Assessing Perturbativity and Vacuum Stability in High-Scale Leptogenesis

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ABSTRACT: We consider the requirements that all coupling constants remain perturbative and the electroweak vacuum metastable up to the Planck scale in high-scale thermal leptogenesis, in the context of a type-I seesaw mechanism. We find a large region of the model parameter space that satisfies these conditions in combination with producing the baryon asymmetry of the Universe. We demonstrate these conditions require $\text{Tr}[Y_N^\dagger Y_N] \lesssim 0.57$ on the neutrino Yukawa matrix. We also investigate this scenario in the presence of a large number N_F of coloured Majorana octet fermions in order to make quantum chromodynamics asymptotically safe in the ultraviolet.

arXiv:1806.00460v1 [hep-ph] 1 Jun 2018

Contents

1 Introduction

The Standard Model (SM) cannot be a complete fundamental theory. In the SM the hypercharge coupling increases with energy in the deep ultraviolet (UV) reaching a Landau pole for a finite value of the energy scale. In addition to this ultraviolet shortcoming, there are a number of phenomenological issues such as the baryon asymmetry of the Universe (BAU), dark matter, inflation, strong CP-violation and neutrino masses that further motivate physics beyond the SM.

Although there has been impressive progress in understanding neutrino physics in the last decades, the nature of neutrinos – namely, whether they are Majorana or Dirac particles – and the origin of their masses remain unknown. One of the most economical methods to generate neutrino masses is via the type-I seesaw mechanism [1–4] In this mechanism one introduces heavy Majorana neutrinos which are singlets under the SM gauge group. In addition to providing an explanation for small but non-zero neutrino masses, the type-I seesaw also provides a solution to the BAU, due to a new source of CP-violation present in the out-of-equilibrium decays of the heavy Majorana neutrinos in the early Universe [5].

The key question we address in this work is: can a minimal extension of the SM by three heavy Majorana neutrinos, simultaneously addressing neutrino masses and the observed matter–anti-matter asymmetry, be self-consistent up to the Planck scale without the addition of new degrees of freedom? In order to answer this question, we investigate the self-consistency of high-scale leptogenesis up to the Planck scale by performing a systematic study of the renormalisation group (RG) of this model to assess whether the coupling constants remain perturbative and the electroweak vacuum metastable. In addition, we ascertain the validity of the model up to $\sim 10^{40}$ GeV, the scale at which the hypercharge develops a Landau pole. Moreover, we extend this study to consider a scenario where we introduce a large number, N_F, of coloured fermions to achieve asymptotic safety in the strong sector of the SM.

There have been recent similar analyses completed in the context of the inverse seesaw mechanism, *e.g.* in Refs. [6–9]. The authors of [10, 11] also studied similar constraints in the type-I seesaw. In our work, we extend their study by explicitly solving the density matrix equations for thermal leptogenesis and studying the high-energy robustness of the associated parameter space. In the latter work, the authors focused particularly on resonant leptogenesis [12] which allows the mass scale of the heavy Majorana neutrinos to be lowered thereby reducing the corrections to the Higgs mass[1]. It has been shown that for heavy neutrino masses $M_N \lesssim 10^7$ GeV, such radiative corrections are small ($\delta m_h^2 < m_h^2$) [11, 13, 14]. However, we choose to remain agnostic about the level of fine tuning in Nature in view that there has not been any experimental evidence for new physics around the electroweak scale, generally predicted by extensions of the SM which intend to address Higgs

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[1]The heavy Majorana neutrinos induce quantum corrections to the Higgs mass and without any new states, *e.g.* supersymmetric partners, such corrections can be large.

naturalness, and hence do not consider this issue any further.

The paper is organised as follows: in Section 2 we present an overview of high-scale thermal leptogenesis and numerically solve the density matrix equations to compute the baryon asymmetry. We describe the procedure for our numerical scan in Section 3 and present the RG analysis and our results in Section 4. Finally, in Section 5 we present our conclusions.

2   High-scale Thermal Leptogenesis

The mechanism of thermal leptogenesis [5] is partly motivated by the observation of small, but non-zero neutrino masses and its possible connection to the seesaw mechanism. In its simplest formulation, the type-I seesaw mechanism [1–3] introduces singlet Majorana fermions to the SM particle spectrum. From the seesaw relation, the scale of the heavy Majorana neutrinos suppresses the light neutrino masses. Moreover, Sakharov's three conditions are inherently satisfied within this framework: **(i)** the heavy Majorana neutrino mass matrix violates lepton number, **(ii)** the Yukawa matrix which couples the heavy Majorana neutrino to the SM particles can be complex and provide new sources of CP-violation and **(iii)** finally, due to the expansion of the Universe, the heavy Majorana neutrino is a good candidate to decay out of thermal equilibrium.

The lepton asymmetry is dynamically produced from the CP-violating decays of the heavy Majorana neutrinos. There are also washout processes present which compete with these decays and act to reduce the overall asymmetry. The final lepton asymmetry is partially reprocessed to a baryon asymmetry via weak sphaleron processes which proceed at unsuppressed rates above the electroweak scale [15]. The leptogenesis era occurs approximately when the temperature of the Universe equals the mass scale of the decaying heavy Majorana neutrino ($T \approx M_1$).

In general, it was thought thermal leptogenesis, in the context of a type-I seesaw, was not viable below $M_1 \approx 10^9$ GeV [16]. This lower limit, otherwise known as the Davidson-Ibarra bound, is derived from the requirement that the CP-asymmetry parameter ϵ is sufficiently large to produce the observed baryon asymmetry assuming the efficiency factor (which is used to parametrise the washout) is approximately unity. However, this bound may be lowered to $M_1 \approx 10^6$ GeV if one foregoes $\gtrsim \mathcal{O}(10)$ fine-tuning to the light neutrino masses [17]. Using $\Delta L = 2$ washout processes, due to scattering mediated by off-shell N_2 or N_3, an upper bound $M_1 \lesssim 10^{14}$ GeV [18] was found. However, a more refined calculation, which includes $\Delta L = 1$ processes, further extends this upper bound to $M_1 \lesssim 10^{15}$ GeV [19, 20]. Therefore, there is a large energy-scale window for non-resonant thermal leptogenesis ranging from 10^6 GeV $\lesssim M_1 \lesssim 10^{15}$ GeV.

To implement a type-I seesaw mechanism the following terms are added to the SM Lagrangian

$$\mathcal{L} = i\overline{N_i}\slashed{\partial}N_i - Y_{N\alpha i}\overline{L_\alpha}\tilde{H}N_i - \frac{1}{2}M_i\overline{N_i^c}N_i + \text{h.c.}, \qquad (2.1)$$

where $\alpha = e, \mu, \tau$, $i = 1, 2, 3$, Y_N is the Yukawa matrix, H the Higgs $\text{SU}(2)_L$ doublet, $\tilde{H} = i\sigma_2 H^*$ and $L^T = \left(\nu_L^T, l_L^T\right)$ is the charged lepton $\text{SU}(2)_L$ doublet. The connection between thermal leptogenesis, or in fact any mechanism of leptogenesis which implements a type-I seesaw, and neutrino observables can be expressed by the Casas-Ibarra parametrisation [21] for the matrix Y_N

$$Y_N = \frac{1}{v}U\sqrt{m_\nu}R^T\sqrt{M_N}, \qquad (2.2)$$

where $v = 174$ GeV is the vacuum expectation value of the Higgs, m_ν (M_N) the diagonal mass matrices of light (heavy) neutrinos and R is an orthogonal, complex matrix. The Pontecorvo-Maki Nakagawa-Sakata (PMNS) matrix, U, describes the misalignment between the mass and flavour basis of the active neutrinos and contains six real parameters: three measured mixing angles and three CP-phases. The Dirac phase, δ, enters the neutrino oscillation probabilities sub-dominantly and remains largely unconstrained by experimental data. The Majorana phases [22, 23], which are physical if and only if neutrinos are Majorana particles, ($\alpha_{21}, \alpha_{31} = [0, 4\pi]^2$) cannot be determined using neutrino oscillation experiments and have to be measured using alternative methods.

We work with the experimental central values for the active neutrino masses, m_{ν_i}, the mixing angles, θ_{ij}, and the Dirac CP-phase, δ, which are given by [25]

$$\theta_{13} = 8.52°, \quad \theta_{12} = 33.63°, \quad \theta_{23} = 48.7°, \quad \delta = 228°,$$
$$\Delta m_{21}^2 = 7.40 \times 10^{-5}\,\text{eV}^2, \quad \Delta m_{31}^2 = 2.515 \times 10^{-3}\,\text{eV}^2,$$

for a normally ordered mass spectrum. Moreover, as the two Majorana phases are currently completely unconstrained, we fix their values to be CP-conserving, $\alpha_{21} = \alpha_{31} = 0$. In addition to the low-energy CP-phases, there are also phases associated with the R matrix. As the R matrix is complex and orthogonal, it may be parametrised in terms of three complex rotation matrices

$$R = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{\theta_1} & s_{\theta_1} \\ 0 & -s_{\theta_1} & c_{\theta_1} \end{pmatrix} \begin{pmatrix} c_{\theta_2} & 0 & s_{\theta_2} \\ 0 & 1 & 0 \\ -s_{\theta_2} & 0 & c_{\theta_2} \end{pmatrix} \begin{pmatrix} c_{\theta_3} & s_{\theta_3} & 0 \\ -s_{\theta_3} & c_{\theta_3} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \qquad (2.3)$$

where $c_{\theta_i} = \cos\theta_i$, $s_{\theta_i} = \sin\theta_i$ for $i = 1, 2, 3$; and θ_i are complex angles. Therefore, in general, the baryon asymmetry produced from thermal leptogenesis is a function of 18 parameters of the Casas-Ibarra parametrisation.

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[2]This range is necessary as the Majorana phases enter into the expression for the neutrino mixing matrix in the form $e^{\frac{i\alpha_{21}}{2}}$ and $e^{\frac{i\alpha_{31}}{2}}$ [24].

Parameter	Scan Range
M_1	$[10^9, 10^{14}]$ GeV
M_2	$[10^1, 10^4]\, M_1$
$\mathrm{Re}[\theta]$	$[-\pi, \pi]$
$\mathrm{Im}[\theta]$	$[-\pi, \pi]$

Table 1: Ranges of the four free parameters in our numerical scan.

2.1 Leptogenesis with Two Heavy Majorana Neutrinos

In order to simplify our discussion, we consider the decoupling limit of the heaviest Majorana neutrino, N_3. From the seesaw relation, this causes the lightest neutrino to be massless, which is consistent with data from oscillation experiments. In this limit, the R matrix assumes the following simplified form [26–28]

$$R^{\mathrm{NO}} = \begin{pmatrix} 0 & \cos\theta & \pm\sin\theta \\ 0 & \pm\sin\theta & \cos\theta \\ 1 & 0 & 0 \end{pmatrix}, \quad R^{\mathrm{IO}} = \begin{pmatrix} \cos\theta & \pm\sin\theta & 0 \\ \pm\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{pmatrix}, \tag{2.4}$$

for normal (NO) and inverted (IO) ordering respectively. As a consequence, the Yukawa matrix, for normal ordering, may be written as

$$
\begin{aligned}
Y_N =& \frac{1}{v} \begin{pmatrix} U_{e1} & U_{e1} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 \\ 0 & \sqrt{m_2} & 0 \\ 0 & 0 & \sqrt{m_3} \end{pmatrix} \begin{pmatrix} 0 & c_\theta & s_\theta \\ 0 & -s_\theta & c_\theta \\ 1 & 0 & 0 \end{pmatrix}^T \begin{pmatrix} \sqrt{M_1} & 0 & 0 \\ 0 & \sqrt{M_2} & 0 \\ 0 & 0 & 0 \end{pmatrix} \\
=& \frac{1}{v} \begin{pmatrix} \sqrt{M_1}\left(U_{e2}\sqrt{m_2}c_\theta + U_{e3}\sqrt{m_3}s_\theta\right) & \sqrt{M_2}\left(U_{e3}\sqrt{m_3}c_\theta - U_{e2}\sqrt{m_2}s_\theta\right) & 0 \\ \sqrt{M_1}\left(U_{\mu2}\sqrt{m_2}c_\theta + U_{\mu3}\sqrt{m_3}s_\theta\right) & \sqrt{M_2}\left(U_{\mu3}\sqrt{m_3}c_\theta - U_{\mu2}\sqrt{m_2}s_\theta\right) & 0 \\ \sqrt{M_1}\left(U_{\tau2}\sqrt{m_2}c_\theta + U_{\tau3}\sqrt{m_3}s_\theta\right) & \sqrt{M_2}\left(U_{\tau3}\sqrt{m_3}c_\theta - U_{\tau2}\sqrt{m_2}s_\theta\right) & 0 \end{pmatrix},
\end{aligned}
\tag{2.5}
$$

where θ is a complex angle. The scenario of thermal leptogenesis with two heavy Majorana neutrinos is particularly appealing as the dimensionality of the model parameter space is greatly reduced (from 18 to 11) and for this reason has been investigated using the un-flavoured approximation [26, 29–31] and also including flavour effects [32–35]. As we have assumed the best-fit values for the low-energy neutrino parameters, the lepton asymmetry depends only on four parameters (M_1, M_2, $\mathrm{Re}[\theta]$ and $\mathrm{Im}[\theta]$) which we assume take the ranges shown in Table 1. It is worth noting that as we assume a strictly hierarchical mass spectrum for the heavy neutrinos ($M_2 \geq 10M_1$) we find the lower range for viable leptogenesis to be $M_1 \approx 10^9$ GeV. Although non-resonant thermal leptogenesis is possible at lower scales, a milder mass hierarchy is required.

2.2 Density Matrix Equations

In order to calculate the time evolution of the lepton asymmetry we solve the density matrix equations detailed in [36] where the theoretical background and derivation of these kinetic equations are presented. Due to our assumption of a hierarchical heavy neutrino mass spectrum, the contribution to the lepton asymmetry from N_2 is negligible and the density matrix equation are given by

$$\frac{dn_{N_1}}{dz} = -D_1(n_{N_1} - n_{N_1}^{\text{eq}}), \tag{2.6}$$

$$\frac{dn_{\alpha\beta}}{dz} = \epsilon_{\alpha\beta}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \frac{1}{2}W_1 \left\{ P^{0(1)}, n \right\}_{\alpha\beta}$$

$$-\frac{\text{Im}(\Lambda_\tau)}{Hz} \left[\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \left[\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, n \right] \right]_{\alpha\beta} - \frac{\text{Im}(\Lambda_\mu)}{Hz} \left[\begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \left[\begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, n \right] \right]_{\alpha\beta},$$

where Greek letters denote flavour indices, n_{N_1} ($n_{N_1}^{\text{eq}}$) is the abundance (equilibrium abundance) of the lightest heavy Majorana neutrino [3], D_1 (W_1) denotes the decay (washout) of N_1. Moreover, H denotes the Hubble expansion rate and Λ_α is the self-energy of α-flavoured leptons. The thermal widths, $\text{Im}(\Lambda_\alpha)$, of the charged leptons is given by the imaginary part of the self-energy correction to the lepton propagator in the thermal plasma. The projection matrices, $P_{\alpha\beta}^{0(i)}$ describe how a given flavour of lepton is washed out and the CP-asymmetry matrix details the decay asymmetry generated by N_1 and is denoted by $\epsilon_{\alpha\beta}^{(1)}$. The density matrix equations of Eq. (2.6) may be used to calculate the lepton asymmetry in all flavour regimes and accurately describes the transitions between them [36–40]. The complex off-diagonal entries of $n_{\alpha\beta}$ allow for a quantitative description of these transitions. For example, if leptogenesis occurs at temperatures 10^9 GeV $\lesssim T \lesssim 10^{12}$ GeV, the term $\text{Im}(\Lambda_\tau)/Hz$ damps the evolution of the off-diagonal elements of $n_{\alpha\beta}$. This reflects the loss of coherence of the tau charged lepton state as the SM tau Yukawa couplings come into thermal equilibrium. Additional formulae and further discussion of the density matrix equations in Eq. (2.6) may be found in Appendix A.

3 Numerical Procedure

Our goal in this work is to ascertain whether or not a minimal extension of the SM, which simultaneously explains neutrino masses and the observed BAU, may be valid up to the Planck scale without the requirements of additional new degrees of freedom. To investigate this, we first fix the measured central values in the active neutrino sector as given in Eq. (2.3) and then perform a random scan of the four-dimensional leptogenesis model parameter space as shown in Table 1[4]. For a given point in this space we calculate a Yukawa matrix, Y_N, as parametrised in Eq. (2.5). Subsequently, we numerically solve the density matrix equation

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[3]This quantity is normalised to a co-moving volume containing one right-handed neutrino which is ultra-relativistic and in thermal equilibrium.

[4]Note that this procedure is undertaken for normally ordered active neutrinos. The results are qualitatively similar for inverted ordering.

of Eq. (2.6) to find the baryon-to-photon ratio associated to a particular point in the model parameter space. The baryon-to-photon ratio is defined as

$$\eta_B \equiv \frac{n_B - n_{\overline{B}}}{n_\gamma}, \tag{3.1}$$

where n_B, $n_{\overline{B}}$ and n_γ are the number densities of baryons, anti-baryons and photons respectively. This quantity can be measured from Big-Bang nucleosynthesis (BBN) [41, 42] and Cosmic Microwave Background (CMB) radiation data [43]:

$$\eta_{B\,\text{BBN}} = (5.80 - 6.60) \times 10^{-10},$$
$$\eta_{B\,\text{CMB}} = (6.02 - 6.18) \times 10^{-10},$$

at 95% CL, respectively. For a given point in the model parameter space, we define *successful leptogenesis* to produce $\eta_B > 5.8 \times 10^{-10}$.

Once we have a subset of points that lead to successful leptogenesis, we subsequently solve the RG equations for all the couplings in the model and determine whether they remain perturbative and the electroweak vacuum stable or metastable up to the Planck scale[5]. We detail this further in Section 4.

4 Results

In this Section, we present the results of our RG analysis of high-scale leptogenesis for normally ordered light neutrino mass spectrum. We consider the Lagrangian in Eq. (2.1), which augments the SM particle spectrum by three heavy Majorana neutrinos that are responsible for the masses of active neutrinos and the baryon asymmetry of the Universe. We determine the UV-robustness of the viable parameter space in this minimal case, as discussed, and the non-standard scenario of asymptotically safe QCD.

4.1 Vacuum Stability and Perturbativity in High-Scale Leptogenesis

Two problems can arise when extrapolating the coupling constants of the model to high scales. **(i)** Dimensionless coupling constants in the Lagrangian could grow with energy such that they become larger than $\mathcal{O}(1)$, rendering the theory non-perturbative. **(ii)** Adding new fermionic degrees of freedom gives a negative contribution to the β-function of the Higgs quartic and this can drive the already-metastable electroweak vacuum to violate the metastability bound.

In order to study the stability of the electroweak vacuum we use the one-loop RG-improved effective potential for the Higgs. For the RG analysis we solve the two-loop β-functions for the SM couplings that can be found in [48] and one-loop for Y_N, both computed in the $\overline{\text{MS}}$ scheme. For simplicity we provide the one-loop RG equations [49] below.

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[5]Similar works that study how the electroweak vacuum is affected by new physics related to the origin of neutrino masses include [44–47].

- Gauge couplings:

$$(4\pi)^2 \frac{dg_Y}{d\ln\mu} = \frac{41}{6}g_Y^3, \qquad (4\pi)^2 \frac{dg_2}{d\ln\mu} = -\frac{19}{6}g_2^3, \qquad (4\pi)^2 \frac{dg_3}{d\ln\mu} = -7g_3^3. \qquad (4.1)$$

- The Higgs quartic, the top Yukawa and the neutrino Yukawa matrix:

$$(4\pi)^2 \frac{d\lambda_H}{d\ln\mu} = \lambda_H \left(24\lambda_H + 12y_t^2 - 9g_2^2 - 3g_Y^2\right) - 6y_t^4 + \frac{9}{8}g_2^4 + \frac{3}{8}g_Y^4 + \frac{3}{4}g_2^2 g_Y^2$$
$$+ 4\mathrm{Tr}[Y_N^\dagger Y_N]\lambda_H - 2\mathrm{Tr}[(Y_N^\dagger Y_N)^2], \qquad (4.2)$$

$$(4\pi)^2 \frac{dy_t}{d\ln\mu} = y_t \left(\frac{9}{2}y_t^2 - \frac{17}{12}g_Y^2 - \frac{9}{4}g_2^2 - 8g_3^2\right) + y_t\mathrm{Tr}[Y_N^\dagger Y_N], \qquad (4.3)$$

$$(4\pi)^2 \frac{dY_N}{d\ln\mu} = \frac{3}{2}Y_N Y_N^\dagger Y_N + Y_N\mathrm{Tr}[Y_N^\dagger Y_N] - Y_N \left(\frac{3}{4}g_Y^2 + \frac{9}{4}g_2^2 - 3y_t^2\right), \qquad (4.4)$$

where μ corresponds to the RG scale and the Higgs quartic λ_H is defined by writing the SM Higgs potential as $V = -\frac{1}{2}M_h^2|H|^2 + \lambda_H|H|^4$. The contribution from each column i of the Yukawa matrix to the β-functions is set to zero when $\mu < M_i$. From the last term in Eq. (4.2), we observe that Y_N gives a negative contribution to the running of λ_H. This implies that large Yukawa couplings will destabilise the electroweak vacuum. Furthermore the positive contribution from Y_N to β_{y_t} in Eq. (4.3) can drive the top Yukawa to large positive values which further pushes λ_H below the metastability bound. We do not consider RG running effects on the parameters of the active neutrino sector as in general such effects are weak [50].

We impose the following perturbativity constraints on the SM and the neutrino Yukawa couplings

$$g_i(\mu), y_t(\mu), \lambda_H(\mu) \leq \sqrt{4\pi}, \qquad |Y_N^{ij}(\mu)| \leq \sqrt{4\pi}, \qquad \mathrm{Tr}[Y_N^\dagger(\mu)Y_N(\mu)] \leq 4\pi. \qquad (4.5)$$

The effective Higgs quartic coupling can be defined in terms of the one-loop contributions to the Higgs potential and is given as follows,

$$\lambda_{\mathrm{eff}} = \lambda_H + \frac{1}{16\pi^2}\left[\frac{3}{16}\left(g_Y^2 + g_2^2\right)^2 \left(\ln\frac{g_Y^2 + g_2^2}{4} - \frac{5}{6}\right) + \frac{3}{8}g_2^4 \left(\ln\frac{g_2^2}{4} - \frac{5}{6}\right)\right.$$
$$\left. - 3y_t^4 \left(\ln\frac{y_t^2}{2} - \frac{3}{2}\right) + 3\lambda_H^4 \left(4\ln\lambda_H - 6 + 3\ln 3\right)\right] + \lambda_N, \qquad (4.6)$$

where the μ dependence of each coupling is not explicitly written and we have taken μ equal to the value of the Higgs field in order to minimize the contribution from the logarithms. The last term in the expression above corresponds to the contribution from the heavy Majorana neutrinos that only enters at $\mu \geq M_{N_i}$. We consider a leptogenesis scenario where the heaviest sterile neutrino N_3 is decoupled; for the RG analysis we set

M_3 close to the Planck scale. The contribution from the neutrino Yukawa couplings to the effective Higgs quartic coupling at one-loop is given as

$$\lambda_N = -\frac{1}{32\pi^2}\left[(Y_N^\dagger Y_N)_{ii}^2\left\{\ln\frac{(Y_N^\dagger Y_N)_{ii}}{2}-1\right\}+(Y_N^\dagger Y_N)_{ii}^2\left\{\ln\frac{(Y_N^\dagger Y_N)_{ii}}{2}-1\right\}\right],\quad(4.7)$$

where $Y_N^\dagger Y_N$ is written in the diagonal basis [6].

A detailed RG study of the Higgs potential in the SM has shown that at high scales the quartic coupling turns negative and the potential develops a new minimum [48]. Using the one-loop RG improved Higgs potential and the two-loop β-functions we find that λ_{eff} becomes negative at $\mu_{\text{inst}}\approx 6\times 10^{11}$ GeV in the SM. Taking the central values for measurements of the Higgs and the top mass, this secondary vacuum is deeper than the electroweak vacuum and hence, given sufficient time, there is a chance the Higgs field will tunnel into it. Requiring the age of the Universe to be larger than the lifetime of the electroweak vacuum implies a lower bound for negative values of $\lambda_{\text{eff}}(\mu)$ [48]

$$|\lambda_{\text{eff}}(\mu)| > \frac{2\pi^2}{3}\frac{1}{\ln(\tau\mu)},\tag{4.8}$$

where $\tau = 4.35\times 10^{17}$ s is the age of the Universe. Although non-perturbatively it is possible to show the gauge-independence of tunneling rates by applying Nielsen identities [51] to the false-vacuum effective action [52], in perturbative calculations the lifetime of the electroweak vacuum does show gauge-dependence [53–56]. In this work, we use the Landau gauge; however, our conclusions do not change for a different choice of gauge-fixing.

The initial conditions of the RG running are taken at $\mu = M_t$ and we use the central value of the top quark mass from recent measurements performed by ATLAS and CMS, $M_t = 172.5$ GeV [57, 58]. We take $M_W = 80.384$ GeV and $M_h = 125.15$ GeV for the pole mass of the W and the Higgs bosons respectively and $\alpha_3(M_Z) = 0.1184$ for the strong coupling constant [59]. We complete the calculations using the next-to-next-to-leading order initial values for the SM couplings as given in Ref. [48]

$$g_3(\mu = M_t) = 1.1666 + 0.00314\frac{\alpha_3(M_Z)-0.1184}{0.0007} - 0.00046\left(\frac{M_t}{\text{GeV}}-173.1\right),$$

$$g_2(\mu = M_t) = 0.64779 + 0.00004\left(\frac{M_t}{\text{GeV}}-173.34\right)+0.00011\frac{M_W-80.384\text{ GeV}}{0.014\text{ GeV}},$$

$$g_Y(\mu = M_t) = 0.35830 + 0.00011\left(\frac{M_t}{\text{GeV}}-173.34\right)-0.00021\frac{M_W-80.384\text{ GeV}}{0.014\text{ GeV}},$$

$$y_t(\mu = M_t) = 0.93690 + 0.00556\left(\frac{M_t}{\text{GeV}}-173.34\right)-0.00042\frac{\alpha_3(M_Z)-0.1184}{0.0007},$$

$$\lambda_H(\mu = M_t) = 0.12604 + 0.00206\left(\frac{M_h}{\text{GeV}}-125.15\right)-0.00004\left(\frac{M_t}{\text{GeV}}-173.34\right).$$
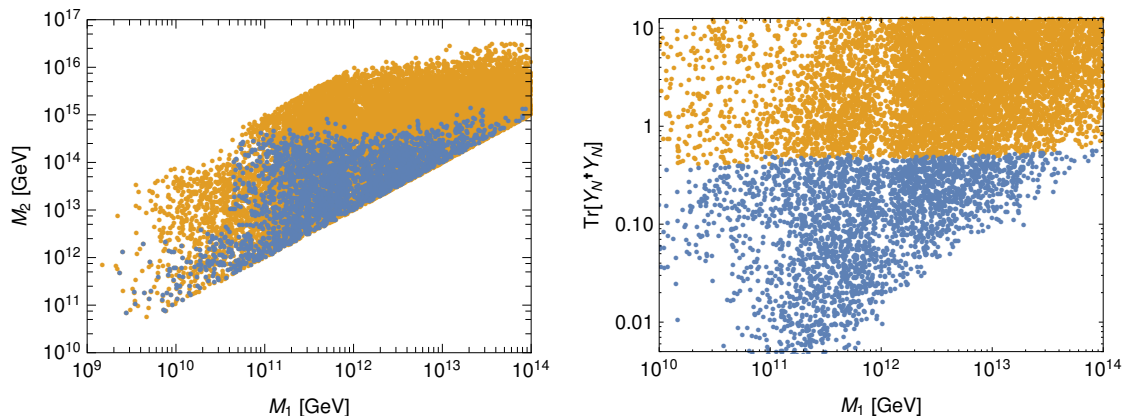
Figure 1: Scatter plot of all the points in our scan that lead to successful leptogenesis. Points in orange correspond to the points where any of the Lagrangian coefficients become non-perturbative below the Planck scale and/or lead to a metastable EW vacuum with a lifetime smaller than the age of the Universe. Points in blue satisfy these constraints up to the Planck scale as well as leading to successful leptogenesis.
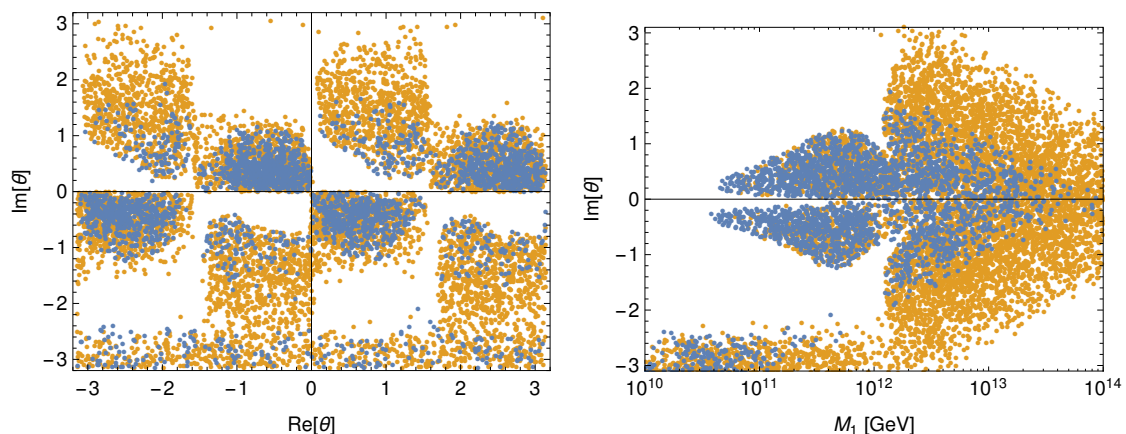
Figure 2: The colouring of the points is the same as in Fig. 1. We display the dependence on the real and imaginary part of the complex angle that enters in the R matrix.

We present our results in Figs. 1-2. As can be seen in the left panel of Fig. 1, the region with smaller M_i is less populated compared to larger M_i. This is expected since the CP-asymmetry in the decays of the heavy Majorana neutrino is proportional to its mass, M_1. As we require the model to be UV-robust up to the Planck scale we find an upper bound on the mass splitting for $M_1 > 10^{13}$ GeV, namely $\Delta M_{12}/M_1 = (M_2 - M_1)/M_1 \lesssim 10^2$ must be satisfied.

The right panel in Fig. 1 shows a scatter plot of M_1 versus $\text{Tr}[Y_N^\dagger Y_N]$ where the values for the latter are computed at the seesaw scale. This plot shows that there is an upper bound $\text{Tr}[Y_N^\dagger Y_N] \lesssim 0.57$. This bound does not significantly differ from the one found in Refs.[6, 7] for the low-scale inverse seesaw mechanism. This is because neutrino Yukawas
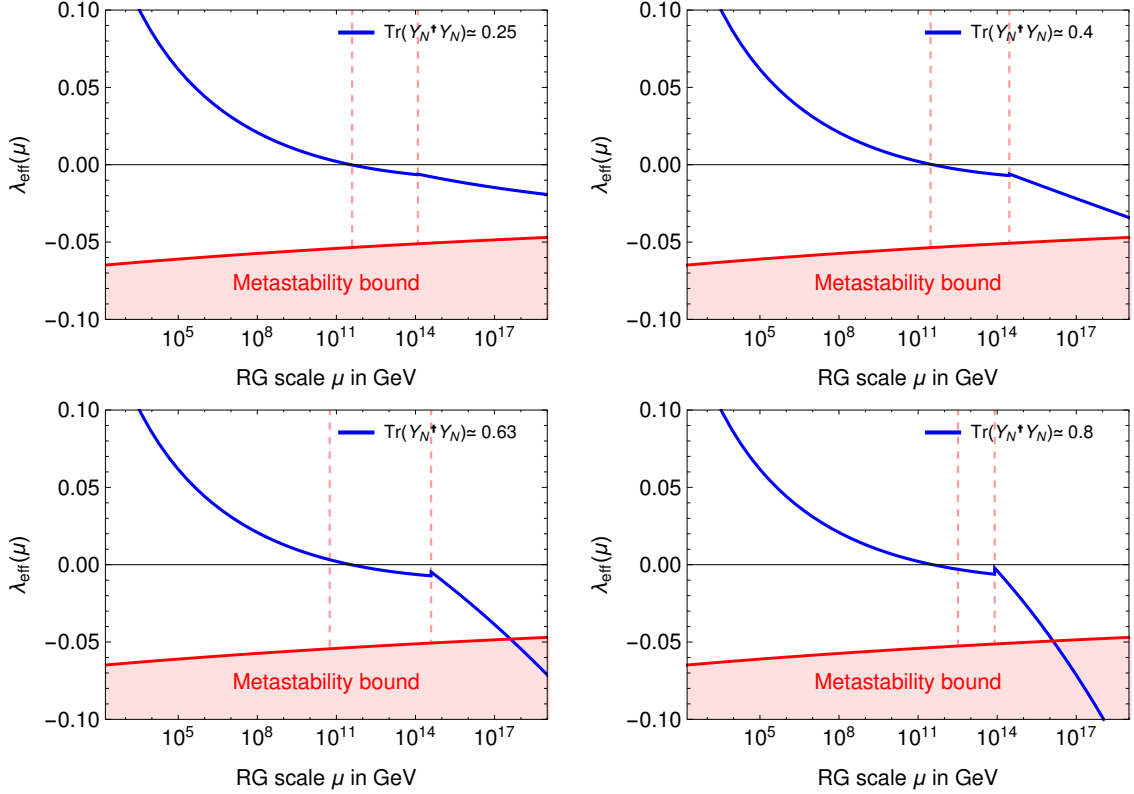
Figure 3: RG running of the effective Higgs quartic coupling as a function of the RG scale for points that lead to successful leptogenesis in the type-I seesaw mechanism. The red shaded region corresponds to the region where the lifetime of the EW vacuum is smaller than the age of the Universe. The dashed vertical lines correspond to the masses of N_1 and N_2. We show the running for different values of $\mathrm{Tr}[Y_N^\dagger Y_N]$ at the seesaw scale.

~ 0.5 have a drastic effect in driving λ_{eff} below the metastability bound. In Fig. 3 we present the running of $\lambda_{\mathrm{eff}}(\mu)$ for different values of $\mathrm{Tr}[Y_N^\dagger Y_N]$. As can be seen, for larger values of the neutrino Yukawa couplings, the effective Higgs quartic quickly crosses into the metastability bound.

In the left panel of Fig. 2, we display the points leading to successful leptogenesis in the $\mathrm{Im}[\theta]$–$\mathrm{Re}[\theta]$ plane. The periodic behaviour in $\mathrm{Re}[\theta]$ may be inferred as the analytic forms of the washout, projection matrices and CP-asymmetries are all trigonometric functions of $\mathrm{Re}[\theta]$. This periodic behaviour we observe concurs with the results of [27]. In spite of this periodicity in $\mathrm{Re}[\theta]$, the constraints from vacuum stability and perturbativity are not sensitive to the absolute magnitude of this parameter.

In the right panel of Fig. 2, we observe that for $M_1 \gtrsim 10^{12}$ GeV, there is a preference for small $\mathrm{Im}[\theta]$. This is because as M_1 is increased, $\mathrm{Im}[\theta]$ cannot grow too large (given that Yukawa couplings are exponentially enhanced with respect to this parameter) as this would

result in the Yukawa matrix entries becoming non-perturbative. Although there are some data points that satisfy all our conditions with large $\text{Im}[\theta]$ around $M_1 \sim 10^9$ GeV, we find that, in general, $|\text{Im}[\theta]| \lesssim 2$ is preferred. Ignoring effects from quantum gravity, a large portion of the points, close to 75%, that satisfy perturbativity and vacuum stability up to the Planck scale, also satisfy these constraints up to the Landau pole of the hypercharge $\sim 10^{40}$ GeV.

4.2 Asymptotically Safe $\text{SU}(3)_c$ and Leptogenesis

In this Section we consider an extension of the SM in which quantum chromodynamics (QCD) becomes asymptotically safe, rather than asymptotically free, in the UV. Asymptotic safety is achieved when the couplings in a model reach an interacting ultraviolet fixed point. These fixed points g_i^* correspond to the zeros of the β-function $\beta_i(g_i^*) = 0$. Asymptotic safety was recently shown to exist for gauge-Yukawa theories in a perturbative manner [60] and has attracted recent attention [61–67]. In [68], the authors provide a prescription for constructing extensions of the SM in which the weak and strong coupling constants reach perturbative fixed points in the UV, but the hypercharge, top Yukawa and Higgs quartic still suffer from a Landau pole.

An alternative approach to achieve an interacting UV-fixed point for a gauge coupling is to add a large number (N_F) of fermions charged under $\text{SU}(N_F)$ and perform a $1/N_F$ expansion in the computation of the β-functions[6]. In [70], a large number of vector-like fermions were added to the SM in order to ensure the asymptotic safety of the gauge couplings; nevertheless, this was computed without the inclusion of the resummation for the Yukawa and the Higgs quartic. This N_F resummation was performed for a Yukawa coupling in [71]. In [72] the resummation was performed for a Yukawa and a scalar quartic coupling. It was shown in this study that when one makes the Abelian coupling safe in the UV, the Higgs quartic is driven to large non-perturbative values. This is because the location of the pole in the resummed functions for the Yukawa and the scalar quartic has the same location as the one in the Abelian case.

We now proceed to study a model where we add a large number (N_F) of coloured fermions in order to make the $\text{SU}(3)_c$ coupling asymptotically safe, which was first proposed in [73], and study the validity of a type-I leptogenesis scenario up to the scale at which the hypercharge develops a Landau pole $\sim 10^{40}$ GeV.

With N_F flavours of vector-like coloured fermions, the UV fixed point for the gauge couplings in the SM is given by,

$$g_3^* = \frac{4\pi}{\sqrt{\Delta b_3}}, \qquad \text{and} \qquad \Delta b_3 = \frac{2}{3} N_F S_{R_3} D_{R_2}, \qquad (4.9)$$

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[6]For a different proposal to achieve asymptotic safety due to an energy cut off in the theory above which there are no quantum fluctuations see [69].
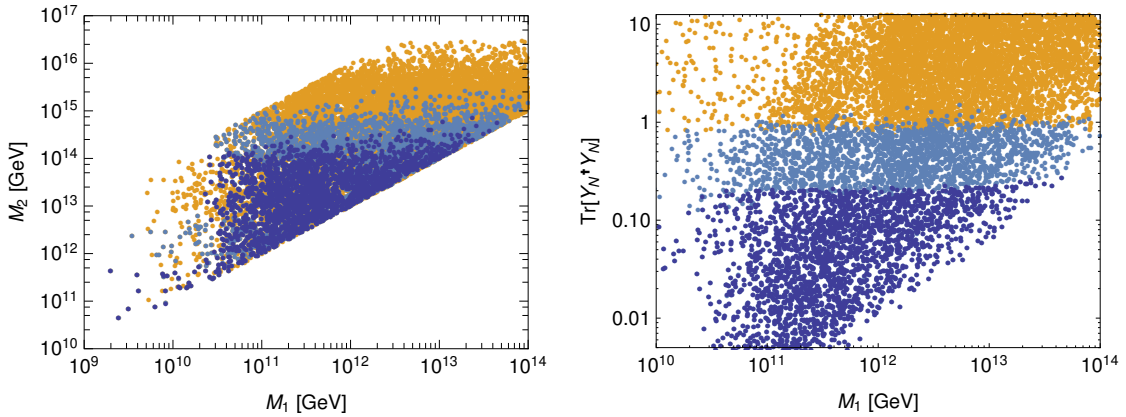
Figure 4: Scatter plot for all the points that lead to successful leptogenesis with an asymptotically safe $SU(3)_c$. Points in orange correspond to the points where any of the Lagrangian coefficients become non-perturbative at some high energy scale and/or lead to a metastable EW vacuum with a lifetime smaller than the age of the Universe. Points in blue satisfy the perturbativity condition and the EW vacuum is metastable. For points in dark blue, the electroweak vacuum is absolutely stable. The RG study is performed up to 10^{40} GeV.

where Δb_3 is the one-loop coefficient for Dirac fermions in the representation R_i, dimension D_{R_i} and Dynkin index S_{R_i}. The large-N_F-resummed beta-function has a pole at $g_3^* = 4\pi/\sqrt{\Delta b_3}$ where it diverges to negative infinity. Before reaching the pole, this resummed contribution cancels out the one-loop contribution and the β-function becomes zero. For a review on the large-N_F expansion see Ref. [74].

In order to perform the RG study we consider the one-loop beta functions with the resummed contribution at leading order in $1/N_F$, which we present in Appendix B. For this scenario, we assume that gravity will only have subleading effects on the RG running of the couplings above the Planck scale, similar to the approach of softened gravity presented in Ref. [75]. In lack of a theory of quantum gravity, we will allow ourselves such speculation.

At one-loop the N_F fermions give a positive contribution to the running of g_3 so that g_3 increases before reaching its fixed point, i.e. $g_3^* \geq g_3(M_t)$. Therefore, the negative contribution from g_3 to the running of y_t can be larger, driving y_t to smaller values compared to the SM case. As was shown in Ref. [72], the addition of $7 \leq N_F \leq 13$ Majorana colour octets stabilises the EW vacuum. Here the lower bound derives from the requirement of convergence in the $1/N_F$ expansion for fermions in the adjoint representation [76]. The achievement of vacuum stability provides a further motivation to consider such a scenario.

For our numerical scan we consider a scenario with $N_F = 13$ Majorana colour octets with common masses $M_F = 5$ TeV. This corresponds to $\Delta b_3 = 26$ and $g_3^* \simeq 2.5$, for the one-loop coefficient and the fixed point for the strong coupling respectively. The calculation of the baryon asymmetry follows the same procedure from before with the exception that
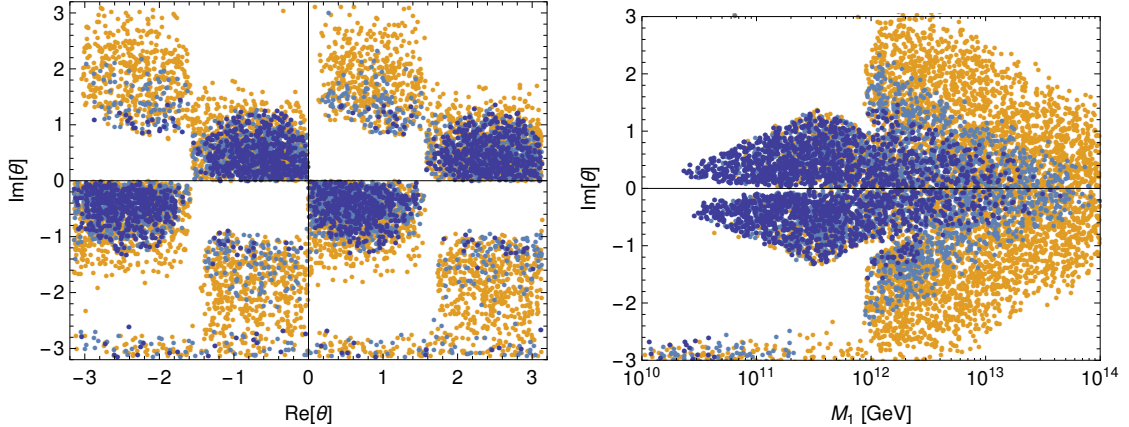
Figure 5: The colouring of the points is the same as in Fig. 4. We display the dependence on the real and imaginary part of the complex angle that enters in the R matrix.

the number of relativistic degrees of freedom is now $g_* = 288.75$ due to the inclusion of the new vector-like fermions. The modification of g_* must be accounted for in the density matrix equations; naturally, the Hubble rate is altered and this affects the decay parameter, K_1, (as detailed in Appendix A) which in turn affects the decay and washout of the lepton asymmetry. In addition, the Hubble-normalised thermal width of the tau and muon charged leptons are changed accordingly. The effect of an enlarged g_* causes suppression of the decay parameter and the washout by a factor of a few. The corresponding results can be seen in Figs. 4-5.

We would like to highlight the similarities and differences in the parameter space between the minimal type-I seesaw leptogenesis scenario and the large-N_F case considered here. However, a larger parameter region satisfy the perturbativity and metastability bounds in the large-N_F case. Specifically, the bound on the neutrino Yukawa couplings is relaxed from $\mathrm{Tr}[Y_N^\dagger Y_N] \lesssim 0.57$ (Fig. 1) in the minimal case to $\mathrm{Tr}[Y_N^\dagger Y_N] \lesssim 1.5$ in the large-N_F case (Fig. 4).

Finally, we note that the addition of a large number of fermions (N_F) that possess weak charge can make the $\mathrm{SU}(2)_L$ gauge coupling asymptotically safe. Nevertheless, in this scenario the Higgs quartic coupling violates the metastability bound. Hence we do not consider this scenario any further.

5   Conclusions

The origin of neutrino masses and the baryon asymmetry of the Universe remain two experimentally observed phenomena that cannot be explained by the Standard Model. One of the most minimal solutions to this shortcoming is the introduction of three heavy Majorana neutrinos to the SM particle spectrum. As a consequence, the active neutrinos acquire their masses via a type-I seesaw mechanism and the baryon asymmetry is produced via

CP-violating, out-of-equilibrium decays of the lightest sterile neutrino.

It is well known that in order to address the baryon asymmetry of the Universe using thermal leptogenesis with a hierarchical mass spectrum in the heavy neutrino sector requires $M_1 \gtrsim 10^9$ GeV. The region of parameter space with heavy Majorana neutrinos $M_1 \gtrsim 10^{13}$ GeV requires large Yukawa couplings and hence the model may suffer from non-perturbative coupling or violate the condition of metastability for the electroweak vacuum. In the present work we have discussed the self-consistency of thermal leptogenesis up to high scales.

We started by performing a numerical scan in order to find the points that produce sufficient baryon asymmetry, where each point in our scan reproduces the central values for the measured neutrino mass differences (with normal ordering) and mixing angles. In order to compute the baryon asymmetry we have solved the density matrix equations that are valid in the whole range of masses studied. We subsequently solved the RG equations for these points in order to assess the validity of the model up to the Planck scale.

In summary, we have identified the region of parameter space in minimal thermal leptogenesis that allow for the **(i)** electroweak vacuum to remain metastable and **(ii)** for all the couplings in the model to remain perturbative up to the Planck scale. We find that the neutrino Yukawa matrix must satisfy $\text{Tr}[Y_N^\dagger Y_N] \lesssim 0.57$ and that there is also a strong preference for $|\text{Im}[\theta]| \lesssim 2$, where θ is the complex angle that parametrises the R matrix. Detailed results can be seen in Figs.1-2. Three quarters of the points that satisfy these constraints up to the Planck scale also satisfy the constraints up to the scale at which the hypercharge develops a Landau pole $\sim 10^{40}$ GeV. Motivated by this and recent progress in making the gauge couplings in the SM asymptotically safe in the UV, we also studied a scenario where the $SU(3)_c$ coupling becomes asymptotically safe and found constraints in the parameter space that leads to successful leptogenesis. However this minimal model still suffers from a Landau pole developed by the hypercharge coupling. It remains a future task to address this issue.

Acknowledgments

A Details of Kinetic Equations

In this Appendix, we provide the formulae used within the density matrix equation Eq. (2.6). The decay and washout terms are given by

$$D_1(z) = K_1 z \frac{\mathcal{K}_1(z)}{\mathcal{K}_2(z)}, \quad \mathcal{W}_1(z) = \frac{1}{4} K_1 \mathcal{K}_1(z) z^3, \tag{A.1}$$

where $\mathcal{K}_1$ and $\mathcal{K}_2$ are modified Bessel functions of the second kind with the decay asymmetry K_1 written as

$$K_1 \equiv \frac{\tilde{\Gamma}_i}{H(T = M_1)}, \quad \tilde{\Gamma}_1 = \frac{M_1 \left(Y^\dagger Y\right)_{11}}{8\pi}. \tag{A.2}$$

These CP-asymmetry parameters may be written as [32, 36, 39, 77]

$$\epsilon_{\alpha\beta}^{(i)} = \frac{3}{32\pi \left(Y^\dagger Y\right)_{ii}} \sum_{j \neq i} \left\{ i[Y_{\alpha i} Y_{\beta j}^* (Y^\dagger Y)_{ji} - Y_{\beta i} Y_{\alpha j}^* (Y^\dagger Y)_{ij}] f_1 \left(\frac{x_j}{x_i}\right) \right. \tag{A.3}$$
$$\left. + i[Y_{\alpha i} Y_{\beta j}^* (Y^\dagger Y)_{ij} - Y_{\beta i} Y_{\alpha j}^* (Y^\dagger Y)_{ji}] f_2 \left(\frac{x_j}{x_i}\right) \right\},$$

where

$$f_1 \left(\frac{x_j}{x_i}\right) = \frac{\xi \left(\frac{x_j}{x_i}\right)}{\sqrt{\frac{x_j}{x_i}}}, \quad f_2 \left(\frac{x_j}{x_i}\right) = \frac{2}{3 \left(\frac{x_j}{x_i} - 1\right)}, \quad \xi(x) = \frac{2}{3} x \left[(1+x) \ln \left(\frac{1+x}{x}\right) - \frac{2-x}{1-x} \right]. \tag{A.4}$$

The density matrix equations of Eq. (2.6) may be expanded straightforwardly in terms of the flavour indices:

$$\frac{dn_{N_1}}{dz} = -D_1(n_{N_1} - n_{N_1}^{\text{eq}})$$

$$\frac{dn_{\tau\tau}}{dz} = \epsilon_{\tau\tau}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \mathcal{W}_1 \left\{ |Y_{\tau 1}|^2 n_{\tau\tau} + \text{Re}\left[Y_{\tau 1}^* \left(Y_{e1} n_{\tau e} + Y_{\mu 1} n_{\tau\mu}\right)\right] \right\}$$

$$\frac{dn_{\mu\mu}}{dz} = \epsilon_{\mu\mu}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \mathcal{W}_1 \left\{ |Y_{\mu 1}|^2 n_{\mu\mu} + \text{Re}\left[Y_{\mu 1}^* \left(Y_{e1} n_{\mu e} + Y_{\tau 1} n_{\tau\mu}^*\right)\right] \right\}$$

$$\frac{dn_{ee}}{dz} = \epsilon_{ee}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \mathcal{W}_1 \left\{ |Y_{e1}|^2 n_{ee} + \text{Re}\left[Y_{e1}^* \left(Y_{\mu 1} n_{\mu e}^* + Y_{\tau 1} n_{\tau e}^*\right)\right] \right\}$$

$$\frac{dn_{\tau\mu}}{dz} = \epsilon_{\tau\mu}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \left(\frac{\text{Im}\left(\Lambda_\tau\right)}{Hz} + \frac{\text{Im}\left(\Lambda_\mu\right)}{Hz}\right) n_{\tau\mu}$$
$$- \frac{\mathcal{W}_1}{2} \left\{ n_{\tau\mu} \left(|Y_{\tau 1}|^2 + |Y_{\mu 1}|^2\right) + Y_{\mu 1}^* Y_{\tau 1} \left(n_{\tau\tau} + n_{\mu\mu}\right) + Y_{e1}^* Y_{\tau 1} n_{\mu e}^* + Y_{\mu 1}^* Y_{e1} n_{\tau e} \right\}$$

$$\frac{dn_{\tau e}}{dz} = \epsilon_{\tau e}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \frac{\text{Im}\left(\Lambda_\tau\right)}{Hz} n_{\tau e}$$
$$- \frac{\mathcal{W}_1}{2} \left\{ n_{\tau e} \left(|Y_{e1}|^2 + |Y_{\tau 1}|^2\right) + Y_{e1}^* Y_{\tau 1} \left(n_{ee} + n_{\tau\tau}\right) + Y_{\mu 1}^* Y_{\tau 1} n_{\mu e} + Y_{e1}^* Y_{\mu 1} n_{\tau\mu} \right\}$$

$$\frac{dn_{\mu e}}{dz} = \epsilon_{\mu e}^{(1)} D_1(n_{N_1} - n_{N_1}^{\text{eq}}) - \frac{\text{Im}\left(\Lambda_\mu\right)}{Hz} n_{\mu e}$$
$$- \frac{\mathcal{W}_1}{2} \left\{ n_{\mu e} \left(|Y_{e1}|^2 + |Y_{\mu 1}|^2\right) + Y_{e1}^* Y_{\mu 1} \left(n_{ee} + n_{\mu\mu}\right) + Y_{e1}^* Y_{\tau 1} n_{\tau\mu}^* + Y_{\tau 1}^* Y_{\mu 1} n_{\tau e} \right\}, \tag{A.5}$$

where the total number density of the lepton asymmetry is given by the trace of this matrix, $n_{B-L} = n_{ee} + n_{\mu\mu} + n_{\tau\tau}$. In order to compare to measurement of the baryon-to-photon ratio, η_B, from cosmic microwave background measurements [43], we have to ensure n_{B-L} is properly rescaled by a factor of 0.0096 which accounts for the sphaleron conversion factor $(28/79)$ and the number density of comoving photons after recombination [19]. The off-diagonal number densities encode the *quantum correlations* between flavours differing flavours of charged leptons within the thermal bath; $n_{\alpha\beta}$ term describes the number density of ℓ_α being converted to $\overline{\ell_\beta}$.

Λ_α represents the self energy of the α-flavoured charged lepton in the thermal bath. The imaginary (real) part of the self energy is the thermal width (mass) of the lepton and will be important in describing the transition between various flavour regimes of leptogenesis. Physically, the thermal width is the mean free path of the lepton in the thermal bath.

At high temperatures, $(T > 10^{12}$ GeV$)$, the Yukawa interactions of all the charged leptons are out of equilibrium and hence there is only one effective flavour of charged lepton. As the Universe expands and cools, the τ Yukawa interactions is the first to come into equilibrium: $\Gamma_\tau \sim H$. At such temperatures the Universe can now distinguish flavour τ from 2, where 2 is a coherent superposition of e and μ flavour. In essence, the τ-state has broken the coherence of the N_1 decays. Im(Λ_τ) enters into the Boltzmann equations in the following way

$$\frac{\text{Im}(\Lambda_\tau)}{Hz} \quad \text{where} \quad H(z) \sim 1.66\sqrt{g^*}\frac{M_1^2}{M_{PL}}\frac{1}{z^2} \implies zH(z) = 1.66g^*\frac{M_1^2}{M_{PL}}\frac{1}{z} \tag{A.6}$$

where $z = \frac{M_1}{T}$. The thermal width of the τ takes the following form [36]

$$\text{Im}(\Lambda_\tau) = 8 \times 10^{-3} f_\tau^2 T, \tag{A.7}$$

Using (A.6) and (A.7) we find,

$$\frac{\text{Im}(\Lambda_\tau)}{Hz} = \frac{8 \times 10^{-3} f_\tau^2 M_{PL}}{1.66\sqrt{g^*}M_1}, \tag{A.8}$$

where $M_{PL} = 1.22 \times 10^{19}$ GeV and $g^* = 106.75$. Note that f_τ is the τ charged lepton Yukawa coupling

$$m_\tau = f_\tau v \implies f_\tau = \frac{m_\tau}{v} = \frac{1.777}{174} \sim 0.01, \tag{A.9}$$

where all the units above are in GeV. We can rewrite (A.8)

$$\frac{\text{Im}(\Lambda_\tau)}{Hz} = 4.85 \times 10^{-8}\frac{M_{PL}}{M_1}. \tag{A.10}$$

As Im$(\Lambda_\alpha)/Hz \propto 1/M_1$, the lower the scale of leptogenesis the larger impact the Hubble normalised thermal width. From Eq. (2.6), it can be seen that Im(Λ) acts in competition with the off-diagonal number densities. At lower values of M_1, the interaction rates of mediated by the SM charged lepton Yukawa couplings become increasingly significant. This

means the τ and $\bar{\tau}$ in the thermal bath are more likely to find each other and annihilate via a Higgs or gauge boson than be converted to an e or μ via a heavy Majorana neutrino. This implies the flavour correlations between the flavours of charged leptons become less significant for smaller M_1 *i.e* $n_{\alpha\beta} \to 0$ as $M_1 \to 10^6$ GeV. In a nutshell, there is a competition between the Y_N Yukawa coupling ($Y_N \ell N H$ which causes flavour oscillations) and f_α ($f_\alpha \ell_\alpha H \overline{\ell_\alpha}$ which does not mix charged lepton flavour).

B   Resummed Contribution to the RGEs with a Large Number of Flavours

We consider an extension to the SM where we introduce a large number of coloured particles, this implies that only the running of g_3 and y_t will be modified by the resummation at leading order in $1/N_F$. The resummed β-function for the strong gauge coupling can be written as,

$$\frac{\partial \alpha_3}{\partial \ln \mu} = -7 \frac{\alpha_3^2}{2\pi} + \Delta b_3 \frac{\alpha_3^2}{2\pi} + F_3\left(A\right) \frac{\alpha_3^2}{2\pi}, \tag{B.1}$$

where $A \equiv \Delta b_3 \alpha_3/(4\pi)$, $\alpha_3 = g_3^2/(4\pi)$ and Δb_3 is the one-loop contribution from the N_F fermions and is given in Eq. (4.9). The resummed contribution is given by the function [74, 78, 79]

$$F_3(A) = \int_0^A I_1(x) I_3(x) \tag{B.2}$$

$$I_1(x) \equiv \frac{(1+x)(2x-1)^2(2x-3)^2 \sin^3(\pi x)\Gamma(x-1)^2\Gamma(-2x)}{\pi^3(x-2)}, \tag{B.3}$$

$$I_3(x) \equiv \frac{4}{3} + \frac{3(20 - 43x + 32x^2 - 14x^3 + 4x^4)}{2(2x-1)(2x-3)(1-x^2)}. \tag{B.4}$$

The β-function for the top Yukawa coupling is modified as follows,

$$(4\pi)^2 \frac{dy_t}{d\ln\mu} = \frac{9}{2}y_t^3 - y_t\left(8g_3^2 R_y(A_3) + \frac{9}{4}g_2^2 + \frac{17}{12}g_Y^2\right), \tag{B.5}$$

where the resummed function is given by,

$$R_y(A) = \frac{2(3-2A)^2(2-A)\sin(\pi A)\Gamma(2-2A)}{9\pi A \Gamma(3-A)^2}, \tag{B.6}$$

and hence at the fixed point, where $\alpha_3^* = 4\pi/\Delta b_3$, $R_y(1) = 1/9$. For details on the class of diagrams that contribute to the resummation and a detailed derivation of the resummed function $R_y(A)$ we refer the reader to Refs. [71, 72]. For the scenario considered in Section 4.2 we solve the one-loop RG equations (4.1)-(4.4) with the equations for g_3 and y_t replaced by (B.1) and (B.5) respectively.

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