

Measurement of the top-quark mass using missing E_T +jets events with secondary vertex b -tagging at CDF II

The CDF Collaboration

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Abstract

We present a measurement of the top-quark mass in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV which uses events with an inclusive signature of missing transverse energy and jets. The event selection is sensitive to $t\bar{t} \rightarrow W^+bW^-\bar{b} \rightarrow l\nu bqq'\bar{b}$ independent of the lepton flavor, and results in a large acceptance for $W \rightarrow \tau\nu$ decays. All-hadronic $t\bar{t}$ decays and events with identified electrons or muons are vetoed to provide a statistically independent sample with respect to all previous measurements. The top-quark mass is inferred from the distribution of the estimated total transverse energy in the detector. Using 311 pb^{-1} of integrated luminosity recorded by the Collider Detector at Fermilab, we measure a top-quark mass $m_t = 172.3_{-9.6}^{+10.8}(\text{stat.}) \pm 10.8(\text{syst.}) \text{ GeV}/c^2$.

The top-quark mass, m_t , is a key parameter in the standard model (SM) of particle physics. Being roughly 40 times larger than the mass of its isospin partner, the b quark, m_t gives large contributions to electroweak radiative corrections which, when connected to precision electroweak measurements, can be used to derive constraints on the masses of yet unobserved Higgs boson [1], and of particles belonging to some SM extensions [2]. At the Tevatron $p\bar{p}$ collider top quarks are produced mainly in pairs through quark-antiquark annihilation and gluon-gluon fusion processes. Because the Cabibbo-Kobayashi-Maskawa matrix element V_{tb} [3] is close to unity and m_t is large, the SM top quark decays to a W boson and a b quark almost 100% of the time. The final state of top-quark pair production thus includes two W bosons and two b -quark jets. When only one W decays leptonically, the $t\bar{t}$ event typically contains a charged lepton, missing transverse energy (\cancel{E}_T) from the undetected neutrino [4], and four high transverse energy jets, two of which originate from b quarks.

Recently the CDF collaboration has reported precision m_t measurements using events containing identified high- p_T leptons (e, μ) [5] and all-hadronic $t\bar{t}$ decays [6]. In this paper we describe a top-quark mass measurement which uses events collected by a multijet trigger, and selected by requiring an inclusive high- p_T neutrino signature, consisting of large \cancel{E}_T . Events containing identified high- p_T electrons or muons ($E_T^e \geq 20$ GeV, $P_T^\mu \geq 20$ GeV/ c), as defined in [7], are removed in order to increase the relative contribution of $W \rightarrow \tau\nu$ decays and provide a statistically independent sample with respect to other lepton-based measurements [5]. All-hadronic $t\bar{t}$ decays are discarded by the \cancel{E}_T requirement so that orthogonality with respect to [6] is ensured. Unlike previous analyses based on the identification of $W \rightarrow e\nu(\mu\nu)$ and $W \rightarrow qq'$ decays, our event selection does not permit a full kinematical reconstruction of the $t\bar{t}$ final state. For this reason, the top-quark mass is derived from the distribution of the estimated total energy release in the detector, H_T , defined as the scalar sum of all jet transverse

energies and the \cancel{E}_T .

Results reported in this paper are obtained using 311 pb^{-1} of integrated luminosity from $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$, recorded by the Collider Detector at Fermilab (CDF II). The CDF II detector has been described in detail elsewhere [8]. It consists of a magnetic spectrometer surrounded by a calorimeter and muon system. The momenta of charged particles are measured up to a pseudorapidity of $|\eta| = 1.0$ in a cylindrical drift chamber, which is inside a 1.4 T superconducting solenoidal magnet. Silicon microstrip vertex detectors, located immediately outside the beampipe, provide precise track reconstruction useful for vertexing and extend the coverage of the tracking system up to $|\eta| = 2.0$. Electromagnetic and hadronic sampling calorimeters, arranged in a projective-tower geometry, surround the tracking systems and measure the energy and direction of electrons, photons, and jets in the range $|\eta| < 3.6$. In addition, the good hermeticity provided by the calorimeter system allows the detection of high- p_T neutrinos by the measurement of the \cancel{E}_T . Muon systems outside the calorimeters allow the reconstruction of track segments for penetrating particles. The beam luminosity is determined using gas Cherenkov counters, which measure the average number of inelastic $p\bar{p}$ collisions per bunch crossing.

The data sample used in this analysis is collected by a multijet trigger which requires four or more $E_T \geq 15 \text{ GeV}$ clusters of contiguous calorimeter towers, and a scalar sum of transverse energy clustered in the calorimeter of $\sum E_T \geq 125 \text{ GeV}$. The initial data sample consists of 4.2 million events and is further reduced offline by the application of kinematical and topological requirements aimed at optimizing the $t\bar{t}$ signal significance [9]. Briefly, we require at least four jets having $E_T \geq 15 \text{ GeV}$ and $|\eta| \leq 2.0$; \cancel{E}_T significance, $\cancel{E}_T^{\text{sig}}$, greater than $4.0 \text{ GeV}^{1/2}$, where $\cancel{E}_T^{\text{sig}}$ is defined as $\cancel{E}_T/\sqrt{\sum E_T}$; and a minimum angular separation between the \cancel{E}_T and the closest jet, $\min \Delta\phi \geq 0.4 \text{ rad}$. Jets are identified as groups of calorimeter tower energy deposits which fall within a

cone of radius $\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2} \leq 0.4$. Jet energies are corrected for calorimeter non-linearity, losses in the gaps between towers, multiple interactions, and particle response calibrations [10]. This selection reduces the data sample to 597 events, with a signal to background ratio $S/B \sim 1/5$. In order to further increase the expected S/B ratio and reject background events with only light quark or gluon jets, b -quark jets (“tags”) are identified by the reconstruction of secondary decay vertices using the SECVTX algorithm, as in [7]. After these selections and the requirement of at least one b -tagged jet, we observe 106 events with $S/B \sim 1$; about 44% of the signal acceptance is accounted for by $t\bar{t} \rightarrow W^+bW^-\bar{b} \rightarrow \tau\nu bqq'\bar{b}$ decays, while the remaining $t\bar{t}$ content is dominated by $e(\mu)$ +jets events, in which the lepton fails the standard high- p_T identification cuts.

Background events with b tags arise from QCD heavy flavor production, electroweak production of W bosons associated with heavy flavor jets, and from false identification by the SECVTX algorithm. The overall number of background b tags in the final data sample, and their corresponding kinematical distributions, are estimated using a per-jet parametrization of the b -tagging probability derived from the multijet sample. For the parametrization, we use events with exactly three jets, having $E_T \geq 15$ GeV and $|\eta| \leq 1.0$, where the $t\bar{t}$ content is negligible. The parametrization exploits the b -tag rate dependencies on the jet E_T , charged track multiplicity inside the jet cone, and the projection of the \cancel{E}_T along the jet direction in the transverse plane, which is defined by $\cancel{E}_T^{\text{prj}} = \cancel{E}_T \cos \Delta\phi(\cancel{E}_T, \text{jet})$. The extrapolation of the 3-jet b -tagging probability to higher jet multiplicity events, and the capability of the parametrization to track sample composition changes introduced by the kinematical selection, are checked using ≥ 4 -jet data samples depleted of signal content, as in [9]: (a) data before the optimized kinematical selection on $\cancel{E}_T^{\text{sig}}$ and $\min \Delta\phi(\cancel{E}_T, \text{jets})$; (b) $\cancel{E}_T^{\text{sig}} \leq 3.0$ GeV $^{1/2}$, $\min \Delta\phi(\cancel{E}_T, \text{jets}) \geq 0.3$ rad, and (c) $\cancel{E}_T^{\text{sig}} \geq 3.0$ GeV $^{1/2}$, $\min \Delta\phi(\cancel{E}_T, \text{jets}) \leq 0.3$ rad. As

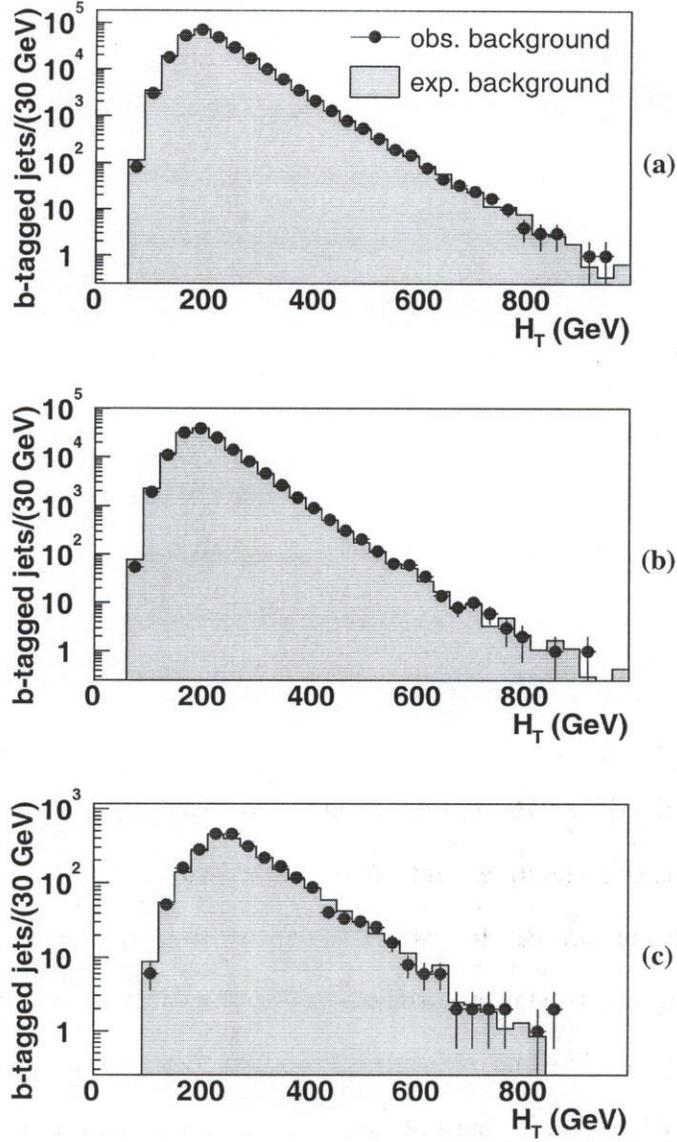


Figure 1: Observed and expected H_T background distributions in data control samples depleted of signal contamination, see text for details.

a result, the b -tag rate parametrization is found to predict the number of background b tags, and the shape of their corresponding kinematical distributions, to within 10% in the $4 \leq N_{\text{jet}} \leq 6$ region, where 96.4% of the $t\bar{t}$ signal is expected. Figure 1 shows the comparison between expected and observed background H_T distributions in the data

control samples (a), (b), and (c). The expected H_T distributions are derived from the b -tag rate parametrization applied to each jet belonging to a given data sample, before b -jet identification requirements. The observed H_T distributions receive one entry per b -tagged jet for a proper normalization with the expectation. The normalization and shape of the observed and expected distributions are in good agreement for all control samples.

The final data sample, after the optimized kinematical selection and the additional requirement of at least one b -tagged jet, contains a total of 127 b -tagged jets. The number of b -tagged jets yielded by background processes in that sample is expected to be $n_b^{\text{exp}} = 57.4 \pm 8.1$. The excess in the number of b tags is ascribed to top-quark pair production. We derive a measurement of the top-quark mass from the observed H_T distribution. The H_T distribution from the selected data is fit to the sum of signal (P_{sig}) and background (P_{bkg}) H_T distribution parametrizations using an unbinned likelihood technique. Probability density functions are determined for signal, as a function of m_t , and background events by fitting a functional form from the corresponding H_T distributions (templates). For consistency with our per-jet background prediction method, the H_T distributions from data and Monte Carlo signal events receive one entry per b -tagged jet.

We calibrate our method using events with inclusive $t\bar{t}$ decays generated with different input values of m_t ranging from 150 to 200 GeV/ c^2 , in steps of 2.5 GeV/ c^2 . These events are simulated using the HERWIG[11] generator in conjunction with the CTEQ5L [12] parton distribution functions (PDFs), QQ [13] for the modeling of b and c hadron decays, and a full simulation of the CDF II detector [14, 15]. They are then subjected to the same selection as the data. The H_T distributions, derived at discrete values of the top-quark mass, are parametrized by a continuous functional form as a function of m_t in order to smooth the distributions and interpolate between the templates. For

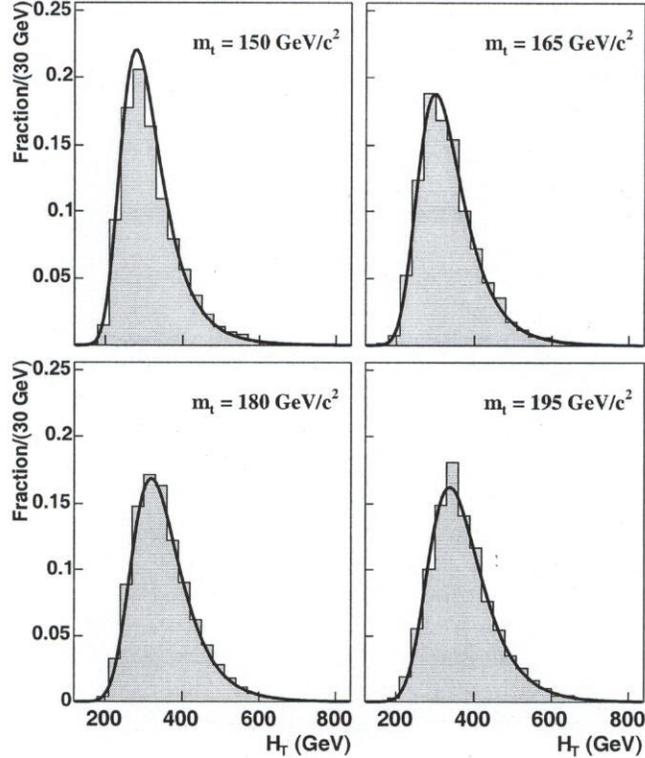


Figure 2: Four H_T signal templates with m_t ranging from 150 to 195 GeV/c^2 . Overlaid are the fitted parametrizations at each generated top-quark mass.

any given m_t the probability to observe a particular H_T value is specified by a normalized Pearson type IV function [16], in which the four parameters are assumed to be linearly dependent on m_t . The best parametrization is determined by a simultaneous binned likelihood fit to all signal templates. In Fig. 2, four signal templates at varying generated top-quark mass are shown overlaid with their corresponding parametrization.

For background, the H_T distribution is derived from the b -tag rate parametrization applied to jets belonging to the kinematically selected data sample, before b -jet identification requirements. It has no dependence on the top-quark mass, except from a procedure adopted to subtract the expected signal content ($\sim 15\%$ for $m_t = 172.5 \text{ GeV}/c^2$). The arbitrary m_t choice in the subtraction procedure is accounted for in the

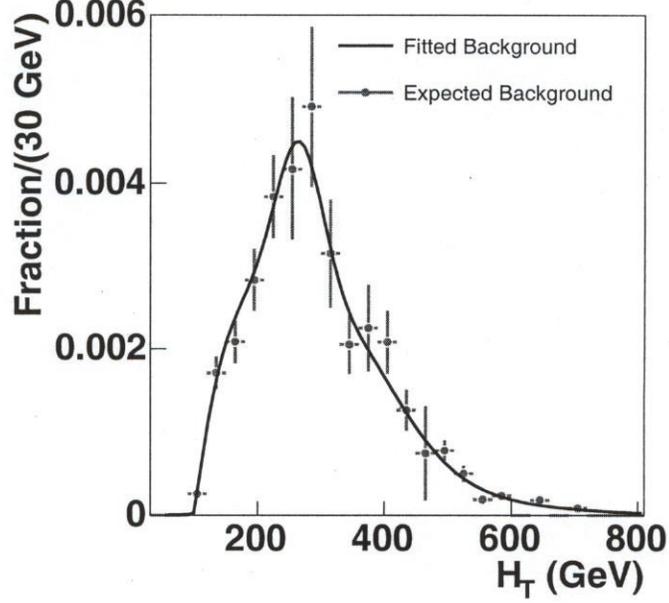


Figure 3: The background H_T template, after the subtraction of the $t\bar{t}$ content (using $m_t=172.5 \text{ GeV}/c^2$), is shown overlaid with the fitted parametrization.

background shape systematic uncertainty. A single probability density function, defined as the sum of a gamma function and two gaussians, is used to fit the background H_T template, as shown in Fig. 3.

The likelihood function used to extract the top-quark mass includes as free parameters the number of expected signal and background b tags (n_s and n_b), and m_t . It is specified by three factors:

$$\mathcal{L}(m_t) = \mathcal{L}_{\text{shape}}(m_t) \times \mathcal{L}_{n_s+n_b} \times \mathcal{L}_{\text{bkg}}, \quad (1)$$

where

$$\mathcal{L}_{\text{shape}}(m_t) = \prod_{i=1}^N \frac{n_s \cdot P_{\text{sig}}(H_T^i | m_t) + n_b \cdot P_{\text{bkg}}(H_T^i)}{n_s + n_b}, \quad (2)$$

$$\mathcal{L}_{n_s+n_b} = \frac{e^{-(n_s+n_b)} \cdot (n_s + n_b)^N}{N!}, \quad (3)$$

$$\mathcal{L}_{\text{bkg}} = e^{-\frac{1}{2}(n_b - n_b^{\text{exp}})^2 / \sigma_{n_b}^2}, \quad (4)$$

and N is the number of observed b tags in the final data sample. In $\mathcal{L}_{\text{shape}}(m_t)$ the product is over the number of observed b tags, and $P_{\text{sig}}(H_T^i|m_t)$ and $P_{\text{bkg}}(H_T^i)$ are the probability density functions for signal and background, respectively. The second factor of Eq. (1) represents a Poisson constraint on the total number of b tags observed in the data. Finally, in Eq. (4) the background normalization is constrained to within its expected value n_b^{exp} . The likelihood is maximized with respect to n_s , n_b and m_t . The statistical uncertainty from the fit procedure is taken from the m_t values where the log-likelihood changes by 0.5 units from its maximum.

We use simulated data ensembles (pseudo-experiments) to check our fitting procedure for possible systematic biases. For each generated top-quark mass, from 150 GeV/ c^2 to 200 GeV/ c^2 , we construct pseudo-experiments, with the same statistical properties as our observed data sample, by randomly sampling from the signal and background templates. Then we perform likelihood fits to each pseudo-experiment and characterize the accuracy of the technique in determining the correct m_t value. In each pseudo-experiment, the number of background b tags is Poisson fluctuated around its expectation, n_b^{exp} , while the number of signal b tags is Poisson fluctuated around the number observed in the data, minus the central value for the background expectation. In this procedure, b tags from single and double b -tagged events are fluctuated separately. For each pseudo-experiment, the likelihood fit provides the measured m_t along with the positive and negative statistical uncertainties from which pull distributions can be derived. The mean of the pull distribution, averaged as a function of the input m_t , are consistent with zero (-0.01 ± 0.02), while the widths are slightly larger than unity, due to the inclusion of duplicated H_T values in the pseudo-experiment dis-

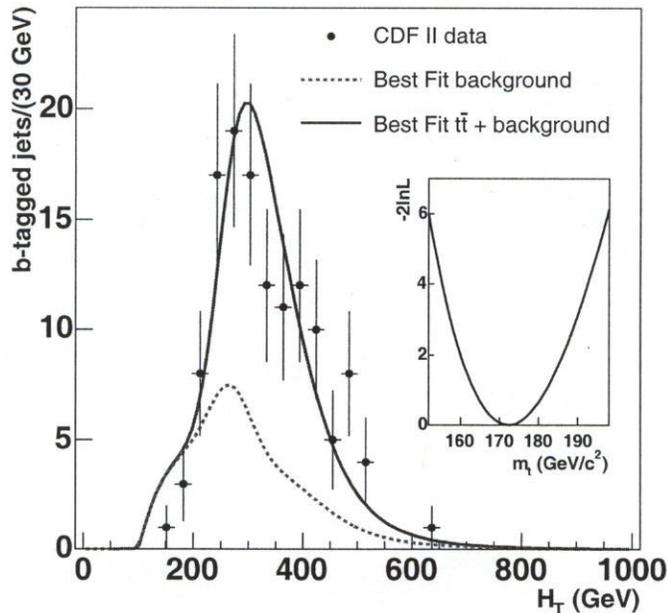


Figure 4: H_T distribution from the selected data sample, overlaid with the expected distribution from the unbinned likelihood fit. The inset shows the $-2\ln\mathcal{L}$ from the final fit as a function of m_t .

tributions in the case of double-tagged events. For the current analysis, the quoted measurement with uncertainties is designed to have a pull width equal to one by scaling the statistical errors taken from $\Delta\ln\mathcal{L} = -1/2$. The scale factor is the pull width averaged over m_t ranging between 150 and 200 GeV/c^2 , giving 1.08 ± 0.02 .

Applying our method to the observed H_T data distribution, we find $n_s = 76.2 \pm 11.4$, $n_b = 54.6 \pm 5.1$, and $m_t = 172.3^{+10.8}_{-9.6}(\text{stat.}) \text{ GeV}/c^2$. The statistical uncertainties on m_t are consistent with expectation from pseudo-experiments performed with an input top-quark mass of $172.5 \text{ GeV}/c^2$. The result from the fit to the data is shown in Fig. 4. The inset shows the function $-2\ln\mathcal{L}$ from the final fit as a function of m_t .

Systematic uncertainties arise from uncertainties in our understanding of the detector response and in the assumptions employed to infer the top-quark mass from the observed data. For each source of systematic uncertainty, the relevant input quan-

Table 1: Relevant sources of systematic uncertainty.

Source	Δm_t (GeV/ c^2)
Jet energy scale	9.6
Generator	3.8
Background shape	2.1
PDFs	1.5
ISR	0.9
FSR	0.9
Background fraction	0.8
b -jet energy scale	0.7
Trigger efficiency	0.7
Limited Monte Carlo statistics	0.6
b tagging	0.5
Total	10.8

tities are varied by $\pm 1\sigma$, and new signal or background H_T templates are produced by performing the event selection and reconstruction on the modified samples. Then these new templates are used to run pseudo-experiments. The mean shift in the fitted top-quark mass with respect to the default result is taken as the systematic uncertainty associated with the given assumption or effect. Table 1 reports all the relevant sources of systematics associated with our measurement. The dominant source of uncertainty (9.6 GeV/ c^2) given the choice of H_T as discriminant variable is associated to jet energy scale (JES) uncertainty. For each jet considered in the H_T calculation the relative jet energy scale uncertainty, which is mainly driven by uncertainties on particle response calibrations and the out-of-cone jet energy modeling, varies from 3% to 8% depending on η and p_T of the jet. We determine the impact of the JES uncertainty on our measurement using pseudo-experiments in which the nominal jet energies are varied by ± 1 standard deviations. Additionally, the dependence on the Monte Carlo generator is estimated as the difference in the extracted top-quark mass in PYTHIA [17] and HERWIG events, and amounts to 3.8 GeV/ c^2 . Other sources of uncertainty are related to the background shape and normalization and are evaluated to be 2.1 and

0.8 GeV/ c^2 , respectively. We estimate the uncertainty from the parton distribution functions (PDFs) using signal samples in which the events are weighted according to their probability to occur using different sets of PDF eigenvectors. The systematic uncertainty is computed by considering differences between the CTEQ5L and MRST72 [18] PDFs parametrizations, different Λ_{QCD} values, and the sum in quadrature of half the difference between the $\pm 1\sigma$ shift of the 20 CTEQ6M uncertainties, for a total of 1.5 GeV/ c^2 . Variation of initial (ISR) and final state (FSR) gluon radiation settings, as in [5], are found to contribute 0.9 GeV/ c^2 of systematic uncertainty each. Systematic uncertainties due to the b-jet energy scale, trigger simulation effects, statistically limited Monte Carlo samples, and b -tagging efficiency modeling, are small and give a combined error contribution of 1.2 GeV/ c^2 . The total systematic uncertainty is estimated to be 10.8 GeV/ c^2 assuming all sources are uncorrelated.

In conclusion, we report the first top-quark mass measurement using inclusively selected \cancel{E}_T +jets $t\bar{t}$ events with a large acceptance to $W \rightarrow \tau\nu$ decays. The result, $m_t = 172.3_{-9.6}^{+10.8}(\text{stat.}) \pm 10.8(\text{syst.})$ GeV/ c^2 , is complementary and statistically independent with respect to precision CDF measurements [5, 6], and consistent with previous direct and indirect top-quark mass determinations.

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