Measurement of the Ratios of Branching Fractions $\mathcal{B}(B^0 \rightarrow D^- \pi^+)/\mathcal{B}(B^0 \rightarrow D^- \pi^-)$ and $\mathcal{B}(B^+ \rightarrow D^{0\pi}+)/\mathcal{B}(B^0 \rightarrow D^- \pi^-)$


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We report an observation of the decay $B^0_d \to D^- \pi^+$ in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV using 115 pb$^{-1}$ of data collected by the CDF II detector at the Fermilab Tevatron. We observe $83 \pm 11$ $B^0_d \to D^- \pi^+$ candidates, representing a large increase in statistics over previous measurements and the first observation of this decay at a $p\bar{p}$ collider. We present the first measurement of the relative branching fraction $B(B^0_d \to D^- \pi^+)/B(B^0 \to D^- \pi^+) = 1.32 \pm 0.18$ (stat.) $\pm 0.38$ (syst.). We also measure $B(B^+ \to D^0 \pi^-)/B(B^0 \to D^- \pi^+) = 1.97 \pm 0.10$ (stat.) $\pm 0.21$ (syst.), which is consistent with previous measurements.

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$B^0_d$-$\bar{B}^0_d$ oscillation is expected to occur in the Standard Model of particle physics. Measurement of the oscillation frequency, when combined with that for $B^0$-$\bar{B}^0$ oscillation, tests the unitarity of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix. A deviation from unitarity could arise from a variety of new physics effects [1]. $B^0_d$ meson oscillations have yet to be directly observed, with a lower limit (95% C.L.) on the oscillation frequency currently at 14.5 ps$^{-1}$ [2]. For comparison, the average $B$ meson lifetime is of the order of 1 ps, and the $B^0$ oscillation frequency is 0.5 ps$^{-1}$. This lower limit implies that excellent proper time resolution is required to
observe the oscillation. In semileptonic $B^0_s$ decays, the proper time measurement is degraded due to the undetected neutrino. Fully reconstructed hadronic $B^0_s$ decays such as $B^0_s \to D^*_s \pi^+$ do not suffer from this problem [3]. Obtaining a large sample of such decays is an important first step toward measuring $B^0_s$ mixing.

In addition, the measurement of the branching ratio of $B^0_s \to D_s^- \pi^+$ decay along with that of $B^0 \to D^- \pi^+$ and $B^+ \to D^+ \pi^+$ can be used to study $B$ meson decay mechanisms. As shown in Fig. 1, $B^0_s \to D^- \pi^+$ decay proceeds only at tree level while the $B^0$ and $B^+$ modes have additional, non-tree, contributions. Therefore, measurements of ratios of branching fractions of these decays can, in principle, isolate contributions from the different decay diagrams [4].

To date, a few $B^0_s \to D_s^- \pi^+$ events have been observed [5, 6] in $e^+e^-$ collisions at LEP. $B$ factories, currently running at the $\Upsilon(4S)$ resonance, do not produce $B^0_s$ mesons. However, large samples of $B^0_s$ are produced at the Tevatron. The ability to trigger on displaced vertices allows the upgraded Collider Detector at Fermilab (CDF II) to collect large samples of fully reconstructed $B^0_s$ decay modes.

In this letter, we present an observation of $B^0_s \to D^- \pi^+$ decays and a measurement of the ratios of branching fractions of $B^0_s \to D^- \pi^+$ and $B^+ \to D^+ \pi^+$ relative to the branching fraction of $B^0 \to D^- \pi^+$ decays. We use a sample of fully reconstructed $B \to D \pi$ decays corresponding to 115 pb$^{-1}$ of $\bar{p}p$ collisions at $\sqrt{s} = 1.96$ TeV collected by the CDF II detector at the Fermilab Tevatron between February 2002 and January 2003. Charge conjugate modes are implied throughout this paper.

The components of the CDF II detector relevant to this analysis are described briefly below; a more complete description can be found elsewhere [7]. We use tracks reconstructed by both the Central Outer Tracker (COT) and the silicon microstrip detector (SVX II) in the range $|\eta| \leq 1$ [8], where $\eta$ is the pseudorapidity defined as $\eta = -\ln(\tan(\theta/2))$ and $\theta$ is the polar angle with respect to the proton beam direction. The SVX II detector consists of double-sided silicon strip sensors arranged in five cylindrical shells with radii between 2.5 and 10.6 cm [9]. Surrounding the SVX II is the COT [10], an open-cell drift chamber that has an inner (outer) radius of 40 (137) cm. The COT has 96 layers, organized in 8 superlay-

![Diagram of Feynman diagrams](image)

**FIG. 1:** Different Feynman diagrams which contribute to $B \to D_s \pi$ decays.
$D$ meson points back, in three dimensions, to the remaining $B$ meson candidate track, and the invariant mass of the $D$ meson decay products is consistent with the world average of the corresponding $D$ meson mass [2]. We also require that at least two of the $B$ meson daughter tracks are consistent with the trigger requirements. The combinatorial background is strongly reduced by requiring that $L_{xy}^B > 400 \mu m$ and $L_{xy}(B \rightarrow D) > -150 \mu m$, where the latter refers to the $L_{xy}$ of the $D$ meson decay vertex with respect to the $B$ meson decay vertex. The impact parameter of the $B$ meson momentum with respect to the beam axis is required to be less than 80 $\mu m$ to assure that the $B$ meson candidate originates from the primary vertex. The invariant mass distributions of $B^0$, $B^+$, and $B^0$ meson candidates are shown in Fig. 2. The prominent peak at each expected $B$ meson mass establishes $B \rightarrow D\pi$ decay signals, including our observation of $B^0 \rightarrow D^-\pi^+$. We measure the following ratio:

$$
\frac{B(B^0 \rightarrow D^-\pi^+)}{B(B^0 \rightarrow D^-\pi^+)} = \frac{N(B^0)}{N(B^0)} \cdot \frac{\epsilon(B^0)}{\epsilon(B^0)} \cdot \frac{f_d}{f_s} \frac{B(D^- \rightarrow K^+\pi^-\pi^-)}{B(D^- \rightarrow \phi\pi^-) \cdot B(\phi \rightarrow K^+K^-)}
$$

where $N(B^0)$ and $N(B^0)$ are the signal yields, $f_d/f_s$ is the ratio of fragmentation fractions for $B^0$ and $B^0$ mesons, and $\epsilon(B^0)/\epsilon(B^0)$ is the ratio of trigger and reconstruction efficiencies. Equation 1 also applies to the $B^+ \rightarrow D^+\pi^+$ mode, with terms for $B^0$ decays replaced by those relevant to $B^+$ decays. There are three components to the ratio of branching fractions measurement: the ratio of $B$ meson yields obtained from fits to the invariant mass spectra, the ratio of signal efficiencies obtained from Monte Carlo simulation, and the product of previously measured production and branching fractions.

In our analysis, we use Monte Carlo simulation to determine shapes of mass spectra and relative efficiencies. The Monte Carlo generation proceeds as follows. Transverse momentum and rapidity distributions of single $b$ quarks are generated based on calculations using NLO perturbative QCD [13]. $B$ meson kinematic distributions are obtained by simulating Peterson fragmentation [14] on quark-level distributions. Additional fragmentation particles, correlated $b$-antibaryon production and the underlying event structure are not simulated. $B$ meson decays are simulated using EvtGen [15]. The simulation of the CDF II detector and trigger is based upon a GEANT description [16] that includes effects of time variation of the beam position and hardware configuration of the SVX II and SVT.

The yield of $B$ mesons is extracted from the invariant mass spectra using a binned $\chi^2$ fit, as shown in Fig. 2. There are three contributions to the background shape used in the fit. The combinatorial background component is modeled with a linear combination of a linear and exponential distribution. The shape of background due to Cabibbo-suppressed $B \rightarrow DK$ decay is modeled by a Gaussian and is shown as shaded distributions in Fig. 2(a)-(c). Backgrounds due to partially reconstructed $B$ decays contribute to the low mass side of the signal peak and are modeled by inclusive $B \rightarrow DX$ Monte Carlo simulation. The structures in the region close to the signal are due to $B \rightarrow D^*\pi$ decays, where a photon or a $\pi^0$ from the $D^*$ decay is not reconstructed. The decay of the polarised $D^*$ produces the double-peaked structure. As an example of the various contributing backgrounds, Fig. 2(d) shows the invariant mass spectrum for $B \rightarrow DX$ Monte Carlo reconstructed as $B^+ \rightarrow D^0\pi^+$. In the fit

![Plot](image_url)

**Fig. 2.** Invariant mass spectra for (a) $D^-\pi^+$, (b) $D^-\pi^+$, and (c) $D^0\pi^+$ for data, with $\chi^2$ fits overlaid. The main background under the signal peak is combinatorial, modeled with a combination of a linear and exponential function. The shaded peak corresponds to $B \rightarrow DK$ decays, and is modeled with a Gaussian. The additional background component in the low mass region is due to partially reconstructed $B$ decays. This background component is modeled using shapes determined by inclusive $B \rightarrow DX$ Monte Carlo. A sample Monte Carlo mass distribution for $B^+ \rightarrow D^0\pi^+$ events is shown in (d). Contributions from different sources in (d) are ordered by peak position, from right to left.
to the data mass spectrum, the fractions of combinatorial background and partially reconstructed B's are allowed to float in the fit. The ratio of Cabibbo-suppressed B → DK background to the corresponding signal is fixed to the world average ratio of branching fractions, with the trigger and reconstruction efficiencies of the two modes taken into account. The fitted yields of B^0 → D^-π^+, B^+ → D^0 and B^0 → D^-π^+ decays are 1118 ± 43(stat.), 1260 ± 42(stat.) and 88 ± 11(stat.) events, respectively.

Trigger and reconstruction efficiencies for B^0, B^+, and B^0 decays are determined using Monte Carlo simulation. The trigger efficiency differs among the three B meson decay modes due to differences in decay kinematics (e.g., opening angle distributions) which arise from the different masses and spins of the intermediate and final state particles. The ratios of efficiencies are ε(B^0)/ε(B^-) = 0.708 ± 0.010 and ε(B^0)/ε(B^0) = 0.903 ± 0.012, where the uncertainties are due to the limited statistics of Monte Carlo samples.

World average values [2] are used for the various branching fractions in Equation 1. In terms of B meson production, we assume f_d = f_s, consistent with previous measurement [17]. The B^0/B^0 production fraction used in this analysis is the world average value, f_s/f_d = 0.270 ± 0.029, currently dominated by LEP measurements. The ratio of fragmentation fractions may be different in a hadron collider environment than in e^+e^- collisions. However, the ratio of fragmentation fractions measured by CDF [17] is consistent with the LEP results.

Many systematic uncertainties cancel in the measurement of ratios of branching fractions due to the similarity of final state kinematics. Systematic uncertainties come from three main sources: fitting the invariant mass distributions to obtain signal yields, determination of the ratio of efficiencies, and uncertainties on external inputs. The contribution to the systematic uncertainty from externally measured quantities is calculated by propagating world average uncertainties. Systematic uncertainties on the signal yields are determined by comparing the fitted yields after changing the background shape within the range allowed by the B → DX Monte Carlo statistics and world average uncertainties on the branching fractions of participating B decays. Systematic uncertainties on the ratio of efficiencies come from physics sources such as the choice of p_T spectrum or meson lifetime, and detector sources such as inaccuracies in the XFT and SVT hardware simulation. The uncertainty due to a given source is estimated by the shift of the ratio of efficiencies when the effect of that source is modified in the Monte Carlo simulation. The effect of the choice of B meson p_T spectrum is estimated by re-weighting the Monte Carlo to match the measured B hadron p_T spectrum [7]. Since the trigger and analysis selection only accept events in which the B meson is displaced from the primary interaction point, the efficiencies depend upon the B and D meson lifetimes. To estimate uncertainties due to B and D meson lifetimes, the Monte Carlo is re-weighted with different lifetimes within the world average uncertainties. Due to the different specific ionization of π^± and K^± in the COT, kaons are 16% less efficient in satisfying the XFT requirements [18]. The Monte Carlo simulation is re-weighted to reproduce this effect. To estimate the uncertainty due to imperfections in simulating the signal selection requirement efficiencies, we compare efficiencies between Monte Carlo simulation and sideband subtracted B^+ and B^0 signal for every selection requirement separately. In the case of the B^+/B^0 branching fraction ratio measurement, there is an additional systematic uncertainty associated with the fact that the B^0 decay has four tracks in the final state while B^+ has only three. We infer the corrections and systematic uncertainties due to the fourth track by comparing trigger and reconstruction efficiencies in data and Monte Carlo for semileptonic B → D^*-l^-X, D^- → D^-π^- decays between the B^0 → K^-π^- and K^-π^-π^-π^- final states.

The systematic uncertainties are summarized in Table 1. The total systematic uncertainty is obtained by adding individual contributions in quadrature. Using Equation 1, we obtain the following values for the ratios of branching fractions:

\[
\frac{B(B^0_p \rightarrow D_s^-\pi^+)}{B(B^0 \rightarrow D^-\pi^+)} = 1.32 \pm 0.18(\text{stat.}) \pm 0.10(\text{syst.}) \\
\pm 0.14(\text{BR}) \pm 0.14(\text{PR})
\]  

(1)

\[
\frac{B(B^+ \rightarrow D^0\pi^+)}{B(B^0 \rightarrow D^-\pi^+)} = 1.97 \pm 0.10(\text{stat.}) \pm 0.15(\text{syst.}) \\
\pm 0.14(\text{BR})
\]  

(2)

where BR and PR refer to the uncertainty on the ratio of D meson branching fractions and B^0 meson production relative to B^0, respectively. Under the assumption of isospin invariance, our measurement of the ratio B(B^+ → D^0\pi^+)/B(B^0 → D^-\pi^+) is consistent with the world average [2]. This provides a high statistics cross-check of the measurement procedure.

In conclusion, we have presented the first observation of B^0_p → D_s^-\pi^+ decays in pp collisions, and the first measurement of the B^0_p → D_s^-\pi^+ branching fraction relative to the B^0 → D^-\pi^+ branching fraction. The precision of this measurement is currently not adequate to separate the contributions of different decay diagrams [4]. We expect the measurement precision to improve as world average values of D meson branching fractions and B meson production fractions improve.

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[8] CDF II uses a cylindrical coordinate system in which $\varphi$ is the azimuthal angle, $r$ is the radius from the nominal beamline, $y$ points up and $z$ points in the proton beam direction with the origin at the center of the detector. The transverse plane is the plane perpendicular to the $z$ axis. A superconducting magnet provides a nearly uniform 1.4 T axial field in which charged particles are reconstructed.