

Narrow ($c\bar{c}$) above Flavor Threshold

B_c excited states

(Stable) Doubly Heavy Tetraquarks

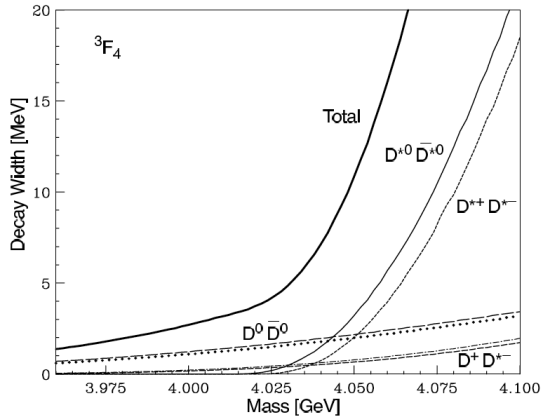
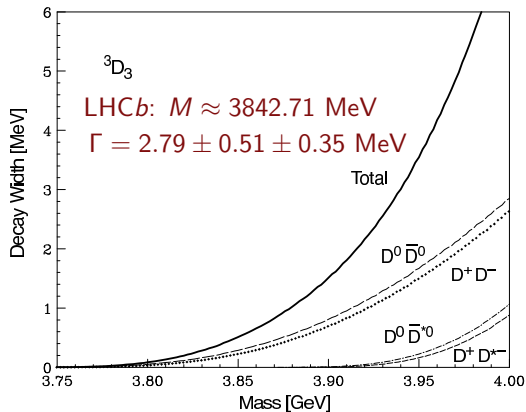
Chris Quigg

Fermilab & TUM

Deciphering strong interactions . . . · MIAPP / Garching · October 25, 2019

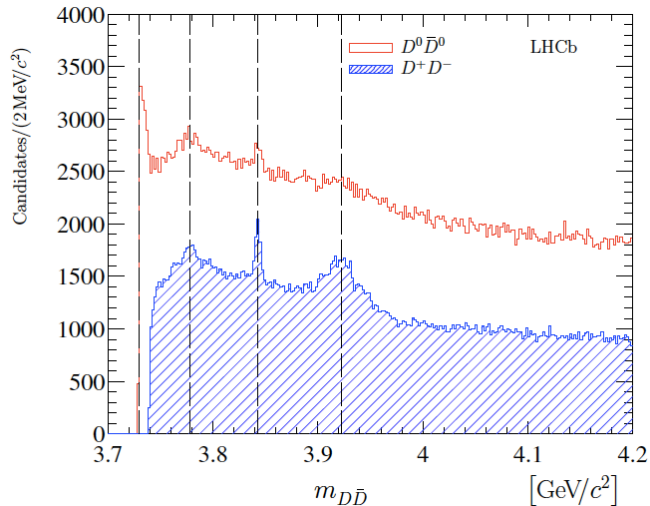
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Narrow ($c\bar{c}$) states above flavor threshold



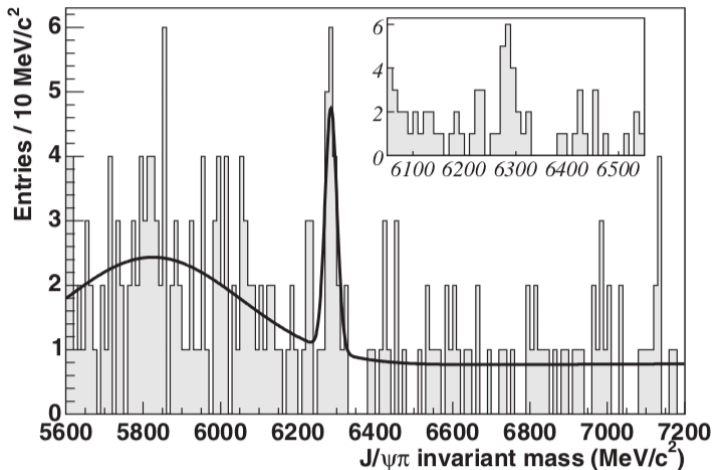
Eichten, Lane, Quigg, Phys. Rev. D **69**, 094019 (2004) / hep-ph/0401210.

LHCb observation of 3D_3 candidate



Can we find 3F_4 , perhaps near 4054 MeV?

Reconstruction of B_c meson (CDF, 2006)



$$M(B_c) = 6274.9 \pm 0.8 \text{ MeV} \text{ (Test of lattice QCD prediction)}$$

Mesons with beauty and charm: stress test for NRQM, LQCD

B_c : weak decays only

$b \rightarrow c$ $c \rightarrow s$ $b\bar{c} \rightarrow W^-$

$B_c \rightarrow J/\psi\pi$: ($Q\bar{Q}$) transmutation

Rich ($b\bar{c}$) excitation spectrum;
interpolates J/ψ , Υ (\neq masses)

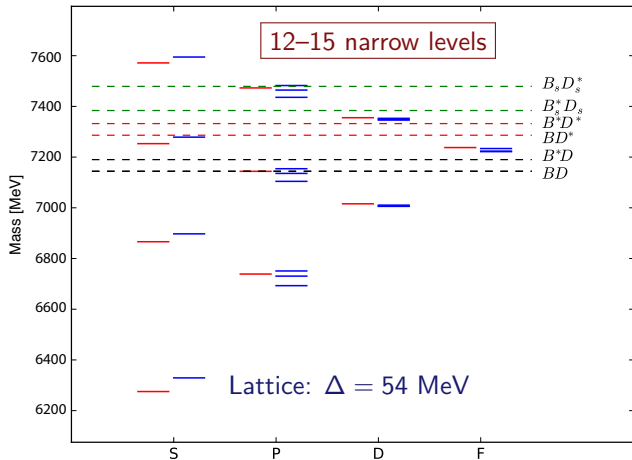
Excited states below $BD \rightarrow B_c + \dots$

$B_c(2S) \rightarrow B_c(1S) + \pi\pi$

P states: γ transitions

Many states observable at LHC, TeraZ

Update: Eichten & CQ (2019)
using “frozen- α_s ” potential, new
approach to spin splittings



Observing the B_c spectrum: $\pi\pi$ transitions

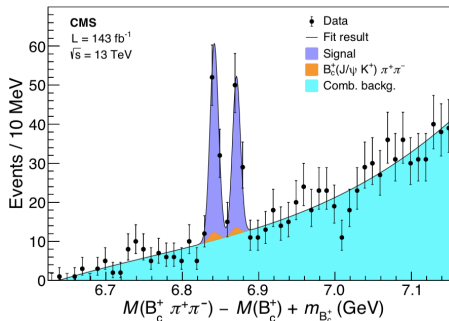
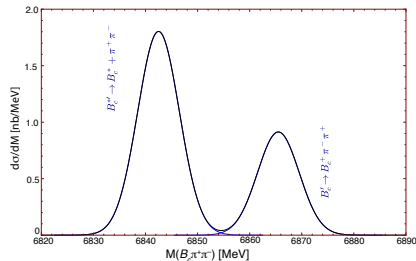
Combine predicted production rates (BCVEGPY2.2) with calculated branching fractions to obtain expectations for $\pi\pi$ transition rates
 \leadsto peak heights: $B_c^{*'} / B_c' \approx 2.5$

M1 $B_c^* \rightarrow \gamma B_c$ unobserved

$$[M(B_c^{*'}) - M(B_c')] - [M(B_c^*) - M(B_c)] \approx -23 \text{ MeV: } B_c^{*'} \text{ lower peak}$$

2S $\rightarrow \pi\pi +$ 1S transitions observed by ATLAS, CMS, LHCb

CMS separation: -29 MeV
 LHCb: -31 MeV



Observing the B_c spectrum: $\pi\pi$ transitions

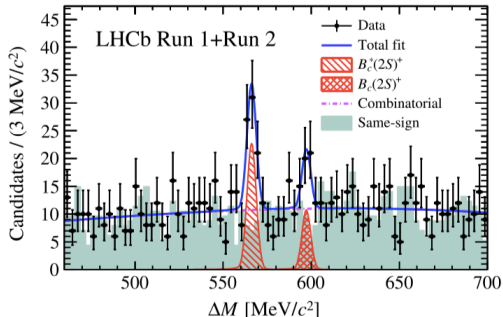
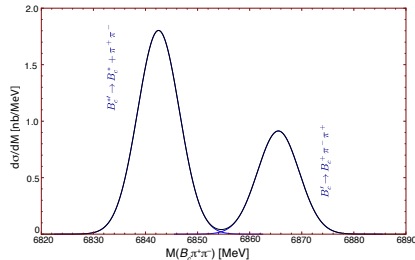
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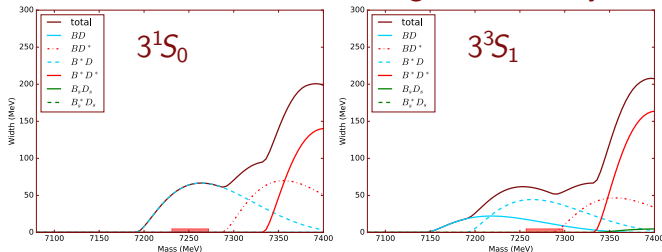
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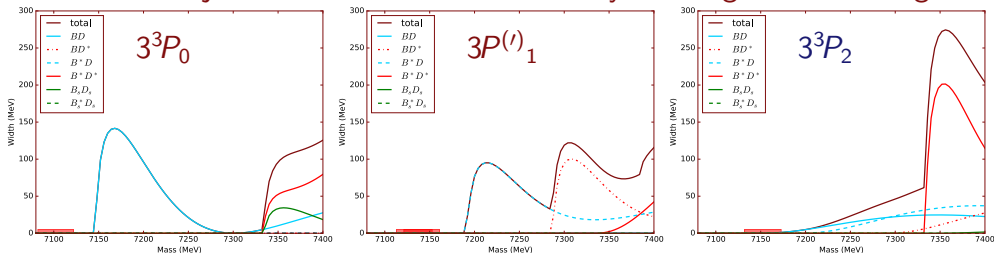


Mesons with beauty and charm: states near flavor threshold

3S states above threshold have significant decay widths



3P states just below threshold; $J = 1$ may have significant mixing



Observing the B_c spectrum: E1 transitions

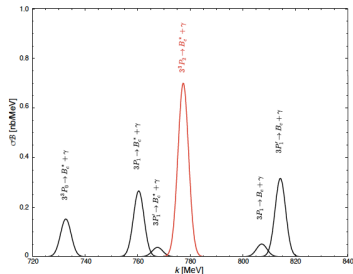
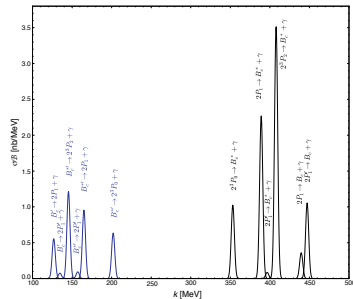
E1 spectroscopy in the $(b\bar{b})$ family:
LHC experiments discovered χ''_{b1}, χ''_{b2} .

Incentive for the search: $2S \rightarrow 2P$ and $2P \rightarrow 1S$ transitions, assuming missing $B_c^* \rightarrow B_c \gamma$ in the reconstruction.

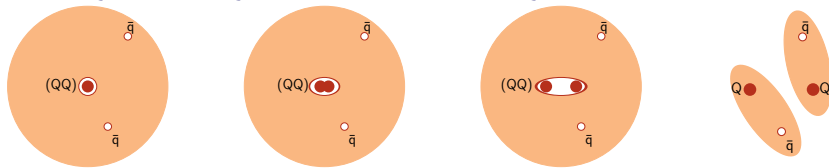
$3S, 3P$ yields $\approx \frac{1}{4} \times 2P \rightarrow 1S$ lines, but higher γ energies may aid detection.

$3^3P_2(7154) \rightarrow B_c^* \gamma(777 \text{ MeV})$

Encourage search for $(3,2)P(b\bar{c})$.



Heavy quark symmetry \Rightarrow stable heavy tetraquarks $Q_i Q_j \bar{q}_k \bar{q}_l$



HQS relates DHTQ mass to masses of QQq , Qqq , $Q\bar{q}$.

Lightest $bb\bar{u}\bar{d}$, $bb\bar{u}\bar{s}$, $bb\bar{d}\bar{s}$ states: (likely) no strong decays.

Heavier $bb\bar{q}_k\bar{q}_l$, $cc\bar{q}_k\bar{q}_l$, $bc\bar{q}_k\bar{q}_l \rightarrow Q\bar{q} + Q\bar{q}$ might be seen as “double-flavor” resonances near threshold.

Observing a weakly decaying double-beauty state would establish the existence of tetraquarks and illuminate the role of heavy color- $\bar{3}$ diquarks as hadron constituents.

Eichten & CQ 1707.09575

Stability in the heavy-quark limit

1) *Dissociation into two heavy-light mesons is kinematically forbidden.*

$$\mathcal{Q} \equiv m(Q_i Q_j \bar{q}_k \bar{q}_l) - [m(Q_i \bar{q}_k) + m(Q_j \bar{q}_l)] =$$
$$\underbrace{\Delta(q_k, q_l)}_{\text{light d.o.f.}} - \frac{1}{2} \left(\frac{2}{3} \alpha_s \right)^2 [1 + O(v^2)] \bar{M} + O(1/\bar{M}) ,$$

$\bar{M} \equiv (1/m_{Q_i} + 1/m_{Q_j})^{-1}$: reduced mass of Q_i and Q_j

$\Delta(q_k, q_l) \xrightarrow{\bar{M} \rightarrow \infty}$ independent of heavy-quark masses

For large enough \bar{M} , QQ Coulomb binding dominates, $\boxed{\mathcal{Q} < 0}$

Stability in the heavy-quark limit

2) *Decay to doubly heavy baryon and light antibaryon?*

$$(Q_i Q_j \bar{q}_k \bar{q}_l) \rightarrow (Q_i Q_j q_m) + (\bar{q}_k \bar{q}_l \bar{q}_m)$$

Core $Q_i Q_j$ is color- $\bar{\mathbf{3}}$, same as \bar{Q}_x . Up to contributions from Q motion and spin interactions,

$$m(Q_i Q_j \bar{q}_k \bar{q}_l) - m(Q_i Q_j q_m) = m(Q_x q_k q_l) - m(Q_x \bar{q}_m)$$

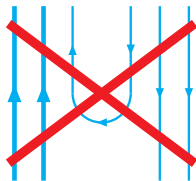
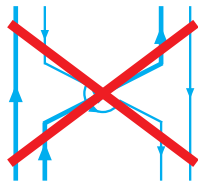
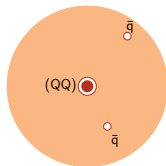
(spin configurations matter)

RHS has generic form $\Delta_0 + \Delta_1/M_{Q_x}$

Using $m(\Lambda_c) - m(D) = 416.87$ MeV and $m(\Lambda_b) - m(B) = 340.26$ MeV, we estimate $\Delta_0 \approx 330$ MeV (asymptotic mass difference).

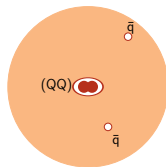
$$\text{All} < m(\bar{p}) = 938 \text{ MeV}$$

No open strong decay channels in the heavy-quark limit!



As $\bar{M} \rightarrow \infty$, stable $Q_i Q_j \bar{q}_k \bar{q}_l$ mesons must exist

Implications for the real world?



$$\langle r^2 \rangle^{1/2} = 0.28 \text{ fm}(cc), 0.24 \text{ fm}(bc), 0.19 \text{ fm}(bb)$$

HQS relations for ground-state tetraquark masses

Assumed: compact diquark, light degrees of freedom “same” for all (QQ)

$$m(Q_i Q_j \bar{q}_k \bar{q}_l) - m(Q_i Q_j q_m) = m(Q_x q_k q_l) - m(Q_x \bar{q}_m)$$

+ finite-mass corrections

RHS is determined from data

One doubly heavy baryon observed, Ξ_{cc} ; others from model calculations*

$$\text{LHCb: } M(\Xi_{cc}^{++}) = 3621.40 \pm 0.78 \text{ MeV}$$

*We adopt Karliner & Rosner, *PRD* **90**, 094007 (2014)

Strong decays $(Q_i Q_j \bar{q}_k \bar{q}_l) \not\rightarrow (Q_i Q_j q_m) + (\bar{q}_k \bar{q}_l \bar{q}_m) \forall$ ground states

Consider decays to pairs of heavy–light mesons case-by-case

Expectations for ground-state tetraquark masses, in MeV

State	J^P	$m(Q_i Q_j \bar{q}_k \bar{q}_l)$	Decay Channel	Q [MeV]
$\{cc\}[\bar{u}\bar{d}]$	1^+	3978	$D^+ D^{*0}$ 3876	102
$\{cc\}[\bar{q}_k \bar{s}]$	1^+	4156	$D^+ D_s^{*+}$ 3977	179
$\{cc\}\{\bar{q}_k \bar{q}_l\}$	$0^+, 1^+, 2^+$	4146, 4167, 4210	$D^+ D^0, D^+ D^{*0}$ 3734, 3876	412, 292, 476
$[bc][\bar{u}\bar{d}]$	0^+	7229	$B^- D^+ / B^0 D^0$ 7146	83
$[bc][\bar{q}_k \bar{s}]$	0^+	7406	$B_s D$ 7236	170
$[bc]\{\bar{q}_k \bar{q}_l\}$	1^+	7439	$B^* D / B D^*$ 7190/7290	249
$\{bc\}[\bar{u}\bar{d}]$	1^+	7272	$B^* D / B D^*$ 7190/7290	82
$\{bc\}[\bar{q}_k \bar{s}]$	1^+	7445	$D B_s^*$ 7282	163
$\{bc\}\{\bar{q}_k \bar{q}_l\}$	$0^+, 1^+, 2^+$	7461, 7472, 7493	$B D / B^* D$ 7146/7190	317, 282, 349
$\{bb\}[\bar{u}\bar{d}]$	1^+	10482	$B^- \bar{B}^{*0}$ 10603	-121
$\{bb\}[\bar{q}_k \bar{s}]$	1^+	10643	$\bar{B} \bar{B}_s^* / \bar{B}_s \bar{B}^*$ 10695/10691	-48
$\{bb\}\{\bar{q}_k \bar{q}_l\}$	$0^+, 1^+, 2^+$	10674, 10681, 10695	$B^- B^0, B^- B^{*0}$ 10559, 10603	115, 78, 136

Cf. M. Karliner & J. L. Rosner model, Phys. Rev. Lett. **119**, 202001 (2017) [arXiv:1707.07666].
 Estimate deeper binding, so additional bc and cc candidates.

Real-world candidates for stable tetraquarks

$J^P = 1^+ \{bb\}[\bar{u}\bar{d}]$ meson, bound by 121 MeV

(77 MeV below $B^- \bar{B}^0 \gamma$)

$\mathcal{T}_{[\bar{u}\bar{d}]}^{\{bb\}}(10482)^- \rightarrow \Xi_{bc}^0 \bar{p}, B^- D^+ \pi^-,$ and $\underbrace{B^- D^+ \ell^- \bar{\nu}}_{\text{manifestly weak!}}$

$J^P = 1^+ \{bb\}[\bar{u}\bar{s}]$ and $\{bb\}[\bar{d}\bar{s}]$ mesons, bound (?) by 48 MeV

(3 MeV below $BB_s \gamma$)

$\mathcal{T}_{[\bar{u}\bar{s}]}^{\{bb\}}(10643)^- \rightarrow \Xi_{bc}^0 \bar{\Sigma}^- \quad \mathcal{T}_{[\bar{d}\bar{s}]}^{\{bb\}}(10643)^0 \rightarrow \Xi_{bc}^0 (\bar{\Lambda}, \bar{\Sigma}^0)$

Unstable doubly heavy tetraquarks

Resonances in “wrong-sign” (double flavor) combinations DD, DB, BB ?

$J^P = 1^+ \mathcal{T}_{[\bar{d}\bar{s}]}^{\{cc\}++}(4156) \rightarrow D^+ D_s^{*+}$: *prima facie evidence* for non- $q\bar{q}$ level

Double charge / double charm

(New kind of resonance: no attractive force at the meson–meson level.)

Also, $1^+ \mathcal{T}_{\{\bar{q}_k\bar{q}_l\}}^{\{bb\}}(10681)^{0,-,--}, \mathcal{Q} = +78 \text{ MeV}$ $1^+ \mathcal{T}_{[\bar{u}\bar{d}]}^{\{bc\}}(7272)^0, \mathcal{Q} = +82 \text{ MeV}$
 $0^+ \mathcal{T}_{[\bar{u}\bar{d}]}^{\{bc\}}(7229)^0, \mathcal{Q} = +83 \text{ MeV}$ $1^+ \mathcal{T}_{[\bar{u}\bar{d}]}^{\{cc\}}(3978)^+, \mathcal{Q} = +102 \text{ MeV}$

Homework for experiment

1. Look for double-flavor resonances near threshold.
2. Discover and determine masses of doubly-heavy baryons.
needed to implement HQS calculation of tetraquark masses
intrinsic interest in these states:
compare heavy–light mesons, possible core excitations
Resolve Ξ_{cc}^+ uncertainty (SELEX/LHCb)
3. Measure cross sections for final states containing 4 heavies:
 B_c , QQq baryons, $Q_i\bar{Q}_i Q_j\bar{Q}_j$.
4. Find stable tetraquarks through weak decays. Lifetime: \sim ps ??

Homework for theory

1. Develop expectations for production. A. Ali talk
2. Refine lifetime estimates for stable states.
3. Understand how color configurations evolve with QQ (and $\bar{q}\bar{q}$) masses. J.-M. Richard, et al., Phys. Rev. C **97**, 035211 (2018) [1803.06155];
A. Czarnecki, B. Leng and M. B. Voloshin, Phys. Lett. B **778**, 233 (2018) [1708.04594];
C. Hughes, E. Eichten and C. T. H. Davies, Phys. Rev. D **97**, 054505 (2018) [1710.03236];
+ ongoing lattice QCD studies (Marc Wagner talk).
4. Investigate stability of different body plans in the heavy-quark limit.
... up to $(Q_i Q_j)(Q_k Q_l)(Q_m Q_n)$: $B = 2$, but $Q_p Q_q Q_r$ color structure?