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Energy and Multiplicity Dependence of Two-Particle
Correlations in 18.5, 100, 200, and 360 GeV/c $\pi^+\pi^-$ Inclusive Reactions

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Abstract

Inclusive and semi-inclusive two-particle rapidity correlations for unlike $(-+)$ and like $(--)$ particle pairs have been studied at $s = 35, 6, 188, 376,$ and 673 GeV^2 . Striking differences in both energy and multiplicity dependence are observed between like and unlike pairs. The $(-+)$ correlations in the central region grow with $\ln s$ and increase with $1/n$ as would be expected for a simple cluster with population $\langle k_0^+ \rangle = 1.60 \pm 0.12$ charged particles per cluster and correlation length $\delta = 0.99 \pm 0.03$. The $(--)$ correlations show no s or n dependence and are consistent with zero except in the region $\phi < 45^\circ$ where Bose-Einstein effects dominate.

Previous investigations¹ have established that central-region hadrons from high energy inclusive reactions are emitted not independently, but in "clusters", correlated in the cms rapidity variable $y = 1/2 \ln\{(E + p_L)/(E - p_L)\}$. Two-particle rapidity correlations are known to be short-range, dependent solely on rapidity difference Δy , and, having been observed for each charge multiplicity separately, cannot be ascribed to the combinatorial effects of inclusive reactions^{2,3}. There are significant differences in correlations between particle pairs of like and unlike charge, particularly when the azimuth-angle separation ϕ is small^{3,4}. When the transverse momenta are approximately the same and aligned ($\phi < 45^\circ$) the correlation observed at small Δy for like-charged pions can be described in terms of Bose-Einstein symmetrization effects of quantum statistics⁵.

Comparatively little is known about hadron clusters. Speculation that conventional resonances could account for most of the correlation observed seems to be ruled out by recent studies⁶. According to the quark-parton picture, the gluons which dominate the central region are driven by the color force to materialize as $q\bar{q}$ color singlets, which may appear as conventional resonances provided there is an appropriate wave function fit, or as clusters ("generalized resonances") if there is not. It has been suggested⁷ that the fundamental cluster parameters $\langle k \rangle$, the average number of charged particles per cluster, and δ , the dispersion parameter or correlation length, could be measured by simultaneously studying the energy and multiplicity dependence of rapidity correlations in the central region, $y_1 = y_2 \approx 0$.

We report the result of a systematic study of the energy and multiplicity dependence of two-particle rapidity correlations in π^-p interactions at 18.5, 100, 200, and 360 GeV/c. The study is based on new data from 30,000 events at 360 GeV/c obtained using the Fermilab 30 in. bubble chamber/wide-gap spark chamber hybrid system, combined with previous data from 17,000 events at 200 GeV/c and 7,700 events at 100 GeV/c obtained with the same apparatus, and 7,800 events at 18.5 GeV/c obtained at BNL. Experimental procedures are described elsewhere^{2,3,8}.

Data at each energy were treated in a consistent manner: events were binned in a $\Delta y = y_1 - y_2$, $y_+ = y_1 + y_2$ coordinate system, in consideration of the fact that correlations are known to depend on rapidity difference. For each charge multiplicity n the single-particle densities $\rho_1(y) = \sigma^{-1} d\sigma/dy$ and the two-particle density $\rho_2(y_1, y_2) = \sigma^{-1} d^2\sigma/dy_1 dy_2$ were computed. The normalized correlation functions $R_n(y_1, y_2) \approx R_n(\Delta y, y_+) = \{\rho_2(y_1, y_2) / (\rho_1(y_1)\rho_1(y_2))\} - 1$ were then determined for each charge multiplicity. The procedure was repeated for the data at each energy.

Semi-inclusive correlations for the 360 GeV/c data are shown for the $(-+)$ pairs and the $(--)$ pairs respectively in Fig. 1(a) and (b). In the case of the unlike $(-+)$ pairs, significant correlation near $\Delta y = 0$ is evident for all orders of the charge multiplicity n , and falls off approximately as $1/n$. For the like-charge $(--)$ pairs⁹ correlation near $\Delta y = 0$ is less prominent, and shows no clear n dependence.

The observed n -dependence for $(-+)$ pairs is consistent with a model⁷ which assumes that clusters are emitted independently, according to the reaction

mechanism which dominates production in the central region, and decay isotropically. When the cluster multiplicity distribution is narrow,

$$R_n(0, 0)^{-+} = \frac{\ln s}{n} \left[\frac{\langle k \rangle^{-+}}{2\delta\sqrt{\pi}} - \frac{\langle k \rangle^{-+}}{\ln s} \right] \quad (1)$$

$$R_n(0, 0)^{--} = \frac{\ln s}{n} \left[\frac{\langle k \rangle^{--} - 1}{2\delta\sqrt{\pi}} - \frac{\langle k \rangle^{--}}{\ln s} \right]. \quad (2)$$

To determine the central-region correlation value $R_n(0, 0)$ with the best statistics the values of $R_n(y_1, y_2)$ along a line of constant y_+ were determined as a function of Δy , and the seven central values¹⁰ of R_n were fitted with a Gaussian function. Fitted values of the $\Delta y = 0$ correlation peak for $y_+ = 0$ and $y_+ = \pm 0.4$ were averaged to obtain $R_n(0, 0)$ for each multiplicity, at each energy.

For the particle pairs of unlike charge, we plot the resulting $R_n(0, 0)^{-+}$ as a function of $1/n$ for the highest-energy data in Fig. 2(a). The energy dependence of $R_n(0, 0)^{-+}$ for $n = 8$ events is shown¹¹ in Fig. 2(b). The narrow-cluster model prediction, eqn. (1), provides an excellent fit to both distributions. Fitting the two distributions jointly yields the measurement of the cluster parameters: $\langle k \rangle^{-+} = 1.60 \pm 0.12$, $\delta = 0.99 \pm 0.03$. Virtually the same values are obtained from the slope and intercept of the distribution of Fig. 2(b) alone¹².

For the particle pairs of like charge, we attempt to distinguish the consequences of Bose-Einstein effects by introducing the $\phi \leq 45^\circ$ cut used in ref. 5. Fig. 1(c) shows the semi-inclusive correlations for the $(--)$ pairs for which $\phi \leq 45^\circ$. Correlations are prominent for all orders of multiplicity, much

more so than in the total (--) sample of Fig. 1(b). For the remaining (-) pairs with $\phi > 45^\circ$ (not shown) there is little evidence of correlation.

To describe (-) particle pairs we introduce the function $R'_n(y_1, y_2) = R_n + (1/n_-)$, which for identical particles is zero in the absence of correlation. $R'_n(0, 0)^{-}$ is shown as a function of $1/n$ for $0 \leq \phi \leq 45^\circ$ and $45^\circ < \phi \leq 180^\circ$ pairs in Fig. 3(a). Neither distribution shows significant n-dependence, and the $\phi > 45^\circ$ correlations are consistent with zero for each multiplicity. The energy dependence of $R'_n(0, 0)^{-}$ for $n = 8$ events is shown in Fig. 3(b). Correlations for the $\phi < 45^\circ$ region show significant s-dependence in contrast to the $\phi > 45^\circ$ region, where correlations are consistent with zero at each energy. We conclude that there is no evidence of significant (-) correlations beyond the Bose-Einstein effect. This is consistent with a model in which the produced clusters contain predominantly two charged particles of opposite sign, and (-) correlations are due to long-range effects between clusters.

If (-) and (-) correlations are a consequence of different mechanisms, as they appear to be, the interpretation of previous results on cluster properties based on experiments¹³ in which the charges of the secondary particles could not be distinguished is open to question. In the sense that these results describe the average behavior of the (+) and (-) systems, they are in agreement with the results reported here. The values obtained in the present experiment, $\langle k \rangle^{+-} = 1.60 \pm 0.12$ and $\delta = 0.79 \pm 0.03$, are reasonably consistent with the data of Kafka et al.¹ for pp collisions at a single energy with limited statistics.

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References

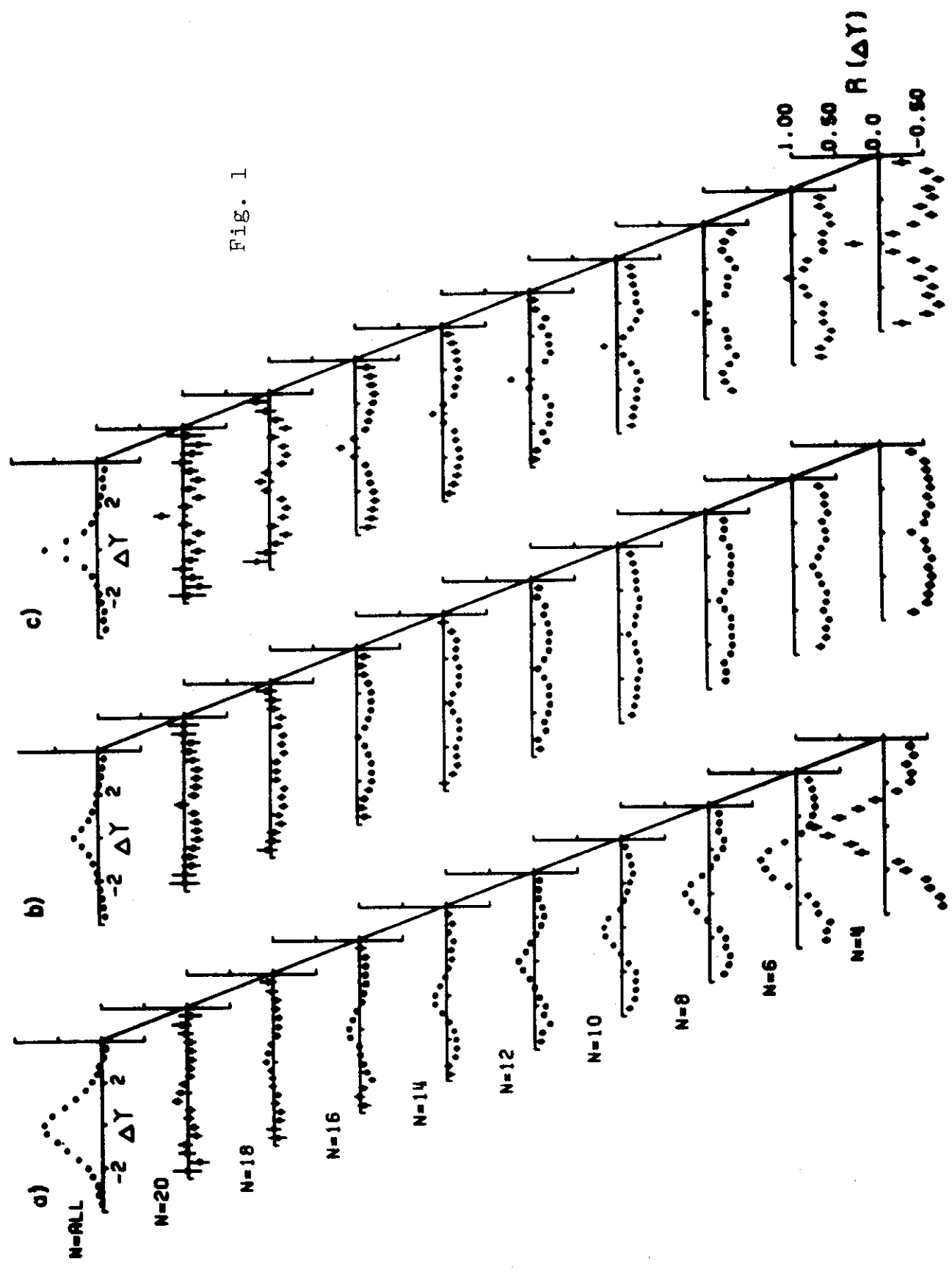
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9. Like-charge (+) pairs were also studied in this experiment. Their correlation behavior was essentially the same as for (-) pairs, and are not further discussed.
10. In the lowest-energy data (18.5 GeV/c), where the central region is small, only 5 values of $R_n(y_1, y_2)$ were fitted.
11. The $n = 8$ topology is the smallest multiplicity for which we can ignore diffractive effects in our 360 GeV/c data, where $\langle n \rangle = 8.73$, and is the largest multiplicity for which clear correlation signals can be obtained.

- in the 18.5 GeV/c and 100 GeV/c data, where statistics are limited.
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Figure Captions

- Fig. 1 Semi-inclusive correlations $R_n(\gamma, \gamma)$ as a function of γ , integrated over a central region $-4.05 \leq \gamma_+ \leq 4.05$, for the data at 360 GeV/c. (a) Correlations for (-+) pairs. (b) Correlations for (-) pairs. (c) Correlations for (--) pairs for which the azimuthal restriction $\phi \leq 45^\circ$ is imposed.
- Fig. 2 Energy and multiplicity dependence of the correlation functions for (-+) unlike-charge pairs. (a) $R_n(0, 0)^+$ as a function of $1/n$ for 360 GeV/c interactions. (b) $R_n(0, 0)^+$ as a function of s for $n = 8$ events.
- Fig. 3 Energy and multiplicity dependence of the correlation functions for (-) like-charge pairs. (a) $R_n(0, 0)^-$ as a function of $1/n$ for 360 GeV/c interactions. Events for which $0 \leq \phi \leq 45^\circ$. (Bose-Einstein cut) are shown as circles, $45^\circ \leq \phi \leq 180^\circ$ as crosses. (b) $R_n(0, 0)^-$ as a function of s for $n = 8$ events, with ϕ cut as above.

Fig. 1



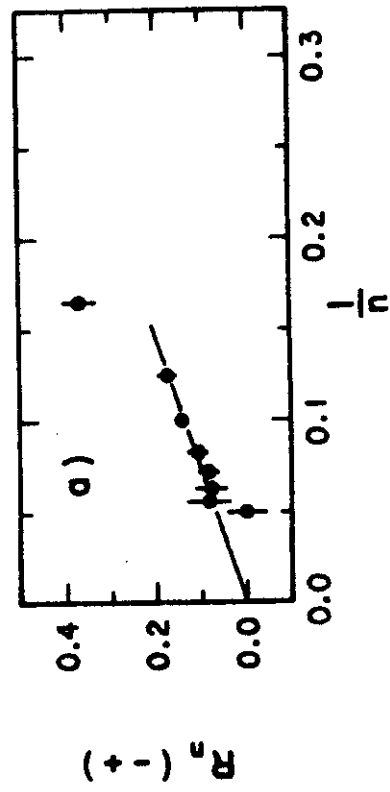
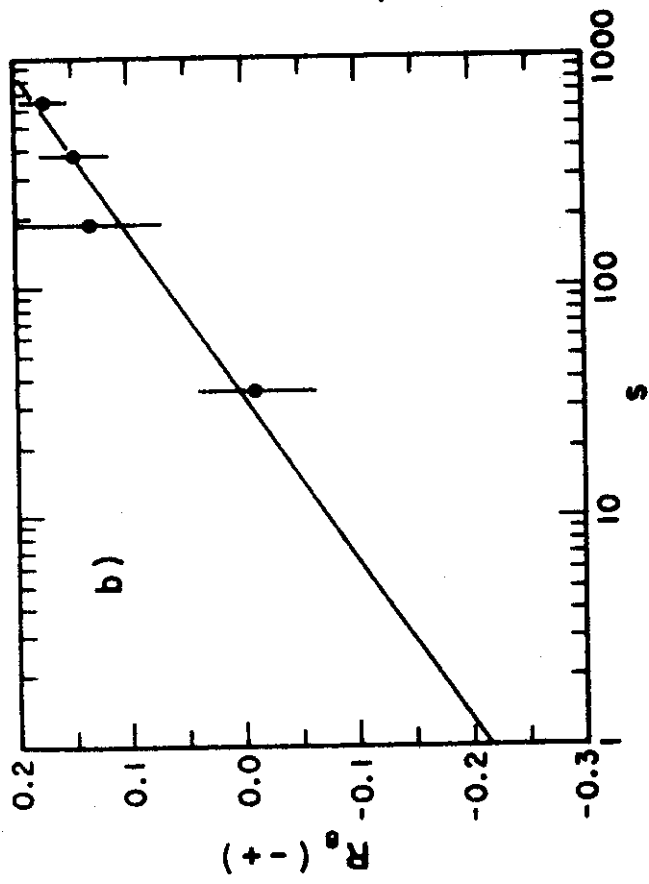


Fig. 2

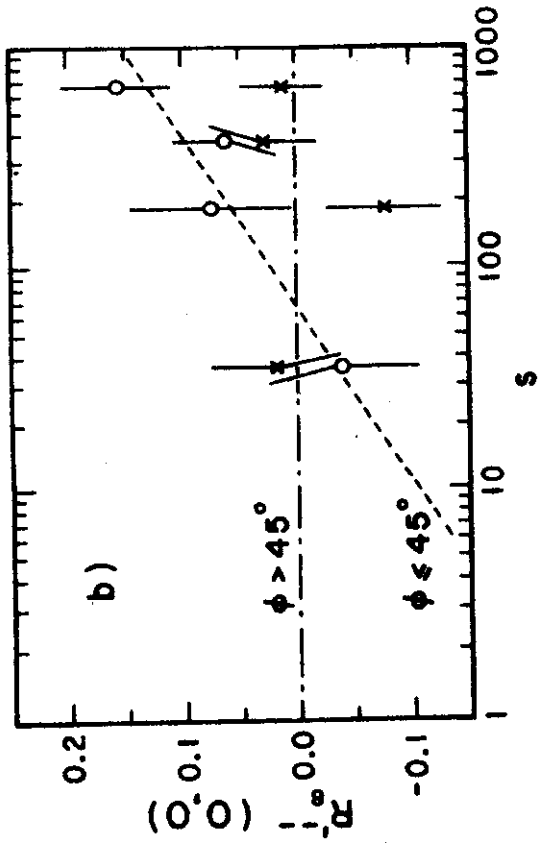
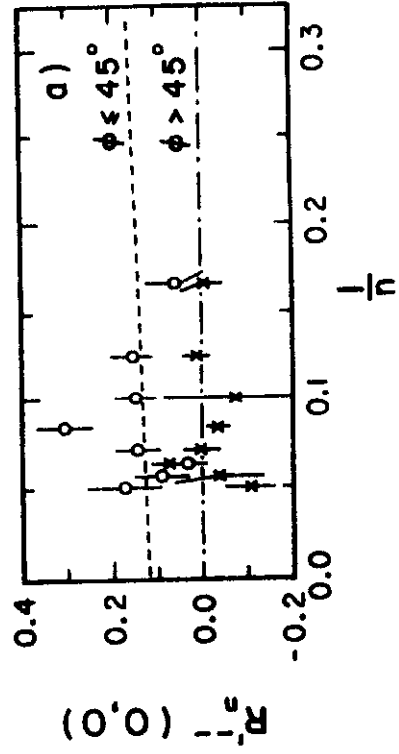


Fig. 3