Measurement of $\gamma + b + X$ and $\gamma + c + X$ production cross sections in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV

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First measurements of the differential cross sections \( \frac{d^3\sigma}{(dp_T^\gamma dy^\gamma dy^{\text{jet}})} \) for the inclusive production of a photon in association with a heavy quark (\( b, c \)) jet are presented, covering photon transverse momenta \( 30 < p_T^\gamma < 150 \text{ GeV} \), photon rapidities \( |y^\gamma| < 1.0 \), jet rapidities \( |y^{\text{jet}}| < 0.8 \), and jet transverse momenta \( p_T^{\text{jet}} > 15 \text{ GeV} \). The results are based on an integrated luminosity of 1 \( \text{fb}^{-1} \) in \( p\bar{p} \) collisions at \( \sqrt{s} = 1.96 \text{ TeV} \) recorded with the D0 detector at the Fermilab Tevatron Collider. The results are compared with next-to-leading order perturbative QCD predictions.

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Photons ($\gamma$) produced in association with heavy quarks $Q$ (i.e. $c$ or $b$) in the final state of hadron-hadron interactions provide valuable information about the parton distributions of the initial state hadrons [1, 2]. Such events are produced primarily through the QCD Compton-like scattering process $gQ \rightarrow \gamma Q$, which dominates up to photon transverse momenta ($p_T^\gamma$) of $\sim 90$ GeV for $\gamma + c + X$ and up to $\sim 120$ GeV for $\gamma + b + X$ production, but also through quark-antiquark annihilation $q\bar{q} \rightarrow \gamma g \rightarrow \gamma Q\bar{Q}$. Consequently, $\gamma + X$ production is sensitive to the $b$, $c$, and gluon ($g$) densities within the colliding hadrons, and can provide constraints on parton distribution functions (PDFs) that have substantial uncertainties [3, 4]. The heavy quark and gluon content is an important aspect of QCD dynamics and of the fundamental structure of the proton. In particular, many searches for new physics, e.g. for certain Higgs boson production modes [5–8], will benefit from a more precise knowledge of the heavy quark and gluon content of the proton.

This Letter presents the first measurements of the inclusive differential cross sections $\mathrm{d}^3\sigma/(\mathrm{d}p_T^\gamma \mathrm{d}y \mathrm{d}y^{\text{jet}})$ for $\gamma + b + X$ and $\gamma + c + X$ production in $pp$ collisions, where $y$ and $y^{\text{jet}}$ are the photon and jet rapidities [9]. The results are based on an integrated luminosity of $1.02 \pm 0.06$ fb$^{-1}$ [10] collected with the D0 detector [11] at the Fermilab Tevatron Collider at $\sqrt{s} = 1.96$ TeV. The highest $p_T$ (leading) photon and jet are required to have $|y| < 1.0$ and $|y^{\text{jet}}| < 0.8$, and transverse momentum $30 < p_T^\gamma < 150$ GeV and $p_T^{\text{jet}} > 15$ GeV. This selection allows one to probe PDFs in the range of parton-momentum fractions $0.01 \lesssim x \lesssim 0.3$, and hard scatter scales of $9 \times 10^2 \lesssim Q^2 \equiv (p_T^\gamma)^2 \lesssim 2 \times 10^4$ GeV$^2$. Differential cross sections are presented for two regions of kinematics, defined by $y^\gamma y^{\text{jet}} > 0$ and $y^\gamma y^{\text{jet}} < 0$. These two regions provide greater sensitivity to the parton $x$ because they probe different sets of $x_1$ and $x_2$ intervals, as discussed in Ref. [12].

The triggers for this analysis identify clusters of large electromagnetic (EM) energy, and are based on $p_T^\gamma$ and on the spatial distribution of energy in the photon shower. The trigger efficiency is $\approx 96\%$ for photon candidates with $p_T^\gamma = 30$ GeV and nearly $100\%$ for $p_T^\gamma > 40$ GeV.

To reconstruct photon candidates, towers [11] with large depositions of energy are used as seeds to create clusters of energy in the EM calorimeter in a cone of radius $R = 0.4$, where $R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$ [13]. Once an EM energy cluster is formed, the final energy $E_{\text{EM}}$ is defined by a smaller cone of $R = 0.2$. Photon candidates are required to be isolated within the calorimeter, and must also have $> 96\%$ of their energy in its EM section. We require the sum of the total energy inside a cone of $R = 0.4$, after the subtraction of $E_{\text{EM}}$, to be $< 7\%$ of $E_{\text{EM}}$. We also require the width of the energy-weighted shower in the most finely segmented part of the EM calorimeter to be consistent with that expected for an electromagnetic shower, and the probability for any track spatially matched to the photon EM cluster to be $< 0.1\%$. Background from dijet events containing $\pi^0$ and $\eta$ mesons that can mimic photon signatures is also rejected using an artificial neural network ($\gamma$-ANN), described in Ref. [12], and the requirement that the $\gamma$-ANN output be $> 0.7$. We calculate photon detection efficiencies using a Monte Carlo (MC) simulation. Signal events are generated using PYTHIA [14] and processed through a GEANT-based [15] simulation of the detector geometry and response, and reconstructed using the same software as for the data. The MC efficiencies are calibrated to those in data using small correction factors in $Z \rightarrow e^+e^-$ samples. The total efficiency of the above photon selection criteria is $63\%$–$80\%$, depending on $p_T^\gamma$. The systematic uncertainties on these values are $5\%$, and are mainly due to uncertainties in the isolation, the track-match veto, and the $\gamma$-ANN requirements.

At least one jet must be present in each event. Jets are reconstructed using the D0 Run II algorithm [16] with a radius of 0.5. The efficiency for a jet to be reconstructed and to satisfy the jet identification criteria is $93\%$, $96.5\%$, and $94.5\%$ for light ($u$, $d$, $s$ quark or $g$), $c$, and $b$ jets at $p_T^j = 30$ GeV and increases to $\approx 98\%$ at $p_T^j = 150$ GeV, independent of the jet flavor. The impact from uncertainties on jet energy scale, jet energy resolution, and difference in energy response between light and $b(c)$ jets is found to be between $8\%$($6\%$) and $2\%$($2\%$) for $p_T^{\text{jet}}$ between 15 GeV and 150 GeV. The leading jet is also required to have at least two associated tracks with $p_T > 0.5$ GeV and the track leading in $p_T$ must have $p_T > 1.0$ GeV, and each track must have at least one hit in the silicon microstrip tracker. These criteria ensure that the jet has sufficient information to be classified as a heavy-flavor candidate. Light jets are suppressed using a dedicated artificial neural network ($b$-ANN) [17] that exploits the longer lifetimes of heavy-flavor hadrons relative to their lighter counterparts. The leading jet is required to have a $b$-ANN output $> 0.85$. Depending on $p_T^\gamma$, this selection is $55\%$–$62\%$ efficient for $\gamma + b$ jet, and $11\%$–$12\%$ efficient for $\gamma + c$ jet events, with $3\%$–$5\%$ relative uncertainties on these values. Only $0.2\%$–$1\%$ of light jets are misidentified as heavy-flavor jets.

A primary collision vertex with $\geq 3$ tracks is required within 35 cm of the center of the detector along the beam axis. The missing transverse momentum in the event is required to be $< 0.7p_T^\gamma$ so as to suppress background from cosmic-ray muons and $W \rightarrow \ell\nu$ decays. Such a requirement is highly efficient for signal, achieving an efficiency $\geq 96\%$ even for events with semi-leptonic heavy-flavor quark decays.

About 13,000 events remain in the data sample after applying all selection criteria. Background for photons stems mainly from dijet events in which one jet is misidentified as a photon. To estimate the photon purity, the $\gamma$-ANN distribution in data is fitted to a linear combination of templates for photons and jets ob-
tained from simulated $\gamma +$ jet and dijet samples, respectively. An independent fit is performed in each $p_T^\gamma$ bin, yielding photon purities between 51% and 93% for $30 < p_T^\gamma < 150$ GeV. The fractional contributions of $b$ and $c$ jets are determined by fitting templates of $P_{HF-jet} = -\ln \prod_i P_i^{\text{track}}$ to the data, where $P_i^{\text{track}}$ is the probability that a track originates from the primary vertex, based on the significance of the track’s distance of closest approach to the primary vertex. All tracks within the jet cone are used in the fit, except the one with lowest value of $P^{\text{track}}$. Jets from $b$ quarks usually have large values of $P_{HF-jet}$, whereas light jets mostly have small values, as their tracks originate from the primary vertex. Templates are used for the shape information of the $P_{HF-jet}$ distributions. For $b$ and $c$ jets these are extracted from MC events whereas the light jet template is taken from a data sample enriched in light jets, which is corrected for contributions from $b$ and $c$ quarks. The result of a maximum likelihood fit, normalized to the number of events in data, is shown in Fig. 1 for $50 < p_T^\gamma < 70$ GeV. The estimated fractions of $b$ and $c$ jets in all $p_T^\gamma$ bins vary between 25–34% and 40–48%, respectively. The corresponding uncertainties range between 7–24%, dominated at higher $p_T^\gamma$ by the limited data statistics.

The differential cross sections are extracted in five bins of $p_T^\gamma$ and in the two regions of $y^\gamma y_{\text{jet}}$, and are all listed in Tab. I. The measured cross sections are corrected for the effect of finite calorimeter energy resolution affecting $p_T^\gamma$ using the unfolding procedure described in Ref. [18]. Such corrections are 1–3%. The measured differential cross sections are shown in Fig. 2 for $\gamma + b + X$ and $\gamma + c + X$ production as a function of $p_T^\gamma$ for the jet and photon rapidity intervals in question. The cross sections fall by more than three orders of magnitude in the range $30 < p_T^\gamma < 150$ GeV. The statistical uncertainty on the results ranges from 2% in the first $p_T^\gamma$ bin to ≈9% in the last bin, while the total systematic uncertainty varies between 15% and 28%. The main uncertainty at low $p_T^\gamma$ is due to the photon purity (10.5%) and the heavy-flavor fraction fit (9%). At higher $p_T^\gamma$, the uncertainty is dominated by the heavy-flavor fraction. Other significant uncertainties result from the jet-selection efficiency (between 8% and 2%), the photon selection efficiency (5%), and the luminosity (6.1%) [10]. Systematic uncertainties have a 60–68% correlation between adjacent $p_T^\gamma$ bins for $30 < p_T^\gamma < 50$ GeV and 20–30% for $p_T^\gamma > 70$ GeV.

Next-to-leading order (NLO) perturbative QCD (pQCD) predictions, with the renormalization scale $\mu_R$, factorization scale $\mu_F$, and fragmentation scale $\mu_f$, all set to $p_T^\gamma$, are also given in Tab. I and compared to data in Fig. 2. These predictions [19] are preliminary, and are based on techniques used to calculate the cross section analytically [20]. The ratios of the measured to the predicted cross sections are shown in Fig. 3.

The uncertainty from the choice of the scale is estimated through a simultaneous variation of all three scales by a factor of two, i.e., to $\mu_{R,F,f} = 0.5 p_T^\gamma$ and $2p_T^\gamma$. The predictions utilize cteq6.6M PDFs [4], and are corrected for effects of parton-to-hadron fragmentation. This correction for $b (c)$ jets varies from 7.5% (3%) at $30 < p_T^\gamma < 40$ GeV to 1% at 90 < $p_T^\gamma < 150$ GeV.

The pQCD prediction agrees with the measured cross sections for $\gamma + b + X$ production over the entire $p_T^\gamma$ range,
Table I: The $\gamma + b + X$ and $\gamma + c + X$ cross sections in bins of $p_T^\gamma$ in the two regions $y^\gamma y^{\text{jet}} > 0$ and $y^\gamma y^{\text{jet}} < 0$ together with statistical, $\delta \sigma_{\text{stat}}$, and systematic, $\delta \sigma_{\text{syst}}$, uncertainties. The theory cross sections $\sigma_{\text{theory}}$ are taken from Ref. [19].

<table>
<thead>
<tr>
<th>$p_T^\gamma$ bin (GeV)</th>
<th>$y^\gamma y^{\text{jet}} &gt; 0$</th>
<th>$y^\gamma y^{\text{jet}} &lt; 0$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$p_T^\gamma$ (GeV)</td>
<td>Cross section (pb/GeV)</td>
</tr>
<tr>
<td>$\gamma + b + X$</td>
<td>30–40</td>
<td>34.1  2.73×10^{-1}</td>
</tr>
<tr>
<td></td>
<td>40–50</td>
<td>44.3  1.09×10^{-1}</td>
</tr>
<tr>
<td></td>
<td>50–70</td>
<td>57.6  2.72×10^{-2}</td>
</tr>
<tr>
<td></td>
<td>70–90</td>
<td>78.7  6.21×10^{-3}</td>
</tr>
<tr>
<td></td>
<td>90–150</td>
<td>108.3  1.23×10^{-3}</td>
</tr>
</tbody>
</table>

We observe disagreement between theory and data for $\gamma + b + X$ production. In the case of the BHPS model [2] it grows with $p_T^\gamma$. The observed difference may also be caused by an underestimated contribution from the $q \rightarrow QQ$ splitting in the annihilation process that dominates for $p_T^\gamma > 90$ GeV [21].

In conclusion, we have performed the first measurement of the differential cross section of inclusive photon production in association with heavy flavor ($b$ and $c$) jets at a $pp$ collider. The results cover the range $30 < p_T^\gamma < 150$ GeV, $|y^\gamma| < 1.0$, and $|y^{\text{jet}}| < 0.8$. The measured cross sections provide information about $b$, $c$, and gluon PDFs for $0.01 \lesssim x \lesssim 0.3$. NLO pQCD predictions using CTEQ6.6M PDFs [19] for $\gamma + b + X$ production agree with the measurements over the entire $p_T^\gamma$ range. We observe disagreement between theory and data for $\gamma + c + X$ production for $p_T^\gamma > 70$ GeV.

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9. Rapidity is defined as $y = -\ln[(E+p_Z)/(E-p_Z)]$, where $E$ is the energy and $p_Z$ is the momentum component along the proton beam direction.
13. Pseudorapidity $\eta$ is defined as $\eta = -\ln[\tan(\theta/2)]$, where $\theta$ is the polar angle with respect to the proton beam direction, with origin at the center of the detector. $\phi$ is defined as the azimuthal angle in the plane transverse to the proton beam direction.