## FIXED TARGET EXPERIMENTS AT THE FERMILAB TEVATRON

Gaston Gutierrez

Fermi National Accelerator Laboratory Batavia, Illinois, 60510, United States of America gaston@fnal.gov

Marco A. Reyes

Physics Department, University of Guanajuato Leon, Guanajuato, 37150, Mexico marco@fisica.ugto.mx

> Received 30 June 2014 Revised 30 July 2014

This paper presents a review of the study of Exclusive Central Production at a Center of Mass energy of  $\sqrt{s} = 40$  GeV at the Fermilab Fixed Target program. In all reactions reviewed in this paper, protons with an energy of 800 GeV were extracted from the Tevatron accelerator at Fermilab and directed to a Liquid Hydrogen target. The states reviewed include  $\pi^+\pi^-$ ,  $K_s^0K_s^0$ ,  $K_s^0K^\pm\pi^\mp$ ,  $\phi\phi$  and  $D^{*\pm}$ . Partial Wave Analysis results will be presented on the light states but only the cross-section will be reviewed in the diffractive production of  $D^{*\pm}$ .

Keywords: Glueballs; Exotics; Double Pomeron Exchange.

PACS numbers: 12.39.Mk, 14.40.Rt, 11.80.Et, 14.40.Be, 14.40.Lb, 13.85.Ni

## 1. Introduction

The Double Pomeron Exchange (DPE) process was first observed at the CERN-ISR.<sup>1</sup> Since then it is generally accepted that Central Production in hadronhadron reactions at high center-of-mass (CM) and low momentum transfers proceeds through DPE. It is also generally accepted that with its vacuum quantum numbers, the Pomeron is largely gluonic in nature. Then proton-proton reactions, where the central object under study is well separated in rapidity from the protons, could be a good place to search for gluonium states. In this paper, we review reactions of the type:

$$p_{beam} + p_{tgt} \to p_s\left(X\right)p_f \tag{1}$$

where the subscripts s and f refer to the slowest and fastest protons in the Laboratory reference frame.

The Fixed Target (FT) program at the Fermilab Tevatron has produced a wealth of results,<sup>2</sup> but only experiment E690 used an 800 GeV/c proton beam on a Liquid Hydrogen target and had a beam spectrometer capable of a precise measurement of

### 2 G. Gutierrez, M.A. Reyes

the forward proton, making this the only experiment in the Fermilab FT program that studied reactions of the type (1) above. In this paper we review the main results of experiment E690 in the production of  $\pi^+\pi^-$ ,  $K_s^0 K_s^0$ ,  $K_s^0 K^{\pm}\pi^{\mp}$ ,  $\phi\phi$ , and the diffractive production of  $D^{*\pm}$ .

## 2. The E690 experiment

The E690 experiment consisted of an 800 GeV/c proton beam hitting a liquid hydrogen  $(LH_2)$  target. A high rate, open geometry multiparticle spectrometer, shown in Fig. 1, followed the hydrogen target. A beam spectrometer was used to accurately measure the 800 GeV/c beam and the scattered proton. Details of the spectrometer can be found in Ref. 3.



Fig. 1. The E690 main Spectrometer.

All final states reviewed in this paper were subject to the following event selection:

- a primary interaction vertex within the fiducial region of the LH<sub>2</sub> target,
- a number of charged tracks consistent with the desired topology,
- a number of secondary vertexes also consistent with the desired topology,
- a fast proton,  $p_f$ , measured in the forward spectrometer.

For Central Production and low  $p_t$  the slow proton  $p_s$  often stays within the LH<sub>2</sub> target. Therefore E690 required that  $p_s$  would not be reconstructed in the main spectrometer and the missing mass squared of the event  $(M_{miss}^2)$  was used to identify this proton by requiring that  $M_{miss}^2$  would agree with the mass squared of the proton. Other selection criteria pertinent to particular final states are discussed in each section below.

# 3. Central production of the $\pi^+\pi^-$ system

In order to select events according to reaction 1 with  $X \to \pi^+\pi^-$ , experiment E690 required,<sup>4,5</sup> in addition to the protons, two charged tracks attached to the primary vertex, both of them with Čerenkov identities compatible with being pions; the missing proton longitudinal momentum was required to be  $|p_l| < 1.0 \text{GeV/c}$ , and a rapidity difference between the missing proton and either pion greater than 1.8 rapidity units to avoid  $\Delta^{++}$  contamination. To select centrally produced events, the Feynman  $x_F$  of the X system was required to be between  $-0.1 < x_F < 0.0$ . The transverse momentum of both scattered protons was required to be  $p_t^2 < 0.1 (\text{GeV/c})^2$ , to enhance S-wave dominance in the selected events. The  $\pi^+\pi^-$  invariant mass distribution for the selected events is shown in Fig. 2.



Fig. 2. Left panel:  $\pi^+\pi^-$  invariant mass distribution for events with  $p_{t,s}^2 < 0.1 (\text{GeV/c})^2$  (solid line) and with both  $p_{t,s}^2$  and  $p_{t,f}^2 < 0.1 (\text{GeV/c})^2$  (dashed line). Center panel: same plot as in the left panel but with a different mass scale. Right panel: same  $\pi^+\pi^-$  invariant mass distribution without the selection in  $p_{t,f}$  to show the presence of the  $f_2(1270)$  resonance; the dashed line includes the  $x_F$  selection the solid line does not.

A Partial Wave Analysis (PWA) was performed following the method described by Chung and Trueman.<sup>6</sup> The reflectivity basis was used for the analysis, with eigenvectors defined in the Gottfried-Jackson (GJ) frame. In the rest frame of the X system, E690 defined the GJ frame with the z-axis in the direction of the momentum transfer of the beam proton, with the y-axis perpendicular to the plane defined by the momentum transfers in the overall CM, and the x-axis defined as in a right handed coordinate system. Only the amplitudes with  $l \leq 2$  and  $m \leq 1$  were used in the analysis:

$$S_0^- = Y_0^0, \quad P_0^- = Y_1^0, \quad D_0^- = Y_2^0$$

$$P_1^{\pm} = \left(Y_1^1 \pm Y_1^{-1}\right) / \sqrt{2}, \quad D_1^{\pm} = \left(Y_2^1 \pm Y_2^{-1}\right) / \sqrt{2}$$
(2)

The assumption of S-wave dominance near threshold is sufficient to select a single, continuous solution throughout the considered mass spectrum, from threshold to 1.5 GeV/c<sup>2</sup>, for events with both  $p_t^2 < 0.1$  (GeV/c)<sup>2</sup>. The  $S_0$  and  $D_0$  waves are

## 4 G.Gutierrez, M.A.Reyes



Fig. 3.  $|S|^2$  and  $|D_0|^2$  wave intensities as a function of the  $\pi^+\pi^-$  invariant mass measured in the final PWA analysis.

plotted in Fig.3. The  $D_+$ -wave contribution is about the same as the  $D_0$  one, and the  $D_-$ -wave contribution is essentially zero. All P-wave contributions are negligible, as expected from double Pomeron exchange. When the low transverse momentum selection on the fast proton is removed a significant D-wave contribution is observed above 1 GeV/c<sup>2</sup> due to the production of the  $f_2(1270)$  (see Right panel in Fig. 2).

The dotted lines on the left and center plots in Figure 2 and the data points on the left plot in Fig. 3 show two prominent drops in the  $\pi^+\pi^-$  invariant mass spectrum. The sharp drop at 1 GeV/c<sup>2</sup> was first explained by Morgan and Pennington<sup>7</sup> as the interference of the  $f_0(980)$  with a background that has a phase of about 90 degrees at 1 GeV/c<sup>2</sup>. The second drop at 1.5 GeV/c<sup>2</sup> is due to the interference of the same background with the  $f_0(1500)$ . These same interference effects are observed in  $\pi\pi$  elastic scattering (for a review see the  $\pi\pi$  scattering section Ref. 8). No other features are observed in the *S*-wave spectrum, for example there is essentially no evidence for the  $f_0(1370)$  or the  $f_0(1710)$ .

# 4. Central production of the $K_s^0 K_s^0$ system

The event selection for the decay  $X \to K_s^0 K_s^0$  included two secondary vertices with a tight  $K_s^0$  invariant mass. The background under the  $K_s^0$  invariant mass peak was so small that no direct particle identification was needed.<sup>9</sup> For every event the difference in rapidity between  $p_s$  and the  $K_s^0 K_s^0$  system was required to be larger than 1.2 units. For  $p_f$  this difference was larger that 3.7 units.

The left panel in Fig. 4 shows the  $K_s^0 K_s^0$  invariant mass between threshold and 3 GeV/c<sup>2</sup>. This mass distribution is smooth beyond 2 GeV/c<sup>2</sup>, with no evidence of the narrow  $f_J(2220)$  state seen by the BES Collaboration.<sup>10,11</sup> The right panel in the same figure shows the rapidity distributions for  $p_s$ ,  $K_s^0 K_s^0$  and  $p_f$ .

A PWA analysis of the 11182 selected events was performed in bins of the  $K_s^0 K_s^0$  invariant mass for events in the range  $-0.22 \leq x_F(X) \leq -0.02$ , integrating over  $p_{t,s}^2$ ,  $p_{t,f}^2$ , and  $\delta$ , the angle between the scattered protons in the  $K_s^0 K_s^0$  CM. Using the reflectivity basis for this parity conserving system, the wave amplitudes



Fig. 4. Left panel:  $K_s^0 K_s^0$  invariant mass distribution after the final event selection. Right panel: Rapidity distributions for the slow proton, the  $K_s^0 K_s^0$  system, and the fast proton.

used were  $S_0^-$ ,  $D_0^-$ ,  $D_1^-$  and  $D_1^+$  (see Eq. 2). Only (even)<sup>++</sup> waves are allowed in the  $K_s^0 K_s^0$  system.<sup>12</sup> E690 performed the partial wave analysis maximizing the extended likelihood with respect to the four wave moduli and the two relative phases  $\phi(D_0^-) - \phi(S_0^-)$  and  $\phi(D_1^-) - \phi(S_0^-)$ .

Using the above four waves there are two solutions for every mass bin. These solutions can be continued from one bin to the next as long as they do not cross. This problem can be expressed in terms of Barrelet zeros,<sup>13</sup> when a zero crosses the real axis the solution bifurcates. In the E690 analysis one of the two Barrelet zeros becomes real at 1.55 GeV/c<sup>2</sup> producing a bifurcation point. At threshold the  $K_s^0 K_s^0$  cross section is dominated by the  $f_0(980)$  resonance, so before the bifurcation point E690 eliminated the solution with a small contribution of S wave near threshold. Of the two solutions after the bifurcation point, one is mainly S wave and the other mainly D wave. These two solutions are shown in Fig. 5.

Three main features are observed before the bifurcation point: (i) the well established  $f_0(1500)$  is clearly seen, (ii) the  $f_2(1270)$  is observed in the *D* wave amplitude, and (iii) there is no evidence of the  $f_0(1370)$ . After the bifurcation point E690 could not determine the spin of the so-called  $f_J(1710)$ . In a similar PWA analysis in  $K^+K^-$  and  $K_s^0K_s^0$ , WA102 later favored the spin-0 interpretation of the  $f_J(1710)$ .<sup>14</sup>

The classification of the scalar mesons has not yet been resolved. The most commonly accepted interpretation is that there are two  $q\bar{q}$  meson resonances in the region between 1300 MeV/c<sup>2</sup> and 1900 MeV/c<sup>2</sup>, and that the three observed states  $f_0(1370)$ ,  $f_0(1500)$  and  $f_0(1710)$  are a mixture of those two  $q\bar{q}$  states and the lowest mass scalar glueball.<sup>8,14</sup> However, E690 did not find evidence of a scalar resonance in the region of the  $f_0(1370)$  in either the  $\pi^+\pi^-$  or the  $K_s^0K_s^0$  systems. This result is in agreement with the absence of the  $f_0(1370)$  in  $\pi\pi$  elastic scattering.<sup>8</sup>

## $6 \quad G. Gutierrez, \ M.A. Reyes$



Fig. 5. Results of the PWA analysis on the  $K_s^0 K_s^0$  system. The plots on the left (right) show  $|S|^2$   $(|D|^2)$  as a function of the  $K_s^0 K_s^0$  invariant mass. As explained in the text there is a bifurcation point at 1.55 GeV/c<sup>2</sup> giving rise to two solutions. The upper (lower) plots show the solution with the largest contribution of S(D) wave after the bifurcation point.

# 5. Central production of the $K_s^0 K^{\pm} \pi^{\mp}$ system

In order to study reaction 1 with  $X \to K_s^0 K^{\pm} \pi^{\mp}$ , experiment E690 selected events where the central cluster consisted of one positive track, one negative track, and a  $K_s^{0,16}$  At least one of the two charged tracks was required to be identified by the Čerenkov counter as either a  $\pi$ , or an ambiguous K/p, and the other track was required to have an identity compatible with the final state. In all selected events, the forward proton,  $p_f$ , was separated from the central mesons by at least 3.5 units of rapidity. A minimum gap of 1.8 units of rapidity was required between each individual meson and  $p_s$  to ensure that there was no contamination of the final state from reactions in which  $p_s$  would be a decay product of a baryon resonance, such as  $\Delta^{++}$  or  $\Lambda(1520)$ . Finally, in order to ensure near uniform acceptance, the  $x_F$  of the meson system was required to be in the range [-0.15, -0.02].

The  $K\bar{K}\pi$  invariant mass distribution for both charge states is shown in Fig. 6. The first peak is easily identified by its mass and width as the  $f_1(1285)$ , and the second peak is nowadays identified as the  $f_1(1420)$  meson. At the time of the E690 publication<sup>16</sup> there were disagreements as to whether this second peak corresponded to the  $f_1(1420)$  state,<sup>17–19</sup> or to a 0<sup>-+</sup> state decaying to  $a_0\pi$  that had been seen in  $K^-p$  interactions.<sup>20</sup> This ambiguity was known as the  $E/\iota$  puzzle.<sup>11,21</sup>

The Dalitz plots in the  $f_1(1420)$  region are shown in the left panel of Fig. 7 for the data, and the Monte Carlo for several different waves. Just by inspection of these plots it is easy to see that the data matches the  $1^{++}K^*K$  simulation very



Fig. 6.  $K_s^0 K^+ \pi^-$  and  $K_s^0 K^- \pi^+$  invariant mass distributions after final event selection.



Fig. 7. Left panel:  $K_s^0 K^+ \pi^-$  Dalitz plots for the data and several MC waves in the  $f_1(1420)$  region. Right panel: results of the PWA analysis on the  $K_s^0 K^+ \pi^-$  final state. The other charge state gives the same results.<sup>16</sup>

well. To assess if there are small amounts of other waves, E690 performed a PWA analysis between threshold and 1.6 GeV/c<sup>2</sup>.<sup>16</sup> The results, shown in the right panel in Fig. 7, clearly demonstrated that only 1<sup>++</sup> waves were needed to describe the data, confirming that pseudoscalar states were not seen in central production,<sup>17</sup> and solving the  $E/\iota$  puzzle.

## 6. Central production of the $\phi\phi$ system

The first observation of the OZI<sup>22</sup> suppressed reaction  $\pi^- p \rightarrow \phi \phi n$ , was made using the BNL–MPS spectrometer.<sup>23</sup> A subsequent PWA analysis on a larger data sample showed that three 2<sup>++</sup> states were necessary to fit the data.<sup>24</sup> Fermilab FT experiment E623 measured the  $\phi \phi$  cross section in the reaction  $pN \rightarrow \phi \phi X$  but

## 8 G.Gutierrez, M.A.Reyes

did not perform a PWA analysis.<sup>25</sup> Given the OZI suppression the  $\phi\phi$  channel is believed to be a good place to look for the production of glueballs.



Fig. 8. Left panel: The  $K^+K^-$  invariant mass when the other  $K^+K^-$  pair lay in the  $\phi$  mass region. Right panel:  $\phi\phi$  invariant mass distributions for the selected events.

E690 measured the Central Production of  $\phi\phi$  in reaction 1 with  $X \to \phi\phi$ and  $\phi \to K^+K^-$ ,<sup>26</sup> selecting events with four charged tracks coming from the primary vertex, in addition to the diffracted proton. The tracks were required to have Čerenkov information compatible with being kaons, and at least one of them identified as not being a pion. A kinematic cut on the missing momentum  $p_z < 250 \text{ MeV/c}$  or  $\arctan(p_t/p_z) > 45$  degrees ensured that the missing proton was outside of the detector's geometrical acceptance. The  $\phi$  mass region was defined as  $1.0124 < m(K^+K^-) < 1.0264 \text{ GeV/c}^2$ . The  $K^+K^-$  and  $\phi\phi$  invariant mass distributions for the selected events are shown in Fig. 8.

E690 performed a PWA analysis of the  $\phi\phi$  system using states defined in terms of the total angular momentum J, orbital angular momentum L, parity P and exchange reflectivity  $\eta$ :

$$G^{J^{P}LSM^{\eta}}(\gamma,\beta,\alpha_{1},\alpha_{2},\theta_{1},\theta_{2}) = \operatorname{Real}\left[\frac{(1-i)-\eta(1+i)}{2}\sum_{\mu,\lambda}C(1,1,S|\mu,-\lambda)\times c(l,s,j|0,\mu-\lambda)e^{-iM\gamma}e^{i\mu\alpha_{1}}e^{i\lambda\alpha_{2}}d^{J}_{M,\mu-\lambda}(\beta)d^{1}_{\mu,0}(\theta_{1})d^{1}_{\lambda,0}(\theta_{2})\right]$$
(3)

where  $M = |J_z|$ .  $\gamma$  and  $\beta$  are defined as the GJ angles of one of the  $\phi$  mesons in the rest frame of the  $\phi\phi$  system, with the z-axis in the direction of  $\vec{p}_{fast} - \vec{p}_{beam}$ , and the y-axis in the direction of the  $(\vec{p}_{fast} - \vec{p}_{beam}) \times (\vec{p}_{slow} - \vec{p}_{tgt})$  cross product, measured in the pp CM system. The other angles  $(\alpha_{1,2}, \theta_{1,2})$  are the two pairs of GJ angles of the  $K^+$ 's in their parent  $\phi$  rest frames, with the z'-axis in the direction of  $\vec{p}_{\phi}$ , and  $y' = z \times z'$ . This system has I = 0, C = +, and L + S =even number.

The analysis was performed in twelve bins of 50  $MeV/c^2$  between 2.04  $GeV/c^2$  and 2.64  $GeV/c^2$ . The result of the analysis is shown by the symbols with error bars in Fig. 9. Only three waves were necessary to describe the data. All waves

have quantum numbers  $J^{PC}LS = 2^{++}02$ , with  $M^{\eta} = 0^{-}/1^{-}$  for the upper/lower symbols in Fig. 9(a), and  $M^{\eta} = 1^{+}$  for the circles in Fig. 9(c). The phase between the interfering waves  $M^{\eta} = 0^{-}/1^{-}$  is shown in Fig. 9(b).



Fig. 9. The symbols with error bars show the only three  $J^{PC}LS = 2^{++}02$  waves needed in the PWA analysis of the  $\phi\phi$  system. The upper/lower points in (a) correspond to the  $M^{\eta} = 0^{-}/1^{-}$  amplitudes. The phase between those waves is shown in (b). Plot (c) shows the  $M^{\eta} = 1^{+}$  amplitude. The lines represent the fit to the data described in the text.

The  $\phi\phi$  cross section opens at threshold very fast, reminiscent of the fast opening of the KK cross section due to the presence on the  $f_0(980)$  just below threshold. This can be taken as an indication of a state right below threshold waiting to go into  $\phi\phi$ . E690 performed a fit to the result of the PWA analysis using a resonance below threshold produced as  $M^{\eta} = 0^{-}$  and another resonance above threshold produced in all  $M^{\eta}$  states. The results of the fit are shown by the lines in Fig. 9. The extracted parameters for the resonance above threshold are:

$$M_R = 2.243 \pm 0.015(stat) \pm 0.010(syst) \quad \text{GeV}/c^2$$
  

$$\Gamma_R = 0.368 \pm 0.033(stat) \pm 0.030(syst) \quad \text{GeV}/c^2$$
(4)

With the available statistics, and only fitting to the  $\phi\phi$  channel, the parameters for the resonance below threshold could only be determined approximately, giving  $M_R \sim 1.9 \text{ GeV/c}^2$  and  $\Gamma_R \sim 0.3 \text{ GeV/c}^2$ . These values are consistent with either the  $f_2(1950)$  or the  $f_2(2010)$ .<sup>28</sup>

#### 7. Diffractive production of charm

To search for intrinsic charm states within the proton that could be excited diffractively,<sup>29</sup> E690 selected inclusive events with a  $D^*$  meson decaying to  $K\pi\pi$ :<sup>30</sup>

$$pp \to Y \left| D^* \to (D^0 \to K\pi)\pi \right| p_f$$

$$\tag{5}$$

with Y being an unidentified recoil system. Even though the  $D^*$  is centrally produced and the forward proton is clearly diffractive this reaction does not qualify as

### 10 G. Gutierrez, M.A. Reyes

exclusive, but we decided to include it in this review because it constitutes the first measurement of the diffractive charm cross section.

The events were selected requiring at least four charged tracks (including the scattered beam proton) with the correct charge assignments coming from the primary vertex. The two tracks from the  $D^0$  decay were required to be identified by the Čerenkov counter as a kaon and a pion, the slow  $\pi^+$  from the  $D^{*+}$  decay was identified by the time-of-flight system. The identification of the slow  $\pi^-$  from the  $D^{*-}$  decay was not required since this background is composed mostly of  $\pi^-$ . The  $D^*$  was selected requiring that  $|Q - 5.83| < 0.5 \text{MeV/c}^2$ , where  $Q = M(K\pi\pi) - M(K\pi) - M(\pi)$ . The  $x_F$  of the diffractive proton was required to be larger than  $x_F > 0.85$ .<sup>31</sup> Figure 10 shows the  $K^-\pi^+\pi^+$  and the  $K^+\pi^-\pi^-$  mass distributions for the selected events.



Fig. 10.  $K\pi\pi$  invariant mass distributions for the selected events in reaction (5). The panel on the left shows  $D^{*+}$  and the right one  $D^{*-}$ . The lines are fits to a Gaussian plus a linear background.

Figure 11 shows the rapidity distribution for the  $D^{*+}$ , the diffractive proton  $p_f$  and the recoil system Y.<sup>32</sup> We can see a clear gap between the central  $D^{*+}$  and the rest of the system.



Fig. 11.  $D^*$ , Y and  $p_f$  rapidity plots for the  $D^{*+} \to D^0(K\pi^+)\pi^+$  decay in reaction (5).

The values of the measured  $D^*$  diffractive cross sections are:

$$\sigma_{\text{diff}}(D^{*+}) = 0.185 \pm 0.044(\text{stat}) \pm 0.054(\text{syst}) \ \mu b$$
  
$$\sigma_{\text{diff}}(D^{*-}) = 0.174 \pm 0.034(\text{stat}) \pm 0.029(\text{syst}) \ \mu b$$
 (6)

These cross sections are compatible with previous limits and predict a total charm diffractive cross section of  $\sigma_{\text{diff}}(c\bar{c}) \sim 0.66 \ \mu\text{b}$ . This gives a ratio of the diffractive charm to the total pp diffractive cross section of  $\sim 10^{-4}$ , which is 10 times smaller than the ratio of the inelastic charm to the inelastic pp cross section.<sup>30</sup>

# 8. Conclusions

In this paper we reviewed the Exclusive Central Production of  $\pi^+\pi^-$ ,  $K_s^0 K_s^0$ ,  $K_s^0 K^{\pm} \pi^{\mp}$  and  $\phi \phi$  and the diffractive production of charm at the Fermilab FT program. All these reactions were produced with an 800 GeV/c proton beam hitting a LH<sub>2</sub> target. A Partial Wave Analysis was performed in all light meson production reactions, only the cross section was measured in the diffractive production of charm. The scalar mesons  $f_0(980)$  and  $f_0(1500)$  are clearly seen both in  $\pi^+\pi^$ and  $K_s^0 K_s^0$ . There is no clear evidence of the  $f_0(1370)$  in either reaction, a result that is in agreement with  $\pi^-\pi^+$  elastic scattering. The spin of the  $f_J(1710)$  could not be determined with this data alone. Only two resonances, the  $f_1(1285)$  and the  $f_1(1420)$ , are seen in the PWA analysis of  $K_s^0 K^{\pm} \pi^{\mp}$ . The existence of a  $0^{-+}$  state decaying to  $a_0\pi$  in this reaction is completely ruled out. The Central Production of  $\phi\phi$  is clearly seen. Two 2<sup>++</sup> resonances, one below and another one above threshold, are needed to explain the  $\phi\phi$  data. The measurement of the  $D^*$  diffractive cross section shows that the ratio of the diffractive charm to the diffractive pp cross section is ten times smaller than the ratio of the inelastic charm to the inelastic pp cross section.

## Acknowledgments

We would like to thank the many people that provided information about the Fermilab Fixed Target program. This work was funded by the US Department of Energy and CONACYT Mexico. M. A. Reyes would like to thank CONACYT for supporting a sabbatical stay at Femilab while this paper was being written.

## References

- 1. CERN-ISR Collab. (L. Baksay et al.), Phys. Lett. B61, 89 (1976).
- 2. For a list of FNAL Fixed Target experiments see http://www.fnal.gov/faw/fermilab\_at\_work.html#faw-experiments-and-projects.
- E690 Collab. (E. P. Hartouni *et al.*), Nucl. Instrum. Methods Phys. Res. A 317, 161 (1992); E690 Collab. (D. C. Christian *et al.*), Nucl. Instrum. Methods Phys. Res. A 345, 62 (1994).
- E690 Collab. (K. Markianos et al.), in Proc. 14th Int. Conf. on Particles and Nuclei '96, eds. C. A. Carlson and J. J. Domingo (World Scientific, 1996), p. 543.

- 12 G. Gutierrez, M.A. Reyes
- 5. K. Markianos, Fermilab-Thesis-1998-57.
- S. U. Chung and T.L. Trueman, *Phys. Rev.* D 11, 633 (1975); S. U. Chung, *BNL Preprint BNL-QGS94-23*; S. U. Chung, *BNL Preprint BNL-QGS95-41*.
- 7. K. L. Au, D. Morgan and M. R. Pennington, Phys. Lett. B167, 229 (1986).
- 8. W. Ochs J. Phys. G: Nucl. Part. Phys. 40, 043001 (2013).
- E690 Collab. (M. A. Reyes et al.), Phys. Rev. Lett. 81, 4079 (1998). Details of this analysis may be found in M. A. Reyes, Ph.D. thesis, CINVESTAV, Mexico, 1996.
- 10. BES Collab. (J. Z. Bai et al.), Phys. Rev. Lett. 76, 3502 (1996).
- 11. Particle Data Group (R. M. Barnett et al.), Phys. Rev. D 54, 1 (1996).
- 12. S. U. Chung, Phys. Rev. D 56, 7299 (1997); also in BNL Preprint BNL-QGS-97-041.
- E. Barrelet, Nuovo Cimento Soc. Ital. Fis. 8A, 331 (1972). S. U. Chung, Phys. Rev. D 56, 7299 (1997).
- 14. WA76 Colab. (T. A. Armstrong et al.), Phys. Lett. B 227, 186 (1989).
- 15. Crystal Barrel Collab. (C. Amsler *et al.*), *Phys. Lett. B* **342**, 433 (1995).
- 16. E690 Collab. (M. Sosa et al.), Phys. Rev. Lett. 83, 913 (1999).
- T. A. Armstrong et al., Phys. Lett. B 146, 273 (1984); Z. Phys. C 34, 23 (1987); Phys. Lett. B 221, 216 (1989); Z. Phys. C 56, 29 (1992).
- 18. D. Barberis et al., Phys. Lett. B 440, 225 (1998).
- H. Aihara *et al.*, Phys. Rev. Lett. 57, 2500 (1986); G. Gidal et al., Phys. Rev. Lett. 59, 2016 (1987).
- LASS Collab. (D. Aston et al.), Phys. Lett. B 201, 573 (1988); P. Gavilet et al., Z. Phys. C 16, 119 (1982).
- 21. Particle Data Group (C. Caso et al.), Eur. Phys. J. C 3, 1 (1998).
- S. Okubo, Phys. Lett. 5, 165 (1963); G. Z. Zweig, CERN Report No. TH-401 and TH-412, 1964 (unpublished); J. Iizuka, Prog. Theor. Phys. Suppl.37-38, 21 (1966).
- 23. A. Etkin et al., Phys. Rev. Lett. 40, 422 (1978).
- 24. A. Etkin et al., Phys. Lett B 201, 568 (1988).
- D. R. Green et al.), Phys. Rev. Lett. 56, 1639 (1986). T. F. Davenport et al.), Phys. Rev. D33, 2519 (1986)
- Fermilab E690 Collab. (M. A. Reyes et al.), Proc. 10th Int. Conf. on Hadron Spectroscopy 2003, AIP Conf. Proc., Vol. 717, eds. E. Klempt, H. Koch and H. Orth (AIP 2004), p. 135.
- A. V. Anisovich *et al.*, *Phys. Lett* B 491, 47 (2000). A. V. Anisovich *et al.*, *Phys. Rev.* D85, 014001 (2012).
- 28. J. Beringer et al. (Particle Data Group), *Phys. Rev.* **D**86, 010001 (2012).
- S. J. Brodsky, P. Hoyer, C. Peterson, and N. Sakai, *Phys. Lett.* 93 B, 451 (1980); S. J. Brodsky, C. Peterson, and N. Sakai, *Phys. Rev. D* 23, 2745 (1981).
- 30. E690 Collab. (M. H. L. S. Wang et al.), Phys. Rev. Lett. 87, 082002 (2001).
- 31. K. Goulianos, Phys. Rep. 101, 169 (1983).
- M. H. L. S. Wang et al, in QCD and Weak Boson Physics in Run II, eds. U. Baur, R.K. Ellis and D. Zeppenfeld (2000), p. 235, Fermilab-Pub-00/297.