

First observation of $K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^-$

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This letter is the first report of the $K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^-$ decay. Based on 19208 ± 144 events, we determine the branching fraction, $B(K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^-; M_{e^+e^-} > 5 \text{ MeV}/c^2, E_{e^+e^-}^* > 30 \text{ MeV}) = (1.285 \pm 0.041) \times 10^{-5}$, and $\Gamma(K_{e3ee}; M_{e^+e^-} > 5 \text{ MeV}/c^2) / \Gamma(K_{e3}) = [4.57 \pm 0.04(\text{stat}) \pm 0.14(\text{syst})] \times 10^{-5}$. This ratio agrees with a theoretical prediction based on chiral perturbation theory (ChPT) calculated to $\mathcal{O}(p^4)$. The measured kinematical distributions agree with those predicted by just ChPT $\mathcal{O}(p^4)$, but show significant disagreement with ones predicted by leading order ChPT.

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The semileptonic mode, $K_L \rightarrow \pi^\pm e^\mp \nu$ (K_{e3}) and its radiative mode, $K_{e3\gamma}$, has been extensively studied [1–3]. In this letter, we introduce the semileptonic kaon decay mode $K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^-$ (K_{e3ee}). We present the first measurement of its branching fraction, and the ratio of its decay width to that of the K_{e3} decay. As shown in Fig. 1, the $K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^-$ decay is dominated by K_{e3} with a virtual photon, γ^* , that converts internally into a real e^+e^- pair. The amplitude of $K_{e3\gamma}$ consists of two

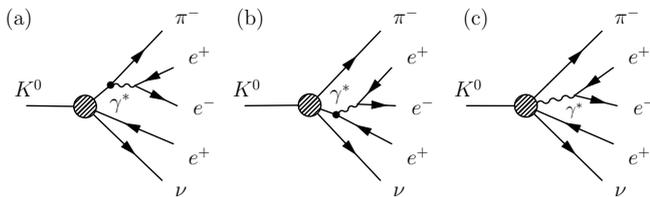


FIG. 1: Processes contributing to the $K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^-$ decay: the virtual photon comes (a) from the charged pion, (b) from the K_{e3} electron, and (c) from the kaon decay vertex. The process (c) includes the structure dependent (SD) amplitudes. The exchange diagrams have been omitted for clarity.

parts. One part is inner bremsstrahlung (IB) from the

pion or the electron, which is illustrated by Fig. 1-(a) and (b). The other part is the photon radiated from an intermediate hadronic state of the K - π current, namely the structure dependent (SD) amplitude (ie. direct emission) [1, 2, 4], as illustrated by Fig. 1-(c).

The model describing the K - π current is important for both studying K_{e3} decays themselves and understanding low energy QCD. A powerful way to express the K - π current is via Chiral Perturbation Theory (ChPT) [5]. ChPT has been developed based on the chiral symmetry of QCD, and it can be applied to all K_{e3} modes, including K_{e3ee} . In this letter, we compare our measurements against ChPT calculated to next-to-leading order, expanded to the fourth power of the momentum of chiral field p [NLO(p^4)].

We search for K_{e3ee} decays in data collected by the KTeV E799-II fixed target experiment, which ran at the Fermi National Accelerator Laboratory. Two parallel K_L beams were produced by 800 GeV/c protons from the Tevatron striking a BeO target. Following the target were beam line elements to sweep away charged particles, to absorb photons, and to allow for short-lived hadrons to decay away. The region from 95 m to 159

m downstream of the target was in vacuum, and defines the fiducial volume for K_L decays. Following a thin vacuum window at the end of the decay region was a drift chamber spectrometer. The spectrometer had two pairs of drift chambers separated by an analysis magnet providing a transverse momentum kick of 0.2 GeV/c. The momentum resolution of the spectrometer was measured to be $\sigma_p/p = 0.016\% \times p \oplus 0.38\%$, where p is the momentum of a charged particle in GeV/c. A set of transition radiation detectors (TRD) downstream of the spectrometer was used to distinguish pions and electrons. Farther downstream, there was a pure cesium iodide (CsI) electromagnetic calorimeter, where the energy resolution for photons and electrons was $\sigma_E/E = 2\%/\sqrt{E} \oplus 0.45\%$, with E in GeV. Immediately upstream of the CsI calorimeter were scintillator hodoscopes, which served as the charged particle trigger. Behind the CsI was a 24 interaction-length steel filter and a set of scintillator hodoscopes to identify muons. Lead-scintillator counters were positioned around the vacuum decay region, the spectrometer and the calorimeter, to reject events with particles escaping these detectors. We analyzed data acquired during the 1997 run. A detailed description for this experiment and analysis can be found in Ref. [6, 7].

The event reconstruction begins with the identification of four charged tracks coming from a vertex in the decay region. The charged tracks are identified as $\pi^\pm e^\mp e^+ e^-$ using E/p , the energy reconstructed in the CsI calorimeter divided by the momentum measured in the spectrometer. Pions tracks are required to have E/p less than 0.9, which selects 99.2% of all pions. Electron tracks are required to have E/p between 0.93 and 1.15, and be tagged by the TRD system. The E/p and TRD requirements select 95.0% of all electrons, while rejecting 99.95% of all pions. Since the K_{e3ee} decay has three electrons, there are two candidates for the e^+e^- pair. Although each event must include both amplitudes in which one of e^+e^- pairs is from the virtual photon, in this letter, we define the pair which has smaller invariant mass as the “ e^+e^- pair”, and call the remaining electron as “ e_{ke3}^\pm ”. The amplitude in which the smaller invariant mass e^+e^- pair emerges from the virtual photon is greater in contribution than the other amplitudes. Because the neutrino is not observed, there is a two-fold ambiguity for the parent kaon energy. The higher kaon energy solution was required to be less than 200 GeV.

Monte Carlo (MC) simulations are used to understand the acceptance of the signal mode, background modes, and the normalization mode $K_L \rightarrow \pi^+\pi^-\pi_D^0$ where π_D^0 denotes the $\pi^0 \rightarrow e^+e^-\gamma$ decay. To simulate K_{e3ee} , the matrix element was computed using ChPT[NLO(p^4)] as described by Tsuji *et al.*[8]. Bremsstrahlung photons from four charged particles in K_{e3ee} are simulated using the PHOTOS program, which includes the interference terms [9, 10]. The number of background MC events are generated according to their branching fractions and K_L

flux estimated using the normalization mode.

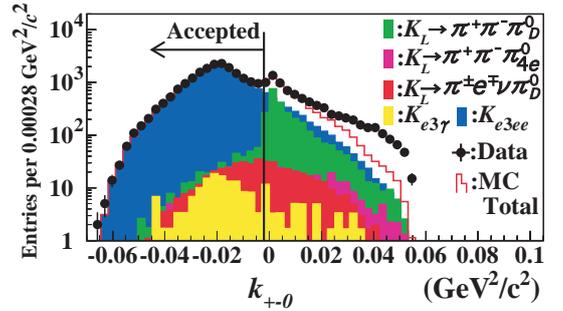


FIG. 2: The k_{+-0} distributions for data and MC after all analysis requirements except for ‘ k_{+-0} ’. The open histogram is the sum of all MC simulated modes (MC Total). The vertical line and arrow show the accepted region for the signal candidates ($k_{+-0} < -0.002$ GeV $^2/c^2$).

The backgrounds are reduced with a combination of particle identification, kinematical cuts, and vetos as indicated in Table I. The major background for the K_{e3ee} mode is due to $K_L \rightarrow \pi^+\pi^-\pi_D^0$. MC studies show that 42% of the background arising from the $K_L \rightarrow \pi^+\pi^-\pi_D^0$ decays are caused by one of the pions misidentified as an electron. The rest are due to an external photon conversion in the detector material and a missing pion and electron. Missing pions are due to track hits corrupted by hadronic interactions in the detector material, while the analysis magnet causes low momentum tracks to escape the detector. We suppress the $K_L \rightarrow \pi^+\pi^-\pi_D^0$ background using the kinematical variable,

$$k_{+-0} = \frac{(M_K^2 - M_{\pi e_{ke3}}^2 - M_{\pi^0}^2)^2 - 4M_{\pi e_{ke3}}^2 M_{\pi^0}^2 - 4M_K^2 p_t^2}{4(M_{\pi e_{ke3}}^2 + p_t^2)}, \quad (1)$$

where M_K and M_{π^0} are the kaon and π^0 masses, respectively. $M_{\pi e_{ke3}}$ is the invariant mass of the π^\pm and e_{ke3}^\mp , while the charged pion mass is assigned to the e_{ke3}^\mp . p_t is the transverse momentum of the $\pi^\pm e_{ke3}^\mp$ system. For $K_L \rightarrow \pi^+\pi^-\pi^0$ decays, k_{+-0} is the squared longitudinal momentum of the π^0 in the frame in which the momentum of $\pi^+\pi^-$ system is transverse to the K_L direction, so that k_{+-0} will be positive definite (Fig. 2). On the other hand, for K_{e3ee} events, k_{+-0} tends to have an unphysical value ($k_{+-0} < 0$). Therefore, we require $k_{+-0} < -0.002$ GeV $^2/c^2$ for the signal events. The radiative K_{e3} decay with an external photon conversion are rejected by requiring $M_{e^+e^-} > 5$ MeV/c 2 . We also considered and simulated backgrounds due to $K_L \rightarrow \pi^\pm e^\mp \nu \pi_D^0$ and $K_L \rightarrow \pi^+\pi^-\pi_{4e}^0$. These backgrounds are small mainly because of the small branching fractions.

In addition to the backgrounds in Table I, we also considered and simulated two coincident $K_L \rightarrow \pi^\pm e^\mp \nu$ decays, and the $\Xi \rightarrow \Lambda(\rightarrow p\pi^-)\pi_D^0$ decay; both of these backgrounds are negligible. After all cuts, we are left

TABLE I: The estimated backgrounds (BG) for the K_{e3ee} analysis and the dependence on analysis cuts. The third column show the BG/Signal reduction factor stemming from the combined particle ID, fiducial, and veto cuts. The fourth column shows the same effect for the kinematic cut.

Background decay mode	BG/Signal before cuts	BG/Signal after all cuts	BG/Signal Reduction Factor	
			Particle ID+Fiducial+Veto Cuts	Kinematic cut
$K_L \rightarrow \pi^+\pi^-\pi_D^0$	117	0.0182	403	16
$K_L \rightarrow \pi^\pm e^\mp \nu \pi_D^0$	0.048	0.0167	1.23	2.4
$K_L \rightarrow \pi^+\pi^-\pi_{4e}^0$	0.307	0.0096	4.48	7.2
$K_L \rightarrow \pi^\pm e^\mp \nu \gamma, \gamma$ conversion	15.0 ^a	0.0081	20.4	91

^aThe minimum simulated photon energy was 1 keV.

with a sample of 20225 events. The estimated total number of background events after all cuts is 1017.1 ± 24.7 , representing $(5.03 \pm 0.12)\%$ of the signal sample.

The normalization mode ($K_L \rightarrow \pi^+\pi^-\pi_D^0$) were collected with the same conditions as the signal mode. They are analyzed using identical cuts, except that the k_{+-0} requirement is reversed to be $k_{+-0} > -0.002 \text{ GeV}^2/c^2$. We ignore the photon in the decay in order to make the analysis more similar to the signal mode analysis, which has a missing neutrino. The only significant background for the normalization analysis is the $K_L \rightarrow \pi^+\pi^-\pi^0$ decay followed by external conversion of one of the π^0 photons. This background is determined by MC simulations to be $(0.558 \pm 0.005)\%$ of 1250828 normalization events after all cuts.

The acceptance ratio of K_{e3ee} to $K_L \rightarrow \pi^+\pi^-\pi_D^0$ depends on the efficiency ratios of an electron and a charged pion, since the signal mode has one more electron and one less pion compared to the normalization mode. Therefore, the efficiencies of an electron and a pion by the particle identification cuts are measured from data by tagging electrons and pions in $K_L \rightarrow \pi^+\pi^-\pi_D^0$ and $K_L \rightarrow \pi^+\pi^-\pi_{\gamma\gamma}^0$ decays, respectively. The differences of the efficiencies between data and MC lead to a correction applied to the MC signal acceptance, which becomes $f_{e/\pi} = 0.9955$.

After applying background subtractions and efficiency corrections, the decay width ratio of K_{e3ee} to $K_L \rightarrow \pi^+\pi^-\pi_D^0$ is

$$\begin{aligned} \mathcal{R}(ke3ee/+ - 0_D) & \\ \equiv \frac{\Gamma(K_{e3ee}; M_{e^+e^-} > 5\text{MeV}/c^2, E_{e^+e^-}^* > 30\text{MeV})}{\Gamma(K_L \rightarrow \pi^+\pi^-\pi_D^0)} & \\ = [8.54 \pm 0.07(\text{stat}) \pm 0.13(\text{syst})] \times 10^{-3}, & \quad (2) \end{aligned}$$

where $E_{e^+e^-}^*$ is the energy of e^+e^- pair system in the kaon rest frame. The acceptance of the signal events generated above the cut-off values is $(0.8986 \pm 0.0025)\%$, and the acceptance of the normalization mode is $(0.4947 \pm 0.0009)\%$. Table II lists the systematic errors in $\mathcal{R}(ke3ee/+ - 0_D)$. The largest systematic error is the uncertainty in the number of the $K_L \rightarrow \pi^+\pi^-\pi_D^0$ decays. The number of $K_L \rightarrow \pi^+\pi^-\pi_D^0$ decays measured

TABLE II: Systematic uncertainties in the ratio of decay widths, $\mathcal{R}(ke3ee/+ - 0_D)$, see Eq. 2 in the text.

Source of uncertainty	Uncertainty on $\mathcal{R}(ke3ee/+ - 0_D)(\%)$
Unobserved photon	
in normalization analysis	± 1.03
Vertex χ^2 cut	± 0.7
Radiative corrections	± 0.51
Corrections for the efficiency difference	± 0.46
E_K distribution	± 0.35
Cut-off on the $M_{e^+e^-}$	-0.18
Background estimations	± 0.05
MC statistics	± 0.32
Total systematic uncertainties	± 1.5

using the photon (full reconstruction measurement) is $(0.88 \pm 0.51)\%$ smaller than the analysis ignoring the photon. With this value and the systematic error in the full reconstruction measurement of $K_L \rightarrow \pi^+\pi^-\pi_D^0$, we assign a 1.03% systematic error on $\mathcal{R}(ke3ee/+ - 0_D)$. The second largest systematic error is based on a slight data-MC discrepancy in the distribution of the vertex χ^2 , which indicates the quality of the four track vertex. The next largest systematic error is uncertainty in the treatment of radiative corrections. With inner bremsstrahlung photons generated in the MC by the PHOTOS program, the signal acceptance decreases by 3.6%. To confirm this acceptance loss, $K_L \rightarrow \pi^\pm e^\mp \nu e^+ e^- \gamma$ ($K_{e3ee\gamma}$) events are identified and compared between data and MC. We assign a systematic uncertainty from the error in the $K_{e3ee\gamma}$ measurement, although the number of $K_{e3ee\gamma}$ events, 935, is consistent with MC prediction. The probability to miss the π track due to hadronic interactions in the TRD is determined by the GEANT program [11]. The correction applied to the MC signal acceptance is 1.0328 ± 0.0045 . We also estimate the uncertainties due to the E/p and TRD requirements. The total error in our estimate of the efficiency difference is $\pm 0.46\%$.

The K_{e3ee} branching fraction with statistical and systematic uncertainty using $B(K_L \rightarrow \pi^+\pi^-\pi^0) = (12.56 \pm 0.05)\%$ and $B(\pi^0 \rightarrow e^+e^-\gamma) = (1.198 \pm 0.032)\%$ [12] is

$$B(K_{e3ee}; M_{e^+e^-} > 5\text{MeV}/c^2, E_{e^+e^-}^* > 30\text{MeV})$$

$$= [1.285 \pm 0.010(stat) \pm 0.040(syst)] \times 10^{-5}. \quad (3)$$

The systematic error is much larger than that of $\mathcal{R}(ke3ee/+ - 0_D)$, due to the 2.7% error on $B(\pi^0 \rightarrow e^+e^-\gamma)$.

In the rest of this letter, we compare our results against the ChPT[NLO(p^4)] description of the K - π current. Using the K_{e3} branching fraction, $B(K_{e3}) = (40.53 \pm 0.15)\%$ [12], we find

$$\begin{aligned} \mathcal{R}_{Ke3ee} &\equiv \frac{\Gamma(K_{e3ee}; M_{e^+e^-} > 5\text{MeV}/c^2)}{\Gamma(K_{e3})} \\ &= [4.57 \pm 0.04(stat) \pm 0.14(syst)] \times 10^{-5}. \end{aligned} \quad (4)$$

The leading order ChPT and ChPT[NLO(p^4)] predictions for \mathcal{R}_{ke3ee} are $(4.06 \pm 0.11) \times 10^{-5}$, and $(4.29 \pm 0.11) \times 10^{-5}$ respectively. Although the experimental determination of \mathcal{R}_{Ke3ee} include all radiative effects, neither the theoretical estimates of the numerator and denominator include these effects. To account for the lack of radiative treatment in the \mathcal{R}_{Ke3ee} predictions, we assign an error of twice the value of δ_{Ke3} . The variable δ_{Ke3} is 0.013 ± 0.003 , and parameterizes the increase in decay width of the K_{e3} mode due to radiative corrections [13]. The ChPT[NLO(p^4)] prediction is consistent with the measurement at the 1.6σ level.

As the K - π form factor is parameterized by the square of the four momentum transfer to the leptons $t \equiv (p_K - p_\pi)^2$, higher order calculations of ChPT are sensitive to t . However, the K_{e3ee} decay has a two-fold ambiguity in t due to the missing neutrino. To avoid this problem, we use the transverse momentum transfer as defined in [14],

$$t_\perp = M_K^2 + M_\pi^2 - 2M_K \sqrt{p_{\perp,\pi}^2 + M_\pi^2}, \quad (5)$$

where M_π is the charged pion mass and $p_{\perp,\pi}$ is the transverse pion momentum.

Figure 3 shows that the data t_\perp/M_π^2 distribution agrees with the NLO(p^4) calculation, but not with the leading order ChPT calculation. Figure 4 shows the invariant mass of the e^+e^- pair, illustrating that ChPT[NLO(p^4)] models well the K_{e3ee} dynamics. The $M_{\pi eee}$, M_{eee} , and $M_{\pi e}$ distributions are also well modeled with the ChPT[NLO(p^4)] prediction.

In summary, we find good agreement between our measurements and the NLO(p^4)ChPT calculation, while the leading-order ChPT calculation is disfavored. Finally, we note that Figure 4 is expected to receive contributions from both IB and SD amplitudes, with the IB amplitudes being dominant. The separation between IB and SD amplitudes has not been performed in the context of ChPT. Additional theoretical work is needed to extract the SD contribution.

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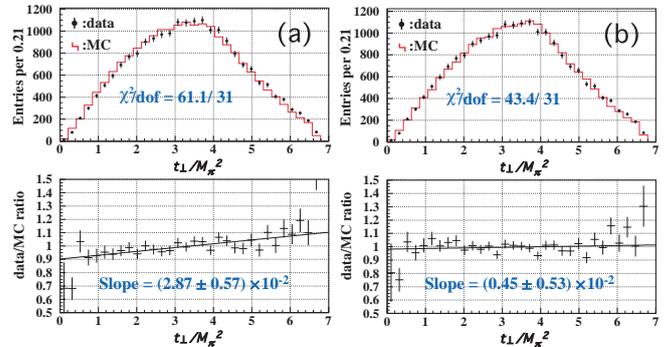


FIG. 3: Comparisons of the t_\perp/M_π^2 distributions for data (dots) and MC (histogram), (a) with MC-LO and (b) with MC-NLO(p^4). The data-to-MC ratios at the bottom are fit to a straight line.

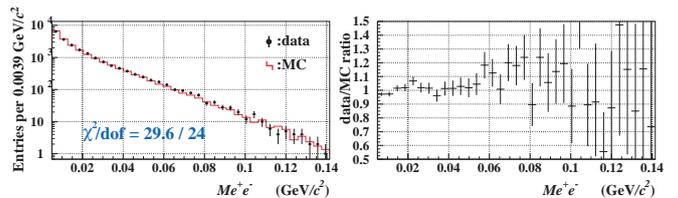


FIG. 4: Comparison of the $M_{e^+e^-}$ distribution for data (dots), and MC (histogram) with NLO(p^4) correction.

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