Is the CMB telling us that dark matter is weaker than weakly interacting?

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If moduli, or other long-lived heavy states, decay in the early universe in part into light and feebly interacting particles (such as axions), these decay products could account for the additional energy density in radiation that is suggested by recent measurements of the CMB. These moduli decays will also, however, alter the expansion history of the early universe, potentially diluting the thermal relic abundance of dark matter. If this is the case, then dark matter particles must annihilate with an even lower cross section than required in the standard thermal scenario ((σv) ≪ 3 × 10^{-26} cm^{3}/s) if they are to make up the observed density of dark matter. This possibility has significant implications for direct and indirect searches for dark matter.

Among other cosmological parameters, the patterns of the temperature fluctuations in the cosmic microwave background (CMB) can be used to determine the energy density of relativistic particles in the early universe. This is typically described in terms of the effective number of neutrino species, N_{\text{eff}}. Although the standard model with three light neutrino species predicts a value of N_{\text{eff}} = 3.046, measurements of the CMB [1][2], when combined with those of the Hubble constant [3][4] and baryon acoustic oscillations in the matter power spectrum [7][11], appear to favor a somewhat higher value: N_{\text{eff}} = 3.52^{+0.48}_{-0.45} (at the 95% confidence level) [1]. If these indications of N_{\text{eff}} > 3.046 are supported by future measurements, it would imply that the early universe contained a higher energy density in relativistic particles than can be accounted for in the standard model. Exotic particle species that could potentially account for this energy density is sometimes referred to as dark radiation.

A natural way to generate dark radiation is through the decays of long-lived massive particles [12][31] (for a review, see Ref. [32]). A particularly well motivated example of such particles are moduli, which are generally expected within the context of string theory, with various theoretical arguments favoring a mass range of m_{\Phi} \sim 10^4 - 10^7 GeV [33][37] (moduli lighter than tens of TeV are in conflict with the successful predictions of big bang nucleosynthesis [37][40]). Although we will limit our discussion to the case of decaying moduli, our conclusions apply to any very heavy, unstable state with highly suppressed interactions.

If moduli exist, they will naturally come to dominate the universe’s energy density (see, for example, Refs. [37][38][40]) and will reheat the universe upon their decay. Moduli, or other states with Planck-scale suppressed couplings, decay at a rate given by:

\[ \Gamma = \frac{1}{4} \frac{m_{\Phi}^3}{(M_{\text{Pl}}/\kappa)^2}, \]  

where \( \kappa \) is a model dependent order one factor, and \( M_{\text{Pl}} = 2.435 \times 10^{18} \) GeV is the reduced Planck mass. This corresponds to a lifetime of \( \tau \simeq 0.05 \text{ sec} \times (1/\kappa)^2 (100 \text{ TeV} / m_{\Phi})^3 \). The decays of these moduli produce relativistic particles and entropy, reheating the universe to a temperature given by:

\[ T_{\text{rh}} = \kappa \left( \frac{5 B_{\text{SM}}}{2 \pi^4 g_{\ast}(T_{\text{rh}})} \right)^{1/4} \left( \frac{m_{\Phi}^2}{M_{\text{Pl}}} \right)^{1/2}, \]  

where \( B_{\text{SM}} \) is the fraction of moduli decays that produce standard model particles, and \( g_{\ast}(T_{\text{rh}}) \) is the number of degrees-of-freedom evaluated at the temperature of reheating. This relationship is shown in the left frame of Fig. [1] for \( \kappa = 1 \). If the moduli decay not only to standard model particles, but also a fraction of the time, \( B_{\text{a}} = 1 - B_{\text{SM}} \), to very light and feebly interacting particles (such as axions, hidden sector photons, etc.), those particles will contribute to the energy density in radiation in the early universe, altering the observed value of N_{\text{eff}} [28][42]:

\[ \Delta N_{\text{eff}} = \frac{43}{7} \frac{B_{\text{a}}}{1 - B_{\text{a}}} \left( \frac{g_{\ast}(T_{\text{decoupling}})}{g_{\ast}(T_{\text{rh}})} \right)^{1/3}, \]  

where \( g_{\ast} \simeq 10.75 \) at the temperature of neutrino decoupling.

In the right frame of Fig. [1] we show the contribution to N_{\text{eff}} predicted in this scenario, as a function of the reheating temperature and the branching fraction for moduli decay to axions (or other dark radiation). We find that for a very wide range of reheating temperatures, branching fractions to axions in the range of \( \sim 2-25\% \) yield contributions comparable to that suggested by CMB observations. Interestingly, moduli branching fractions to axions are naturally expected to be of this order, \( B_{\text{a}} = \mathcal{O}(0.1) \) [42].

The late time decays of moduli or other heavy states can also have a very significant impact on the process of thermal freeze-out of dark matter and on the resulting relic density produced in the early universe [43][45] (for a review, see Ref. [49]). In the standard thermal scenario, weakly interacting dark matter particles freeze-out in a highly radiation dominated universe, at the temperature at which the effects of Hubble expansion first over-
FIG. 1: Left frame: The temperature to which moduli decays reheat the universe, as a function of moduli mass, for the case of $\kappa = 1$. Right frame: The contribution from moduli decay to the effective number of neutrino species, $\Delta N_{\text{eff}}$, as a function of the reheating temperature and the branching fraction for moduli decays into axions or other dark radiation. For a wide range of reheating temperatures (and moduli masses), branching fractions on the order of 10% for moduli to decay to dark radiation can accommodate the value favored by recent CMB data, $\Delta N_{\text{eff}} = 0.474^{+0.48}_{-0.45}$ (95% CL).

come those of annihilation ($T_{\text{FO}}$). If there exist, however, a long-lived massive particle species with couplings too feeble to be maintained in thermal equilibrium (e.g. moduli), they will naturally come to dominate the energy density of the universe (this can be seen by simply comparing the scalings of the densities of relativistic and non-relativistic particles, $\rho \propto a^{-4}$ and $\rho \propto a^{-3}$, respectively). If these decays reheat the universe to a temperature that is below that of the dark matter’s freeze-out temperature, then the expansion rate of the universe will be faster during the period of time between freeze-out and reheating, diluting the density of dark matter by a factor of $(T_{\text{rh}}/T_{\text{FO}})^3$.

For illustration, consider dark matter within a simple supersymmetric scenario: a 200 GeV bino-like neutralino dark matter candidate, 2 TeV squarks and gluinos (to evade LHC constraints [50]), 700 GeV for all other mass parameters, $\tan \beta = 10$, and a value of the top trilinear coupling chosen to accommodate the observed mass of the light Higgs. If it were not for cosmological constraints, such a model would be perfectly reasonable. But, assuming the standard thermal history, the neutralino relic abundance predicted in this model is $\Omega_\chi h^2 \approx 5.1$ [51], well above the measured value of 0.12. And although we can bring this model into line with the observed cold dark matter density by simply lowering the higgsino mass to $\mu \approx 240$ GeV, leading to a mixed bino-higgsino neutralino with sufficient couplings to avoid being overproduced in the early universe, these same couplings also increase the dark matter’s spin-independent elastic scattering cross section with nuclei to $3.4 \times 10^{-44}$ cm$^2$, which is almost an order of magnitude larger than the upper limit placed by the XENON-100 collaboration [52].

The above example illustrates two key points. First, while the “WIMP miracle” has provided a great deal of motivation for dark matter candidates with weak-scale masses and interactions, in many theoretical frameworks (including minimal supersymmetry) the connection between electroweak-scale physics and the measured dark matter abundance is very tenuous. The vast majority of the otherwise viable supersymmetric parameter space predicts a thermal relic abundance of neutralinos that is in considerable excess of the observed dark matter density. Second, if one naively increases the couplings of their dark matter candidate to avoid being thermally overproduced in the early universe, this also tends to increase the dark matter’s elastic scattering cross section with nuclei to values above current experimental constraints. Only in rather special regions of parameter space, such as those in which the lightest neutralino efficiently co-annihilates with another nearly-degenerate sparticle (such as a stau, chargino, or stop) [53] or annihilates through a somewhat fine-tuned resonance [53–55], can the observed dark matter abundance match the predicted thermal relic density without exceeding the constraints placed by direct detection experiments.\(^1\) Note that these arguments are not limited to the specific case of neutralino dark matter, but apply to a broad range of weakly interacting dark matter candidates (for example, see Ref. [56]).

We reach a very different conclusion, however, if we consider the same supersymmetry model within the context of a scenario with a low reheating temperature induced by moduli decay. A 200 GeV neutralino will undergo thermal freeze-out at a temperature of approximately $T_{\text{FO}} \approx m_\chi/20 \approx 10$ GeV. From Fig. 1, we see

\(^1\) There also exist regions of supersymmetric parameter space in which a mixed gaugino-higgsino can satisfying these constraints [57–59], although direct detection experiments should be able to exclude such models in the near future if no signal is detected [60, 61].
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FIG. 2: The annihilation cross section, thermally averaged at the temperature of freeze-out, required for a particle to generate the observed cosmological dark matter abundance, as a function of the reheating temperature. For high reheating temperatures, \( T_{rh} > T_{FO} \), we recover the standard value expected for a thermal relic. For lower reheating temperatures, viable dark matter candidates must annihilate with smaller cross sections than are predicted in the standard scenario.

than for moduli lighter than \( \sim 20 \) PeV, the decays will reheat the universe to a temperature below the freeze-out temperature, and thus will significantly dilute the abundance of neutralinos. Considering \( m_{\Phi} = 10 \) PeV and \( \kappa = 1 \), for example, the moduli decays reheat the universe to a temperature of approximately 2.8 GeV, diluting the neutralino dark matter density by a factor of \( (2.8 \text{ GeV}/10 \text{ GeV})^3 \approx 0.02 \). For the same supersymmetric parameters described two paragraphs above, and for \( \mu \approx 1 \) TeV, this degree of dilution yields a neutralino abundance that is consistent with the measured density of dark matter, and predicts a spin-independent elastic scattering cross section of \( \sigma_{SI} \approx 2 \times 10^{-46} \text{ cm}^2 \), well below current constraints.

In Fig. 2 we show the annihilation cross section (thermally averaged at the temperature of freeze-out) required for a 10 GeV, 100 GeV or 1000 GeV particle to make up the observed dark matter abundance, as a function of the reheating temperature. For reheating temperatures greater than the freeze-out temperature, we recover the standard value for a thermal relic, \( \langle \sigma v \rangle \approx (2 - 3) \times 10^{-26} \text{ cm}^3/\text{s} \). For lower reheating temperatures (corresponding to lower moduli masses), however, lower annihilation cross sections are required; in some cases dramatically lower. If the couplings and exchanged particles responsible for the dark matter’s annihilation cross section are also those (or are related to those) which generate its elastic scattering cross section nuclei, we would expect rates at direct detection experiments to be suppressed by a similar factor.

Throughout this letter, we have assumed that the dark matter abundance is dominated by thermal relics (albeit with a density diluted by late time reheating). Moduli may also produce dark matter particles directly, as non-thermal decay products. In such scenarios, the resulting dark matter will have an annihilation cross section that is larger than predicted in the standard thermal scenario (parametrically, larger by a factor of \( \sim T_{FO}/T_{rh} \)). A well studied example is dark matter in the form of non-thermally produced winos. The large annihilation cross sections predicted for dark matter originating as moduli decay products lead to strong constraints from indirect detection experiments; gamma-ray observations presently limit wino dark matter to \( m_W \gtrsim 700 \) GeV, for example. The combination of such indirect detection constraints and the increasingly stringent limits from direct detection experiments appear to disfavor dark matter that is produced through non-thermal decays, although some scenarios remain viable. Fortunately, it is not difficult to suppress the branching fractions of moduli to superpartners (or, more generally, to the sector carrying the parity or charge that stabilizes the dark matter). For example, despite the fact that supersymmetry requires moduli to have identical couplings to gauge bosons and gauginos, their decay to gauginos is chirality suppressed by a factor of \( (m_\chi/m_\Phi)^2 \). For weak-scale gaugino masses, this naturally leads to very small branching fractions to supersymmetric particles, on the order of \( 10^{-8} \times (1 \text{ PeV}/m_\Phi)^2 \).

At this time, we will summarize the main points made in this letter:

- If moduli (or other long-lived heavy states) decay with an order 10% branching fraction to axions (or other very light and feebly interacting particles), this could account for the “dark radiation” suggested by recent CMB observations, \( N_{eff} = 3.52_{-0.45}^{+0.48} \) (95% CL) > 3.046.
- If the moduli have a mass in the range of tens of TeV to tens of PeV, they will alter the expansion history of the universe, resulting in the dilution of the thermal abundance of dark matter particles.
- When this dilution is taken into account, we find that the dark matter’s annihilation cross section must be smaller, and possibly much smaller, than predicted in the standard thermal scenario.
- If the particles exchanged in the process of dark matter annihilation are also those responsible for elastic scattering with nuclei, then we also expect lower rates in direct detection experiments than would be predicted in the standard thermal scenario.
- Whereas supersymmetric dark matter with a standard thermal history predicts a thermal abundance
of neutralinos that is in considerable excess of the observed dark matter density in all but a few corners of parameter space (such as the focus point, co-annihilation, and resonance regions), the dilution of the thermal abundance via moduli decay opens up a large range of less finely tuned models.

In other words, moduli decay provides a simple and well-motivated way to explain the high value of $\Delta N_{\text{eff}}$ suggested by observations, and such decays will also alter the thermal history of the early universe. Once this is taken into account, we find that dark matter particles may annihilate with a much smaller cross section than is predicted for a standard thermal history — the dark matter may interact more weakly than weak. The prospects for direct and indirect detection may be suppressed in such scenarios, reliving the tension introduced by the null results of XENON100 and other experiments searching for dark matter.

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[50] For an up-to-date summary, see: https://twiki.cern.ch/twiki/bin/view/AtlasPublic/SupersymmetryPublicResults and https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsSUS.

[51] For these calculations, we have used the publicly available tool, micrOEGAS: G. Belanger, F. Boudjema, A. Pukhov, A. Semenov, [arXiv:1005.4138 [hep-ph]].


