Measurement of associated production of $Z$ bosons with charm quark jets in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV


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We present the first measurements of the ratios of cross sections, \( \sigma(pT → Z+c\text{ jet})/\sigma(pT → Z+\text{ jet}) \) and \( \sigma(pT → Z+c\text{ jet})/\sigma(pT → Z+b\text{ jet}) \) for the associated production of a Z boson with at least one charm or bottom quark jet. Jets have transverse momentum \( p_T > 20 \text{ GeV} \) and pseudorapidity \( |\eta| < 2.5 \). These cross section ratios are measured differentially as a function of jet and Z boson transverse momenta, based on 9.7 fb\(^{-1}\) of \( pT\bar{p} \) collisions collected with the D0 detector at the Fermilab Tevatron Collider at \( \sqrt{s} = 1.96 \text{ TeV} \). The measurements show significant deviations from perturbative QCD calculations and predictions from various event generators.

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Studies of Z boson production in association with heavy flavor (HF) jets originating from b or c quarks provide important tests of perturbative quantum chromodynamics (pQCD) calculations [1]. A good theoretical description of these processes is essential since they form a major background for a variety of physics processes, including standard model Higgs boson production in association with a Z boson, \( ZH(H → bb) \) [2]. Furthermore, the relative contributions of the different flavors to the background is important since Z + c jet events can be misidentified as Z + b jet events, or vice versa, and therefore introduce additional uncertainties into measurements.

The ratio of \( Z + b \) jet to inclusive \( Z + \) jet production cross sections for events with one or more jets has previously been measured by the CDF [3, 4] and D0 [5, 6] Collaborations. This Letter reports the first measurement of associated charm jet production with a Z boson. In particular, we present the measurement of the ratio of cross sections for \( Z+c \) jet to \( Z+\) jet production as well as \( Z+c \) jet to \( Z+b \) jet production in events with at least one jet. The measurement of the ratio of cross sections benefits from the cancellation of several systematic uncertainties and therefore allows for a more precise comparison of data with the theoretical predictions. These ratio measurements are also presented differentially as a function of the transverse momenta of the jet \( pT_{\text{jet}} \) and Z boson \( pT_Z \).

The current analysis is based on the complete Run II data sample collected using the D0 detector [7] at Fermilab’s Tevatron \( pT\bar{p} \) Collider with a center-of-mass energy of 1.96 TeV, and corresponds to an integrated luminosity of 9.7 fb\(^{-1}\) following the application of relevant data quality requirements. We use the same triggering, selections, object reconstruction, and event modeling as described in the recent D0 measurement of \( Z+b \) jet production [6], but with a dedicated strategy for the extraction of the c-jet fraction. Events must contain a \( Z → \ell\ell \) candidate with a dilepton invariant mass in the range 70 < \( M_{\ell\ell} < 110 \text{ GeV} \) (\( \ell = e, \mu \)).

Dielectron (ee) events are required to have two electrons, with no requirement on the sign of their electric charge, with transverse momentum \( pT > 15 \text{ GeV} \) identified through electromagnetic (EM) showers in the calorimeter. One electron must be identified in the central calorimeter (CC), within a pseudorapidity [8] region \( |\eta| < 1.1 \), while the second electron can be reconstructed either in the CC or the endcap calorimeters, 1.5 < \( |\eta| < 2.5 \). Dimuon (\( \mu\mu \)) events are required to have two oppositely charged muons, with \( pT > 15 \text{ GeV} \) and \( |\eta| < 2 \), detected in the muon spectrometer and matched to central tracker tracks. In addition, at least one hadronic jet must be reconstructed in the event us-
ing an iterative midpoint cone algorithm [9] with a cone size of $\Delta R = \sqrt{(\Delta \phi)^2 + (\Delta y)^2} = 0.5$ where $\phi$ is the azimuthal angle and $y$ is the rapidity. This jet must satisfy $p_T^{\text{jet}} > 20$ GeV and $|\eta^{\text{jet}}| < 2.5$.

Several processes can mimic the signature of $Z + \text{jet}$ events. These include top quark pair ($t\bar{t}$), diboson ($WW$, $WZ$, and $ZZ$), and multijet production. To suppress the contributions from $t\bar{t}$ production, events with significant imbalance in the measured transverse energy, $E_T$, due to undetected neutrinos from the $W$ boson decay ($t \rightarrow Wb \rightarrow \ell \nu b$), are rejected if $E_T > 60$ GeV. These selection criteria retain an inclusive sample of 176,498 $Z + \text{jet}$ event candidates in the $ee$ and $\mu\mu$ channels.

To estimate acceptances, efficiencies, and backgrounds, the $Z + \text{jet}$ events (including HF jets) and $t\bar{t}$ events are modeled by ALPGEN [10], which generates sub-processes using higher-order QCD tree-level matrix elements (ME), interfaced with the PYTHIA Monte Carlo (MC) event generator [11] for parton showering and hadronization and EVTFGEN [12] for modeling the decay of particles containing $b$ and $c$ quarks. Inclusive diboson production is simulated with PYTHIA. The CT10Q6L1 [13] parton distribution functions (PDFs) are used in these simulations and the cross sections are scaled to the corresponding higher-order theoretical calculations. For the diboson and $Z + \text{jet}$ processes, including $Z + \text{bb}$ and $Z + \text{cc}$ production, next-to-leading order (NLO) cross section predictions are taken from MCFM [14]. The $t\bar{t}$ cross section is determined from approximate next-to-NLO calculations [15]. To improve the modeling of the $p_T$ distribution of the $Z$ boson, simulated $Z + \text{jet}$ events are also reweighted to be consistent with the measured $p_T$ spectrum of $Z$ bosons observed in data [16]. The multijet background, where jets are misidentified as leptons, is determined using a data-driven method, as described in the recent D0 publication [6]. The fractions of non-$Z + \text{jet}$ events in the $ee$ and $\mu\mu$ samples are about 9.6% and 1.3%, respectively. These fractions are dominated by multijet production where a jet is either mis-reconstructed as a lepton in the electron channel, or a lepton from decays of hadrons in a jet that passes the isolation requirement, in the muon channel.

This analysis employs a two-step procedure to determine the HF content of jets in the selected $Z + \text{jet}$ events. We employ a HF tagging algorithm [17] to enrich the sample in $b$ and $c$ jets. The $b$, $c$, and light jet composition of the data is then extracted via a template-based fit.

Jets considered for HF tagging are subject to a preselection requirement, known as taggability [17] to decouple the intrinsic performance of the HF jet tagging algorithm from effects related to track reconstruction efficiency. For this purpose, the jet is required to have at least two associated tracks with $p_T > 0.5$ GeV and the highest-$p_T$ track must have $p_T > 1$ GeV. The efficiency of the taggability requirement is 90% for both $c$ and $b$ jets.

The HF tagging algorithm is based on a multivariate analysis (MVA) technique [18] that provides an improved performance over the neural network HF tagging discriminant, described in Ref. [17], used in earlier D0 analyses. This new algorithm, known as MVA$_M$, also utilizes the relatively long lifetime of HF hadrons with respect to their lighter counterparts. Events with at least one jet passing the HF tagging selection are considered in the analysis.

To extract the fraction of different flavor jets in the data sample, a second discriminant, $D_{\text{MJL}}$, is employed, which offers improved flavor separation for jets passing our MVA$_M$ requirement [6]. It is a combination of two discriminating variables, the secondary vertex mass ($M_{\text{SV}}$) and the jet lifetime impact parameter (JLIP) [17]: $D_{\text{MJL}} = 0.5 \times (M_{\text{SV}}/5 \text{ GeV} - \ln(\text{JLIP})/20)$. The coefficients in this expression are chosen to optimize the separation of the HF and light quark components. Fig. 1(a) shows the $D_{\text{MJL}}$ distributions (templates) obtained from simulations of all three considered jet flavors that pass an MVA$_M > 0.5$ requirement.

To measure the relative fraction of $c$ jets in the HF enriched sample, the following two approaches were considered. The first is based on the methods used in Ref. [6] where the composition of $b$, $c$, and light jets is extracted by fitting MC templates to the data. This approach yields a large uncertainty on the $c$-jet fraction since the $D_{\text{MJL}}$ distributions of $c$ and light jets are similar. The second approach is to suppress events with light jets by employing a more stringent MVA$_M$ requirement. The remaining small $Z + \text{light jet}$ contribution, as estimated with data-corrected simulations, is then subtracted from the data. This allows for the data to be fit with only

![FIG. 1: (color online) (a) The probability densities of the $D_{\text{MJL}}$ discriminant for $b$, $c$, and light jets passing the final selection requirements. These templates are obtained from MC. (b) The $D_{\text{MJL}}$ discriminant distribution of events in the combined sample after background subtraction. The distributions of the $b$ and $c$ jets are weighted by the fractions found from the fit. Uncertainties are statistical only.](image-url)
$b$ and $c$ jet templates. Both methods yield consistent results, but the second method benefits from a reduced overall uncertainty since only the normalization of $b$ and $c$ jet templates are allowed to vary when fitting the data. Events are retained for further analysis if they contain at least one jet with an MVA$_b$ output greater than 0.5. After these requirements, 2,665 $Z +$ jet events are selected where only the highest-$p_T$ HF tagged jet is examined. The efficiencies of the MVA$_b$ selection for $b$ and $c$ jets, and the light jet misidentification rate are 40%, 9.0%, and 0.24%, respectively. The background is dominated by $Z+$light jet events that comprise 12% of the total sample. Before the two parameter fit, all background components are subtracted from the data, yielding a sample of 2,125 events.

We measure the fraction of events that contain at least one $b$ or $c$ jet in the $ee$ and $\mu\mu$ samples separately, yielding $c$ jet flavor fractions of $0.509 \pm 0.041$ (stat.) and $0.470 \pm 0.039$ (stat.), respectively. Since these are consistent and the kinematics of the corresponding events are similar, we combine the two samples to increase the statistical power of the fit. The combined $D_{\text{MIL}}$ distribution of the HF-enriched background subtracted data and the fitted templates for the $b$ and $c$ jets are shown in Fig. 1(b). The corresponding fractions of $b$ and $c$ jets in the data are found to be $0.486 \pm 0.027$ (stat.) and $0.514 \pm 0.027$ (stat.), respectively. These fractions are combined with the relevant detector acceptances and efficiencies to determine the ratios of cross sections using

$$R_{c/jet} = \frac{\sigma(Z+c \text{ jet})}{\sigma(Z+\text{jet})} = \frac{N_{\text{HF}} f_c}{N_{\text{incl}} f_{c/tag}} \times \frac{A_{\text{incl}}}{A_c}$$

$$R_{c/b} = \frac{\sigma(Z+c \text{ jet})}{\sigma(Z+b \text{ jet})} = \frac{f_b}{f_c f_{c/tag}} \times \frac{A_{\text{incl}}}{A_c}$$

where $N_{\text{incl}}$ is the total number of $Z +$ jet events before the tagging requirements, $N_{\text{HF}}$ is the number of $Z +$ jet events used in the $D_{\text{MIL}}$ fit, $f_{c/b}$ is the extracted $b(c)$ jet fraction, and $f_{c/b}$ is the selection efficiency for $b(c)$ jets, which combines the efficiencies for taggability and MVA$_b$ discriminant selection. $N_{\text{incl}}$ and $N_{\text{HF}}$ correspond to the number of events that remain after the contributions from various background processes have been subtracted. We subtract contributions from $t\bar{t}$, diboson, and multijet production to obtain $N_{\text{incl}}$, while we also subtract the $Z +$ light jet events when calculating $N_{\text{HF}}$.

The detector acceptances for the inclusive jet, $A_{\text{incl}}$, and $b(c)$ jets, $A_{b(c)}$, are determined from MC simulation in the kinematic region that satisfies the $p_T$ and $\eta$ requirements for leptons and jets. In these ratios, the effect of migration of events near the kinematic thresholds, or between neighboring kinematic bins, due to detector resolution is found to be negligible.

Using Eqs. (1), the ratio of the cross sections $Z + c$ jet to inclusive $Z +$ jet in the combined $\mu\mu$ and $ee$ channel, $R_{c/jet}$, is $0.0829 \pm 0.0052$ (stat.) and the ratio of cross sections $Z + c$ jet to $Z + b$ jet, $R_{c/b}$, is found to be $4.00 \pm 0.21$ (stat.). These ratios have also been measured differentially as a function of $p_T^c$ and $p_T^b$. For $R_{c/b}$, the highest-$p_T$ tagged jet from the HF enriched sample is used in the numerator, while the denominator uses the highest-$p_T$ jet from the $Z +$ jet sample. The selected bin sizes along with the corresponding statistics of data events are listed in Table I. In each case, all the quantities that enter into Eqs. (1) are determined in each bin separately.

Several systematic uncertainties cancel when the ratios are measured. These include uncertainties on the luminosity measurement, as well as trigger, lepton, and the jet reconstruction efficiencies. The remaining uncertainties are estimated separately for the integrated and differential results. For the two ratios the systematic uncertainties are estimated separately.

For the integrated $R_{c/jet}$ measurement, the largest systematic uncertainty of 8.1% comes from the estimation of the $Z +$ light jet background. This is quantified by comparing the value extracted from the data, using a three template (light, $c$, and $b$ jet) fit, for various MVA$_b$ selections. The next largest systematic uncertainty comes from the shape of the $D_{\text{MIL}}$ templates used in the fit. A variety of different aspects can affect the shape of the templates: two HF jets being reconstructed as a single jet; models of $b$ and $c$ quark fragmentation; the background from the non-$Z +$ jet events; the difference in the shape of the light jet MC template and a template derived from a light jet enriched dijet data sample; and the uncertainty of shape of the templates due to MC statistics. These are all evaluated by varying the central values by the corresponding uncertainties, one at a time, and repeating the entire analysis chain, resulting in a 5.5% uncertainty. An additional uncertainty of 3.4% comes from jet energy calibration; it comprises the uncertainties on the jet energy resolution and the jet energy scale. An uncertainty is also associated with the $c$ jet tagging efficiency (1.9%) [17]. Finally, a

<table>
<thead>
<tr>
<th>$p_T^c$ [GeV]</th>
<th>$N$</th>
<th>$R_{c/jet}$ [%]</th>
<th>$R_{c/b}$ [%]</th>
<th>$R_{c/jet}$ [%]</th>
<th>$R_{c/b}$ [%]</th>
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</thead>
<tbody>
<tr>
<td>20 – 30 (24.6)</td>
<td>741</td>
<td>0.068</td>
<td>12</td>
<td>16</td>
<td>3.64</td>
</tr>
<tr>
<td>30 – 40 (34.3)</td>
<td>525</td>
<td>0.084</td>
<td>11</td>
<td>12</td>
<td>3.97</td>
</tr>
<tr>
<td>40 – 60 (47.3)</td>
<td>474</td>
<td>0.099</td>
<td>11</td>
<td>9.1</td>
<td>3.98</td>
</tr>
<tr>
<td>60 – 200 (78.0)</td>
<td>380</td>
<td>0.085</td>
<td>13</td>
<td>11</td>
<td>4.30</td>
</tr>
<tr>
<td>$p_T^b$ [GeV]</td>
<td>0 – 20 (10.2)</td>
<td>285</td>
<td>0.041</td>
<td>29</td>
<td>22</td>
</tr>
<tr>
<td>20 – 40 (29.5)</td>
<td>763</td>
<td>0.073</td>
<td>8.2</td>
<td>12</td>
<td>6.10</td>
</tr>
<tr>
<td>40 – 60 (49.0)</td>
<td>588</td>
<td>0.104</td>
<td>10</td>
<td>11</td>
<td>5.06</td>
</tr>
<tr>
<td>60 – 200 (92.7)</td>
<td>487</td>
<td>0.108</td>
<td>13</td>
<td>8.3</td>
<td>3.41</td>
</tr>
</tbody>
</table>
small contribution (< 0.1%) is coming from the dependence of the acceptance on modeling of the signal events. When summed in quadrature the total systematic uncertainty for the integrated \( R_{c/jet} \) ratio is 10.6%. The corresponding total systematic uncertainty is 14.4% for \( R_{c/b} \). Table I lists the total statistical and systematic uncertainties (added in quadrature) for the differential results. Finally, for the integrated ratios we obtain values of \( R_{c/jet} = 0.0829 \pm 0.0052 \text{(stat.)} \pm 0.0089 \text{(syst.)} \) and \( R_{c/b} = 4.00 \pm 0.21 \text{(stat.)} \pm 0.58 \text{(syst.)} \).

The measurements are compared to predictions from an MCFM NLO pQCD calculation and three MC event generators, SHERPA [20], PYTHIA, and ALPGEN. The NLO predictions are based on MCFM [1], version 6.3, with the MSTW2008 PDFs [21] and the renormalization and factorization scales set at \( \mu_R = \mu_F = M_Z^2 + p_{T,\text{total}}^2 \). Here, \( M_Z \) is the Z boson mass and \( p_{T,\text{total}} \) is the scalar sum of the transverse momentum for all the jets with \( p_T > 20 \text{ GeV} \) and \( |\eta| < 2.5 \) in the event. Corrections are applied to account for non-perturbative effects, on the order of 5%, estimated using the ALPGEN+PYTHIA simulation. The NLO pQCD predictions of \( R_{c/jet} = 0.0368 \) and \( R_{c/b} = 1.64 \) [1] disagree significantly with the measurements. In the case where the intrinsic charm of the proton is enhanced, as suggested in the CTEQ6.6c PDF sets [13], MCFM yields ratios of \( R_{c/jet} = 0.0425 \) and \( R_{c/b} = 2.23 \), which are still in disagreement with our data.

The uncertainty on the \( R_{c/jet} \) theoretical predictions are evaluated by simultaneously changing the \( \mu_R \) and \( \mu_F \) scales up and down by a factor of two, yielding an uncertainty of up to 11% on \( R_{c/jet} \), while this uncertainty cancels in \( R_{c/b} \). However, this uncertainty is smaller than the effect due to the intrinsic charm enhancement, which is 15% and 36% for \( R_{c/jet} \) and \( R_{c/b} \), respectively.

ALPGEN generates multi-parton final states using tree-level MEs. When interfaced with PYTHIA, it employs the MLM scheme [22] to match ME partons with those after showering in PYTHIA, resulting in an improvement over leading-logarithmic accuracy.
SHERPA uses the CKKW matching scheme between the leading-order ME partons and the parton-shower jets following the prescription given in Ref. [23]. This effectively allows for a consistent combination of the ME and parton shower.

PYTHIA includes only 2 → 2 MEs with $gQ \rightarrow ZQ$ and $qq \rightarrow Zg$ scatterings followed by $g \rightarrow Q\bar{Q}$ splitting, where $Q$ is either a $b$ or $c$ quark. The Perugia0 tune [24] and the cteq6l1 PDF set are used for the PYTHIA predictions.

The ratios of differential cross sections as a function of $p_T^{\text{jet}}$ and $p_T^Z$ are compared to various predictions in Fig. 2. On average, the NLO predictions significantly underestimate the data, by a factor of 2.5 for the integrated results. As for the MC event generators, PYTHIA predictions are closer to data. An improved description can be achieved by enhancing the default rate of $g \rightarrow c\bar{c}$ in PYTHIA by a factor of 1.7, motivated by the $\gamma + c$ jet production measurements at the Tevatron [25, 26].

The largest discrepancy between data and predictions, in particular for the shape of the differential distributions, is for $R_{c/b}$ as a function of $p_T^Z$ (Fig. 2(d)). The level of disagreement in shape is quantified for the mcfm NLO prediction when its integrated result is scaled up to match the data. We generated a large number of pseudo-experiments and found the p-value for the four bins in $p_T^Z$ to simultaneously fluctuate to the observed $R_{c/b}$ values (or beyond) to be 2%.

We have presented the first measurements of the ratios of integrated cross sections, $\sigma(p\bar{p} \rightarrow Z + c \text{jet})/\sigma(p\bar{p} \rightarrow Z + \text{jet})$ and $\sigma(p\bar{p} \rightarrow Z + c \text{jet})/\sigma(p\bar{p} \rightarrow Z + b \text{jet})$, as well as the ratios of the differential cross sections in bins of $p_T^{\text{jet}}$ and $p_T^Z$, for events with a Z boson decaying to electrons or muons and at least one jet in the final state. Measurements are based on the data sample collected by the D0 experiment in Run II of the Tevatron, corresponding to an integrated luminosity of 9.7 fb$^{-1}$ at a center-of-mass energy of 1.96 TeV. For jets with $p_T^{\text{jet}} > 20$ GeV and $|p_T^{\text{jet}}| < 2.5$, the measured integrated ratios are $R_{c/b}^{\text{jet}} = 0.0829 \pm 0.0052$ (stat.) $\pm 0.0089$ (syst.), and $R_{c/b} = 4.00 \pm 0.21$ (stat.) $\pm 0.58$ (syst.). The NLO pQCD predictions disagree significantly with the results. PYTHIA agrees better with the measured ratios, especially when the gluon splitting to $c\bar{c}$ pairs is enhanced.

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[8] Pseudorapidity is defined as $\eta = -\ln[\tan(\theta/2)]$, with the polar angle $\theta$ measured relative to the proton beam direction.