Lawrence W. Jones University of Michigan Department of Physics Ann Arbor, MI 48109

or

The momentum acceptance of the Fermilab booster for 5.18 GeVp's limits the accepted \overline{p} momentum spread to $\delta P/P = 3 \times 10^{-3}$. It is noted here that a larger momentum spread from a \overline{p} production target may be accepted if a short linac section is used to give the \overline{p} 's an energy kick following a drift space from their production target, so that their time of arrival at the linac is related to their momentum error.

The scenario would be as follows: first the 80 GeV protons in the MR would be debunched (not necessarily completely) and then rebunched tightly at a high frequency f by a linac section. Then the extracted protons would strike the \overline{p} production target in tight bunches, e.g., spread in time by $\lesssim 0.1 \text{ f}^{-1}$. Then a drift space Z would follow (occupied by the \overline{p} beam transfer optics). Finally, a linac section, also at f and phased with the section in the main ring, would transmit the central particles of each spread bunch at 0° phase angle but would accelerate the late particles and decelerate the early particles in order to leave an ongoing beam debunched in time (over \lesssim π radians) but homogenized in momentum. This beam is then inflected into the booster for deceleration and cooling.

The time dispersion of particles starting simultaneously after drifting a distance z meters in terms of their energy difference is given by

$$\delta t = \frac{\beta z}{c} = \frac{\delta \gamma}{\gamma^3} \frac{z}{c}, \qquad (\gamma >> 1),$$

so that

$$\frac{dE}{dt} = \frac{E_{o}\gamma^{2}c}{z} , \quad (\frac{\delta\gamma}{\gamma} \cong \frac{dE}{E_{o}})$$

This energy spread can be compensated by an energy kick from the linac section where, from the linac rf,

$$\frac{dE}{dt} = 2\pi f E_{L},$$

and ${\bf E}_{\rm L}$ is the peak energy of the linac.

The momentum spread which can be compressed is just 2E for a maximum, although the linear portion of LdE/dt is ~ 2/3 of that. Combining the two above expressions,

$$z = \frac{E_o \gamma^2 c}{2\pi f E_T} .$$

 $2\pi f E_{1} = \frac{E_{0}\gamma^{2}c}{2}$,

As a numerical example, consider 5.18 GeV \overline{p} (γ = 6.51) with a 3% momentum spread compressed by a linac section of 1.0 GHz. The linac energy E_L would have to be at least 0.015 x 6 GeV = 90 MeV.

To preserve a greater region of linear dE/dt, $E_{L} = 130$ MeV. These values give

z = 121 meters.

The 3% momentum spread will be compressed to a fraction of 3% corresponding to the tightness of the 1 GHz bunching of the protons; if they are bunched to $1/20 \times 10^{-9}$ sec (1.5 cm), the 3% should compress to about 0.2% $\Delta p/p$.

There are some questions. The rf on-time required for the high frequency bunching hardware in the main ring is long, corresponding to a phase oscillation period at that frequency. Of course only one booster batch need be bunched each booster extraction cycle (60 millisec, the rf could be on for 1.5 μ sec and off for 19 μ sec each revolution). The second, debunching rf, would only need to be on for 2 μ sec.

The path length dispersion from the betatron phase space in the \overline{p} beam transport must be small compared to the energy-related dispersion. Hence if the beam crosses the axis at 10 mr, the path length spread of extreme rays is $\sim \frac{2}{3} \frac{\theta^2}{2} \approx 3 \times 10^{-5}$. This corresponds to $\delta E/E_0 = 1.26 \times 10^{-3}$.

If the rf systems are reasonable, technically and economically, it seems that a scheme such as this could gain a factor of 10 in \overline{p} flux and require minimal new construction or engineering. In particular, this could obviate the need for a stochastic cooling ring.