

# Neutrinos Beyond the $\nu$ Standard Model

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# Beyond **S**tandard **M**odel **because**

**1) Experimental evidence** for new particle physics:

**\*\*\* Neutrino masses**

**\*\*\* Dark matter**

**\*\* Matter-antimatter asymmetry**

**2) SM fine-tunings/uneasiness**

$SU(3) \times SU(2) \times U(1) \times \text{classical gravity}$

We ~understand ordinary particles= excitations over the vacuum

We DO NOT understand the vacuum = state of lowest energy:

## SU(3) x SU(2) x U(1) x classical gravity

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We DO NOT understand the vacuum = state of lowest energy:

- The **gravity** vacuum: cosmological cte.  $\Lambda$ ,  $\Lambda \sim 10^{-123} M_{\text{Planck}}^4$
- \* The **QCD** vacuum : Strong CP problem,  $\theta_{\text{QCD}} < 10^{-10}$
- \* The **electroweak** vacuum: Higgs-mass, v.e.v.  $\sim O(100)$  GeV

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- \* The **electroweak** vacuum: Higgs-mass, v.e.v.  $\sim O(100)$  GeV

The Higgs excitation has the quantum numbers of the EW vacuum

# BSM because

**1) Experimental evidence** for new particle physics:

**\*\*\* Neutrino masses**

**\*\*\* Dark matter**

**\*\* Matter-antimatter asymmetry**

**2) SM fine-tunings/uneasiness**, i.e. in electroweak:

**\*\*\* Hierarchy problem**

**\*\*\* Flavour puzzle**

## More wood for the Flavour Puzzle

$$\begin{array}{l} \text{Leptons} \\ V_{\text{PMNS}} = \end{array} \left( \begin{array}{ccc} 0.8 & 0.5 & ? (<10^\circ) \\ -0.4 & 0.5 & -0.7 \\ -0.4 & 0.5 & +0.7 \end{array} \right)$$
  
$$\begin{array}{l} \text{Quarks} \\ V_{\text{CKM}} = \end{array} \left( \begin{array}{ccc} \sim 1 & \lambda & \lambda^3 \\ \lambda & \sim 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & \sim 1 \end{array} \right) \lambda \sim 0.2$$

**Why so different?**

## More wood for the Flavour Puzzle

$$\text{Leptons } V_{\text{PMNS}} = \begin{pmatrix} 0.8 & 0.5 & ? (<10^\circ) \\ -0.4 & 0.5 & -0.7 \\ -0.4 & 0.5 & +0.7 \end{pmatrix}$$

$$\text{Quarks } V_{\text{CKM}} = \begin{pmatrix} \sim 1 & \lambda & \lambda^3 \\ \lambda & \sim 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & \sim 1 \end{pmatrix} \lambda \sim 0.2$$

**Maybe because of Majorana neutrinos?**



## Dirac or Majorana ?

- **The only thing we have really understood in particle physics is the gauge principle**
- **$SU(3) \times SU(2) \times U(1)$  gauge allow Majorana masses....**

**Lepton number was an accidental symmetry of the SM:  
unless you impose it by hand, Majorana masses will be there**

**Anyway, it is for experiment to decide**

# Main physics goals in $\nu$ physics

- To determine the absolute scale of masses
- To determine whether they are Majorana
- To discover Leptonic CP-violation

**Let us go for those discoveries !**

Can we foresee how to go beyond?

Neutrino masses indicate new  
physics beyond the SM

Maybe new physics could appear  
also in neutrino couplings ?

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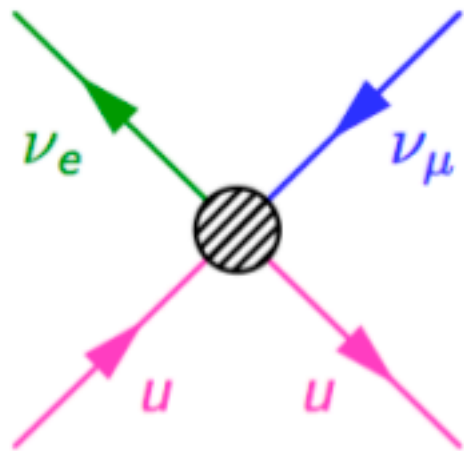


Maybe new physics could appear  
also in NSI ?

NSI = non-standard neutrino interactions

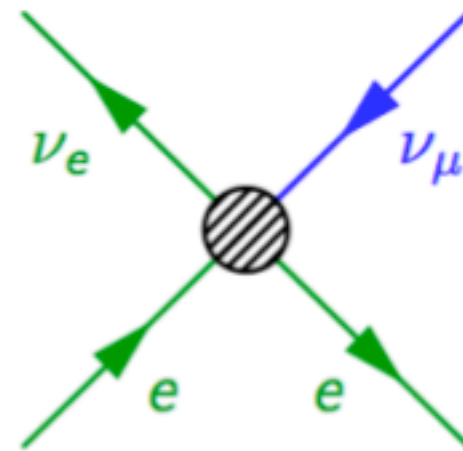
# What are non-standard neutrino interactions (NSI)?

Four-fermion interactions that do not preserve flavour, i.e.



$$\frac{1}{\Lambda^2} \bar{\nu}_e \nu_\mu \bar{u} u$$

$$\Lambda > v$$



$$\frac{1}{\Lambda^2} \bar{\nu}_e \nu_\mu \bar{e} e$$

## Two topics

- “Seesaw NSI” and the flavour puzzle
- “Why not” NSI



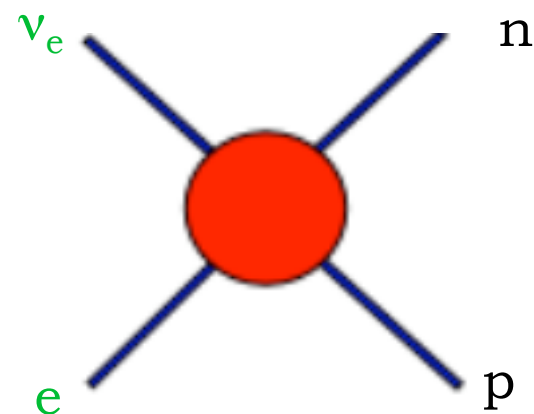
How to go about it model-independent ?....

## Effective field theory

Recall Fermi's times,

→ Four-Fermi interaction

$$G_F (\bar{e}_L \gamma_\mu \nu_e) (\bar{n} \gamma_\mu p)$$



$U(1)_{em}$  gauge invariant

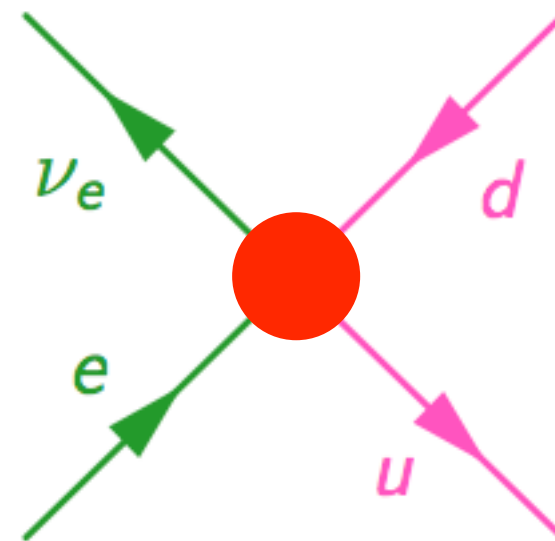
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## Effective field theory

Glashow, Weinberg, Salam times:

→ Four-Fermi interaction

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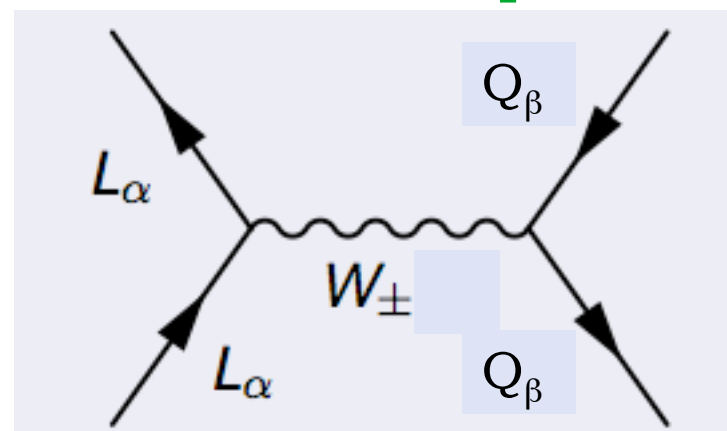
## Effective field theory

Glashow, Weinberg, Salam era:

→ Four-Fermi interaction

$$\frac{g^2}{M_W^2} (\bar{L}_\alpha \gamma_\mu L_\alpha) (\bar{Q}_{L\beta} \gamma_\mu Q_\beta)$$

### Mediator decomposition



$SU(2) \times U(1)_{em}$  gauge invariant

# $\nu$ masses and couplings beyond the SM

In the spirit of Fermi,

Can we build Standard Model operators that

give mass to the neutrinos

and/or new flavoured couplings ?

**YES!**

If new physics scale  $M > v$

$$\mathcal{L} = \mathcal{L}_{\text{low-energy}} + \frac{\mathcal{O}^{d=5}}{M} + \frac{\mathcal{O}^{d=6}}{M^2} + \dots$$

If new physics scale  $M > v$

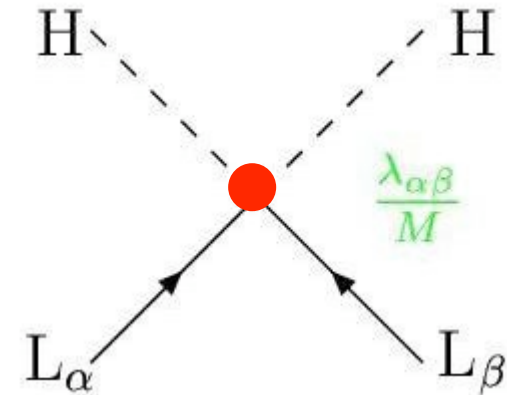
$$\mathcal{L} = \mathcal{L}_{\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)} + \frac{\text{O}^{d=5}}{M} + \frac{\text{O}^{d=6}}{M^2} + \dots$$

# $\nu$ masses beyond the SM

## The Weinberg operator

Dimension 5 operator:

$$\lambda/M \underbrace{(\text{L L H H})}_{\text{O}^{d=5}} \rightarrow \lambda \nu^2/M (\nu\nu)$$



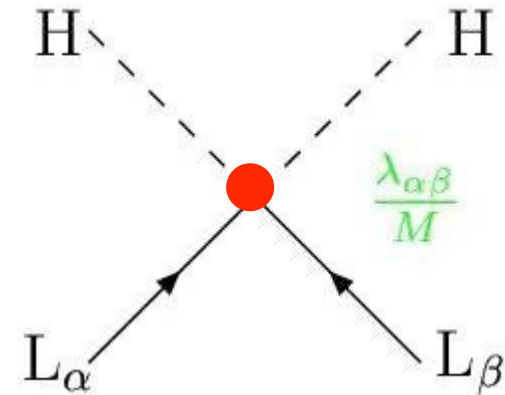
It's unique → very special role of  $\nu$  masses:  
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This mass term **violates lepton number (B-L)**  
→ **Majorana** neutrinos

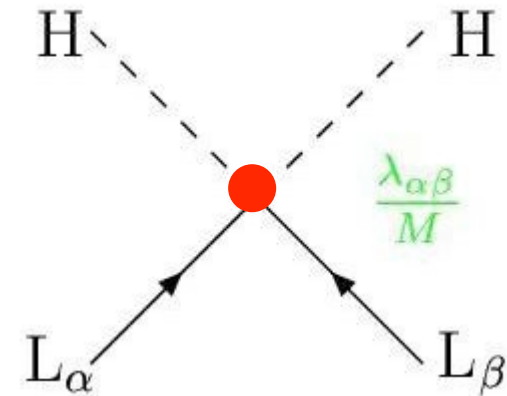


# $\nu$ masses beyond the SM

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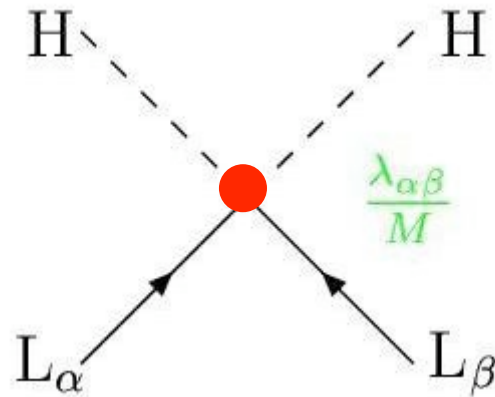
This mass term **violates lepton number (B-L)**  
→ **Majorana neutrinos**

$\text{O}^{d=5}$  is common to all models of Majorana  $\nu$ s

New Standard Model  $\nu$ SM ?

$$\mathcal{L}_{\nu SM} = \mathcal{L}_{SM} + c^{d=5} \frac{O^{d=5}}{\Lambda_{LN}} + \dots$$

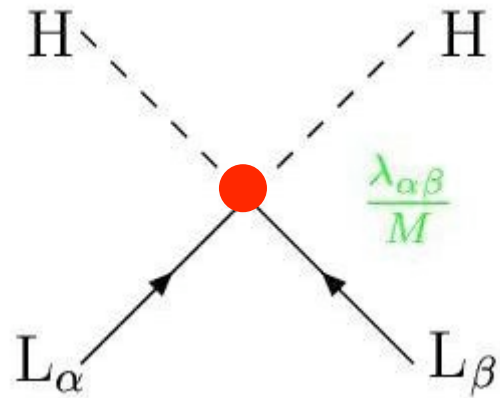
# $\nu$ masses beyond the SM : tree level



$$\delta\mathcal{L} = c^{d=5} \mathcal{O}^{d=5}$$

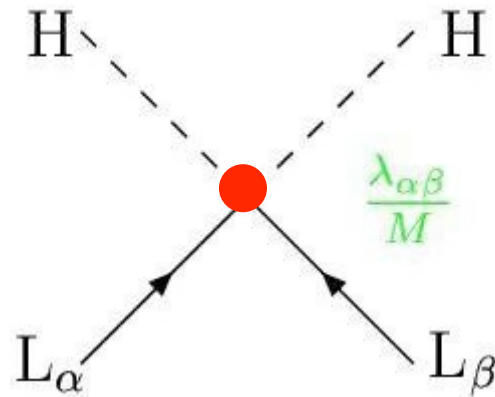
3 generic types (Ma)

# $\nu$ masses beyond the SM : tree level



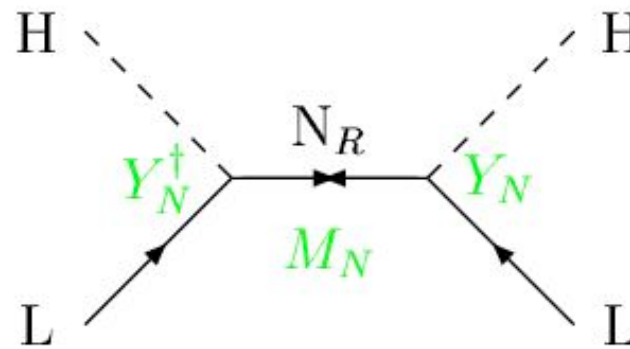
$$2 \times 2 = 1 + 3$$

# $\nu$ masses beyond the SM : tree level



$$2 \times 2 = \textcircled{1} + 3$$

# $\nu$ masses beyond the SM : tree level

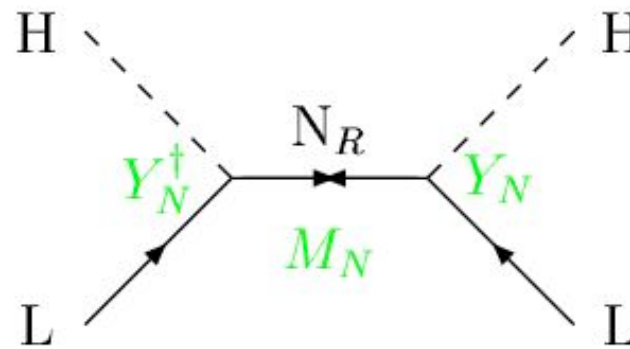


Fermionic Singlet  
Seesaw ( or type I)

$$2 \times 2 = \textcircled{1} + 3$$

$$m_\nu \sim v^2 \mathbf{C}^{d=5} = v^2 Y_N^\top Y_N / M_N$$

# $\nu$ masses beyond the SM : tree level



Fermionic Singlet  
Seesaw ( or type I)

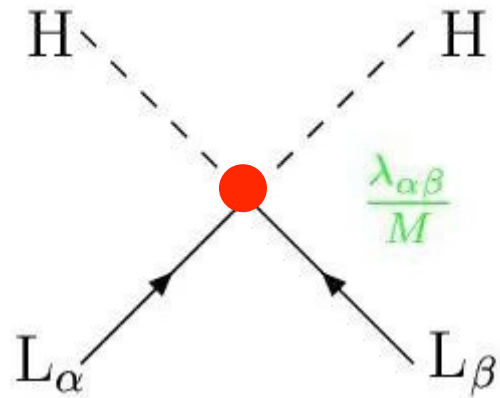
$$2 \times 2 = \textcircled{1} + 3$$

$$m_\nu \sim v^2 \mathbf{C}^{d=5} = v^2 Y_N^\top Y_N / M_N$$

Which allows  $Y_N \sim 1 \rightarrow M \sim M_{\text{Gut}}$

$Y_N \sim 10^{-6} \rightarrow M \sim \text{TeV}$

# $\nu$ masses beyond the SM : tree level

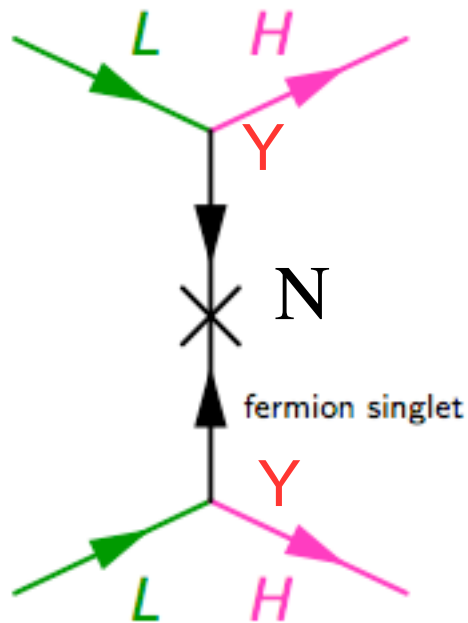


$$2 \times 2 = 1 + \textcircled{3}$$



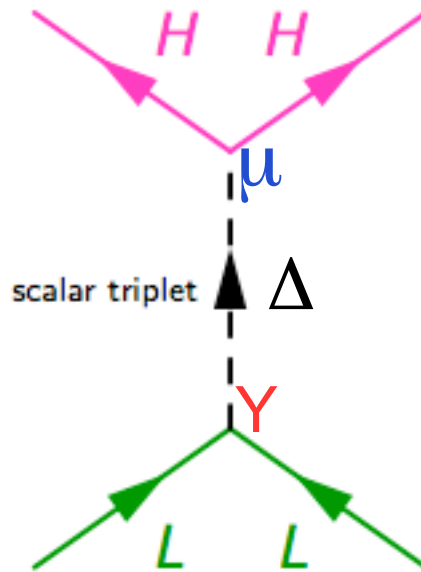
# The Seesaw models

- Three types of models yield the Weinberg operator at tree level



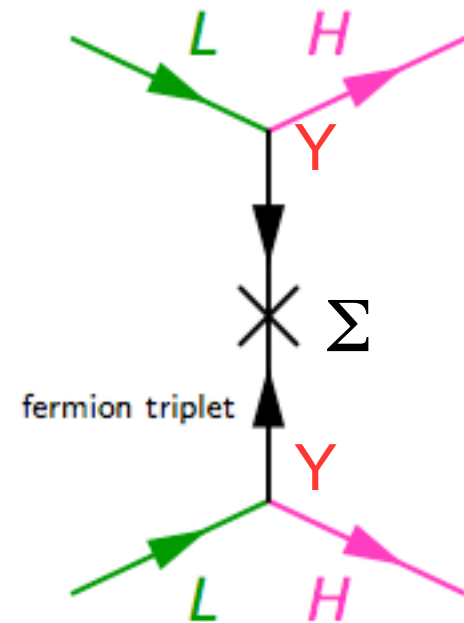
Type I

$$m_\nu \sim v^2 Y_N^T \frac{1}{M_N} Y_N$$



Type II

$$m_\nu \sim v^2 Y_\Delta \frac{\mu}{M_\Delta^2}$$

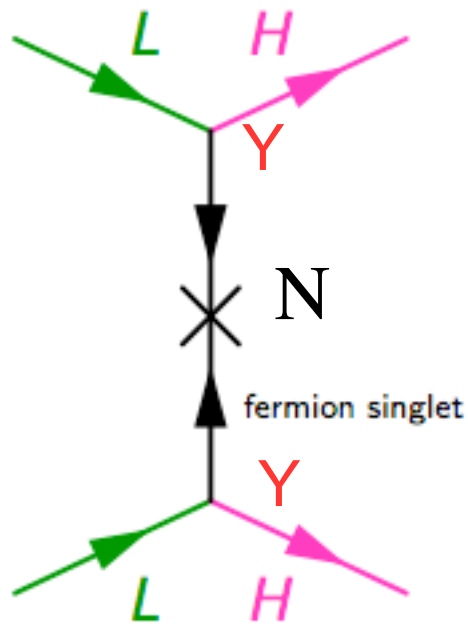


Type III

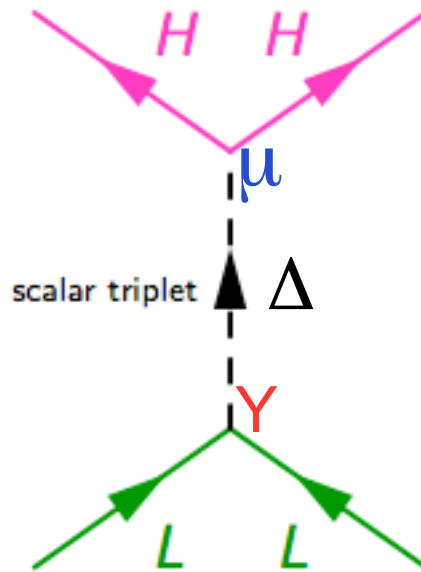
$$m_\nu \sim v^2 Y_\Sigma^T \frac{1}{M_\Sigma} Y_\Sigma$$

# The Seesaw models

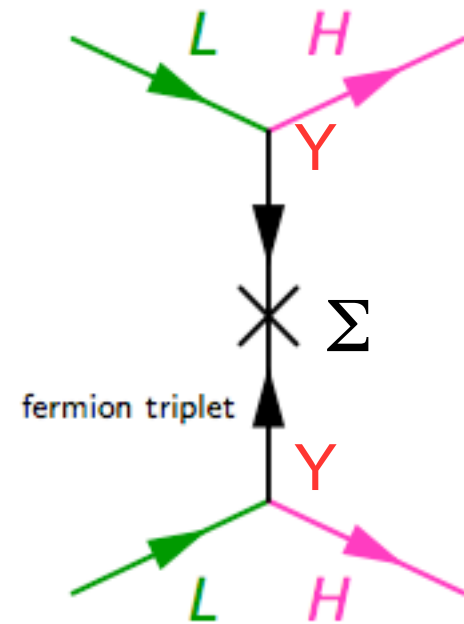
- Three types of models yield the Weinberg operator at tree level



Type I



Type II



Type III

Heavy fermion singlet  $N_R$   
 Minkowski, Gell-Mann, Ramond,  
 Slansky, Yanagida, Glashow,  
 Mohapatra, Senjanovic

Heavy scalar triplet  $\Delta$   
 Magg, Wetterich, Lazarides,  
 Shafi, Mohapatra,  
 Senjanovic, Schechter, Valle

Heavy fermion triplet  $\Sigma_R$   
 Ma, Roy, Senjanovic, Hambye et al.,

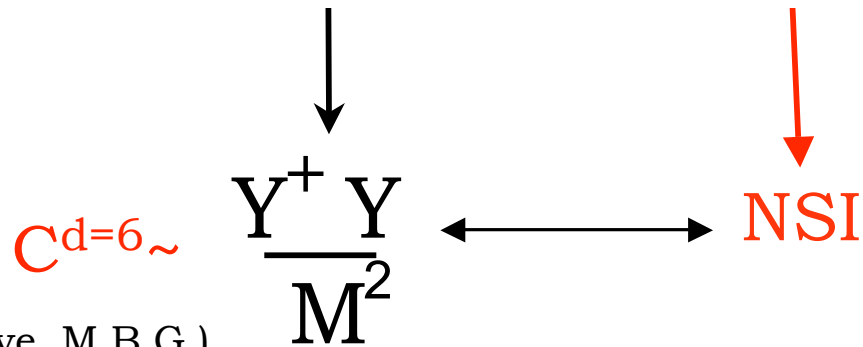
Those fields,  $N_R$ ,  $\Delta$ ,  $\Sigma_R$ , would mediate other processes too....

Which are the new exotic couplings,  
that is,  $d=6$  operators, in Seesaws?

Model	Effective Lagrangian $\mathcal{L}_{eff} = c_i \mathcal{O}_i$		
	$c^{d=5}$	$c_i^{d=6}$	$\mathcal{O}_i^{d=6}$
Fermionic Singlet (type I)	$Y_N^T \frac{1}{M_N} Y_N$	$Y_N^\dagger \frac{1}{ M_N ^2} Y_N$	$(\bar{L}\tilde{H}) i\not{\partial} (\tilde{H}^\dagger L)$
Fermionic Triplet (type III)	$Y_\Sigma^T \frac{1}{M_\Sigma} Y_\Sigma$	$Y_\Sigma^\dagger \frac{1}{ M_\Sigma ^2} Y_\Sigma$	$(\bar{L}\vec{\tau}\tilde{H}) i\not{D} (\tilde{H}^\dagger \vec{\tau} L)$
Scalar Triplet (type II)	$4Y_\Delta \frac{\mu_\Delta}{ M_\Delta ^2}$	$Y_\Delta^\dagger \frac{1}{2 M_\Delta ^2} Y_\Delta$	$(\bar{L}\vec{\tau} L) (\bar{L}\vec{\tau}\tilde{L})$
		$\frac{ \mu_\Delta ^2}{ M_\Delta ^4}$	$(H^\dagger \vec{\tau} \tilde{H}) (\bar{D}_\mu \vec{D}^\mu) (\tilde{H}^\dagger \vec{\tau} H)$
		$-2(\lambda_3 + \lambda_5) \frac{ \mu_\Delta ^2}{ M_\Delta ^4}$	$(H^\dagger H)^3$

(Abada, Biggio, Bonnet, Hambye, M.B.G.)

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		$\frac{ \mu_\Delta ^2}{ M_\Delta ^4}$	$(H^\dagger \vec{\tau} \tilde{H}) (D_\mu D^\mu) (\tilde{H}^\dagger \vec{\tau} H)$
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(Abada, Biggio, Bonnet, Hambye, M.B.G.)

## Non-unitary NSI

The complete theory of  $\nu$  masses is unitary.

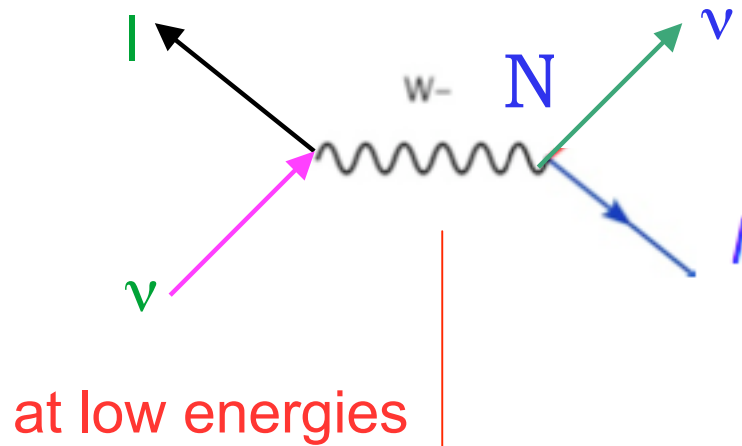
In all fermionic seesaws

the neutrino mass matrix is larger than  $3 \times 3$

$$\left[ \begin{array}{c} \left( \begin{array}{c} 3 \times 3 \end{array} \right) \\ \phantom{\left( \begin{array}{c} 3 \times 3 \end{array} \right)} \end{array} \right]$$

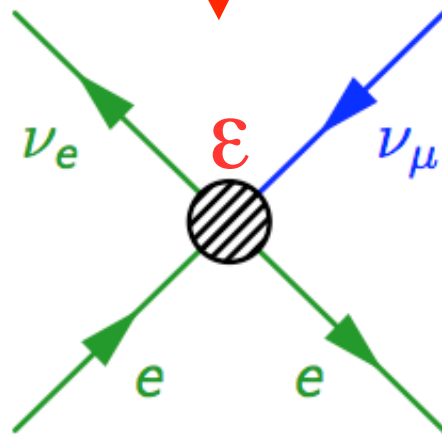
All fermionic Seesaws exhibit non-unitary mixing

i.e.



$$N = (1 + \epsilon) U_{\text{PMNS}}$$

NSI



$$\epsilon_{\alpha\beta} = \frac{v^2}{2} |Y^\dagger \frac{1}{|M|^2} Y|_{\alpha\beta}$$

All fermionic Seesaws exhibit non-unitary mixing

$$|\mathcal{E}| \approx \begin{pmatrix} < 2.5 \cdot 10^{-3} & < 3.6 \cdot 10^{-5} & < 8.0 \cdot 10^{-3} \\ < 3.6 \cdot 10^{-5} & < 2.5 \cdot 10^{-3} & < 5.0 \cdot 10^{-3} \\ < 8.0 \cdot 10^{-3} & < 5.0 \cdot 10^{-3} & < 2.5 \cdot 10^{-3} \end{pmatrix}$$

Very strong bounds for **NSI** from non-unitarity...



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Very strong bounds for **NSI** from non-unitarity...

..... because non-unitarity affects simultaneously:

**matter propagation + production and detection (= rare decays...)**

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		$-2(\lambda_3 + \lambda_5) \frac{ \mu_\Delta ^2}{ M_\Delta ^4}$	$(H^\dagger H)^3$

$C^{d=6} \sim$

$$\frac{Y^\dagger Y}{M^2}$$

Exotic lepton couplings

(Abada, Biggio, Bonnet, Hambye, M.B.G.)

For all scalar and fermionic  
Seesaw models, present bounds:

$$\frac{v^2}{2} |c^{d=6}|_{\alpha\beta} = \frac{v^2}{2} |Y^\dagger \frac{1}{M^2} Y|_{\alpha\beta} \lesssim 10^{-2}$$



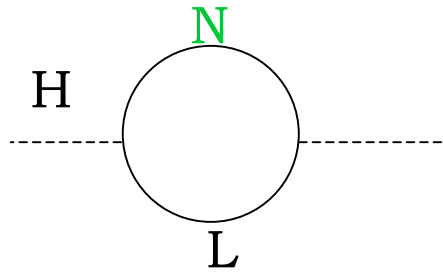
$$|Y| \lesssim 10^{-1} \frac{M}{1\text{TeV}}$$

or stronger

Observable effects?

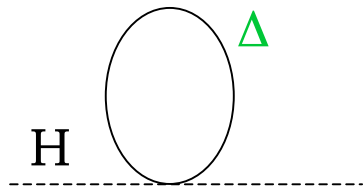
Obviously requires scale near the TeV

$M \sim 1$  TeV is suggested by electroweak hierarchy problem



$$\delta m_H^2 = -\frac{Y_N^\dagger Y_N}{16\pi^2} \left[ 2\Lambda^2 + 2M_N^2 \log \frac{M_N^2}{\Lambda^2} \right]$$

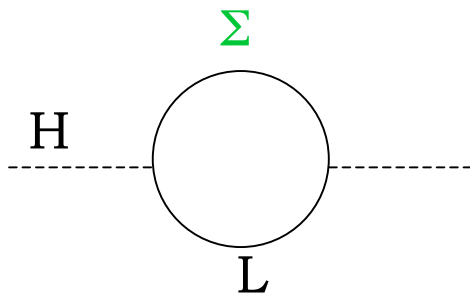
(Vissani, Casas et al., Schmaltz)



$$\delta m_H^2 = -3 \frac{\lambda_3}{16\pi^2} \left[ \Lambda^2 + M_\Delta^2 \left( \log \frac{M_\Delta^2}{\Lambda^2} - 1 \right) \right]$$

$$- \frac{\mu_\Delta^2}{2\pi^2} \log \left( \left| \frac{M_\Delta^2 - \Lambda^2}{M_\Delta^2} \right| \right)$$

(Abada, Biggio, Bonnet, Hambye, M.B.G.)



$$\delta m_H^2 = -3 \frac{Y_\Sigma^\dagger Y_\Sigma}{16\pi^2} \left[ 2\Lambda^2 + 2M_\Sigma^2 \log \frac{M_\Sigma^2}{\Lambda^2} \right]$$

# Could d=6 be stronger than d=5 ?

\* Two independent scales in d=5, d=6 may result from a symmetry principle: lepton number

Cirigliano et al; Kersten, Smirnov; Abada et al

\* d=5 requires to violate lepton number

\* d=6 does not violate any symmetry

$$\Lambda_5 \sim \Lambda_{\text{LN}} \gg \Lambda_6 \sim \Lambda_{\text{LFV}} \sim \text{TeV}$$

$$\Lambda_{LN} \gg \Lambda_{fl} \sim \text{TeV} ?$$

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{\alpha}{\Lambda_{LN}} O_i^{d=5} + \sum_i \frac{\beta_i}{\Lambda_{\text{flavour}}^2} O_i^{d=6} + \dots$$

Cirigliano, et al

There is a sensible physics motivation:

- Origin of lepton/quark flavour violation linked/close to the EW scale
- (Effective) Lepton number breaking scale higher and responsible for the gap between  $\nu$  and other fermion



Seesaw mechanism

vs

Minimal Flavour Violation

T. Hambye, D. Hernández, P. Hernández, MBG

## Minimal Flavour violation (MFV)

- Flavour data (i.e. B physics) consistent with all flavour physics coming from Yukawa

**MFV Hypothesis**  $\equiv$  The Yukawas are the only sources (*irreducible*) of flavour violation. in BSM

R. S. Chivukula and H. Georgi, Phys. Lett. B **188**, 99 (1987).



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R. S. Chivukula and H. Georgi, Phys. Lett. B 188, 99 (1987).

It is very predictive for quarks:

$$O^{d=6} \sim \bar{Q}_\alpha Q_\beta \bar{Q}_\gamma Q_\delta$$

$$\mathcal{L} = \mathcal{L}_{SM} + c^{d=6} O^{d=6} + \dots$$

i.e.

$$c^{d=6} \sim \frac{Y_{\alpha\beta}^+ Y_{\gamma\delta}}{\Lambda_{\text{flavour}}^2} \quad O^{d=6} \sim \bar{Q}_\alpha Q_\beta \bar{Q}_\gamma Q_\delta$$

# WHY MFV?

# FOR QUARKS

- Hierarchy Problem points to  $\Lambda \sim \text{TeV}$

$\mathcal{O}_{d=6}^i$	$\Lambda_{fl} C_{d=6} = 1$	
$(\bar{s}_L \gamma^\mu d_L)^2$	$9.8 \times 10^2$	$1.6 \times 10^4$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	$1.8 \times 10^4$	$3.2 \times 10^5$
$(\bar{c}_L \gamma^\mu u_L)^2$	$1.2 \times 10^3$	$2.9 \times 10^3$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	$6.2 \times 10^3$	$1.5 \times 10^4$
$(\bar{b}_L \gamma^\mu d_L)^2$	$5.1 \times 10^2$	$9.3 \times 10^2$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	$1.9 \times 10^3$	$3.6 \times 10^3$
$(\bar{b}_L \gamma^\mu s_L)^2$		$1.1 \times 10^2$
$(\bar{b}_R s_L)(\bar{b}_L s_R)$		$3.7 \times 10^2$

$C_{d=6} \equiv C_{d=6}(Y_u, Y_d)$

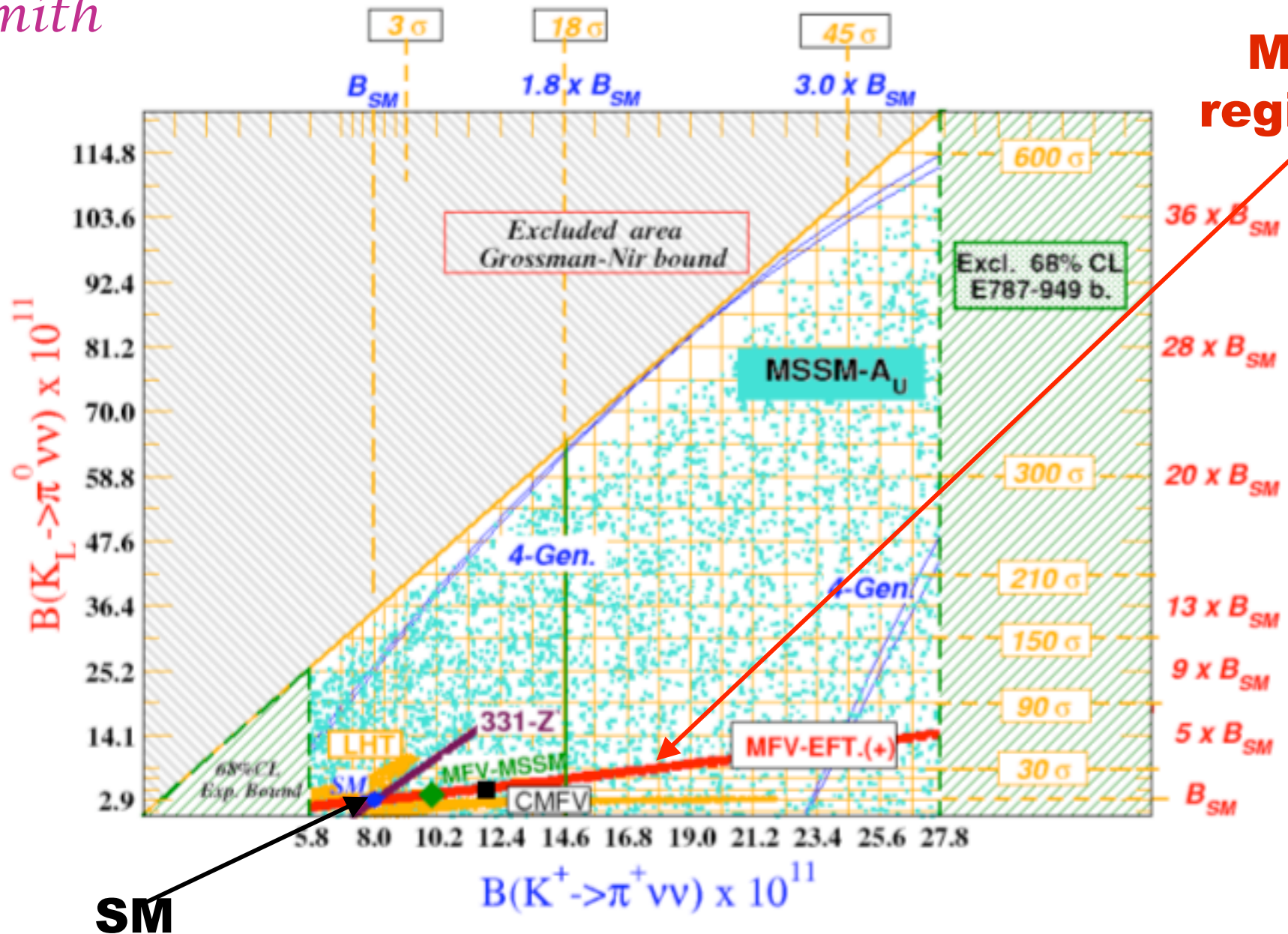
$\mathcal{O}_{d=6}^i$	$\Lambda_{fl}$
$H^\dagger (\bar{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} Q_L) (e F_{\mu\nu})$	6.1 TeV
$\frac{1}{2} (\bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L)^2$	5.9 TeV
$H_D^\dagger (\bar{D}_R Y^{d\dagger} Y^u Y^{u\dagger} \sigma_{\mu\nu} T^a Q_L) (g_s G_{\mu\nu}^a)$	3.4 TeV
$(\bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (\bar{E}_R \gamma_\mu E_R)$	2.7 TeV
$i (\bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) H_U^\dagger D_\mu H_U$	2.3 TeV
$(\bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (\bar{L}_L \gamma_\mu L_L)$	1.7 TeV
$(\bar{Q}_L Y^u Y^{u\dagger} \gamma_\mu Q_L) (e D_\mu F_{\mu\nu})$	1.5 TeV

WITHOUT MFV:  $\Lambda_{fl} \gtrsim 10^2 \text{ TeV}$

WITH MFV:  $\Lambda_{fl} \gtrsim \text{TeV}$

I. NA62 main targets are the rare K decays ( $Br \lesssim 10^{-11}$ ), e.g.  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  5

Smith



**MFV region**

**SM**

# What happens in the presence of neutrino masses?

Cirigliano, Isidori, Grinstein, Wise

In the lepton sector

$$\mathcal{L} = \underbrace{\dots + Y_e \bar{L} \phi e_R}_{\mathcal{L}_{SM}} + \sum_i c_{d=5}^i \mathcal{O}_{d=5}^i + c_{d=6}^i \mathcal{O}_{d=6}^i \dots$$

The diagram shows the decomposition of the lepton sector Lagrangian. The Standard Model part is  $\mathcal{L}_{SM}$ . The new physics part consists of dimension-5 operators  $\mathcal{O}_{d=5}^i$  and dimension-6 operators  $\mathcal{O}_{d=6}^i$ . The coefficients  $c_{d=5}^i$  are associated with the lepton number violation parameter  $\Lambda_{LN}$ , and the coefficients  $c_{d=6}^i$  are associated with the flavour violation parameter  $\Lambda_{flavour}$ .

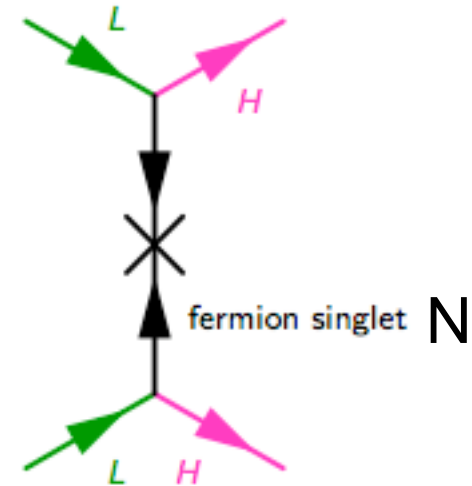
Delicate:

- \* Majorana masses are model dependent :  $c^{d=5}(Y_e, ?)$ ,  $c^{d=6}(Y_e, ?)$
- \* Requires to separate lepton number from flavour origin

# An unsuccessful model: simplest type I

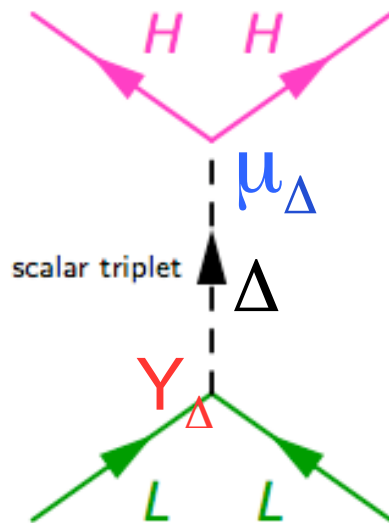
Standard Seesaw (Type I) doesn't work

$$\mathcal{L} = \dots - Y_N \bar{N} \phi^\dagger L_L - \Lambda_{LN} \bar{N}^c N \dots$$



- **Neutrino masses:** Ok.  $m_\nu \propto Y_N^T \frac{1}{\Lambda_{LN}} Y_N$
- **Measurable flavour:** NOT OK!.  $\Lambda_{fl} \equiv \Lambda_{LN}$
- **Predictivity:** More or less Ok.  $c_{d=5} \propto c_{d=6}$  if no CP

# A successful model: Scalar-triplet Seesaw (type II)

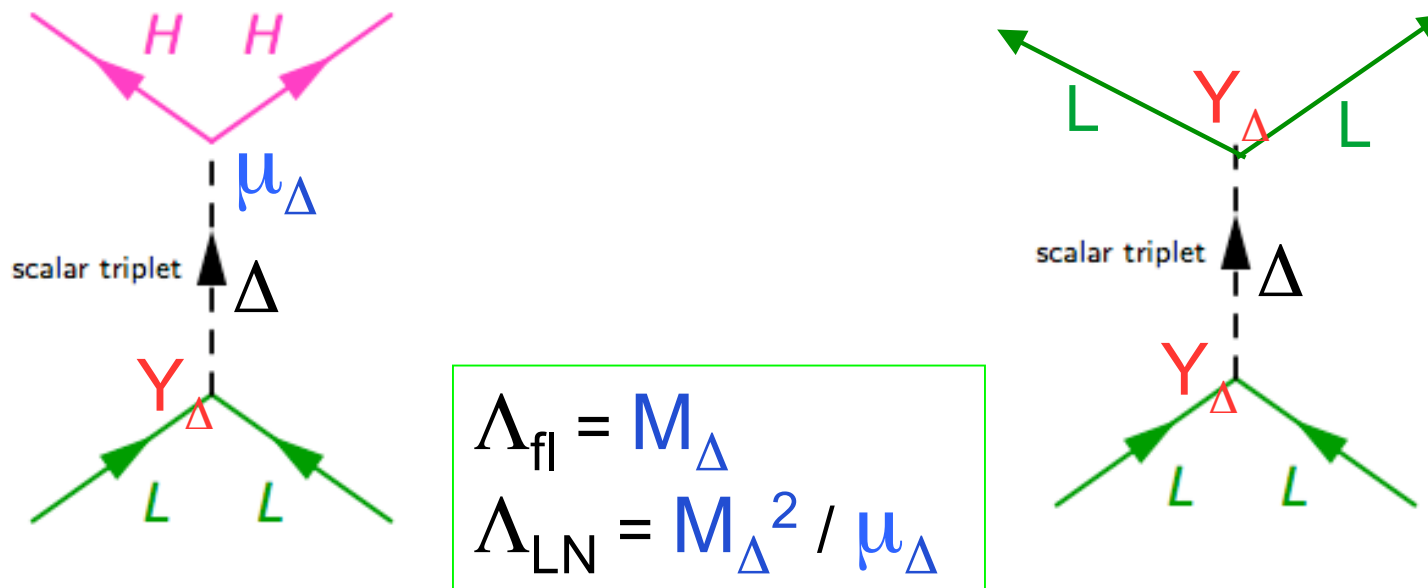


$$\mathcal{L}_\Delta = \dots + (D_\mu \Delta)^\dagger (D^\mu \Delta) - M_\Delta^2 \Delta^\dagger \Delta + +$$

$$+ Y_\Delta^{\alpha\beta} \widetilde{L} (\tau \cdot \Delta) L + \mu_\Delta \widetilde{\phi}^\dagger (\tau \cdot \Delta)^\dagger \phi + \dots$$



# A successful model: Scalar-triplet Seesaw (type II)



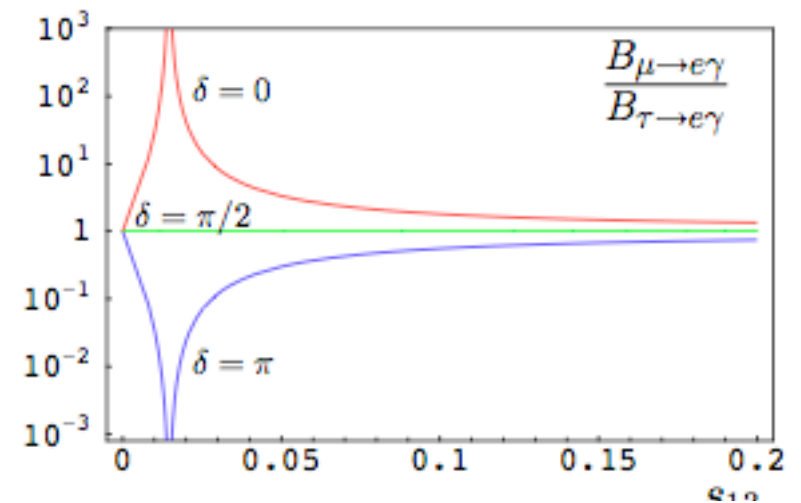
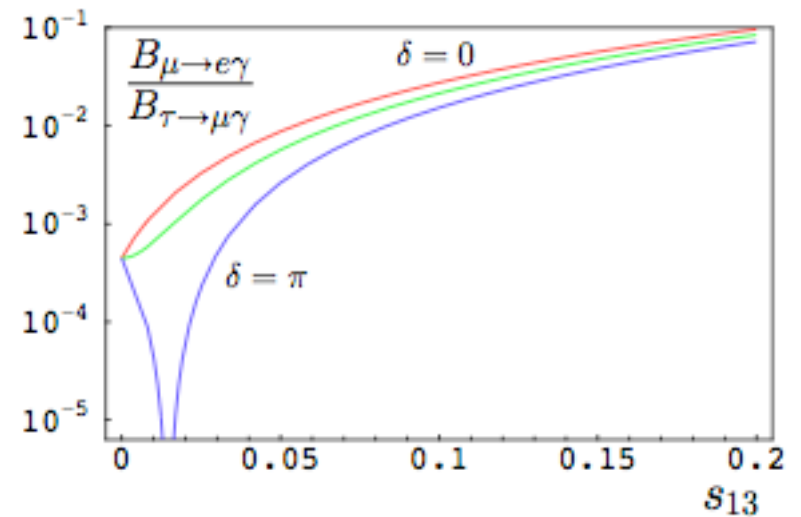
$$\mathcal{L}_\Delta = \dots + (D_\mu \Delta)^\dagger (D^\mu \Delta) - M_\Delta^2 \Delta^\dagger \Delta + +$$

$$+ Y_\Delta^{\alpha\beta} \widetilde{L} (\tau \cdot \Delta) L + \mu_\Delta \widetilde{\phi}^\dagger (\tau \cdot \Delta)^\dagger \phi + \dots$$

# Correlations among weak processes, i.e.



- \* Neutrino masses OK
- \* Measurable flavour OK
- \* Predictivity OK



# Successful fermionic-mediated Seesaws:

One more mediator, one more scale.... i.e. Inverse seesaws

Instead of  $\mathcal{L}_m = \begin{pmatrix} 0 & Y_N^T v \\ Y_N v & M_N \end{pmatrix}$

# Successful fermionic-mediated Seesaws:

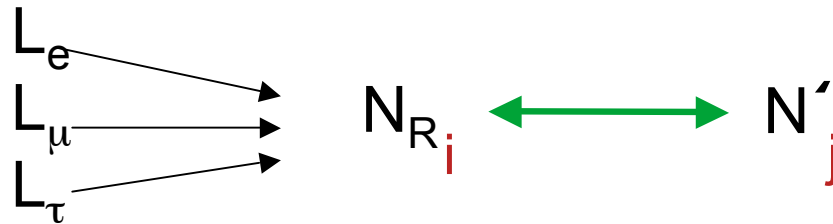
One more mediator, one more scale.... i.e. Inverse seesaws

$$\mathcal{L}_{M\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & 0 \\ Y_N \nu & 0 & \bar{\Lambda}^T \\ 0 & \Lambda & 0 \end{pmatrix}$$

# Successful fermionic-mediated Seesaws:

One more mediator, one more scale.... i.e. Inverse seesaws

$$\mathcal{L}_{M_\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & 0 \\ Y_N \nu & 0 & \bar{\Lambda}^T \\ 0 & \Lambda & 0 \end{pmatrix}$$



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*Lepton number conserved*

U(1)

$$\begin{array}{l} \Lambda_{fl} = \Lambda \\ \Lambda_{LN} = \infty \end{array}$$

$$C^{d=6} \sim \frac{Y^+ Y}{\Lambda^2}$$

# Successful fermionic-mediated Seesaw:

One more mediator, one more scale.... i.e. Inverse seesaws

$$\mathcal{L}_{M_\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & -Y_N'^T \nu \\ Y_N \nu & \mu' & \Lambda^T \\ -Y_N' \nu & \Lambda & \mu \end{pmatrix}$$

*Lepton number violated  
by any of those 3 entries*

# Successful fermionic-mediated Seesaw:

One more mediator, one more scale.... i.e. Inverse seesaws

$$\mathcal{L}_{M\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & Y_N'^T \nu \\ Y_N \nu & \mu' & \Lambda^T \\ -Y_N' \nu & \Lambda & \mu \end{pmatrix}$$

*Lepton number violated  
by any of those 3 entries*

$\Lambda$  may be  $\sim$  TeV and  $Y$ s  $\sim 1$ , and be ok with  $m_\nu$



Case: Three light active families + one  $N_R$  + one  $N_R'$

$$\mathcal{L}_{M_\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & \epsilon Y_N'^T \nu \\ Y_N \nu & \mu' & \Lambda^T \\ \epsilon Y_N' \nu & \Lambda & \mu \end{pmatrix}$$

$\mu'$  is irrelevant (at tree-level)

- one massless neutrino
- just one low-energy Majorana phase

*arguably the simplest model of neutrino mass*

Case: Three light active families + one  $N_R$  + one  $N_R'$

$$\mathcal{L}_{M_\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & \epsilon Y_N'^T \nu \\ Y_N \nu & \mu' & \Lambda^T \\ \epsilon Y_N' \nu & \Lambda & \mu \end{pmatrix}$$

$\mu'$  is irrelevant (at tree-level)

### FUNDAMENTAL

	moduli	phases
$Y_N$	3	3
$Y_N'$	3	3
$\Lambda$	1	1

vs

### LOW ENERGY

- 3 angles and 2 phases in the  $U_{PMNS}$
- 2 masses and 0 phases in  $M_\nu$
- 2 overall factors and 5 phases absorbed.

**\*Yukawas are completely determined from  $U_{PMNS} + m_\nu$ , except for a normalization + a degeneracy in the Majorana phase**

Case: Three light active families + one  $N_R$  + one  $N_R'$

$$\mathcal{L}_{M_\nu} = \begin{pmatrix} \bar{L}_i & \bar{N}^c & \bar{N}'^c \\ 0 & Y_N^T \nu & \epsilon Y_N'^T \nu \\ Y_N \nu & \mu' & \Lambda^T \\ \epsilon Y_N' \nu & \Lambda & \mu \end{pmatrix}$$

$\mu'$  is irrelevant (at tree-level)

i.e.

$$Y_N^T \simeq y \begin{pmatrix} e^{i\delta} s_{13} + e^{-i\alpha} s_{12} r^{1/4} \\ s_{23} \left( 1 - \frac{\sqrt{r}}{2} \right) + e^{-i\alpha} r^{1/4} c_{12} c_{23} \\ c_{23} \left( 1 - \frac{\sqrt{r}}{2} \right) - e^{-i\alpha} r^{1/4} c_{12} s_{23} \end{pmatrix} \quad r = \frac{|\Delta m_{12}^2|}{|\Delta m_{13}^2|}$$

Normal hierarchy

**\*Yukawas are completely determined from  $U_{PMNS} + m_\nu$ , except for a normalization + a degeneracy in the Majorana phase**

## Normal hierarchy:

Up to terms of  $\mathcal{O}(\sqrt{r}, s_{13})$ , we find

$$r = \frac{|\Delta m_{12}^2|}{|\Delta m_{13}^2|}$$

$$Y_N^T \simeq y \begin{pmatrix} e^{i\delta} s_{13} + e^{-i\alpha} s_{12} r^{1/4} \\ s_{23} \left(1 - \frac{\sqrt{r}}{2}\right) + e^{-i\alpha} r^{1/4} c_{12} c_{23} \\ c_{23} \left(1 - \frac{\sqrt{r}}{2}\right) - e^{-i\alpha} r^{1/4} c_{12} s_{23} \end{pmatrix}.$$

## Inverted hierarchy:

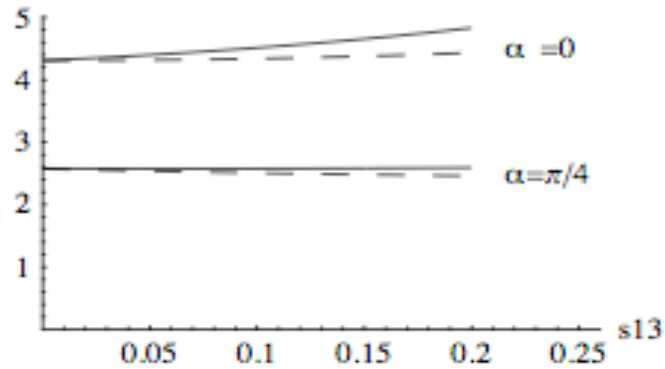
$$Y_N^T \simeq \frac{y}{\sqrt{2}} \begin{pmatrix} c_{12} e^{i\alpha} + s_{12} e^{-i\alpha} \\ c_{12} (c_{23} e^{-i\alpha} - s_{23} s_{13} e^{i(\alpha-\delta)}) - s_{12} (c_{23} e^{i\alpha} + s_{23} s_{13} e^{-i(\alpha+\delta)}) \\ -c_{12} (s_{23} e^{-i\alpha} + c_{23} s_{13} e^{i(\alpha-\delta)}) + s_{12} (s_{23} e^{i\alpha} - c_{23} s_{13} e^{-i(\alpha+\delta)}) \end{pmatrix}$$

$$B_{\mu \rightarrow e\gamma} \propto |Y_{N_e} Y_{N_\mu}|^2$$

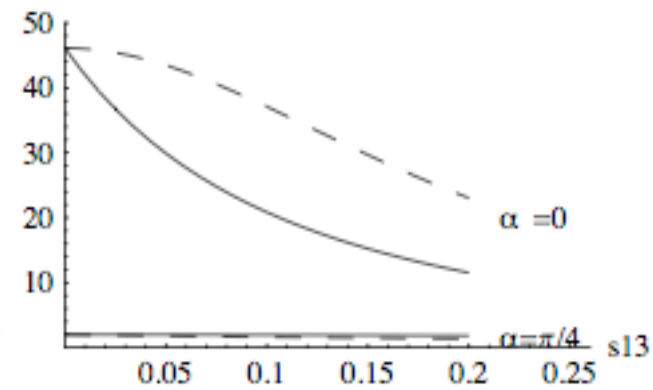
## NORMAL HIERARCHY

## INVERTED HIERARCHY

$$\frac{B_{\mu \rightarrow e\gamma}}{B_{\tau \rightarrow e\gamma}}$$

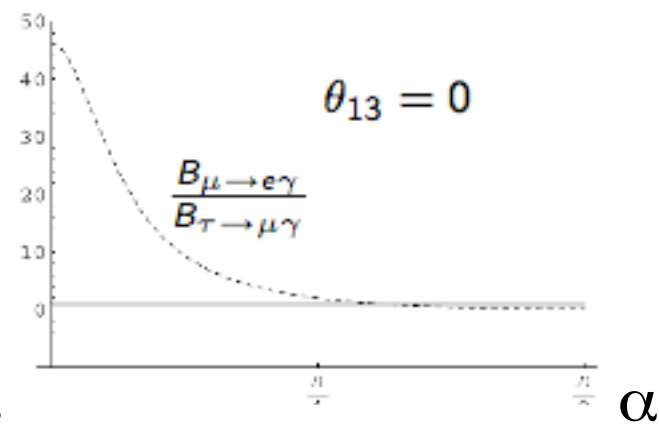
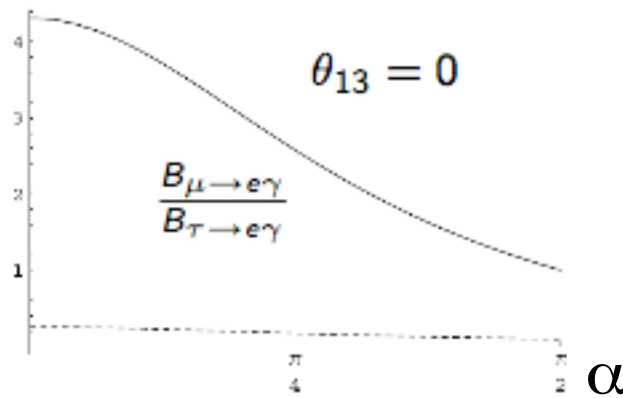


$$\frac{B_{\mu \rightarrow e\gamma}}{B_{\tau \rightarrow \mu\gamma}}$$



$\theta_{13}$

Strong dependence on the Majorana phase!



## Degeneracy in the Majorana phase $\alpha$

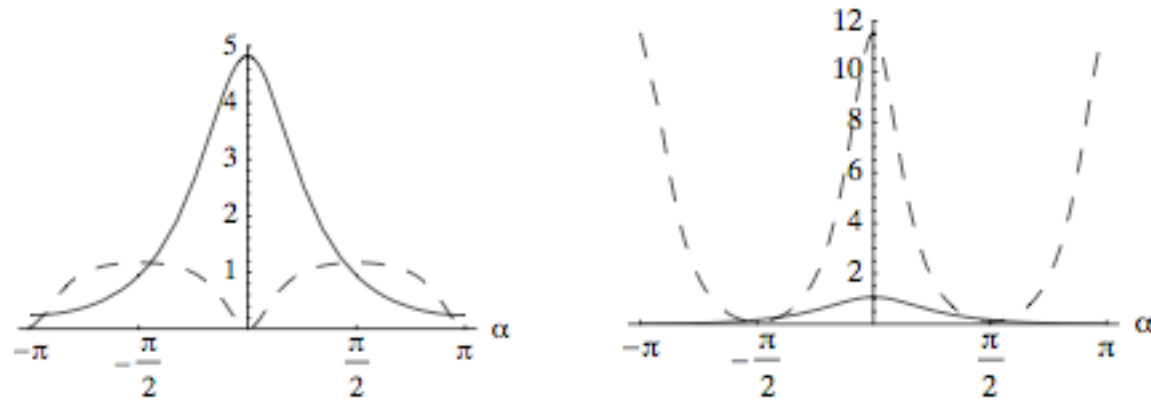
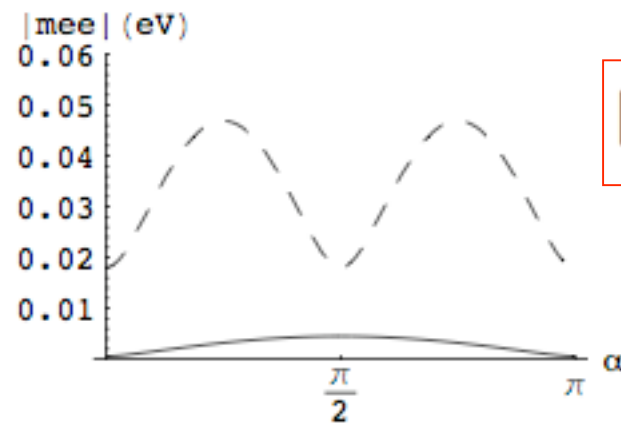


Figure 3: Left: Ratio  $B_{e\mu}/B_{e\tau}$  for the normal hierarchy (solid) and the inverse hierarchy (dashed) as a function of  $\alpha$  for  $(\delta, s_{13}) = (0, 0.2)$ . Right: the same for the ratio  $B_{e\mu}/B_{\mu\tau}$ .



$$|m_{ee}|_{IH} \simeq |s_{12}^2 e^{-2i\alpha} - c_{12}^2 e^{2i\alpha}|$$

Figure 5:  $m_{ee}$  as a function of  $\alpha$  for the normal (solid) and inverted (dashed) hierarchies, for  $(\delta, s_{13}) = (0, 0.2)$ .

This model with just 2 heavy neutrinos added to SM:

\*Leptogenesis OK for small mass splittings between the right handed (heavy) neutrinos

(Blanchet, Hambye, Josse-Michaux 09)

## NON UNITARITY

\*

There are bounds on non-unitarity coming from:

Rare decays

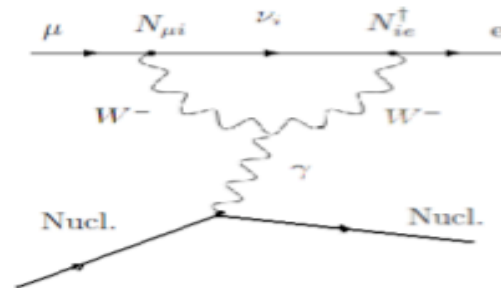
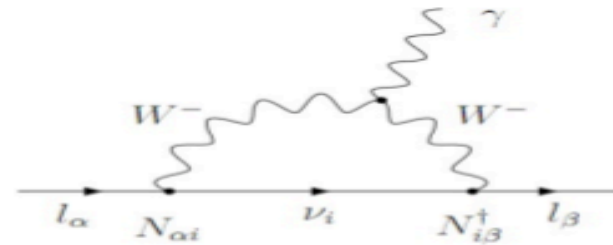
Weak decays

Invisible Z width

Neutrino Oscillations

(and future experiments that will test it further)

mu to e conversion



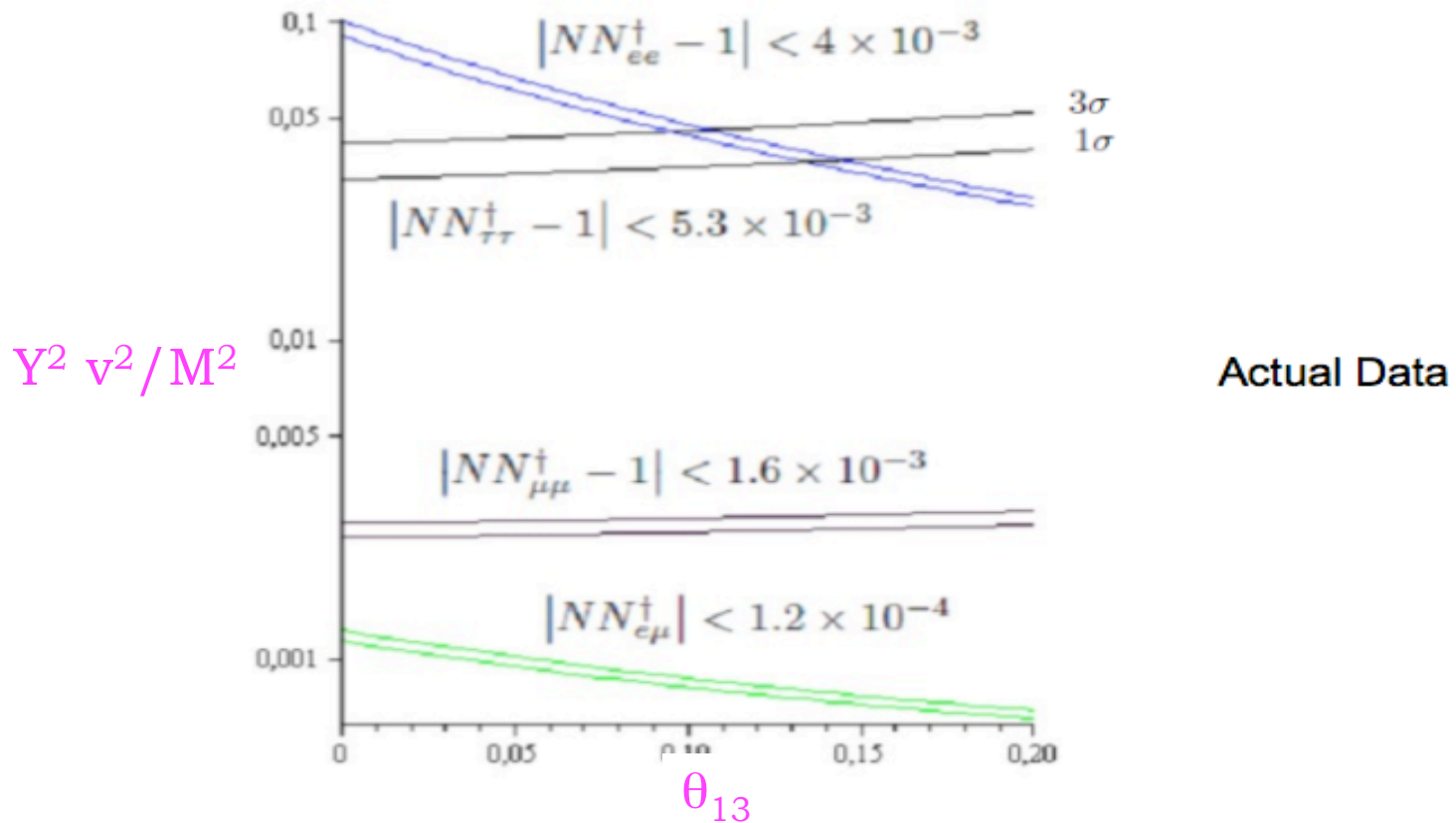
that we can use to restrict the parameters in our model:

(Alonso, Gavela, Hernandez, Li ongoing)

# Normal hierarchy:

$Y^2 v^2 / M^2$  vs  $\theta_{13}$

$$N \sim U_{\text{PMNS}} + Y^+ Y v^2 / M^2$$



To date, the best Bound comes from the rare decay  $\mu \rightarrow e\gamma$

$$\sim < 10^{-4}$$

(Alonso, Gavela, Hernandez, Li ...ongoing)

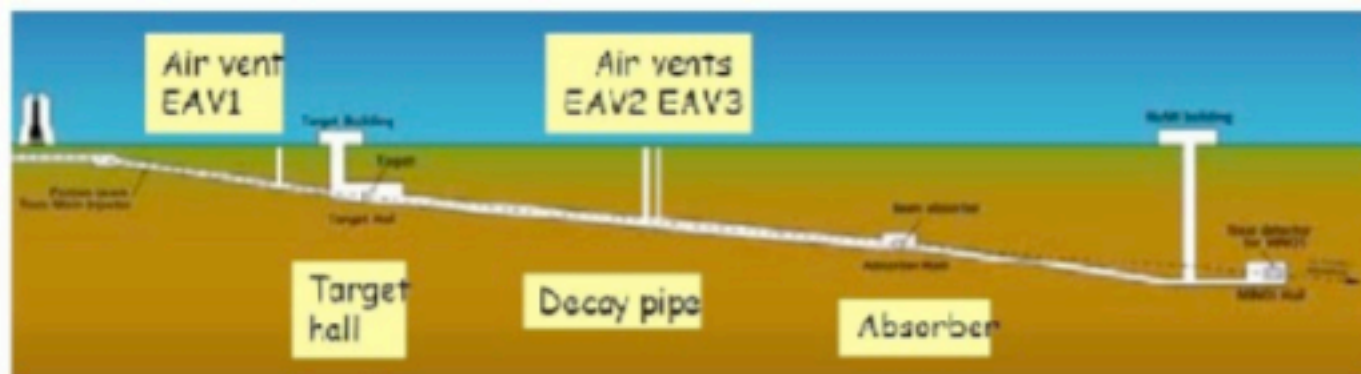




# MINISIS

Main  
Injector  
Non Standard  
Interactions

Minsis is a project for a **short baseline** experiment in Fermilab



That would look for  $\nu_{\mu}$  disappearance

$$\nu_{\mu} \dashrightarrow \nu_{\tau}$$

$$B_{\mu \rightarrow e\gamma} \propto |Y_{N_e} Y_{N_\mu}|^2$$

i.e.

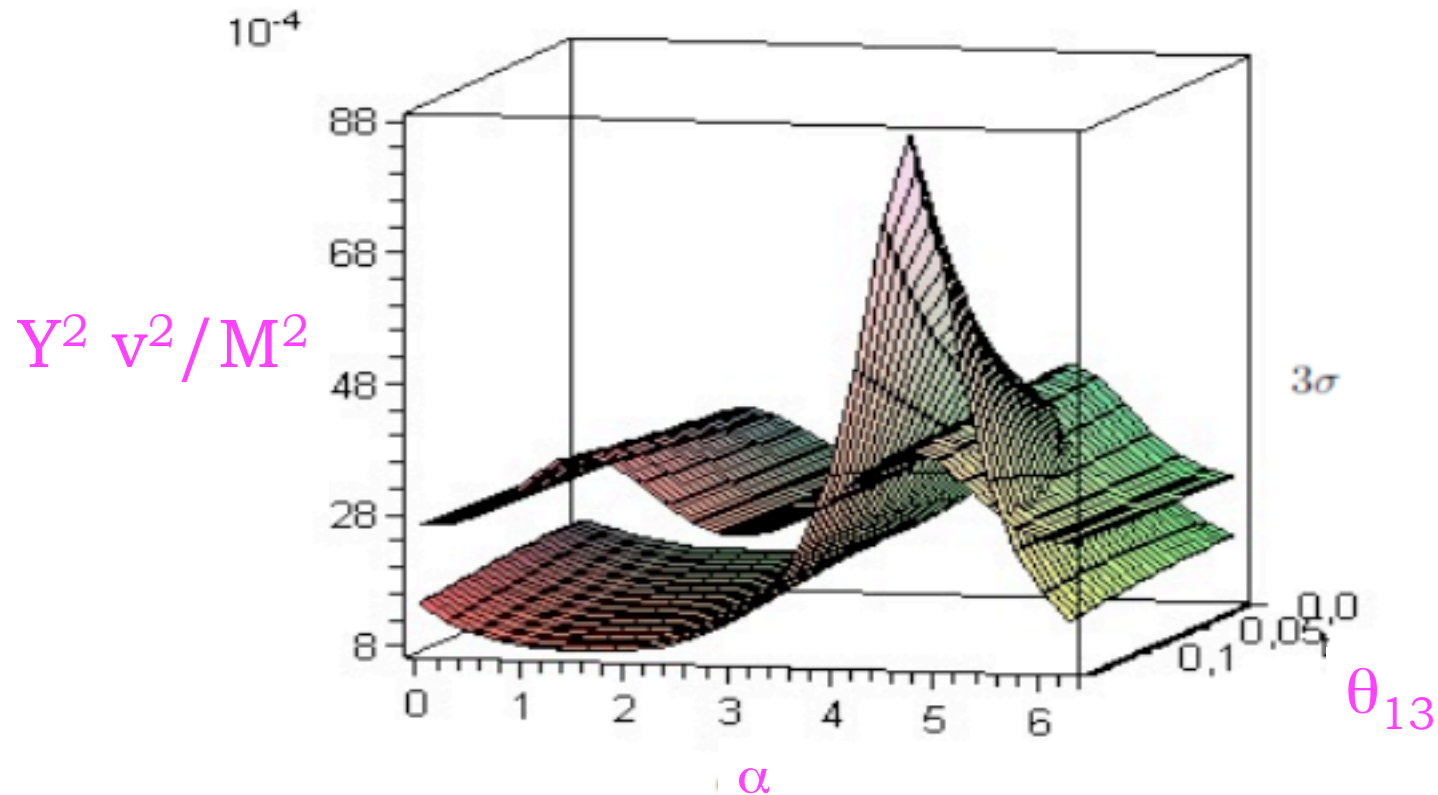
$$Y_N^T \simeq y \begin{pmatrix} e^{i\delta} s_{13} + e^{-i\alpha} s_{12} r^{1/4} \\ s_{23} \left(1 - \frac{\sqrt{r}}{2}\right) + e^{-i\alpha} r^{1/4} c_{12} c_{23} \\ c_{23} \left(1 - \frac{\sqrt{r}}{2}\right) - e^{-i\alpha} r^{1/4} c_{12} s_{23} \end{pmatrix}$$

Normal hierarchy

$$r = \frac{|\Delta m_{12}^2|}{|\Delta m_{13}^2|}$$

# Normal hierarchy: MINSIS and MFV

If we explore a wider range of parameters



We find that there are regions where an experiment as MINSIS would improve the present bounds on our Model

**MINSIS could also improve by two orders  
of magnitude the search for light steriles  
coupled to the heavier families**

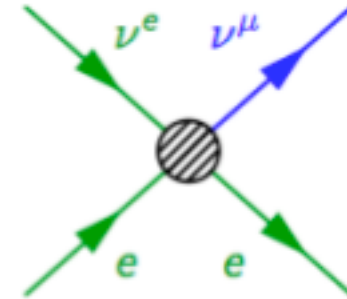
**... but this is another story**

“Why not” NSIs

(Non-Seesaw NSIs)

i.e., purely matter NSI?

Extra effects in **matter propagation**



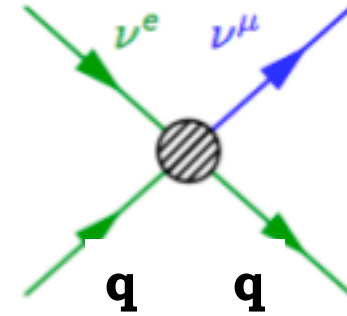
$$\mathcal{L}_{\text{NSI}} \propto -\epsilon_{\alpha\beta}^l (\bar{\nu}^\alpha \gamma^\rho P_L \nu_\beta) (\bar{l} \gamma_\rho l)$$

$$\mathcal{H}_F = U \begin{pmatrix} 0 & & \\ & \frac{\Delta m_{21}^2}{2E} & \\ & & \frac{\Delta m_{31}^2}{2E} \end{pmatrix} U^\dagger + V \begin{pmatrix} 1 + \epsilon_{ee}^m & \epsilon_{e\mu}^m & \epsilon_{e\tau}^m \\ \epsilon_{\mu e}^m & \epsilon_{\mu\mu}^m & \epsilon_{\mu\tau}^m \\ \epsilon_{\tau e}^m & \epsilon_{\tau\mu}^m & \epsilon_{\tau\tau}^m \end{pmatrix}$$

$$V \propto N_e$$

i.e., purely matter NSI?

Extra effects in matter propagation



$$\mathcal{L}_{\text{NSI}} \propto -\epsilon_{\alpha\beta}^{\ell} (\bar{\nu}^{\alpha} \gamma^{\rho} P_L \nu^{\beta}) (\bar{q} \gamma_{\mu} q)$$

$$\mathcal{H}_F = U \begin{pmatrix} 0 & & \\ & \frac{\Delta m_{21}^2}{2E} & \\ & & \frac{\Delta m_{31}^2}{2E} \end{pmatrix} U^{\dagger} + V \begin{pmatrix} 1 + \epsilon_{ee}^m & \epsilon_{e\mu}^m & \epsilon_{e\tau}^m \\ \epsilon_{\mu e}^m & \epsilon_{\mu\mu}^m & \epsilon_{\mu\tau}^m \\ \epsilon_{\tau e}^m & \epsilon_{\tau\mu}^m & \epsilon_{\tau\tau}^m \end{pmatrix}$$

$$V \propto N_e$$

# BOUNDS

\*Absolute maxima:

$$|\epsilon_{\alpha\beta}^{\oplus}| < \begin{pmatrix} 4.2 & 0.33 & 3.0 \\ 0.33 & 0.068 & 0.33 \\ 3.0 & 0.33 & 21 \end{pmatrix}$$

from  $\nu$  scattering  
in NuTeV  
and in CHARM II

C. Biggio, M. Blennow, E. Fdez-Mtnez, 0907.0097



# BOUNDS

\*Absolute maxima:

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from  $\nu$  scattering  
in NuTeV  
and in CHARM II

C. Biggio, M. Blennow, E. Fdez-Mtnez, 0907.0097

•Also from atmospheric data, unless cancellations among epsilons:

$$|\epsilon_{\mu\tau}| < 5 \cdot 10^{-2}$$

Fornengo, Maltoni, Tomás-Bayo, Valle, hep-ph 0108043

## Potential Trouble:

NSI  $\text{SU}(2) \times \text{U}(1)$  gauge invariance  $\rightarrow$  Dangerous four charged lepton couplings

## Potential Trouble:

NSI  $\text{SU}(2) \times \text{U}(1)$  gauge invariance  $\rightarrow$  Dangerous four charged lepton couplings

$$\Lambda > v$$

The new physics has to CONTAIN the SM

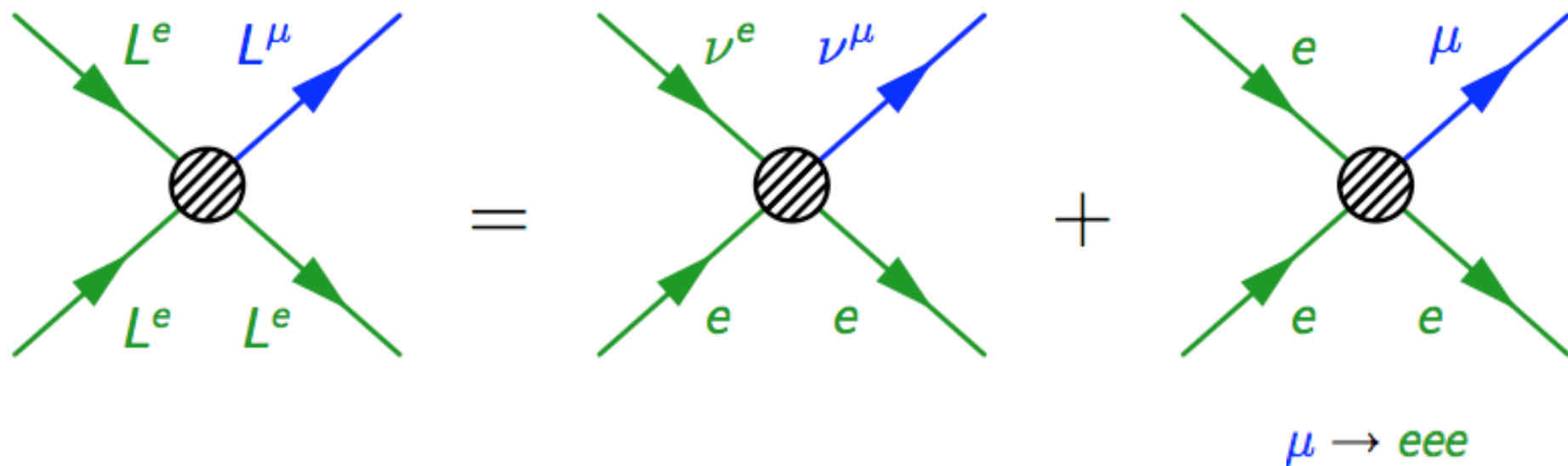


The new couplings MUST have a  
 $SU(3) \times SU(2) \times U(1)$  gauge invariant  
formulation

- **Gauge invariance** ( $SU(3) \times SU(2) \times U(1)$ )

$$\frac{1}{\Lambda^2} (\bar{\nu}^e \gamma^\rho P_L \nu^\mu) (\bar{e}_L \gamma_\rho e_L) \rightarrow \frac{1}{\Lambda^2} (\bar{L}^e \gamma^\rho L^\mu) (\bar{L}_e \gamma_\rho L_e)$$

Trouble, for instance  $\mu \rightarrow eee$



# Systematical analysis

## Two possibilities

A) There could be **NO** lepton charged processes involved

Ex: For  $d = 6$

(Davidson, Kuypers) 
$$(\bar{L}^c i\tau^2 L)(\bar{L} i\tau^2 L^c) \rightarrow (\bar{\nu}_\tau^c e_L)(\bar{\nu}_\mu e_L^c)$$

Ex: For  $d = 8$

$$O_{\text{NSI}} = (\bar{L}H)\gamma^\mu(H^\dagger L)(\bar{E}\gamma_\mu E) \rightarrow v^2(\bar{\nu}_\tau \gamma^\mu \nu^\mu)(\bar{e}_L \gamma_\mu e)$$

(Berezhiani, Rossi)

# Systematical analysis

## Two possibilities

A) There could be **NO** lepton charged processes involved

Ex: For  $d = 6$

(Davidson, Kuypers)  $(\bar{L}^c i\tau^2 L)(\bar{L} i\tau^2 L^c) \rightarrow (\bar{\nu}_\tau^c e_L)(\bar{\nu}_\mu e_L^c)$

But it also produces  $\tau \rightarrow \mu \nu_e \bar{\nu}_e$  !

Ex: For  $d = 8$

And  $\mu \rightarrow e \nu_\tau \bar{\nu}_e$

$$\epsilon_{\mu\tau} < 3 \cdot 10^{-2}$$

$$O_{\text{NSI}} = (\bar{L}H)\gamma^\mu(H^\dagger L)(\bar{E}\gamma_\mu E) \rightarrow v^2(\bar{\nu}_\tau \gamma^\mu \nu^\mu)(\bar{e}_L \gamma_\mu e)$$

Fdez-Martinez

(Berezhiani, Rossi)

## Systematical analysis

### Two possibilities

- B) In general, "fine tune" some of them to obtain desired suppression

Ex:

$$\mathcal{L}_{\text{eff}} = \frac{C^1}{\Lambda^2} (\bar{L}^e \gamma^\rho L^\mu) (\bar{L}^e \gamma_\rho L^\mu) + \frac{C^3}{\Lambda^2} (\bar{L}^e \gamma^\rho \vec{\tau} L^\mu) (\bar{L}^e \gamma_\rho \vec{\tau} L^\mu)$$

We can avoid charged lepton interactions  $(\bar{e}_L \gamma^\mu P_L \mu) (\bar{e} \gamma_\mu P_L e)$  if

$$C^1 + C^3 \simeq 0$$

**ALL cancellation conditions examined**



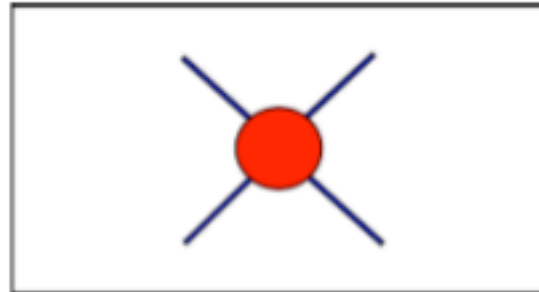
## Finally, gauge invariance implies:

- From d=6 ops.:  $\varepsilon_{\mu\tau} < 3 \cdot 10^{-2}$
- Or you avoid altogether d=6 ops. combining d=8 ones with a very strong **-unbelievable- fine-tuning !** (check cancellations in our table if you have the stomach for it)

# TREE-LEVEL MEDIATOR DECOMPOSITION

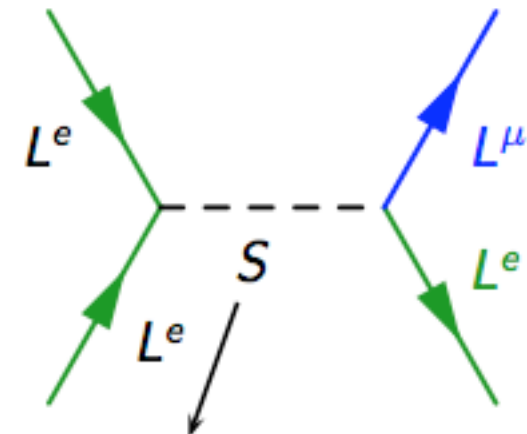
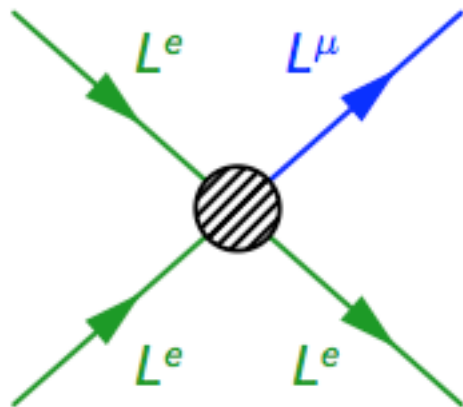
Would give even stronger bounds...

Constraints are then stronger and odds even worse:



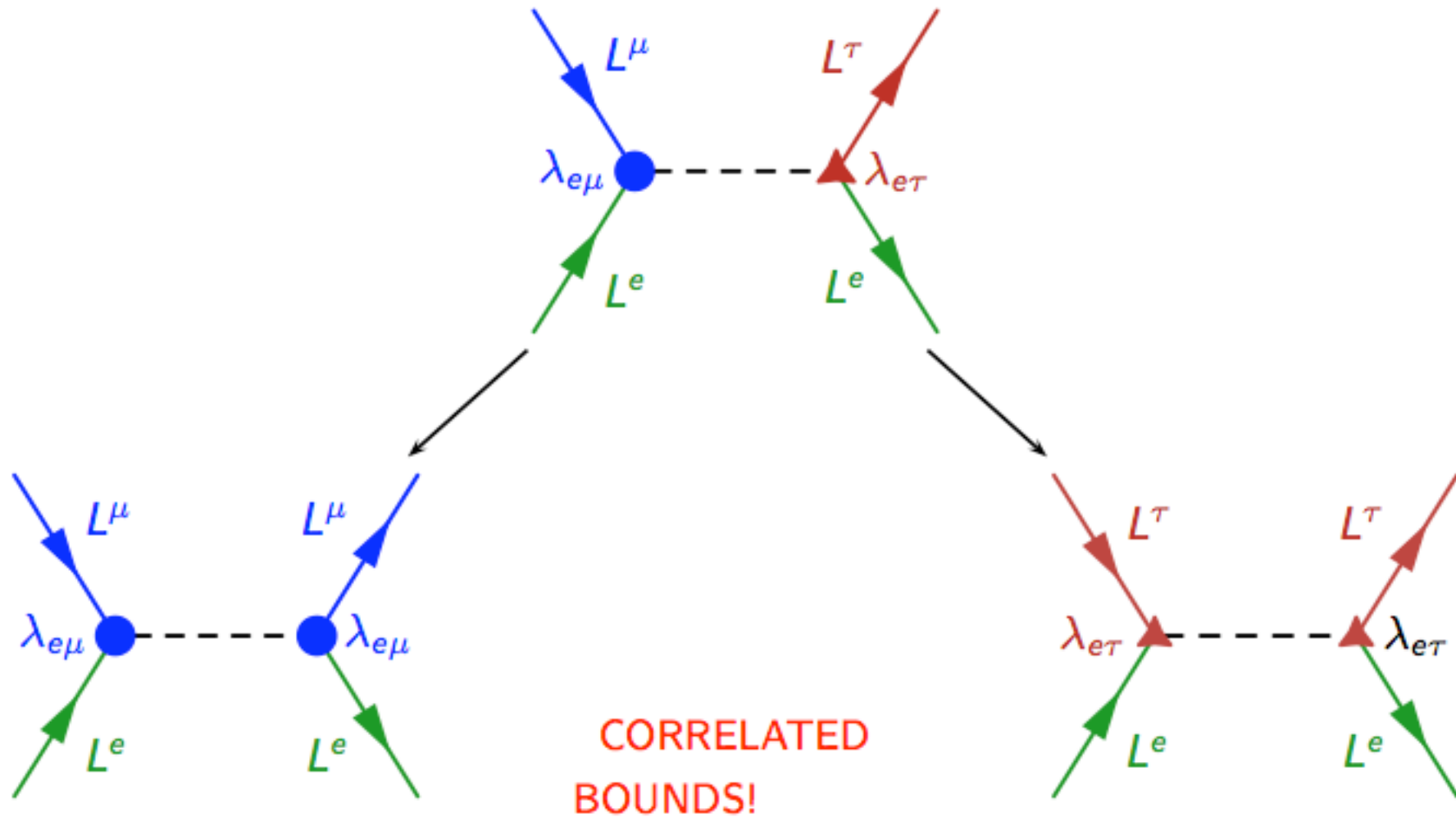
We can open the  $d = 6$  vertex (remember Fermi, Weinberg?)

Ex: For instance, take the  $(\bar{L}^c i\tau^2 L)(\bar{L} i\tau^2 L^c)$  Davidson+Kuypers



singlet scalar,  $Y = -1$

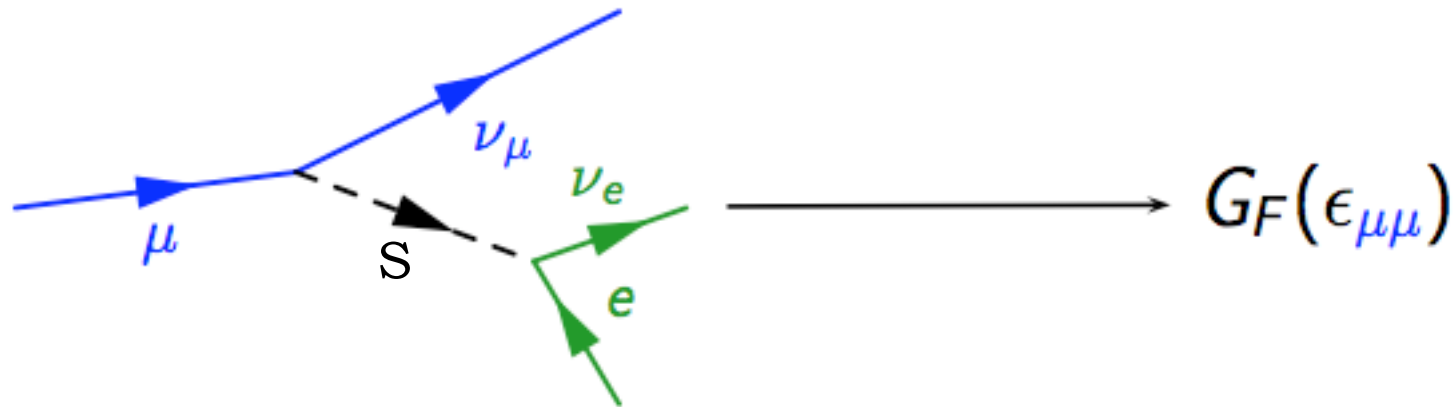
**BUT...** you might run into troubles



**SEVERELY CONSTRAINED:**

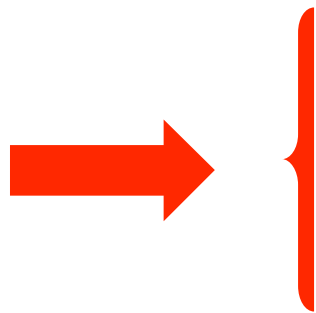
S. Antusch, J. P. Baumann, E. Fdez-Mtnez; 0807.1003  
F. Cuypers, S. Davidson; hep-ph/ 9609487

Moreover...



Davidson+Kuypers..... Antusch,Baumann, Fdez.-Martinez

$$\epsilon_{\mu\tau} < 2 \cdot 10^{-3}$$



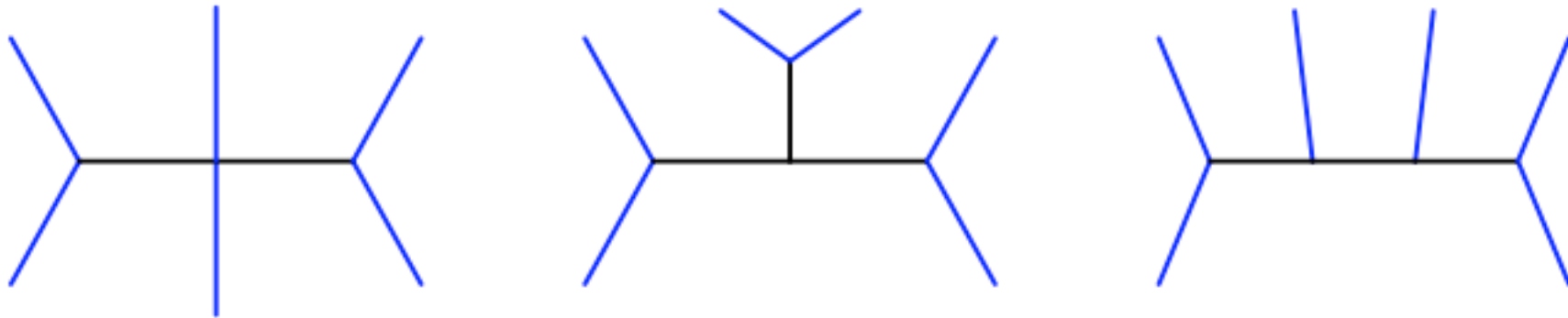
- This  $S$  is disconnected from the seesaw mechanism... although connected to radiatively generated masses -Zee model-
- d=6 NSI are very very constrained.

Bottom line:  $d = 6$  doesn't look promising

Maybe things get better at  $d = 8$

Is it possible to generate  $d = 8$  and NO  $d = 6$  operators??

Several possibilities



(Antusch, Baunman, Fdez-Martinez;

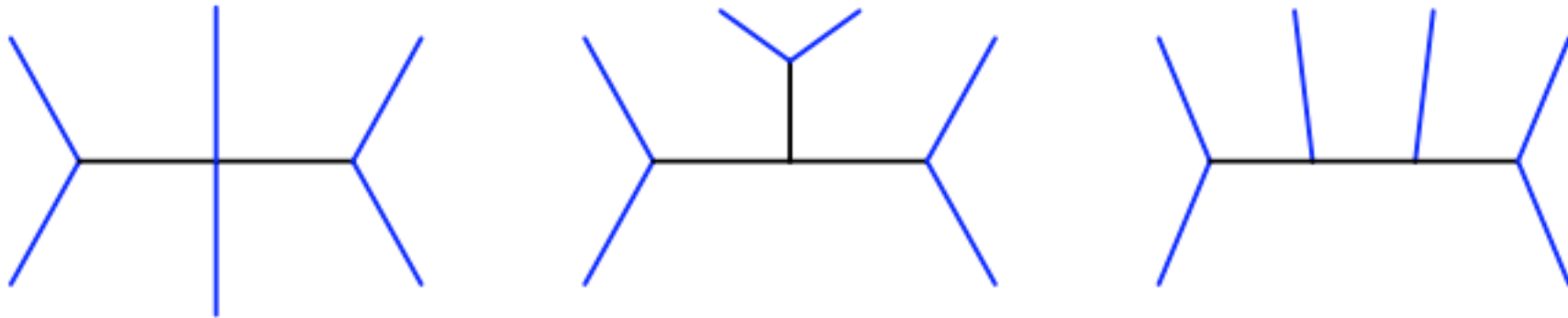
D. Hernandez, Ota, Winter + MBG )

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**Require at least 2 new fields ( and unrelated to seesaw)**

(Antusch, Baunman, Fdez-Martinez;

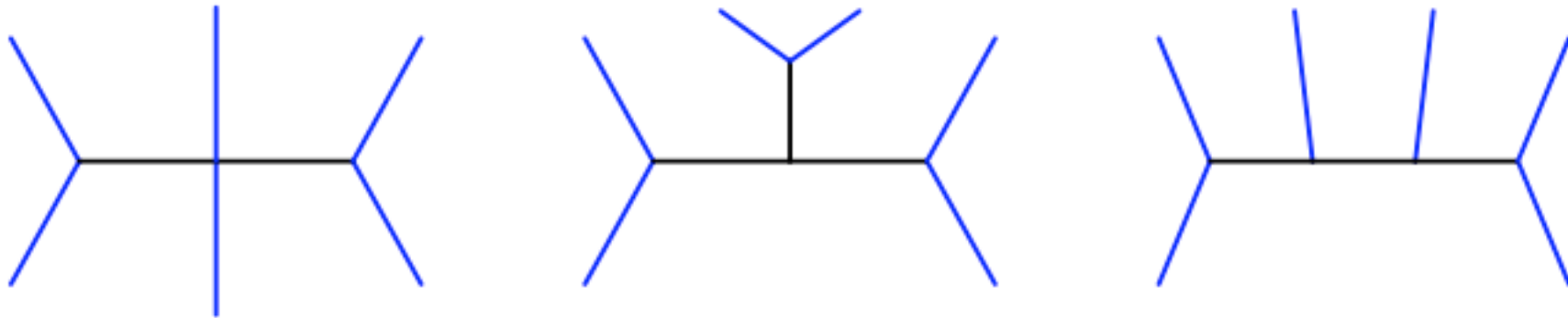
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**TERRIBLY COMPLICATED**

(Antusch, Baunman, Fdez-Martinez;

D. Hernandez, Ota, Winter + MBG )



# Complete list of d=8 operators and their mediators

#	Dim. eight operator	$\mathcal{C}_{LEH}^1$	$\mathcal{C}_{LEH}^2$	$\mathcal{O}_{NSI}^2$	Mediators
<b>Combination <math>LL</math></b>					
1	$(\bar{L}\gamma^\mu L)(\bar{E}\gamma_\mu E)(H^\dagger H)$	1			$1_0^5$
2	$(\bar{L}\gamma^\mu L)(\bar{E}H^\dagger)(\gamma_\mu)(HE)$	1			$1_0^5 + 2_{-3/2}^{L/R}$
3	$(\bar{L}\gamma^\mu L)(\bar{E}H^\dagger)(\gamma_\mu)(H^*E)$	1			$1_0^5 + 2_{-1/2}^{L/R}$
4	$(\bar{L}\gamma^\mu \not{r} L)(\bar{E}\gamma_\mu E)(H^\dagger \not{r} H)$		1		$3_0^5 + 1_0^5$
5	$(\bar{L}\gamma^\mu \not{r} L)(\bar{E}H^\dagger)(\gamma_\mu \not{r})(HE)$		1		$3_0^5 + 2_{-3/2}^{L/R}$
6	$(\bar{L}\gamma^\mu \not{r} L)(\bar{E}H^\dagger)(\gamma_\mu \not{r})(H^*E)$		1		$3_0^5 + 2_{-1/2}^{L/R}$
<b>Combination <math>\bar{E}L</math></b>					
7	$(\bar{L}E)(\bar{E}L)(H^\dagger H)$	-1/2			$2_{+1/2}^*$
8	$(\bar{L}E)(\not{r})(\bar{E}L)(H^\dagger \not{r} H)$		1/2		$2_{+1/2}^*$
9	$(\bar{L}H)(H^\dagger E)(\bar{E}L)$	-1/4	-1/4	✓	$2_{+1/2}^* + 1_0^5 + 2_{-1/2}^{L/R}$
10	$(\bar{L}\not{r}H)(H^\dagger E)(\not{r})(\bar{E}L)$	-3/4	1/4		$2_{-1/2}^* + 3_0^{L/R} + 2_{-1/2}^{L/R}$
11	$(\bar{L}i\tau^2 H^*)(H^\dagger E)(i\tau^2)(\bar{E}L)$	1/4	-1/4		$2_{-1/2}^* + 1_{-1}^{L/R} + 2_{-3/2}^{L/R}$
12	$(\bar{L}\bar{i}\tau^2 H^*)(H^\dagger E)(i\tau^2 \bar{r})(\bar{E}L)$	3/4	1/4		$2_{-1/2}^* + 3_{-1}^{L/R} + 2_{-3/2}^{L/R}$
<b>Combination <math>E^c L</math></b>					
13	$(\bar{L}\gamma^\mu E^c)(\bar{E}^c\gamma_\mu L)(H^\dagger H)$	-1			$2_{-3/2}^*$
14	$(\bar{L}\gamma^\mu E^c)(\not{r})(\bar{E}^c\gamma_\mu L)(H^\dagger \not{r} H)$		-1		$2_{-3/2}^*$
15	$(\bar{L}H)(\gamma^\mu)(H^\dagger E^c)(\bar{E}^c\gamma_\mu L)$	-1/2	-1/2	✓	$2_{-3/2}^* + 1_0^5 + 2_{-3/2}^{L/R}$
16	$(\bar{L}\not{r}H)(\gamma^\mu)(H^\dagger E^c)(\not{r})(\bar{E}^c\gamma_\mu L)$	-3/2	1/2		$2_{-3/2}^* + 3_0^{L/R} + 2_{+3/2}^{L/R}$
17	$(\bar{L}i\tau^2 H^*)(\gamma^\mu)(H^\dagger E^c)(i\tau^2)(\bar{E}^c\gamma_\mu L)$	-1/2	1/2		$2_{-3/2}^* + 1_{-1}^{L/R} + 2_{+1/2}^{L/R}$
18	$(\bar{L}\bar{i}\tau^2 H^*)(\gamma^\mu)(H^\dagger E^c)(i\tau^2 \bar{r})(\bar{E}^c\gamma_\mu L)$	-3/2	-1/2		$2_{-3/2}^* + 3_{-1}^{L/R} + 2_{+1/2}^{L/R}$
<b>Combination <math>H^c L</math></b>					
19	$(\bar{L}E)(\bar{E}H)(H^c L)$	-1/4	-1/4	✓	$2_{+1/2}^* + 1_0^5 + 2_{-1/2}^{L/R}$
20	$(\bar{L}E)(\not{r})(\bar{E}H)(H^c \not{r} L)$	-3/4	1/4		$2_{-1/2}^* + 3_0^{L/R} + 2_{-1/2}^{L/R}$
21	$(\bar{L}H)(\gamma^\mu)(H^c L)(\bar{E}\gamma_\mu E)$	1/2	1/2	✓	$1_0^5 + 1_0^5$
22	$(\bar{L}\not{r}H)(\gamma^\mu)(H^c \not{r} L)(\bar{E}\gamma_\mu E)$	3/2	-1/2		$1_0^5 + 3_0^{L/R}$
23	$(\bar{L}\gamma^\mu E^c)(\bar{E}^c H)(\gamma^\mu)(H^c L)$	-1/2	-1/2	✓	$2_{-3/2}^* + 1_0^5 + 2_{+3/2}^{L/R}$
24	$(\bar{L}\gamma^\mu E^c)(\bar{E}^c H)(\gamma^\mu)(H^c L)$	-3/2	1/2		$2_{-3/2}^* + 3_0^{L/R} + 2_{+3/2}^{L/R}$
<b>Combination <math>HL</math></b>					
25	$(\bar{L}E)(i\tau^2)(\bar{E}H^*)(H^c i\tau^2 L)$	1/4	-1/4		$2_{-1/2}^* + 1_{-1}^{L/R} + 2_{-3/2}^{L/R}$
26	$(\bar{L}E)(\bar{i}\tau^2)(\bar{E}H^*)(H^c \bar{i}\tau^2 L)$	3/4	1/4		$2_{-1/2}^* + 3_{-1}^{L/R} + 2_{-3/2}^{L/R}$
27	$(\bar{L}i\tau^2 H^*)(\gamma^\mu)(H^c i\tau^2 L)(\bar{E}\gamma_\mu E)$	-1/2	1/2		$1_0^5 + 1_{-1}^{L/R}$
28	$(\bar{L}\bar{i}\tau^2 H^*)(\gamma^\mu)(H^c \bar{i}\tau^2 L)(\bar{E}\gamma_\mu E)$	-3/2	-1/2		$1_0^5 + 3_{-1}^{L/R}$
29	$(\bar{L}\gamma^\mu E^c)(i\tau^2)(\bar{E}^c H^*)(\gamma_\mu)(H^c i\tau^2 L)$	1/2	-1/2		$2_{-3/2}^* + 1_{-1}^{L/R} + 2_{+1/2}^{L/R}$
30	$(\bar{L}\gamma^\mu E^c)(\bar{i}\tau^2)(\bar{E}^c H^*)(\gamma_\mu)(H^c \bar{i}\tau^2 L)$	3/2	1/2		$2_{-3/2}^* + 3_{-1}^{L/R} + 2_{+1/2}^{L/R}$

**Table 3:** Complete list of  $LL\bar{E}E$ -type  $d = 8$  interactions which involve two SM fields at any possible vertex of interaction (field bilinears within brackets). The columns show an ordinal for each operator, the  $d = 8$  interaction, the corresponding combination of interactions in the BR basis, whether  $\mathcal{O}_{NSI}$  is satisfied and the necessary mediators, respectively. Those mediators leading as well to  $d = 6$  operators in Table 2 are in boldface. The superscript  $L/R$  indicates massive vector fermions. The flavor structure is to be understood as  $\bar{L}^i L_j \bar{E}^k E_l$ .

$(\bar{L}H)(H^\dagger E)(\bar{E}L)$

$-1/4 \quad -1/4 \quad \checkmark$

$2_{+1/2}^s + 1_0^R + 2_{-1/2}^{L/R}$

MINOS: neutrino/antineutrino difference (?)  
in  $\nu_\mu$  disappearance ??

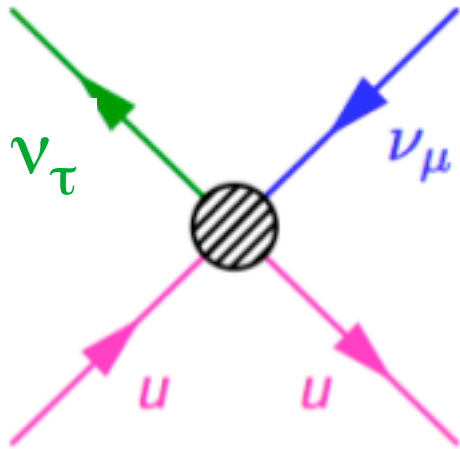
# Could MINOS effect, if ever it becomes a signal (which is NOT), be NSI?

- Certainly not NSI related to non-unitarity (ie. Seesaw related),

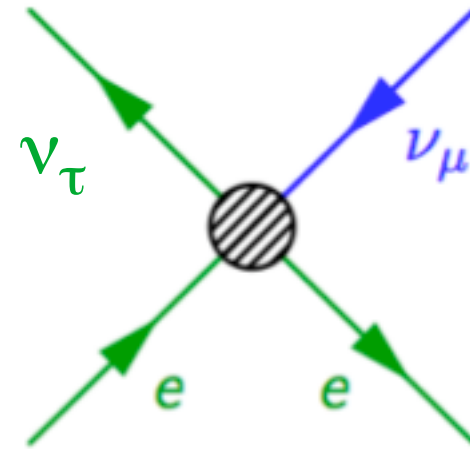
$$|\mathcal{E}| \approx \begin{pmatrix} < 2.5 \cdot 10^{-3} & < 3.6 \cdot 10^{-5} & < 8.0 \cdot 10^{-3} \\ < 3.6 \cdot 10^{-5} & < 2.5 \cdot 10^{-3} & < 5.0 \cdot 10^{-3} \\ < 8.0 \cdot 10^{-3} & < 5.0 \cdot 10^{-3} & < 2.5 \cdot 10^{-3} \end{pmatrix}$$

\*What about a “Why Not” NSI, i.e. purely matter NSI?

Could MINOS effect, if ever it becomes a signal (which is NOT), be matter NSI?



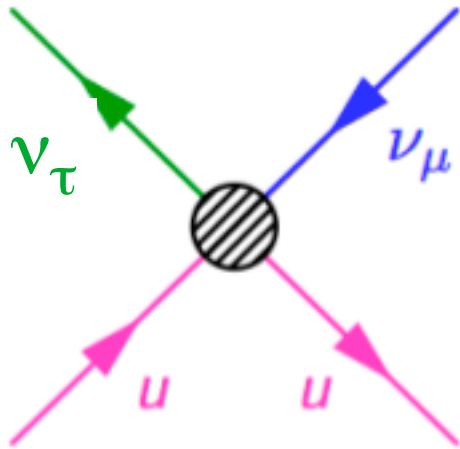
$$\frac{1}{\Lambda^2} \bar{\nu}_\tau \nu_\mu \bar{u} u$$



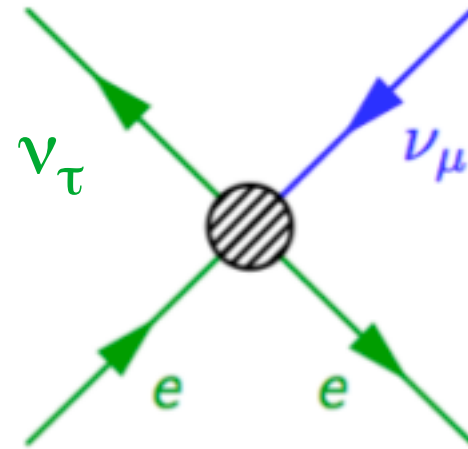
$$\frac{1}{\Lambda^2} \bar{\nu}_\tau \nu_\mu \bar{e} e$$

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Two weeks ago: Mann et al.:  $\epsilon_{\mu\tau}$   
arXiv:1006.5720



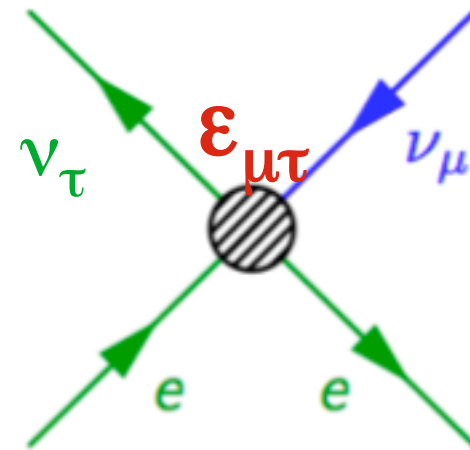
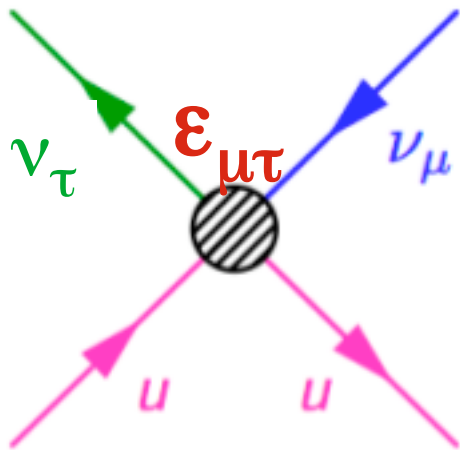
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$$\mathcal{P}\left(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu\right) \simeq 1 - \sin^2\left(\left|\frac{\Delta m_{32}^2}{4E_\nu} \mp \epsilon_{\mu\tau}|V_e|\right|L\right).$$

They  
claim

$$\varepsilon_{\mu\tau} = - (0.12 \pm 0.21), \quad \Delta m_{32}^2 = 2.56_{-0.24}^{+0.27} \times 10^{-3} \text{ eV}^2$$
$$\sin^2 2\theta_{23} = 0.90 \pm 0.05.$$

To be compared with the bounds:

$$|\varepsilon_{\alpha\beta}^{\oplus}| < \begin{pmatrix} 4.2 & 0.33 & 3.0 \\ 0.33 & 0.068 & 0.33 \\ 3.0 & 0.33 & 21 \end{pmatrix}$$

C. Biggio, M. Blennow, E. Fdez-Mtnez, 0907.0097



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Plausible? NO! : gauge invariance  $\rightarrow \varepsilon_{\mu\tau} < 3 \cdot 10^{-2}$  from d=6,  
or d=8 ops. with ad hoc cancellat.

This morning: Kopp, Machado, Parke

arXiv:0076594

“Could it be  $\epsilon_{\mu\tau}$  matter NSI?”

\* It is a similar analysis, but taking into account both  $\epsilon_{\mu\tau}$  and  $\epsilon_{\tau\tau}$  and performing a simulation of MINOS event spectrum:

They  
claim

$$\epsilon_{\mu\tau} = 0.41 e^{0.95i\pi}$$

$$\sin^2 \theta_{23} = 0.38$$

$$\epsilon_{\tau\tau} = -2.12$$

$$\Delta m_{31}^2 = +2.83 \times 10^{-3} \text{ eV}^2$$

(Signs can be changed, eightfold degeneracy)

- \* Discovery at NOVA in less than one nominal year
- \* They acknowledge that gauge invariance disfavors  $d=6$  ops., and  $d=8$  ops. unlikely:

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My conclusion:

a  $\bar{\nu}_\mu/\nu_\mu$  difference in MINOS

based on matter  $\nu_\mu \leftrightarrow \nu_\tau$  NSI ( $\Lambda > v$ )

**is terribly unlikely**

**because of gauge invariance**

Anyway, at maximum  $\varepsilon_{\mu\tau} < 0.33$

AND

Atmospheric indicate  $< 5 \cdot 10^{-2}$  unless  
brutal cancellations  
among different  $\varepsilon$

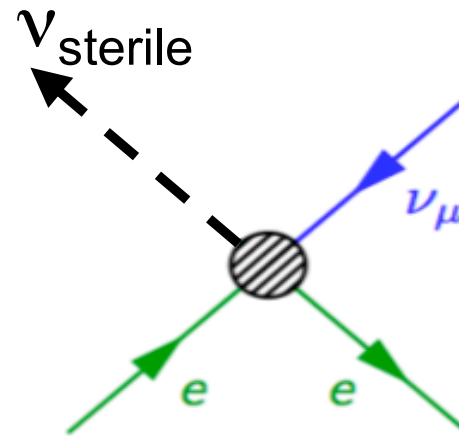
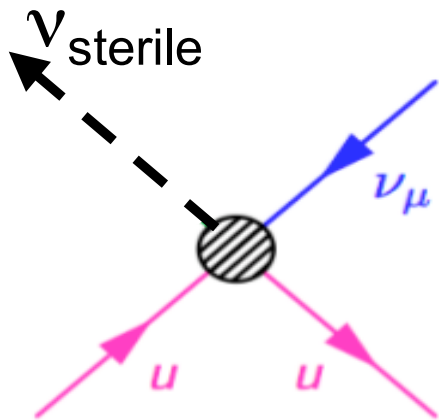
**Why everybody forgets atmospheric?**

More promising ? :

What about steriles lighter than the electroweak scale, with matter effects, for the MINOS “would-be” effect?

Steriles lighter than  $M_W$  evade non-unitarity bounds and some of the pure matter NSI bounds

Ie. Ann Nelson and collab.; light steriles, gauged B-L



All this underlies the importance  
of searching for  $\nu_{\mu} \leftrightarrow \nu_{\tau}$  transitions  
in general (i.e. at near detectors)



## And light steriles for the new MiniBoone data?

- Interesting: Same L/E than LSND, but different L and E  
--> different backgrounds

CP in vacuum?: CP does not depend on L/E if matter effects negligible, but differs for neutrinos and antineutrinos

seems difficult (arXiv:0906.1997 and arXiv:0705.0107) but.. ?

**And light s... data?**

• Interest

**Anyway,**

and E

**all those Fnal data are only  $2\sigma$  !!!**

CP in

matter effects

**only combined they are intriguing**

antineutrinos

(5.0107) but.. ?

**And light s... data?**

• Interest... and E

**Recall: Paul the octopus predictions**

**are a  $2.6 \sigma$  effect!!!**

CP in... matter effects  
antineutrinos

(5.0107) but.. ?



**2.6  $\sigma$  effect for the world cup !** (Marc Sher)



**It is an appearance experiment (Spain)**





# Conclusions

**Neutrino masses and mixings have added a precious  
piece to the flavour puzzle**

**Hopefully we will get to the physics behind it...**

**..... if new scale under # TeV**

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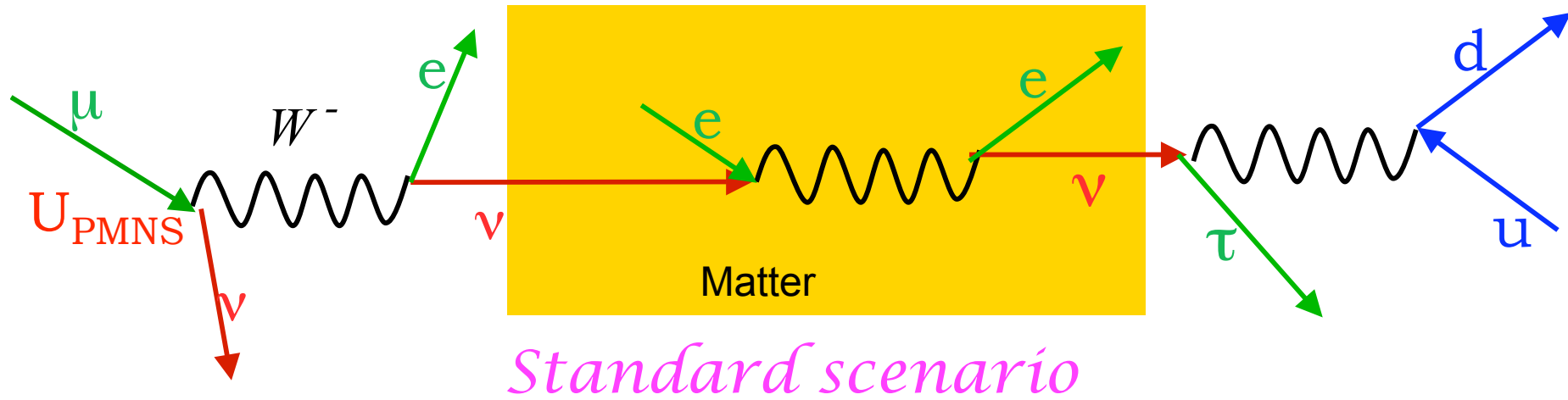
**..... if new scale under # TeV**

- Scalar seesaws and extended fermionic seesaws respect Minimal Flavour Violation
- SM + 2 heavy neutrinos, with approximate  $U(1)_{LN}$  is very successful: almost fully determined by light masses and mixings
- Non-unitary mixing is a NSI characteristic of fermionic seesaws. Keep improving bounds!
- Pure matter-NSI severely constrained by gauge invariance; unlikely explanation of the (non-existing) MINOS  $\bar{\nu}/\nu$  signal. But keep tracking  $\nu_{\mu}-\nu_{\tau}$  and  $\nu_{\mu}-\nu_{\text{sterile}}$  couplings

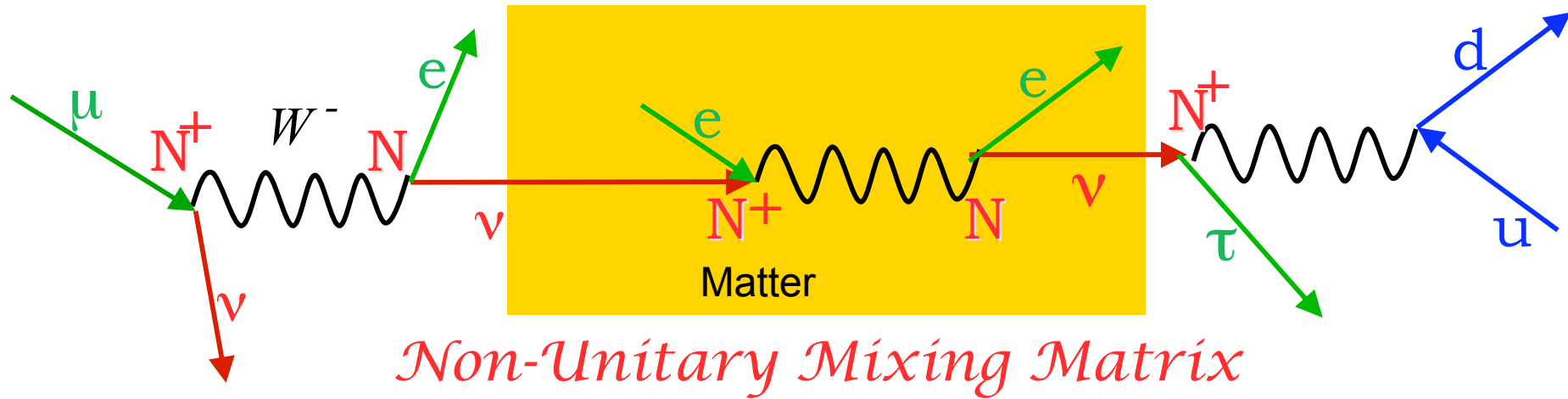


# Back-up slides

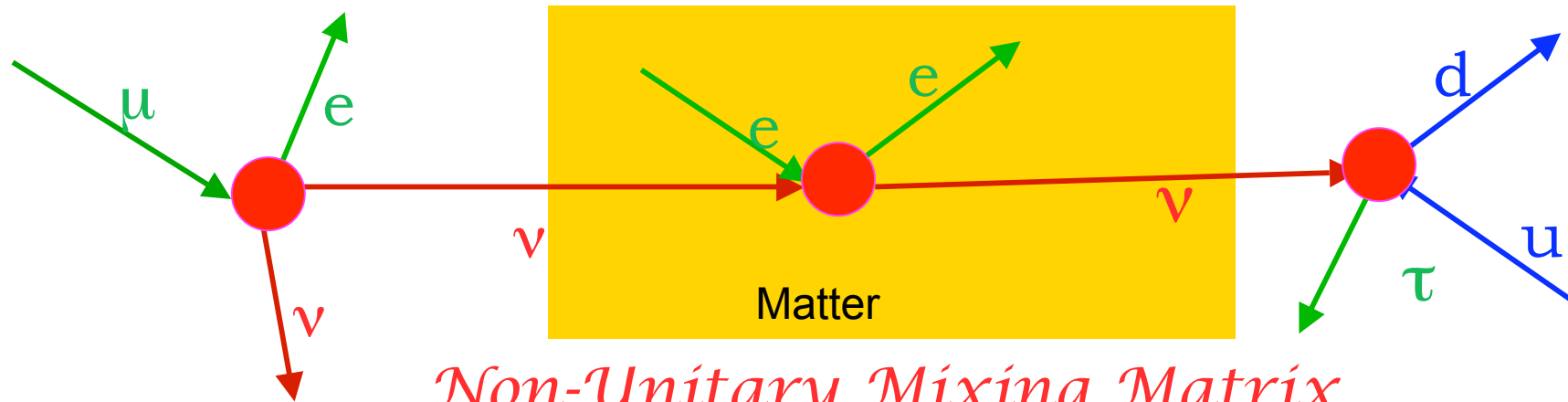
YES! These effects ARE non-standard neutrino interactions



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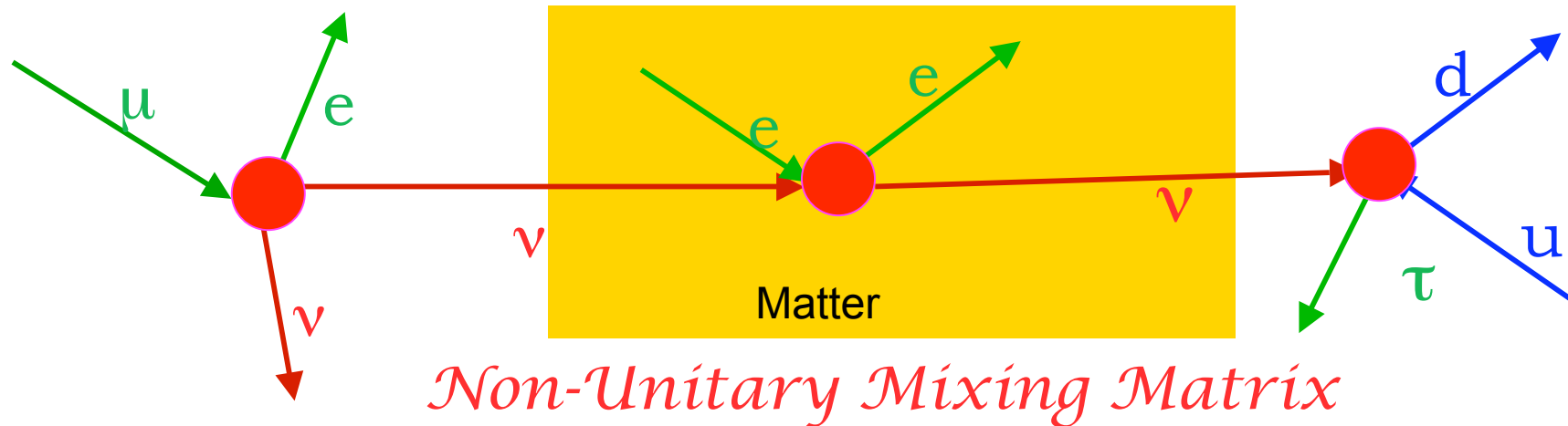
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*Non-Unitary Mixing Matrix*

...affecting simultaneously *production, propagation and detection.*

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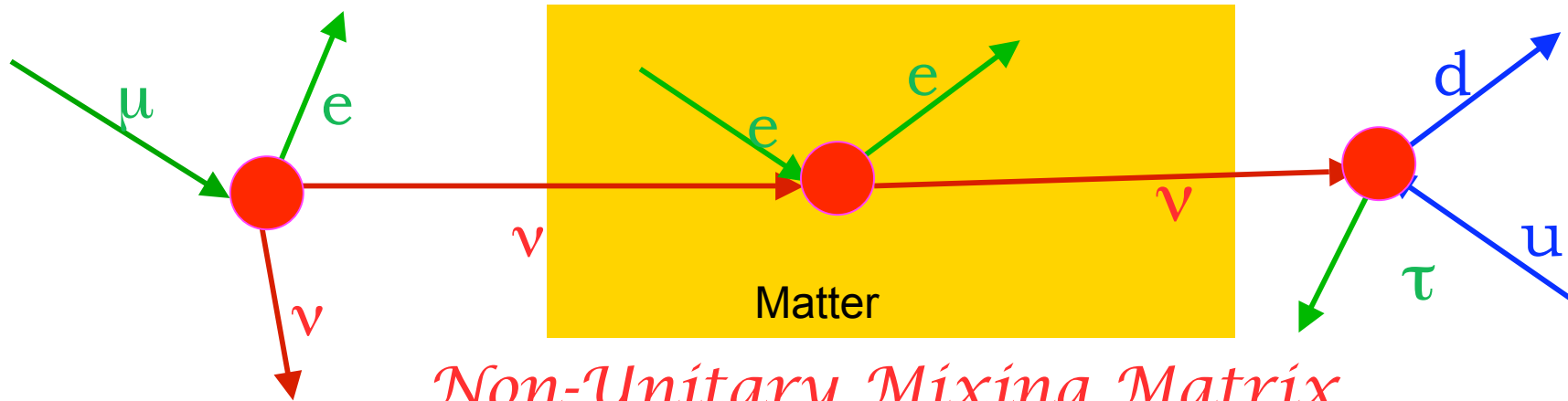


*Non-Unitary Mixing Matrix*

...affecting simultaneously *production, propagation and detection.*

These NSI are a generic signature  
of fermionic Seesaws

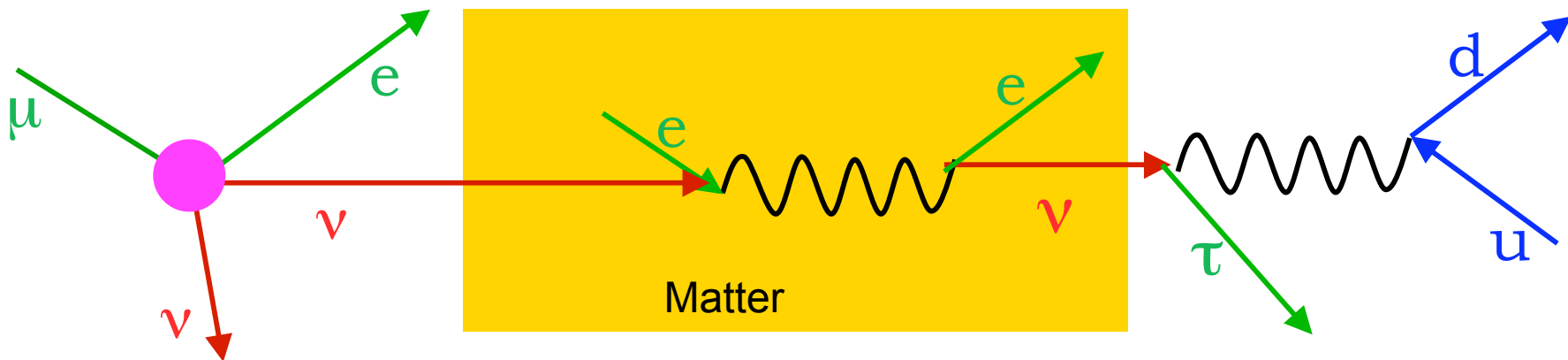
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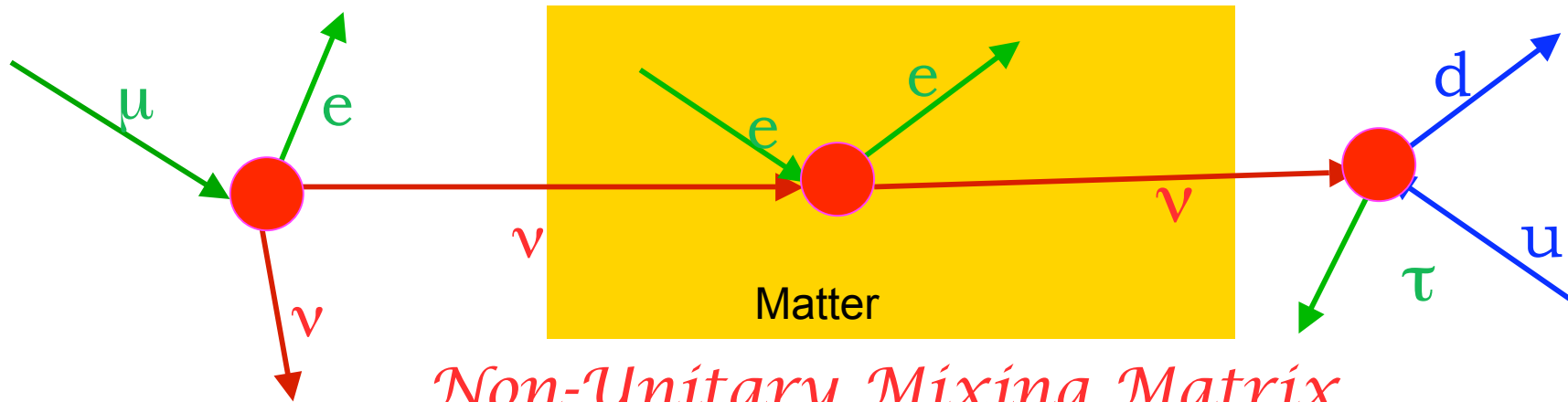
...affecting simultaneously production, propagation and detection.

To be compared with popular non-standard interactions, with either:



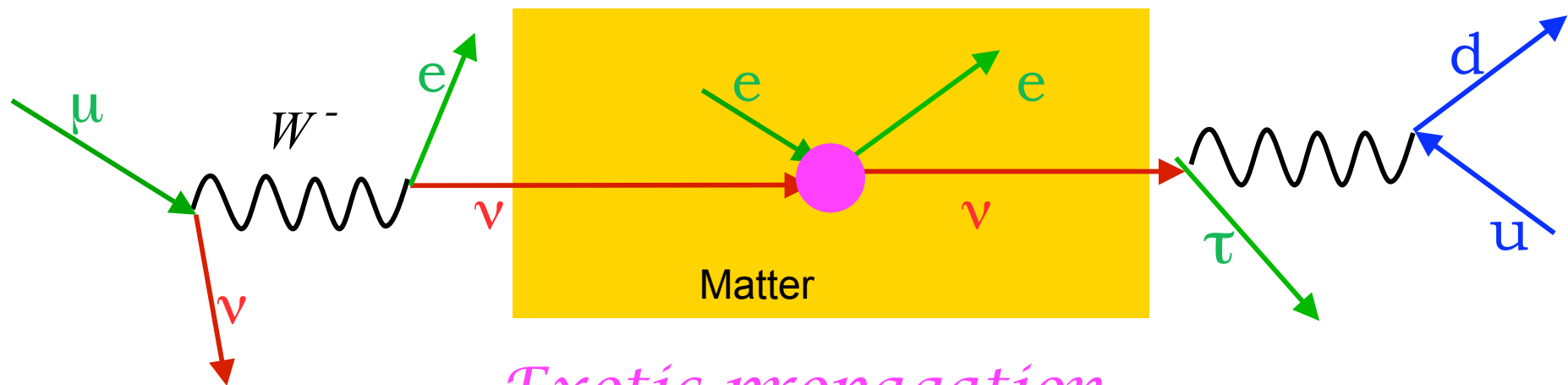
*Exotic production*

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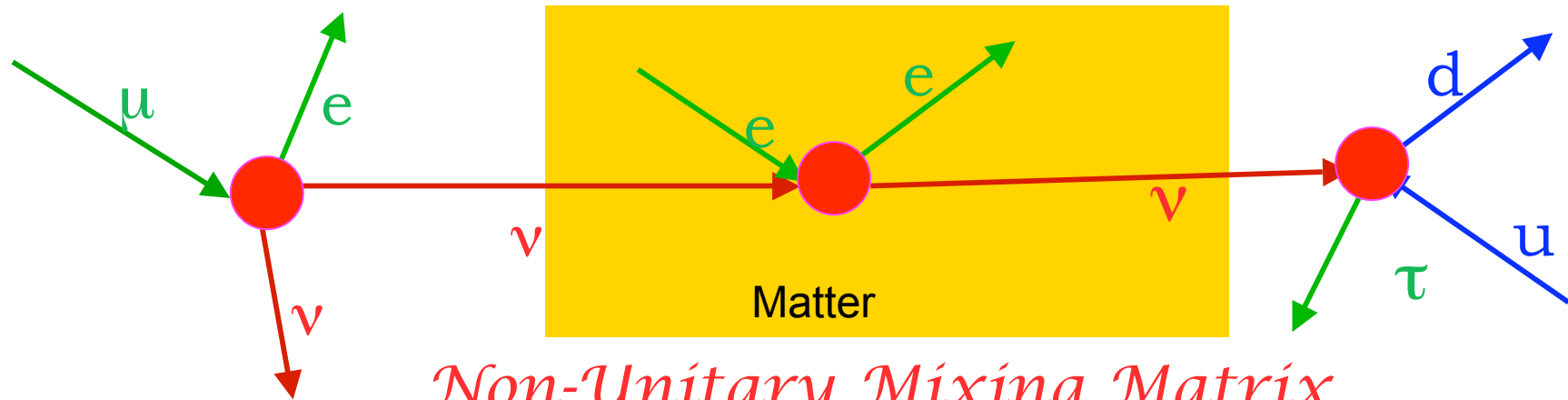
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*Exotic propagation*

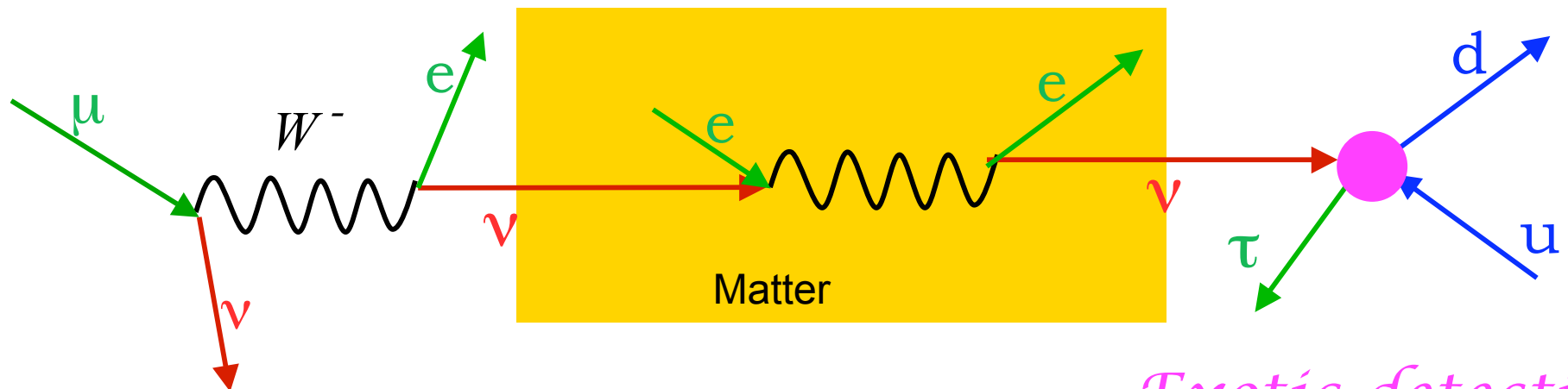
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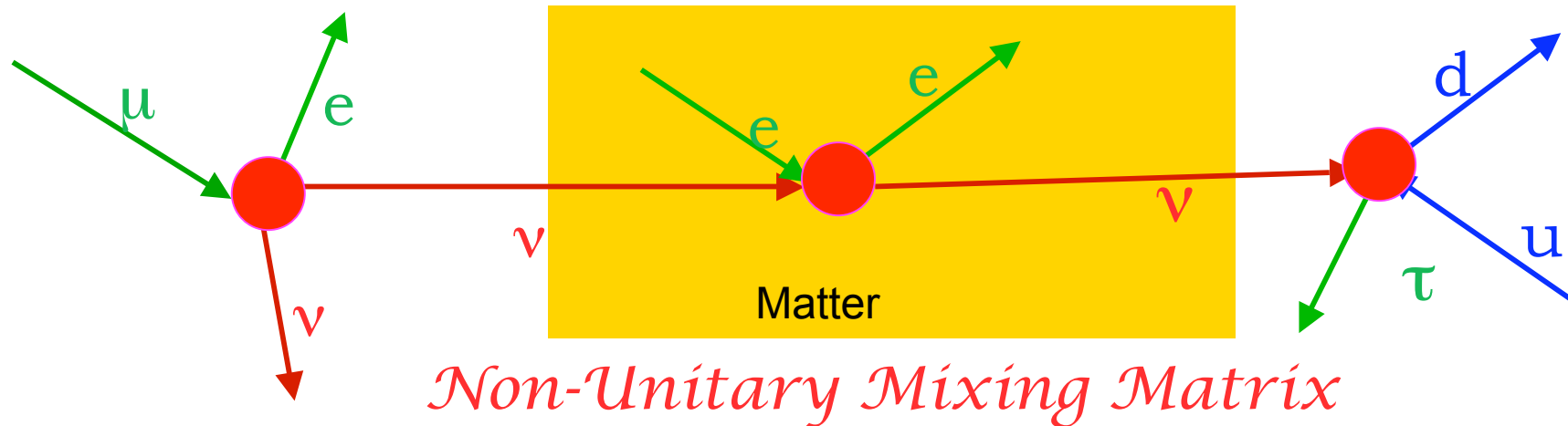
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*Exotic detection*



YES! These effects ARE non-standard neutrino interactions...



*Non-Unitary Mixing Matrix*

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These NSI are a generic signature  
of fermionic Seesaws

→ New CP-violation signals  
even in the two-family approximation

E. Fdez-Martinez, J.Lopez, O. Yasuda, M.B.G.

$$\text{i.e. } P(\nu_\mu \rightarrow \nu_\tau) \neq P(\bar{\nu}_\mu \rightarrow \bar{\nu}_\tau)$$

→ Increased sensitivity to the moduli  $|N|$   
in future Neutrino Factories

# Can we measure the phases of $N$ ?

E. Fdez-Martinez, J.Lopez, O. Yasuda, M.B.G.

If we parametrize  $N \approx (1 + \boldsymbol{\varepsilon}) U_{PMNS}$  with  $\boldsymbol{\varepsilon} = -\frac{v^2}{4} \mathbf{C}^{d=6}$

$$P_{\alpha\beta} \approx \left| 2\boldsymbol{\varepsilon}_{\alpha\beta} - i \sin(2\theta) \sin\left(\frac{\Delta m^2 L}{4E}\right) \right|^2$$

If  $L/E$  small

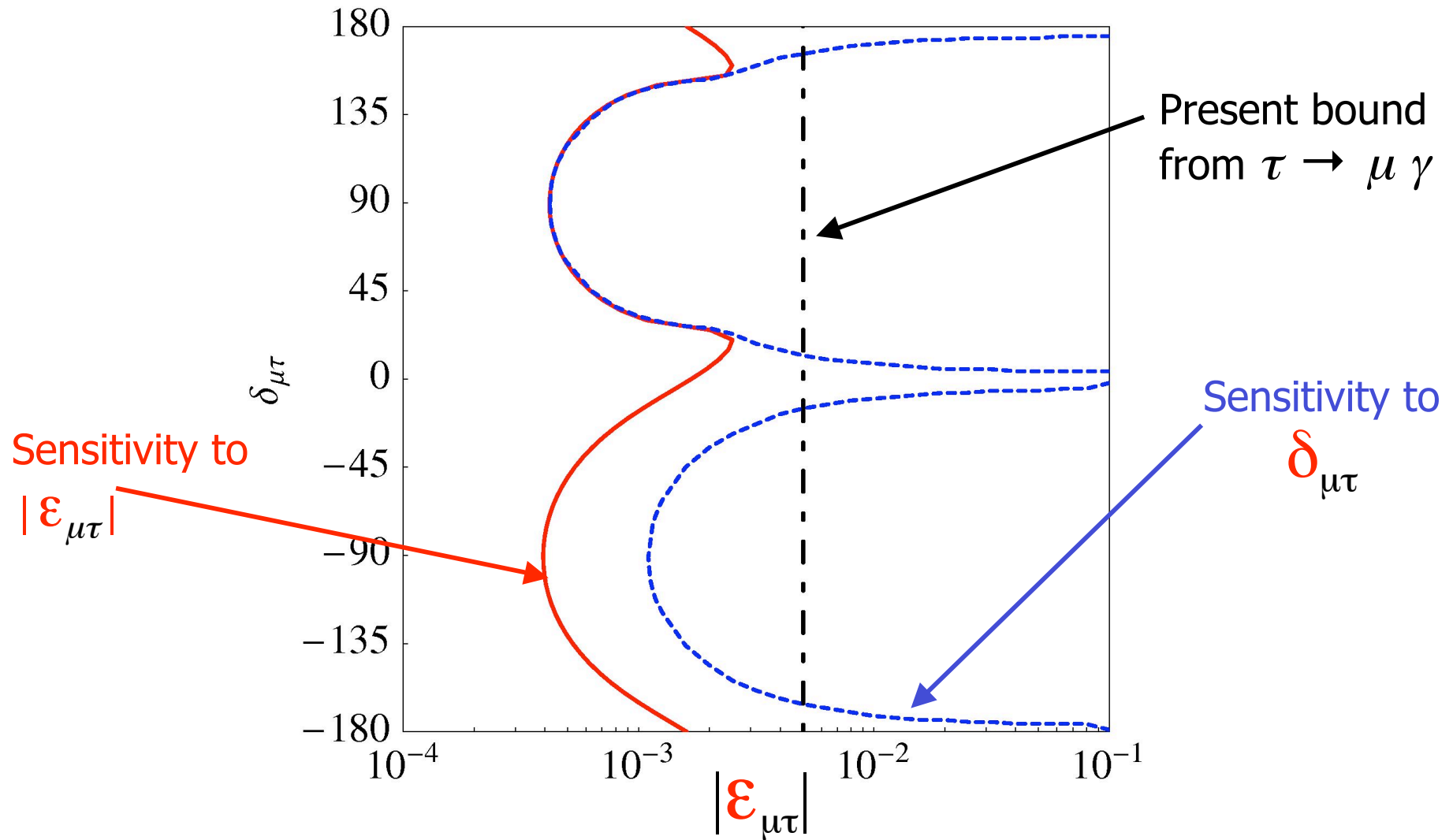
$$P_{\alpha\beta} = \underbrace{\sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)}_{\text{SM}} - \underbrace{2\text{Im}(\boldsymbol{\varepsilon}_{\alpha\beta}) \sin(2\theta) \sin\left(\frac{\Delta m^2 L}{2E}\right)}_{\text{CP violating interference}} + \underbrace{4|\boldsymbol{\varepsilon}_{\alpha\beta}|^2}_{\text{Zero dist. effect}}$$

SM

CP violating  
interference

Zero dist.  
effect

# Measuring non-unitary phases

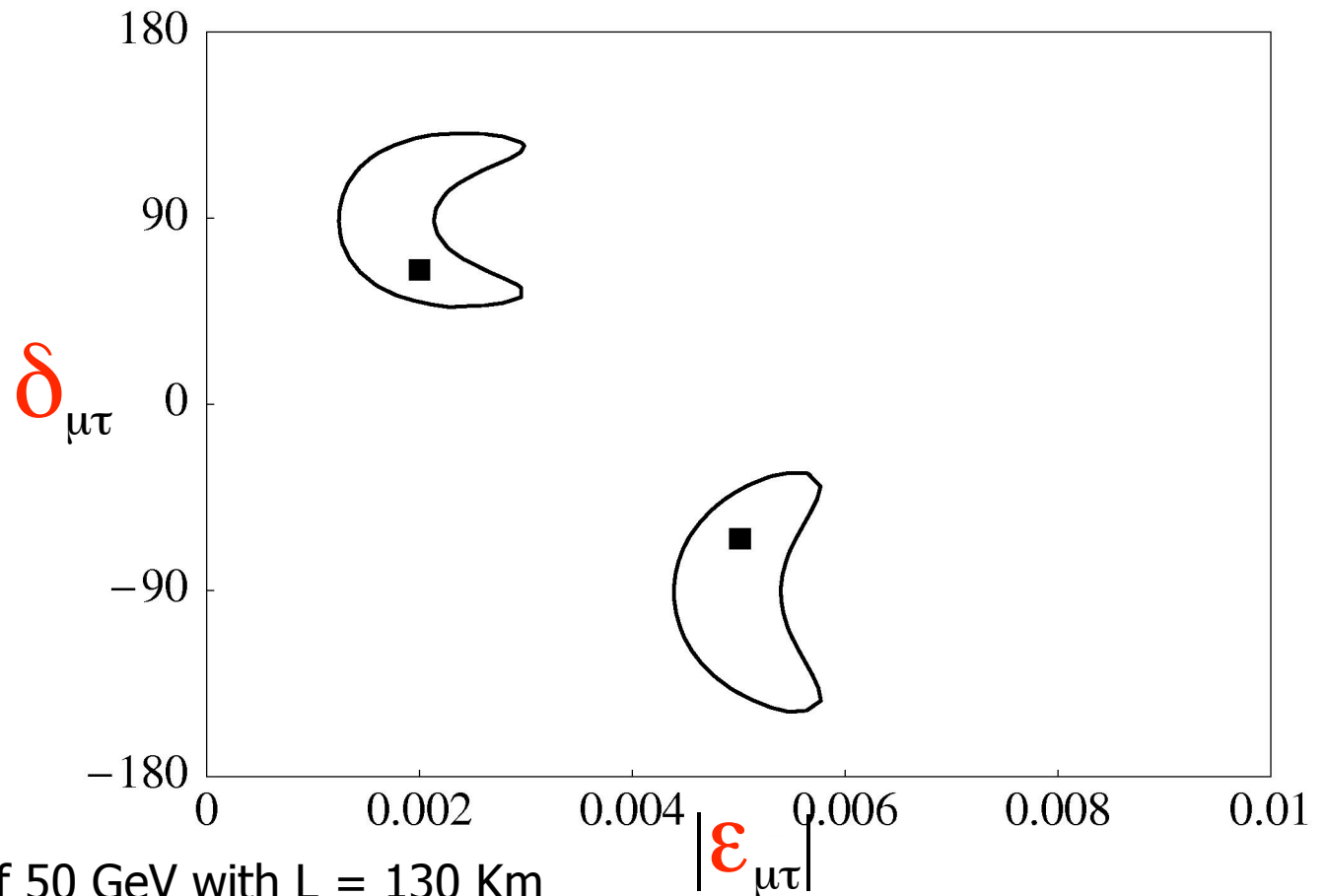


For non-trivial  $\delta_{\mu\tau}$ , one order of magnitude improvement for  $|N|$

In  $P_{\mu\tau}$  there is no  $\sin\theta_{13}$  or  $\Delta_{12}$  suppression:

$$P_{\mu\tau} - P_{\bar{\mu}\bar{\tau}} = -4 \operatorname{Im}(\epsilon_{\mu\tau}) \sin(2\theta_{23}) \sin\left(\frac{\Delta m_{23}^2 L}{2E}\right)$$

The CP phase  $\delta_{\mu\tau}$   
can be measured



At a Neutrino Factory of 50 GeV with  $L = 130$  Km



Good prospect for  $\nu_\mu - \nu_\tau$  channel at near detector  $\sim O(100 \text{ km})$

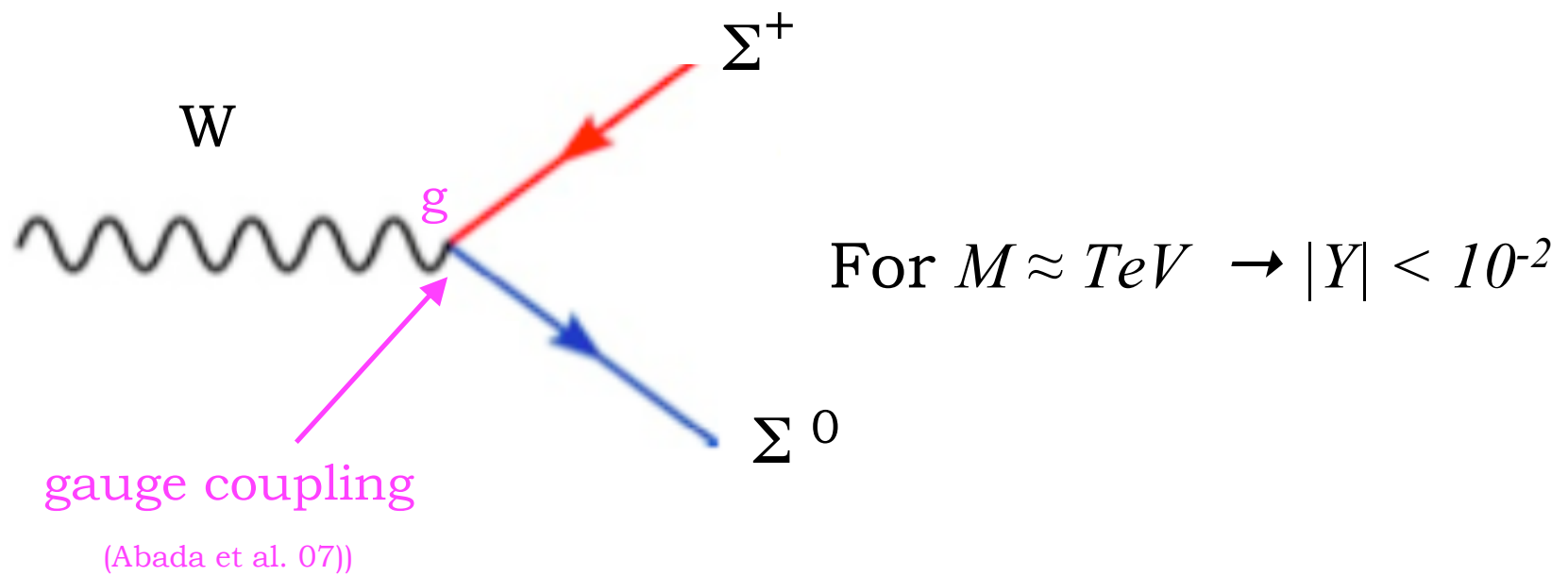
\* Recently: Goswami+ Ota; Altarelli+Meloni, Tang+Winter at nufact

• Also today!

Antusch et al.--> impact of e-tau non-unitary contribution to the golden channel in standard nufact setup, detector at  $\sim 1000 \text{ km}$

# Fermion-triplet seesaws:

similar - although richer! - analysis



➔ For the Triplet-fermion Seesaws (type III):

$$(\mathbb{N}\mathbb{N}^+ - 1)_{\alpha\beta} = \frac{v^2}{2} |c^{d=6}|_{\alpha\beta} = \frac{v^2}{2} |Y_{\Sigma}^{\dagger} \frac{1}{M_{\Sigma}^{\dagger}} \frac{1}{M_{\Sigma}} Y_{\Sigma}|_{\alpha\beta} \lesssim \begin{pmatrix} 3 \cdot 10^{-3} & < 1.1 \cdot 10^{-6} & < 1.2 \cdot 10^{-3} \\ < 1.1 \cdot 10^{-6} & 4 \cdot 10^{-3} & < 1.2 \cdot 10^{-3} \\ < 1.2 \cdot 10^{-3} & < 1.2 \cdot 10^{-3} & 4 \cdot 10^{-3} \end{pmatrix}$$

(Abada et al 07)



# Scalar triplet seesaw

Bounds on  $c^{d=6}$

Process	Constraint on	Bound ( $\times (\frac{M_\Delta}{1 \text{ TeV}})^2$ )
$M_W$	$ Y_{\Delta\mu e} ^2$	$< 7.3 \times 10^{-2}$
$\mu^- \rightarrow e^+ e^- e^-$	$ Y_{\Delta\mu e}   Y_{\Delta ee} $	$< 1.2 \times 10^{-5}$
$\tau^- \rightarrow e^+ e^- e^-$	$ Y_{\Delta\tau e}   Y_{\Delta ee} $	$< 1.3 \times 10^{-2}$
$\tau^- \rightarrow \mu^+ \mu^- \mu^-$	$ Y_{\Delta\tau\mu}   Y_{\Delta\mu\mu} $	$< 1.2 \times 10^{-2}$
$\tau^- \rightarrow \mu^+ e^- e^-$	$ Y_{\Delta\tau\mu}   Y_{\Delta ee} $	$< 9.3 \times 10^{-3}$
$\tau^- \rightarrow e^+ \mu^- \mu^-$	$ Y_{\Delta\tau e}   Y_{\Delta\mu\mu} $	$< 1.0 \times 10^{-2}$
$\tau^- \rightarrow \mu^+ \mu^- e^-$	$ Y_{\Delta\tau\mu}   Y_{\Delta\mu e} $	$< 1.8 \times 10^{-2}$
$\tau^- \rightarrow e^+ e^- \mu^-$	$ Y_{\Delta\tau e}   Y_{\Delta\mu e} $	$< 1.7 \times 10^{-2}$
$\mu \rightarrow e\gamma$	$ \sum_{l=e,\mu,\tau} Y_{\Delta l\mu}^\dagger Y_{\Delta el} $	$< 4.7 \times 10^{-3}$
$\tau \rightarrow e\gamma$	$ \sum_{l=e,\mu,\tau} Y_{\Delta l\tau}^\dagger Y_{\Delta el} $	$< 1.05$
$\tau \rightarrow \mu\gamma$	$ \sum_{l=e,\mu,\tau} Y_{\Delta l\tau}^\dagger Y_{\Delta\mu l} $	$< 8.4 \times 10^{-1}$

# Scalar triplet seesaw

Combined bounds on  $c^{d=6}$

Combined bounds		
Process	Yukawa	Bound $\left(\times \left(\frac{M_\Delta}{1\text{TeV}}\right)^4\right)$
$\mu \rightarrow e\gamma$	$ Y_{\Delta_{\mu\mu}}^\dagger Y_{\Delta_{\mu e}} + Y_{\Delta_{\tau\mu}}^\dagger Y_{\Delta_{\tau e}} $	$< 4.7 \times 10^{-3}$
$\tau \rightarrow e\gamma$	$ Y_{\Delta_{\tau\tau}}^\dagger Y_{\Delta_{\tau e}} $	$< 1.05$
$\tau \rightarrow \mu\gamma$	$ Y_{\Delta_{\tau\tau}}^\dagger Y_{\Delta_{\tau\mu}} $	$< 8.4 \times 10^{-1}$

Observable non-standard interactions from

$$\boxed{Y_{\Delta}^{\dagger} Y_{\Delta} / M^2 (\bar{L}_{\alpha} L_{\beta}) (\bar{L}_{\gamma} L_{\delta})} \quad \text{in scalar triplet seesaw ???}$$

Barely so ! (Malinsky Ohlsson and Zhang 08):

- Require Yukawa couplings are almost diagonal--> *degenerate neutrino spectrum*
- Not excluded are

$$\mu^{-} \rightarrow e^{-} \nu_e \bar{\nu}_{\mu} \dots \quad \text{Wrong sign muons at near detector}$$

# No $\nu$ masses in the SM

because the SM *accidentally* preserves B-L

i.e. Adding singlet neutrino fields  $N_R$

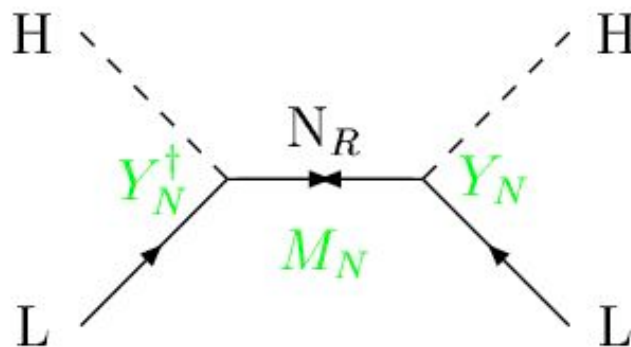
- right-handed  $N_R \rightarrow Y_N \tilde{H} \bar{L} N_R + h.c. \rightarrow m_D \bar{\nu}_L N_R + h.c.$

Would require  $Y_N \sim 10^{-12}$  !!! Why  $\nu_s$  are so light???

Why  $N_R$  does not acquire **large** Majorana mass?

$$\delta\mathcal{L} \sim M (N_R N_R)$$

OK with gauge invariance



## Seesaw model

Which allows  $Y_N \sim 1 \rightarrow M \sim M_{\text{Gut}}$

# $N$ elements from oscillations & decays

**MUV**

without unitarity  
OSCILLATIONS  
+DECAYS

$$|N| = \begin{pmatrix} .75 - .89 & .45 - .65 & <.20 \\ .19 - .55 & .42 - .74 & .57 - .82 \\ .13 - .56 & .36 - .75 & .54 - .82 \end{pmatrix}$$

Antusch, Biggio, Fernández-Martínez,  
López-Pavón, M.B.G. 06

$3\sigma$

with unitarity  
OSCILLATIONS

$$|U| = \begin{pmatrix} .79 - .88 & .47 - .61 & < .20 \\ .19 - .52 & .42 - .73 & .58 - .82 \\ .20 - .53 & .44 - .74 & .56 - .81 \end{pmatrix}$$

M. C. Gonzalez Garcia hep-ph/0410030