FERMILAB-PUB-11-520-AD-AE-CD-TD

A search for ultra-high energy neutrinos in highly inclined events at the Pierre Auger Observatory

P. Abreu, S. Andringa, P. Assis, P. Brogueira, L. Cazon, R. Conceição,
J. Espadanal, P. Gonçalves, M. Pimenta, C.E. Santo, E. Santos, and B. Tomé
LIP and Instituto Superior Técnico, Technical University of Lisbon, Portugal

M. Aglietta, R. Bonino, A. Castellina, A. Chiavassa, A. Gorgi, S. Maldera, C. Morello, and G. Navarra
Istituto di Fisica dello Spazio Interplanetario (INAF),
Università di Torino and Sezione INFN, Torino, Italy

E.J. Ahn, A. Chou, N. Fazzini, H. Glass, C. Hojvat, P. Kasper, F. Kuehn, P. Lebrun, P. Mantsch, and P.O. Mazur
Fermilab, Batavia, IL, USA

I.F.M. Albuquerque, P. Gouffon, and D.B. Tridapalli
Universidade de São Paulo, Instituto de Física, São Paulo, SP, Brazil

D. Allard, G. Decerprit, C. Lachaud, E. Parizot, and G. Tristram
Laboratoire AstroParticule et Cosmologie (APC),
Université Paris 7, CNRS-IN2P3, Paris, France

I. Allekotte, H. Asorey, X. Bertou, G. Golup, M. Gómez Berisso, D. Harari, S. Mollerach, V.H. Ponce, and E. Roulet
Centro Atómico Bariloche and Instituto Balseiro (CNEA-UNCuyo-CONICET), San Carlos de Bariloche, Argentina

J. Allen, G. Farrar, J. Roberts, and I. Zaw
New York University, New York, NY, USA

P. Allison, B. Baughman, J.J. Beatty, E. Grashorn, N. Griffith, C. Morris, and J. Stapleton
Ohio State University, Columbus, OH, USA

J. Alvarez Castillo, J.C. D'Olivo, I. Fajardo Tapia, A. Guzman, G. Medina-Tanco, B. Morales,
L. Nellen, H.H. Silva Lopez, C.G. Tavera Ruiz, J.F. Valdés Galicia, and B. Vargas Cárdenas
Universidad Nacional Autonoma de Mexico, Mexico, D.F., Mexico

J. Alvarez-Muñiz, A. Lopez Agüera, V.M. Olmos-Gilbaja, G. Parente, A. Parra,
R. Pelayo, G. Rodriguez, I. Rodriguez-Cabo, R.A. Vázquez, and E. Zas
Universidad de Santiago de Compostela, Spain

M. Ambrosio, C. Aramo, D. D'Urso, F. Guarino, and L. Valore
Università di Napoli "Federico II" and Sezione INFN, Napoli, Italy

A. Aminaei, J.R. Hörandel, A. Horneffer, S. Jiraskova, and J.L. Kelley
IMAPP, Radboud University Nijmegen, Netherlands

L. Anchordoqui
University of Wisconsin, Milwaukee, WI, USA

T. Antičić, K. Kadija, S. Mićanović, and T. Šuša
Rudjer Bošković Institute, 10000 Zagreb, Croatia

A. Anzalone, O. Catalano, G. La Rosa, M.C. Maccarone, A. Segreto, and E. Strazzeri
Istituto di Astrofisica Spaziale e Fisica Cosmica di Palermo (INAF), Palermo, Italy

E. Arganda, F. Arqueros, F. Blanco, D. Garcia-Pinto, M. Ortiz, J. Rosado, and J.R. Vázquez
Universidad Complutense de Madrid, Madrid, Spain

J. Aublin, P. Billoir, R. Gaior, A. Letessier-Selvon, C. Macolino, I.C. Maris, and M. Münchmeyer
Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE),

Operated by Fermi Research Alliance, LLC under Contract No. De-AC02-07CH11359 with the United States Department of Energy.

Universités Paris 6 et Paris 7, CNRS-IN2P3, Paris, France

M. Ave, H. Dembinski, D. Gonzalez, J.G. Gonzalez, K. Link, M. Ludwig, M. Melissas, and N. Palmieri
Karlsruhe Institute of Technology - Campus South - Institut für Experimentelle Kernphysik (IEKP), Karlsruhe, Germany

M. Avenier, C. Berat, J. Chauvin, D.-H. Koang, D. Lebrun, F. Montanet, A. Stutz, and M. Tartare
Laboratoire de Physique Subatomique et de Cosmologie (LPSC),
Université Joseph Fourier, INPG, CNRS-IN2P3, Grenoble, France

G. Avila
Pierre Auger Southern Observatory and Comisión Nacional de Energía Atómica, Malargüe, Argentina

T. Bäcker, P. Buchholz, U. Fröhlich, M. Pontz, M. Risse, M. Settimo, R. Tcaciuc, P. Younk, and M. Ziolkowski
Universität Siegen, Siegen, Germany

M. Balzer, H. Gemmeke, M. Kleifges, O. Krömer, N. Kunka, A. Menshikov, C. Rühle, A. Schmidt, and M. Weber
Karlsruhe Institute of Technology - Campus North - Institut für Prozessdatenverarbeitung und Elektronik, Karlsruhe, Germany

K.B. Barber, J.A. Bellido, R.W. Clay, M.J. Cooper, B.R. Dawson, T.A. Harrison,
A.E. Herve, V.C. Holmes, J. Sorokin, P. Wahrlich, B.J. Whelan, and M.G. Winnick
University of Adelaide, Adelaide, S.A., Australia

A.F. Barbosa, J.C. dos Anjos, and B. Fuchs
Centro Brasileiro de Pesquisas Fisicas, Rio de Janeiro, RJ, Brazil

R. Bardenet, A. Cordier, S. Dagoret-Campagne, B. Kégl, K. Louedec, D. Monnier Ragaigne, and M. Urban
Laboratoire de l'Accélérateur Linéaire (LAL), Université Paris 11, CNRS-IN2P3, Orsay, France

S.L.C. Barroso
Universidade Estadual do Sudoeste da Bahia, Vitoria da Conquista, BA, Brazil

J. Bäuml, K. Daumiller, R. Engel, A. Haungs, D. Heck, T. Huege, B. Keilhauer,
H.O. Klages, J. Kleinfeller, H.J. Mathes, S. Mueller, J. Oehlschläger, T. Pierog, M. Roth,
H. Schieler, F. Schröder, M. Szuba, M. Unger, A. Weindl, M. Will, and M. Wommer
Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany

B.R. Becker, K. Gesterling, M.S. Gold, J.D. Hague, J.A.J. Matthews, W. Miller, and N. Phan
University of New Mexico, Albuquerque, NM, USA

K.H. Becker, C. Bleve, K.H. Kampert, N. Krohm, D. Kruppke-Hansen, D. Kuempel, J. Neuser,
L. Niemietz, N. Nierstenhoefer, P. Oliva, S. Querchfeld, J. Rautenberg, B. Sarkar, and O. Taşcău
Bergische Universität Wuppertal, Wuppertal, Germany

A. Bellétoile, R. Dallier, P. Lautridou, V. Marin, L. Martin, O. Ravel, and B. Revenu
SUBATECH, École des Mines de Nantes, CNRS-IN2P3, Université de Nantes, Nantes, France

S. BenZvi, C. Pfendner, and S. Westerhoff
University of Wisconsin, Madison, WI, USA

P.L. Biermann, L. Caramete, A. Curutiu, and I. Dutan
Max-Planck-Institut für Radioastronomie, Bonn, Germany

M. Blanco, L. del Peral, N. Pacheco, M.D. Rodríguez-Frías, and G. Ros
Universidad de Alcalá, Alcalá de Henares (Madrid), Spain

H. Blümer
Karlsruhe Institute of Technology - Campus South - Institut für Experimentelle Kernphysik (IEKP), Karlsruhe, Germany and
Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany

M. Boháčová, J. Chudoba, J. Ebr, D. Mandat, P. Necesal, L. Nožka, M. Nyklicek, M. Palatka, M. Pech, M. Prouza, J. Ridky, J. Schovancova, P. Schovánek, P. Travnicek, and J. Vicha
Institute of Physics of the Academy of Sciences of the Czech Republic, Prague, Czech Republic

D. Boncioli, G. Matthiae, P. Petrinca, G. Salina, and V. Verzi
Università di Roma II "Tor Vergata" and Sezione INFN, Roma, Italy

C. Bonifazi
Universidade Federal do Rio de Janeiro, Instituto de Física, Rio de Janeiro, RJ, Brazil and Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE), Universités Paris 6 et Paris 7, CNRS-IN2P3, Paris, France

N. Borodai, P. Homola, J. Pękala, J. Stasielak, B. Wilczyńska, and H. Wilczyński
Institute of Nuclear Physics PAN, Krakow, Poland

J. Brack, A. Dorofeev, C.E. Fracchiolla, B. Gookin, J.L. Harton, M. Mostafá, Y. Petrov, F. Salesa Greus, D. Thomas, and D. Warner
Colorado State University, Fort Collins, CO, USA

W.C. Brown
Colorado State University, Pueblo, CO, USA

R. Bruijn, H. Cook, S.R. Gozzini, J. Knapp, L. Lu, D. Newton, R.D. Parsons, and A.A. Watson
School of Physics and Astronomy, University of Leeds, United Kingdom

A. Bueno, A. Gascon, J. Lozano Bahilo, L. Molina-Bueno, J.L. Navarro, S. Navas, and B. Zamorano
Universidad de Granada & C.A.F.P.E., Granada, Spain

R.E. Burton, C.E. Covault, and A.P. Ferguson
Case Western Reserve University, Cleveland, OH, USA

K.S. Caballero-Mora, S.H. Cheng, S. Coutu, A. Criss, and P. Sommers
Pennsylvania State University, University Park, PA, USA

R. Caruso, M. De Domenico, A. Insolia, A. Italiano, V. Pirronello, M. Scuderi, and E. Trovato
Università di Catania and Sezione INFN, Catania, Italy

G. Cataldi, M.R. Coluccia, I. De Mitri, U. Giaccari, and D. Martello
Dipartimento di Fisica dell'Università del Salento and Sezione INFN, Lecce, Italy

R. Cester, D. Maurizio, E. Menichetti, R. Mussa, and A. Tonachini
Università di Torino and Sezione INFN, Torino, Italy

J.A. Chinellato, W.J.M. de Mello Junior, C. Dobrigkeit, C.O. Escobar, A.C. Fauth, E. Kemp, M.A. Muller, and D. Pakk Selmi-Dei
Universidade Estadual de Campinas, IFGW, Campinas, SP, Brazil

F. Contreras, J. Rodriguez Martino, J. Rodriguez Rojo, R. Sato, and R. Squartini
Pierre Auger Southern Observatory, Malargüe, Argentina

J. Coppens, S.J. de Jong, S. Grebe, A. Nelles, and H. Schoorlemmer
IMAPP, Radboud University Nijmegen, Netherlands and Nikhef, Science Park, Amsterdam, Netherlands

A. Creusot
Laboratoire AstroParticule et Cosmologie (APC), Université Paris 7, CNRS-IN2P3, Paris, France and Laboratory for Astroparticle Physics, University of Nova Gorica, Slovenia

J. Cronin, P. Facal San Luis, N. Hollon, F. Ionita, K. Kotera, M. Monasor, A. Olinto, P. Privitera, B. Rouillé-d'Orfeuil, F. Schmidt, C. Williams, and T. Yamamoto
University of Chicago, Enrico Fermi Institute, Chicago, IL, USA

S. Dasso
Instituto de Astronomía y Física del Espacio (CONICET-UBA), Buenos Aires, Argentina and Departamento de Física, FCEyN, Universidad de Buenos Aires y CONICET, Argentina

R.M. de Almeida
Universidade Federal Fluminense, EEIMVR, Volta Redonda, RJ, Brazil

C. De Donato
Universidad Nacional Autonoma de Mexico, Mexico, D.F., Mexico and Università di Milano and Sezione INFN, Milan, Italy

G. De La Vega, B. García, and M. Videla
National Technological University, Faculty Mendoza (CONICET/CNEA), Mendoza, Argentina

J.R.T. de Mello Neto and E.M. Santos
Universidade Federal do Rio de Janeiro, Instituto de Física, Rio de Janeiro, RJ, Brazil

V. de Souza
Universidade de São Paulo, Instituto de Física, São Carlos, SP, Brazil

K.D. de Vries, W. Docters, E.D. Fraenkel, O. Scholten, and A.M. van den Berg
Kernfysisch Versneller Instituut, University of Groningen, Groningen, Netherlands

M. del Río
Università di Roma II "Tor Vergata" and Sezione INFN, Roma, Italy and Pierre Auger Southern Observatory, Malargüe, Argentina

O. Deligny, A. Lemiere, I. Lhenry-Yvon, H. Lyberis, and T. Suomijärvi
Institut de Physique Nucléaire d'Orsay (IPNO), Université Paris 11, CNRS-IN2P3, Orsay, France

N. Dhital, J.C. Diaz, B. Fick, R.M. Kieckhafer, D. Nitz, and T. Yapici
Michigan Technological University, Houghton, MI, USA

C. Di Giulio
Università dell'Aquila and INFN, L'Aquila, Italy and Università di Roma II "Tor Vergata" and Sezione INFN, Roma, Italy

M.L. Díaz Castro
Pontifícia Universidade Católica, Rio de Janeiro, RJ, Brazil

P.N. Diep, P.T. Nhung, and N.T. Thao
Institute for Nuclear Science and Technology (INST), Hanoi, Vietnam

P.N. Dong
Institute for Nuclear Science and Technology (INST), Hanoi, Vietnam and Institut de Physique Nucléaire d'Orsay (IPNO), Université Paris 11, CNRS-IN2P3, Orsay, France

M.T. Dova, F. Gomez Albarracin, P. Hansen, C. Jarne, A.G. Mariazzi, J.C. Moreno, S.J. Sciutto, and H. Wahlberg
IFLP, Universidad Nacional de La Plata and CONICET, La Plata, Argentina

M. Erdmann, S. Fliescher, M. Grigat, T. Hebbeker, C. Meurer, G. Müller, N. Scharf, P. Schiffer, S. Schulte, M. Stephan, Walz, K. Weidenhaupt, and T. Winchen
RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany

A. Etchegoyen, A. Ferrero, A. Filevich, R.F. Gamarra, M. Josebachuili, M. Platino,
D. Ravignani, F. Sánchez, I. Sidelnik, F. Suarez, A. Tapia, O. Wainberg, and B. Wundheiler
Centro Atómico Constituyentes (Comisión Nacional de Energía Atómica/CONICET/UTN-FRBA), Buenos Aires, Argentina

H. Falcke
IMAPP, Radboud University Nijmegen, Netherlands and
ASTRON, Dwingeloo, Netherlands

A. Filipčič and M. Zavrtanik
J. Stefan Institute, Ljubljana, Slovenia and
Laboratory for Astroparticle Physics, University of Nova Gorica, Slovenia

S. Gambetta, R. Pesce, and A. Petrolini
Dipartimento di Fisica dell'Università and INFN, Genova, Italy

D. García Gámez
Laboratoire de l'Accélérateur Linéaire (LAL), Université Paris 11, CNRS-IN2P3, Orsay, France and
Universidad de Granada & C.A.F.P.E., Granada, Spain

P.L. Ghia
Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE),
Universités Paris 6 et Paris 7, CNRS-IN2P3, Paris, France and
Istituto di Fisica dello Spazio Interplanetario (INAF),
Università di Torino and Sezione INFN, Torino, Italy

M. Giller, A. Śmiałkowski, W. Tkaczyk, and G. Wieczorek
University of Łódź, Łódź, Poland

D. Góra
Karlsruhe Institute of Technology - Campus South - Institut für Experimentelle Kernphysik (IEKP), Karlsruhe, Germany and
Institute of Nuclear Physics PAN, Krakow, Poland

A.F. Grillo
INFN, Laboratori Nazionali del Gran Sasso, Assergi (L'Aquila), Italy

Y. Guardincerri, R. Piegaia, P. Pieroni, and J. Tiffenberg
Departamento de Física, FCEyN, Universidad de Buenos Aires y CONICET, Argentina

G.P. Guedes
Universidade Estadual de Feira de Santana, Brazil

S. Harmsma
Kernfysisch Versneller Instituut, University of Groningen, Groningen, Netherlands and
Nikhef, Science Park, Amsterdam, Netherlands

P. Horvath and T. Rossler
Palacky University, RCATM, Olomouc, Czech Republic

M. Hrabovský
Palacky University, RCATM, Olomouc, Czech Republic and
Institute of Physics of the Academy of Sciences of the Czech Republic, Prague, Czech Republic

P. Karhan and D. Nosek
Charles University, Faculty of Mathematics and Physics,
Institute of Particle and Nuclear Physics, Prague, Czech Republic

A. Keivani, A. Shadkam, and G. Yuan
Louisiana State University, Baton Rouge, LA, USA

J.K. Kulbartz and G. Sigl
Universität Hamburg, Hamburg, Germany

M.S.A.B. Leão and M.A. Leigui de Oliveira
Universidade Federal do ABC, Santo André, SP, Brazil

R. López, O. Martínez Bravo, E. Moreno, C. Robledo, H. Salazar, and E. Varela
Benemérita Universidad Autónoma de Puebla, Puebla, Mexico

A. Lucero
Centro Atómico Constituyentes (Comisión Nacional de Energía Atómica/CONICET/UTN-FRBA), Buenos Aires, Argentina and Istituto di Fisica dello Spazio Interplanetario (INAF), Università di Torino and Sezione INFN, Torino, Italy

J. Marin
Pierre Auger Southern Observatory, Malargüe, Argentina and Istituto di Fisica dello Spazio Interplanetario (INAF), Università di Torino and Sezione INFN, Torino, Italy

H.R. Marquez Falcon, D.K. Tiwari, and L. Villaseñor
Universidad Michoacana de San Nicolas de Hidalgo, Morelia, Michoacan, Mexico

G. Marsella and L. Perrone
Dipartimento di Ingegneria dell'Innovazione dell'Università del Salento and Sezione INFN, Lecce, Italy

H. Martinez and A. Zepeda
Centro de Investigación y de Estudios Avanzados del IPN (CINVESTAV), México, D.F., Mexico

J. Matthews
Louisiana State University, Baton Rouge, LA, USA and Southern University, Baton Rouge, LA, USA

D. Melo
Centro Atómico Constituyentes (Comisión Nacional de Energía Atómica/CONICET/UTN-FRBA), Buenos Aires, Argentina and Università di Torino and Sezione INFN, Torino, Italy

P. Mertsch and S. Sarkar
Rudolf Peierls Centre for Theoretical Physics, University of Oxford, Oxford, United Kingdom

M.I. Micheletti
Instituto de Física de Rosario (IFIR) - CONICET/U.N.R. and Facultad de Ciencias Bioquímicas y Farmacéuticas U.N.R., Rosario, Argentina

L. Miramonti, H. Rivera, and V. Scherini
Università di Milano and Sezione INFN, Milan, Italy

C.A. Moura
Universidade Federal do ABC, Santo André, SP, Brazil and Università di Napoli "Federico II" and Sezione INFN, Napoli, Italy

J. Pallotta, E.J. Quel, and P. Ristori
Centro de Investigaciones en Láseres y Aplicaciones, CITEFA and CONICET, Argentina

S. Pastor
Instituto de Física Corpuscular, CSIC-Universitat de València, Valencia, Spain

T. Paul and J. Swain

Northeastern University, Boston, MA, USA

I.M. Pepe
Universidade Federal da Bahia, Salvador, BA, Brazil

E. Petermann and G.R. Snow
University of Nebraska, Lincoln, NE, USA

S. Petrera and V. Rizi
Università dell'Aquila and INFN, L'Aquila, Italy

J. Petrovic
Nikhef, Science Park, Amsterdam, Netherlands

S. Riggi
Universidad de Santiago de Compostela, Spain and
Università di Catania and Sezione INFN, Catania, Italy

W. Rodrigues de Carvalho
Universidad de Santiago de Compostela, Spain and
Universidade de São Paulo, Instituto de Física, São Paulo, SP, Brazil

A.C. Rovero and A. Tamashiro
Instituto de Astronomía y Física del Espacio (CONICET-UBA), Buenos Aires, Argentina

F. Salamida
Università dell'Aquila and INFN, L'Aquila, Italy and
Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany

F. Sarazin, D. Schuster, and L. Wiencke
Colorado School of Mines, Golden, CO, USA

R.C. Shellard
Centro Brasileiro de Pesquisas Fisicas, Rio de Janeiro, RJ, Brazil and
Pontifícia Universidade Católica, Rio de Janeiro, RJ, Brazil

R. Šmída
Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany and
Institute of Physics of the Academy of Sciences of the Czech Republic, Prague, Czech Republic

H. Spinka
Argonne National Laboratory, Argonne, IL, USA and
Fermilab, Batavia, IL, USA

S. Stanic
Laboratory for Astroparticle Physics, University of Nova Gorica, Slovenia

A.D. Supanitsky
Instituto de Astronomía y Física del Espacio (CONICET-UBA), Buenos Aires, Argentina and
Universidad Nacional Autonoma de Mexico, Mexico, D.F., Mexico

M.S. Sutherland
Louisiana State University, Baton Rouge, LA, USA and
Ohio State University, Columbus, OH, USA

Z. Szadkowski
University of Łódź, Łódź, Poland and
Bergische Universität Wuppertal, Wuppertal, Germany

D. Tegolo
Università di Catania and Sezione INFN, Catania, Italy and
Università di Palermo and Sezione INFN, Catania, Italy

C. Timmermans
Nikhef, Science Park, Amsterdam, Netherlands and
IMAPP, Radboud University Nijmegen, Netherlands

C.J. Todero Peixoto
Universidade de São Paulo, Instituto de Física, São Carlos, SP, Brazil and
Universidade Federal do ABC, Santo André, SP, Brazil

M. Tueros
Universidad de Santiago de Compostela, Spain and
Departamento de Física, FCEyN, Universidad de Buenos Aires y CONICET, Argentina

R. Ulrich
Pennsylvania State University, University Park, PA, USA and
Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany

I. Valiño
Universidad de Santiago de Compostela, Spain and
Karlsruhe Institute of Technology - Campus North - Institut für Kernphysik, Karlsruhe, Germany

D. Veberič and D. Zavrtanik
Laboratory for Astroparticle Physics, University of Nova Gorica, Slovenia and
J. Stefan Institute, Ljubljana, Slovenia

A. Yushkov
Universidad de Santiago de Compostela, Spain and
Università di Napoli "Federico II" and Sezione INFN, Napoli, Italy

M. Zimbres Silva
Bergische Universität Wuppertal, Wuppertal, Germany and
Universidade Estadual de Campinas, IFGW, Campinas, SP, Brazil
(The Pierre Auger Collaboration)

The Surface Detector of the Pierre Auger Observatory is sensitive to neutrinos of all flavours above 0.1 EeV. These interact through charged and neutral currents in the atmosphere giving rise to extensive air showers. When interacting deeply in the atmosphere at nearly horizontal incidence, neutrinos can be distinguished from regular hadronic cosmic rays by the broad time structure of their shower signals in the water-Cherenkov detectors. In this paper we present for the first time an analysis based on down-going neutrinos. We describe the search procedure, the possible sources of background, the method to compute the exposure and the associated systematic uncertainties. No candidate neutrinos have been found in data collected from 1 January 2004 to 31 May 2010. Assuming an E^{-2} differential energy spectrum the limit on the single flavour neutrino is $E^2 \mathrm{d}N/\mathrm{d}E < 1.74 \times 10^{-7}$ GeV cm^{-2} s^{-1} sr^{-1} at 90% C.L. in the energy range $1 \times 10^{17}\mathrm{eV} < E < 1 \times 10^{20}\mathrm{eV}$.

PACS numbers: 95.55.Vj, 95.85.Ry, 98.70.Sa

I. INTRODUCTION

Neutrinos play a key role in the understanding of the origin of ultra high energy cosmic rays (UHECRs). Their observation should open a new window to the universe since they can give information on regions that are otherwise hidden by large amounts of matter in the field of view. Moreover, neutrinos are not deviated by magnetic fields and would point back to their sources.

In the EeV range, neutrinos are expected to be produced in the same sources where UHECRs are thought to be accelerated, as well as during the propagation of UHECRs through the cosmic microwave background (CMB) radiation [1]. The latter are called cosmogenic neutrinos and their presence is expected if the UHECRs above the spectral cut-off reported in [2] contain a significant fraction of protons [3–8].

There are many current programs to search for high

energy neutrinos with dedicated experiments [9–11]. Although the primary goal of the Pierre Auger Observatory Surface (SD) and Fluorescence Detectors (FD) is to detect UHECRs, UHE neutrinos (UHEνs) can also be identified and limits to the diffuse flux of UHEνs in the EeV range and above have been set using earlier Auger data [12–14]. Earth-skimming τ neutrinos are expected to be observed through the detection of showers induced by the decay of emerging τ leptons which are created by ν_τ interactions in the Earth [15]. Using this mechanism for data collected from 1 January 2004 until 30 April 2008, an upper limit was set: $E_\nu^2 dN_{\nu_\tau}/dE_\nu < 6^{+3}_{-3} \times 10^{-8}\,\mathrm{GeV\,cm^{-2}s^{-1}sr^{-1}}$ at 90% CL for each neutrino flavour [16]. The SD of the Pierre Auger Observatory has also been shown to be sensitive to "down-going" neutrinos of all flavours interacting in the atmosphere or in the mountains surrounding the SD, and inducing a shower close to the ground [14, 17, 18]. In this paper we present an analysis based on down-going neutrinos and place a competitive limit on the all-flavour diffuse neutrino flux using data from 1 January 2004 until 31 May 2010.

The main challenge in detecting UHE neutrinos with the Pierre Auger Observatory is to identify a neutrino-induced shower in the background of showers initiated by UHECRs, possibly protons or heavy nuclei [19] and, in a much smaller proportion, even photons [20].

The identification of ν-induced showers is illustrated in Fig. 1. If the incidence is nearly horizontal, "old" showers induced in the upper atmosphere by protons, nuclei or photons have a thin and flat front at ground level, containing only high energy muons and their radiative and decay products, concentrated within a few tens of nanoseconds. On the other hand, "young" showers, induced by neutrinos at a low altitude, have a thick, curved front with a significant electromagnetic component spread in time over hundreds of nanoseconds, specially in their earlier part that traverses less atmosphere. In this work, to obtain an unambiguous identification of neutrinos, we select showers with zenith angle $\theta > 75°$ and we apply criteria to ensure a deep interaction. Using less inclined showers is in principle possible, but will require a better control of the various sources of background.

The method was tuned using data taken at the SD in the period from 1 January 2004 until 31 October 2007. A blind scan over the data collected in the remaining period, i.e., from 1 November 2007 until 31 May 2010 reveals no candidates and we place a stringent limit on the diffuse flux of UHE neutrinos.

For that purpose, we calculate the probability for a shower, produced deeply in the atmosphere, to trigger the SD and to be identified as a neutrino candidate. This probability depends on the neutrino flavour and type of interaction – charged current (CC) or neutral current (NC) – and is also a function of neutrino energy E_ν, incident zenith angle θ, and atmospheric interaction depth. From these identification probabilities we calculate the exposure of the SD to deep inclined neutrino showers. We give an estimate of the systematic uncertainties on the diffuse neutrino flux limit, and discuss the implications of our observations for models of UHE neutrino production.

II. THE PIERRE AUGER OBSERVATORY

The Pierre Auger Observatory is a hybrid detector located in Malargüe, Mendoza, Argentina [21]. It consists of an array of particle detectors [22] and a set of fluorescence telescopes [23] at four sites that provide a unique cross calibration capability.

The SD is spread over a surface of $\sim$3000 km^2 at an altitude of $\sim$1400 m above sea level. This corresponds to an average vertical atmospheric depth above ground of $X_{ground} = 880$ g cm^{-2}. The slant depth D is the total grammage traversed by a shower measured from ground in the direction of the incoming primary particle. In the flat-Earth approximation $D = (X_{ground} - X_{int})/\cos\theta$, where X_{int} is the interaction depth and θ the zenith angle. For very inclined showers the curvature of the atmosphere is taken into account.

The four fluorescence sites are located at the perimeter of the surface array viewing the atmosphere above it [23]. In this work only data collected with the SD of the Pierre Auger Observatory are used to search for down-going neutrinos.

A. The Surface Detector

Since the beginning of its operation for physics analysis, in January 2004, the SD array has grown steadily and it has been recording an increasing amount of data. It consists of $\sim$1660 detector units (water-Cherenkov stations) regularly spaced in a triangular grid of side 1.5 km. Each detector unit is a cylindrical polyethylene tank of 3.6 m diameter and 1.2 m height containing 12,000 liters of purified water. The top surface has three photomultiplier tubes (PMTs) in optical contact with the water in the tank. The PMT signals are sampled by flash analog digital converters (FADC) with a frequency of 40 MHz. Each surface detector is regularly monitored and calibrated in units of vertical equivalent muons (VEM) corresponding to the signal produced by a μ traversing the tank vertically and through its center [24]. The surface stations transmit information by radio links to the Central Data Acquisition System (CDAS) located in Malargüe. The PMTs, local processor, GPS receiver, and the radio system are powered by batteries regulated by solar panels. Once installed, the local stations work continuously without external intervention.

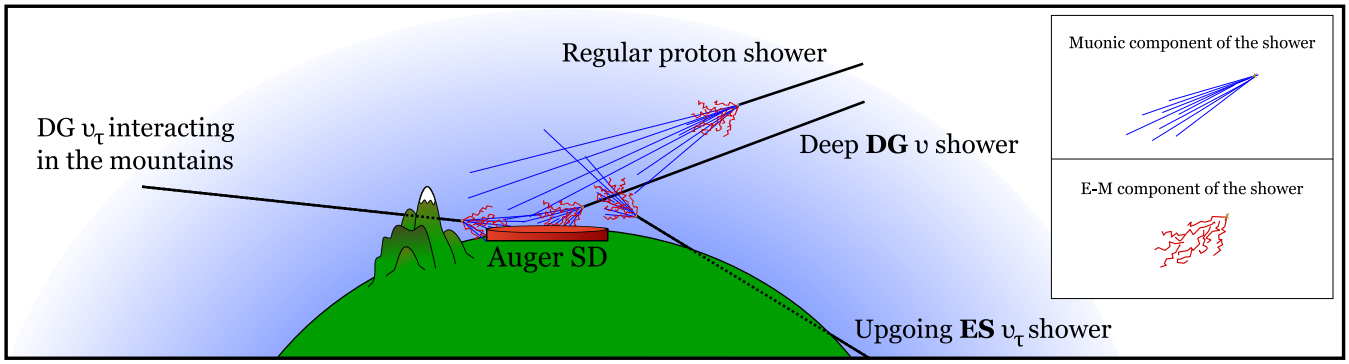

FIG. 1. Pictorial representation of the different types of showers induced by protons, heavy nuclei and "down-going" (DG) as well as "Earth-skimming" (ES) neutrinos. The search for down-going showers initiated deep in the atmosphere is the subject of this work.

B. The trigger

A local trigger selects signals, either with a high peak value, or with a long duration. The second condition favours stations hit in the early stage of the shower development (moderately inclined or deeply induced showers). The global trigger requires either 4 stations satisfying one of the conditions, or 3 stations satisfying the second one, in a compact configuration (see [25] for more details).

With the complete array, the global trigger rate is about two events per minute, one half being actual shower events with median energy of 3×10^{17} eV.

III. SIMULATION OF NEUTRINO INTERACTIONS, INDUCED SHOWERS AND THE RESPONSE OF THE SURFACE DETECTOR.

Monte Carlo simulations of neutrino-induced showers are used to establish identification criteria and to compute the acceptance of the SD to UHEνs. The whole simulation chain is divided in three stages:

1. High energy processes:
   - The ν-nucleon interaction is simulated with HERWIG [26].
   - In the case of ν_τ CC interactions, the τ lepton propagation is simulated with a dedicated code and its decay (when necessary) with TAUOLA [27].
2. The shower development in the atmosphere is processed by AIRES [28].
3. The Surface Detector simulation is performed with the $\overline{\text{Off}}\underline{\text{line}}$ software [29].

In the next subsections we discuss each stage in detail.

A. Neutrino interaction

HERWIG is a general-purpose event generator for high-energy processes, with particular emphasis on the detailed simulation of QCD parton showers. Here it is used to compute the fraction of the primary energy that goes into the hadronic vertex and to provide the secondary particles produced for both charged (CC) and neutral current (NC) interactions (see Fig. 2 for a summary of all the channels considered in this work).

The energy carried by the hadronic jet is always converted into a shower which could be seen by the SD. In addition, the energy of the lepton produced in a CC interaction may be totally or partially visible. An electron is promptly converted into an electromagnetic shower. A τ at EeV energies has a decay length of $\sim$ 50 km and may decay before reaching the ground producing a secondary shower that can be detected (so called "double bang" event). On the other hand, it is very unlikely that a high energy muon will produce a detectable shower, so its interaction and/or decay are not simulated. For all channels and neutrino flavours a set of primary ν interactions is constructed from a grid of incoming neutrino energies, zenith angles and interaction depths. In "double bang" events the decay products of the τ lepton are generated by TAUOLA. The energies and momenta of the secondary particles are then injected into the program AIRES to generate the atmospheric cascade.

B. Down-going neutrinos interacting in the mountains

In addition to the interactions in the atmosphere, we also take into account the possibility of τ neutrino interactions within the mountains around the Pierre Auger Observatory (mainly the Andes located to the north-west of the array), producing a hadronic jet and a τ lepton. The hadronic or electromagnetic showers produced by neutrinos of any flavour are absorbed either in

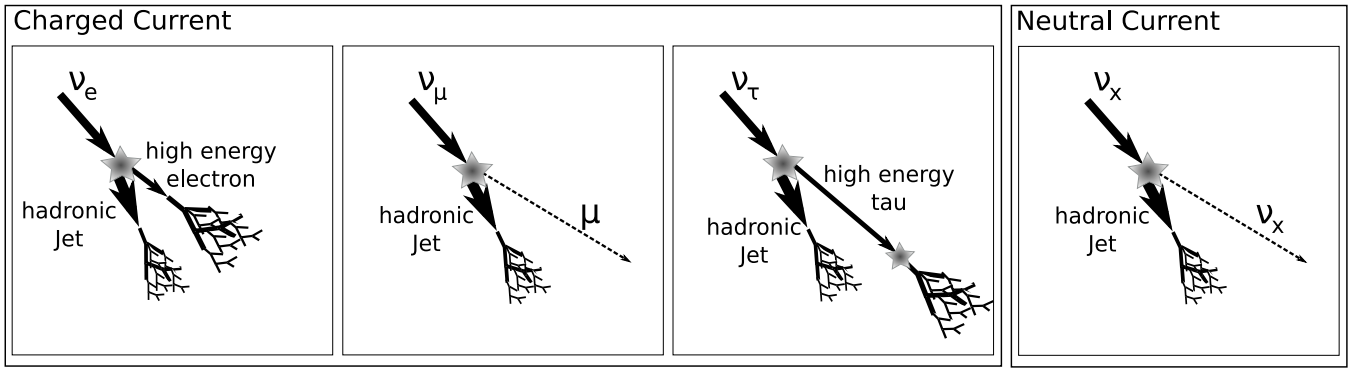

FIG. 2. Different types of atmospheric showers induced by neutrinos.

the rock itself, or in the few ten kilometers of atmosphere between the mountains and the Auger array, and may be neglected. So only showers induced by the decay of the τs may be seen. In other terms, this process is exactly equivalent to the "Earth-skimming" mechanism, but it is included in this study because such showers are going downwards.

The topography surrounding the SD of the Auger Observatory is accounted for using a digital elevation map [30]. For the Auger site, the line of sight intercepting the mountains corresponds only to zenith angles very close to the horizon ($\theta > 89°$). Even though the solid angle is much smaller than for showers with $\theta > 75°$, this mechanism is still relevant because mountains are much more massive. It is simulated in the same way as the "double bang" process, accounting in addition for energy loss of the τ lepton in the rock [31].

C. Detector simulation

To avoid excessively long computing times AIRES uses the standard thinning procedure [32] consisting in following only some branches in the tree of interactions in the atmosphere. Weights are attributed to the surviving branches, obtaining a representative set of particles at any stage, especially at ground level. The first step in the detector response simulation is to regenerate a fair sample of the particles expected in each station from the thinned output of AIRES. This unthinning procedure is detailed in [33]. Each particle reaching a surface detector station is injected in the station, and the amount of Cherenkov light produced in water calculated with GEANT4 [34]. The FADC traces of the PMT signals are simulated using the $\overline{\text{Off}}\underline{\text{line}}$ framework [29]. The total signal due to the particles entering the station, as well as several quantities characterizing the FADC trace which will be relevant for neutrino identification (see below) are then calculated. The local and global trigger conditions are applied in the same way as for real data.

IV. INCLINED EVENT SELECTION AND RECONSTRUCTION

Events occurring during periods of data acquisition instabilities [25] are excluded. After a "trace cleaning" procedure removing the accidental signals (mainly atmospheric muons), the start times of the signals in the stations are requested to be compatible with a plane shower front moving at speed c. If this condition is not fulfilled using all stations included in the global trigger, an iterative procedure removes stations until a satisfactory configuration is found with at least four stations. Otherwise the event is rejected. The angle between a vertical axis and the perpendicular direction to this plane is the reconstructed zenith angle θ_{rec} of the shower. Nearly horizontal showers are selected by requiring $\theta_{rec} > 75°$. In some cases a non-inclined event, produced by detector fluctuations or two independent showers arriving close in time (less that 60 ns), may be incorrectly reconstructed as inclined. To remove these events we also compute the apparent speed of propagation of the trigger between every pair of stations (V_{ij}) and the average speed of the event ($\langle V \rangle$), as in [16]. Genuine inclined showers have a "footprint" (configuration of the stations) elongated in the direction of arrival (left panel of Fig. 3). The apparent speed of propagation of the signal, along the major axis of the footprint, is concentrated around the speed of light c.

Under the plane front approximation, the zenith angle is $\simeq \arcsin(c/\langle V \rangle)$. In Fig. 4 we show the distribution of $\langle V \rangle$ for events with $\theta_{rec} > 75°$ acquired between 1 January 2004 and 31 October 2007. The shaded region corresponds to misreconstructed or low quality events (see right panel of Fig. 3 for an example). To remove these events we optimized a set of quality cuts using a MC sample of 5000 regular inclined showers initiated by hadrons near the top of the atmosphere: $\langle V \rangle$ is required to be less than 0.313 m ns^{-1}, with a relative spread smaller than 0.08%. Also, the "footprint" is required to be elongated: $L/W > 3$, where L and W are the length and the width (eigenvalues of the inertia tensor, as defined

in [16]). These cuts reject only 10% of genuine inclined showers.

For events where all stations are aligned along one of the directions of the array, θ_{rec} cannot be computed and we rely on the average speed of the event, $\langle V \rangle$. These "in-line" events are of great importance since the Monte Carlo simulations show that low energy neutrinos ($\lesssim 10^{18}$ eV) typically present this type of configuration in the SD.

There is an additional requirement for events constituted by an in-line event plus a non-aligned station (a non-aligned event that would become in-line by removing just one station). This kind of spatial configuration is particularly prone to bad reconstruction if the non-aligned station was triggered by accidental muons not belonging to the shower front. To avoid this problem we also reconstruct the in-line event obtained by the removal of the non-aligned station and require it to have mean ground speed compatible with a zenith angle larger than 75°.

V. IDENTIFICATION OF NEUTRINO CANDIDATES

For this analysis, the whole data period (1 Jan 04 - 31 May 10), was divided into two separate samples. Selected events recorded between 1 Jan 04 and 31 Oct 07 (equivalent to ~ 1.4 years of a complete SD array working continuosly) constitute the "training" sample, used to develop and optimize the neutrino identification algorithms. Data collected between 1 Nov 07 and 31 May 10 (equivalent to $\sim$ 2 yr of the full array), constitute the "search" sample. These latter events were not processed before the final tuning of the algorithms defining the neutrino identification criteria.

A. Discrimination of neutrinos from hadronic showers

Neutrinos, unlike protons and heavier nuclei, can generate showers initiated deeply into the atmosphere. The main signature of these deep showers in the SD is a significant electromagnetic (EM) component spread in time over hundreds of nanoseconds, especially in the region on the ground at which the shower arrives earlier (see Fig. 5). On the other hand, hadron-induced showers start high in the atmosphere, their electromagnetic component is fully absorbed and only high energy muons and their radiative and decay products reach the surface, concentrated within a few tens of nanoseconds.

We identify stations reached by wide EM-rich shower fronts via their Area-over-Peak ratio (AoP), defined as the ratio of the integral of the FADC trace to its peak value, normalized to 1 for the average signal produced by a single muon. In background horizontal showers the muons and their electromagnetic products are concentrated within a short time interval, so their AoP is close to 1. In the first stations hit by a deep inclined shower, it is typically between 3 and 5 (see left panel of Fig. 6).

To keep a simple physical interpretation of the identification process we chose a multivariate technique known as the Fisher discriminant method [35]. To tune it we used as a "signal" sample the Monte Carlo simulations – exclusively composed of neutrino-induced showers – and as "background" the training sample introduced above – overwhelmingly, if not totally, constituted of nucleonic showers. We use real data to train the Fisher discrimination method, instead of simulations of hadronic showers, for two main reasons:

- the composition of the primary flux is not known, and moreover the interaction models used to simulate hadronic showers may bias some features of the tail of the distributions of the observables used in this analysis.
- the detector simulation may not account for all possible detector defects or fluctuations that may contribute to the background to ultra-high energy neutrinos, while the real data contain all of them, including those which are not well known, or even not yet diagnosed.

Note that, since we apply a statistical method for the discrimination, the use of real data as a background sample does not imply that we assume it contains no neutrinos, but just that, if any, they constitute a small fraction of the total recorded events.

After training the Fisher method, a good discrimination is found when using the following ten variables [14]: the AoP of the four earliest triggered stations in each event, their squares, their product, and a global early-late asymmetry parameter of the event. We include the square of the AoP because when the distribution of the input variables is not gaussian the addition of a non-linear combination of them improves the discrimination power [36]. The product of the AoP of the earliest four stations in the event aims at minimizing the relative weight of an accidentally large AoP produced, for instance, by a single muon which does not belong to the shower front arriving at a station before or after the shower itself. This variable is also a very good discriminator as shown in the right panel of Fig. 6. The early-late asymmetry parameter is a global observable of the event defined as the difference between the mean AoP of the earliest and latest stations in the event. We have checked in simulations that neutrino-induced events typically have an asymmetry parameter larger than proton or nucleus-induced showers [14]. Finally, the addition of other observables characterizing the time spread of the signals, such as the rise-time (between 10% and 50% of the integrated signal) or the fall-time (between 50% and 90%), or including local observables of the stations that trigger last in the event, do not bring about significant improvements in the discrimination.

As the shower front is broader at larger distance from the core for both young and old showers, the discrim-

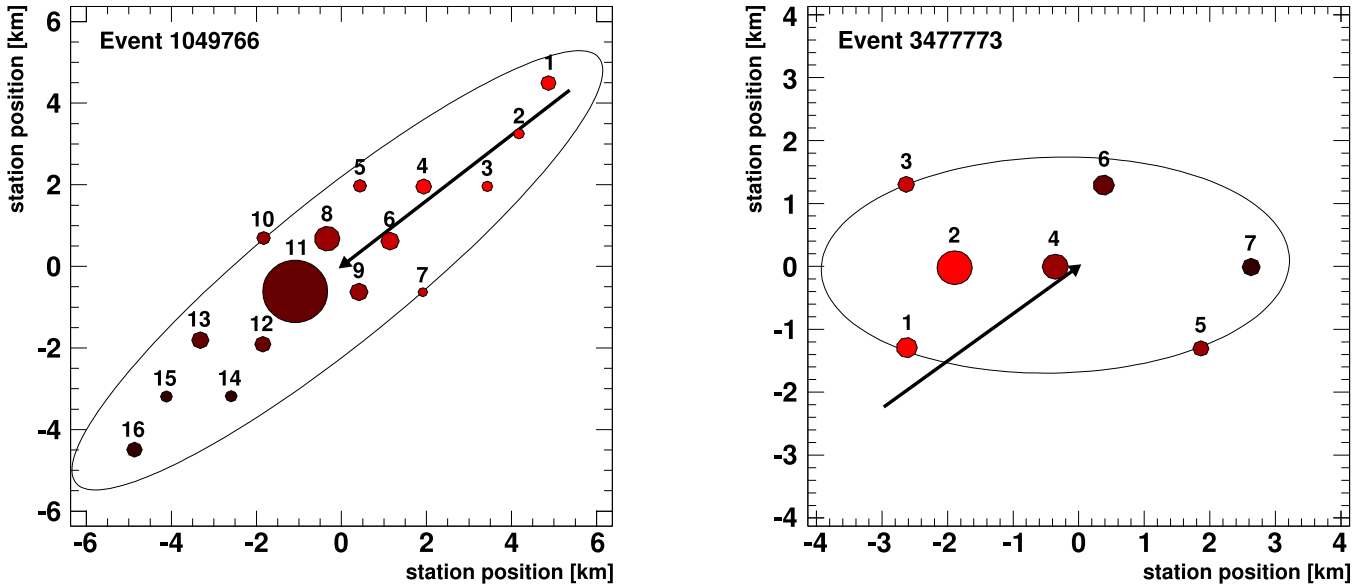

FIG. 3. *Left panel:* Event produced by a nearly horizontal shower ($\theta_{rec} = 80°$). The footprint (ellipse) is elongated along the reconstructed direction of arrival (arrow). *Right panel:* a non-inclined event with $\theta_{rec} = 79°$. The major axis of the footprint and the reconstructed direction of arrival do not point in the same direction. Close inspection of the event suggests that stations 3 and 5 are accidental and corrupt the reconstruction. The numbers indicate the triggering order of the stations.

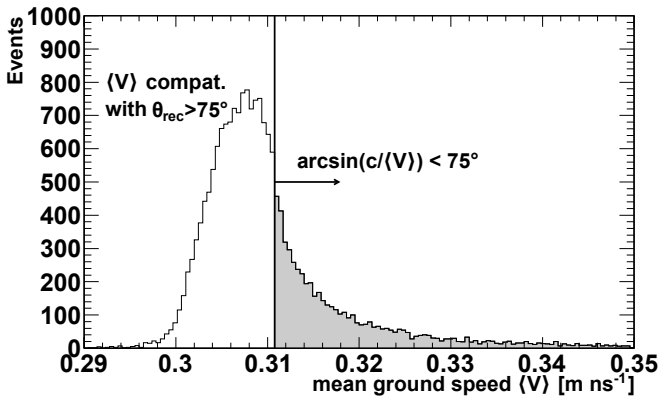

FIG. 4. Distribution of the mean ground speed of the signal for events with $\theta_{rec} > 75°$ acquired between 1 January 2004 and 31 October 2007.

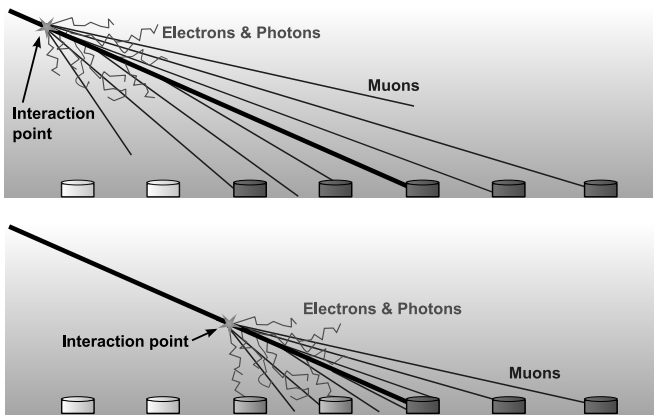

FIG. 5. *Upper panel*: sketch of an inclined shower induced by a hadron interacting high in the atmosphere. The EM component is absorbed and only the muons reach the detector. *Lower panel*: deep inclined shower. Its early region has a significant EM component at the detector level.

ination is better when splitting the samples according to the multiplicity N (number of selected stations). A Fisher discriminant was built separately for $4 \leq N \leq 6$, $7 \leq N \leq 11$ and $N \geq 12$. Left panel of Fig. 7 shows the excellent separation achieved for events in each of the 3 sub-samples.

Once the Fisher discriminant $\mathcal{F}$ is defined, one has to choose a threshold value that separates neutrino candidates from regular hadronic showers. Because the predictions of the neutrino detection rates are very low, we want to keep the expected rate of background events incorrectly classified as neutrinos well below any detectable signal: in practice, we wish it to be less than one event for each multiplicity subsample within the expected 20-year lifetime of the Auger Observatory.

The training period was used to produce a reasonable prediction of the background. We observe that the tail of the background distribution of $\mathcal{F}$ is consistent with an exponential shape. In this way, we produced a fit to the distribution of $\mathcal{F}$ for the training data in the $[1\sigma, 3\sigma]$ region, where σ is the RMS of the training sample. This procedure is illustrated in Fig. 7. We then extrapolated it to find the cuts corresponding to 1 event per 1, 20 or

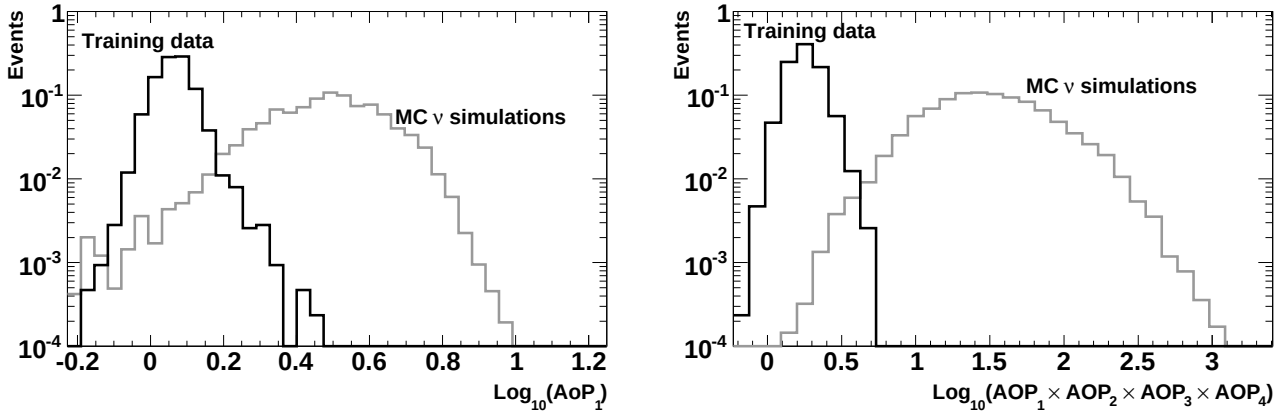

FIG. 6. Distributions of the AoP of the earliest station (left) and the product of the first four AoP (right) in background (real events in the training sample) and simulated ν_e CC events. There is a clear separation between both samples indicating that the AoP of the early stations is a good discrimination observable to be used in the Fisher method. See text for more details.

100 years on the full array. The validity of the extrapolation is not guaranteed, but some physical arguments support an exponential tail, such as the fact that showers produced by nuclei or protons (or even photons) have a distribution of X_{max} that shows an exponential shape, dictated by the distribution of the primary interaction. The exponential model may be checked below the cut by comparing the actual number of events observed in the $[3\sigma, 4\sigma]$, $[4\sigma, 5\sigma]$, $[5\sigma, 6\sigma]$ and $[6\sigma, 7\sigma]$ regions, to the number of events predicted by extrapolating the fit done in the $[1\sigma, 3\sigma]$ region. The values are in good agreement as shown in Fig. 7. For our search sample (equivalent to two years of full detector data) we have an estimated background of 0.1 events for each multiplicity class that add up to a total of 0.3 events with a statistical uncertainty of 30%. As we do not have at present a robust estimation of the background systematics we take a conservative approach and do not use this value to improve our flux upper limit.

As can be seen in Fig. 7 the identification cuts reject a small fraction of the neutrino events. Consequently, its choice has only a small impact on the neutrino identification efficiency. The neutrino-induced showers rejected by these cuts are those interacting far from the ground and similar to nucleonic-induced showers.

VI. IDENTIFICATION EFFICIENCIES AND EXPOSURE

During the data taking, the array was growing and had sporadic local inefficiencies. Simulations of deep inclined neutrino showers indicate that besides an elongated pattern on the ground they have a large longitudinal uncertainty on the core position. For these reasons we cannot apply (as done in the case of vertical showers [25]) a geometrical method relying on the estimated position of the shower core within a triangle or hexagon of active stations at each time. Moreover, a shower can trigger the surface detector even if the core falls outside the array. Besides, for deep inclined showers the trigger and identification efficiencies depend not only on the shower energy and zenith angle but also on the depth of the first interaction. For these reasons a specific procedure was designed to compute the time dependent acceptance and the integrated exposure.

The instantaneous status of the array is obtained from the trigger counting files, which respond to the modifications of the array configuration at every second. To avoid having to cope with an enormous number of configurations, we approximate the calculation of the aperture by subdividing the search period in three-day intervals, and we select a reference array configuration to represent each. Once this is done we calculate the neutrino identification efficiencies and the aperture assuming that the array remains unchanged during each three-day interval. Each reference configuration was chosen so that this approximation, if wrong, underestimates the exposure by a small amount ($\sim 1\%$).

MC generated neutrino showers produced by AIRES were randomly distributed over an extended circular area around the array, such that a shower with a core falling outside this area has no chance to trigger the array. For each three-day configuration the FADC traces of the active Cherenkov stations were simulated, the local and global trigger conditions were applied and the events were processed through the same reconstruction and identification algorithms as the data (Sec. V).

Fig. 8 shows an example of a shower that would be a neutrino candidate in an ideal array, placed at four random positions on the circular surface defined above. Two of the realizations are effectively recognized as neutrino events in the real array for that particular layout. The other two are either not seen, or not identified as neutri-

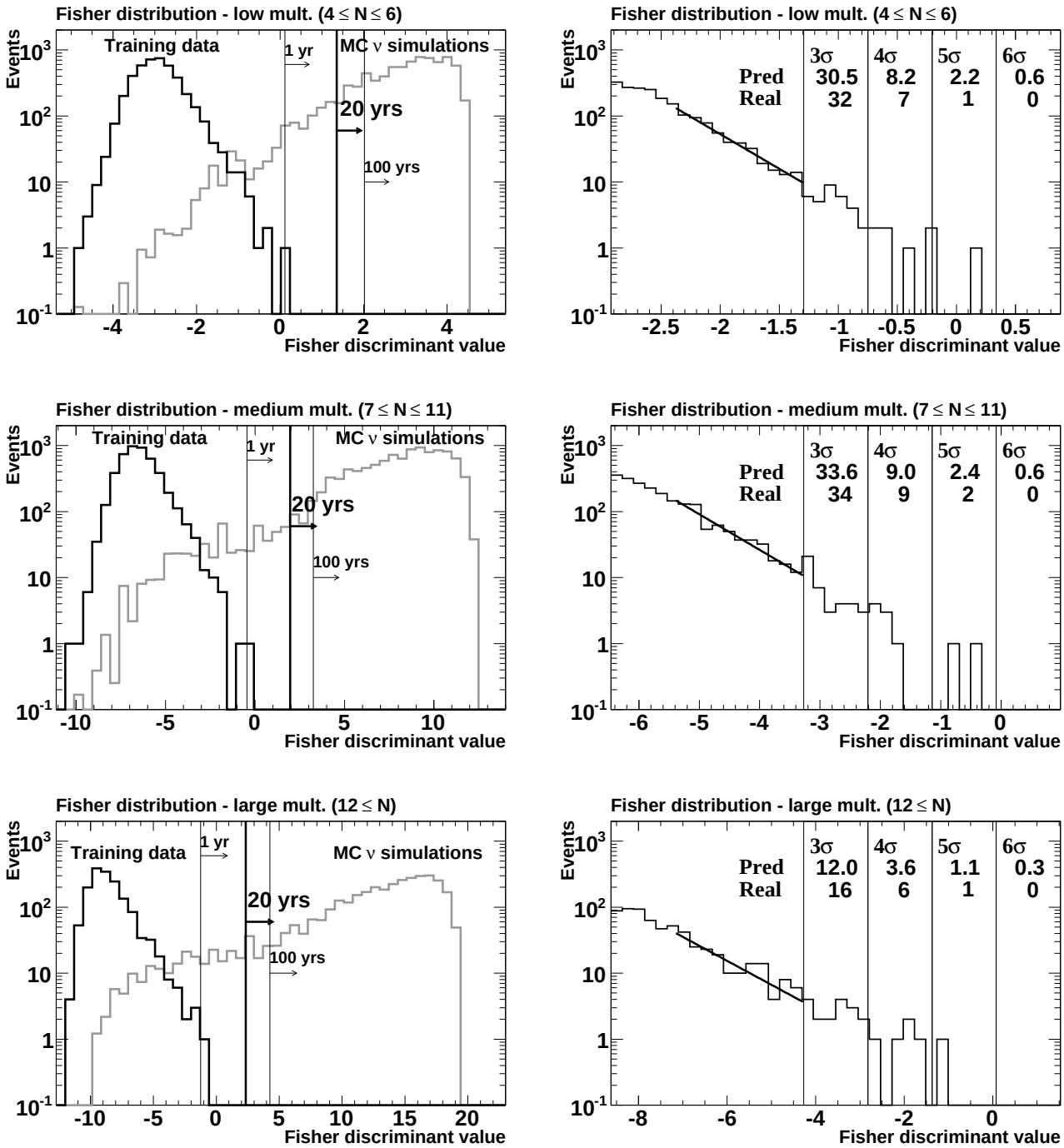

FIG. 7. *Left panel:* distribution of the Fisher discriminant (see text for details) for events with station multiplicity $4 \leq N \leq 6$ (*top*), $7 \leq N \leq 11$ (*middle*), $12 \leq N$ (*bottom*). Real data in the training period (1 Jan 04 - 31 Oct 07) describe the nucleonic background, while Monte Carlo simulated down-going neutrinos correspond to the signal. The vertical lines indicate the cut in the Fisher value that needs to be placed to have less than 1 event in each period of time (1 yr, 20 yr, 100 yr). *Right panel:* fit of an exponential function to the distribution of the Fisher discriminant $\mathcal{F}$ for the training data over the $[1\sigma, 3\sigma]$ interval. The predicted (Pred.), see text, and actual (Real) number of events are given for each of the test zones ($[3\sigma, 4\sigma]$, $[4\sigma, 5\sigma]$, $[5\sigma, 6\sigma]$ and $[6\sigma, 7\sigma]$).

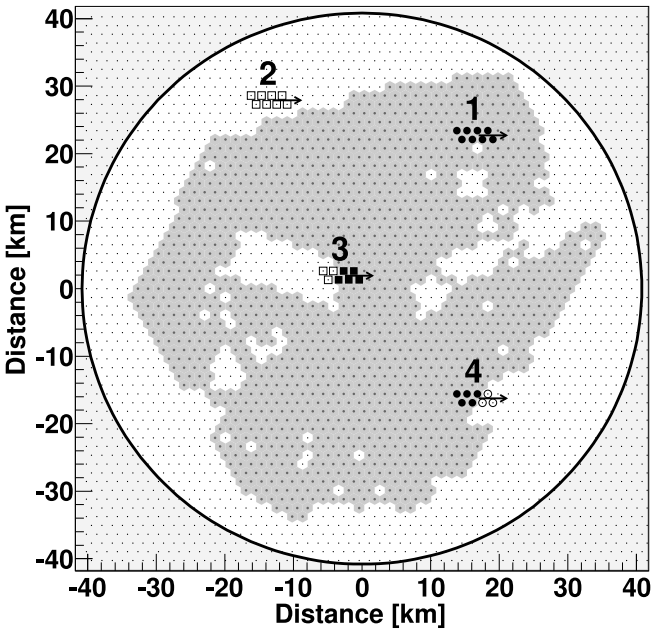

FIG. 8. An example of the result of placing the same deeply penetrating neutrino-induced shower at 4 different positions in an actual array configuration (shaded area) corresponding to 27 Oct 2007. The arrows indicate the azimuthal arrival direction of the shower, the dots represent the infinite ideal array and the circumference the extended area (see text). Solid symbols – either circles or squares – correspond to triggered stations of the simulated shower that are also on the actual array. Open symbols are stations that are not in the real array. Shower 1 is completely contained and identified as a neutrino. Shower 2 falls entirely outside the real array and it does not trigger the array. Although shower 3 triggers the array, it is not identified as a neutrino because the earliest three stations are not in the real array. Shower 4 loses some stations but keeps the earliest which are enough to identify the event as a neutrino.

nos.

Fig. 9 shows the efficiency (fraction of events which pass all steps) as a function of interaction depth in the atmosphere for neutrinos of $E_\nu = 10^{18}$ eV and $\theta = 80°$, in an "ideal" array without holes nor edges. There is essentially a plateau between a minimal depth (needed for the ν-induced shower to reach a sufficient lateral expansion) and a maximal one (such that the electromagnetic component is almost extinguished at ground level) . Below and above this plateau, the efficiency drops rapidly to zero. In other words, for a given channel and given values of θ and E_ν, there is a slice of atmosphere above the array where the interactions are detected and distinguished: the matter contained in this volume will be referred to as the "mass aperture" in the following.

For each three-day period, we compute the effective area defined as the integral of the efficiency over core

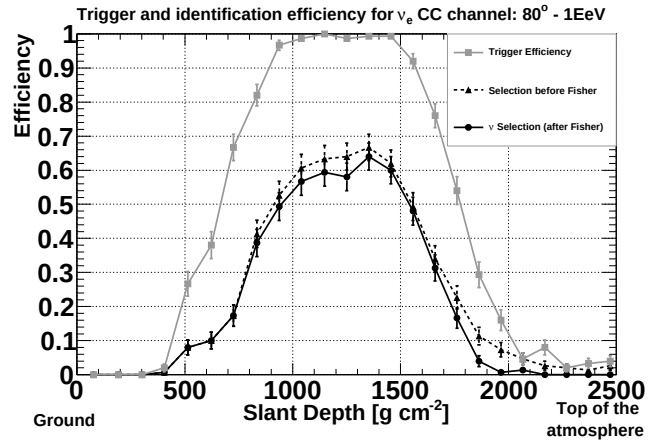

FIG. 9. Example of trigger and identification efficiency as a function of the slant depth of the interaction above the ground. Notice that the Fisher discriminant neutrino selection actually keeps most of the neutrino showers that pass the quality and reconstruction cuts discussed in Section IV.

position:

$$A_{\rm eff}(E_\nu, \theta, D, t) = \int \varepsilon(\vec{r}, E_\nu, \theta, D, t)\, {\rm d}A. \qquad (1)$$

The effective mass aperture $M_{\rm eff}(E_\nu, t)$ is obtained by integrating over the injection depth D and the solid angle:

$$M_{\rm eff}(E_\nu, t) = 2\pi \iint \sin\theta \cos\theta \; A_{\rm eff}(E_\nu, \theta, D, t)\, {\rm d}\theta\, {\rm d}D. \qquad (2)$$

To compute this integral we perform a spline interpolation on the finite three-dimensional mesh where $A_{\rm eff}$ is determined. The total mass aperture is then obtained summing $M_{\rm eff}(E_\nu, t)$ over different configurations corresponding to a certain period of time. It is defined independently of the ν-nucleon cross-section.

A combined exposure can be obtained by a summation over the search period:

$$\mathcal{E}(E_\nu) = \sum_i \left[\omega^i\, \sigma^i(E_\nu) \int \frac{M^i_{\rm eff}(E_\nu, t)}{m}\, {\rm d}t \right]. \qquad (3)$$

The sum runs over the three neutrino flavours (with fractions ω^i) and the CC and NC interactions; m is the mass of a nucleon. Here we assume a full $\nu_\tau \leftrightarrow \nu_\mu$ mixing, leading to $\omega^i = 1$ for the three flavours.

We use the ν–nucleon cross-section given in [37] (CSS hereafter) to compute the reference exposure of our search period. It is shown in Fig. 10 as a function of neutrino energy. In Table I we also give the mass aperture integrated in time for all the considered channels, allowing the reader to compute the exposure using different cross-sections or flux models.

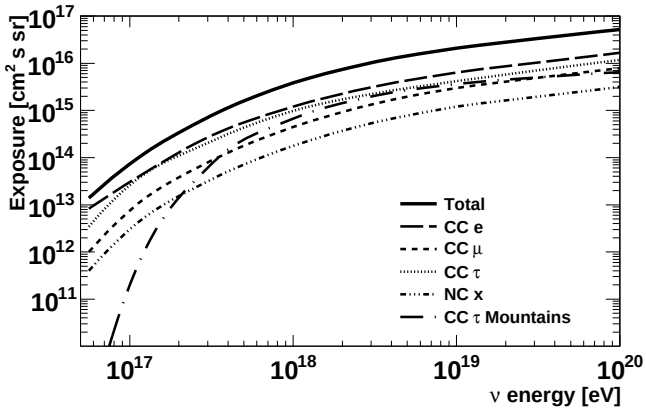

FIG. 10. SD Exposure for our search period for down-going neutrino-initiated showers. The total exposure is shown as a full line. The exposure for individual neutrino flavours and interaction channels is also shown.

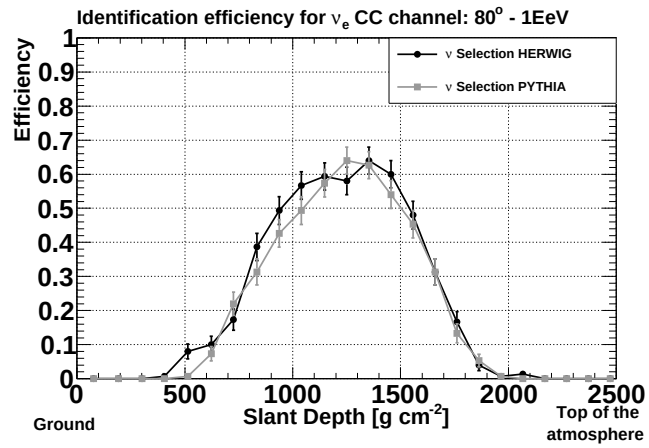

FIG. 11. Identification efficiency as function of the slant depth for systematic uncertainties studies. Comparison between interaction generators (HERWIG and PYTHIA). The rest of the Monte Carlo input parameters remain the same.

$\log E$/eV	ν_e CC	ν_μ CC	ν_τ CC	ν_x NC	ν_τ Mount.
16.75	$4.35 \cdot 10^{21}$	$5.27 \cdot 10^{20}$	$1.82 \cdot 10^{21}$	$2.11 \cdot 10^{20}$	-
17	$1.27 \cdot 10^{22}$	$3.16 \cdot 10^{21}$	$1.09 \cdot 10^{22}$	$1.26 \cdot 10^{21}$	-
17.5	$7.94 \cdot 10^{22}$	$2.34 \cdot 10^{22}$	$6.02 \cdot 10^{22}$	$9.37 \cdot 10^{21}$	$1.98 \cdot 10^{22}$
18	$2.17 \cdot 10^{23}$	$8.01 \cdot 10^{22}$	$1.77 \cdot 10^{23}$	$3.20 \cdot 10^{22}$	$1.21 \cdot 10^{23}$
18.5	$3.95 \cdot 10^{23}$	$1.71 \cdot 10^{23}$	$2.84 \cdot 10^{23}$	$6.84 \cdot 10^{22}$	$2.51 \cdot 10^{23}$
19	$5.44 \cdot 10^{23}$	$2.56 \cdot 10^{23}$	$3.58 \cdot 10^{23}$	$1.03 \cdot 10^{23}$	$3.13 \cdot 10^{23}$
19.5	$6.32 \cdot 10^{23}$	$2.99 \cdot 10^{23}$	$4.36 \cdot 10^{23}$	$1.20 \cdot 10^{23}$	$3.06 \cdot 10^{23}$
20	$7.29 \cdot 10^{23}$	$3.45 \cdot 10^{23}$	$5.19 \cdot 10^{23}$	$1.38 \cdot 10^{23}$	$2.82 \cdot 10^{23}$

TABLE I. Effective mass aperture integrated over time for the search period (1 Nov 2007 to 31 May 2010) for down-going neutrinos of the Pierre Auger Surface Detector (in units of [g sr s]).

VII. SYSTEMATIC UNCERTAINTIES

The calculation of the mass aperture of the Auger Observatory for neutrino showers requires the input of several ingredients which we have selected from amongst conventionally used options. Some of these choices are directly related to the Monte Carlo simulation of the showers, i.e. generator of the first neutrino interaction, parton distribution function (PDF), air shower development and hadronic model. Others have to do with the precision of our knowledge of the topography of the mountains surrounding the Observatory, and some come from the limitations on the theoretical models estimating, for instance, the interaction cross-section or the τ energy loss at high energies. By adding linearly all these contributions, our estimate of the total systematic uncertainty on the exposure amounts to +22% -46%.

In the following subsections we discuss in detail the dependence of the exposure on each of the above mentioned choices by modifying the different ingredients one by one.

A. Monte Carlo simulation of the shower

The reference Monte Carlo neutrino sample was produced with HERWIG 6.5.10 [26] as interaction generator in combination with the CTEQ06m [38] parton distribution functions, AIRES 2.8 as shower simulator (thinning value of 10^{-6}) and QGSJETII.03 [39] as hadronic model.

In order to assess the influence of this particular choice of models on the detector aperture, independent sets of CC ν_e showers were generated at 1 EeV and 80° using different combinations of several interaction generators, PDFs, shower simulators, thinning values and hadronic models. We chose this particular energy and angle bin because it is the one that contributes the most to the limit.

In Fig. 11 we show, as an example, the detection efficiency as a function of the slant depth when using our reference options (HERWIG) and when changing only the interaction generator (PYTHIA). Since the shapes of the neutrino-selection efficiency curves remain similar, we can estimate the effect of changing the interaction generator by computing the integral of the curves and reporting the relative difference (RD) between them. The same procedure is applied to estimate the effect of changing other ingredients of the simulation. A summary of this RDs is given in Table II.

We observe that the changes in interaction generator, PDF, shower simulator and hadronic model brought about a decrease of the estimated aperture, with the choice of the shower simulation being the dominating effect. On the other hand, an improvement of the relative thinning level causes the opposite effect. Although we cannot recompute the aperture for all possible alternatives of the relevant ingredients, the relative differences reported in Table II serve as an estimate of the systematic dependence of our result on the simulation options.

Parameter	Reference (A)	Modification (B)	RD $\frac{\int \mathbf{B} - \int \mathbf{A}}{(\int \mathbf{B} + \int \mathbf{A})/\mathbf{2}}$
Interaction generator	HERWIG	PYTHIA [40]	-7%
		HERWIG++ [41]	-7%
PDF (gen. level)	CTEQ06m	MSTW [42]	-7%
Shower Simulator	AIRES	CORSIKA 6.9 [43]	-17%
Hadronic Model	QGSJETII	QGSJETI [44]	+2%
		SIBYLL [45]	-2%
		SIBYLL (E=0.3 EeV)	-1%
		SIBYLL (E=3 EeV)	-2%
		SIBYLL (θ=85°)	0%
		SIBYLL (θ=89°)	+4%
Thinning	10^{-6}	10^{-7}	+7%

TABLE II. Summary of the relative differences (RD) between the reference calculation of the exposure and the calculations done changing one of the ingredients of the Monte Carlo simulations at a time. The RD were obtained for zenith angle θ=80° and energy E=1 EeV unless otherwise stated. The statistical uncertainty of all the relative differences is ±4%.

For each category of potential systematic effects in Table II, we take the maximum observed RD as an estimate of the corresponding systematic uncertainty. A total systematic uncertainty of +9% -33% on the exposure is obtained by linear addition of the maximum positive and negative deviations.

B. ν–nucleon cross-sections and τ energy loss

We adopted the uncertainty in the ν-nucleon cross-section as calculated in [37]. It translates into a ±7 % uncertainty in the total exposure. In any case, as mentioned above, Table I shows the Auger mass aperture for down-going neutrinos which does not depend on the ν cross-section; hence the expected neutrino event rate (and neutrino flux limit) can be computed as necessary for other models and values of the ν cross-section (see e.g. [46, 47]).

C. Topography

As explained in section III B, the actual topography surrounding the Observatory has been taken into account by detailed Monte Carlo simulations which include digital elevation maps. In principle, uncertainties due to different tau energy loss models should not be important for down-going neutrinos, but, due to the fact that the Pierre Auger Observatory is close to the Andes, a non negligible contribution to the event rate from down-going τ neutrinos interacting in the mountains and producing a τ lepton is expected (see Table III). The systematic error on the total reference exposure due to this channel amounts to ±6%, dominated by the uncertainties on the cross-section and energy loss models.

VIII. RESULTS AND DISCUSSION

In this section we present the calculation of the upper limit to the diffuse flux of UHEνs and compare our results to some selected model predictions and discuss the implications.

A. Upper limit on the diffuse neutrino flux

Once the multivariate algorithms and selection cuts defining a neutrino candidate were studied and tuned with the Monte Carlo simulations and the training data sample, we applied them to the search data sample. We first tested the compatibility between the shapes of the tails of the Fisher distributions during training and search periods by using an unbinned Kolmogorov hypothesis test, and found them to be in agreement with p-values of 0.37, 0.16 and 0.17 for the small, medium and large multiplicity classes.

We found no candidate events in the search period (see Fig. 12). The highest test zone with events in the Fisher distribution of the search sample is the 6-7 sigma region. It has only one event and we expected 2.2 from the exponential fit to the test sample.

The expected number of events from a diffuse flux of neutrinos in a given energy range is given by:

$$N_{\text{expected}} = \int_{E_{\min}}^{E_{\max}} \Phi(E_\nu)\, \mathcal{E}(E_\nu)\, \mathrm{d}E_\nu, \qquad (4)$$

where $\mathcal{E}(E_\nu)$ is our reference exposure (eq. 3 and Fig. 10). The upper limit is derived for a differential neutrino flux $\Phi(E_\nu) = k \cdot E_\nu^{-2}$. Also, we assume that due to neutrino oscillations the diffuse flux is composed of electron, muon and τ neutrinos in the same proportion. We expect less than one background event after the neutrino selection procedure is applied to the data sample corresponding to the reference exposure (see section 5). Given the uncertainties of this estimate, the number of background events will be assumed to be zero, which results in a more conservative upper limit. A semi-Bayesian extension [48] of the Feldman- Cousins approach [49] is used to include the uncertainty in the exposure, giving an upper limit at 90% CL on the integrated flux of diffuse neutrinos of:

$$k < 1.74 \times 10^{-7}\ \text{GeV cm}^{-2}\ \text{s}^{-1}\ \text{sr}^{-1}. \qquad (5)$$

The effect of including the systematics from MC, ν–nucleon cross-sections and τ energy loss is to increase the limit by 15%. The limit is quoted for a single neutrino flavour. The relative importance of each neutrino flavour in the determination of the upper limit can be derived from Table III, which gives the expected fractions of neutrinos in the selected sample according to their flavour and interaction channel. The largest contribution comes from ν_e CC. The second largest is ν_τ CC, due to double-bang interactions and the large average fraction of energy going into the shower in the decay of the

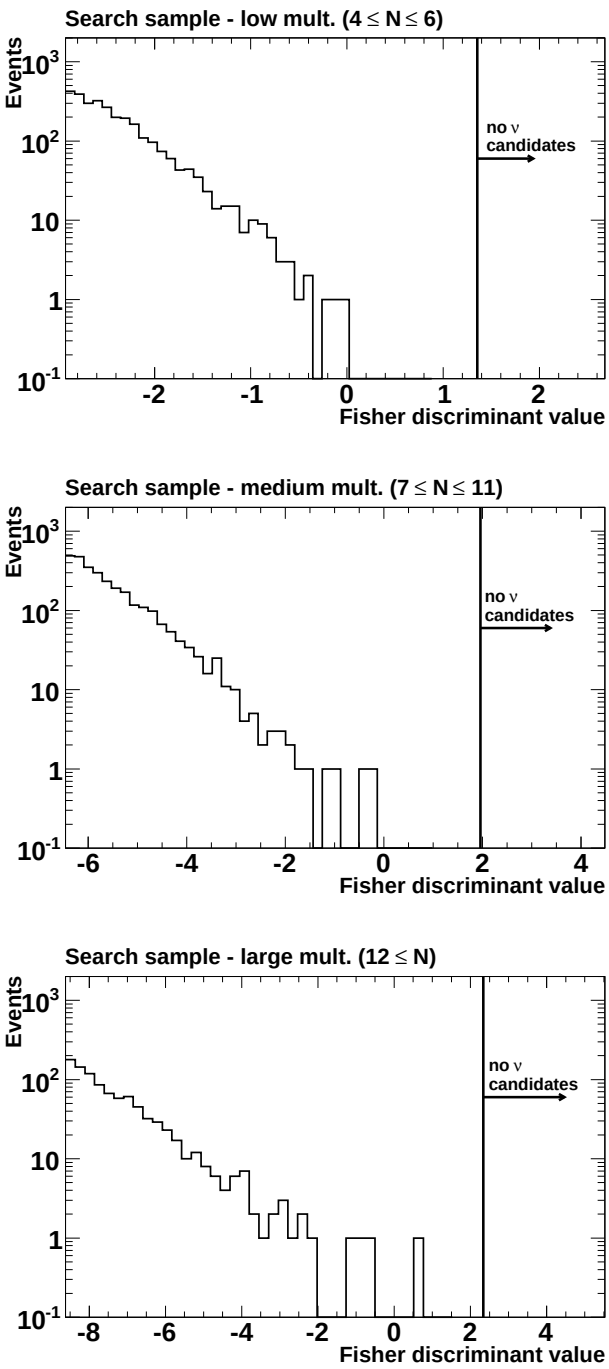

FIG. 12. Fisher distribution of the search sample (1 Nov 07 - 31 May 10) for events with multiplicity $4 \leq N \leq 6$ (*top*), $7 \leq N \leq 11$ (*middle*), $12 \leq N$ (*bottom*). No neutrino candidates are found.

τ lepton. Our result together with other experimental limits [50] is shown in Fig. 13.

Another usual way of presenting the upper bound is in the less-model-dependent differential form. It assumes that the diffuse neutrino flux behaves as $\sim 1/E^2$ within energy bins of unity width on a natural logarithmic scale,

Channel	CC	NC	Total
e	33%	5%	38%
μ	13%	5%	18%
τ air	24%	5%	29%
τ mountains	15%		15%
Total	85%	15%	100%

TABLE III. Expected fractions of neutrinos in the selected sample according to their flavour and interaction channel (CC and NC). These fractions are derived assuming that electron, muon and τ neutrinos are in the same proportion in the diffuse flux.

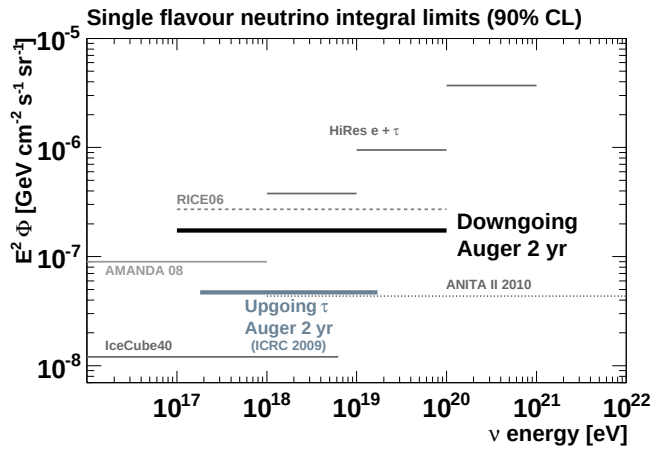

FIG. 13. Integrated upper limits (90% CL) from the Pierre Auger Observatory for a diffuse flux of down-going ν in the period 1 Nov 2007 - 31 May 2010. For comparison up-going ν_τ (1 Jan 2004 - 28 Feb 09)[13] and limits from other experiments [50] are also plotted.

and is given by $2.44/\mathcal{E}(E_\nu)E_\nu$ accounting for statistical uncertainties only and assuming no background [51]. The differential limit obtained including systematic uncertainties is shown in Fig. 14, together with our previous result on up-going ν_τ [13] and two theoretical predictions for cosmogenic neutrinos [6, 7]. We observe that we achieve maximum sensitivity in the 0.3-10 EeV energy range.

B. Model predictions

There is a wide variety of models predicting fluxes of neutrinos with energies in the EeV range [1]. They are usually separated into three groups: cosmogenic neutrinos [e.g. 6, 7], neutrinos produced in accelerating sources [e.g. 53, 54] and neutrinos of exotic origin [e.g. 52]. In all these models there are parameters with unknown values which can change the spectral shape and strength of the flux. In Table IV we give the event rates

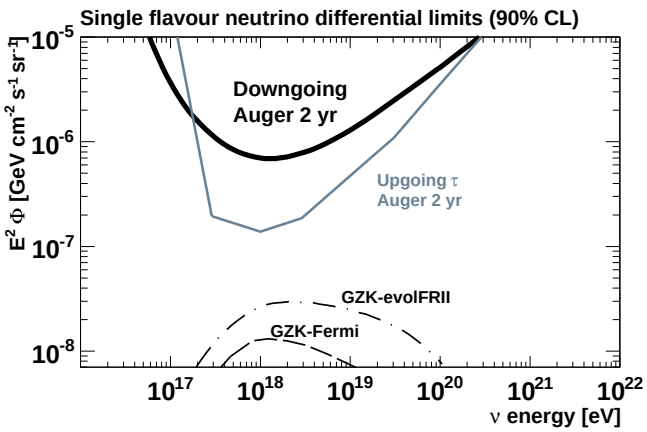

FIG. 14. Differential limits (90% CL) from the Pierre Auger Observatory for a diffuse flux of down-going ν in the period 1 Nov 2007 - 31 May 2010 and up-going ν_τ (1 Jan 2004 - 28 Feb 2009)[13]. For reference, two recent calculations of this flux are shown: "GZK-Fermi" [6] takes into account the Fermi-LAT constraint on the GZK cascade photons; the other "GZK-evolFRII" [7] adopts a strong source evolution model for FR-II galaxies, assumed to be the sources of UHECRs.

Reference	N expected	P. of obs. 0
GZK-Fermi	0.1	0.9
GZK-evolFRII	0.3	0.7
MPR-max	2.0	0.1
BBR	0.8	0.4
TD-Necklaces	0.8	0.4
Z-Burst	7.8	4×10^{-4}

TABLE IV. Expected number of events using the current exposure of down-going ν measured by the Pierre Auger Observatory for several models [6, 7, 52–54]. The third column gives the probabilities of observing 0 events given that we expect N.

after folding these fluxes with our reference exposure.

Current theoretical flux predictions for cosmogenic neutrinos [6, 7] seem to be out of reach of our present sensitivity. Concerning neutrinos produced in accelerating sources there are popular models [53, 54] which predict event rates which could be detected in the next few years. Regarding exotic models [52], TD-Necklaces will be within our sensitivity range in one or two years, while Z-Burst models are already strongly disfavoured. Note that all such 'top down' models are also tightly constrained by the limits of the Pierre Auger Observatory on the photon fraction in UHECR [20].

IX. ACKNOWLEDGMENTS

The successful installation, commissioning and operation of the Pierre Auger Observatory would not have been possible without the strong commitment and effort from the technical and administrative staff in Malargüe.

We are very grateful to the following agencies and organizations for financial support: Comisión Nacional de Energía Atómica, Fundación Antorchas, Gobierno De La Provincia de Mendoza, Municipalidad de Malargüe, NDM Holdings and Valle Las Leñas, in gratitude for their continuing cooperation over land access, Argentina; the Australian Research Council; Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq), Financiadora de Estudos e Projetos (FINEP), Fundação de Amparo à Pesquisa do Estado de Rio de Janeiro (FAPERJ), Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP), Ministério de Ciência e Tecnologia (MCT), Brazil; AVCR AV0Z10100502 and AV0Z10100522, GAAV KJB100100904, MSMT-CR LA08016, LC527, 1M06002, and MSM0021620859, Czech Republic; Centre de Calcul IN2P3/CNRS, Centre National de la Recherche Scientifique (CNRS), Conseil Régional Ile-de-France, Département Physique Nucléaire et Corpusculaire (PNC-IN2P3/CNRS), Département Sciences de l'Univers (SDU-INSU/CNRS), France; Bundesministerium für Bildung und Forschung (BMBF), Deutsche Forschungsgemeinschaft (DFG), Finanzministerium Baden-Württemberg, Helmholtz-Gemeinschaft Deutscher Forschungszentren (HGF), Ministerium für Wissenschaft und Forschung, Nordrhein-Westfalen, Ministerium für Wissenschaft, Forschung und Kunst, Baden-Württemberg, Germany; Istituto Nazionale di Fisica Nucleare (INFN), Ministero dell'Istruzione, dell'Università e della Ricerca (MIUR), Italy; Consejo Nacional de Ciencia y Tecnología (CONACYT), Mexico; Ministerie van Onderwijs, Cultuur en Wetenschap, Nederlandse Organisatie voor Wetenschappelijk Onderzoek (NWO), Stichting voor Fundamenteel Onderzoek der Materie (FOM), Netherlands; Ministry of Science and Higher Education, Grant Nos. 1 P03 D 014 30, N202 090 31/0623, and PAP/218/2006, Poland; Fundação para a Ciência e a Tecnologia, Portugal; Ministry for Higher Education, Science, and Technology, Slovenian Research Agency, Slovenia; Comunidad de Madrid, Consejería de Educación de la Comunidad de Castilla La Mancha, FEDER funds, Ministerio de Ciencia e Innovación and Consolider-Ingenio 2010 (CPAN), Xunta de Galicia, Spain; Science and Technology Facilities Council, United Kingdom; Department of Energy, Contract Nos. DE-AC02-07CH11359, DE-FR02-04ER41300, National Science Foundation, Grant No. 0450696, The Grainger Foundation USA; ALFA-EC / HELEN, European Union 6th Framework Program, Grant No. MEIF-CT-2005-025057, European Union 7th Framework Program, Grant No. PIEF-GA-2008-220240, and UNESCO.

[1] F. Halzen and D. Hooper, Rep. Prog. Phys. **65**, 1025 (2002); P. Bhattacharjee and G. Sigl, Phys. Rep. **327**, 109 (2000); J. K. Becker, Phys. Rep. **458**, 173 (2008).

[2] J. Abraham *et al.* [Pierre Auger Collaboration], Phys. Rev. Lett. **101**, 061101 (2008); R. U. Abbasi *et al.* [HiRes], Phys. Rev. Lett. **100**, 101101 (2008).

[3] V. Beresinsky and G. Zatsepin, Phys. Lett. B **28**, 423 (1969).

[4] S. Yoshida and M. Teshima, Prog. Theor. Phys. **89**, 833 (1993).

[5] R. Engel, D. Seckel, and T. Stanev, Phys. Rev. D **64**, 093010 (2001).

[6] M. Ahlers, L. A. Anchordoqui, M. C. Gonzalez-Garcia, F. Halzen and. S. Sarkar, Astropart. Phys. **34**, 106 (2010).

[7] K. Kotera, D. Allard and A. V. Olinto, JCAP **10**, 013 (2010).

[8] V. Berezinsky, A. Gazizov, M. Kachelriess and S. Ostapchenko, Phys. Lett. B **695**, 13 (2011).

[9] A. Achterberg *et al.* [IceCube Collaboration], Astropart. Phys. **26**, 155 (2006).

[10] J. A. Aguilar *et al.* [ANTARES Collaboration], Phys. Lett. B **696** 16, (2011).

[11] P. W. Gorham *et al.* [ANITA Collaboration], Phys. Rev. Lett. **103**, 051103 (2009); Astropart. Phys. **32**, 10 (2009).

[12] J. Abraham *et al.* [Pierre Auger Collaboration], Phys. Rev. Lett. **100**, 211101 (2008).

[13] J. Tiffenberg [Pierre Auger Collaboration], in *Proceedings of the 31st International Cosmic Ray Conference, Lodz* (2009), #0180, arXiv:0906.2347.

[14] D. Gora [Pierre Auger Collaboration], in *Proceedings of the 31st International Cosmic Ray Conference, Lodz* (2009), #0077, arXiv:0906.2319.

[15] X. Bertou, P. Billoir, O. Deligny, C. Lachaud, and A. Letessier-Selvon, Astropart. Phys **17**, 183 (2002).

[16] J. Abraham *et al.* [Pierre Auger Collaboration], Phys. Rev. D **79**, 102001 (2009).

[17] J. Alvarez-Muñiz [Pierre Auger Collaboration], in *Proceedings of the 30th International Cosmic Ray Conference, Mérida* Vol. 4, (2007), p. 607; I. Valiño (PhD thesis) Univ. de Santiago de Compostela, ISBN: 9788497509664, (2008).

[18] K. S. Capelle, J. W. Cronin, G. Parente and E. Zas, Astropart. Phys. **8**, 321 (1998); P. Billoir [Pierre Auger Collaboration], J. Phys. Conf. Ser. **203**, 012125 (2010).

[19] J. Abraham *et al.* [Pierre Auger Collaboration], Phys. Rev. Lett. **104**, 091101 (2010).

[20] J. Abraham *et al.* [Pierre Auger Collaboration], Astropart. Phys. **27**, 155 (2007); J. Abraham *et al.* [Pierre Auger Collaboration], Astropart. Phys. **29**, 243 (2008); J. Abraham *et al.* [Pierre Auger Collaboration], Astropart. Phys. **31**, 399 (2009).

[21] J. Abraham *et al.* [Pierre Auger Collaboration] Nucl. Instr. and Meth. A **523**, 50 (2004).

[22] I. Allekotte *et al.* [Pierre Auger Collaboration], Nucl. Instr. and Meth. A **586**, 409 (2008).

[23] J. Abraham *et al.* [Pierre Auger Collaboration], Nucl. Instr. and Meth. A **620**, 227 (2010).

[24] X. Bertou *et al.* [Pierre Auger Collaboration], Nucl. Instr. and Meth. A **568**, 839 (2006).

[25] J. Abraham *et al.* [Pierre Auger Collaboration], Nucl. Instr. and Meth. A **613**, 29 (2010).

[26] G. Corcella, I. G. Knowles, G. Marchesini, S. Moretti, K. Odagiri, P. Richardson, M. H. Seymour and B. R. Webber, HERWIG 6.5, JHEP 0101 (2001).

[27] R. Decker, S. Jadach, J. H. Kuhn and Z. Was, Comput. Phys. Commun. **76**, 361 (1993).

[28] S. Sciutto, AIRES. Available from http://www.fisica.unlp.edu.ar/auger/aires/.

[29] S. Argirò *et al.* [The Offline group - Pierre Auger Collaboration] Nucl. Instr. and Meth. A, **580**, 1485 (2007).

[30] T. G. Farr *et al.*, Rev. Geophys. **45**, 33 (2007).

[31] O. Blanch Bigas, O. Deligny, K. Payet, and V. Van Elewyck, Phys. Rev. D **77**, 103004 (2008).

[32] A. M. Hillas, in *Proceedings of the 17th International Cosmic Ray Conference, Paris* Vol. 8, (1981) p. 193.

[33] P. Billoir, Astropart. Phys. **30**, 270 (2008).

[34] S. Agostinelli *et al.*, Nucl. Instr. and Meth. A **506**, 250 (2003); J. Allison *et al.*, IEEE Trans. Nucl. Sci. **53**, 270 (2006). See also http://geant4.web. cern.ch/geant4/.

[35] R. Fisher, Ann. of Eugenics **7**, 179 (1936).

[36] B. Roe, PHYSTAT-2003-WEJT003, 215 (2003).

[37] A. Cooper-Sarkar and S. Sarkar, JHEP **0801**, 075 (2008).

[38] J. Pumplin, D. R. Stump, J. Huston, H. L. Lai, P. Nadolsky and W. K. Tung, JHEP **0207**, 012 (2002).

[39] S. Ostapchenko, Nucl.Phys. B - Proc. Supp. **151**, 143 (2006); S. Ostapchenko, Nucl.Phys. B - Proc. Supp. **151**, 147 (2006).

[40] T. Sjöstrand, S. Mrenna and P. Skands, Comput. Phys. Commun. **178**, 11, 852 (2008).

[41] M. Bähr *et al.*, Eur. Phys. J. C **58**, 639 (2008).

[42] A. D. Martin, W. J. Stirling, R. S. Thorne and G. Watt, Eur. Phys. J. C **63**, 189 (2009).

[43] D. Heck, J. Knapp, J. N. Capdevielle, G. Schatz and T. Thouw, Report FZKA **6019** (1998).

[44] N. Kalmykov and S. Ostapchenko, Phys. Atom. Nucl. **56**, 346 (1993).

[45] R. Engel, T. K. Gaisser, T. Stanev and P. Lipari, in *Proceedings of the 26th International Cosmic Ray Conference, Salt Lake City* Vol. 1 (1999) p. 415.

[46] A. Connolly, R. S. Thorne and D. Waters, Phys. Rev. D **83**, 113009 (2011).

[47] A. Cooper-Sarkar, P. Mertsch and S. Sarkar, arXiv:1106.3723, (2011).

[48] J. Conrad, O. Botner, A. Hallgren and C. Perez de los Heros, Phys. Rev. D **67** (2003) 12002.

[49] G. J. Feldman and R. D. Cousins, Phys. Rev. D **57**, 3873 (1998).

[50] M. Ackermann *et al.* [AMANDA], Astrophys. J. 675, 1014 (2008); R. Abbasi *et al.* [IceCube], Phys. Rev. D **83**,092003 (2011); I. Kravchenko *et al.* [RICE], Phys. Rev. D **73**, 082002 (2006); P. W. Gorham *et al.* [ANITA-II Collaboration], Phys. Rev. D **82** 022004 (2010), Erratum arXiv:1011.5004v1 [astro-ph]; R. Abbasi *et al.* [HiRes], Astrophys. J. 684, 790 (2008); K. Martens [HiRes], arXiv:0707.4417.

[51] L. A. Anchordoqui, J. L. Feng, H. Goldberg and A. D. Shapere, Phys. Rev. D **66**, 103002 (2002).

[52] O. E. Kalashev, V. A. Kuzmin, D. V. Semikoz and G. Sigl, Phys. Rev. D **66**, 063004 (2002).

[53] K. Mannheim, R. J. Protheroe and J. P. Rachen, Phys. Rev. D **63** 23003, (2001).

[54] J. K. Becker, P. L. Biermann and W. Rhode, Astropart. Phys. **23** 355, (2005).
[55] L. B. Bezrukov and E. V. Bugaev, Yad. Fiz. **33**, 1195 (1981); E. V. Bugaev and Yu V. Shlepin, Phys. Rev. D **67**, 34027 (2003).