



**SDC**  
**SOLENOIDAL DETECTOR NOTES**

**SPATIAL RESOLUTION OF A SINGLE SCINTILLATING  
FIBER OF CIRCULAR CROSS-SECTION**

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SPATIAL RESOLUTION OF A SINGLE SCINTILLATING  
FIBER OF CIRCULAR CROSS-SECTION\*

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ABSTRACT

With the simplifying assumption that the detection probability of a normally-crossing, minimum-ionizing particle is directly proportional to the length of the chord traversed, the rms deviation for a single circular scintillating-fiber position detector of diameter  $d$  is shown to be  $d/4 = 0.25d$ . This value is slightly smaller than  $d/\sqrt{12} = 0.28d$  obtained for a rectangular detection-probability distribution.

It is well known that the spatial resolution of a one-dimensional detector of extent  $d$  is  $d/\sqrt{12}$ . This quantity is the rms deviation of a probability distribution which is constant across the detector's extent and is zero elsewhere. While this value has been applied in discussions of the spatial resolution of scintillating-fiber tracking detectors, it is not really applicable to detectors employing circular fibers since the detection probability is *not* constant across a fiber diameter. The purpose of this note is to obtain a more appropriate value.

Consider a scintillating fiber of diameter  $d$  subject to normally-crossing, minimum-ionizing particles, as shown in Fig. 1. As discussed in Refs. 1 and 2, even in this special case the detection probability is not easily expressed as a function of the crossing position coordinate,  $x$ . However, for the purpose of this

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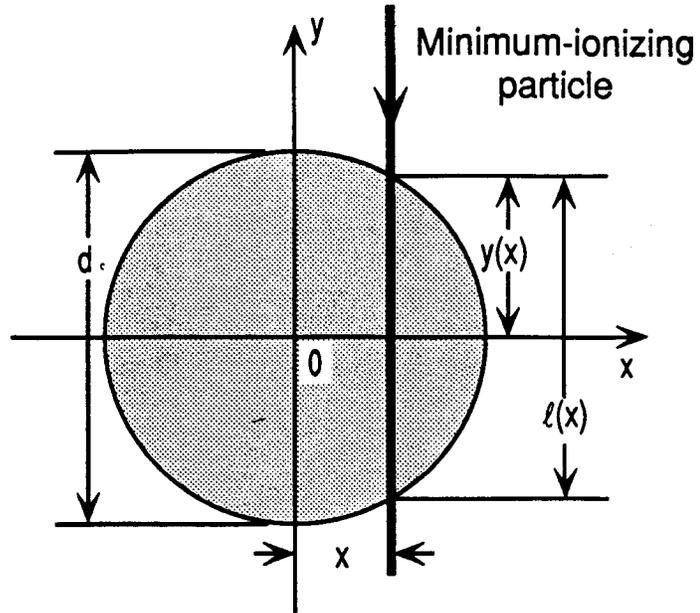


Figure 1. Minimum-ionizing particle normally crossing a circular scintillating fiber.

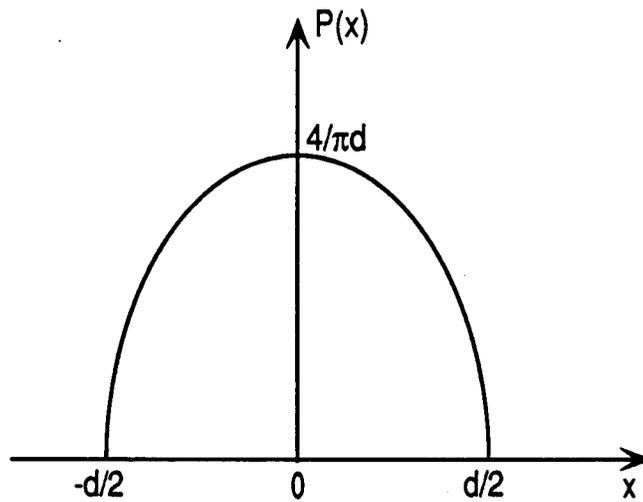


Figure 2. Detection probability distribution for the assumptions made in the text.