Dark Energy Survey Year 1 Results: Cosmological Constraints from Galaxy Clustering and Weak Lensing


(DES Collaboration)
We present cosmological results from a combined analysis of galaxy clustering and weak gravitational lensing, using 1321 deg$^2$ of $griz$ imaging data from the first year of the Dark Energy Survey (DES Y1). We combine three two-point functions: (i) the cosmic shear correlation function of 26 million source galaxies in four redshift bins, (ii) the galaxy angular autocorrelation function of 650,000 luminous red galaxies in five redshift bins, and (iii) the galaxy-shear cross-correlation of luminous red galaxy positions and source galaxy shears. To demonstrate the robustness of these results, we use independent pairs of galaxy shape, photometric redshift estimation and validation, and likelihood analysis pipelines. To prevent confirmation bias, the bulk of the analysis was carried out while “blind” to the true results; we describe an extensive suite of systematics checks performed and passed during this blinded phase. The data are modeled in flat ΛCDM and wCDM cosmologies, marginalizing over 20 nuisance parameters, varying 6 (for ΛCDM) or 7 (for wCDM) cosmological parameters including the neutrino mass density and including the 457 × 457 element analytic covariance matrix. We find consistent cosmological results from these three two-point functions, and from their combination obtain $S_8 \equiv \sigma_8 (\Omega_m/0.3)^{0.5} = 0.783^{+0.023}_{-0.022}$ and $\Omega_m = 0.264^{+0.014}_{-0.013}$ for ΛCDM; for wCDM, we find $S_8 = 0.794^{+0.029}_{-0.027}$, $\Omega_m = 0.279^{+0.023}_{-0.022}$, and $w = -0.80^{+0.27}_{-0.22}$ at 68% CL. The precision of these DES Y1 results rivals that from the Planck cosmic microwave background measurements, allowing a comparison of structure in the very early and late Universe on equal terms. Although the DES Y1 best-fit values for $S_8$ and $\Omega_m$ are lower than the central values from Planck for both ΛCDM and wCDM, the Bayes factor indicates that the DES Y1 and Planck data sets are consistent with each other in the context of ΛCDM. Combining DES Y1 with Planck, Baryonic Acoustic Oscillation measurements from SDSS, 6dF, and BOSS, and type Ia supernovae from the Joint Lightcurve Analysis (JLA) dataset, we derive very tight constraints on cosmological parameters: $S_8 = 0.799^{+0.024}_{-0.020}$ and $\Omega_m = 0.301^{+0.016}_{-0.008}$ in ΛCDM, and $w = -1.00^{+0.54}_{-0.05}$ in wCDM. Upcoming DES analyses will provide more stringent tests of the ΛCDM model and extensions such as a time-varying equation of state of dark energy or modified gravity.

I. INTRODUCTION

The discovery of cosmic acceleration [1,2] established the Cosmological Constant (Λ) [3] + Cold Dark Matter (ΛCDM) model as the standard cosmological paradigm that explains a wide variety of phenomena, from the origin and evolution of large-scale structure to the current epoch of accelerated expansion [4,5]. The successes of ΛCDM, however, must be balanced by its apparent implausibility: three new entities beyond the Standard Model of particle physics — one that drove the early epoch of inflation; another that serves as dark matter; and a third that is driving the current epoch of acceleration — are required, none of them easily connected to the rest of physics [6]. Ongoing and planned cosmic surveys are designed to test ΛCDM and more generally to shed light on the mechanism driving the current epoch of acceleration, be it the vacuum energy associated with the cosmological constant, another form of dark energy, a modification of General Relativity, or something more drastic.

The Dark Energy Survey (DES) [7] is an on-going, five-year survey that, when completed, will map 300 million galaxies and tens of thousands of galaxy clusters in five filters ($grizY$) over 5000 deg$^2$, in addition to discovering several thousand type Ia supernovae in a 27 deg$^2$ time-domain survey. DES will use several cosmological probes to test ΛCDM; galaxy clustering and weak gravitational lensing are two of the most powerful. Jointly, these complementary probes sample the underlying matter density field through the galaxy population and the distortion of light due to gravitational lensing. In this paper, we use data on this combination from the first year (Y1) of DES to constrain ΛCDM and its simplest extension — wCDM, having a free parameter for the dark energy equation of state.

The spatial distribution of galaxies in the Universe, and its temporal evolution, carry important information about the physics of the early Universe, as well as details of structure evolution in the late Universe, thereby testing some of the most precise predictions of ΛCDM. Indeed, measurements of the galaxy two-point correlation function, the lowest-order statistic describing the galaxy spatial distribution, provided early evidence for the ΛCDM model [8,19]. The data-model comparison in this case depends upon uncertainty in the galaxy bias [20], the relation between the galaxy spatial distribution and the theoretically predicted matter distribution.

In addition to galaxy clustering, weak gravitational lensing has become one of the principal probes of cosmology. While the interpretation of galaxy clustering is complicated by galaxy bias, weak lensing provides direct measurement of the mass distribution via cosmic shear, the correlation of the apparent shapes of pairs of galaxies induced by foreground large-scale structure. Further information on the galaxy bias is provided by galaxy–galaxy lensing, the cross-correlation of lens galaxy positions and source galaxy shapes.

The shape distortions produced by gravitational lensing, while cosmologically informative, are extremely difficult to measure, since the induced source galaxy ellipticities are at the percent level, and a number of systematic effects can obscure the signal. Indeed, the first detections of weak lensing were made by cross-correlating observed shapes of source galaxies with massive foreground lenses [21,22]. A watershed moment came in the year 2000 when four research groups nearly simultaneously announced the first detections of cosmic shear [23–26]. While these and subsequent weak lensing measurements are also consistent with ΛCDM, only recently have they begun to provide competitive constraints
on cosmological parameters. Galaxy–galaxy lensing measurements have also matured to the point where their combination with galaxy clustering breaks degeneracies between the cosmological parameters and bias, thereby helping to constrain dark energy. The combination of galaxy clustering, cosmic shear, and galaxy–galaxy lensing measurements powerfully constrains structure formation in the late universe. As for cosmological analyses of samples of galaxy clusters, redshift space distortions in the clustering of galaxies and other measurements of late-time structure, a primary test is whether these are consistent, in the framework of LCDM, with measurements from cosmic microwave background (CMB) experiments that are chiefly sensitive to early-universe physics.

The main purpose of this paper is to combine the information from galaxy clustering and weak lensing, using the galaxy and shear correlation functions as well as the galaxy-shear cross-correlation. It has been recognized for more than a decade that such a combination contains a tremendous amount of complementary information, as it is remarkably resilient to the presence of nuisance parameters that describe systematic errors and non-cosmological information. It is perhaps simplest to see that the combined analysis could separately solve for galaxy bias and the cosmological parameters; however, it can also internally solve for (or, self-calibrate) the systematics associated with photometric redshifts, intrinsic alignment, and a wide variety of other effects. Such a combined analysis has recently been executed by combining the KiDS 450 deg$^2$ weak lensing survey with two different spectroscopic galaxy surveys. While these multi-probe analyses still rely heavily on prior information about the nuisance parameters, obtained through a wide variety of physical tests and simulations, this approach does significantly mitigate potential biases due to systematic errors and will likely become even more important as statistical errors continue to drop. The multi-probe analyses also extract more precise information about cosmology from the data than any single measurement could.

Previously, the DES collaboration analyzed data from the Science Verification (SV) period, which covered 139 deg$^2$, carrying out several pathfinding analyses of galaxy clustering and gravitational lensing, along with numerous others. The DES Y1 data set analyzed here covers about ten times more area, albeit shallower, and provides 650,000 lens galaxies and the shapes of 26 million source galaxies, each of them divided into redshift bins. The lens sample comprises bright, red-sequence galaxies, which have secure photometric redshift (photo-z) estimates. We measure three two-point functions from these data: (i) $w(\theta)$, the angular correlation function of the lens galaxies; (ii) $\gamma_2(\theta)$, the correlation of the tangential shear of sources with lens galaxy positions; and (iii) $\xi_{\ell}(\theta)$, the correlation functions of different components of the ellipticities of the source galaxies. We use these measurements only on large angular scales, for which we have verified that a relatively simple model describes the data, although even with this restriction we must introduce twenty parameters to capture astrophysical and measurement-related systematic uncertainties.

This paper is built upon, and uses tools and results from, eleven other papers:

- Ref. [79], which describes the theory and parameter-fitting methodologies, including the binning and modeling of all the two point functions, the marginalization of astrophysical and measurement related uncertainties, and the ways in which we calculate the covariance matrix and obtain the ensuing parameter constraints;
- Ref. [80], which applies this methodology to image simulations generated to mimic many aspects of the Y1 data sets;
- a description of the process by which the value-added galaxy catalog (Y1 Gold) is created from the data and the tests on it to ensure its robustness [81];
- a shape catalog paper, which presents the two shape catalogs generated using two independent techniques and the many tests carried out to ensure that residual systematic errors in the inferred shear estimates are sufficiently small for Y1 analyses [82];
- Ref. [83], which describes how the redshift distributions of galaxies in these shape catalogs are estimated from their photometry, including a validation of these estimates by means of COSMOS multi-band photometry;
- three papers [84–86] that describe the use of angular cross-correlation with samples of secure redshifts to independently validate the photometric redshift distributions of lens and source galaxies;
- Ref. [87], which measures and derives cosmological constraints from the cosmic shear signal in the DES Y1 data and also addresses the question of whether DES lensing data are consistent with lensing results from other surveys;
- Ref. [88], which describes galaxy–galaxy lensing results, including a wide variety of tests for systematic contamination and a cross-check on the redshift distributions of source galaxies using the scaling of the lensing signal with redshift;
- Ref. [89], which describes the galaxy clustering statistics, including a series of tests for systematic contamination. This paper also describes updates to the red-MaGiC algorithm used to select our lens galaxies and to estimate their photometric redshifts.

Armed with the above results, this paper presents the most stringent cosmological constraints from a galaxy imaging survey to date and, combined with external data, the most stringent constraints overall.

One of the guiding principles of the methods developed in these papers is redundancy: we use two independent shape measurement methods that are independently calibrated, several photometric redshift estimation and validation
techniques, and two independent codes for predicting our signals and performing a likelihood analysis. Comparison of these, as described in the above papers, has been an important part of the verification of each step of our analysis.

The plan of the paper is as follows. §II gives an overview of the data used in the analysis, while §III presents the two-point statistics that contain the relevant information about cosmological parameters. §IV describes the methodology used to compare these statistics to theory, thereby extracting cosmological results. We validated our methodology while remaining blinded to the results of the analyses; this process is described in §V and some of the tests that convinced us to unblind are recounted in Appendix A. §VI presents the cosmological results from these three probes as measured by DES in the context of two models, ΛCDM and ωCDM, while §VII compares DES results with those from other experiments, offering one of the most powerful tests to date of ΛCDM. Then, we combine DES with external data sets with which it is consistent to produce the tightest constraints yet on cosmological parameters. Finally, we conclude in §VIII. Appendix B presents further evidence of the robustness of our results.

II. DATA

DES uses the 570-megapixel Dark Energy Camera (DECam [90]), built by the collaboration and deployed on the Cerro Tololo Inter-American Observatory (CTIO) 4m Blanco telescope in Chile, to image the South Galactic Cap in the grizY filters. In this paper, we analyze DECam images taken from August 31, 2013 to February 9, 2014 (“DES Year 1” or Y1), covering 1786 square degrees in griz after coaddition and before masking [81]. The data were processed through the DES Data Management (DESDM) system [91–94], which detrends and calibrates the raw DES images, combines individual exposures to create coadded images, and detects and catalogs astrophysical objects. Further vetting and subsampling of the DESDM data products was performed by [81] to produce a high-quality object catalog (Y1 Gold) augmented by several ancillary data products including a star/galaxy separator. With up to 4 exposures per filter per field in Y1, and individual griz exposures of 90 sec and Y exposures of 45 sec, the characteristic 10σ limiting magnitude for galaxies is $g = 23.4$, $r = 23.2$, $i = 22.5$, $z = 21.8$, and $Y = 20.1$ [81]. Additional analyses produced catalogs of red galaxies, photometric-redshift estimates, and galaxy shape estimates, as described below.

As noted in §II, we use two samples of galaxies in the current analysis: lens galaxies, for the angular clustering measurement, and source galaxies, whose shapes we estimate and correlate with each other (“cosmic shear”). The tangential shear is measured for the source galaxies about the positions of the lens galaxies (galaxy–galaxy lensing).

A. Lens Galaxies

We rely on redMaGiC galaxies for all galaxy clustering measurements [89] and as the lens population for the galaxy–galaxy lensing analysis [85]. They have the advantage of being easily identifiable, relatively strongly clustered, and of having relatively small photometric-redshift errors; they are selected using a simple algorithm [85]:

1. Fit every galaxy in the survey to a red-sequence template and compute the corresponding best-fit redshift $z_{\text{red}}$.
2. Evaluate the goodness-of-fit $\chi^2$ of the red-sequence template and the galaxy luminosity, using the assigned photometric redshift.
3. Include the galaxy in the redMaGiC catalog if and only if it is bright ($L \geq L_{\text{min}}$) and the red-sequence template is a good fit ($\chi^2 \leq \chi^2_{\text{max}}$).

In practice, we do not specify $\chi^2_{\text{max}}$ but instead demand that the resulting galaxy sample have a constant comoving density as a function of redshift. Consequently, redMaGiC galaxy selection depends upon only two parameters: the selected luminosity threshold, $L_{\text{min}}$, and the comoving density, $n$, of the sample. Of course, not all combinations of parameters are possible: brighter galaxy samples must necessarily be less dense.

Three separate redMaGiC samples were generated from the Y1 data, referred to as the high-density, high-luminosity, and higher-luminosity samples. The corresponding luminosity threshold and comoving densities for these samples are, respectively, $L_{\text{min}} = 0.5L_\odot$, $L_\odot$, and $1.5L_\odot$, and $n = 10^{-3}$, $4 \times 10^{-4}$, and $10^{-4}$ galaxies/(h$^{-1}$Mpc)$^3$, where $h = H_0/(100$ km sec$^{-1}$ Mpc$^{-1})$ parametrizes the Hubble constant. Naturally, brighter galaxies are easier to map at higher redshifts than are the dimmer galaxies. These galaxies are placed in five nominally disjoint redshift bins. The lowest three bins $z = [(0.15 - 0.3), (0.3 - 0.45), (0.45 - 0.6)]$ are high-density, while the galaxies in the two highest redshift bins ($(0.6 - 0.75)$ and $(0.75 - 0.9)$) are high-luminosity and higher-luminosity, respectively. The estimated redshift distributions of these five binned lens galaxy samples are shown in the upper panel of Figure 1.

The clustering properties of these galaxies are an essential part of this combined analysis, so great care is taken in [89] to ensure that the galaxy maps are not contaminated by systematic effects. This requires the shallowest or otherwise irregular or patchy regions of the total 1786 deg$^2$ Y1 area to be masked, leaving a contiguous 1321 deg$^2$ as the area for the analysis, the region called “SPT” in [81]. The mask derived for the lens sample is also applied to the source sample.

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2 Here and throughout, whenever a cosmology is required, we use ΛCDM with the parameters given in Table 1 of [19].
B. Source Galaxies

1. Shapes

Gravitational lensing shear is estimated from the statistical alignment of shapes of source galaxies, which are selected from the Y1 Gold catalog \[81\]. In DES Y1, we measure galaxy shapes and calibrate those measurements by two independent and different algorithms, METACALIBRATION and IM3SHAPE, as described in \[82\].

METACALIBRATION \[96\] \[97\] measures shapes by simultaneously fitting a 2D Gaussian model for each galaxy to the pixel data for all available r-, i-, and z-band exposures, convolving with the point-spread functions (PSF) appropriate to each exposure. This procedure is repeated on versions of these images that are artificially sheared, i.e. de-convolved, distorted by a shear operator, and re-convolved by a symmetrized version of the PSF. By means of these, the response of the shape measurement to gravitational shear is measured from the images themselves, an approach encoded in METACALIBRATION.

METACALIBRATION also includes an algorithm for calibration of shear-dependent selection effects of galaxies, which could bias shear statistics at the few percent level otherwise, by measuring on both unsheared and sheared images all those galaxy properties that are used to select, bin and weight galaxies in the catalog. Details of the practical application of these corrections to our lensing estimators are given in \[82\] \[87\] \[88\] \[97\].

IM3SHAPE estimates a galaxy shape by determining the maximum likelihood set of parameters from fitting either a bulge or a disc model to each object’s r-band observations \[98\]. The maximum likelihood fit, like the Gaussian fit with METACALIBRATION, provides only a biased estimator of shear. For IM3SHAPE, this bias is calibrated using a large suite of image simulations that resemble the DES Y1 data set closely \[82\] \[99\].

Potential biases in the inferred shears are quantified by multiplicative shear-calibration parameters $m^i$ in each source redshift bin $i$, such that the measured shear $\gamma_{\text{meas}} = (1 + m^i)\gamma_{\text{true}}$. The $m^i$ are free parameters in the cosmological inferences, using prior constraints on each as determined from the extensive systematic-error analyses in \[82\]. These shear-calibration priors are listed in Table I. The overall METACALIBRATION calibration is accurate at the level of 1.3 percent. This uncertainty is dominated by the impact of neighboring galaxies on shape estimates. For tomographic measurements, the widths of the overall $m^i$ prior is increased to yield a per-bin uncertainty in $m^i$, to account conservatively for possible correlations of $m^i$ between bins [see appendices of \[82\] \[83\]. This yields the 2.3 percent prior per redshift bin shown in Table I. The IM3SHAPE prior is determined with 2.5 percent uncertainty for the overall sample [increased to a 3.5 percent prior per redshift bin], introduced mostly by imperfections in the image simulations.

In both catalogs, we have applied conservative cuts, for instance on signal-to-noise ratio and size, that reduce the number of galaxies with shape estimates relative to the Y1 Gold input catalog significantly. For METACALIBRATION, we obtain 35 million galaxy shape estimates down to an r-band magnitude of $\approx 23$. Of these, 26 million are inside the restricted area and redshift bins of this analysis. Since its calibration is more secure, and its number density is higher than that of IM3SHAPE, we use the METACALIBRATION catalog for our fiducial analysis.

2. Photometric redshifts

Redshift probability distributions are also required for source galaxies in cosmological inferences. For each source galaxy, the probability density that it is at redshift $z$, $p_{\text{BPZ}}(z)$, is obtained using a modified version of the BPZ algorithm \[100\], as detailed in \[83\]. Source galaxies are placed

<table>
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<th>Parameter</th>
<th>Prior</th>
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<tbody>
<tr>
<td>$\Omega_m$</td>
<td>flat (0.1, 0.9)</td>
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<tr>
<td>$A_X$</td>
<td>flat ($5 \times 10^{-10}$, $5 \times 10^{-9}$)</td>
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<tr>
<td>$n_A$</td>
<td>flat (0.87, 1.07)</td>
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<tr>
<td>$\delta b$</td>
<td>flat (0.03, 0.07)</td>
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<tr>
<td>$h$</td>
<td>flat (0.55, 0.91)</td>
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<tr>
<td>$\Omega_L h^2$</td>
<td>flat ($5 \times 10^{-4}$, $10^{-2}$)</td>
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<tr>
<td>$w$</td>
<td>flat ($-2$, $-0.33$)</td>
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<th>Lens Galaxy Bias</th>
<th>Prior</th>
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<td>$b_i (i = 1, 3)$</td>
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<td>$A_{1A}(z) = A_{1A}[(1 + z)/1.62]\eta_{1A}$</td>
<td>flat ($-5$, 5)</td>
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<td>$\eta_{1A}$</td>
<td>flat ($-5$, 5)</td>
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<th>Lens photo-z shift (red sequence)</th>
<th>Prior</th>
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<tr>
<td>$\Delta z_{\text{1}}$</td>
<td>Gauss (0.001, 0.008)</td>
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<tr>
<td>$\Delta z_{\text{2}}$</td>
<td>Gauss (0.002, 0.007)</td>
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<tr>
<td>$\Delta z_{\text{3}}$</td>
<td>Gauss (0.001, 0.007)</td>
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<tr>
<td>$\Delta z_{\text{4}}$</td>
<td>Gauss (0.003, 0.01)</td>
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<tr>
<td>$\Delta z_{\text{5}}$</td>
<td>Gauss (0.0, 0.01)</td>
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<th>Source photo-z shift</th>
<th>Prior</th>
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<tbody>
<tr>
<td>$\Delta z_{\text{1}}$</td>
<td>Gauss ($-0.001$, 0.016)</td>
</tr>
<tr>
<td>$\Delta z_{\text{2}}$</td>
<td>Gauss ($-0.019$, 0.013)</td>
</tr>
<tr>
<td>$\Delta z_{\text{3}}$</td>
<td>Gauss ($+0.009$, 0.011)</td>
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<tr>
<td>$\Delta z_{\text{4}}$</td>
<td>Gauss ($-0.018$, 0.022)</td>
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<td>$m^1_{\text{METACALIBRATION}}(i = 1, 4)$</td>
<td>Gauss (0.012, 0.023)</td>
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<tr>
<td>$m^1_{\text{IM3SHAPE}}(i = 1, 4)$</td>
<td>Gauss (0.0, 0.035)</td>
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* The lens photo-z priors changed slightly after unblinding due to changes in the cross-correlation analysis, as described in \[83\]; we checked that these changes did not impact our results.
in one of four redshift bins, \( z = [(0.2 - 0.43), (0.43 - 0.63), (0.63 - 0.9), (0.9 - 1.3)] \), based upon the mean of their \( p_{BPZ}(z) \) distributions. As described in [83, 87] and [88], in the case of METACALIBRATION these bin assignments are based upon photo-z estimates derived using photometric measurements made by the METACALIBRATION pipeline in order to allow for correction of selection effects.

We denote by \( n_i^{BPZ}(z) \) an initial estimate of the redshift distribution of the \( N_i \) galaxies in bin \( i \) produced by randomly drawing a redshift \( z \) from the probability distribution \( p_{BPZ}(z) \) of each galaxy assigned to the bin, and then bin all these \( N_i \) redshifts into a histogram. For this step, we use a BPZ estimate based on the optimal flux measurements from the multi-epoch multi-object fitting procedure (MOF) described in [81].

For both the source and the lens galaxies, uncertainties in the redshift distribution are quantified by assuming that the true redshift distribution \( n_i(z) \) in bin \( i \) is a shifted version of the photometrically derived distribution:

\[
n_i(z) = n_i^{BPZ}(z - \Delta z^i), \tag{II.1}
\]

with the \( \Delta z^i \) being free parameters in the cosmological analyses. Prior constraints on these shift parameters are derived in two ways.

First, we constrain \( \Delta z^i \) from a matched sample of galaxies in the COSMOS field, as detailed in [83]. Reliable redshift estimates for nearly all DES-selectable galaxies in the COSMOS field are available from 30-band imaging [101]. We select and weight a sample of COSMOS galaxies representative of the DES sample with successful shape measurements based upon their color, magnitude, and pre-seeing size. The mean redshift of this COSMOS sample is our estimate of the true mean redshift of the DES source sample, with statistical and systematic uncertainties detailed in [83]. The sample variance in the best-fit \( \Delta z^i \) from the small COSMOS field is reduced, but not eliminated, by reweighting the COSMOS galaxies to match the multiband flux distribution of the DES source sample.

Second, the \( \Delta z^i \) of both lens and source samples are further constrained by the angular cross-correlation of each with a distinct sample of galaxies with well-determined redshifts. The \( \Delta z^i \) for the three lowest-redshift lens galaxy samples are constrained by cross-correlation of redMaGiC with spectroscopic redshifts [85] obtained in the overlap of DES Y1 with Stripe 82 of the Sloan Digital Sky Survey. The \( \Delta z^i \) for the three lowest-redshift source galaxy bins are constrained by cross-correlating the sources with the redMaGiC sample, since the redMaGiC photometric redshifts are much more accurate and precise than those of the sources [84, 86]. The \( z < 0.85 \) limit of the redMaGiC sample precludes use of cross-correlation to constrain \( \Delta z^i \), so its prior is determined solely by the reweighted COSMOS galaxies.

For the first three source bins, both methods yield an estimate of \( \Delta z^i \), and the two estimates are compatible, so we combine them to obtain a joint constraint. The priors derived for both lens and source redshifts are listed in Table I. The resulting estimated redshift distributions are shown in Figure 1.

Ref. [83] and Figure 20 in Appendix B demonstrate that, at the accuracy attainable in DES Y1, the precise shapes of the \( n_i(z) \) functions have negligible impact on the inferred cosmology as long as the mean redshifts of every bin, parametrized by the \( \Delta z^i \), are allowed to vary. As a consequence, the cosmological inferences are insensitive to the choice of photometric redshift algorithm used to establish the initial \( n_i^{BPZ}(z) \) of the bins.

![Figure 1](image-url)

FIG. 1. Estimated redshift distributions of the lens and source galaxies used in the Y1 analysis. The shaded vertical regions define the bins: galaxies are placed in the bin spanning their mean photo-z estimate. We show both the redshift distributions of galaxies in each bin (colored lines) and their overall redshift distributions (black lines).

Note that source galaxies are chosen via two different pipelines IM3SHAPE and METACALIBRATION, so their redshift distributions and total numbers differ (solid vs. dashed lines).

III. TWO-POINT MEASUREMENTS

We measure three sets of two-point statistics: the auto-correlation of the positions of the redMaGiC lens galaxies, the cross-correlation of the lens positions with the shear of the source galaxies, and the two-point correlation of the source galaxy shear field. Each of the three classes of statistics is measured using treecorr [102] in all pairs of redshift bins of the galaxy samples and in 20 log-spaced bins of angular separation \( 2.5 < \theta < 250' \), although we exclude some of the scales and cross-correlations from our fiducial data vector (see section IV). Figures 2 and 3 show these measurements and our best-fit ΛCDM model.

A. Galaxy Clustering: \( w(\theta) \)

The inhomogeneous distribution of matter in the Universe is traced by galaxies. The overabundance of pairs at angular separation \( \theta \) above that expected in a random distribution,
$w(\theta)$, is one of the simplest measurements of galaxy clustering. It quantifies the strength and scale dependence of the clustering of galaxies, which in turn reflects the clustering of matter.

The upper panel of Figure 2 shows the angular correlation function of the redMaGiC galaxies in the five lens redshift bins described above. As described in [89], these correlation functions were computed after quantifying and correcting for spurious clustering induced by each of multiple observational variables. Figure 2 shows the data with the error bars set equal to the square root of the diagonal elements of the covariance matrix, but we note that data points in nearby angular bins are highly correlated. Indeed, as can be seen in Figure 5 of [79], in the lowest redshift bins the correlation coefficient between almost all angular bins is close to unity; at higher redshift, the measurements are highly correlated only over the adjacent few angular bins. The solid curve in Figure 2 shows the best-fit prediction from $\Lambda$CDM after fitting to all three two-point functions. In principle, we could also use the angular cross-correlations between galaxies in different redshift bins in the analysis, but the amount of information in these cross-bin two-point functions is quite small and would require substantially enlarging the covariance matrix, so we use only the auto-correlations.

B. Galaxy–galaxy lensing: $\gamma_i(\theta)$

The shapes of background source galaxies are distorted by the mass associated with foreground lenses. The characteristic distortion is a tangential shear, with the source galaxy ellipticities oriented perpendicular to the line connecting the foreground and background galaxies. This shear, $\gamma_i(\theta)$, is sensitive to the mass associated with the foreground galaxies. On scales much larger than the sizes of parent halos of the galaxies, it is proportional to the lens galaxy bias parameters $b^i$ in each lens bin which quantifies the relative clumping of matter and galaxies. The lower panels of Figure 2 show the measurements of galaxy–galaxy lensing in all pairs of lens-source tomographic bins, including the model prediction for our best-fit parameters. The plots include bin pairs for which the lenses are nominally behind the sources (those towards the upper right), so might be expected to have zero signal. Although the signals for these bins are expected to be small, they can still be useful in constraining the intrinsic alignment parameters in our model (see, e.g., [103]).

In [88], we carried out a number of null tests to ensure the robustness of these measurements, none of which showed evidence for significant systematic uncertainties besides the ones characterized by the nuisance parameters in this analysis. The model fits the data well. Even the fits that appear quite bad are misleading because of the highly off-diagonal covariance matrix. For the nine data points in the 3–1 bin, for example, $\chi^2 = 14$, while $\chi^2$ would be 30 if the off-diagonal elements were ignored.

C. Cosmic shear: $\xi_{\pm}(\theta)$

The two-point statistics that quantify correlations between the shapes of galaxies are more complex, because they are the products of the components of a spin-2 tensor. Therefore, a pair of two-point functions are used to capture the relevant information: $\xi_+(\theta)$ and $\xi_-(\theta)$ are the sum and difference of the products of the tangential and cross components of the shear, measured with respect to the line connecting each galaxy pair. For more details, see [87] or earlier work in Refs [104–111]. Figure 3 shows these functions for different pairs of tomographic bins.

As in Figure 2, the best-fit model prediction here includes the impact of intrinsic alignment; the best-fit shifts in the photometric redshift distributions; and the best-fit values of shear calibration. The one-dimensional posteriors on all of these parameters are shown in Figure 19 in Appendix A.

IV. ANALYSIS

A. Model

To extract cosmological information from these two-point functions, we construct a model that depends upon both cosmological parameters and astrophysical and observational nuisance parameters. The cosmological parameters govern the expansion history as well as the evolution and scale dependence of the matter clustering amplitude (as quantified, e.g., by the power spectrum). The nuisance parameters account for uncertainties in photometric redshifts, shear calibration, the bias between galaxies and mass, and the contribution of intrinsic alignment to the shear spectra. §IV B will enumerate these parameters, and our priors on them are listed in Table I. Here, we describe how the two-point functions presented in §III are computed in the model.

1. Galaxy Clustering: $w(\theta)$

The lens galaxies are assumed to trace the mass distribution with a simple linear biasing model. Although this need not be true in general, the validity of this assumption over the scales used in this analysis was demonstrated in [79, 88], and [89]. The measured angular correlation function of the galaxies is thus related to the matter correlation function by a simple factor of $(b^i)^2$ in each redshift bin $i$. The theoretical prediction for $w^i(\theta)$ in bin $i$ depends upon the galaxy redshift distribution of that bin according to

$$w^i(\theta) = (b^i)^2 \int \frac{dl}{2\pi} J_0(\theta) \int d\chi \frac{[n_i(z(\chi))]^2}{\chi^2 H(z)} P_{\text{NL}} \left( \frac{l + 1/2}{\chi}, z(\chi) \right), \quad (IV.1)$$

where the speed of light has been set to one; $\chi(z)$ is the comoving distance to that redshift (in a flat universe, which is
FIG. 2. Top panels: scaled angular correlation function, $\theta w(\theta)$, of redMaGiC galaxies in the five redshift bins in the top panel of Figure 1 from lowest (left) to highest redshift (right) [89]. The solid lines are predictions from the $\Lambda$CDM model that provides the best fit to the combined three two-point functions presented in this paper. Bottom panels: scaled galaxy–galaxy lensing signal, $\theta_{\gamma\ell}$ (galaxy-shear correlation), measured in DES Y1 in four source redshift bins induced by lens galaxies in five redMaGiC bins [88]. Columns represent different lens redshift bins while rows represent different source redshift bins, so e.g., bin labelled 12 is the signal from the galaxies in the second source bin lensed by those in the first lens bin. The solid curves are again our best-fit $\Lambda$CDM prediction. In all panels, shaded areas display the angular scales that have been excluded from our cosmological analysis (see §IV).
FIG. 3. The cosmic shear correlation functions $\xi_+$ (top panel) and $\xi_-$ (bottom panel) in DES Y1 in four source redshift bins, including cross correlations, measured from the METACALIBRATION shear pipeline (see [87] for the corresponding plot with IM3SHAPE); pairs of numbers in the upper left of each panel indicate the redshift bins. The solid lines show predictions from our best-fit $\Lambda$CDM model from the analysis of all three two-point functions, and the shaded areas display the angular scales that are not used in our cosmological analysis (see §IV).
assumed throughout); \( b^i \) is the linear redMaGiC bias in redshift bin \( i \); \( J_0 \) is the Bessel function of order zero; \( n_i^s(z(\chi)) \) is the redshift distribution of redMaGiC galaxies in the bin \( i \) normalized so that the integral over \( \chi \) is equal to unity; \( H(z) \) is the Hubble expansion rate at redshift \( z \); and \( P_{NL}(k;z) \) is the 3D matter power spectrum at wavenumber \( k \) (which, in this Limber approximation, is set equal to \((l + 1/2)/\chi \)) and at the comoving time associated with redshift \( z \). The expansion rate, comoving distance, and power spectrum all depend upon the cosmological parameters, and the redshift distribution depends implicitly upon the shift parameter introduced in Eq. (II.1). Thus, the angular correlation function in a given redshift bin depends upon eight parameters in \( \Lambda \)CDM.

The expression in Eq. (IV.1) and the ones in Eqs. (IV.2) and (IV.4) use the “flat-sky” approximation, while the corresponding expressions in [79] use the more accurate expression that sums over Legendre polynomials. However, we show there that the differences between these two expressions are negligible over the scales of interest.

The model power spectrum here is the fully nonlinear power spectrum in \( \Lambda \)CDM or \( w \)CDM, which we estimate on a grid of \((k,z) \) by first running CAMB [112] or CLASS [113] to obtain the linear spectrum and then HALOFIT [114] for the nonlinear spectrum. The smallest angular separations for which the galaxy-two-point function measurements are used in the cosmological inference, indicated by the boundaries of the shaded regions in the upper panels of Figure 2 correspond to a comoving scale of \( 8\ h^{-1} \) Mpc; this scale is chosen such that modeling uncertainties in the non-linear regime cause negligible impact on the cosmological parameters relative to their statistical errors, as shown in [79] and [87].

As described in §VI of [79], we include the impact of neutrino bias [115–117] when computing the angular correlation function of galaxies. For Y1 data, this effect is below statistical uncertainties, but it is computationally simple to implement and will be relevant for upcoming analyses.

2. Galaxy–galaxy lensing: \( \gamma_t(\theta) \)

We model the tangential shear as we modeled the angular correlation function, since it is also a two-point function: the correlation of lens galaxy positions in bin \( i \) with source galaxy shear in bin \( j \). On large scales, it can be expressed as an integral over the power spectrum, this time with only one factor of bias,

\[
\gamma_{ij}^t(\theta) = b^i(1 + m^j) \int \frac{dl}{2\pi} J_2(l\theta) \int d\chi n_i^s(z(\chi)) \times \frac{q_i^z(\chi)}{H(z)\chi^2} P_{NL} \left(\frac{l + 1/2}{\chi}, z(\chi)\right),
\]

where \( m^j \) is the multiplicative shear bias, \( J_2 \) is the 2nd-order Bessel function, and the lensing efficiency function is given by

\[
q_i^z(\chi) = \frac{3\Omega_m H_0^2}{2 a(\chi)} \int_{\chi}^{(z=\infty)} d\chi' n_i^s(z(\chi')) \frac{dz}{d\chi'} \frac{\chi' - \chi}{\chi},
\]

with \( n_i^s(z) \) the source galaxy redshift distribution. Because both the source and lens redshift distributions impact the signal, the shift parameters \( \Delta z_i^s \) and \( \Delta z_i^l \) are implicit, as are all the cosmological parameters. The shear signal also depends upon intrinsic alignments of the source shapes with the tidal fields surrounding the lens galaxies; details of our model for this effect (along with an examination of more complex models) are given in [79] and [87]. The smallest angular separations for which the galaxy–galaxy lensing measurements are used in the cosmological inference, indicated by the boundaries of the shaded regions in the lower panels of Figure 2 correspond to a comoving scale of \( 12 h^{-1} \) Mpc; above; this scale is chosen such that the model uncertainties in the non-linear regime cause insignificant changes to the cosmological parameters relative to the statistical uncertainties, as derived in [79] and verified in [80].

3. Cosmic shear \( \xi_{\pm}(\theta) \)

The cosmic shear signal is independent of galaxy bias but shares the same general form as the other sets of two-point functions. The theoretical predictions for these shear-shear two-point functions are

\[
\xi_{\pm}(\theta) = (1 + m^i)(1 + m^j) \int \frac{dl}{2\pi} J_0(l\theta) \int d\chi \times q_i^z(\chi) q_j^z(\chi) P_{NL} \left(\frac{l + 1/2}{\chi}, z(\chi)\right),
\]

where the efficiency functions are defined above, and \( J_0 \) and \( J_4 \) are the Bessel functions for \( \xi_+ \) and \( \xi_- \). Intrinsic alignment affects the cosmic shear signal, especially the low-redshift bins, and are modeled as in [79]. Baryons affect the matter power spectrum on small scales, and the cosmic shear signal is potentially sensitive to these uncertain baryonic effects; we restrict our analysis to the unshaded, large-scale regions shown in Figure 3 to reduce uncertainty in these effects below our measurement errors, following the analysis in [87].

B. Parameterization and Priors

We use these measurements from the DES Y1 data to estimate cosmological parameters in the context of two cosmological models, \( \Lambda \)CDM and \( w \)CDM. \( \Lambda \)CDM contains three energy densities in units of the critical density: the matter, baryon, and massive neutrino energy densities, \( \Omega_m, \Omega_b, \) and \( \Omega_\nu \). The energy density in massive neutrinos is a free parameter but is often fixed in cosmological analyses to either zero or to a value corresponding to the minimum allowed neutrino mass of 0.06 eV from oscillation experiments [118]. We think it is more appropriate to vary this unknown parameter, and we do so throughout the paper (except in §VII D where we show that this does not affect our qualitative conclusions).

Since most other survey analyses have fixed \( \Omega_\nu \), our results for the remaining parameters will differ slightly from theirs, even when using their data.
\( \Lambda \)CDM has three additional free parameters: the Hubble parameter, \( H_0 \), and the amplitude and spectral index of the primordial scalar density perturbations, \( A_s \) and \( n_s \). This model is based on inflation, which fairly generically predicts a flat universe. Further when curvature is allowed to vary in \( \Lambda \)CDM, it is constrained by a number of experiments to be very close to zero. Therefore, although we plan to study the impact of curvature in future work, in this paper we assume the universe is spatially flat, with \( \Omega_m = 1 - \Omega_{\Lambda} \). It is common to replace \( A_s \) with the RMS amplitude of mass fluctuations on 8 h\(^{-1}\) Mpc scale in linear theory, \( \sigma_8 \), which can be derived from the aforementioned parameters. Instead of \( \sigma_8 \), in this work we will focus primarily on the related parameter

\[
S_8 \equiv \sigma_8 \left( \frac{\Omega_m}{0.3} \right)^{0.5} \quad (\text{IV.5})
\]

since \( S_8 \) is better constrained than \( \sigma_8 \) and is largely uncorrelated with \( \Omega_m \) in the DES parameter posterior.

We also consider the possibility that the dark energy is not a cosmological constant. Within this \( w \)CDM model, the dark energy equation of state parameter, \( w \) (not to be confused with the angular correlation function \( w(\theta) \)), is taken as an additional free parameter instead of being fixed at \( w = -1 \) as in \( \Lambda \)CDM. \( w \)CDM thus contains 7 cosmological parameters. In future analyses of larger DES data sets, we anticipate constraining more extended cosmological models, e.g., those in which \( w \) is allowed to vary in time.

In addition to the cosmological parameters, our model for the data contains 20 nuisance parameters, as indicated in the lower portions of Table 1. These are the nine shift parameters, \( \Delta z^i \), for the source and lens redshift bins, the five redMaGiC bias parameters, \( b^i \), the four multiplicative shear biases, \( m^i \), and two parameters, \( A_{1A} \) and \( \eta_{1A} \), that parametrize the intrinsic alignment model.

Table 1 presents the priors we impose on the cosmological and nuisance parameters in the analysis. For the cosmological parameters, we generally adopt wide, flat priors that conservatively span the range of values well beyond the uncertainties reported by recent experiments. As an example, although there are currently potentially conflicting measurements of \( h \), we choose the lower end of the prior to be 10σ below the lower central value from the Planck cosmic microwave background measurement \( 5 \) and the upper end to be 10σ above the higher central value from local measurements \( 119 \). In the case of \( w \)CDM, we impose a physical upper bound of \( w < -0.33 \), as that is required to obtain cosmic acceleration. As another example, the lower bound of the prior on the massive neutrino density, \( \Omega_{\nu} h^2 \), in Table 1 corresponds to the experimental lower limit on the sum of neutrino masses from oscillation experiments.

For the astrophysical parameters \( b^i, A_{1A}, \) and \( \eta_{1A} \) that are not well constrained by other analyses, we also adopt conservatively wide, flat priors. For all of these relatively uninformative priors, the guiding principle is that they should not impact our final results, and in particular that the tails of the posterior parameter distributions should not lie close to the edges of the priors. For the remaining nuisance parameters, \( \Delta z^i \) and \( m^i \), we adopt Gaussian priors that result from the comprehensive analyses described in Refs. 82, 86. The prior and posterior distributions of these parameters are plotted in Appendix A in Figure 19.

In evaluating the likelihood function (\text{IV.C}), the parameters with Gaussian priors are allowed to vary over a range roughly five times wider than the prior; for example, the parameter that accounts for a possible shift in the furthest lens redshift bin, \( \Delta z^3 \), is constrained in \( 85 \) to have a 1σ uncertainty of 0.01, so it is allowed to vary over \( |\Delta z^3| < 0.05 \). These sampling ranges conservatively cover the parameter values of interest while avoiding computational problems associated with exploring parameter ranges that are overly broad. Furthermore, overly broad parameter ranges would distort the computation of the Bayesian evidence, which would be problematic as we will use Bayes factors to assess the consistency of the different two-point function measurements, consistency with external data sets, and the need to introduce additional parameters (such as \( w \)) into the analysis. We have verified that our results below are insensitive to the ranges chosen.

C. Likelihood Analysis

For each data set, we sample the likelihood, assumed to be Gaussian, in the many-dimensional parameter space:

\[
\ln L(\tilde{p}) = -\frac{1}{2} \sum_{ij} [D_i - T_i(\tilde{p})] C^{-1} [D_j - T_j(\tilde{p})],
\]

(IV.6)

where \( \tilde{p} \) is the full set of parameters, \( D_i \) are the measured two-point function data presented in Figures 2 and 3, and \( T_i(\tilde{p}) \) are the theoretical predictions as given in Eqs. (IV.1, IV.2, IV.4). The likelihood depends upon the covariance matrix \( C \) that describes how the measurement in each angular and redshift bin is correlated with every other measurement. Since the DES data vector contains 457 elements, the covariance is a symmetric 457 × 457 matrix. We generate the covariance matrices using CosmoLike \( 120 \), which computes the relevant four-point functions in the halo model, as described in \( 79 \). We also describe there how the CosmoLike-generated covariance matrix is tested with simulations.

Eq. (IV.6) leaves out the \( \ln(\text{det}(C)) \) in the prefactor\( 3 \) and more generally neglects the cosmological dependence of the covariance matrix. Previous work \( 121 \) has shown that this dependence is likely to have a small impact on the central value; our rough estimates of the impact of neglecting the determinant confirm this; and — as we will show below — our results did not change when we replaced the covariance matrix with an updated version based on the best-fit parameters. However, as we will see, the uncertainty in the covariance matrix leads to some lingering uncertainty in the error bars. To form the posterior, we multiply the likelihood by the priors, \( P(\tilde{p}) \), as given in Table 1.
Parallel pipelines, CosmoSIS and CosmoLike, are used to compute the theoretical predictions and to generate the Monte Carlo Markov Chain (MCMC) samples that map out the posterior space leading to parameter constraints. The two sets of software use the publicly available samplers MultiNest and emcee. The former provides a powerful way to compute the Bayesian evidence described below so most of the results shown here use CosmoSIS running MultiNest.

D. Tests on Simulations

The collaboration has produced a number of realistic mock catalogs for the DES Y1 data set, based upon two different cosmological N-body simulations (Buzzard, MICE), which were analyzed as described in [80]. We applied all the steps of the analysis on the simulations, from measuring the relevant two-point functions to extracting cosmological parameters. In the case of simulations, the true cosmology is known, and [80] demonstrates that the analysis pipelines we use here do indeed recover the correct cosmological parameters.

V. BLINING AND VALIDATION

The small statistical uncertainties afforded by the Y1 data set present an opportunity to obtain improved precision on cosmological parameters, but also a challenge to avoid confirmation biases. To preclude such biases, we followed the guiding principle that decisions on whether the data analysis has been successful should not be based upon whether the inferred cosmological parameters agreed with our previous expectations. We remained blind to the cosmological parameters implied by the data until after the analysis procedure and estimates of uncertainties on various measurement and astrophysical nuisance parameters were frozen.

To implement this principle, we first transformed the ellipticities $\epsilon$ in the shear catalogs according to $\text{arctanh}(\epsilon) \rightarrow \lambda \text{arctanh}(\epsilon)$, where $\lambda$ is a fixed blind random number between 0.9 and 1.1. Second, we avoided plotting the measured values and theoretical predictions in the same figure (including simulation outputs as “theory”). Third, when running codes that derived cosmological parameter constraints from observed statistics, we shifted the resulting parameter values to obscure the best-fit values and/or omitted axis labels on any plots.

These measures were all kept in place until the following criteria were satisfied:

1. All non-cosmological systematics tests of the shear measurements were passed, as described in [82], and the priors on the multiplicative biases were finalized.

2. Photo-z catalogs were finalized and passed internal tests, as described in [83, 86].

3. Our analysis pipelines and covariance matrices, as described in [79, 80], passed all tests, including robustness to intrinsic alignment and bias model assumptions.

4. We checked that the $\Lambda$CDM constraints (on, e.g., $\Omega_m, \sigma_8$) from the two different cosmic shear pipelines IM3SHAPE and METACALIBRATION agreed. The pipelines were not tuned in any way to force agreement.

5. $\Lambda$CDM constraints were stable when dropping the smallest angular bins for METACALIBRATION cosmic shear data.

6. Small-scale METACALIBRATION galaxy–galaxy lensing data were consistent between source bins (shear-ratio test, as described in §6 of [88]). We note that while this test is performed in the nominal $\Lambda$CDM model, it is close to insensitive to cosmological parameters, and therefore does not introduce confirmation bias.

Once the above tests were satisfied, we unblinded the shear catalogs but kept cosmological parameter values blinded while carrying out the following checks, details of which can be found in Appendix A:

7. Consistent results were obtained from the two theory/inference pipelines, CosmoSIS and CosmoLike.

8. Parameter posteriors did not impinge on the edges of the sampling ranges and were in agreement with associated priors for all parameters.

9. Consistent results on all cosmological parameters were obtained with the two shear measurement pipelines, METACALIBRATION and IM3SHAPE.

10. Consistent results on the cosmological parameters were obtained when we dropped the smallest-angular-scale components of the data vector, reducing our susceptibility to baryonic effects and departures from linear galaxy biasing. This test uses the combination of the three two-point functions (as opposed to from shear only as in test 5).

11. An acceptable goodness-of-fit value ($\chi^2$) was found between the data and the model produced by the best-fitting parameters. This assured us that the data were consistent with some point in the model space that we are constraining, while not yet revealing which part of parameter space that is.

12. Parameters inferred from cosmic shear ($\xi_\perp$) were consistent with those inferred from the combination of galaxy–galaxy lensing ($\gamma_\ell$) and galaxy clustering ($w(\theta)$).

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4 https://bitbucket.org/joezuntz/cosmosis/
Once these tests were satisfied, we unblinded the parameter inferences. The following minor changes to the analysis procedures or priors were made after the unblinding: as planned before unblinding, we re-ran the MCMC chains with a new covariance matrix calculated at the best-fit parameters of the original analysis. This did not noticeably change the constraints (see Figure 27 in Appendix 15), as expected from our earlier tests on simulated data [29]. We also agreed before unblinding that we would implement two changes after unblinding: small changes to the photo-z priors referred to in the footnote to Table 4 and fixing a bug in IM3SHAPE object blacklisting that affected ≈ 1% of the footprint.

All of the above tests passed, most with reassuringly unremarkable results; more details are given in Appendix A.

For test 11 we calculated the $\chi^2 = -2 \log L$ value of the 457 data points used in the analysis using the full covariance matrix. In ΛCDM, the model used to fit the data has 26 free parameters, so the number of degrees of freedom is $\nu = 431$. The model is calculated at the best-fit parameter values of the posterior distribution (i.e. the point from the posterior sample with lowest $\chi^2$). Given the uncertainty on the estimates of the covariance matrix, the formal probabilities of a $\chi^2$ distribution are not applicable. We agreed to unblind as long as $\chi^2$ was less than 605 ($\chi^2/\nu < 1.4$). The best-fit value $\chi^2 = 572$ passes this test, with $\chi^2/\nu = 1.33$. Considering the fact that 13 of the free parameters are nuisance parameters with tight Gaussian priors, we will use $\nu = 444$, giving $\chi^2/\nu = 1.29$.

The best-fit models for the three two-point functions are over-plotted on the data in Figures 2 and 3 from which it is apparent that the $\chi^2$ is not dominated by conspicuous outliers. Figure 4 offers confirmation of this, in the form of a histogram of the differences between the best-fit theory and the data in units of the standard deviation of individual data points. The three probes show similar values of $\chi^2/\nu$: for $\xi_{\pm}(\theta)$, $\chi^2 = 273$ for 227 data points; for $\gamma_{\ell}(\theta)$, $\chi^2 = 215$ for 187 data points; and for $w(\theta)$, $\chi^2 = 54$ for 43 data points. A finer division into each of the 45 individual 2-point functions shows no significant concentration of $\chi^2$ in particular bin pairs. We also find that removing all data at scales $\theta > 100'$ yields $\chi^2 = 312$ for 277 data points ($\chi^2/\nu = 1.18$), not a significant reduction, and also yields no significant shift in best-fit parameters. Thus, we find that no particular piece of our data vector dominates our $\chi^2$ result.

The $\chi^2$ value for the full 3 × 2-point data vector passed our unblinding criterion, even though it would be unacceptable ($p = 4 \times 10^{-5}$ for $\nu = 444$) if we were expecting adherence to the $\chi^2$ distribution. We argue that the $p$-value of the $\chi^2$ distribution should be treated with caution since it may not be a robust statistic here. We can expect deviations from a strict $\chi^2$ distribution due to a number of factors: potential non-Gaussian error distributions, which will have less impact on our likelihood estimates than on the $p$-value; the effect of priors and marginalized systematic parameters; and uncertainties in our estimation of the covariance matrix. For example, if we increase the diagonal elements of the covariance matrix by a factor 1.1, we obtain a $\chi^2 = 467$, and the $p$-value rises to 0.22, easily acceptable. We expect such a change in the covariance to, at most, increase the size of the uncertainty we obtain on cosmological parameters by 5%. Based on these observations, we believe that a pessimistic view of our $\chi^2/\nu \approx 1.3$ result is that it indicates that our error bars are underestimated by ≈ 10% (since multiplying the whole covariance matrix by 1.2 would clearly obtain an acceptable $\chi^2$).

![FIG. 4. Histogram of the differences between the best-fit ΛCDM model predictions and the 457 data points shown in Figures 2 and 3 in units of the standard deviation of the individual data points. Although the covariance matrix is not diagonal, and thus the diagonal error bars do not tell the whole story, it is clear that there are no large outliers that drive the fits.](image-url)
ample of such a hypothesis is that dataset $\bar{D}$ can be described by a model $M$, in which case the Bayesian evidence is

$$P(\bar{D}|H) = \int d^N \theta P(\bar{D}|\theta, M)P(\theta|M) \quad \text{(V.1)}$$

where $\theta$ are the $N$ parameters of model $M$.

For two hypotheses $H_0$ and $H_1$, the Bayes factor is given by

$$R = \frac{P(\bar{D}|H_0)}{P(\bar{D}|H_1)} = \frac{P(H_0|\bar{D})P(H_1)}{P(H_1|\bar{D})P(H_0)} \quad \text{(V.2)}$$

where the second equality follows from Bayes’ theorem and clarifies the meaning of the Bayes factor: if we have equal a priori belief in $H_0$ and $H_1$ (i.e., $P(H_0) = P(H_1)$), the Bayes factor is the ratio of the posterior probability of $H_0$ to the posterior probability of $H_1$. The Bayes factor can be interpreted in terms of odds, i.e., it implies $H_0$ is favored over $H_1$ with $R : 1$ odds (or disfavored if $R < 1$). We will adopt the widely used Jeffreys scale [127] for interpreting Bayes factors: $3.2 < R < 10$ and $R > 10$ are respectively considered substantial and strong evidence for $H_0$ over $H_1$. Conversely, $H_1$ is strongly favored over $H_0$ if $R < 0.1$, and there is substantial evidence for $H_1$ if $0.1 < R < 0.31$.

We follow [128] by applying this formalism as a test for consistency between cosmological probes. In this case, the null hypothesis, $H_0$, is that the two datasets were measured from the same universe and therefore share the same model parameters. Two probes would be judged discrepant if they strongly favour the alternative hypothesis, $H_1$, that they are measured from two different universes with different model parameters. So the appropriate Bayes factor for judging consistency of two datasets, $D_1$ and $D_2$, is

$$R = \frac{P(\bar{D}_1, \bar{D}_2|M)}{P(\bar{D}_1|M)P(\bar{D}_2|M)} \quad \text{(V.3)}$$

where $M$ is the model, e.g., $\Lambda$CDM or $\omega$CDM. The numerator is the evidence for both datasets when model $M$ is fit to both datasets simultaneously. The denominator is the evidence for both datasets when model $M$ is fit to both datasets individually, and therefore each dataset determines its own parameter posteriors.

Before the data were unblinded, we decided that we would combine results from these two sets of two-point functions if the Bayes factor defined in Eq. (V.3) did not suggest strong evidence for inconsistency. According to the Jeffreys scale, our condition to combine is therefore that $R > 0.1$ (since $R < 0.1$ would imply strong evidence for inconsistency). We find a Bayes factor of $R = 2.8$, an indication that DES Y1 cosmic shear and galaxy clustering plus galaxy–galaxy lensing are consistent with one another in the context of $\Lambda$CDM.

The DES Y1 data were thus validated as internally consistent and robust to our assumptions before we gained any knowledge of the cosmological parameter values that they imply. Any comparisons to external data were, of course, made after the data were unblinded.

VI. DES Y1 RESULTS: PARAMETER CONSTRAINTS

A. $\Lambda$CDM

We first consider the $\Lambda$CDM model with six cosmological parameters. The DES data are most sensitive to two cosmological parameters, $\Omega_m$ and $S_8$ as defined in Eq. (IV.5), so for the most part we focus on constraints on these parameters.

![Figure 5](https://via.placeholder.com/150)

**FIG. 5.** $\Lambda$CDM constraints from DES Y1 on $\Omega_m$, $\sigma_8$, and $S_8$ from cosmic shear (green), redMaGiC galaxy clustering plus galaxy–galaxy lensing (red), and their combination (blue). Here, and in all such 2D plots below, the two sets of contours depict the 68% and 95% confidence levels. Given the demonstrated consistency of cosmic shear with clustering plus galaxy–galaxy lensing in the context of $\Lambda$CDM as noted above, we proceed to combine the constraints from all three probes. Figure 5 shows the constraints on $\Omega_m$, and $\sigma_8$ (bottom panel), and on $\Omega_m$ and the less degenerate parameter $S_8$ (top panel). Constraints from cosmic shear, galaxy clustering + galaxy–galaxy lensing, and their combination are shown in these two-dimensional subspaces after marginalizing over the 24 other parameters. The combined results lead to constraints

$$\begin{align*}
\Omega_m &= 0.264^{+0.032}_{-0.019} \\
S_8 &= 0.783^{+0.021}_{-0.025} \\
\sigma_8 &= 0.807^{+0.062}_{-0.041}.
\end{align*} \quad \text{(VI.1)}$$

The value of $\Omega_m$ is slightly lower than that inferred from either cosmic shear or clustering plus galaxy–galaxy lensing separately. In general, when projecting down onto a small subspace, this can occur. In this particular case, we get a glimpse of why by noting from the bottom panel of Figure 5 that the degeneracy directions of shear differ slightly in the
$\Omega_m - \sigma_8$ plane from $w(\theta) + \gamma(\theta)$, with the two converging on lower values of $\Omega_m$. We present the resulting marginalized constraints on the cosmological parameters in the top rows of Table II.

The results shown in Figure 5, along with previous analyses such as that using KiDS + GAMA data [62], are an important step forward in the capability of combined probes from optical surveys to constrain cosmological parameters. These combined constraints transform what has, for the past decade, been a one-dimensional constraint on $S_8$ (which appears banana-shaped in the $\Omega_m - \sigma_8$ plane) into tight constraints on both of these important cosmological parameters. Figure 6 shows the DES Y1 constraints on $S_8$ and $\Omega_m$ along with some previous results and in combination with external data sets, as will be discussed below. The sizes of these parameter error bars from the combined DES Y1 probes are comparable to those from the cosmic microwave background (CMB) obtained by Planck.

In addition to the cosmological parameters, these probes constrain important astrophysical parameters. The intrinsic alignment (IA) signal is modeled to scale as $A_{IA}(1 + z)^{\alpha_A}$; while the data do not constrain the power law well ($\alpha_A = -0.0^{+1.7}_{-2.5}$), they are sensitive to the amplitude of the signal:

$$A_{IA} = 0.50^{+0.32}_{-0.38} \quad (95\% \text{ CL}).$$

(VI.2)

Further strengthening evidence from the recent combined probes analysis of KiDS [62, 63], this result is the strongest evidence to date of IA in a broadly inclusive galaxy sample; previously, significant IA measurements have come from selections of massive elliptical galaxies, usually with spectroscopic redshifts (e.g., [129]). The ability of DES data to produce such a result without spectroscopic redshifts demonstrates the power of this combined analysis and emphasizes the importance of modeling IA in the pursuit of accurate cosmology from weak lensing. We are able to rule out $A_{IA} = 0$ at 99.36\% CL with DES alone and at 99.89\% CL with the full combination of DES and external data sets. The mean value of $A_{IA}$ is nearly the same when combining with external data sets, suggesting that IA self-calibration has been effective. Interestingly, the measured amplitude agrees well with a prediction made by assuming that only red galaxies contribute to the IA signal, and then extrapolating the IA amplitude measured from spectroscopic samples of luminous galaxies using a realistic luminosity function and red galaxy fraction [79]. Our measurement extends the diversity of galaxies with evidence of IA, allowing more precise predictions for the behavior of the expected IA signal.

The biases of the redMaGiC galaxy samples in the five lens bins are shown in Figure 7 along with the results with fixed cosmology obtained in [88] and [89]. Most interesting is the constraining power: even when varying a full set of cosmological parameters (including $\sigma_8$, which is quite degenerate with bias when using galaxy clustering only) and 15 other nuisance parameters, the combined probes in DES Y1 constrain bias at the ten percent level.

### B. $w$CDM

A variety of theoretical alternatives to the cosmological constant have been proposed [4]. For example, it could be that the cosmological constant vanishes and that another degree of freedom, e.g., a very light scalar field, is driving the current epoch of accelerated expansion. Here we restrict our analysis to the simplest class of phenomenological alternatives, models in which the dark energy density is not constant, but rather evolves over cosmic history with a constant equation of state parameter, $w$. We constrain $w$ by adding it as a seventh cosmological parameter. Here, too, DES obtains interesting constraints on only a subset of the seven cosmological parameters, so we show the constraints on the three-dimensional subspace spanned by $\Omega_m$, $S_8$, and $w$. Figure 8 shows the constraints in this 3D space from cosmic shear and from galaxy–galaxy lensing + galaxy clustering. These two sets of probes agree with one another. The consistency in the three-dimensional subspace shown in Figure 8, along with the tests in the previous subsection, is sufficient to combine the two sets of probes. The Bayes factor in this case was equal to 0.6. The combined constraint from all three two-point functions is also shown in Figure 8.

The marginalized 68\% CL constraints on $w$ and on the other two cosmological parameters tightly constrained by DES, $S_8$ and $\Omega_M$, are shown in Figure 9 and given numerically in Table II. In the next section, we revisit the question of how consistent the DES Y1 results are with other experiments. The marginalized constraint on $w$ from all three DES Y1 probes is

$$w = -0.80^{+0.20}_{-0.22}.$$  

(VI.3)

Finally, if one ignores any intuition or prejudice about the mechanism driving cosmic acceleration, studying $w$CDM translates into adding an additional parameter to describe the data. From a Bayesian point of view, the question of whether $w$CDM is more likely than $\Lambda$CDM can again be addressed by computing the Bayes factor. Here the two models being compared are simpler: $\Lambda$CDM and $w$CDM. The Bayes factor is

$$R_w = \frac{P(D|w\text{CDM})}{P(D|\Lambda\text{CDM})}.$$  

(VI.4)

Values of $R_w$ less than unity would imply $\Lambda$CDM is favored, while those greater than one argue that the introduction of the additional parameter $w$ is warranted. The Bayes factor is $R_w = 0.36$ for DES Y1, so although $\Lambda$CDM is slightly favored, there is no compelling evidence to favor or disfavor an additional parameter $w$.

It is important to note that, although our result in Eq. (VI.3) is compatible with $\Lambda$CDM, the most stringent test of the model from DES Y1 is not this parameter, but rather the constraints on the parameters in the model shown in Figure 5, as compared with constraints on those parameters from the CMB measurements of the universe at high redshift. We turn next to that comparison.
We next explore the cosmological implications of comparison and combination of DES Y1 results with other experiments’ constraints. For the CMB, we take constraints from Planck [51]. In the first subsection below, we use only the temperature and polarization auto- and cross-spectra from Planck, omitting the information due to lensing of the CMB that is contained in the four-point function. The latter depends on structure and distances at late times, and we wish in this subsection to segregate late-time information from early-Universe observables. We use the joint TT, EE, BB and TE likelihood for \( \ell \) between 2 and 29 and the TT likelihood for \( \ell \) between 30 and 2508 (commonly referred to as TT+lowP), provided by Planck [51]. In all cases that we have checked, use of WMAP [130] data yields constraints consistent with, but weaker than, those obtained with Planck. Recent results from the South Pole Telescope [131] favor a value of \( \sigma_8 \) that is 2.6-\( \sigma \) lower than Planck, but we have not yet tried to incorporate these results.

We use measured angular diameter distances from the Baryon Acoustic Oscillation (BAO) feature by the 6dF Galaxy Survey [132], the SDSS Data Release 7 Main Galaxy Sample [133], and BOSS Data Release 12 [48], in each case extracting only the BAO constraints. These BAO distances are all measured relative to the physical BAO scale corresponding to the sound horizon distance \( r_{\text{d}} \); therefore, dependence of \( r_{\text{d}} \) on cosmological parameters must be included when determining the likelihood of any cosmological model (see [48] for details). We also use measures of luminosity distances from observations of distant Type Ia supernovae (SNe) via the Joint Lightcurve Analysis (JLA) data from [134].

This set of BAO and SNe experiments has been shown to be consistent with the \( \Lambda \)CDM and \( \omega \)CDM constraints from the CMB [49] [51], so we can therefore sensibly merge this suite of experiments—BAO, SNe, and Planck—with the DES Y1 results to obtain unprecedented precision on the cosmological parameters. We do not include information about direct measurements of the Hubble constant because those are in tension with this bundle of experiments [135].

5 Late-universe lensing does smooth the CMB power spectra slightly, so these data sets are not completely independent of low redshift information.
FIG. 6. 68% confidence levels for ΛCDM on $S_8$ and $\Omega_m$ from DES Y1 (different subsets considered in the top group, black); DES Y1 with all three probes combined with other experiments (middle group, green); and results from previous experiments (bottom group, purple). Note that neutrino mass has been varied so, e.g., results shown for KiDS-450 were obtained by re-analyzing their data with the neutrino mass left free. The table includes only data sets that are publicly available so that we could re-analyze those using the same assumptions (e.g., free neutrino mass) as are used in our analysis of DES Y1 data.

FIG. 7. The bias of the redMaGiC galaxy samples in the five lens bins from three separate DES Y1 analyses. The two labelled “fixed cosmology” use the galaxy angular correlation function $w(\theta)$ and galaxy–galaxy lensing $\gamma_t$ respectively, with cosmological parameters fixed at best-fit values from the 3x2 analysis, as described in [53] and [89]. The results labelled “DES Y1 - all” vary all 26 parameters while fitting to all three two-point functions.

A. High redshift vs. low redshift in ΛCDM

The CMB measures the state of the Universe when it was 380,000 years old, while DES measures the matter distribution in the Universe roughly ten billion years later. Therefore, one obvious question that we can address is: Is the ΛCDM prediction for clustering today, with all cosmological parameters determined by Planck, consistent with what DES observes? This question, which has of course been addressed by previous surveys (e.g., [31, 34, 62, 63]), is so compelling because (i) of the vast differences in the epochs and conditions measured; (ii) the predictions for the DES Y1 values of $S_8$ and $m$ have no free parameters in ΛCDM once the recombination-era parameters are fixed; and (iii) those predictions for what DES should observe are very precise, with $S_8$ and $\Omega_m$ determined by the CMB to within a few percent.

We saw above that $S_8$ and $m$ are constrained by DES Y1 at the few-percent level, so the stage is set for the most stringent test yet of ΛCDM growth predictions. Tension between these two sets of constraints might imply the breakdown of ΛCDM. Figure 10 compares the low-$z$ constraints for ΛCDM from all three DES Y1 probes with the $z = 1100$ constraints from the Planck anisotropy data. Note that the Planck contours are shifted slightly and widened significantly from those in Figure 18 of [51], because we are marginalizing over the unknown sum of the neutrino masses. We have verified that when the sum of the neutrino masses is fixed as [51] assumed in their fiducial analysis, we recover the constraints shown in
FIG. 8. Constraints on the three cosmological parameters $\sigma_8$, $\Omega_m$, and $w$ in $w$CDM from DES Y1 after marginalizing over four other cosmological parameters and ten (cosmic shear only) or 20 (other sets of probes) nuisance parameters. The constraints from cosmic shear only (green); $w(\theta) + \gamma_z(\theta)$ (red); and all three two-point functions (blue) are shown. Here and below, outlying panels show the marginalized 1D posteriors and the corresponding 68% confidence regions.

Their Figure 18.

The two-dimensional constraints shown in Figure 10 visually hint at tension between the Planck $\Lambda$CDM prediction for RMS mass fluctuations and the matter density of the present-day Universe and the direct determination by DES. The 1D marginal constraints differ by more than 1 $\sigma$ in both $S_8$ and $\Omega_m$, as shown in Figure 6. The KiDS survey [34, 62] also reports lower $S_8$ than Planck at marginal significance.

However, a more quantitative measure of consistency in the full 26-parameter space is the Bayes factor defined in Eq. (V.3). As mentioned above, a Bayes factor below 0.1 suggests strong inconsistency and one above 10 suggests strong evidence for consistency. The Bayes factor here is $R = 4.2$, indicating "substantial" evidence for consistency on the Jeffreys scale, so any inconsistency apparent in Figure 10 is not statistically significant according to this metric. In order to test the sensitivity of this conclusion to the priors used in our analysis, we halve the width of the prior ranges on all cosmological parameters (the parameters in the first section of Table I). For this case we find $R = 1.6$, demonstrating that our conclusion that there is no evidence for inconsistency is robust even to a dramatic change in the prior volume. The Bayes factor in Eq. (V.3) compares the hypothesis that two datasets can be fit by the same set of $N$ model parameters (the null hypothesis), to the hypothesis that they are each allowed an independent set of the $N$ model parameters (the alternative hypothesis). The alternative hypothesis is naturally penalized in the Bayes factor since the model requires an extra $N$ parameters. We also test an alternative hypothesis where only $\Omega_m$ and $A_s$ are allowed to be constrained independently by the two datasets; in this case we are introducing only two extra parameters with respect to the null hypothesis. For this
FIG. 9. 68% confidence levels on three cosmological parameters from the joint DES Y1 probes and other experiments for \( w \)CDM.

FIG. 10. \( \Lambda \)CDM constraints from the three combined probes in DES Y1 (blue), Planck with no lensing (green), and their combination (red). The agreement between DES and Planck can be quantified via the Bayes factor, which indicates that in the full, multi-dimensional parameter space, the two data sets are consistent (see text).

We therefore combine the two data sets, resulting in the red contours in Figure 10. This quantitative conclusion that the high– and low– redshift data sets are consistent can even be gleaned by viewing Figure 10 in a slightly different way: if the true parameters lie within the red contours, it is not unlikely for two independent experiments to return the blue and green contour regions.

FIG. 11. \( \Lambda \)CDM constraints from high redshift (Planck, without lensing) and multiple low redshift experiments (DES Y1+BAO+JLA), see text for references.

Figure 11 takes the high-\( z \) vs. low-\( z \) comparison a step fur-
ther by combining DES Y1 with results from BAO experiments and Type Ia supernovae. While these even tighter low-redshift constraints continue to favor slightly lower values of $\Omega_m$ and $S_8$ than Planck, the Bayes factor rises to 9.0, i.e. near Jeffrey’s threshold for “strongly” favoring consistency of DES Y1+BAO+JLA with Planck. The addition of BAO and SNe to DES Y1 thus strengthens the agreement between high- and low-$z$ measures within the $\Lambda$CDM model.

The goal of this subsection is to test the $\Lambda$CDM prediction for clustering in DES, so we defer the issue of parameter determination to the next subsections. However, there is one aspect of the CMB measurements combined with DES that is worth mentioning here. DES data do not constrain the Hubble constant directly. However, as shown in Figure 12, the DES $\Lambda$CDM constraint on $\Omega_m$ combined with Planck’s measurement of $\Omega_m h^2$ leads to a shift in the inference of the Hubble constant (in the direction of local measurements). Since $\Omega_m$ is lower in DES, the inferred value of $h$ moves up. As shown in the figure and quantitatively in Table II, this shift in the value of $h$ persists as more data sets are added in.

B. Cosmological Parameters in $\Lambda$CDM

To obtain the most stringent cosmological constraints, we now compare DES Y1 with the bundle of BAO, Planck, and JLA that have been shown to be consistent with one another by combining DES Y1 with results from BAO experiments and Type Ia supernovae. While these even tighter low-redshift constraints continue to favor slightly lower values of $\Omega_m$ and $S_8$ than Planck, the Bayes factor rises to 9.0, i.e. near Jeffrey’s threshold for “strongly” favoring consistency of DES Y1+BAO+JLA with Planck. The addition of BAO and SNe to DES Y1 thus strengthens the agreement between high- and low-$z$ measures within the $\Lambda$CDM model.

Here “Planck” includes the data from the four-point function of the CMB, which captures the effect of lensing due to large-scale structure at late times. Figure 13 shows the constraints in the $\Omega_m-S_8$ plane from this bundle of data sets and from DES Y1, in the $\Lambda$CDM model. Here the apparent consistency of the data sets is borne out by the Bayes factor for dataset consistency (Eq. V.3):

$$\frac{P(JLA + Planck + BAO + DES Y1) \cdot P(DES Y1)}{P(JLA + BAO + Planck) \cdot P(DES Y1)} = 244.$$  \hfill (VII.1)

Combining all of these leads to the tightest constraints yet on $\Lambda$CDM parameters, shown in Table II. Highlighting some of these: at 68% C.L., the combination of DES with these external data sets yields

$$\Omega_m = 0.301_{-0.008}^{+0.006}.$$  \hfill (VII.2)

This value is about 1σ lower than the value without DES Y1, with comparable error bars. The clustering amplitude is also constrained at the percent level:

$$\sigma_8 = 0.801 \pm 0.014$$  \hfill (VII.3)

$$S_8 = 0.799_{-0.009}^{+0.014}.$$  \hfill (VII.4)

Note that fortuitously, because $\Omega_m$ is so close to 0.3, the difference in the central values of $\sigma_8$ and $S_8$ is negligible. The combined result is about 1σ lower than the inference without DES, and the constraints are tighter by about 20%.

As mentioned above, the lower value of $\Omega_m$ leads to a higher value of the Hubble constant:

$$h = 0.656_{-0.026}^{+0.015} \quad \text{(Planck : No Lensing)}.$$
with neutrino mass varied.

C. $\omega$CDM

Figure 14 shows the results in the extended $\omega$CDM parameter space using Planck alone, and DES alone, combined, and with the addition of BAO+SNe. As discussed in [51], the constraints on the dark energy equation of state from Planck alone are misleading. They stem from the measurement of the distance to the last scattering surface, and that distance (in a flat universe) depends upon the Hubble constant as well, so there is a strong $w-h$ degeneracy. The low values of $w$ seen in Figure 14 from Planck alone correspond to very large values of $h$, ruled out by local distance indicators. Since DES is not sensitive to the Hubble constant, it does not break this degeneracy. Additionally, the Bayes factor in Eq. (VII.4) that quantifies whether adding the extra parameter $w$ is warranted is $R_w = 0.018$. Therefore, opening up the dark energy equation of state is not favored on a formal level for the DES+Planck combination. Finally, the Bayes factor for combining DES and Planck (no lensing) in $\omega$CDM is equal to 0.18, which we identified earlier as “substantial” evidence in favor of the hypothesis that these two data sets are not consistent in the context of this model. These factors degrade the legitimacy of the value $w = -1.34_{-0.15}^{+0.08}$ returned by the DES+Planck combination.

The addition of BAO, SNe, and Planck lensing data to the DES+Planck combination yields the red contours in Figure 14 shifting the solution substantially along the Planck degeneracy direction, demonstrating (i) the problems mentioned above with the DES+Planck (no lensing) combination and (ii) that these problems are resolved when other data sets are introduced that restrict the Hubble parameter to reasonable values. The Bayes factor for combination of Planck with the low-z suite of DES+BAO+SNe in the $\omega$CDM model is $R = 699$, substantially more supportive of the combination of experiments than the case for Planck and DES alone. The DES+Planck+BAO+SNe solution shows good consistency in the $\Omega_m = w = S_8$ subspace and yields our final constraint on the dark energy equation of state:

$$w = -1.00_{-0.05}^{+0.04}.$$  \hspace{1cm} (VII.5)

DES Y1 reduces the width of the allowed 68% region by ten percent. The evidence ratio $R_w = 0.08$ for this full combination of data sets, favoring the introduction of $w$ as a free parameter.

D. Neutrino Mass

The lower power observed in DES (relative to Planck) has implications for the constraint on the sum of the neutrino masses, as shown in Figure 15. The current most stringent constraint comes from the cosmic microwave background and Lyman-alpha forest [136]. The experiments considered here (DES, JLA, BAO) represent an independent set so offer an alternative method for measuring the clustering of matter as a function of scale and redshift, which is one of the key drivers of the neutrino constraints. The 95% C.L. upper limit on the sum of the neutrino masses in $\Lambda$CDM becomes less constraining:

$$\sum m_\nu < 0.29 \text{eV}.$$  \hspace{1cm} (VII.6)

Adding in DES Y1 loosens the constraint by close to 20% (from 0.245 eV). This is consistent with our finding that the clustering amplitude in DES Y1 is slightly lower than expected in $\Lambda$CDM informed by Planck. The three ways of reducing the clustering amplitude are to reduce $\Omega_m$, reduce $\sigma_8$, or increase the sum of the neutrino masses. The best fit cosmology moves all three of these parameters slightly in the direction of less clustering in the present day Universe.

We may, conversely, be concerned about the effect of priors on $\Omega_\nu h^2$ on the cosmological inferences in this paper. The results for DES Y1 and Planck depicted in Figure 10 in $\Lambda$CDM were obtained when varying the sum of the neutrino masses. Neutrinos have mass [137] and the sum of the masses of the three light neutrinos is indeed unknown, so this parameter does need to be varied. However, many previous analyses have either set the sum to zero or to the minimum value allowed by oscillation experiments ($\sum m_\nu = 0.06 \text{eV}$), so it is of interest to see if fixing neutrino mass alters any of our conclusions. In particular: does this alter the level of agreement between low- and high-redshift probes in $\Lambda$CDM? Figure 16 shows the extreme case of fixing the neutrino masses to the lowest value allowed by oscillation data: both the DES and Planck constraints in the $S_8 - \Omega_m$ plane change. The Planck contours shrink toward the low-$\Omega_m$ side of their contours, while the DES constraints shift slightly to lower $\Omega_m$ and higher $S_8$. The Bayes factor for the combination of DES and Planck in the $\Lambda$CDM space changes from $R = 4.2$ to $R = 7.1$ when the minimal neutrino mass is enforced. Indeed, we get a glimpse of this improved agreement from Figure 16 the area in the 2D plane allowed by Planck when the neutrino mass is fixed is much smaller than when $\Omega_\nu h^2$ varies, and the area that is favored lies closer to the region allowed by DES.

Finally, fixing the neutrino mass allows us to compare directly to previous analyses that did the same. Although there are other differences in the analyses, such as the widths of the priors, treatments of systematics, and covariance matrix generation, fixing the neutrino mass facilitates a more accurate comparison. On the main parameter $S_8$ within $\Lambda$CDM, again with neutrino mass fixed, the comparison is:

$$S_8 = 0.797 \pm 0.022 \hspace{1cm} \text{DES Y1}$$
$$= 0.801 \pm 0.032 \hspace{1cm} \text{KiDS+GAMA [62]}$$
$$= 0.742 \pm 0.035 \hspace{1cm} \text{KiDS+2dFLenS+BOSS [63]},$$  \hspace{1cm} (VII.7)

so we agree with KiDS+GAMA, but disagree with [63] at greater than 1-$\sigma$. 

\[ h = 0.682^{+0.006}_{-0.006} \hspace{1cm} (\text{DES Y1 + JLA + BAO + Planck}) \]  \hspace{1cm} (VII.4)
FIG. 14. $w$CDM constraints from the three combined probes in DES Y1 and Planck with no lensing in the $\Omega_m$-$S_8$-$h$ subspace. Note the strong degeneracy between $h$ and $w$ from Planck data. The lowest values of $w$ are associated with very large values of $h$, which would be excluded if other data sets were included.

VIII. CONCLUSIONS

We have presented cosmological results from a combined analysis of galaxy clustering and weak gravitational lensing, using imaging data from the first year of DES. These combined probes demonstrate that cosmic surveys using clustering measurements have now attained constraining power comparable to the cosmic microwave background in the $\Omega_m$-$S_8$ plane, heralding a new era in cosmology. The combined constraints on several cosmological parameters are the most precise to date.

The constraints on $\Omega_m$ from the CMB stem from the impact of the matter density on the relative heights of the acoustic peaks in the cosmic plasma when the universe was only 380,000 years old and from the distance between us today and the CMB last scattering surface. The CMB constraints on $S_8$ are an expression of both the very small RMS fluctuations in the density at that early time and the model’s prediction for how rapidly they would grow over billions of years due to gravitational instability. The measurements themselves are of course in microwave bands and probe the universe when it was extremely smooth. DES is different in every way: it probes in optical bands billions of years later when the universe had evolved to be highly inhomogeneous. Instead of using the radiation as a tracer, DES uses galaxies and shear. It is truly extraordinary that a simple model makes consistent predictions for these vastly different sets of measurements.

The results presented here enable precise tests of the $\Lambda$CDM and $w$CDM models, as shown in Figures 10 and 14. Our main findings are:

- DES Y1 constraints on $\Omega_m$ and $S_8$ in $\Lambda$CDM are competitive (in terms of their uncertainties) and compatible (according to tests of the Bayesian evidence) with constraints derived from Planck observations of the CMB. This is true even though the visual comparison (Figure 10) of DES Y1 and Planck shows differences at the
1 to 2-σ level, in the direction of offsets that other recent lensing studies have reported.

- The statistical consistency allows us to combine DES Y1 results with Planck, and, in addition, with BAO and supernova data sets. This yields $S_8 = 0.799^{+0.014}_{-0.009} \text{ and } \Omega_m = 0.301^{+0.006}_{-0.008}$ in ΛCDM, the tightest such constraints to date (Figure 13).

- None of our likelihoods, including those combining DES with external data, prefer the addition of a free dark energy equation of state parameter $w$ to the parameters of ΛCDM. The $w$CDM likelihoods from DES and Planck each constrain $w$ poorly; moreover, allowing $w$ as a free parameter makes the two data sets less consistent (in terms of the Bayesian evidence) and does not bring the DES and Planck central values of $S_8$ closer. DES is, however, consistent with the bundle of Planck, BAO, and supernova data, and this combination tightly constrains the equation-of-state parameter, $w = -1.00^{+0.04}_{-0.05}$ (Figure 14).

- The two-point functions measured in DES Y1 contain some information on two other open questions in cosmological physics: the combination of DES and Planck shifts the Planck constraints on the Hubble constant by more than 1σ in the direction of local measurements (Figure 12), and the joint constraints on neutrino mass slightly loosens the bound from external experiments to $\sum m_\nu < 0.29\text{eV} \text{ (95% C.L.)} \text{ (Figure 15).}$

- All results are based on redundant implementations and tests of the most critical components. They are robust to a comprehensive set of checks that we defined a priori and made while blind to the resulting cosmological parameters (see Section V and Appendix A). All related analyses, unless explicitly noted otherwise, marginalize over the relevant measurement systematics and neutrino mass.

- Joint analyses of the three two-point functions of weak lensing and galaxy density fields have also been executed recently by the combination of the KiDS weak lensing data with the GAMA [62] and 2dLenS [63] spectroscopic galaxy surveys, yielding ΛCDM bounds of $S_8$ that are compared to ours in Eq. (VII.7). Our results agree with the former, but differ from the latter at greater than 1-σ. DES Y1 uncertainties are roughly $\sqrt{2}$ narrower than those from KiDS-450; while one might have expected a greater improvement considering the ~3× increase in survey area, we caution against any detailed comparison of values or uncertainties until the analyses are homogenized to similar choices of scales, priors on neutrino masses, and treatments of observational systematic uncertainties.

The next round of cosmological analyses of DES data will include data from the first three years of the survey (DES Y3), which cover more than three times as much area to greater depth than Y1, and will incorporate constraints from clusters,
supernovae, and cross-correlation with CMB lensing, shedding more light on dark energy and cosmic acceleration.

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Appendix A: Unblinding Tests

Here we describe some of the results of the tests enumerated in §V. The most relevant metrics are the values of the cosmological parameters best constrained by DES Y1, namely $\Omega_m$ and $S_8$. We report here on the few instances in which the robustness tests yielded shifts in either the values or the uncertainties on $S_8$ or $\Omega_m$ exceeding 10% of their 68% CL intervals.

Fig. 17 shows the result of test 7. As CosmoSIS and CosmoLike use the same data and models, there should in principle be no difference between them except for the sampling noise of their finite MCMC chains. CosmoSIS yields error bars on $\Omega_m$ slightly smaller than those obtained from CosmoLike, with $< 0.2\sigma$ change in central value. The $S_8$ constraints agree to better than a percent and the error bars to within 3%. These numbers and the contours shown in Figure 17 improved over the results obtained before unblinding, when the difference in the error bars was larger. Longer emcee chains account for the improvement, so it is conceivable that these small differences — which do not affect our conclusions — go away with even longer chains.

When carrying out test 8, we found that for both METACALIBRATION and IM3SHAPE, almost all of the parameters were tightly constrained to lie well within their sampling ranges. The lone exception was the power law of the intrinsic alignment signal, $\eta_{HA}$, which had an error that is large relative to the prior, but this was entirely expected, as our simulations indicated that the Y1 data have little constraining power on $\eta_{HA}$. For those parameters with more informative priors, the posteriors typically fell close to the priors, indicating that the data were consistent with the calibrations described in [82] and [83]. One exception was the IM3SHAPE value $\Delta z_s^4$, the shift in the mean value of the redshift in the 4th source bin, where the posterior and prior differed by close to 1$\sigma$.

The largest discrepancy arises in test 9 of METACALIBRATION vs IM3SHAPE results. Note that Figure 11 of [87] shows good agreement between the two pipelines on inferences purely with cosmic shear. However, Figure 18 shows that when all $3 \times 2$-point data are combined, METACALIBRATION leads to a value of $S_8$ that is 1.3$\sigma$ lower than that produced by IM3SHAPE. The IM3SHAPE and METACALIBRATION data vectors are not directly comparable, since they bin and weight the source galaxies differently and thus have distinct redshift distributions—they can be properly compared only in cosmological-parameter tests such as this. To the extent that this 1.3$\sigma$ discrepancy is meaningful, we found evidence that the 4th source redshift bin might be responsible.

In fact, part of the analysis plan included estimating parameters without the highest redshift bin during the blinded phase,
as there are no redMaGiC galaxies at $z > 0.9$, and therefore we cannot use the cross-correlation technique to cross-check the COSMOS calibration of $n_s(z)$. Further, as mentioned above, the shift in the mean of the 4th source bin was larger than other shifts. So we eliminated that bin from the analysis; this reduced the disagreement between the METACALIBRATION and IM3SHAPE $S_8$ values to be less than 1σ. Since the parameter shift from this test is not statistically significant, especially given the number of robustness tests we execute, and the METACALIBRATION results are insignificantly altered by exclusion of this redshift bin, we retain the METACALIBRATION results with all four source bins, for our fiducial constraints.

For test [10] we deleted from the data vector angular scales $< 20$ arcmin from $\xi_+,$ $< 150$ arcmin from $\xi_-$, $< 65$ arcmin from $\gamma_1,$ and $< 50$ arcmin from $w(\theta)$. The cosmological parameter constraints expanded slightly, as expected, but shifted by much less than 1σ.

Finally, although we looked at these blinded, Figure [19] shows the posteriors of all 20 nuisance parameters used to model the data. Note the agreement of the two sets of probes with each other and with the priors on the parameters.

Before unblinding, we listed several additional robustness tests that would be carried out after unblinding. These are described in Appendix B.

### Appendix B: Robustness of Results

Here we test the impact on the final results of some of the choices made during analysis. These tests, conducted while unblinded but identified beforehand, supplement those described in §V.

All of our inferences require assumptions about the redshift distributions for the source and lens galaxies. We have quantified the uncertainties in the redshift distributions with a shift parameter, as described in and around Eq. (II.1). This allows for the means of the distributions to change but does not allow for any flexibility in the shapes. We now check that the uncertainty in the photometric distributions in the source bins is adequately captured by using the BPZ redshift distribution accompanied by the free shift parameter in each bin. Instead of redshift distributions obtained via BPZ, we use those obtained directly from the COSMOS data, as described in [83]. As shown in Figure 4 there, the shapes of the redshift distributions are quite different from one another, so if we obtain the same cosmological results using these different shape $n(z)$’s, we will have demonstrated that the detailed shapes do not drive the constraints. Again we allow for a free shift in each of the source distributions. Figure [20] shows that the ensuing constraints are virtually identical to those that use the BPZ $n(z)$’s for the source galaxies, suggesting that our results are indeed sensitive only to the means of the redshift distributions in each bin, and not to the detailed shapes.

We also considered the impact of the choices made while computing the covariance matrix. These choices require assumptions about all 26 parameters that are varied. We generated an initial covariance matrix assuming fiducial values for these parameters, but then after unblinding, recomputed it using the means of the posteriors of all the parameters as input. How much did this (small) change in the covariance matrix affect our final results? Figure [21] shows that the updated covariance matrix had essentially no impact on our final parameter determination.

There are no redMaGiC galaxies in our catalog at redshifts overlapping the fourth source bin, so the only way to verify the mean redshift of the galaxies in that bin is to use the COSMOS galaxies. All the other source bins benefit from the two-fold validation scheme. We therefore checked to see if removing the highest redshift bin affected our constraints. Figure [22] shows that our fiducial constraints are completely consistent with the looser ones obtained when the highest redshift bin is removed.
FIG. 19. The posteriors from cosmic shear; from $w(\theta) + \gamma_t(\theta)$; and for all three probes using the METACALIBRATION pipeline for all 20 nuisance parameters used in the $\Lambda$CDM analysis. The priors are also shown. There are no priors for the bias and intrinsic alignment parameters, the biases and the lens shifts are not constrained by $\xi \pm$. Therefore, the bottom panels have only two curves: posteriors from $w(\theta) + \gamma_t(\theta)$ and from all three probes. Similarly, there are only three curves for the two intrinsic alignment parameters.

FIG. 20. Constraints on $\Omega_m$ and $S_8$ when using the shifted BPZ redshift distributions as the default for $n_s(z)$, compared with those obtained when using the COSMOS redshift distribution, which have different shape, as seen in Figure 4 of [83].

FIG. 21. Constraints on $\Omega_m$ and $S_8$ when updating the covariance matrix after initial unblinding and using the means of the posteriors generated when using the old covariance matrix.
FIG. 22. Constraints from all three probes using all four source bins (“Fiducial”) and with the 4th source bin removed.