

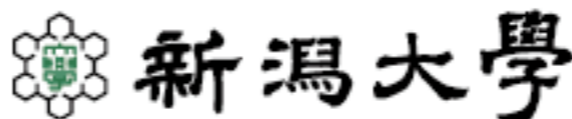
# CP violation in B decays with Belle and BABAR

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NIIGATA UNIVERSITY



# Contents of talk today

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- Final  $\sin^2 \phi_1$  from 1st generation B-factories
- $\phi_3$  measurements with new analysis techniques
- Prospects in near future

# Quark mixing and CP violation

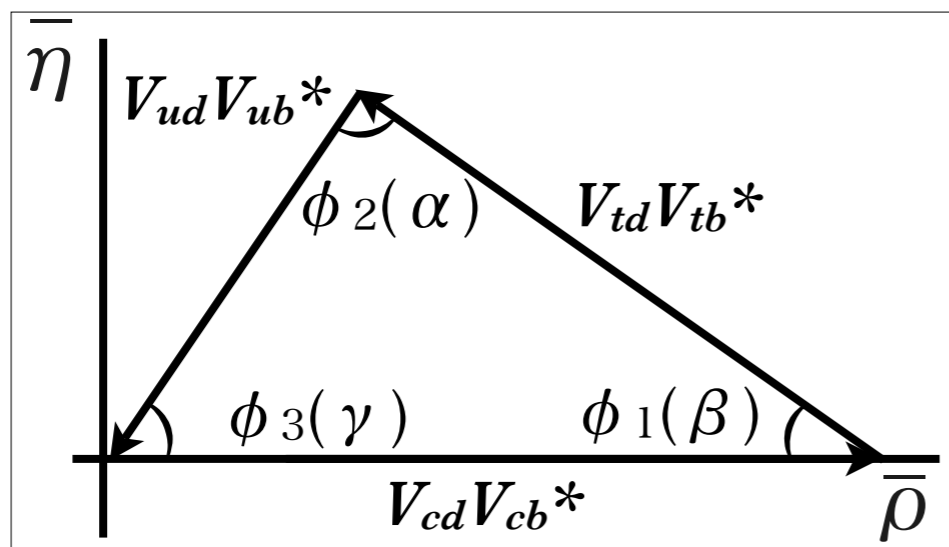
3-generation quark mixing : Cabibbo-Kobayashi-Maskawa matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Wolfenstein representation

CP violation is induced by complex phase of CKM matrix

$$\sum_i V_{ij}^* V_{ik} = \delta_{jk} \Rightarrow V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0 \quad (k = b)$$



Unitary triangle

CP violation parameters

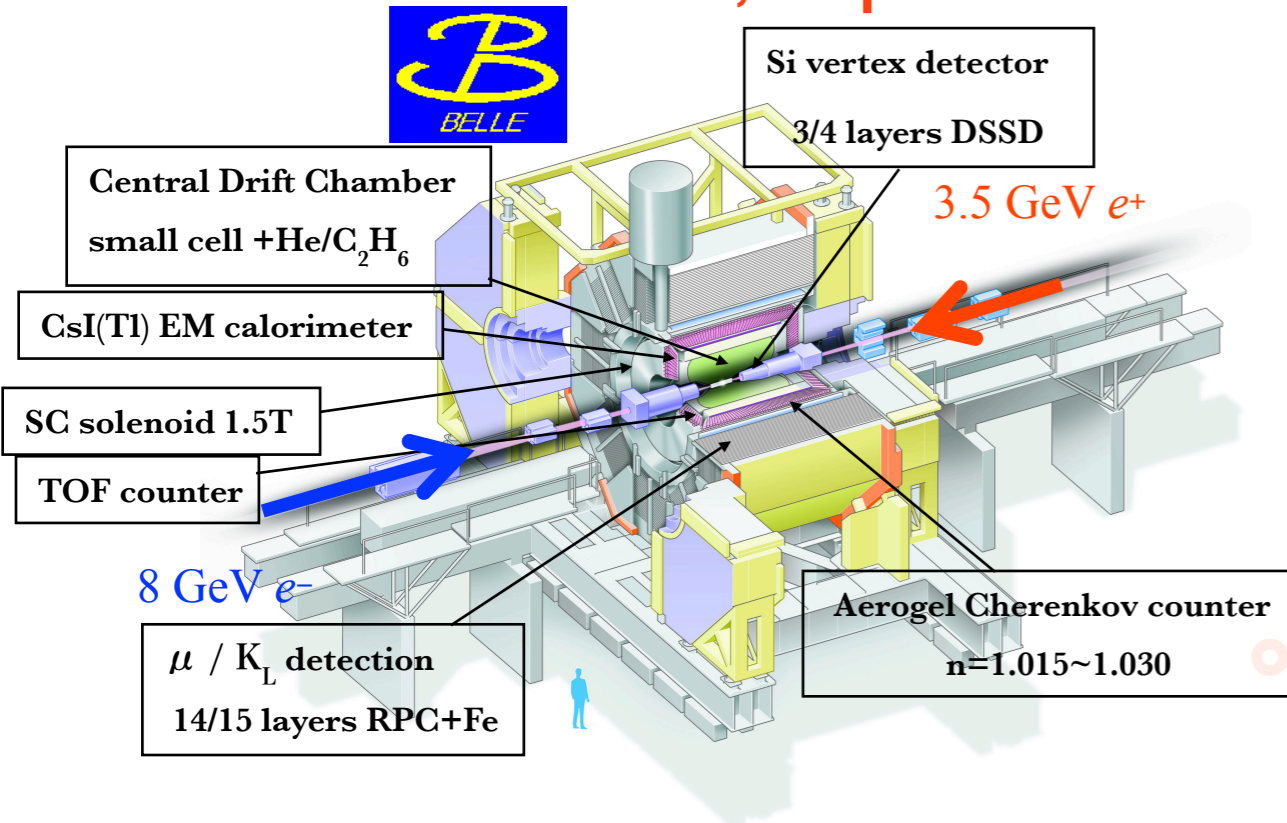
$$\phi_1(=\beta) = \arg(V_{cd} V_{cb}^* / V_{td} V_{tb}^*)$$

$$\phi_2(=\alpha) = \arg(V_{ud} V_{ub}^* / V_{td} V_{tb}^*)$$

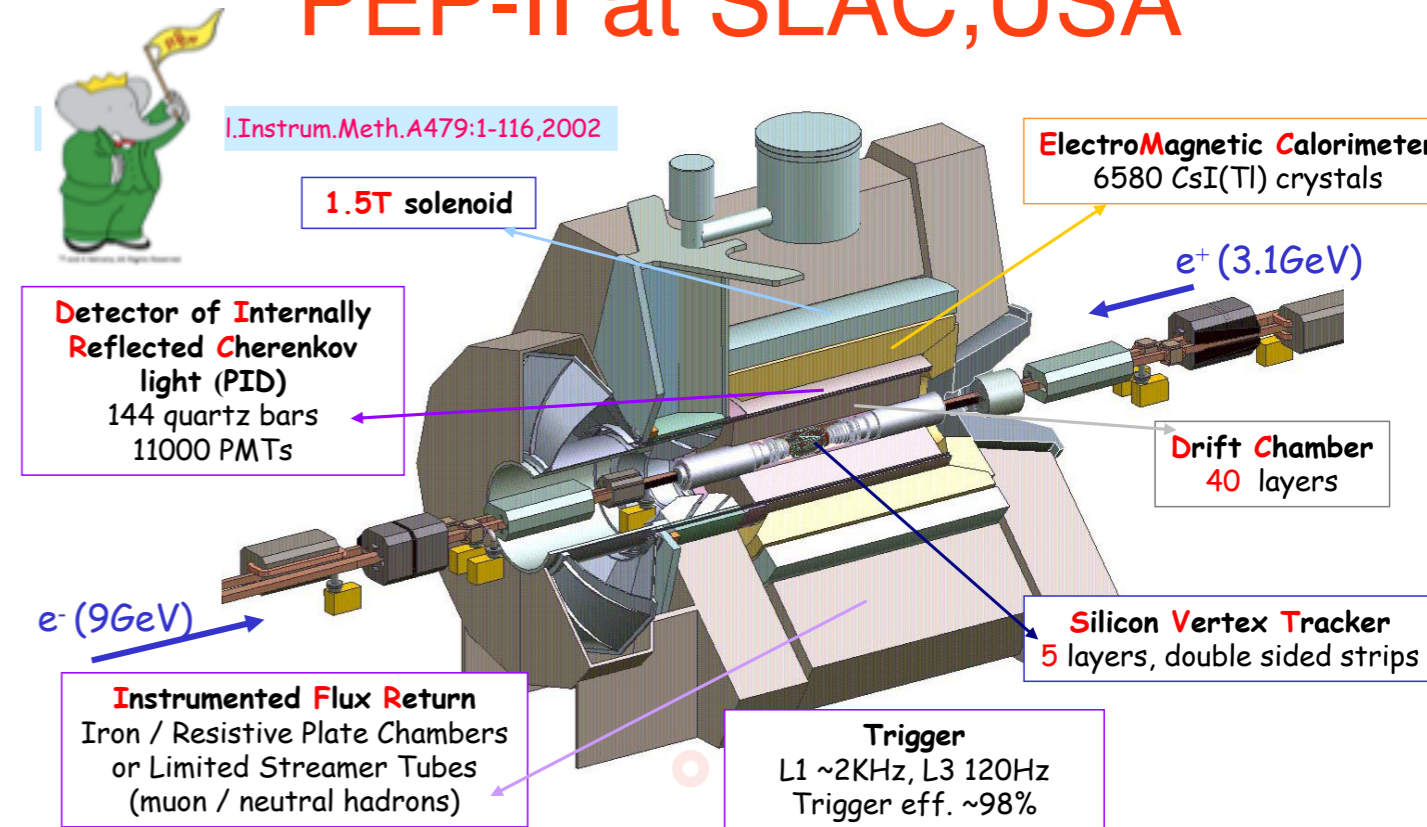
$$\phi_3(=\gamma) = \arg(V_{cd} V_{cb}^* / V_{ud} V_{ub}^*)$$

# B-factories

## KEKB at KEK, Japan

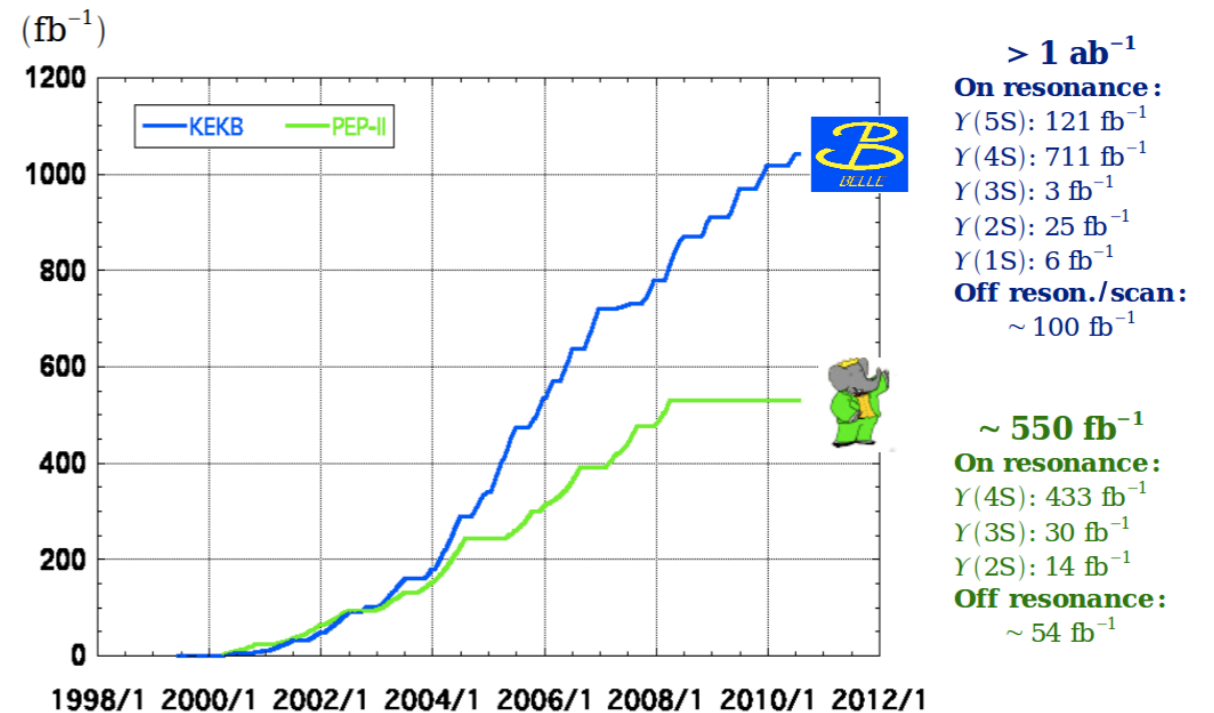


## PEP-II at SLAC, USA



**772M + 463M B $\bar{B}$   
accumulated!**

## Integrated luminosity of B factories



# Measurement of $\sin 2\phi_1$

Time-dependent CP violation:

Quantum interference between  $B^0-\bar{B}^0$  mixing and  $B^0$  decay to CP eigenstate.

$$A_{CP}(\Delta t) = \frac{\mathcal{P}(\bar{B}^0(\Delta t) \rightarrow f_{CP}) - \mathcal{P}(B^0(\Delta t) \rightarrow f_{CP})}{\mathcal{P}(\bar{B}^0(\Delta t) \rightarrow f_{CP}) + \mathcal{P}(B^0(\Delta t) \rightarrow f_{CP})}$$

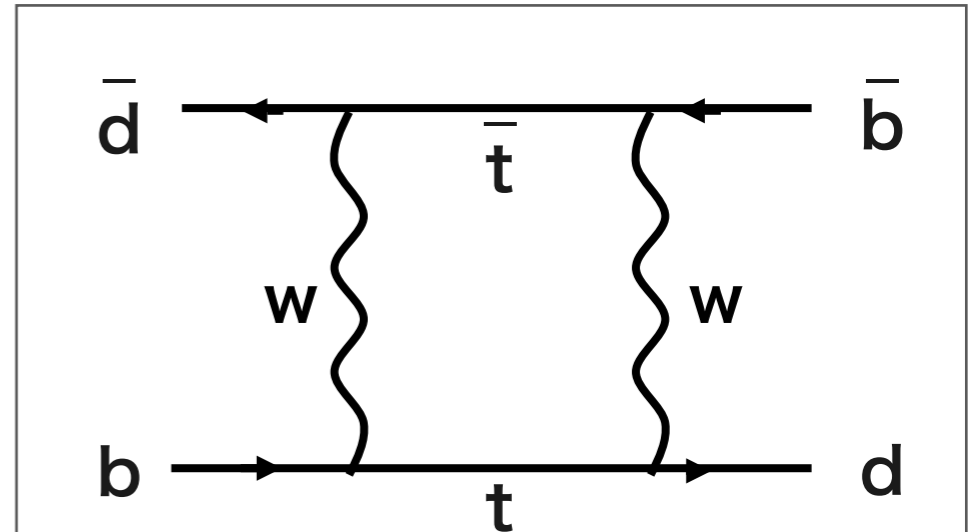
$$= S \sin \Delta m \Delta t + A \cos \Delta m \Delta t$$

$S$ : Mixing induced CPV parameter

$A(=-C)$ : Direct CPV parameter

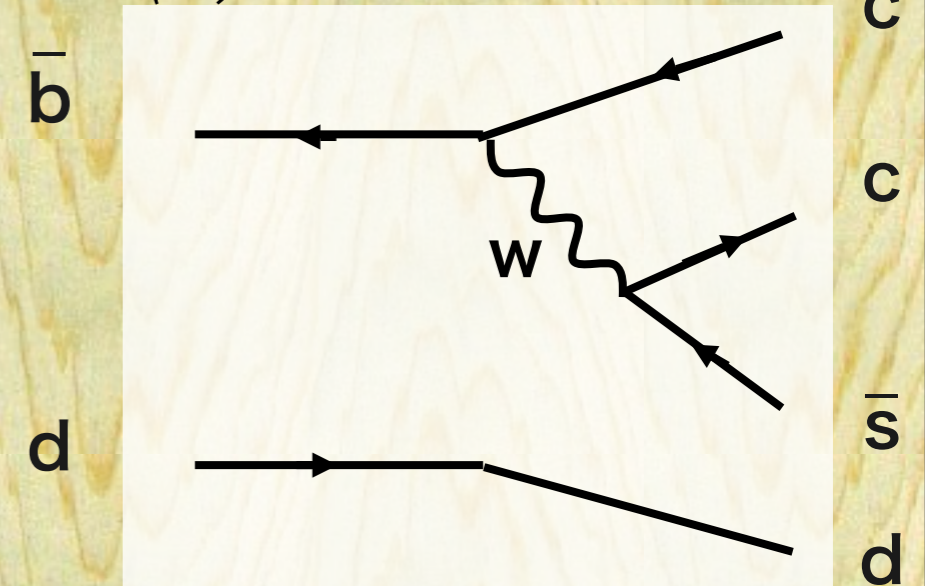
$\Delta m$ :  $B$ - $B$  mass difference

$\Delta t$ :  $B$ - $B$  decay time difference



—  $b \rightarrow c\bar{c}s$  tree diagram

$B^0 \rightarrow (c\bar{c}) K^0$  “Golden mode”



$(c\bar{c}) = J/\psi, \psi(2S), \chi_{c1}, \eta_{c\dots}$

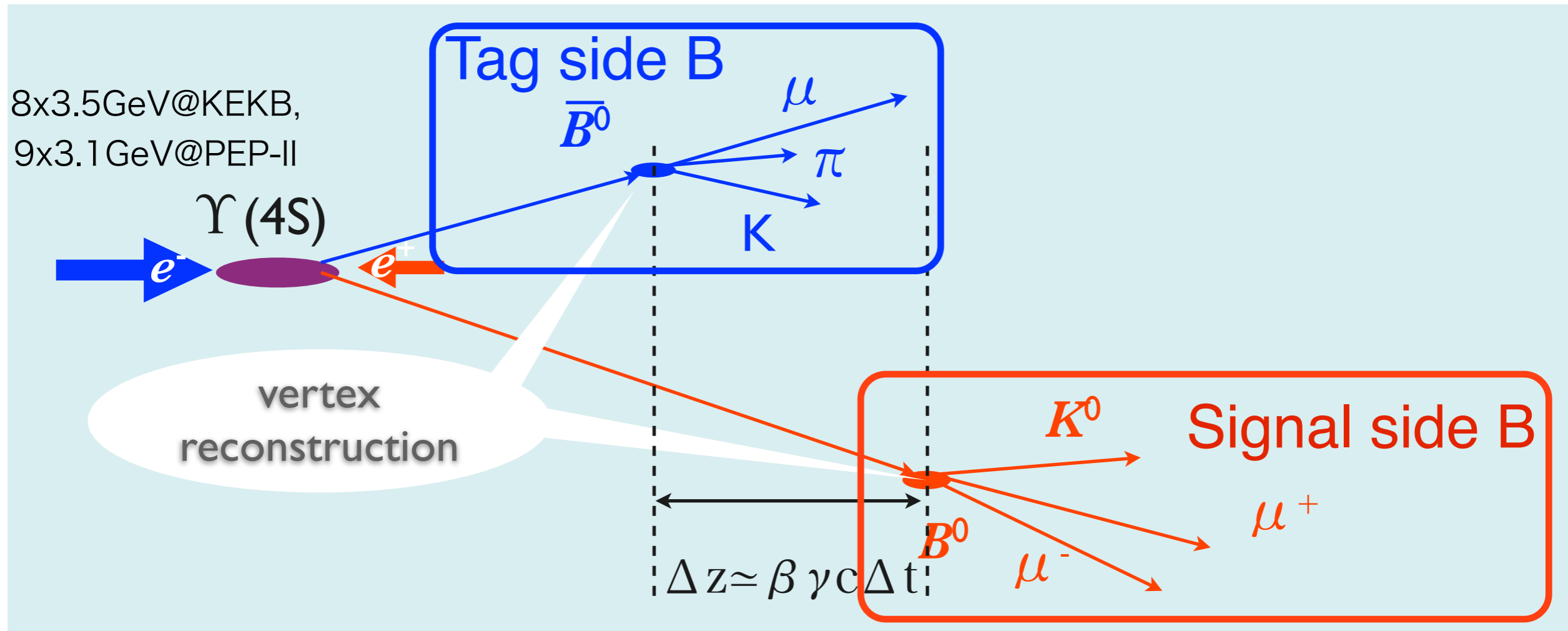
$$S = -\xi_f \sin 2\phi_1$$

$\xi_f$ : CP eigenvalue :

-1 for  $(c\bar{c})K^0_S$ , +1 for  $(c\bar{c})K^0_L$

# Principle of $\sin 2\phi_1$ measurement

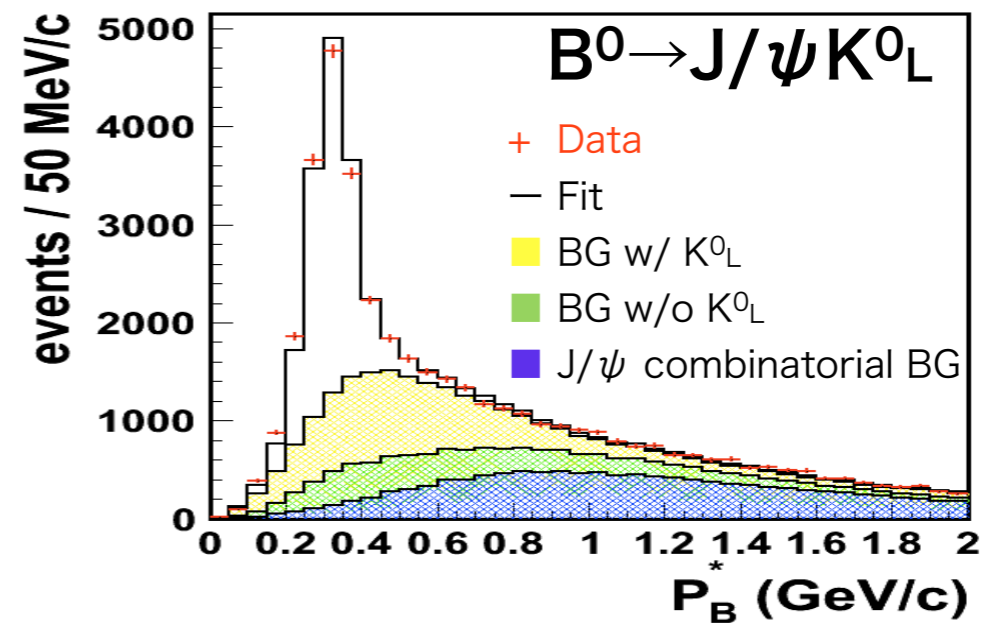
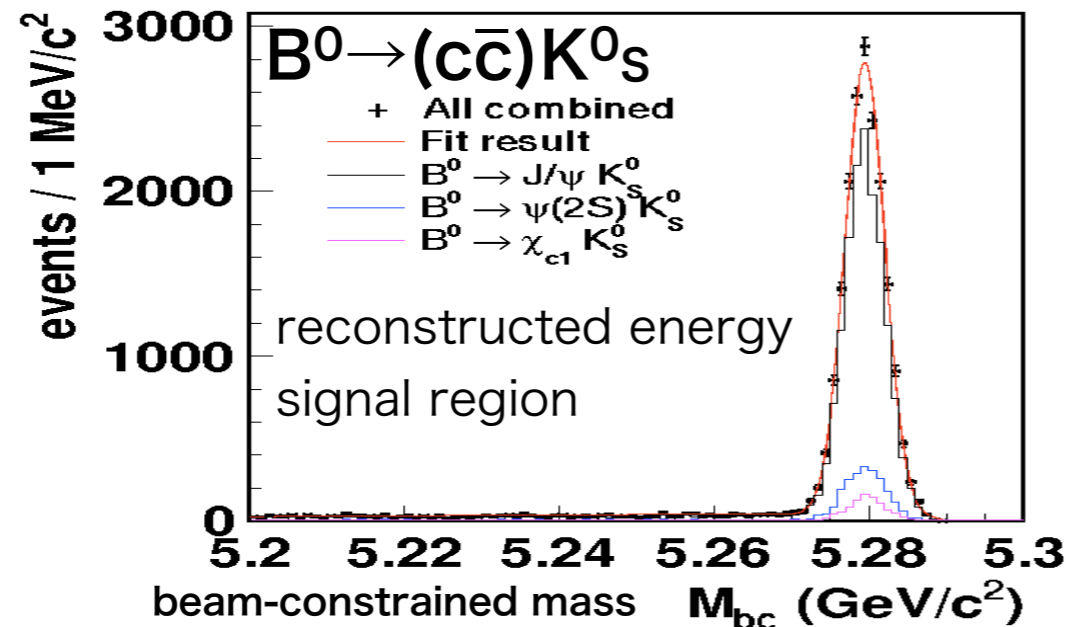
When ( $\Delta t$ ) / Which  $B^0$  (flavor) decay into CP eigenstate?



- Reconstruct  $B^0$  (beam constraint mass, energy, momentum etc.)
- Tag  $B^0$  flavor (charge of decay products of accompany  $B^0$ )
  - $\bar{B}^0 \rightarrow D^{*+} l^- \nu$ ,  $\bar{B}^0 \rightarrow D^{*\pm} \rightarrow D^0 \pi^+$
  - $\hookrightarrow K^- l^+ \nu$
- $\Delta t$  measurement from decay vertices

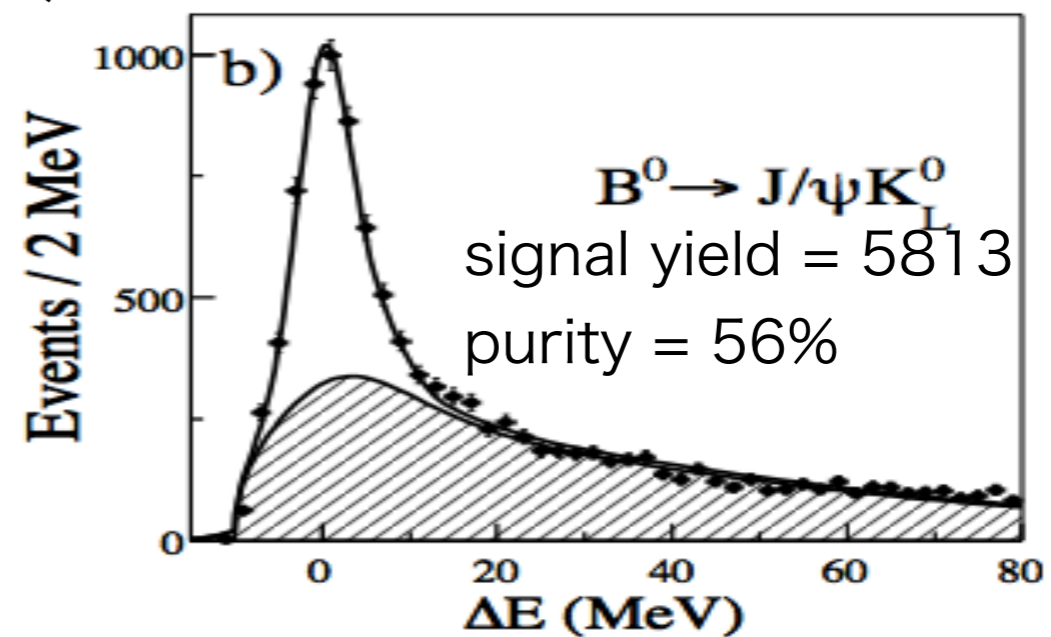
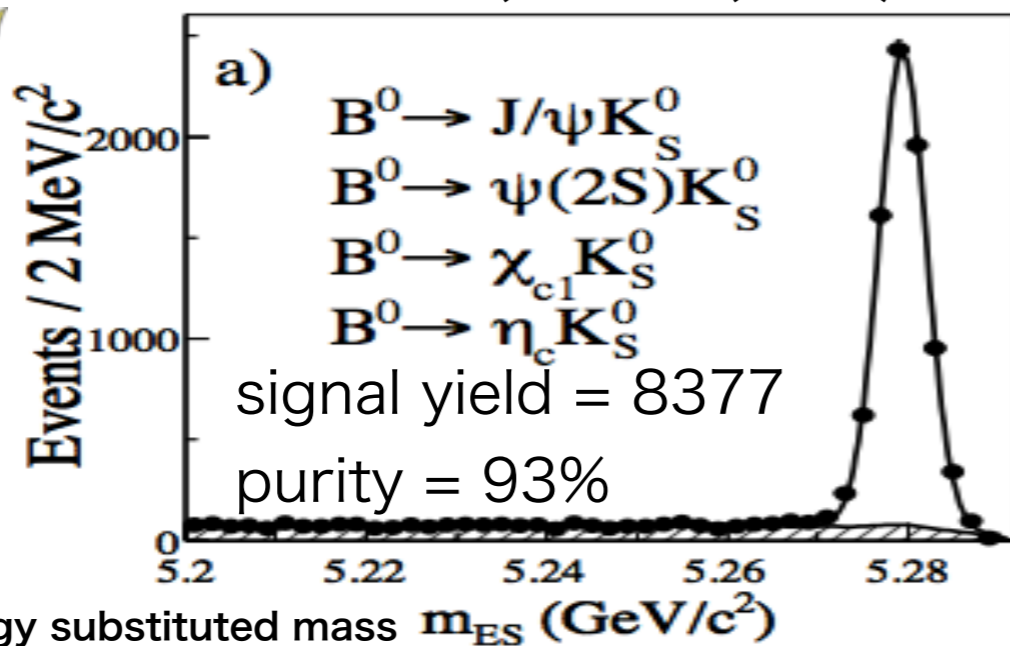
# Reconstruction of CP sample

Belle 772M  $B\bar{B}$  (Preliminary)



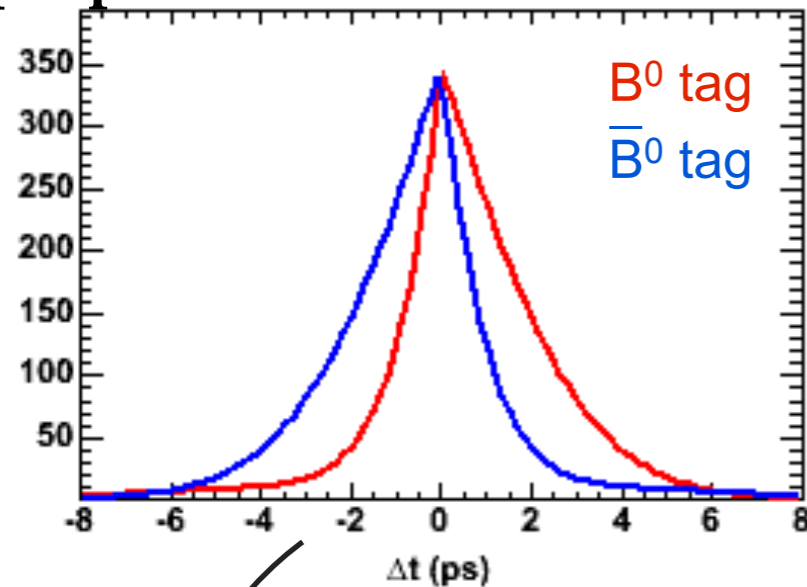
	$J/\psi K_S^0$	$J/\psi K_L^0$	$\psi(2S)K_S^0$	$\chi_{c1}K_S^0$
Signal yield	$12681 \pm 114$	$10041 \pm 154$	$1981 \pm 46$	$949 \pm 33$
Purity (%)	97	63	93	89

BABAR 465M  $B\bar{B}$  (PRD 79 (2009) 072009)



# Time-dependent CPV measurement

proper-time  $\Delta t$  distribution

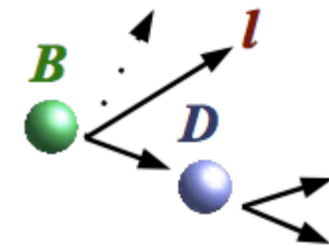


Time dependent decay rate

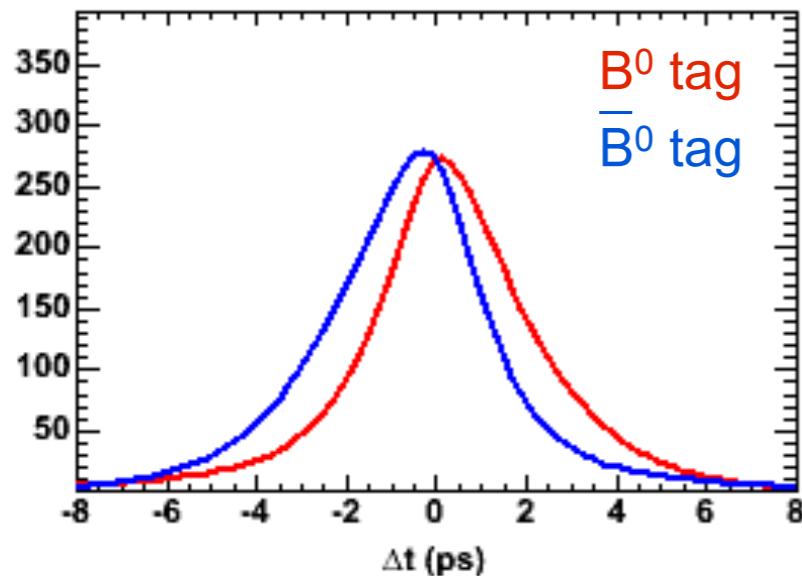
$$\mathcal{P}_{sig} = \frac{1}{4\tau} e^{-\frac{|\Delta t|}{\tau}} q(A \cos \Delta m \Delta t + S \sin \Delta m \Delta t)$$

$\tau$  : B lifetime  
 $\Delta m$  : B- $\bar{B}$  mass difference

- Detector resolution
- Non-primary tracks from companion B
- Kinematic approximation:  $\Delta z \approx \beta \gamma c \Delta t$
- Failure of  $B^0$  flavor tagging



smearred  $\Delta t$  distribution



$$\mathcal{P}_{sig} = \frac{1}{4\tau} e^{-\frac{|\Delta t|}{\tau}} (1-2\omega) q(A \cos \Delta m \Delta t + S \sin \Delta m \Delta t) \otimes R(\Delta t)$$

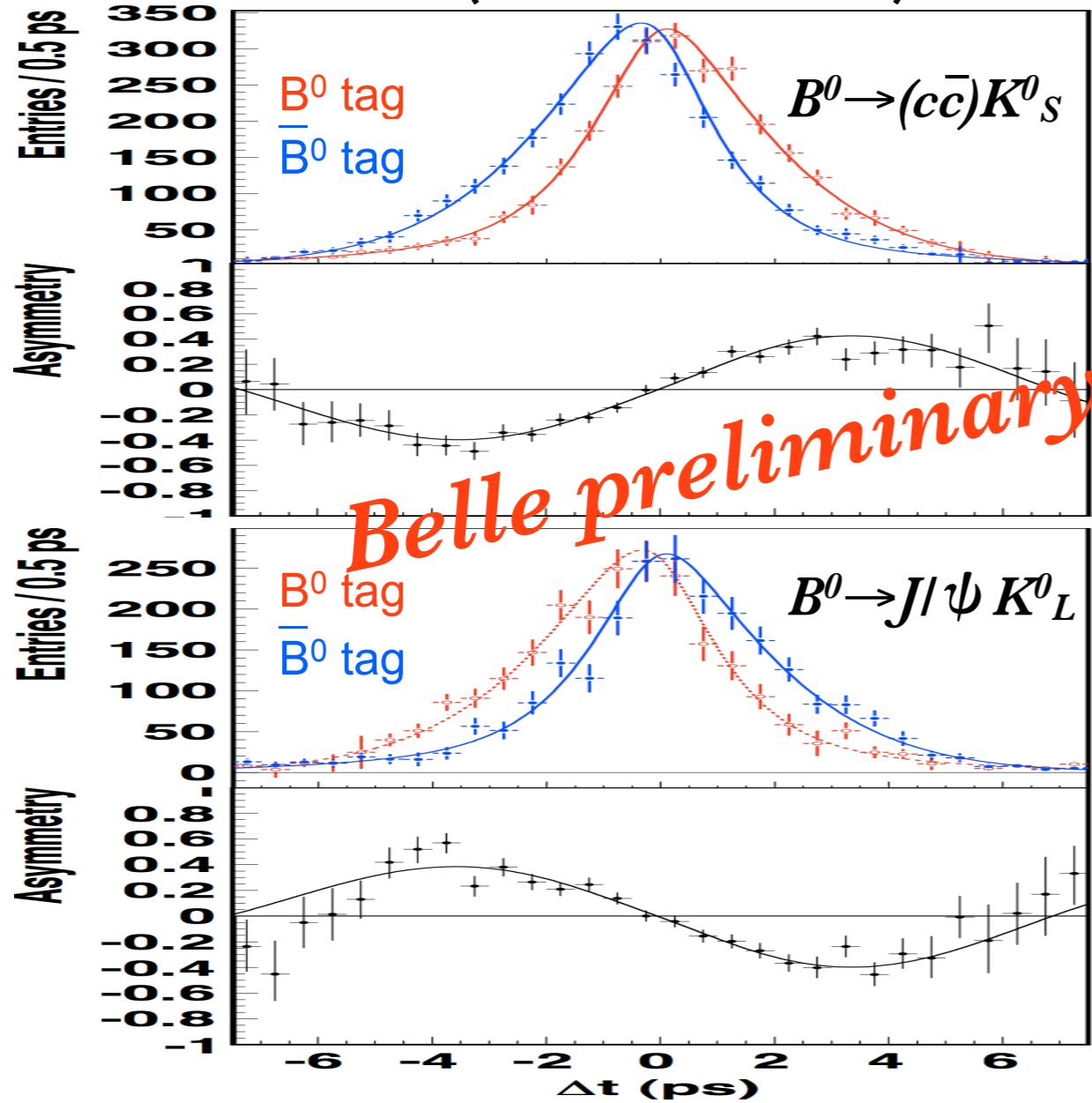
flavor tagging quality      resolution function

→ Determined using flavor specific  
 null-CPV control sample ( $B^0 \rightarrow D^{(*)} h$ ,  $B^0 \rightarrow D^* l \nu$ )



# Measurement of $\sin 2\phi_1$

Belle 772M  $B\bar{B}$  (Moriond EW 2011)



*background subtracted,  
good flavor tag quality only*

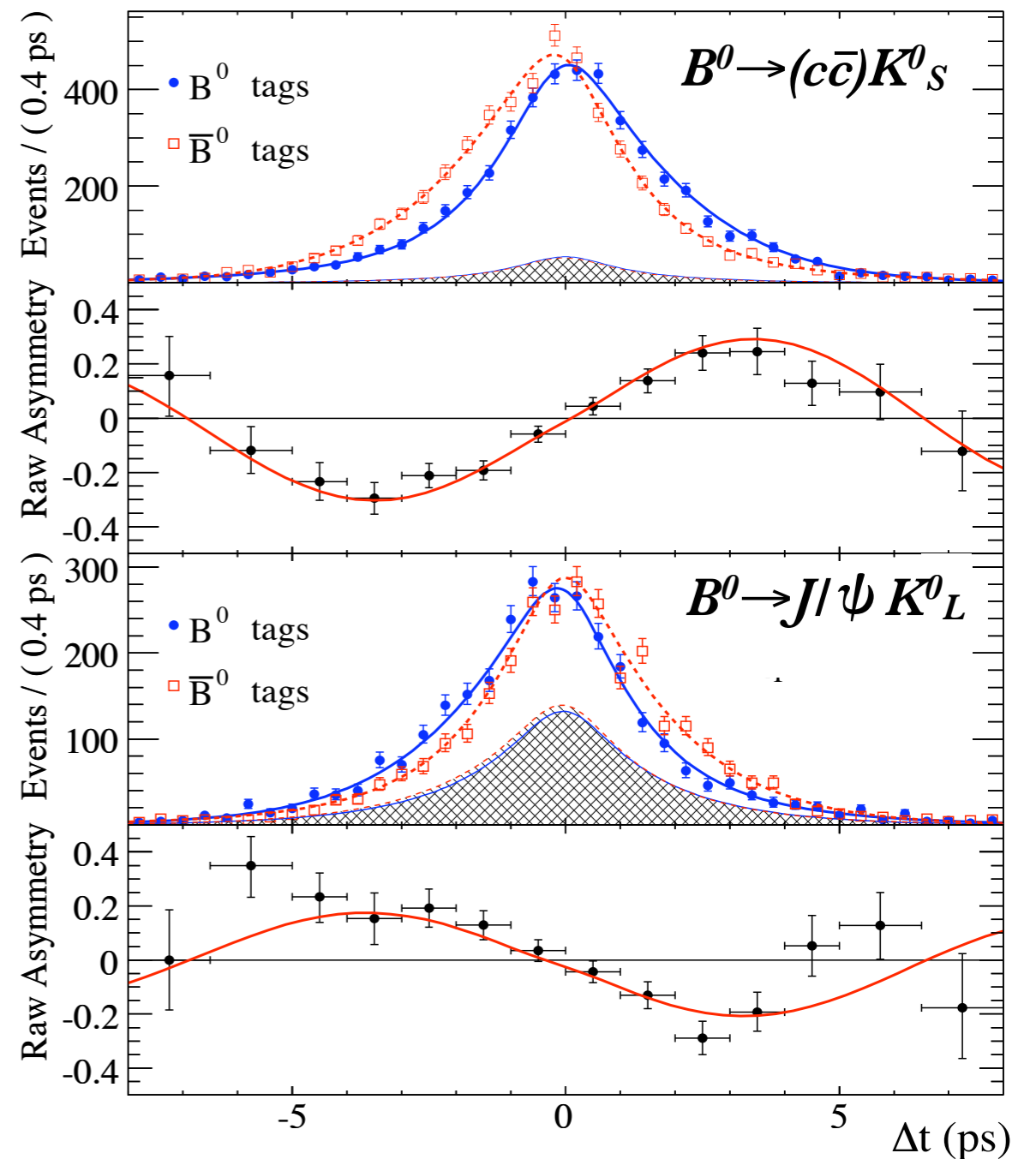
$B^0 \rightarrow (c\bar{c})K^0_S$   $B^0 \rightarrow J/\psi K^0_L$  combined

$$\sin 2\phi_1 = 0.668 \pm 0.023 \pm 0.013$$

$$A = 0.007 \pm 0.016 \pm 0.013$$



BABAR 465M  $B\bar{B}$  (PRD 79 (2009) 072009)



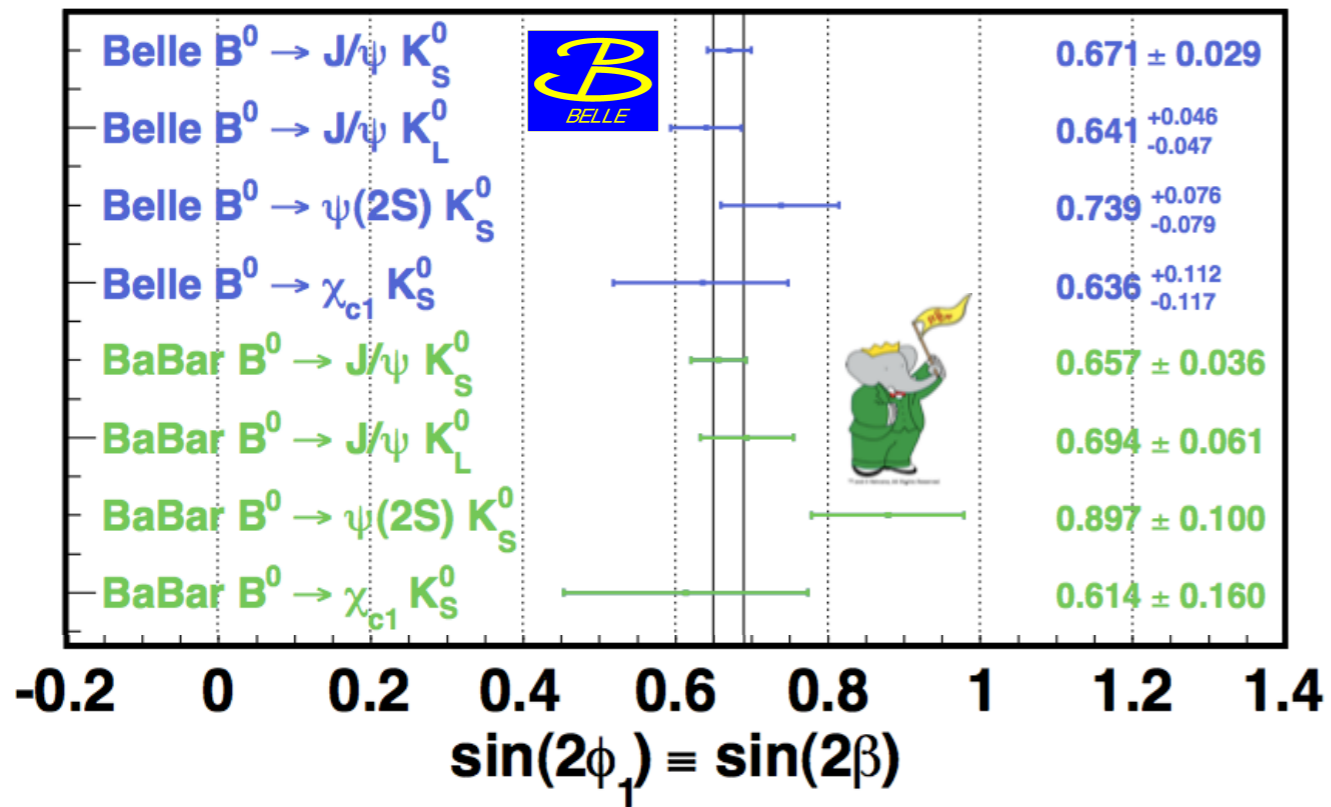
$B^0 \rightarrow (c\bar{c})K^0_S$   $B^0 \rightarrow J/\psi K^0_L$  combined

$$\sin 2\phi_1 = 0.687 \pm 0.028 \pm 0.012$$

$$A = -0.024 \pm 0.020 \pm 0.016$$



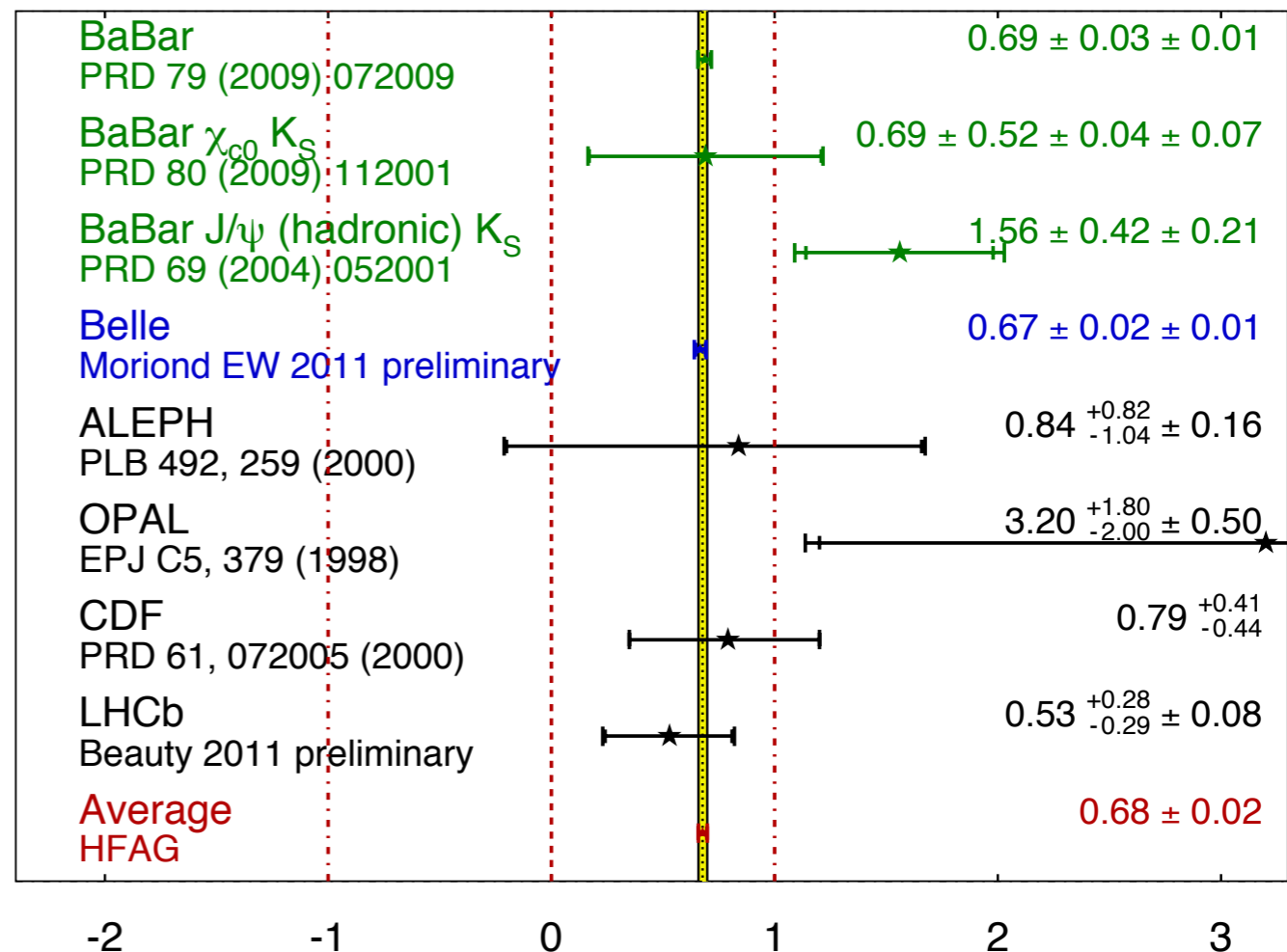
# Measurement of $\sin 2\phi_1$



Both Belle and BABAR observe CP violation in all decay modes

$$\sin(2\beta) \equiv \sin(2\phi_1) \quad \text{HFAG Beauty 2011 PRELIMINARY}$$

$\sin 2\phi_1$  is mainly determined by results of B-factories



# $\phi_3$ determination

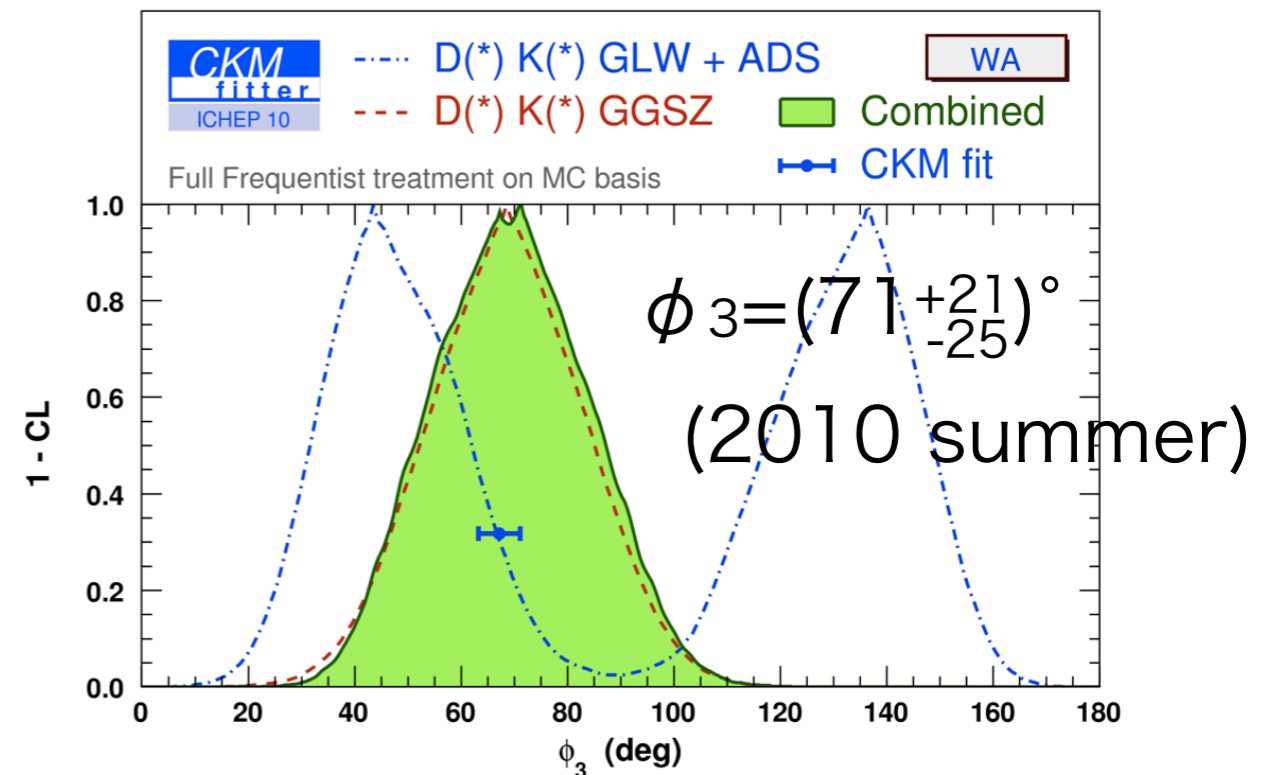
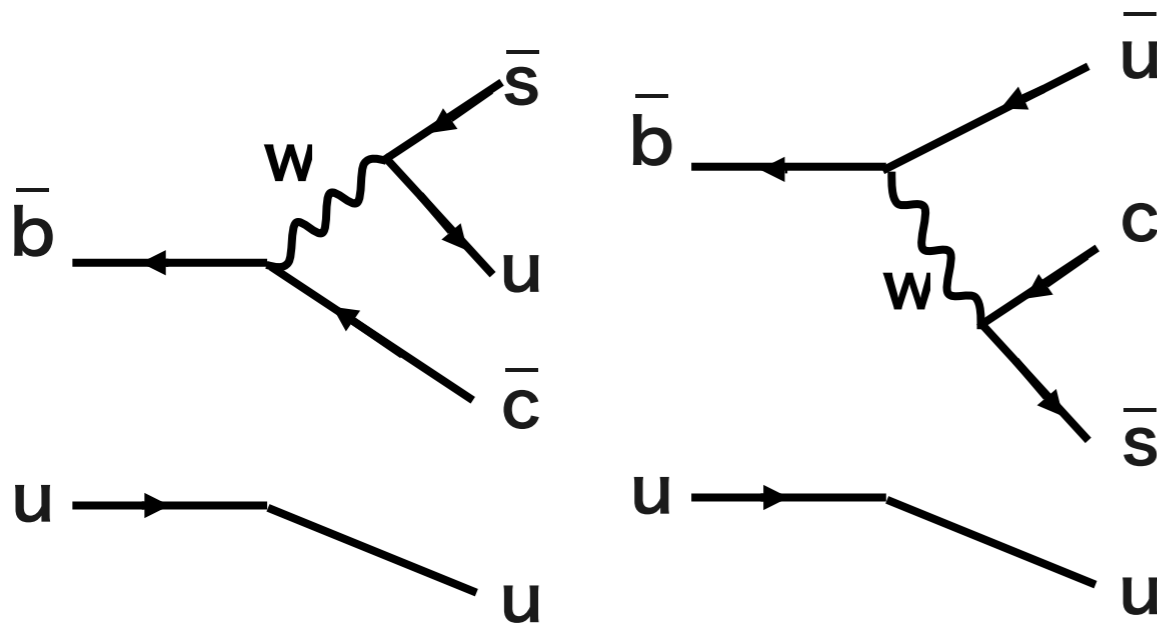
Measurements using interference between  $V_{ub}$  contribution and another weak vertex.

Relative phase of  $B^\pm \rightarrow DK^\pm$

$$|\tilde{D}\rangle = |D^0\rangle + re^{i\theta} |\bar{D}^0\rangle$$

$$\theta = \pm \phi_3 + \delta$$

(weak phase) + (strong phase)

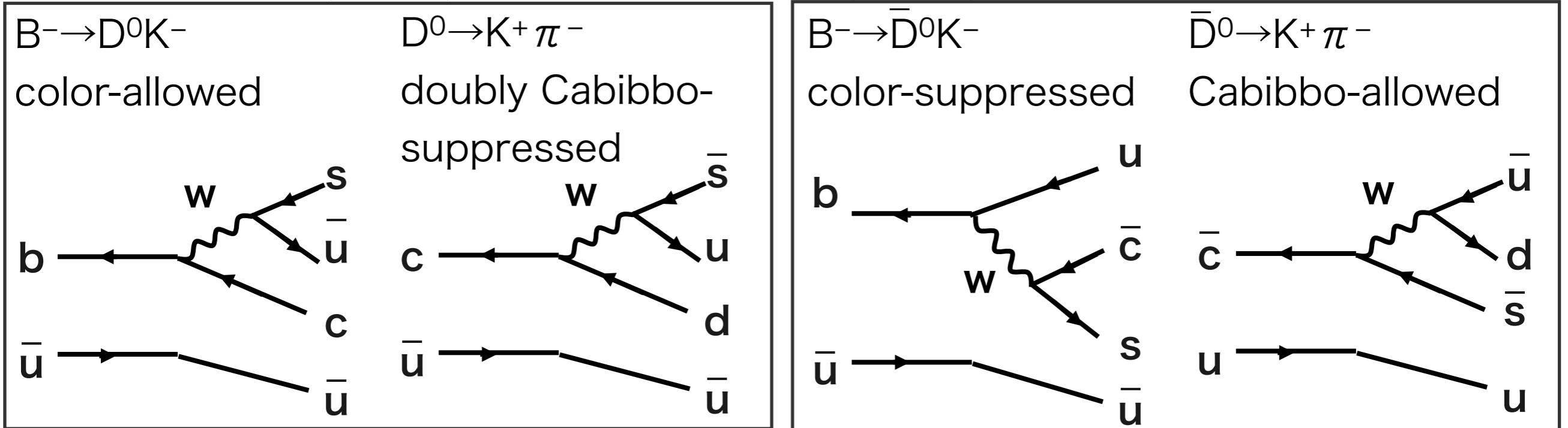


Several decays modes of D meson are used to determine  $\phi_3$

# Measurement of $\phi_3$ with ADS

D. Atwood, I. Dunietz and A. Soni,

PRL78, 3357 (1997); PRD 63, 036005 (2001)



⇒ Magnitudes of interfering amplitudes are comparable

→ CP violation effects are enhanced

$$\mathcal{R}_{DK} \equiv \frac{\mathcal{B}([K^+ \pi^-]_D K^-) + \mathcal{B}([K^- \pi^+]_D K^+)}{\mathcal{B}([K^- \pi^+]_D K^-) + \mathcal{B}([K^+ \pi^-]_D K^+)}$$

$$= r_B^2 + r_D^2 + 2r_B r_D \cos \delta \cos \phi_3$$

$$\mathcal{A}_{DK} \equiv \frac{\mathcal{B}([K^+ \pi^-]_D K^-) - \mathcal{B}([K^- \pi^+]_D K^+)}{\mathcal{B}([K^+ \pi^-]_D K^-) + \mathcal{B}([K^- \pi^+]_D K^+)}$$

$$= 2r_B r_D \sin \delta \sin \phi_3 / \mathcal{R}_{DK}$$

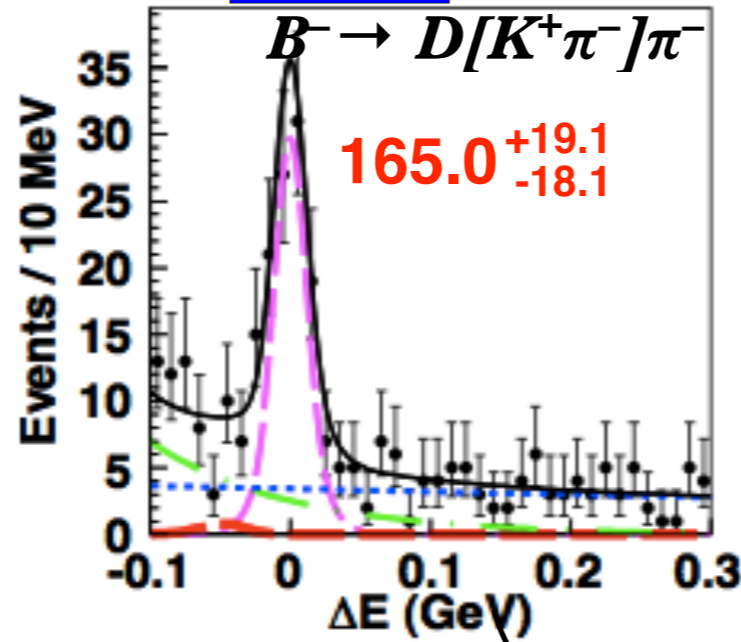
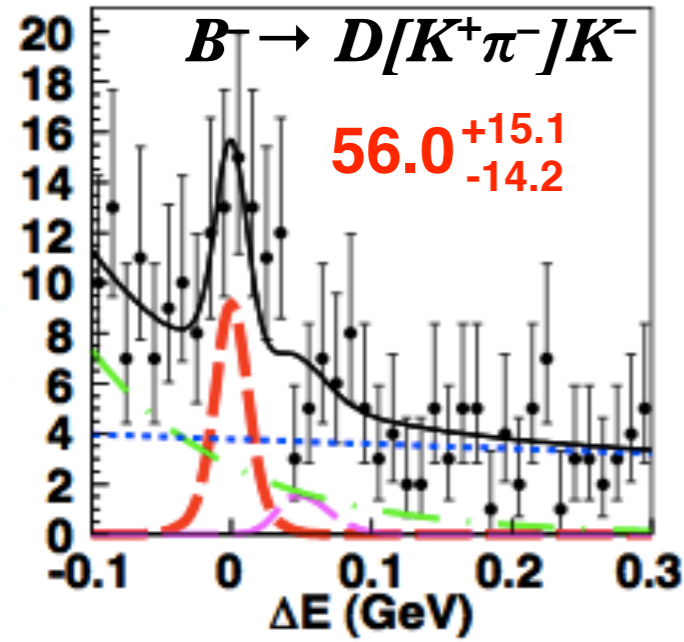
$$r_B \equiv \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|, \quad \delta \equiv \delta_B + \delta_D,$$

$$r_D \equiv \left| \frac{A(D^0 \rightarrow K^+ \pi^-)}{A(D^0 \rightarrow K^- \pi^+)} \right|$$

# Results of ADS method

Belle 772M  $B\bar{B}$

(arXiv:1103.5951 (hep-ex))



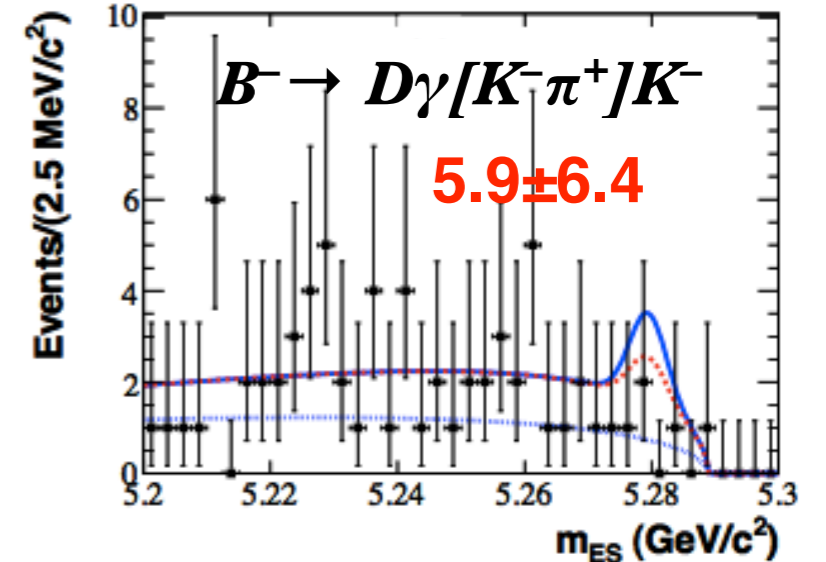
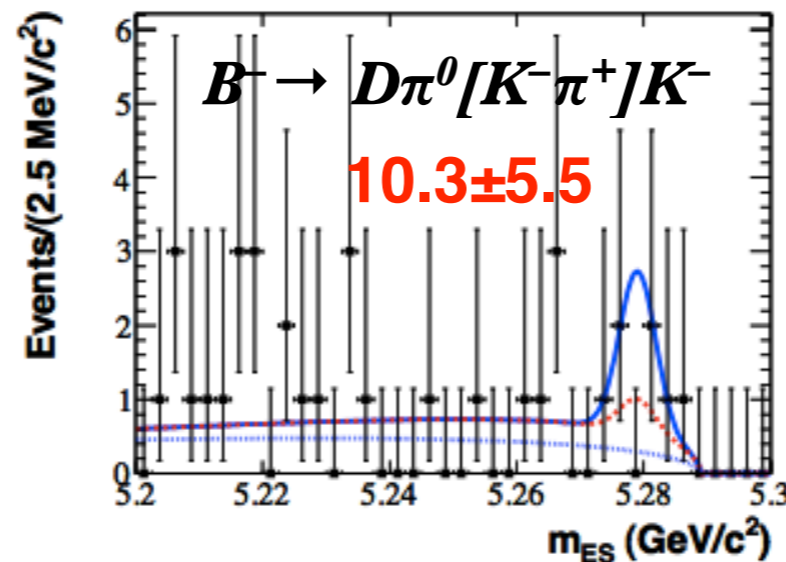
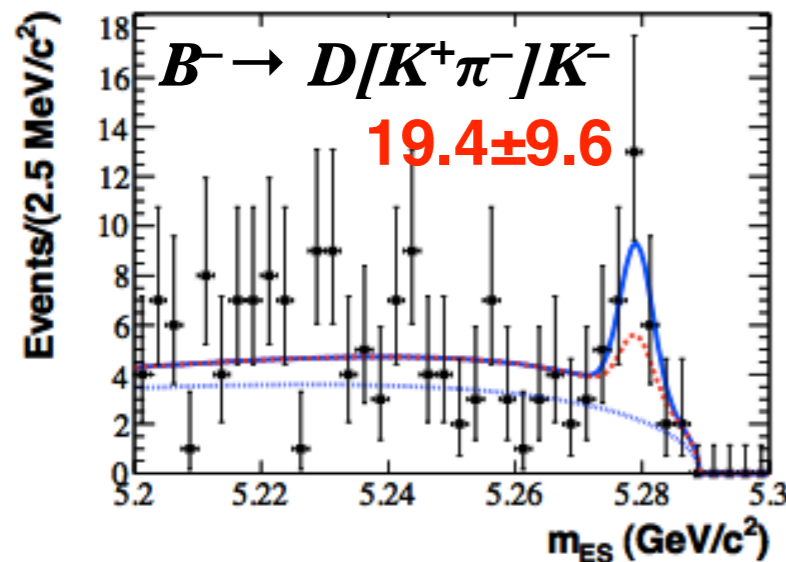
First evidence of suppressed  $B \rightarrow D[K^+\pi^-]K$  decay signal due to increasing of data and cleverer continuum background suppression based on neural-net

BABAR 467M  $B\bar{B}$

(PRD82 072006 (2010))



Larger signal yield but sensitivity of  $\phi_3$  is lower due to smallness of  $r_B$

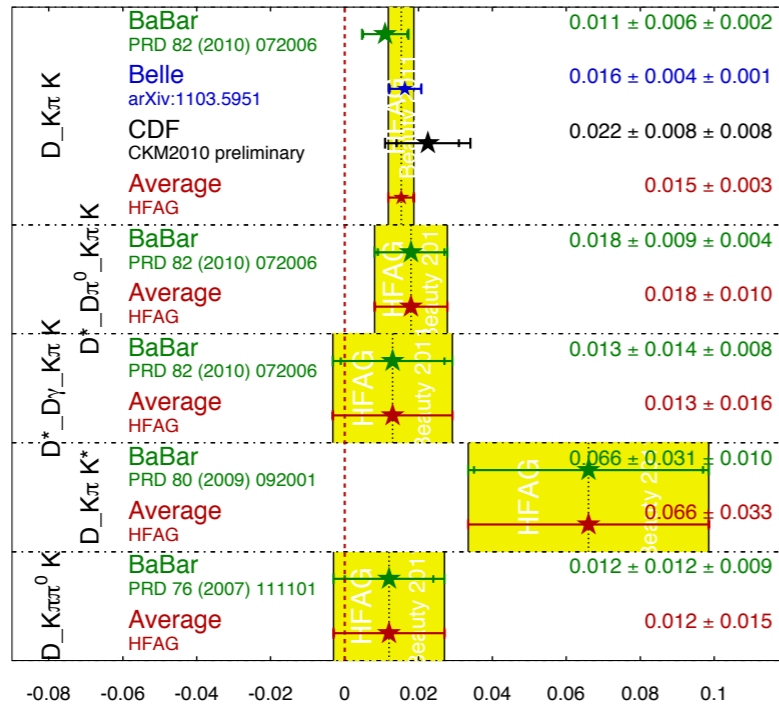


# Results of ADS method

$$B^- \rightarrow D^{(*)0} K^{(*)-}$$

$R_{ADS}$  Averages

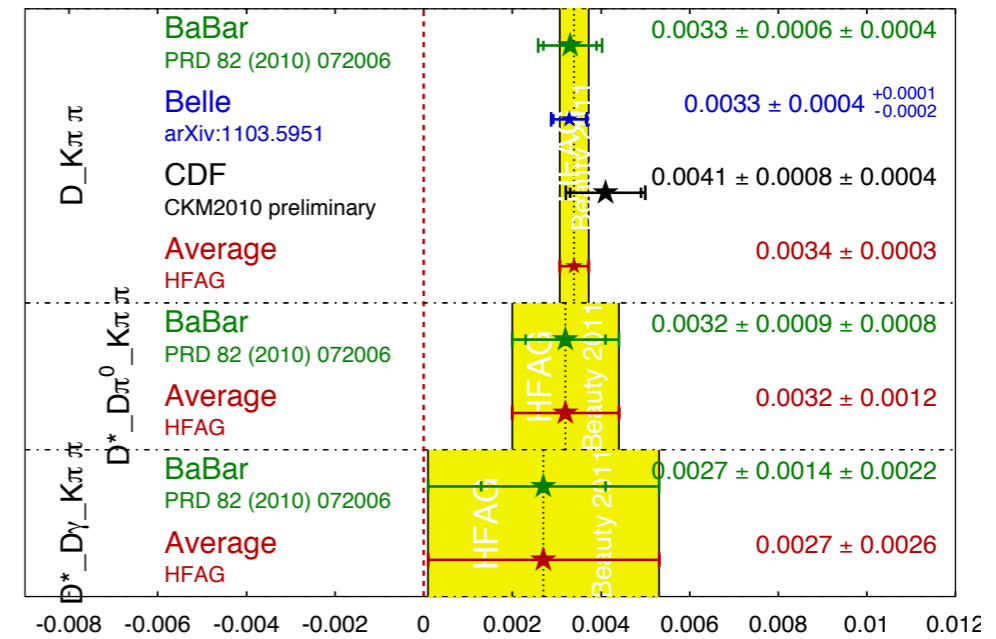
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$$B^- \rightarrow D^{(*)0} \pi^-$$

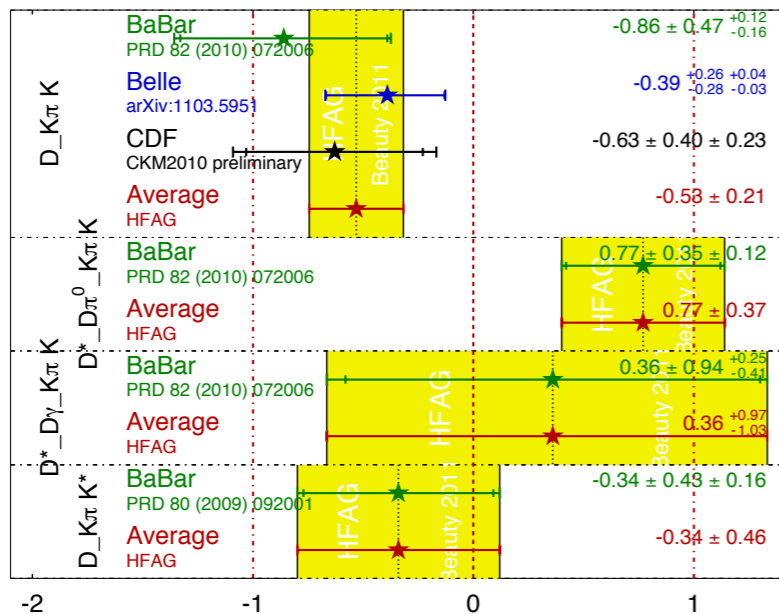
$R_{ADS}$  Averages

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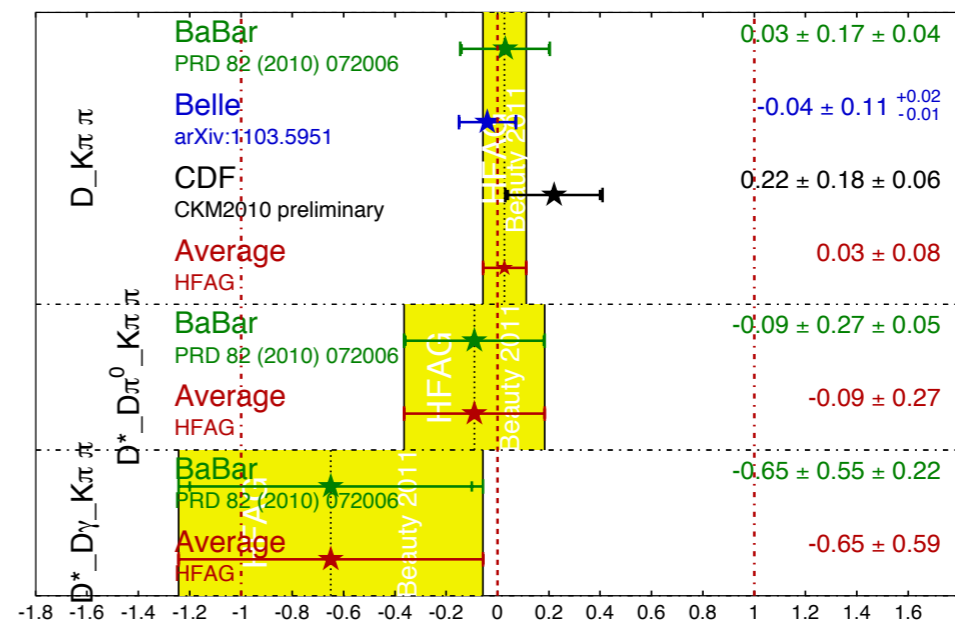
$A_{ADS}$  Averages

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$A_{ADS}$  Averages

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- Most precise measurement by Belle in  $D \rightarrow K\pi$
- BABAR attempted to use  $D^*K$  and  $DK^*$  as well

# Measurement of $\phi_3$ with GGSZ

Dalitz plot analysis using  $D \rightarrow K_S^0 \pi^+ \pi^-$  3-body decay

A. Giri, Yu. Grossman, A. Soffer, J. Zupan, PRD 68, 054018 (2003)

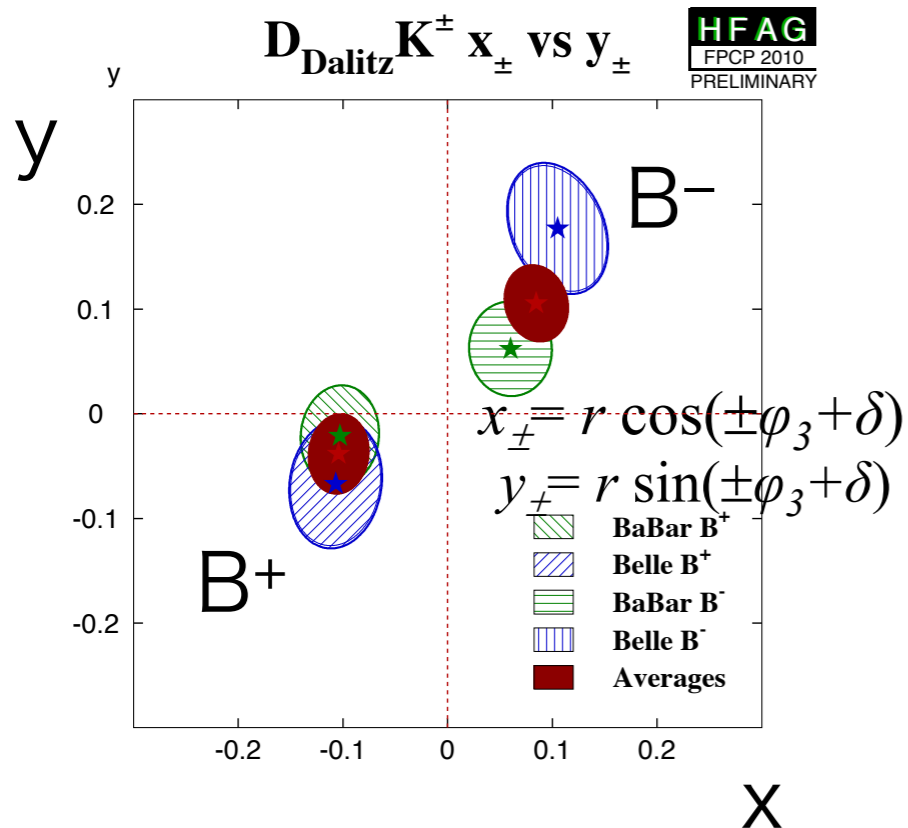
Dalitz plot density:  $d\sigma_{\pm}(m_+^2, m_-^2) \sim |M_{\pm}|^2 dm_+^2 dm_-^2$

$$|M_{\pm}(m_+^2, m_-^2)|^2 = |f_D(m_+^2, m_-^2) + re^{i\delta_B \pm i\phi_3} f_D(m_-^2, m_+^2)|^2$$

$$m_+^2 = m_{K_S \pi^+}^2, \quad m_-^2 = m_{K_S \pi^-}^2$$

$D^0 \rightarrow K_S^0 \pi^+ \pi^-$  amplitude  $f_D$  : fit to flavor-tagged  $D^* \rightarrow D^0 \pi$  sample

(Phase term is based on **model assumption**)



$$\phi_3 = (78^{+11}_{-12} \pm 4 \pm 9)^\circ$$

(Belle,  $DK^-$  and  $D^*K^-$  combined)

$$(68^{+15}_{-14} \pm 4 \pm 3)^\circ$$

(BABAR,  $DK^-$ ,  $D^*K^-$  and  $DK^*$  combined)

3rd errors are from Dalitz model

→ becomes dominant in future

high-statistic experiments

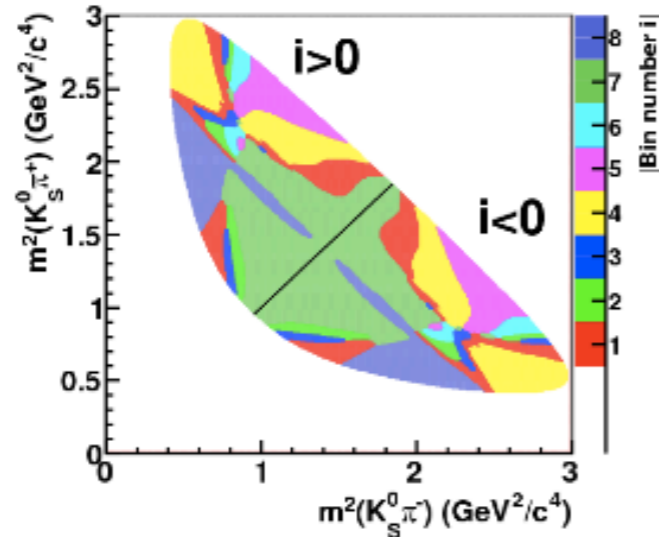


# Measurement of $\phi_3$ with GGSZ

Binned Dalitz plot analysis : Model independent

A. Giri, Yu. Grossman, A. Soffer, J. Zupan, PRD 68, 054018 (2003)

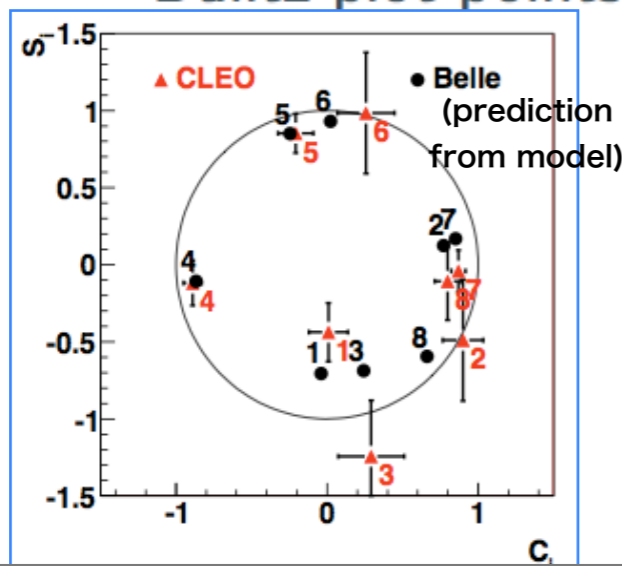
A. Bondar, A. Poluektov, EPJ C 47, 347 (2006); EPJ C 55, 51 (2008)



$$M_i^\pm = h\{K_i + r_B^2 K_{-i} + 2\sqrt{K_i K_{-i}}(x_\pm c_i + y_\pm s_i)\}$$

$$x_\pm = r_B \cos(\delta_B \pm \phi_3) \quad y_\pm = r_B \sin(\delta_B \pm \phi_3)$$

- $M_i^\pm$ : numbers of events in  $D \rightarrow K_S^0 \pi^+ \pi^-$  bins from  $B^\pm \rightarrow DK^\pm$
- $K_i$ : numbers of events in bins of flavor  $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$  from  $D^* \rightarrow D\pi$ .
- $c_i, s_i$  contain information about strong phase difference between symmetric Dalitz plot points  $(m_{K_S^0 \pi^+}^2, m_{K_S^0 \pi^-}^2)$  and  $(m_{K_S^0 \pi^-}^2, m_{K_S^0 \pi^+}^2)$ :



$$c_i = \langle \cos \Delta\delta_D \rangle, \quad s_i = \langle \sin \Delta\delta_D \rangle$$

→ estimated from quantum correlations

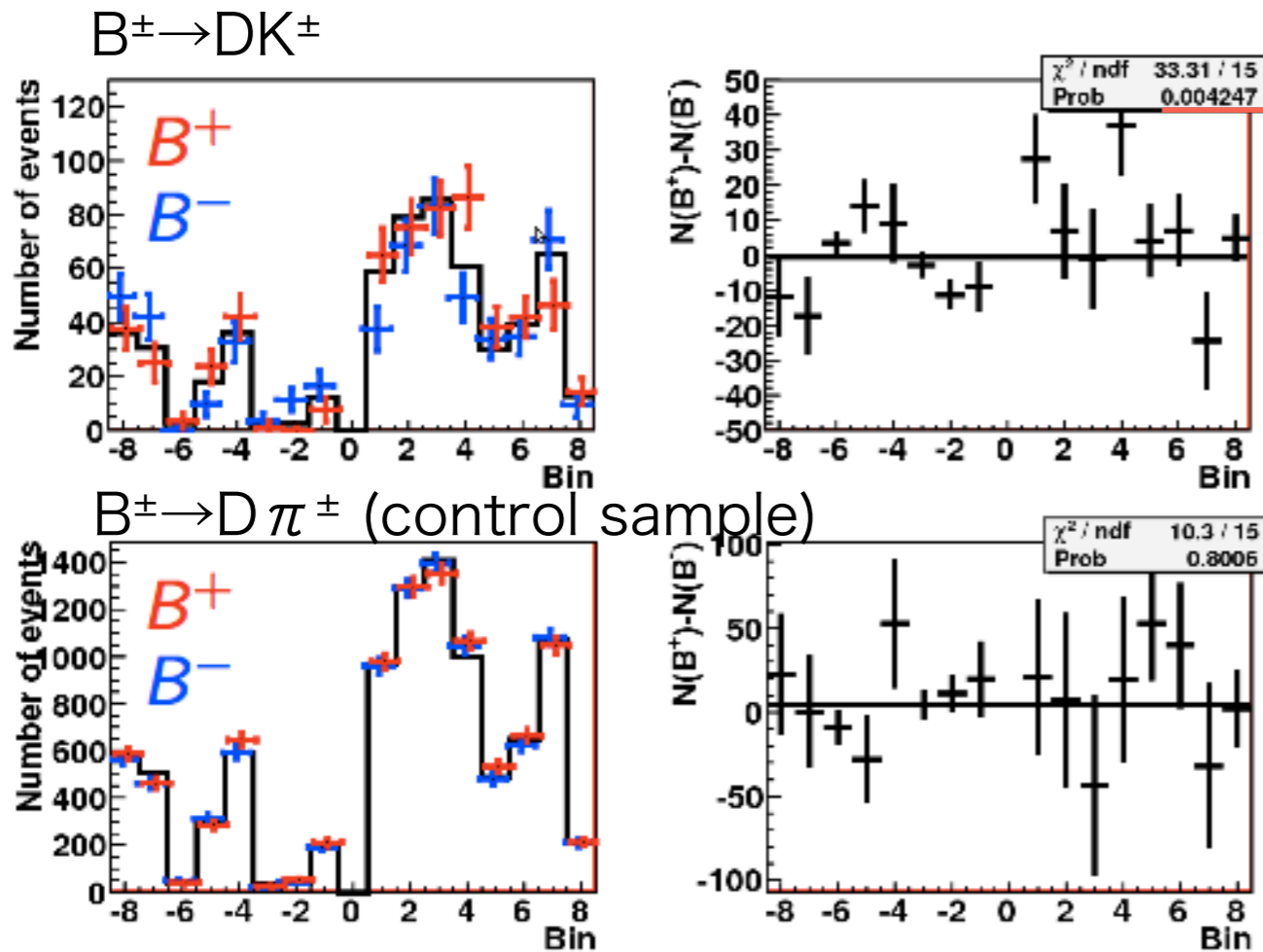
between  $D^0$  and  $\bar{D}^0$  in  $\psi(3770) \rightarrow D^0 \bar{D}^0$  decays

CLEO collaboration, PRD 82, 112006 (2010)

⇒ No model uncertainty



# Measurement of $\phi_3$ with GGSZ



→ significant direct CP-violation

$$\phi_3 = (77.3^{+15.1}_{-14.9} \pm 4.2 \pm 4.3)^\circ$$

$$r_B = 0.145 \pm 0.030 \pm 0.011 \pm 0.011$$

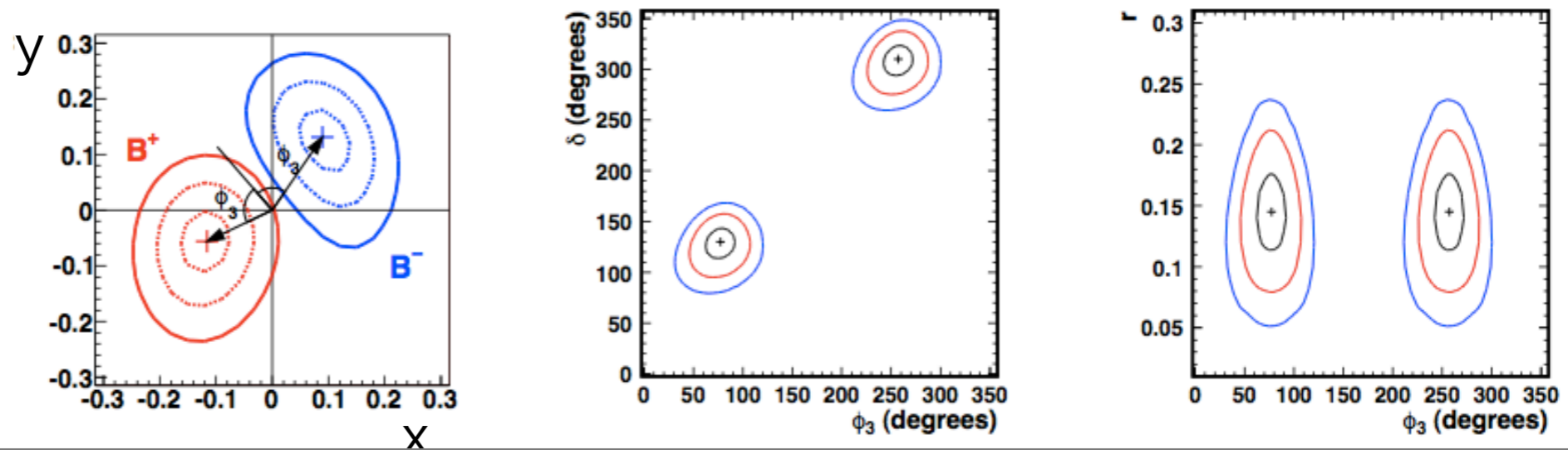
$$\delta_B = (129.9 \pm 15.0 \pm 3.9 \pm 4.7)^\circ$$

*Belle preliminary*

3rd errors are came from uncertainty of  $c_i$  and  $s_i$   
 → improved by charm-factory results

Simultaneous fit to kinematic information together with entries in each Dalitz bin.

→  $x_\pm = r \cos(\pm \phi_3 + \delta)$ ,  
 $y_\pm = r \sin(\pm \phi_3 + \delta)$   
 from  $B^\pm$



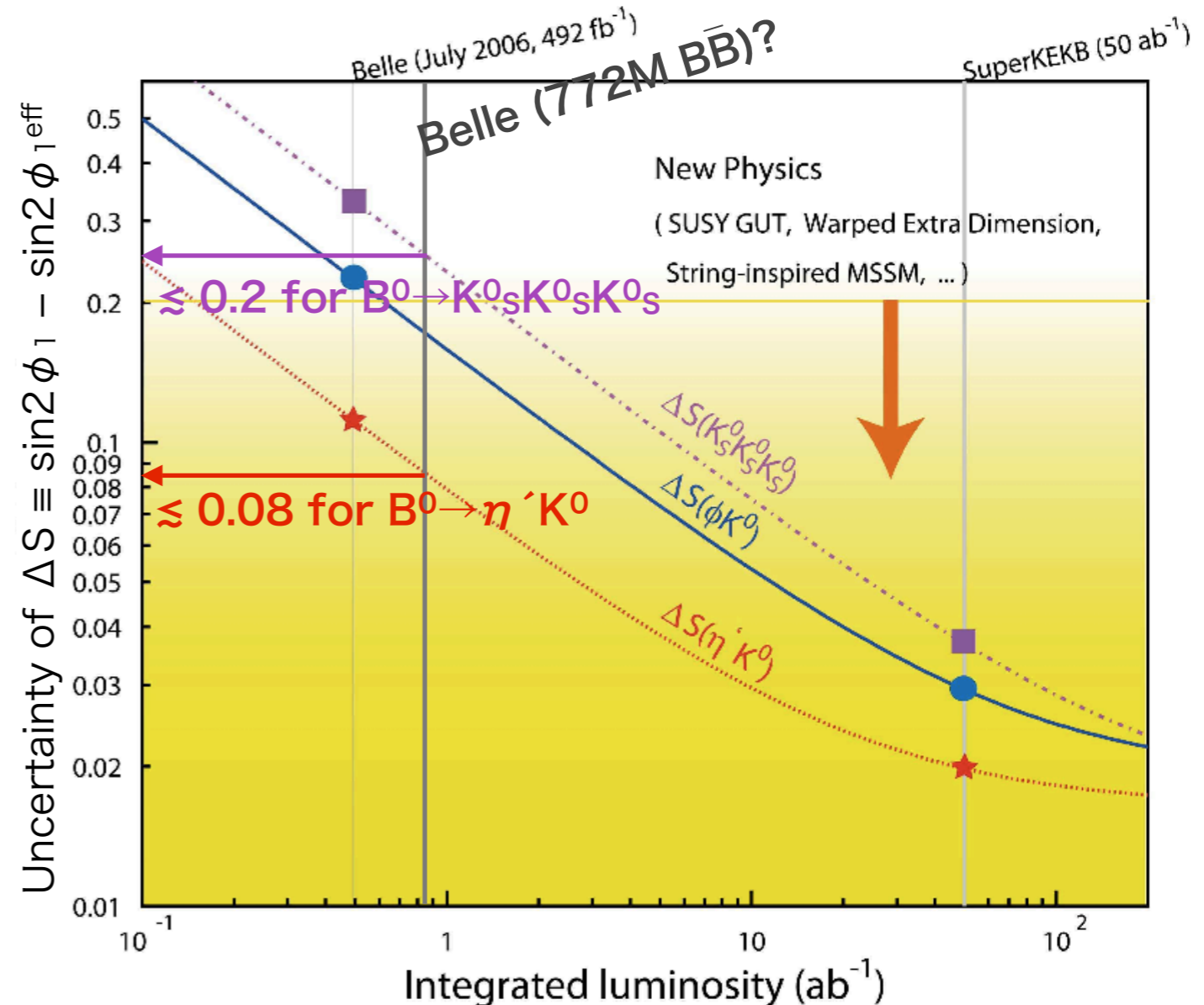
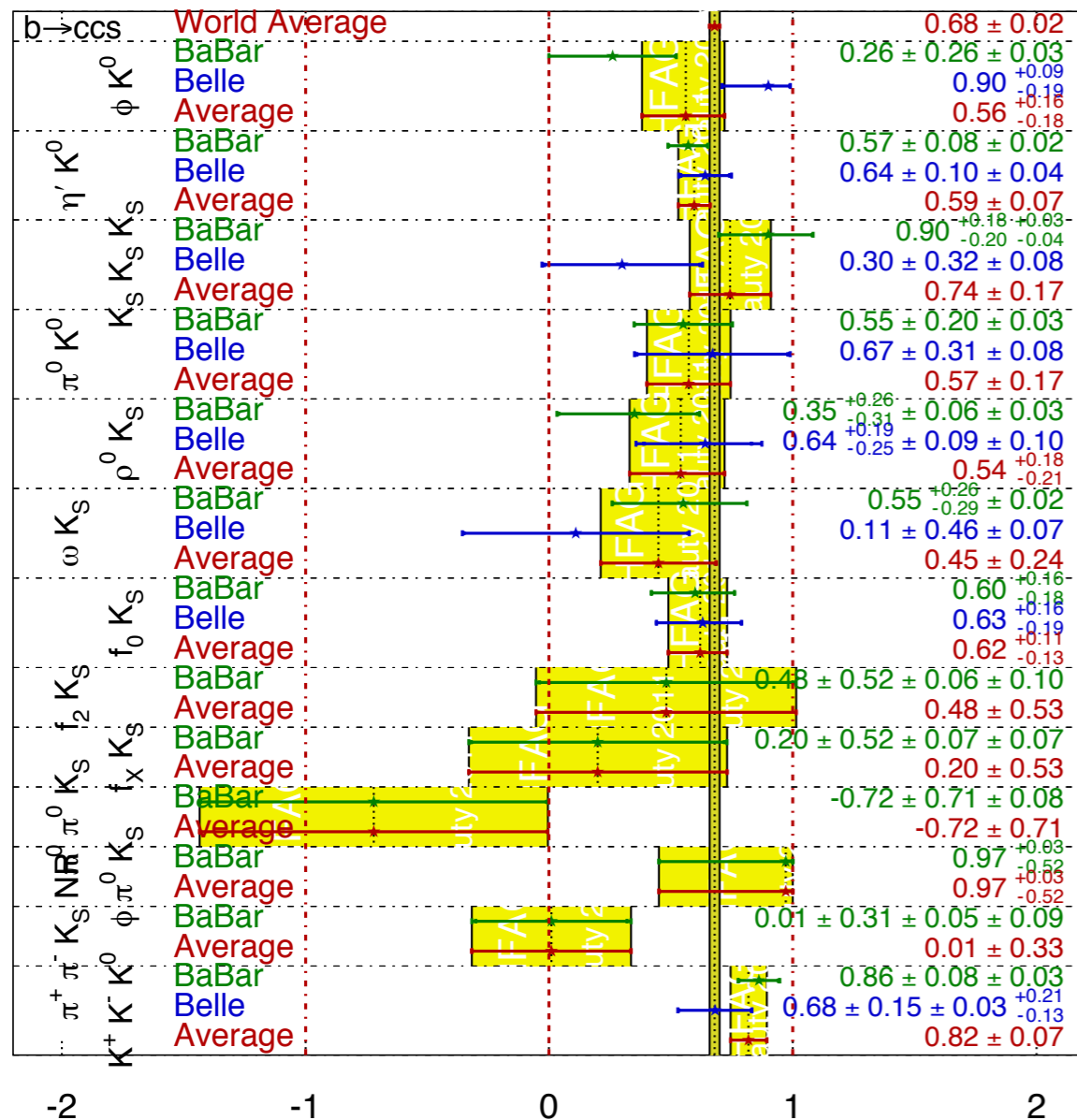
# Prospects in short term

Common analysis variables for time-dependent CPV study has been ready ( $\Delta t$  resolution, B flavor wrong tagging...)

-  $\sin 2\phi_1$  from  $b \rightarrow s$  penguin (“effective”  $\sin 2\phi_1 \equiv \sin 2\phi_1^{\text{eff}}$ )

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

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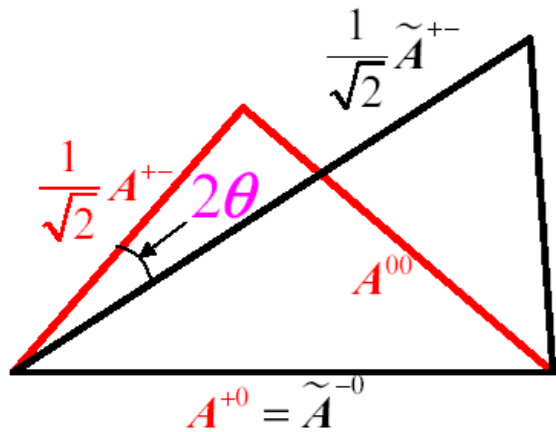
# Prospects in short term

Common analysis variables for time-dependent CPV study has been ready ( $\Delta t$  resolution, B flavor wrong tagging...)

- Time-dependent analysis and branching fraction measurements of  $B^0 \rightarrow \pi \pi$ ,  $B^0 \rightarrow \rho \rho$  for iso-spin relation analysis of  $\phi_2$
- CP violation in  $b \rightarrow c \bar{c} d$  :  $B^0 \rightarrow D^{(*)+} D^{(*)-}$

Interpretation:  $\phi_2$  constraint using isospin

M. Gronau and D. London, PRL 65, 3381 (1990)



	Amplitude for
$A^{+-}(\bar{A}^{+-})$	$B^0(\bar{B}^0) \rightarrow \pi^+ \pi^-$
$A^{00}(\bar{A}^{00})$	$B^0(\bar{B}^0) \rightarrow \pi^0 \pi^0$
$A^{+0}(\bar{A}^{-0})$	$B^+(B^-) \rightarrow \pi^+ \pi^0 (\pi^- \pi^0)$

$$\tilde{A}^{ij} = e^{2\phi_2} \bar{A}^{ij}$$

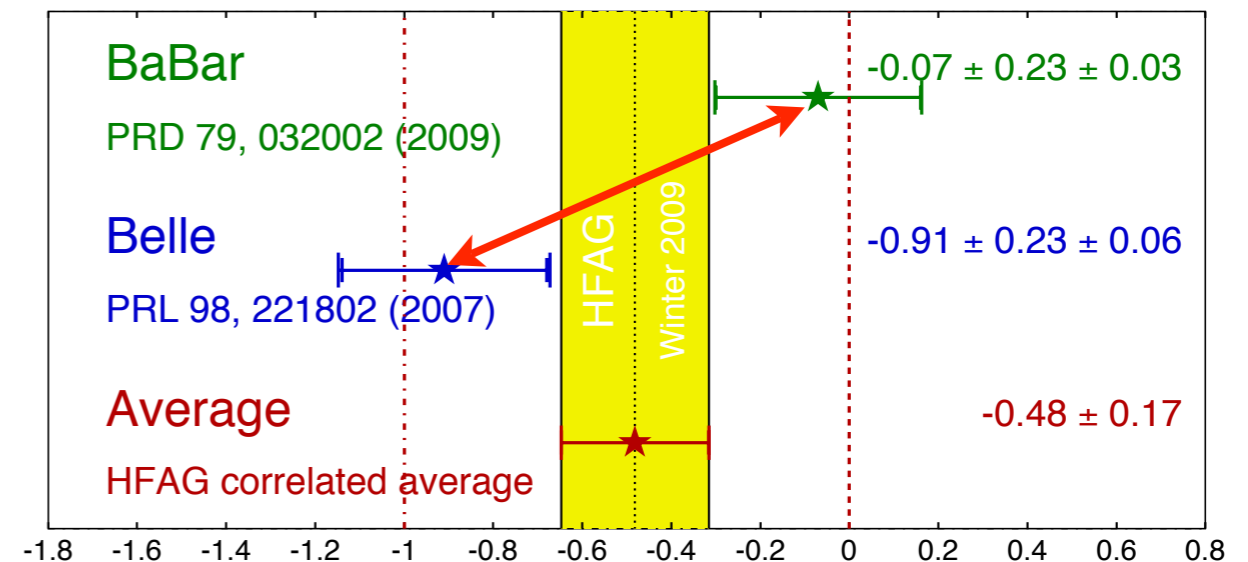
The cleanest method to extract  $\phi_2$

$$S_{\pi\pi} = \sqrt{1 - A_{\pi\pi}^2} \sin(2\phi_2 + 2\theta)$$

We use the statistical treatment of J. Charles *et al.*, Eur. Phys. J. C 41, 1 (2005)

$D^+ D^- C_{CP}$

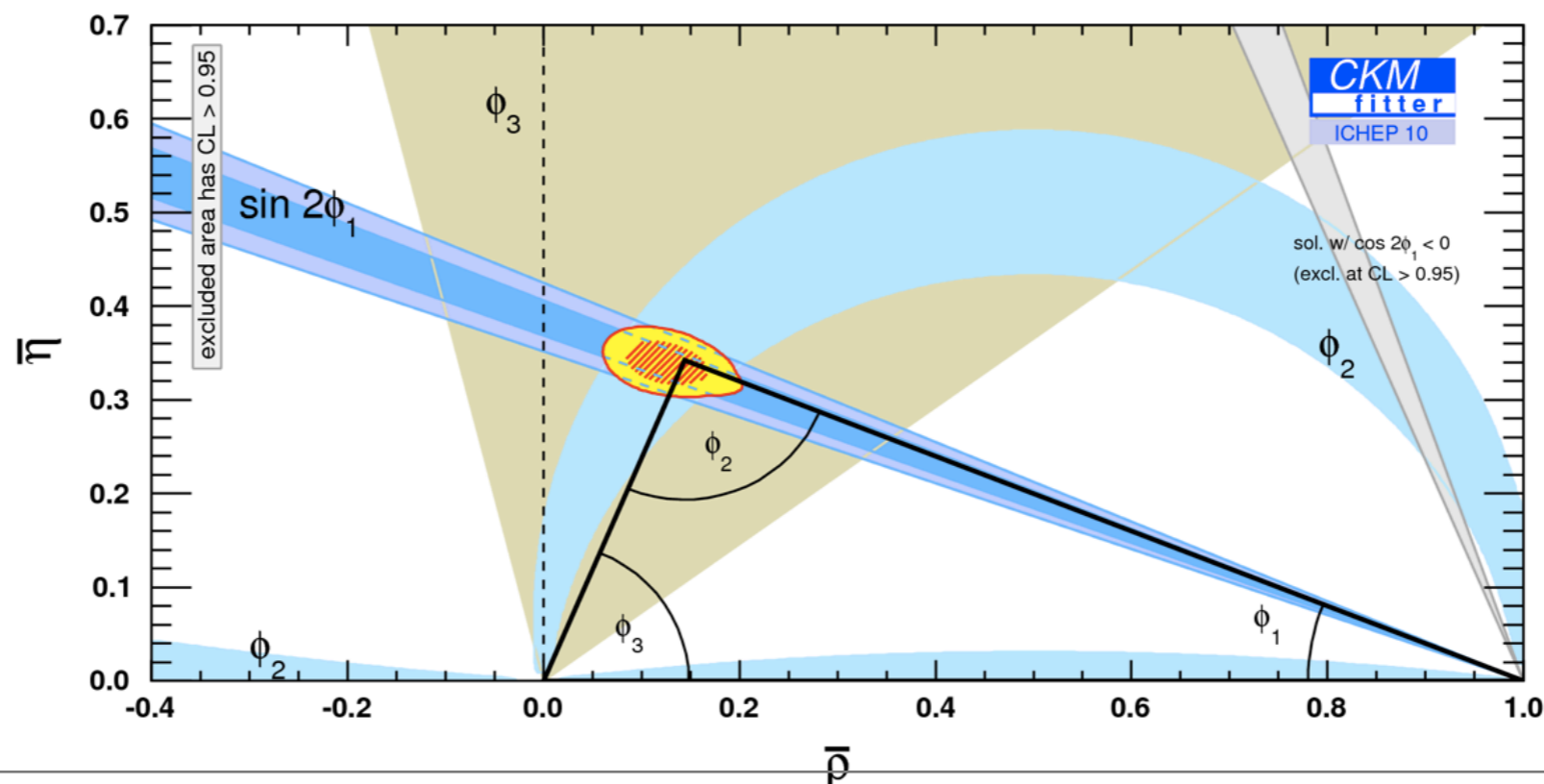
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Belle observed direct CPV in  $B^0 \rightarrow D^+ \bar{D}^-$  decay using  $535 M B \bar{B}$  → How about using full data?

# Summary

- $\sin 2\phi_1 = 0.68 \pm 0.02$  is measured in B-factories.  
( $\rightarrow$  good reference point of Standard Model)
- New technical approaches to  $\phi_3$  measurements using interference of  $B^\pm \rightarrow DK^\pm$  decays.
- We expect soon all the results from Belle final data sample.



# backup



# Systematic error of $\sin 2\phi_1$



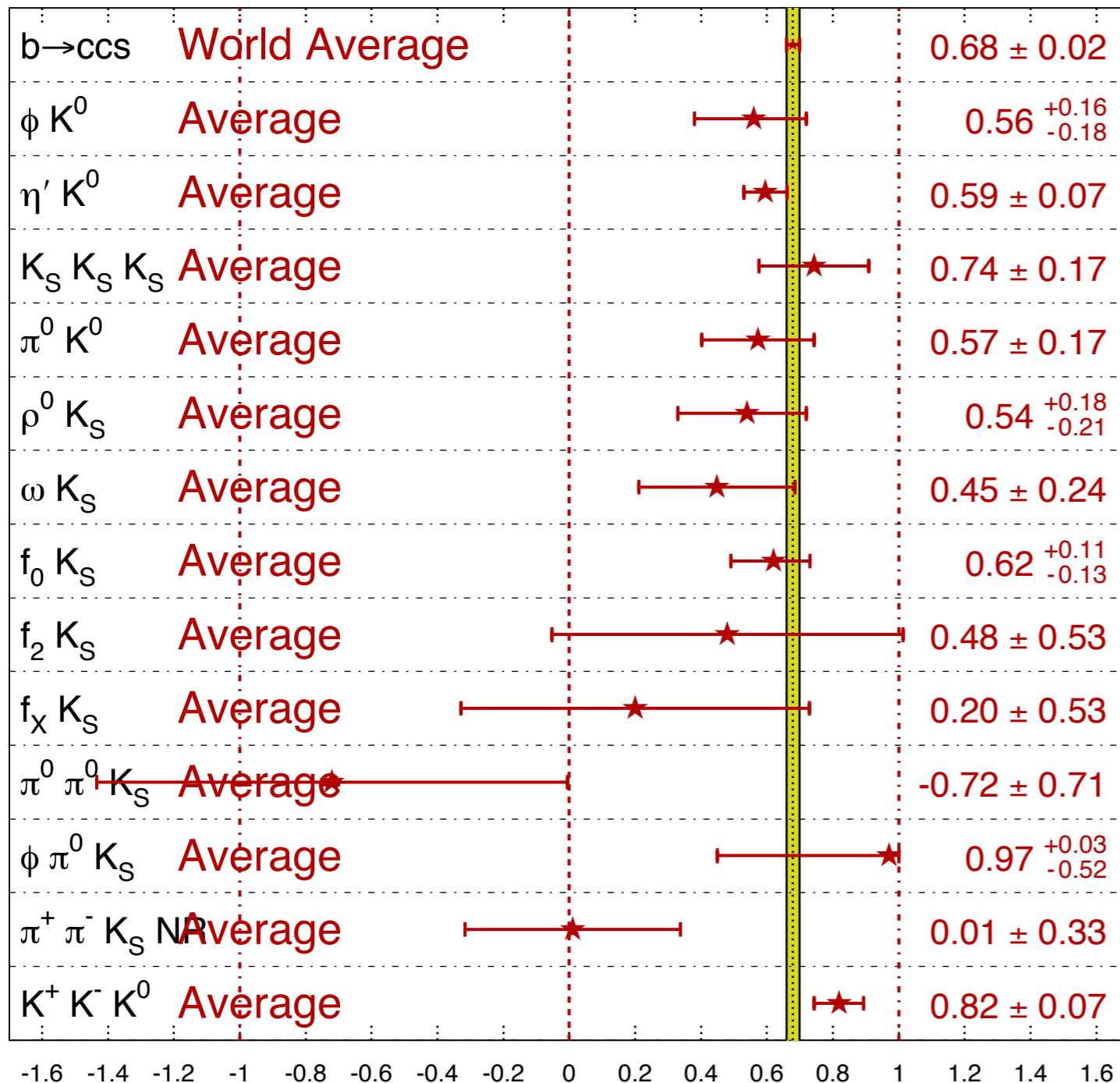
	$\delta S$	$\delta A$
Vertexing	+0.008/-0.009	$\pm 0.008$
Flavor tagging	+0.004/-0.003	$\pm 0.003$
Resolution function	$\pm 0.007$	$\pm 0.001$
Physics parameters	$\pm 0.001$	$< 0.001$
Fit bias	$\pm 0.004$	$\pm 0.005$
J/ $\psi$ Ks signal fraction	$\pm 0.002$	$\pm 0.001$
J/ $\psi$ KL signal fraction	$\pm 0.004$	+0.000/-0.002
$\psi$ 2sKs signal fraction	$< 0.001$	$< 0.001$
chic1Ks signal fraction	$< 0.001$	$< 0.001$
Background Delta_t	$\pm 0.002$	$\pm 0.001$
Tag-side interference	$\pm 0.001$	$\pm 0.008$
-----		
Total	$\pm 0.013$	$\pm 0.013$

Source/sample		Full
Beam spot	$S_f$	0.001
	$C_f$	0.001
Mistag differences	$S_f$	0.006
	$C_f$	0.002
$\Delta t$ resolution	$S_f$	0.007
	$C_f$	0.003
J/ $\psi$ $K_L^0$ background	$S_f$	0.006
	$C_f$	0.001
Background fraction and CP content	$S_f$	0.005
	$C_f$	0.003
$m_{ES}$ parameterization	$S_f$	0.002
	$C_f$	0.000
$\Delta m_d, \tau_B, \Delta \Gamma_d / \Gamma_d$	$S_f$	0.003
	$C_f$	0.001
Tag-side interference	$S_f$	0.001
	$C_f$	0.014
Fit bias (MC statistics)	$S_f$	0.002
	$C_f$	0.003
Total	$S_f$	0.012
	$C_f$	0.016

# $\sin 2\phi_1$ from $b \rightarrow s$ penguin

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

**HFAG**  
Beauty 2011  
PRELIMINARY



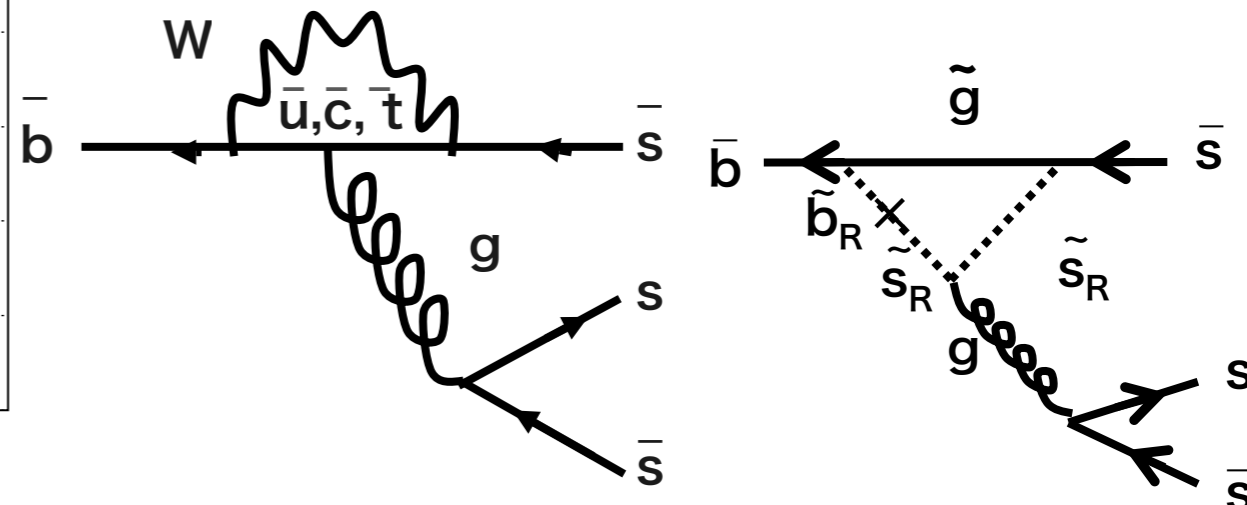
	$\Delta S$
$B^0 \rightarrow \eta' K^0$	$0.01 \pm 0.01$
$B^0 \rightarrow \phi K^0$	$0.02 \pm 0.01$
$B^0 \rightarrow \omega K_S^0$	$0.13 \pm 0.08$
$B^0 \rightarrow \rho^0 K_S^0$	$-0.08^{+0.08}_{-0.12}$
$B^0 \rightarrow K_S^0 \pi^0$	$0.07^{+0.05}_{-0.04}$

J. Zupan, hep-ph/0707.1323

	$\Delta S$
$B^0 \rightarrow K^+ K^- K_S^0$	$0.03^{+0.02}_{-0.03}$
$B^0 \rightarrow K_S^0 K_S^0 K_S^0$	$0.02^{+0.02}_{-0.03}$
$B^0 \rightarrow K_S^0 \pi^0 \pi^0$	$0.03^{+0.02}_{-0.03}$

Hai-Yang Cheng, hep-ph/0702252

Generally,  $\Delta S > 0$  is expected in SM



# Model uncertainty of $\phi_3$ Dalitz analysis



TABLE VI: Estimation of the  $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$  decay model uncertainty.

Fit model	$(\Delta r)_{\max}$	$(\Delta \phi_3)_{\max}$ ( $^\circ$ )	$(\Delta \delta)_{\max}$ ( $^\circ$ )
$F_r = F_D = 1$	0.01	3.1	3.3
$\Gamma(q^2) = \text{constant}$	0.02	4.7	9.0
$K^*(892)^+, \rho, \omega, K^*(892)^-, f_0(980), K_0^*(1430), \text{non-res.}$	0.05	8.5	22.9
No $\sigma_1$	0.01	2.6	4.3
No $\sigma_2$	0.01	0.6	0.7
CLEO model	0.02	5.7	8.7

Source	$x_-$	$y_-$	$x_+$	$y_+$	$x_-^*$	$y_-^*$	$x_+^*$	$y_+^*$	$x_{s-}$	$y_{s-}$	$x_{s+}$	$y_{s+}$
Mass and width of Breit-Wigner's	0.001	0.001	0.001	0.002	0.001	0.002	0.001	0.002	0.001	0.002	0.001	0.002
$\pi\pi$ S-wave parameterization	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.002	0.001	0.001	0.001	0.002
$K\pi$ S-wave parameterization	0.001	0.004	0.003	0.008	0.001	0.006	0.002	0.004	0.003	0.002	0.003	0.007
Angular dependence	0.001	0.001	0.002	0.001	0.001	0.001	0.001	0.002	0.002	0.001	0.002	0.001
Blatt-Weisskopf radius	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.002	0.001
Add/remove resonances	0.001	0.001	0.001	0.001	0.001	0.002	0.001	0.001	0.001	0.001	0.001	0.002
DP efficiency	0.003	0.002	0.003	0.001	0.001	0.001	0.001	0.001	0.004	0.002	0.003	0.001
Background DP shape	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001	0.001
Mistag rate	0.003	0.003	0.002	0.001	0.001	0.001	0.001	0.001	0.003	0.003	0.001	0.001
Effect of mixing	0.003	0.001	0.003	0.001	0.001	0.001	0.001	0.001	0.003	0.001	0.003	0.001
DP complex amplitudes	0.001	0.001	0.001	0.002	0.001	0.001	0.001	0.002	0.002	0.001	0.001	0.002
Total $D^0$ decay amplitude model	0.006	0.006	0.007	0.009	0.002	0.007	0.003	0.006	0.007	0.006	0.006	0.008





# $\phi_3$ : Systematic errors

Systematic errors in units  $10^{-3}$ .



Source of uncertainty	$\Delta x_-$	$\Delta y_-$	$\Delta x_+$	$\Delta y_+$
Dalitz plot efficiency	4.8	2.0	5.6	2.1
Crossfeed between bins	0.4	9.0	0.6	3.0
Signal shape	7.3	7.4	7.3	5.1
$u, d, s, c$ continuum background	6.7	5.6	6.6	3.2
$B\bar{B}$ background	7.8	12.2	7.2	6.1
$B^\pm \rightarrow D\pi^\pm$ background	1.2	4.2	1.9	1.9
Flavor-tagged statistics	1.5	2.7	1.7	1.9
Fit bias	3.2	5.8	3.2	5.8
$c_i, s_i$ precision	10.1	22.5	7.2	17.4
Total without $c_i, s_i$ precision	$\pm 14.0$	$\pm 19.4$	$\pm 14.0$	$\pm 11.3$
Total	$\pm 17.3$	$\pm 29.7$	$\pm 15.7$	$\pm 20.7$