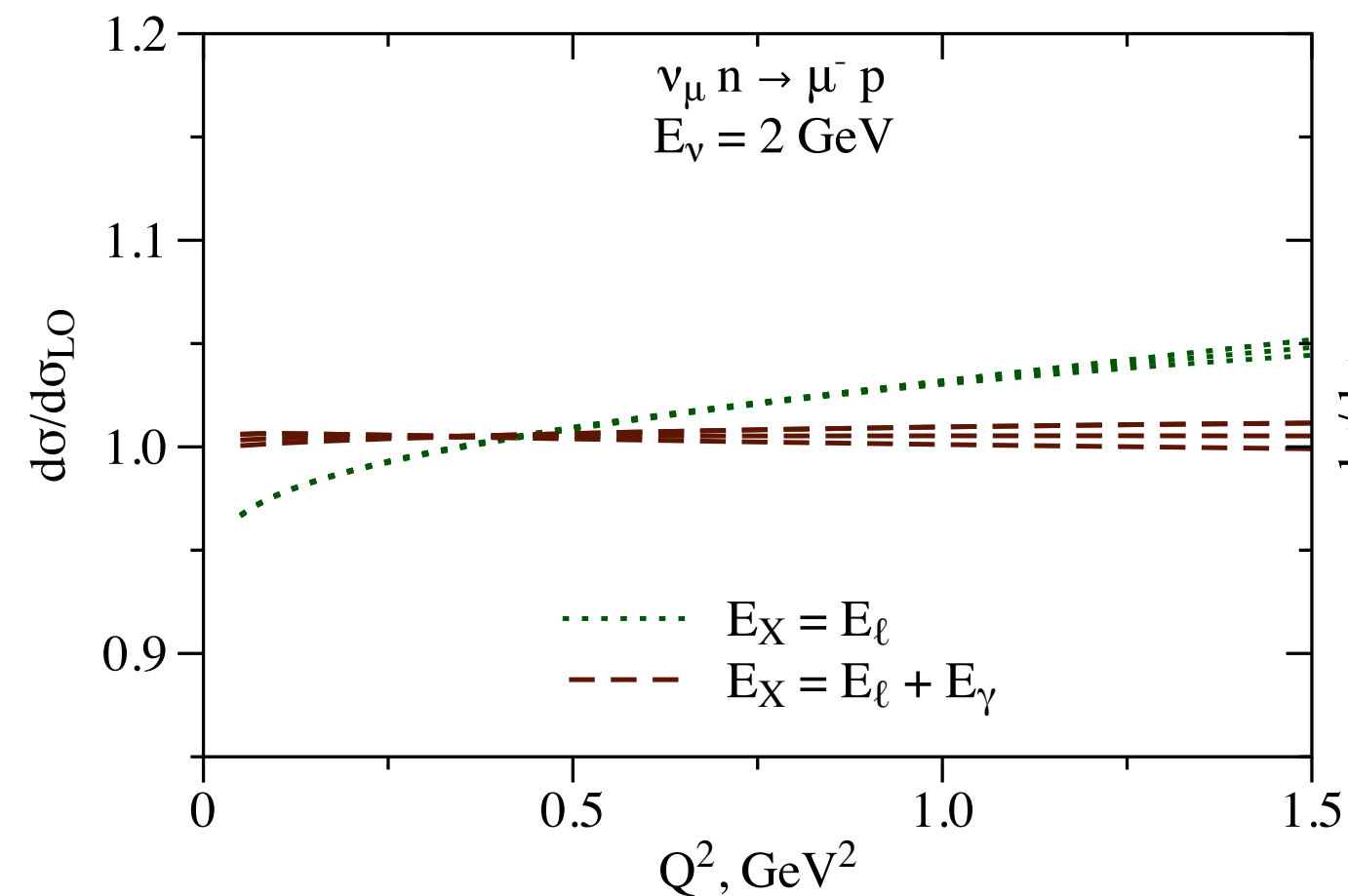
- kinematics $Q^2 = 2M(E_\nu - E_X)$ is reconstructed with 3 different E_X
- inclusive observables



- dependence on reconstruction of kinematics and cuts

Cross section. Muon flavor

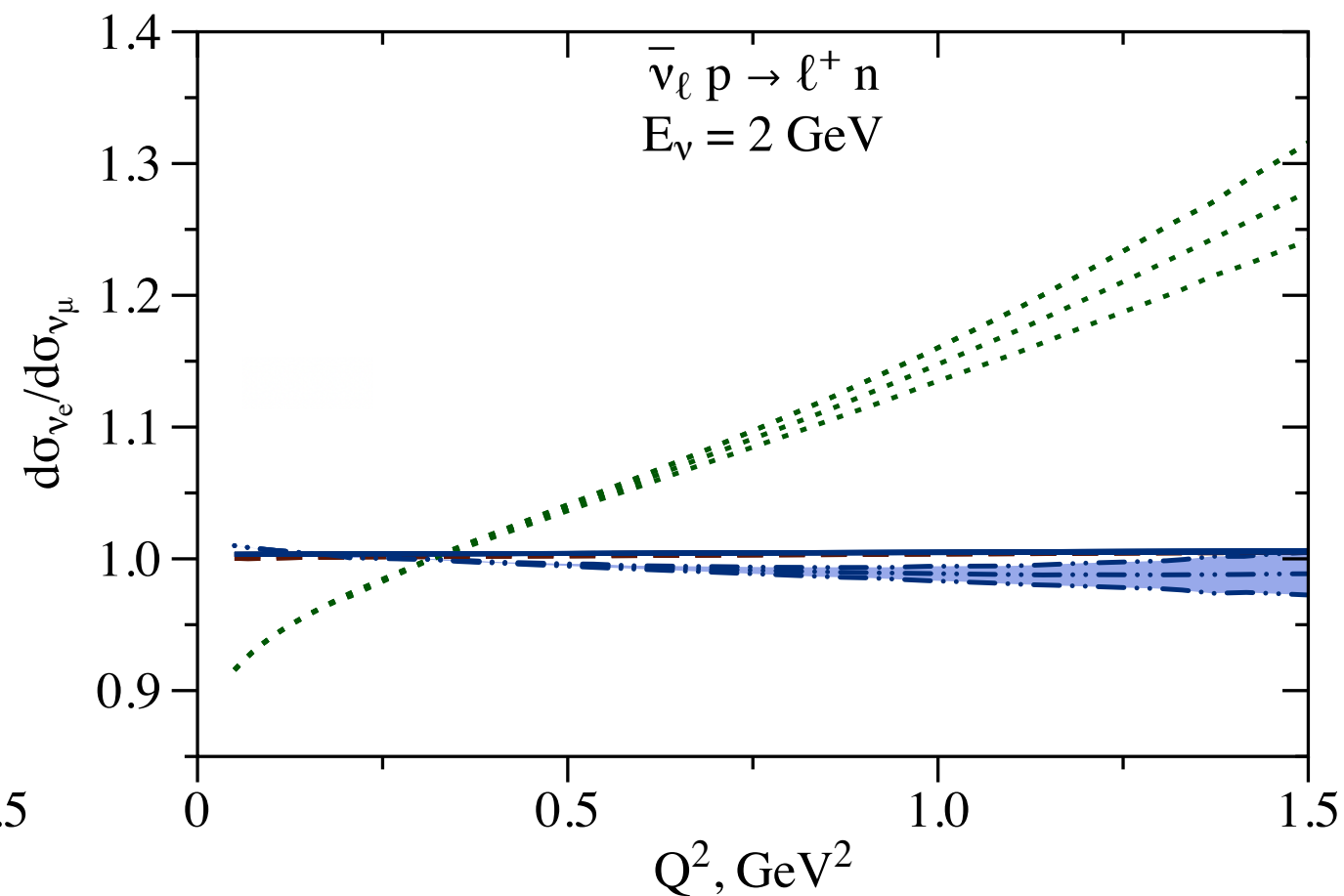
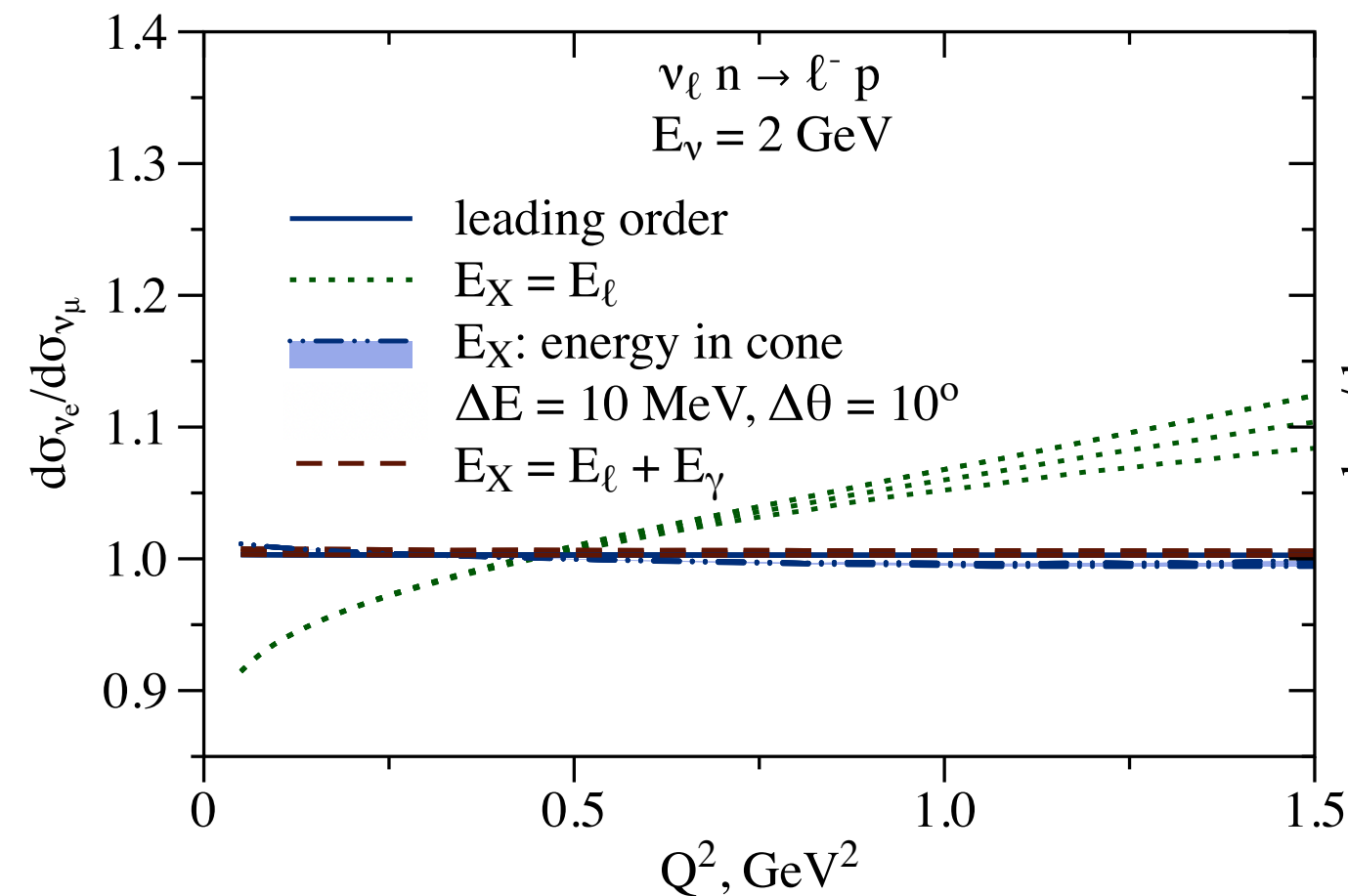
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Electron/muon ratio

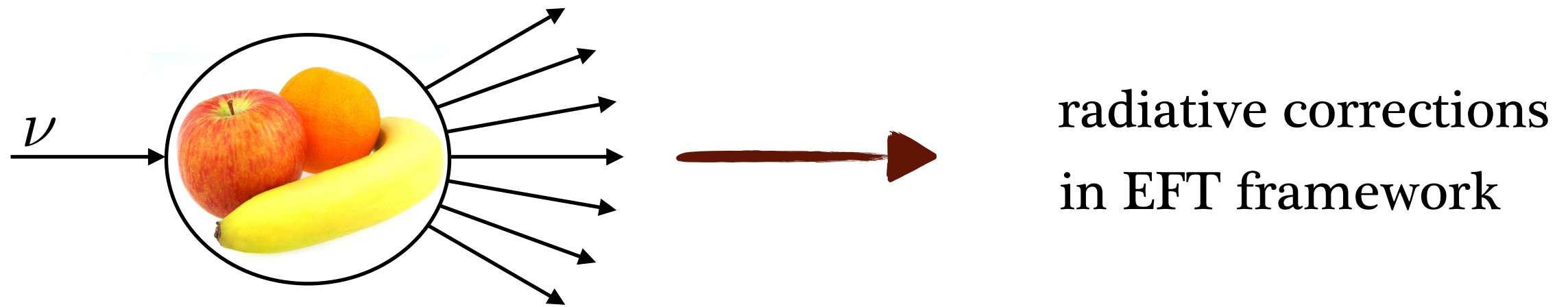
- kinematics $Q^2 = 2M(E_\nu - E_X)$ is reconstructed with 3 different E_X
- inclusive observables



- predict σ_{ν_e} from σ_{ν_μ} measurements with neutrino beam



Conclusions



- radiative corrections to neutrino-nucleon cross sections in factorization framework
- model for the hard function
- σ_{ν_e} can be predicted from σ_{ν_μ} measurements with neutrino beam

Thanks for your attention !!!



This presentation is based upon work
that is supported by the Visiting Scholars Award Program
of the Universities Research Association