

NAL PROPOSAL No. 0086A

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A PROPOSAL TO STUDY INELASTIC DIFFRACTIVE PROCESSES
BY OBSERVING COHERENT PRODUCTION OF MULTI-PION FINAL STATES
FROM HE NUCLEI

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Orsay

July 20, 1970.

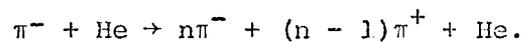
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University of Washington and Orsay Collaboration

ABSTRACT

We propose to study the diffraction dissociation of pions into multi-pion final states, by obtaining the missing mass spectra from the reaction:



The missing mass is calculated from a measurement of the He recoil which is observed in a streamer chamber. In this first exploratory experiment we propose to count the outgoing fast particles, and to measure in a very crude fashion their momenta.

Names of Experimenters:

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Date:

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I. INTRODUCTION.

We are proposing to study the surface states of the pion by observing the diffraction dissociation of pions into multi-pion final states. Such an experiment yields information about the "surface" because, by the nature of diffraction dissociation, we are constrained to small momentum transfers. In particular, in this experiment, we propose to use helium nuclei as a target. The form factor for the helium nucleus will then insure that the momentum transfer is less than ~ 300 MeV/c. The physics in this experiment is not unlike that obtained when we have the collision of two carbon nuclei in which the incident nucleus has only a peripheral collision and we observe the excitation of surface waves on the nucleus (the analog of deep inelastic scattering for nuclei would then be those collisions in which nucleons are excited into the continuum). As is well known from the study of nuclei, both the excitation of surface states and the study of deep inelastic scattering is necessary for a good understanding of the physics; likewise, in order to understand the structure of a pion, it will be necessary to obtain detailed information about the surface states as well as detailed information about the deep inelastic scattering. This experiment proposes to study only the former, namely, the surface states of the pion.

This experiment is a rather simple one which is aimed at "getting a look" at the various surface states which exist. Therefore, we are purposely designing this experiment not to restrict ourselves in the trigger logic, because, while results at existing accelerator energies give us some indication of what we might expect, the extrapolation of the incident energy by an order of magnitude will undoubtedly provide many surprises. Hence, we are using existing experimental information as a guide, but we are designing with very loose criteria so that new and unsuspected occurrences will not be overlooked.

The experimental apparatus, which will be discussed in greater detail in Section III and IV consists of a streamer chamber filled with helium gas. The helium nuclei act as both target and detector. By placing the streamer chamber in a magnetic field, it will be possible to obtain good momentum and angle measurements of the recoiling helium nucleus. We will, therefore, be

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able to obtain the missing mass of the multi-pion system which is recoiling against the helium nucleus. In addition, the fast charged pions will be visible in the chamber, and we will be able to measure the laboratory opening angle. A Charpak chamber at the downstream end of the chamber will allow us to count the number of outgoing pions and use this, if necessary, in the trigger. However, at the outset we would propose to take all interactions where more than two fast particles come out. In Section II we discuss the intuitive ideas behind diffraction dissociation, and what one might expect at higher energies based on the rather sparse data which now exist. In Sections III and IV we discuss the experimental set-up and the resolution which we think we will be able to obtain in this experiment.

This experiment makes no request of NAL other than for a pion beam and power for operating the magnet. The magnet will be supplied by the group at Orsay. It is capable of 20 kg over a volume of $1 \times .5 \times .5 \text{ m}^3$ and has provisions for 3 view stereo photography. It is the Ecole Polytechnique magnet designed by A. Lagarrigue's group for use with the Ecole's heavy liquid bubble chamber which has now been retired.

II. PHYSICS JUSTIFICATION.

A. Background on Diffraction Dissociation.

Diffraction dissociation was first proposed by Feinberg and Pomeranchuk in 1953¹⁾. It was then employed by Glauber in a discussion of deuteron stripping²⁾. The concept was later applied to hadronic processes by Good and Walker in 1960³⁾. It was this last paper which generated considerable interest in diffractive processes for the production of hadronic states and lead to a considerable amount of experimental work, using both nuclei and nucleons as targets.

The basic idea is that at high energies a particle of mass m can dissociate into a system of mass m^* with only very little momentum transfer to the target M , such that the phase difference of the de Broglie waves of states m and m^* are degenerate over the target. Another way of saying this is that as a particle passes through the nucleon or nucleus, it is a mixture of its eigen states in "nucleon stuff". Good and Walker pointed out that

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the absorption of the m^* component would result in the Fraunhofer diffraction scattering of m^* . Such a picture requires of the target that it absorb the incoming wave and take up whatever recoil momentum is necessary in order to account for the mass difference $\delta m = m^* - m$. We should note in passing that this is very much like the role of a proton or heavy nucleus in pair production. Now from such a picture, we would not expect any change in the internal quantum numbers $(C, G, T, Y, \sigma = P(-1)^J)$ of the incident particle. (There of course could always be a change in the angular momentum state.) We would, however, expect the cross section to be nearly constant with energy, since in diffractive processes the cross section depends only on the area of the absorbing disk. In addition, the diffractive nature of the interaction dictates that there be sharp forward peaking of the differential cross section. To summarize, we would expect for such diffractive processes:

- (1) Sharp forward peaking (Fraunhofer diffraction).
- (2) Small or no energy dependence of the cross section.
- (3) No change in the internal quantum numbers of the dissociated particle.

In the modern language of particle exchange models, one would say that a diffractive process is one in which a Pomeron is exchanged between the incident and target particle, and since the target plays no role in the dynamics of the inelastic diffraction, such processes are sensitive probes of the surface structure of the pion.

B. Existing Information.

Coherent production of multi-pion final states has been studied in great detail by the Orsay-Saclay-Milan-Berkeley (OSMB) collaboration using a heavy liquid bubble chamber filled with $C_2F_5Cl^4$. In their experiment, the coherent production of three and five pion final states was observed. The momentum transfer to the nucleus observed by the OSMB experiment is shown in Figure 1. One notices two slopes: The first slope $\sim 80(\text{GeV}/c)^{-2}$ is characteristic of the form factor of the nucleus involved, while the second slope $\sim 10(\text{GeV}/c)^{-2}$ represents events in which the nucleus has been broken up; therefore, the interaction is an incoherent one which takes place on a nucleon.

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The 3π and 5π mass spectra which were observed in these experiments are shown in Figure 2. The first peak that occurs in the 3π mass spectrum occurs near the $\rho\pi$ threshold at $1.08 \text{ GeV}/c^2$ (a_1); indeed, the OSMB collaboration finds that the mass spectrum up to $1.4 \text{ GeV}/c^2$ consists almost entirely of $\rho\pi$ final states. They also observe an enhancement at approximately $1.6 \text{ GeV}/c^2$ which is mainly $f^0\pi$ ($A_{1.6}$). The coherently produced 5π events show a peak in the 5π mass spectrum at approximately $1.9 \text{ GeV}/c^2$ ($A_{1.9}$) which, as is noted in reference 4c, is near the $A_1 \rho$ threshold. In the OSMB data, although the statistics are not overwhelming, there is indication of A_1 and ρ .

Further evidence of coherent production of multi-pion final states has been obtained by a Russian collaboration at Serpukhov⁵⁾. This experiment was performed using an emulsion stack as the target and detector. In this experiment, they did not measure the momentum of the outgoing particles, and therefore, could not observe the invariant mass spectrum. However, they did obtain a multiplicity plot which is shown in Figure 3b. They found that the number of 3 pion events far exceeded the other multiplicities. For the events in which no nuclear breakup was observed, they found that $\sum_i \sin \theta_i$ peaked near zero, where θ is measured relative to the beam, while for nuclear breakup events the distribution is broader; since the $\sum_i \sin \theta_i$ is proportional to the longitudinal momentum transfer, it is very likely that this experiment is observing dissociation of a pion into 3 and 5 pions.

An experiment has been performed at CERN with a pion beam using several nuclei as targets. The beam momentum was approximately $16 \text{ GeV}/c$. The fast secondaries were detected by optical spark chambers placed in a magnet. Analysis of this experiment is nearly completed and private communications indicate that dissociation into three pions has been observed, and the effective mass spectrum has the classical diffraction shape of the OSMB experiment.

The apparent lack of events at the higher multiplicities in the existing experiments can be understood in terms of the momentum transfer necessary to produce the final state. At high energies the minimum momentum transfer which is necessary to produce a multi-pion state of invariant mass M is given

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by

$$q_1 = (M^2 - m_\pi^2) / 2p_{inc} ,$$

where p_{inc} is the momentum of the incident pion. In Figure 4 we show typical minimum momentum transfers for various invariant masses and incident pion momenta between 50 and 250 GeV/c. The momentum transfer distribution for interactions on the nucleus, where a pion dissociates and a nucleus recoils without breaking up, is dependent on the nuclear form factor. This was demonstrated by the OSMB data in Figure 2, where the two slopes clearly show coherent recoil of the nucleus (slope of $\sim 80(\text{GeV}/c)^{-2}$), and a nucleon recoil (slope of $\sim 10(\text{GeV}/c)^{-2}$). Intermediate nuclei in the range of 12 - 40 nucleons have diffraction minima ranging from 150 to 200 MeV/c. The heavy nuclei such as Pb have the first minima occurring at 100 MeV/c or less. Therefore, the above experiments performed either at 16 GeV/c on intermediate nuclei, or at 60 GeV/c on heavy emulsion nuclei are not terribly sensitive to the heavier states into which a pion can dissociate.

There has been considerable controversy over the true nature of such diffractively produced mass enhancements. The question of whether such enhancements are in fact resonances in the usual sense, or merely manifestations of the kinematics of the interaction has not been satisfactorily answered. A model known as the Drell-Haida-Deck model has been proposed which gives rise to threshold enhancements in the $\rho\pi$ system at $1 \text{ GeV}/c^2$ (see Figure 5). In such a model the mass peak results purely from the kinematics and has no dynamical origin. Goldhaber et al. have suggested that a possible way to test such a model would be to measure the interaction cross section of the $\rho\pi$ system with nucleons⁷⁾. The argument is that if the A_1 system has a cross section for interacting with nucleons which is essentially that of the π -nucleon or the ρ -nucleon cross section rather than the sum of the two, then the conclusion is that the $\rho\pi$ system does not behave as though it were a free ρ and π . The only way to measure such cross sections is to produce the system in question on nuclei and make use of the Glauber or high energy model in order to measure the attenuation of the multi-pion system as it leaves the nucleus. The details of this model have

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been worked out by Glauber and others⁸⁾, and it is this model which has been used with great success by Ting and co-workers in obtaining the ρ -nucleon cross section from the photo production of ρ mesons on nuclei⁹⁾. Goldhaber et al. found that when they analyzed the OSMB data in this way, the effective A_1 nucleon cross section was compatible with the π -nucleon cross section, which argues against the A_1 being simply a Deck like kinematic effect⁷⁾.

C. Expectations at Higher Energies.

It is interesting to note that in the OSMB experiment the Q per pion is approximately 220 MeV in both the 1.09 and 1.9 GeV/c² peaks shown in Figure 2. If one extrapolates to a 7π system assuming 220 MeV per pion, we would expect the 7π system to show a peak near 2.6 GeV/c² which is, amazingly enough, approximately the threshold of the $A_{1.9} + \rho$, whereas the 1.9 GeV/c² (5π) enhancement occurs at approximately $A_1 + \rho$ threshold. This leads one to the interesting speculation that the pion is composed basically of many ρ 's, and it dissociates by kicking out "one more ρ ". The 9π peak in this simple model would then occur at approximately 3.4 GeV/c². A similar conclusion can be reached for the $f^0\pi$ system, where 1.6 GeV/c² enhancement implies a Q per pion of 410 MeV. Such a model suggests the multi-pion spectra shown in Figure 6. The solid lines indicate the enhancements which have been produced diffractively in the existing experiments. The dotted lines indicate the enhancements which are suggested by the constant Q per pion discussed above. We expect a mass resolution of $\Delta m_x = (100-150)/m_x$ MeV/c², where m_x is in GeV/c². This is sufficient for the spectra shown in Figure 6; however, it is possible that the resolution may be improved. (See Appendix A.)

The cross section which has been obtained by the emulsion groups, indicates that at 100 GeV/c we should expect approximately 2 mb for the 3π channel alone, which will be ample cross section for us to observe.

IV. EXPERIMENTAL ARRANGEMENTS.

The ideal detector for investigating coherent production on helium (or other noble gas nuclei) is the streamer chamber. The chamber gas serves both as target and detector. The low density of the gas means that the recoil nucleus has a range long enough to allow us to measure

the track curvature in a magnetic field. Below ~ 200 MeV/c, a recoil He nucleus will stop in the gas, thus allowing us to use Range to determine the momentum as well (see Figure 7). The target density is still sufficient to give us a high trigger rate. For a fiducial volume 50 cm long, we have in He 1.5×10^{-6} interactions/mb of cross section/beam π . We envisage using a chamber 1 meter long by 50 cm wide. It will be a standard double gap chamber, with 15 cm gaps. A chamber of this size has already been successfully run using both pure helium and the standard 90%-10% Ne-He mixture.

In keeping with the large number of possible final states, we would like to use as flexible a trigger as possible. The counters used in the trigger logic as shown in Figure 8a. The incoming beam direction is defined by small proportional chambers. C4 is also a proportional chamber, used as a logic element which allows us to predetermine the minimum number of particles desired for a trigger. Since no recoil nucleus can get through the walls of the chamber, the presence of particles out the sides indicates an event of no interest. Counter C5, a combination of scintillator and thin lead sheet, is to be used in an anti-coincidence mode. C5 is extended to cover the bottom of the chamber as well. Thus a complete trigger for the chamber would be

$$C1 C2 C3 C4 (X \geq n) \overline{C5} \overline{C6} .$$

The chamber will be operated with a memory time of 2 to 5 μ sec., using chemical clearing. Due to the extremely high multiple track efficiency, we do not foresee any difficulties with high beam rates or random extra tracks in the chamber. The magnet in which the chamber will be placed is the one in which Professor Lagarrigue's heavy liquid bubble chamber BP3 was previously housed. (See Appendix B for details.) A floor plan of the experimental set-up is given in Figure 10.

As mentioned above the trigger requirements are designed to be initially as loose as possible. This will, of course, lead to a fairly large number of pictures. This is not a serious problem however, as we plan to use our PEPR automatic measuring machine for analysis. A developmental program to enable PEPR to read streamer chamber film is beginning. The advantage of using a proportional chamber for C4 is that the trigger requirement can easily be changed during the course of the experiment. We plan to trigger initially

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on three or more fast particles. If we then find that the majority of our triggers contain 3 pions, as we expect, we can use the proportional chamber to demand five tracks and concentrate on the higher multiplicities.

Aside from the beam, and of course, water and power for our analyzing magnet, there is essentially no contribution necessary from NAL. Our equipment is relatively simple. A prototype streamer chamber with a Marx generator and Blumlein already exists. As a result of the work of the SLAC streamer chamber group, optics is no longer a problem. Sufficiently fast film and lenses exist and are in hand. Proportional chambers have been built at the University of Washington and further development is in progress. Thus, we feel that this experiment is sufficiently simple so that we can be ready as soon as there is a pion beam. We envisage 4 to 6 weeks of set-up and testing in which only approximately %50 is beam time. This testing can be done parasitically or even before a 0.1% π beam is available. The beam rate needed is quite low, 10^5 /pions/pulse would be sufficient.

We would like to collect approximately 10^5 events. Under the assumption of five to ten triggers/coherent event, we are then talking about 5×10^5 to 10^6 total pictures. With PEPR, this is not an unreasonably large number. The streamer chamber system is capable of two and possibly three triggers/pulse, if the beam rate and cross section are high enough to give us the triggers. We would then require about 800 hours of data taking time (at one trigger/pulse). The amount of time required will obviously be less if we can reduce the 10:1 pictures/event ratio. We plan to test the efficiency of our trigger and chamber arrangement in a high energy π beam at a machine either in the U.S.A. or at CERN if time permits.

IV. APPARATUS.

In the following table, we list the apparatus necessary for this experiment and by whom it shall be provided.

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LIST	UW	Orsay	NAL
1 x .5 x .5 m ³ 20 kg magnet with 3 cameras		X	
Streamer chamber	X		
Proportional Chambers	X	X	
Scintillator Counter and Electronic logic	X		
PEPR for Measuring Film	X		
Small Computer (PDP-8)	X		
Beam, π^- ($10^5 - 10^6$)/Pulse, $\Delta p/p = 0.1\%$			X
Power and Water for Magnet			X
Space Requirement of Approximately 10 - 12 Meters by 6 meters and trailer space			X

APPENDIX A

The ability to reconstruct the missing mass is critical to this experiment. In the reaction $\pi + \text{He} \rightarrow \text{He} + X$, the mass of X is given by

$$m_X^2 = m_\pi^2 + 2 m_\alpha^2 + 2 m_\alpha E_\pi - 2 E_\alpha (E_\pi + m_\alpha) + 2 p_\alpha p_\pi \cos \theta .$$

In this equation, m_π and m_α refer to the masses of the incident pion and the target nucleus respectively. $E_\pi(p_\pi)$ is the energy (momentum) of the incident beam, $E_\alpha(p_\alpha)$ is the energy (momentum) of the recoil nucleus, and θ is the scattering angle of the recoil nucleus. In order to make an estimate of what the mass resolution will be, we form the following quantities:

$$\frac{\partial m_X}{\partial p_\pi} = - \frac{T_\alpha + p_\alpha \cos \theta}{m_X} ,$$

where T_α is the kinetic energy of the recoil nucleus,

$$\frac{\partial m_X}{\partial p_\alpha} = \frac{1}{m_X} (p_\pi \cos \theta - \beta_\alpha (E_\pi + m_\alpha)) ,$$

$$\frac{\partial m_X}{\partial \theta} = - \frac{p_\alpha p_\pi \sin \theta}{m_X} .$$

Since T_α , p_α and $\cos \theta$ are all rather small quantities $\frac{\partial m_X}{\partial p_\pi}$ is small.

As Δp_π , the uncertainty in the beam momentum, is also small (100 MeV/c), the uncertainty in m_X due to Δp_π is negligible. The analysis of the contributions of Δp_α and $\Delta \theta$ to Δm_X are not as simple. Using a measuring error in p_α of 1 - 2% and an error in θ of 1 - 5 milliradians, we find that the error in m_X

$$\Delta m_X \sim \frac{100 - 150}{m_X} \text{ MeV}$$

A more careful calculation of the resolution to be expected by measuring the recoil alone is in progress. It must be pointed out, however, that we do have additional constraints in the problem. The combination of the streamer chamber and the downstream proportional chamber give us a very accurate determination of the directions of the outgoing pions and a measurement, albeit, not

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very accurate, of their momenta. These additional data will certainly improve our mass resolution. We are currently performing Monte Carlo calculations in order to better determine our mass resolution.

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APPENDIX B

The magnet has been used for the Ecole Polytechnique's heavy liquid bubble chamber. The chamber, which has now been retired, operated for several years and has taken over 3×10^6 pictures. A sketch of the magnet is given in Figure 10.

The visible volume is $1 \times .5 \times .5 \text{ m}^3$. There is additional free space on top and bottom which can be used for high voltage cables and anti-coincidence counters. If necessary the depth can easily be increased at the cost of slightly reducing the magnetic field. There is easy access to the useable volume at the beam entry and beam exit side of the magnet. The connection to the blumlein can be made at the entrance as is shown in Figures 10 a,b. The present optical system has a total stereo angle of 29° . The maximum magnetic field is 22 kg at a current of 7,500 amps, and a voltage of 575 volts, which implies 4.3 megawatts of power. Under these conditions cooling the magnet requires a water flow of $77 \text{ m}^3/\text{hour}$ at a pressure head of 25 atmospheres. The temperature rise is then 50° C .

For this experiment a field of about 17 kg requiring only approximately 2 megawatts of power (see Figure 9) is adequate. Then maintaining the same Δt (temperature rise) a water flow of $35 \text{ m}^3/\text{hr}$ would be sufficient.

Under these operating conditions we would require 5,000 amps at 400 volts; however, since electrical connections of the pancakes are accessible, it is possible to match the magnet to a generator of different characteristics.

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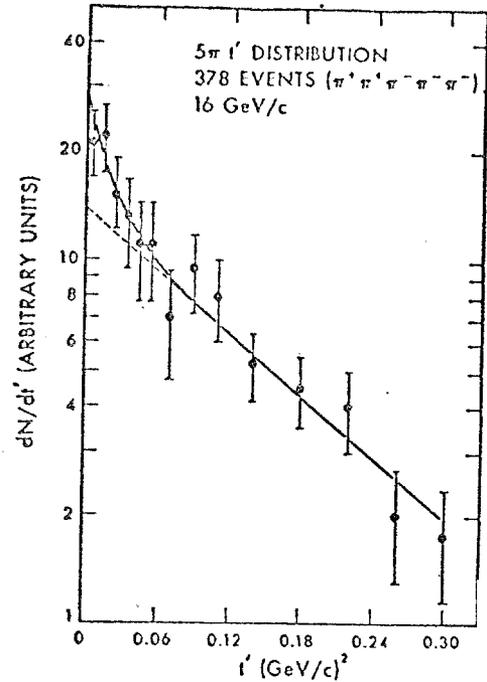


Fig. 2. Distribution in $t' = t - t_{\min}$ for all data.

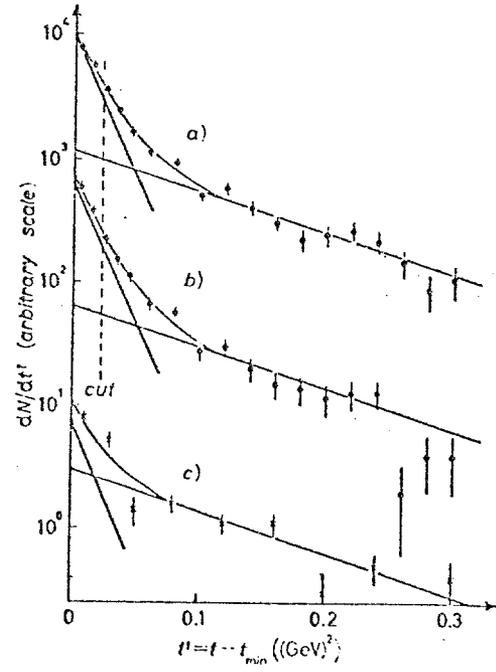


Fig. 1. - dN/dt' for a) all $\pi^+\pi^-\pi^-$, b) π^-p^0 , c) π^-f^0 events. The steeper slope is $54 (\text{GeV})^{-2}$ ($80 (\text{GeV})^{-2}$ after correcting for resolution) and the other $7.7 (\text{GeV})^{-2}$ ($8.1 (\text{GeV})^{-2}$ after correcting for resolution). The cut taken for coherent events is shown by the dashed line.

Figure 1, Momentum Transfer Distribution for Production of 3π and 5π Charged Pions in the OSMB Experiment.

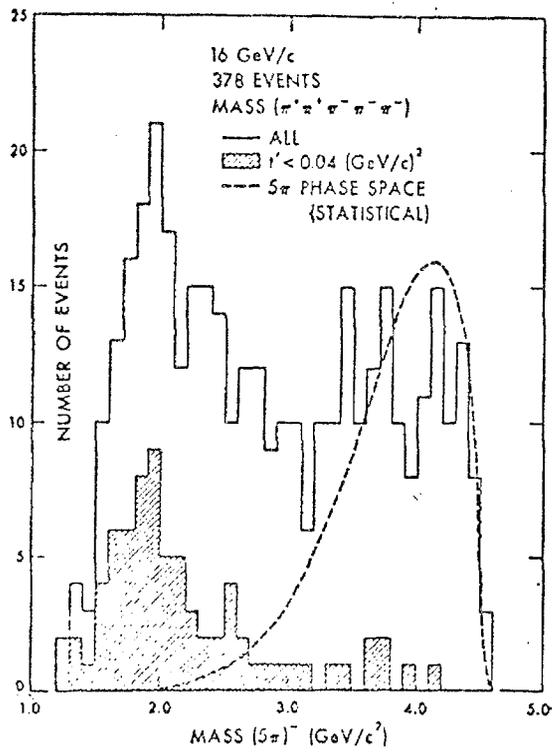
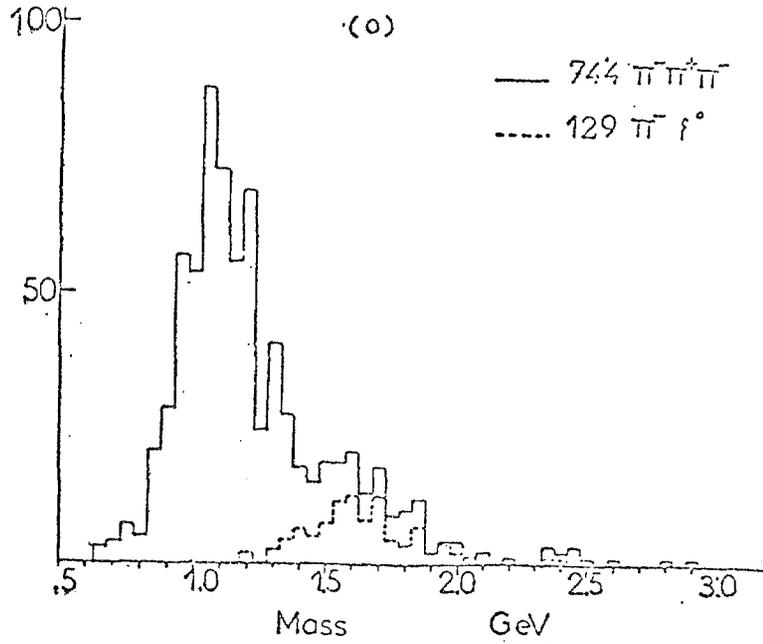


Figure 2, Mass Spectra in the OSMB Experiment.

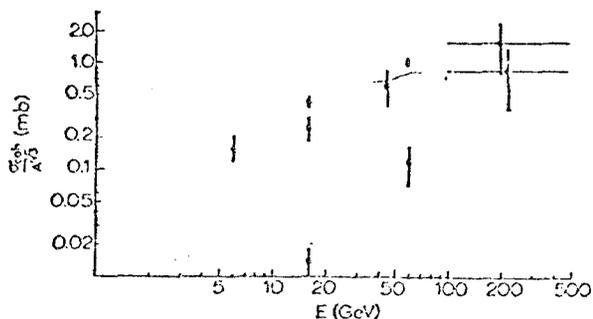


Fig. 3a "Normalized" cross section $\sigma_{coh}/A^{2/3}$ for the coherent reactions $\pi^- \rightarrow 3\pi^-$ and $\pi^- \rightarrow 5\pi^-$ as a function of the primary energy E_0 . A 20% correction for the contamination of the three-prong coherent events by the reaction (1) has not been introduced at 60 GeV/c since it cannot be done at 45 GeV/c and at ~ 200 GeV/c.

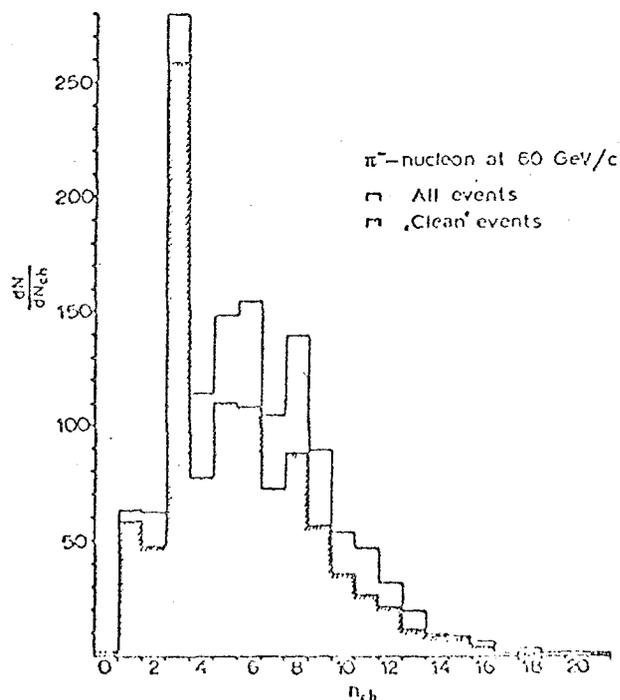


Fig. 3b Prong-number distribution of π^- -nucleon interactions at 60 GeV/c. The dashed distribution corresponds to the "clean" events.

Figure 3, Results of the Serpukhov Emulsion Experiment for 60 GeV/c Incident π^-

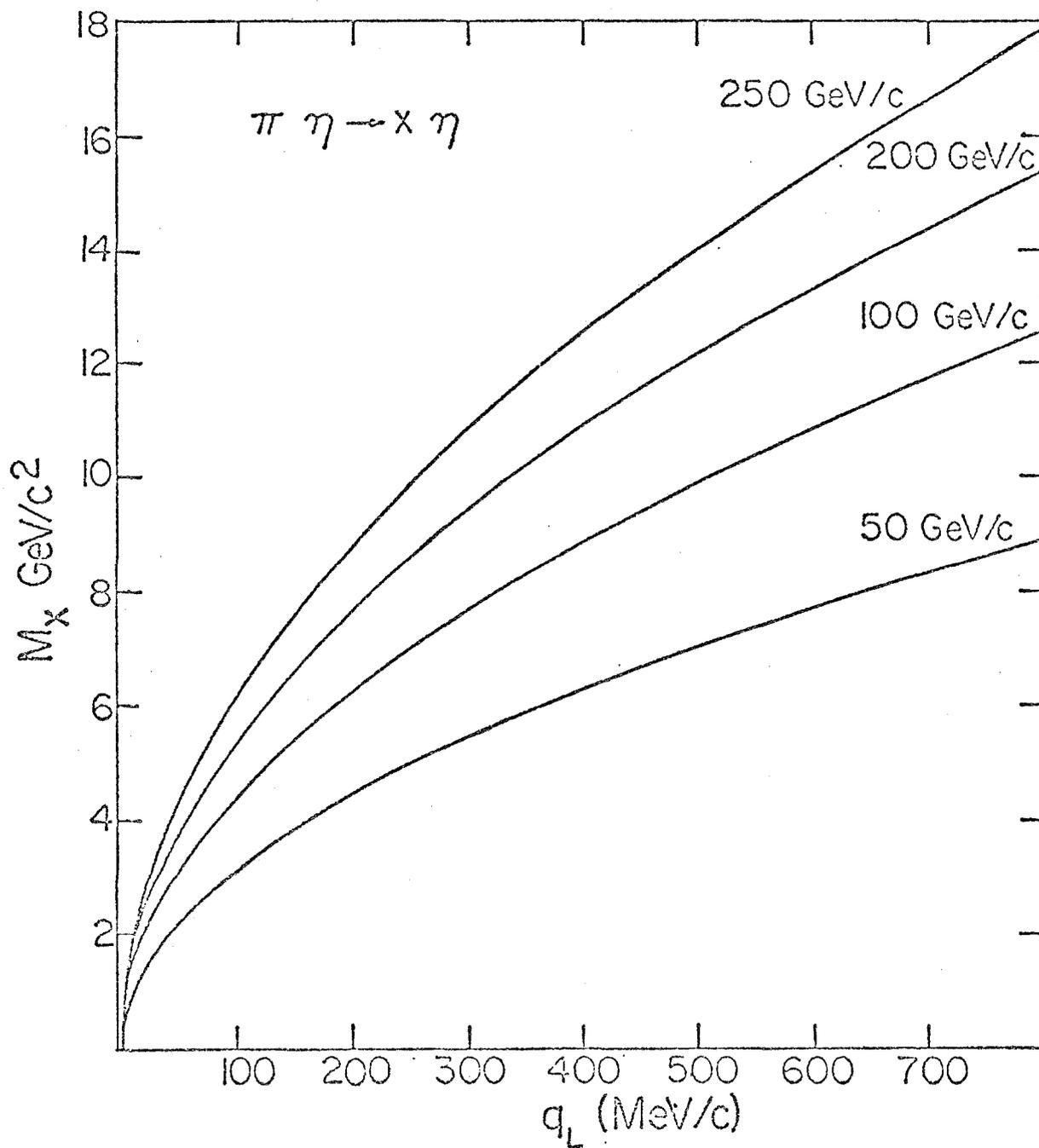


Figure 4, Minimum Momentum Transfer to the Nucleus in the dissociation of a pion into a system of mass M_x for incident momenta between 50 and 250 GeV/c .

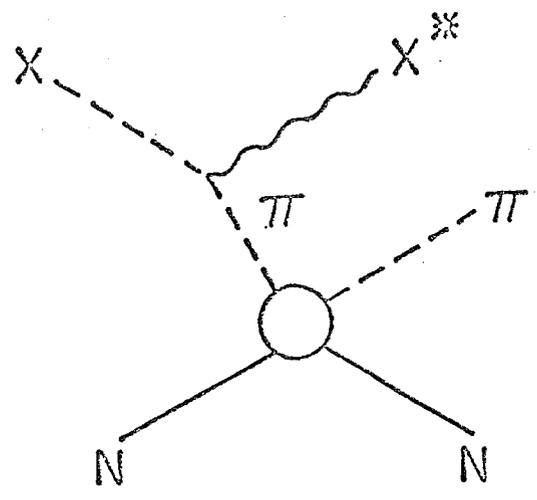


Figure 5, Diffraction Dissociation Diagram. For this case the $X \equiv \pi$, $X^* \equiv \rho$.

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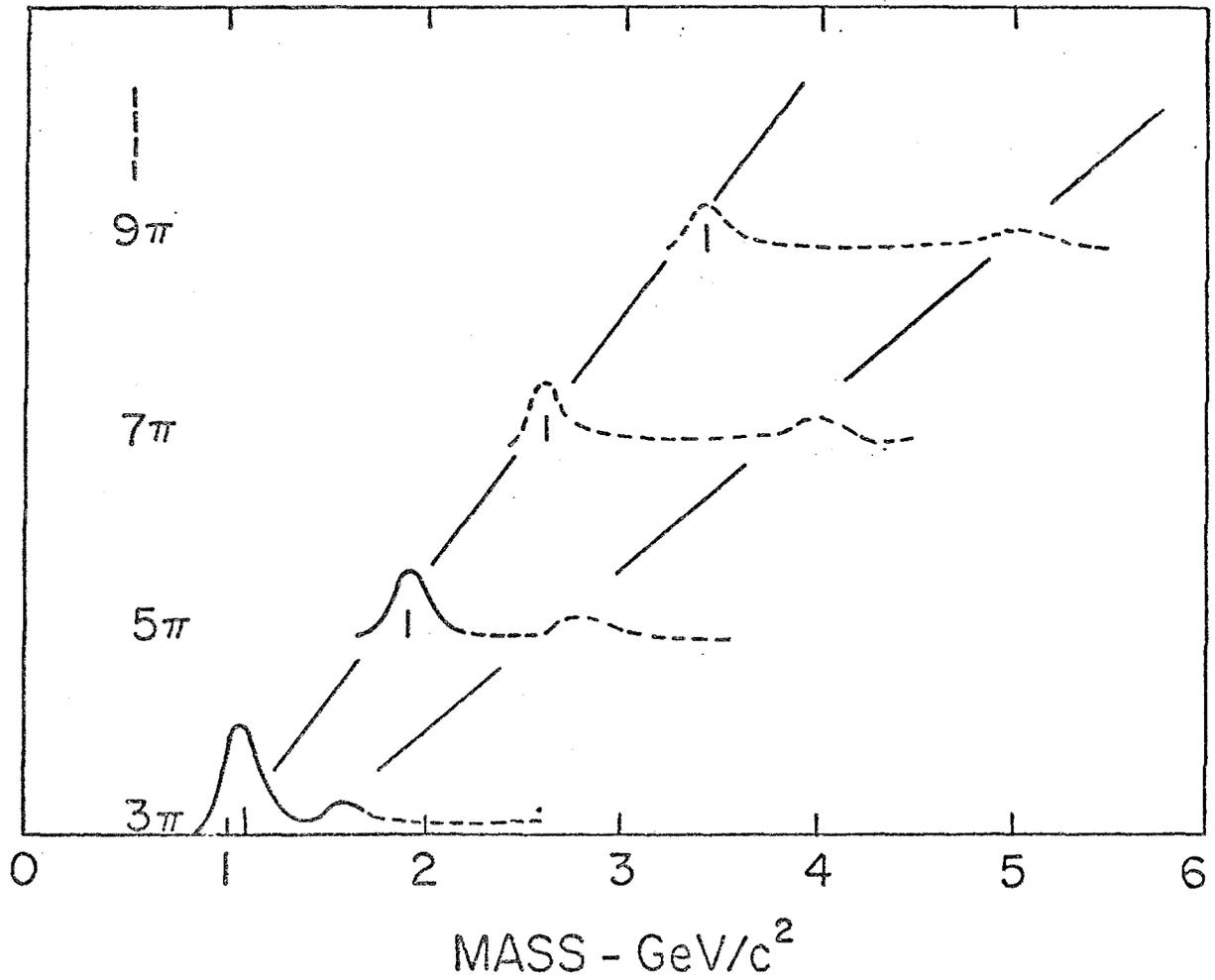


Figure 6, Mass Spectra for the various multiplicities into which a pion can dissociate. The solid curves indicate observed enhancements, while the dotted curves are predictions based on the constant Q per pion hypothesis discussed in the text.

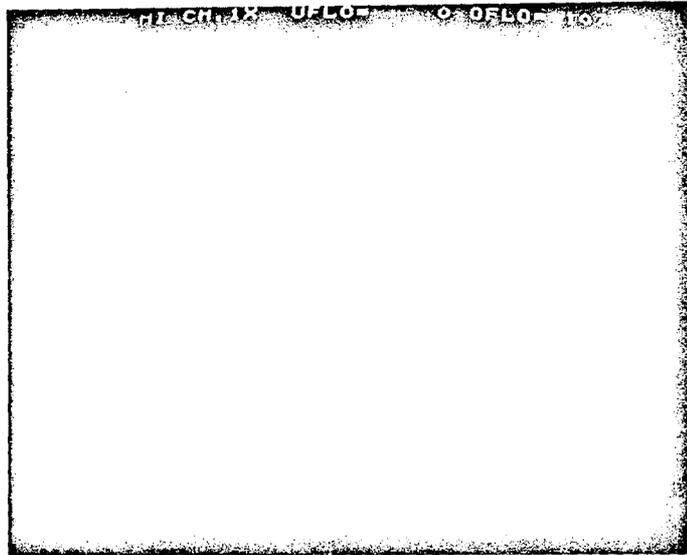


Figure 9a: On-line histogram of chamber resolution. Deviation/degree of freedom for all attempts at track fitting. Each bin represents 0.002" deviation.

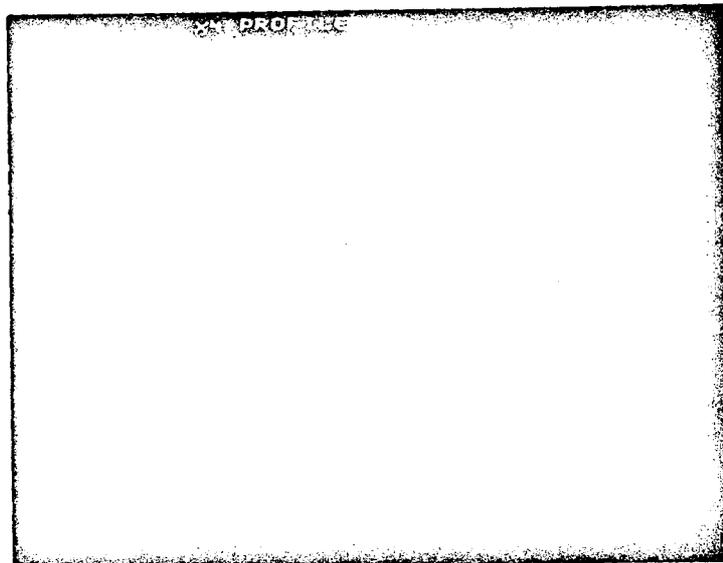


Figure 9b: On-line display of distribution of counts in the trigger hodoscope (H4) at the downstream end of the forward leg of the spectrometer.

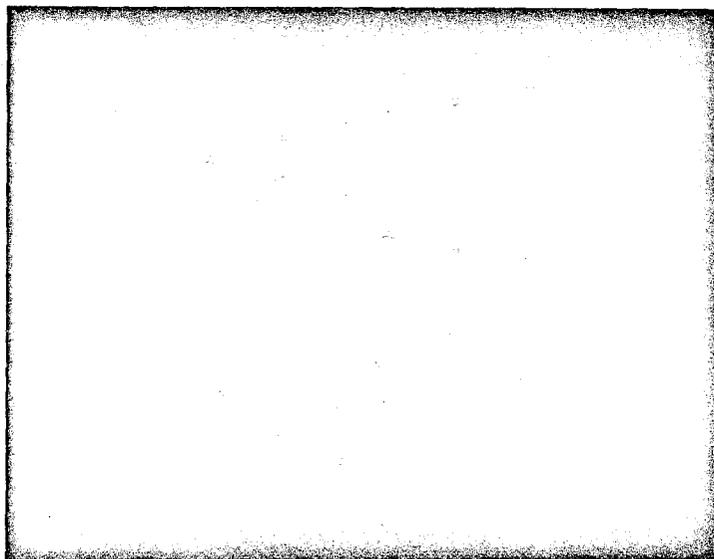


Figure 9c: On-line display of four views of a K^0 decay detected in the forward spectrometer. To the left are the views before entering the magnet, plan view at the bottom, elevation at top. To the right are similar views after the magnet. The bright, short horizontal lines represent the spark positions in the chamber gaps; the dotted lines through them are the tracks fitted by the computer. On each track in the bottom righthand view, the short vertical line representing the size of the trigger counter in hodoscope H4 struck by the pion can be seen. The vertical lines at the left of each view are rulers for calibration, representing 10 inches (total length) in all views except the lower righthand view, where the ruler is 75 inches long.

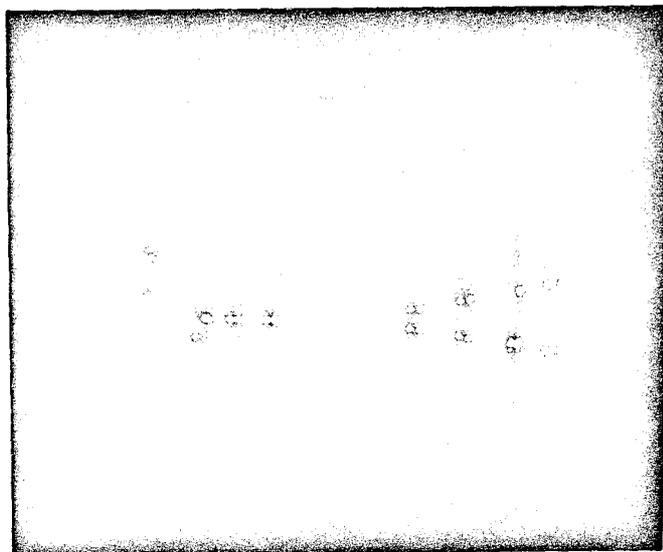


Figure 9d: On-line display of an event showing a plan view of all the chambers. The beam enters from the left. The event has a K^0 decaying after passing the first chamber of the forward arm (the opening angle is too small to be resolved on this display photograph). The decay pions are bent in opposite directions by the 48D48 magnet which is between the two sets of chambers represented by vertical lines on the plot. The last two vertical lines at the right are the trigger hodoscopes H4 and H4'. The horizontal lines represent the recoil arm chambers which have detected one large angle, low momentum track.

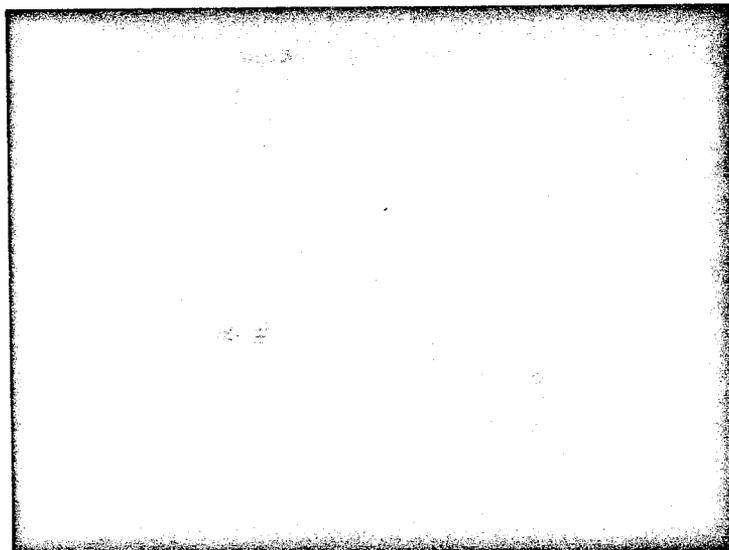


Figure 9e: Similar view to Figure 9d of an elastic scattering event used to align the recoil chambers.

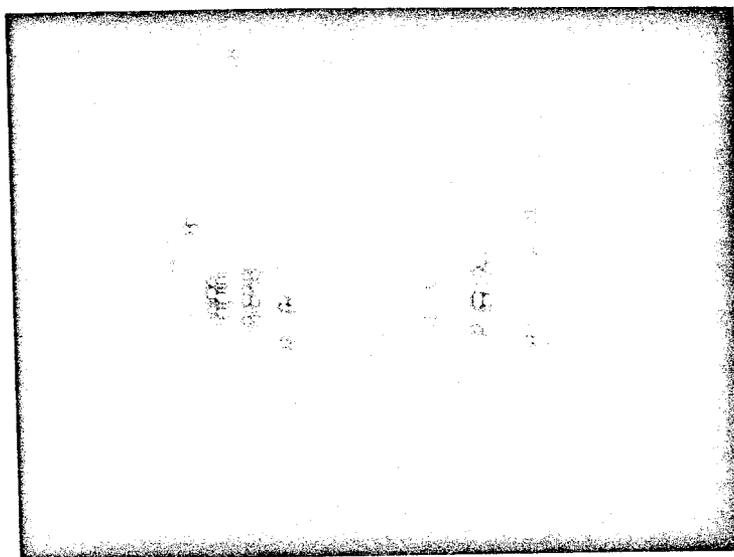


Figure 9f: A more typical picture including many old, out-of-time tracks as well as the scattering event which caused the trigger.

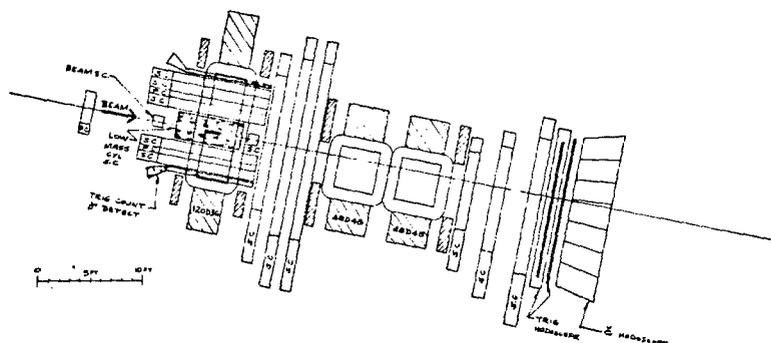


Figure 10: The proposed MK I(a) differs from the MK I in that the 120D36 is placed crosswise along the beam line, and the hydrogen target is placed inside the magnet and surrounded by digitized spark chambers and proportional chambers. The solid angle for the recoil Vee is greatly increased ($\sim 4\pi$), but the same limitations on solid angle for the forward Vee as in the MK I remain. This system is considered generally only a limited substitute for the MK I(b).

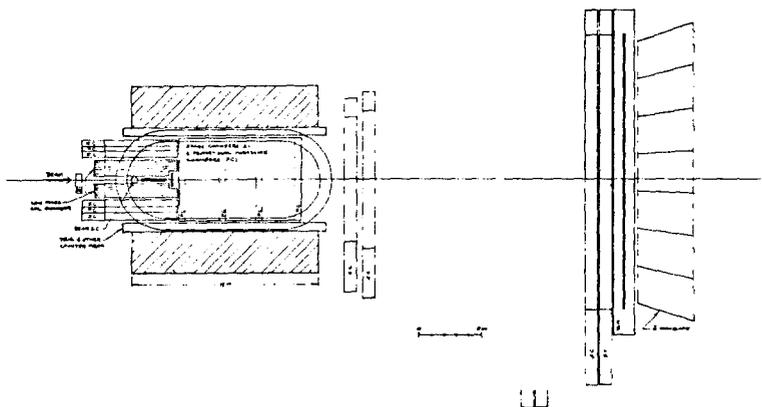


Figure 11: One of the proposed setups for the MK I(b) using the 10 kg MURA magnet, which has a field volume of about 15 feet in length, six feet of usable field width (8 feet physical width), and four feet of vertical height between the poles. The particles emerge in the forward direction and are detected by spark chambers, triggering scintillation hodoscopes (or proportional mode chambers) and Cerenkov counter hodoscopes.

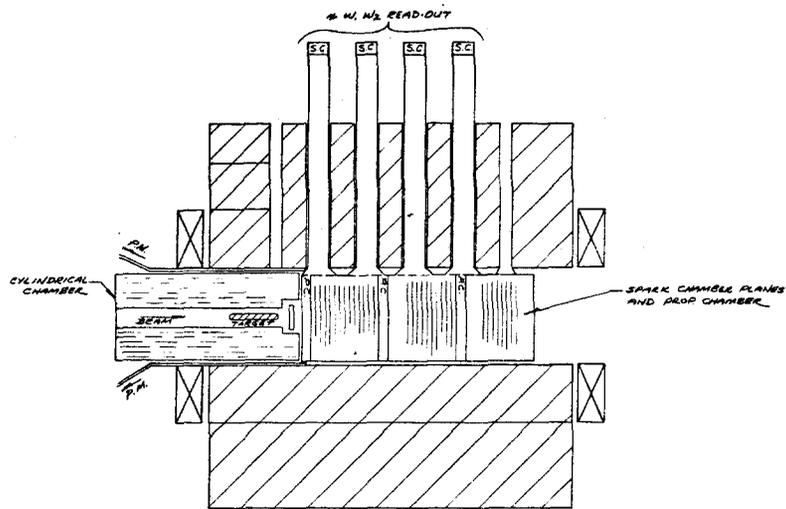


Figure 12a: The proposed MK I(b) arrangement with x , w_1 and w_2 wires being read out through the striated top.

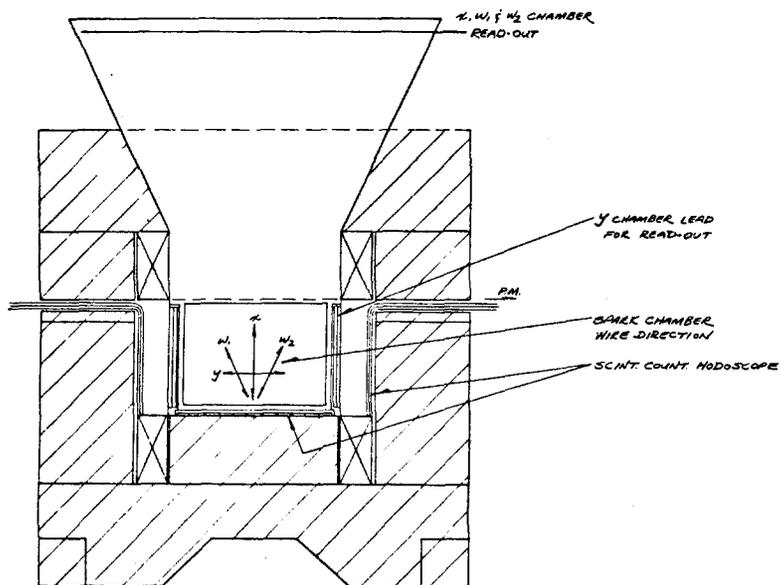


Figure 12b: An end view of the MK I(b) readout arrangement. w_1 and w_2 (45° inclined) wire planes alternate in the arrangement.

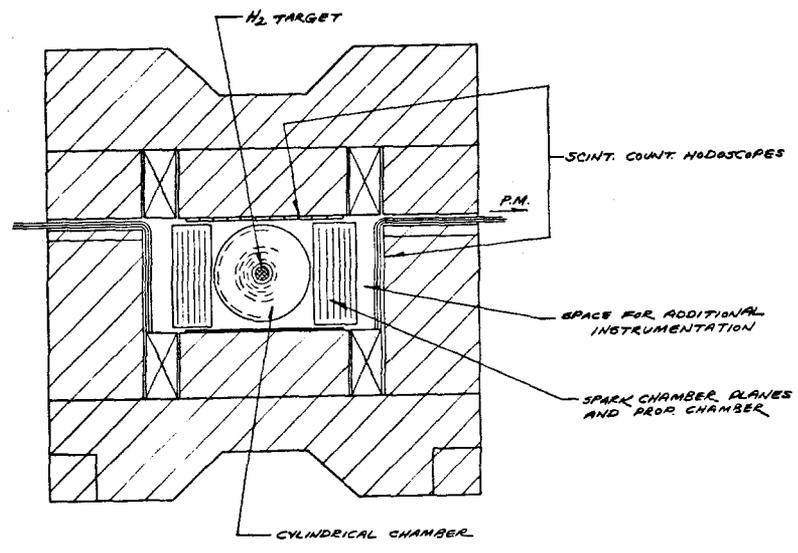


Figure 13: End view of the MK I(b).

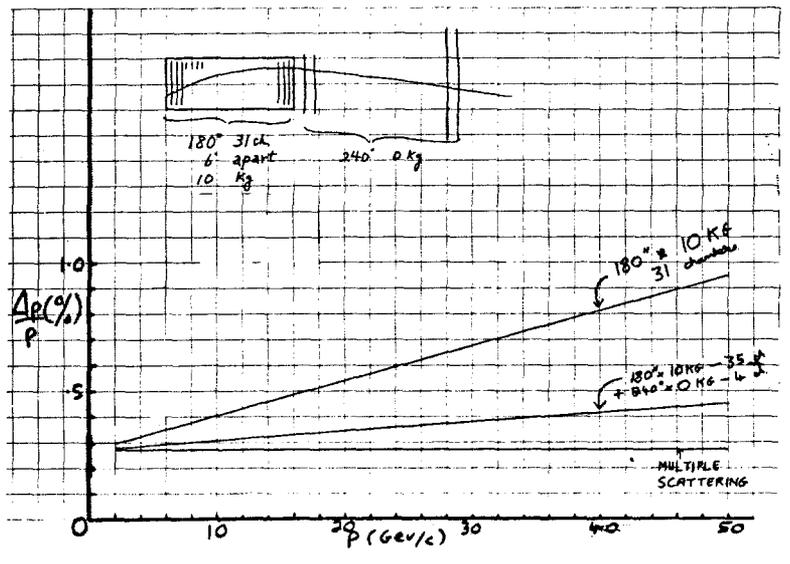


Figure 14: Momentum resolution versus momentum for MK I(b).

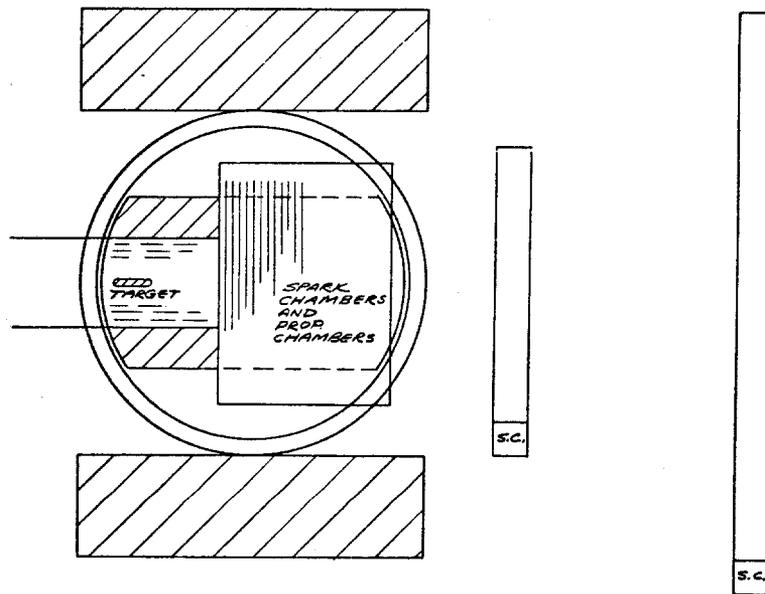


Figure 15: A proposed MK II arrangement.

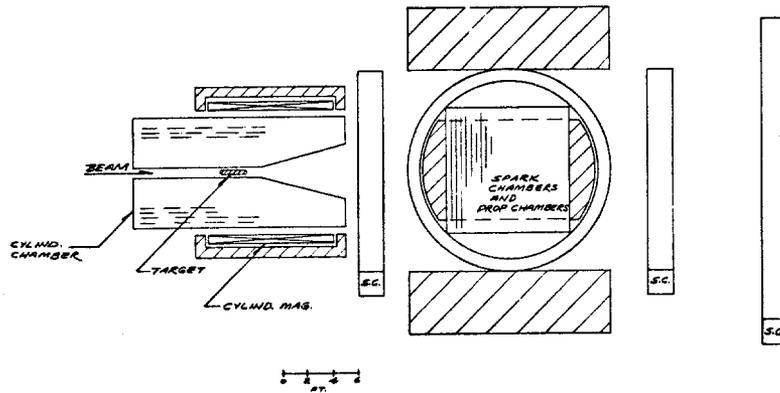


Figure 16: The MK II preceded by a cylindrical magnet (i.e., field along beam) for analyzing wide-angle particles.

DATA ACQUISITION RATES AT 15 BEV/C

Reaction	$\sigma(\mu b)$ at 15 BeV/c	Events/100 Hours	Measure angles of all Recoil Particles*	Measure Recoil Momentum + Recoil Angle*
$n^+ p \rightarrow K^0 \pi^0$	10	2×10^6	~ 25%	~ 3%
$\rho^0 \pi^0$	100	1×10^6	-----	-----
$\phi^0 \pi^0$?	$1.5 \times 10^4 \times \sigma$	-----	-----
$K^{*0} \pi^0 (\pi^0 \pi^0)$?	$1 \times 10^4 \times \sigma$		
$n^+ n^- \rightarrow K^0 \pi^0$?	$3 \times 10^3 \times \sigma$		
$K^+ p \rightarrow \bar{K}^0 \pi^0$	30	1×10^3	-----	-----
$\bar{K}^0 \pi^0$	100	1×10^4	-----	-----
$\omega^0 \Lambda$?	$2.5 \times 10^2 \times \sigma$	~ 25%	~ 3%
$\bar{p} + p \rightarrow \bar{\Lambda} + \Lambda$?	$8 \times \sigma$	~ 20%	~ 3%
$\bar{K}^0 \pi^0$?	$6 \times \sigma$	~ 20%	~ 2%
$n^+ p \rightarrow K^0 \pi^0 \pi^0 (!?)$?	$4 \times 10^2 \times \sigma$		
$\rho^0 \pi^0 \pi^0$	300	4×10^3	~ 10%	~ 3%
$\phi^0 \pi^0 \pi^0$?	$2 \times 10^3 \times \sigma$	10%	3%
$n^+ n^- \rightarrow K^0 \pi^0$?	$4 \times 10^2 \times \sigma$		
$K^+ p \rightarrow K^0 \pi^0 \pi^0$	20	1×10^3	~ 10%	~ 3%
$K^0 \pi^0 \pi^0$	50	1×10^4	~ 10%	~ 3%
$K^+ n^- \rightarrow K^0 \pi^0$	30	1×10^3	~ 60%	~ 10%
$p + p \rightarrow \pi^+ \pi^0$?	$1.5 \times 10^3 \times \sigma$	~ 10%	~ 3%

* -- Typical Value at $|t| \sim 0.3 (\text{BeV})^2$

Table I: The event rates shown are approximate estimates in events/100 hours, starting with t=0. Obviously, in experiments detecting recoil particles, there will be a minimum useable t-value typically $\sim 0.1 (\text{GeV}/c)^2$, and depending upon the t-dependence, the resultant useable rate will be accordingly reduced. The range of incident momenta available in the beam is typically 8-25 GeV/c. Obviously, the rates per μb will decrease at the lower momenta and increase at the higher momenta due to changes in detection efficiency. Suitably detailed information along these lines can be provided to users upon their written request outlining the programs they are interested in.

TABLE II

Estimated Resolutions (\sim HWHM) of MK I
(10-20 GeV/c)

Part of System	Momentum Resolution	$\Delta\theta$ in m.r.	Δ Mass (forward Vee) in MeV	Δ Mass (Baryon Recoil) in MeV
Incident Beam Detectors	$\frac{\Delta p}{p} \approx 0.2\%$	$\approx 0.3 \pm 0.1$		15-25 MeV
Forward Vee Detector	$\frac{\Delta p}{p} \approx 0.25-0.5\%$		Typically 2-4 MeV (for K^0)	25-35 MeV (estimate)
Overall Forward Vee and Beam	$\approx 0.3-0.5\%$			30-50 MeV
Wide Angle Vee	$\frac{\Delta p}{p} \sim 1$ to several %	typically several m.r.		
Overall System				15-20 MeV

RECENT THEORETICAL DEVELOPMENTS ON INCLUSIVE
DIFFRACTIVE PROCESSES

Addendum to Proposal #86

Spokesman: H. J. Lubatti
19 February 1971

SUMMARY

Recent unpublished theoretical developments by Abarbanel, Chew, Goldberger and Saunders at Princeton and DeTar, Jones, Low, Tan, Weis and Young at MIT have demonstrated the importance of studying diffraction dissociation in order to understand one of the most puzzling notions in the theory of strong interactions, namely the role of the vacuum or Pomeron coupling. In this addendum we discuss the relation of these new theoretical developments to Experiment #86 which proposes to study in a simple way diffraction dissociation of a hadron by using a helium nucleus as a target.

Recall that Experiment #86 plans to use the helium streamer chamber as a "living target"; that is, the helium gas in the chamber serves as a target as well as a detector of the recoiling helium nucleus. Measurement of momentum and angle of the recoiling helium in the chamber allows us to calculate the missing mass of the dissociated hadron system. In the original proposal we stress the significance of studying the states into which a pion dissociates. We still feel that it is an important part of our experiment; however, what we wish to discuss in this addendum is a slightly different region of the missing mass spectrum which we obtain automatically: namely, the high missing mass region where there should be no resonant structure. It is this region which the above theorists have studied in great detail. In particular they have found that the interesting quantity to measure is the differential cross section $d\sigma/dt ds'$ for the inclusive reaction $\pi + He \rightarrow \text{anything} + He$, where s' is the mass squared of the hadron system labeled above by "anything".

We emphasize that these new theoretical ideas involve data in a kinematic region that was already covered in the experiment already proposed. Therefore, we are not discussing any change in the experimental apparatus or running time, but rather the heightened interest in a part of the data we shall obtain. In fact, the inclusive cross section is the easiest part of the experiment to analyze, since it does not require any information about the multiplicity of the fast particles. We need only measure the He recoil and calculate a missing mass.

In the following we discuss the importance of diffraction dissociation and summarize the new theoretical developments.

DETAILED DISCUSSION

Diffraction processes, which have long played a prominent role in elementary particle physics are the most simple processes to study, but at the same time they are among the most difficult and challenging phenomena which we have encountered. In attempting to explain such phenomena in terms of exchange models, we have been forced to the concept of the vacuum exchange or, in the Regge model language, the exchange of the Pomeron trajectory. Such a concept, while preserving the basic ideas inherent in the exchange model, presents some difficulties. The chief problem has been that while other trajectories all have known particles lying on them, there has not yet been observed a particle which unambiguously can be associated with the Pomeron trajectory. In addition, the original conjecture that $\alpha_{\text{Pomeron}}(0)$ is equal to 1, never has been adequately tested in the energy range available at existing accelerators.

Experimentally, we can define a diffractive process as one in which no internal quantum numbers (B, Y, T, G, and $\sigma = (-1)^{J-P}$) are exchanged. This simply means that for the process $1 + 2 \rightarrow 3 + 4$ particle, 1(2) and 3(4) have the same internal quantum numbers. Elastic scattering is an obvious example of such a process. Another example of such a process is $p + p \rightarrow p + N^*$, where the N^* 's are the $T = \frac{1}{2}$ isobars. Another example which has been observed is the production of the A_1 and Q mesons. All of the data which have been obtained at existing accelerator energies have merely served to wet our appetite about the true nature of the diffractive process. The amazing result that an inelastic diffractive cross section remains constant with energy suggests that at NAL energies diffraction dissociation should become an important if not the most important phenomenon in strong interactions.

Recent theoretical work by Chew, Abarbanel, Goldberger and Saunders at Princeton ¹⁾, and DeTar, Jones, Low, Tan, Young and Weis ²⁾ at MIT has given considerable insight into the question of diffraction dissociation. The crucial observation of the Princeton group has been that in order to better understand the vacuum coupling one

should study inclusive diffraction dissociation reactions, and not quasi-two-body processes. The importance of this observation is greatly enhanced by the fact that experimentally it is much simpler to study inclusive reactions than it is to try to pick out specific quasi-two-body channels. Now, in fact, we know that all of the quasi-two-body production data which we have accumulated in the past ten years has served only as an indication that there is validity to the exchange model, but has not given us any profound insight into the theory of strong interactions. What we have learned is that at higher energies quasi-two-body processes become less important because of the $1/s^n$ dependence; with the exception, of course, of those processes which are diffractive.

The particular theoretical process which has been studied in detail by the Princeton theorists has been $A + \text{target} \rightarrow \text{anything} + \text{target}$, where A is a high energy hadron. The only requirement for the target is that it simply take up the recoil momentum necessary for conservation of energy when the incident particle changes its mass to some effective $M^2 \equiv s'$. Diagrammatically, this is demonstrated in Figure 1. Since precisely this process is mediated by the Pomeron exchange, it is quite obvious that a detailed study of such a process will serve as a test for any theoretical model which purports to study diffractive processes. The Princeton theorists have

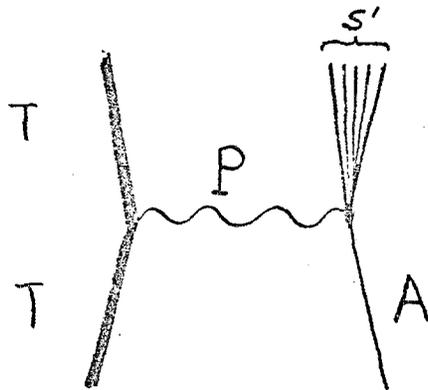


Figure 1

been able to relate this process to a fundamental notion in the theory of strong interactions, namely that of the three Pomeron vertex. Such ideas have also been discussed by Gribov³⁾ and others, but the more recent work of Abarbanel, Chew, Goldberger and Saunders¹⁾ makes explicit statements about what one should expect from such inclusive reactions and their profound relevance to the theory of strong interactions. The salient result found by these workers is that the inclusive diffraction dissociation cross section at large missing masses (i.e., large s' in Figure 1) is proportional to $\sqrt{1 - \alpha_P(0)}$. Therefore, in this experiment where we are measuring the cross section for the reaction $\pi + \text{He} \rightarrow \text{anything} + \text{He}$, we are measuring $\alpha_P(0)$. It is this fact which I have referred to as an amazing discovery because heretofore the only way we thought we could learn something about the intercept of the Pomeron at $t = 0$ was to study the energy dependence of the total cross sections, and since we expect that $1 - \alpha_P(0)$ is of the order of 0.01 or smaller, we would have to observe an energy dependence of the total cross sections which goes as $1/s^{(0.01)}$. Needless to say, such an experiment would require extraordinarily precise cross section measurements with extremely fine granularity in energy; however, since in the inclusive $\pi + \text{He}$ reaction we measure the square root of $1 - \alpha_P(0)$; a 1% effect in the total cross section becomes a 10% effect in this experiment. In the following we give a summary of the relevant formalism developed by the Princeton group.

The theoretical developments alluded to above have demonstrated that in the collision shown in Figure 1, taking target $\Xi \equiv \text{He}$ and $A \equiv \pi$, the cross section can be asymptotically represented by

$$s^2 \frac{d\sigma}{ds'dt} \underset{\text{large}}{\sim} \frac{1}{16\pi} \left| \beta_{\text{HeP}}(t) \right|^2 \beta_{\pi\text{P}}(0) g_{\text{PPP}}(t) (s')^{\alpha_P(0)} \left(\frac{s}{s'}\right)^{2\alpha_P(t)}. \quad (1)$$

The normalization of the vertex factors is such that $\pi + \text{He} \rightarrow \pi + \text{He}$ has the asymptotic form

$$s^2 \frac{d\sigma_{\pi\text{He}}}{dt} \underset{s \text{ large}}{\sim} \frac{1}{16\pi} \left| \beta_{\text{HeP}}(t) \right|^2 \left| \beta_{\pi\text{P}}(t) \right|^2 s^{2\alpha_P(t)}. \quad (2)$$

The quantity $g_{PPP}(t)$ is the triple Pomeranchuk vertex function, and it is this quantity which Chew feels is of central importance in the theory of strong interactions ¹⁾. In particular, the Princeton theorists show that

$$\eta_P \equiv \frac{1}{16\pi} \frac{1}{2\alpha'(0)} [g_{PPP}(0)]^2 \leq 1 - \alpha_P(0) . \quad (3)$$

If we integrate over t and then normalize Eq. (1) to the elastic cross section Eq. (2), we find the following relationships

$$\frac{1}{\sigma_{el}} \frac{d\sigma}{d\ln s'} (s', \sim s/s') \underset{\text{large}}{\sim} \frac{g_{PPP}(0)}{\sqrt{\sigma_{\pi\pi}}} = \sqrt{\frac{16\pi(2\alpha')\eta_P}{\sigma_{\pi\pi}}} . \quad (4)$$

Therefore, we can estimate the experimental effect we would observe by taking η_P to be of the order of 0.01 and $\alpha' \approx \frac{1}{2}$; $\sigma_{\pi\pi}$ is known to be approximately 15 mb. We find that

$$\frac{1}{\sigma_{el}} \frac{d\sigma}{d\ln s'} \approx 0.1 \dots \quad (5)$$

We have also calculated, using the Glauber model, the elastic π He cross section to be about 11 mb at 100 GeV/c; hence, we expect $d\sigma/d\ln s'$ to be of the order of 1 mb, which is easily detectable in our experiment. In fact, in our recent supplement to the proposal, which dealt with triggering rates, we estimated conservatively the total π He coherent production cross section to be 3 mb. Thus, the result in Eq. (5) is not unreasonable, since our 3 mb estimate also included resonant structure in the s' mass distribution. What Chew and co-workers are calculating is applicable to large s' where the resonant structure has damped out.

Note that if $g_{PPP}(0) = 0$ then we would observe a decrease of (or absence?) of events at large s' . This, in itself, would be an important discovery. For example such a result would exclude certain proposals which have been made about the Pomeranchuk trajectory ⁴⁾.

Even more significant will be a study $g_{PPP}(t)$ as a function of t . We will be able to measure the momentum of the He recoil to approximately 2 MeV/c (recall that the He stops in the chamber), and hence we will have precise momentum transfer distributions at small values of t .

We remind the reader that the above theoretical predictions apply only to the region of large s' . In the resonance region (small s') we will apply the analysis we have discussed in detail in the proposal.

It is to be noted that because the above theoretical arguments stress small momentum transfers, the nuclear form factor which restricts us to small t values makes the nucleus a better target than a nucleon. For example, we expect the He form factor to give us approximately an e^{40t} dependence in momentum transfer, while a nucleon gives an e^{10t} dependence. Another important point is that the above arguments do not depend on the exact nature of the incident particle, only that it be a hadron. Hence, protons will be as interesting as pions, and the final choice of beam particle should best be left to the convenience of the scheduling committee, although we confess to having a historical preference for pions.

In conclusion, this simple experiment measures a profoundly important quantity, namely the diffraction dissociation cross section of a hadron dissociating into anything. This cross section has already been related to η_p which measures the strength of the three Pomeron coupling which in turn is related to the intercept of the Pomeron trajectory at $t = 0$, and is therefore a parameter of central importance in the theory of strong interactions. Because such measurements require that both s and s/s' be large, it is necessary to perform these experiments at NAL. We stress once more the enormous role which diffractive processes play in the understanding of strong interactions. Therefore, we feel that an experiment which is simple in nature and can give results which are relevant to new, exciting theoretical ideas should be done as soon as possible.

References

- 1) Private communication from G. F. Chew. At present these results exist only in handwritten manuscript; however, Chew has offered to discuss this with the NAL committee if necessary.
- 2) C.E. DeTar, C.E. Jones, F.E. Low, J.H. Weis, J.E. Young and Chung-I Tan, "Helicity Poles, Triple Regge Behavior and Single Particle Spectra in High Energy Collisions". MIT Preprint.
- 3) V.N. Gribov and A.A. Migdal, Sov. J. Nucl. Phys. 8, 1002 (1968).
V.N. Gribov and A.A. Migdal, Sov. Phys.—JETP, 28, 784 (1968).
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