



## Heavy Flavour Lifetimes and Lifetime Differences

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We give an overview of heavy flavour lifetime measurements, focusing on recent results from the Tevatron and the B factories.

### 1 Introduction

In the first part of this article we summarise the status and latest measurements of B-hadron lifetimes and lifetime ratios, including some recent result from the Tevatron and the B factories, and compare those results with the predictions from Heavy Quark Expansion (HQE). Future prospects for lifetime measurements at the B factories and the Tevatron are discussed.

In the second part, we review the status and prospects of measuring the difference between the lifetimes of the two CP eigenstates in the  $B_s^0$ - $\overline{B}_s^0$  system.

### 2 Lifetimes and Lifetime Ratios

#### 2.1 Theoretical Predictions on B Hadron Lifetimes

Life time measurements in the heavy quark sector gain specific significance due to the precise predictions of Heavy Quark expansion (see e.g. [1], [2]) thus providing a testing ground for this theoretical tool that is frequently used, for example to relate experimental measurements to CKM parameters like  $\Gamma_d$  to  $|V_{cb}|$  or  $\Delta m_s/\Delta m_d$  to  $|V_{ts}/V_{td}|$ .

The hierarchy expected for b hadron lifetimes is [3]:

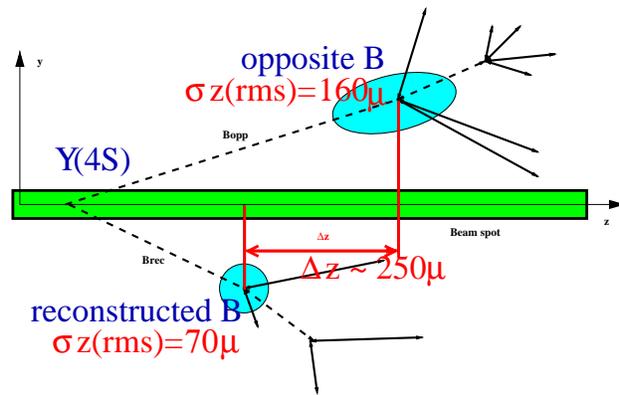
$$\begin{aligned} \tau(B_c) &\ll \tau(\Xi_b^0) \\ &\sim \tau(\Lambda_b) < \tau(B_d^0) \sim \tau(B_s^0) < \tau(B^-) \\ &< \tau(\Xi_b^-) < \tau(\Omega_b). \end{aligned}$$

Recent HQE predictions for the lifetime ratios are [4]:

- $\tau(B^-)/\tau(B_d^0) = 1.06 \pm 0.02$
- $\tau(B_s)/\tau(B_d^0) = 1.00 \pm 0.01$
- $\tau(\Lambda_b)/\tau(B_d^0) = 0.90 \pm 0.05$

#### 2.2 The B Factories

The B factories BABAR and BELLE at the asymmetric  $e^+e^-$  colliders PEP-II and KEK have collected  $123 \text{ fb}^{-1}$  and  $145 \text{ fb}^{-1}$  worth of data respectively up to May 2003, running at the  $\Upsilon(4S)$  resonance.



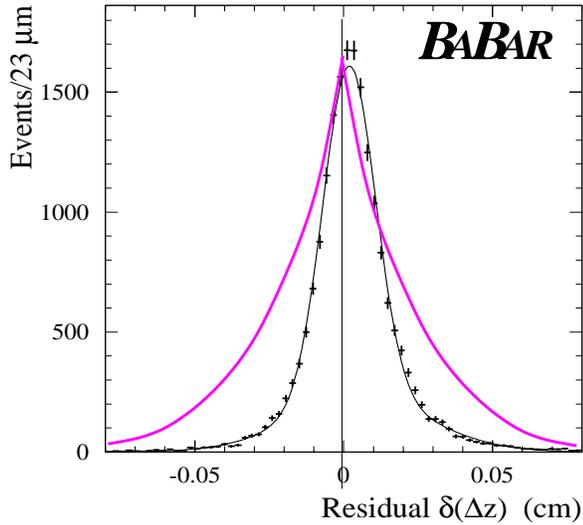
**Figure 1.** Schematic of lifetime measurements at BABAR (from [11] with added comments).

#### 2.2.1 Lifetimes at the B Factories: Method

The  $\Upsilon(4S)$  decays to  $B_d^0$ ,  $\overline{B}_d^0$  or  $B^+$ ,  $B^-$ , nearly at rest in the  $\Upsilon(4S)$  rest frame. By colliding  $e^+$  and  $e^-$  of different energies, the CM frame is boosted ( $\beta\gamma \sim 0.54$  for BABAR and  $\sim 0.43$  for BELLE) such that the  $B_d^0$  and  $\overline{B}_d^0$  travel a measurable distance in the detector before decaying.

Because the B mesons decay virtually at rest in the  $\Upsilon(4S)$  frame, their momenta in the lab frame are known from the beam momentum. This constrains the decay dynamics considerably with the important consequence that the decay vertex of a B meson can be obtained from a single decay product, by intersecting its track with the beam axis. The decay distance along the beamline ( $z$ ) is directly proportional to the proper decay time for a given beam momentum (small corrections apply [11]). Lacking primary vertex information, it is the distance between the decay vertices of the two B mesons that is used for measuring the life time. This distance is typically  $\sim 250 \mu\text{m}$  and  $\sim 200 \mu\text{m}$  at BABAR and BELLE respectively.

In the standard method, one B meson is fully reconstructed ( $B_{\text{rec}}$ ), and another one partially, from as little as one or two tracks ( $B_{\text{opp}}$ ), with a correspondingly degraded vertex resolution. The lifetime difference is calculated from the difference in the position along the beam line ( $\Delta z = z_{B_{\text{reco}}} - z_{B_{\text{opp}}}$ ) of the two B vertices. This is illustrated in Fig. 1. The resolution function is modeled using Monte Carlo simulation.



**Figure 2.**  $\Delta z$  Resolution at BABAR for  $B^+ \rightarrow J/\psi K^+$  [11], with  $\exp(\Delta z/250 \mu\text{m})$  superimposed for illustration.

In Fig. 2, the Monte Carlo generated resolution function for  $\Delta z$  at BABAR for the decay  $B^+ \rightarrow J/\psi K^+$  is shown [11]. An exponential with a mean decay distance of 250  $\mu\text{m}$ , representing approximately the signal distribution before detector effects, is superimposed, illustrating how the signal is of a similar width as the resolution function, which must therefore be modeled carefully. This modeling of the resolution function, together with the modeling of the background distribution, is the biggest systematic uncertainty in both experiments. The so-called “outliers”, a relatively small number of events with very large reconstructed  $\Delta z$ , represent a particular problem. Both experiments are able to control it well enough to keep the systematic error below the statistical uncertainty.

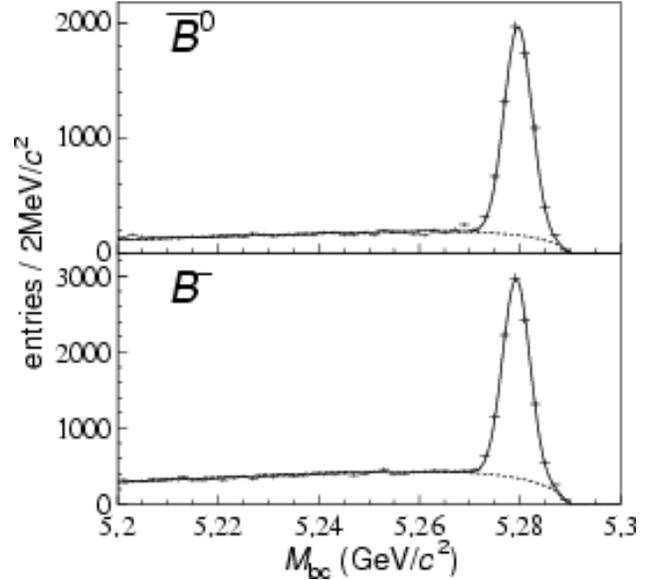
Both experiments describe the  $\Delta t = \Delta z / (c(\beta\gamma)_r)$  distribution in terms of three components: signal, background and outliers. The beam constrained mass (shown in Fig. 3 for BELLE) is used for an event-by-event signal probability. The fraction of outliers is a free fit parameter. The  $B_d^0$  and  $B^+$  distributions are fit simultaneously in an unbinned likelihood fit. Besides these commonalities, there are some differences in the event selection and modeling of the resolution function which are described in detail in the publications by the respective experiments [10] [12].

### 2.2.2 Results

#### BELLE

Using the following fully reconstructed hadronic decays:  $B^0 \rightarrow D^{(*)-}(\pi^+, \rho^+), J/\psi K_S^0, J/\psi K^{*0}$ ,  $B^+ \rightarrow \bar{D}^0 \pi^+, J/\psi K^+$ , BELLE find the following  $B_d^0$  and  $B^+$  lifetimes [12]:

$$\tau_{B_d^0} = 1.554 \pm 0.030 \pm 0.019 \text{ ps}$$



**Figure 3.**  $N^2$  of events vs Beam Constrained Mass at BELLE [12]

$$\begin{aligned} \tau_{B^+} &= 1.695 \pm 0.026 \pm 0.015 \text{ ps} \\ \tau_{B^+} / \tau_{B_d^0} &= 1.091 \pm 0.023 \pm 0.014 \end{aligned}$$

The fit result to the data, showing separately the background and the outlier contribution, is shown in Fig. 4.

#### BABAR Fully Hadronic

Using the following fully reconstructed hadronic decays:  $B^0 \rightarrow D^{(*)-}(\pi^+, \rho^+, a_1^+), J/\psi K_S^0, J/\psi K^{*0}$  and  $B^+ \rightarrow \bar{D}^0 \pi^+, J/\psi K^+, \psi(2S)K^+$  BABAR find the following  $B_d^0$  and  $B^+$  lifetimes [10]:

$$\begin{aligned} \tau_{B_d^0} &= 1.546 \pm 0.032 \pm 0.022 \text{ ps} \\ \tau_{B^+} &= 1.673 \pm 0.032 \pm 0.023 \text{ ps} \\ \tau_{B^+} / \tau_{B_d^0} &= 1.082 \pm 0.026 \pm 0.012 \end{aligned}$$

The fit result to the data is shown in Fig. 5.

#### More results from BABAR

As mentioned earlier, the decay kinematics at BABAR and BELLE allow to find the  $z$  position of a decay vertex from as little as a single track. While in the previously mentioned measurements, one of the pair of B’s is fully reconstructed, BABAR also published a set of measurements where also the  $B_{\text{rec}}$  is reconstructed partially. These are summarised in Table 1.

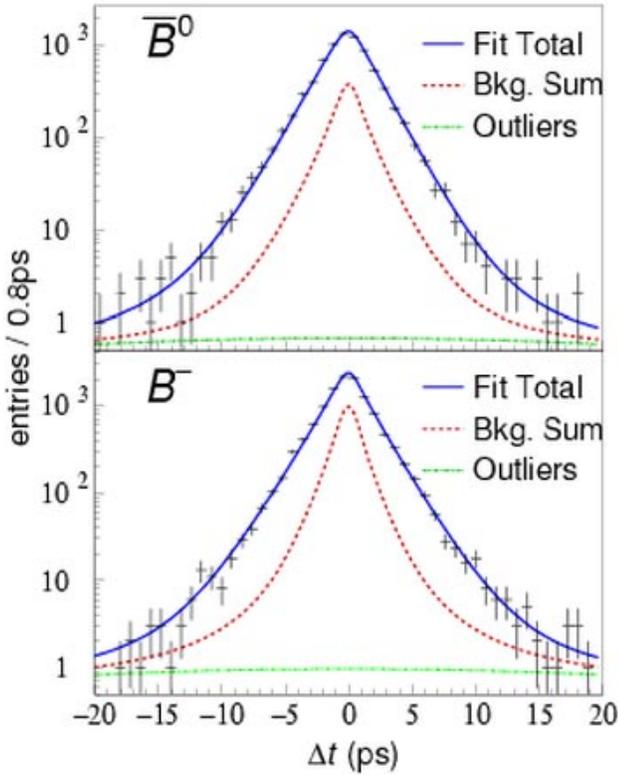


Figure 4. BELLE's life time fit [12].

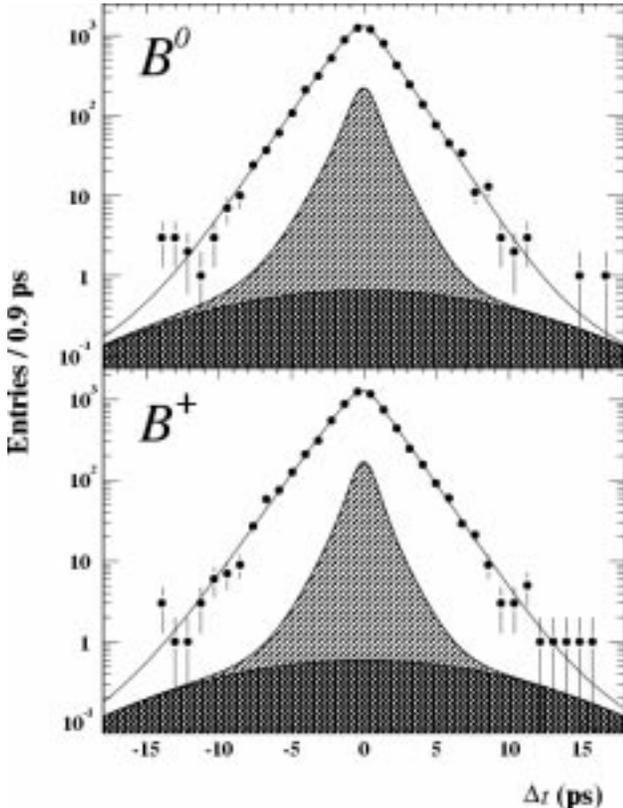
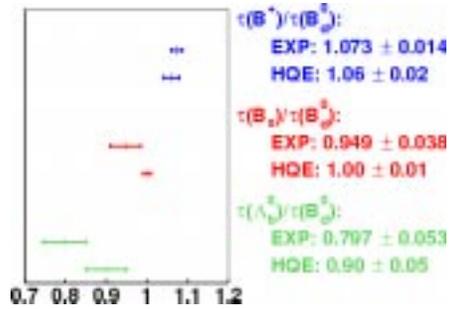


Figure 5. BABAR's life time fit [10]. Solid line: total fit. Single hatched: total background. Cross hatched: outliers.

	$B^0 \rightarrow D^{*-}(\text{partial})\ell^+\nu$ [13]
$\tau_{B_d^0}$	$1.529 \pm 0.012 \pm 0.029$ ps
	$B^0 \rightarrow D^{*-}(\text{partial})(\pi^+, \rho^+)$ [14]
$\tau_{B_d^0}$	$1.533 \pm 0.034 \pm 0.038$ ps
	$B^0 \rightarrow D^{*-}\ell^+\nu$ [15]
$\tau_{B_d^0}$	$1.523^{+0.024}_{-0.023} \pm 0.022$ ps
	Di-lepton (prelim) [16]
$\tau_{B_d^0}$	$1.557 \pm 0.028 \pm 0.027$ ps
$\tau_{B^+}$	$1.655 \pm 0.026 \pm 0.027$ ps
$\tau_{B^+}/\tau_{B_d^0}$	$1.064 \pm 0.031 \pm 0.026$ ps

 Table 1. BABAR's results from partially reconstructed decays. Here, a "partial  $D^*$ " is a  $D^*$  decaying to  $D^0\pi$ , reconstructed using kinematic constraints and the pion momentum, only, without reconstructing the  $D^0$  [14].

 Figure 6. Status of lifetime ratio measurements, incl. results from BABAR, BELLE, CDF, LEP.  $\tau(B_s)/\tau(B_d)$  and  $\tau(B^+)/\tau(B_d)$  from [17],  $\tau(\Lambda_b)/\tau(B_d)$  from [18].

### 2.2.3 Status of Lifetime Measurements Including Results from BABAR and BELLE

Since the B factories have started taking data, they have reduced the error on  $\tau_{B^+}/\tau_{B_d^0}$  by half. Fig. 6 shows the current status of the life time measurements and compares them with HQE predictions. The  $\tau_{B^+}/\tau_{B_d^0}$  measurement, dominated by the precise results from the B factories, is already more precise than that of the HQE prediction, and we can expect further improvements in the near future.

The situation is different for the  $B_s$  and the  $\Lambda_b$ , which are not accessible at the B factories. The experimental precision of the  $\tau_{B_s^0}/\tau_{B_d^0}$  measurement lags behind that of the HQE calculations. For the  $\Lambda_b$ , experiment and theory don't appear to be in very good agreement, but the experimental and theoretical uncertainties are still rather large. Improved measurements and calculations are needed for clarification.

Both,  $B_s$  and  $\Lambda_b$  particles are produced abundantly at hadron colliders, from where we expect dramatically improved lifetime measurements in the near future. The hadron collider currently producing large numbers of  $B_s$  and  $\Lambda_b$  is the Tevatron at Fermilab.

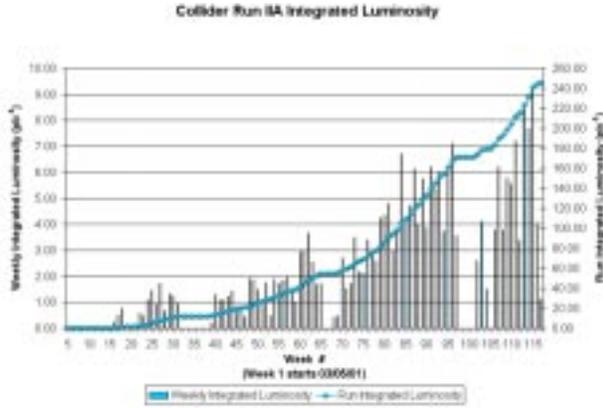


Figure 7. Luminosity at the Tevatron

Projected $\int \mathcal{L} dt / (\text{fb}^{-1})$		
Year	Baseline	Stretch
2002	0.08	0.08
2003	0.2	0.32
2004	0.4	0.6
2005	1.0	1.5
2006	1.5	2.5
2007	1.5	3.0
2008	1.8	3.0
Total	6.5	11.

Table 2. Projected integrated luminosity at the Tevatron for baseline and best-case (“stretch”) scenario. The total integrated luminosity by 2008 is expected to be between  $6 \text{ fb}^{-1}$  and  $11 \text{ fb}^{-1}$ .

## 2.3 Lifetimes at the Tevatron

### 2.3.1 Run II

CDF and DØ have been taking data at Tevatron Run IIA for about two years. For  $p\bar{p}$  collisions at 1.96 TeV, the  $b\bar{b}$  production cross section is  $\sigma_{b\bar{b}} \sim 0.1 \text{ mb}$ . The integrated luminosity delivered until June 2003 is shown in Fig. 7. The integrated luminosity at Run IIA is expected to be  $2 \text{ fb}^{-1}$ .

The projected luminosity for each year until 2008 is listed in Table 2, for two scenarios: The base-line scenario, and a best-case scenario (“stretch”). The total integrated luminosity at the end of Run II in 2008 is expected to lie between  $6 \text{ fb}^{-1}$  and  $11 \text{ fb}^{-1}$ .

### 2.3.2 DØ and CDF

Both experiments at the Tevatron have undergone major upgrades for Run II, optimising their B physics potential. The most significant upgrade at DØ is the introduction of a magnetic field and a new tracking system providing precise momentum information. This significantly improves the mass resolution. CDF also improved its tracking with a new, faster drift chamber. Both experiments have new

L1: 2 XFT tracks, $p_t > 2 \text{ GeV}$ , $\Delta\phi < 135^\circ$ , $p_{t1} + p_{t2} > 5.5 \text{ GeV}$ .	
L2:	
2-body: e.g. $B_d^0 \rightarrow \pi\pi$	Multi-body: e.g. $B_s^0 \rightarrow D_s\pi$
$100 \mu\text{m} < IP < 2 \text{ mm}$	$120 \mu\text{m} < IP < 2 \text{ mm}$
$20^\circ < \Delta\phi < 135^\circ$	$2^\circ < \Delta\phi < 90^\circ$
$L_{xy} > 200 \mu\text{m}$	$L_{xy} > 200 \mu\text{m}$
IP of B $< 140 \mu\text{m}$	–
L3: Same with refined tracks & mass cuts.	

Table 3. The CDF hadron trigger.  $\Delta\phi$  is the angle between the tracks in the transverse plane. IP is the impact parameter in that plane.  $L_{xy}$  is the decay length in the transverse plane, which can be calculated from the impact parameters and  $\Delta\phi$ .

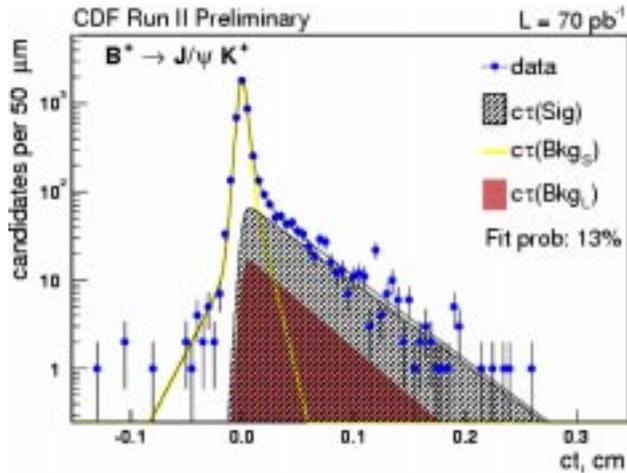
Silicon vertex trackers providing excellent proper time resolution, sufficient to resolve the expected fast oscillations in the  $B_s^0$  system. The excellent impact parameter resolution is used for triggering on B-events. Both experiments have increased their muon coverage since Run I, and have an efficient di-muon trigger for finding  $B^0 \rightarrow J/\psi X$  decays. DØ’s  $\mu$ -trigger covers a particularly large pseudo rapidity range up to  $|\eta| = 2$ .

### IP Trigger

One of the most innovative improvements for B physics at the Tevatron is the large-bandwidth hadron trigger at CDF, which triggers on the impact parameters of tracks at Level 2. The eXtremely Fast Tracker (XFT) uses pattern matching to find tracks in the COT (drift chamber) within  $5.5 \mu\text{s}$ , with about 96% efficiency for momenta above  $1.5 \text{ GeV}$ . These XFT tracks are combined with tracks in the Silicon Vertex Detector by the Silicon Vertex Tracker (SVT), which makes impact parameter information available at Level 2 to a precision of  $\sim 50 \mu\text{m}$ . The 2-Track hadron trigger combines the information on the direction (XFT), momentum (XFT) and impact parameter (SVT) to trigger on hadronic B decays. The trigger requirements for the two scenarios, 2-body and multi-body B decays, are given in Table 3. The SVT+lepton trigger for semileptonic B decays has impact parameter requirements on one track only and requires additionally an electron or muon with  $p_t > 4 \text{ GeV}$ .

DØ also has impact parameter information available at Level 2, and will have a lepton+displaced track trigger, which was however not yet available for the data presented here.

For lifetime measurements it is essential that the bias due to the impact parameter cuts in the trigger is corrected for. We will first consider measurements that do not suffer from such a trigger bias, and then those that do.



**Figure 8.** Projection of Fit to  $c\tau_{B^+}$  from  $B_u^+ \rightarrow J/\psi(\mu^+\mu^-)K^+$  at CDF, using  $70 \text{ pb}^{-1}$  of data.

### 2.3.3 Measurements Using Fully Reconstructed Decays, Without IP Trigger

Both experiments have published results from fully reconstructed hadronic  $B \rightarrow J/\psi X$  decays from the dimuon trigger, which are not biased by any impact parameter cut. An example fit (CDF,  $70 \text{ pb}^{-1}$ ,  $B_u^+ \rightarrow J/\psi(\mu^+\mu^-)K^+$ ) is shown in Fig. 8. The signal is modeled with an exponential, the background by a prompt component and two positive and one negative exponential tails (only one positive tail for  $B_s^0$  because of lower statistics). Signal and background function are convolved with a single Gaussian to take into account detector effects. The B mass is fit simultaneously and provides an event-by-event signal probability. DØ use a somewhat different approach, as illustrated in Fig. 9, modeling the background using a separate fit to the right sideband. The left sideband has a long-lifetime component from incompletely reconstructed other B decays. This B contamination in the signal region is modeled from Monte Carlo and found to be 12%.

The results are given in Table 2.3.3. The table shows that the error on the life time ratios obtained from  $B \rightarrow J/\psi X$  decays is about twice that achieved in Run I, all channels combined. By the end of this year, CDF is expected to have collected  $\sim 300 \text{ pb}^{-1}$ , four times as much as used for the analyses presented here, so we can expect CDF to achieve the combined Run I precision using the exclusive channels alone by the end of this year.

### 2.3.4 Measurements Using Partially Reconstructed Decays, Without IP Trigger

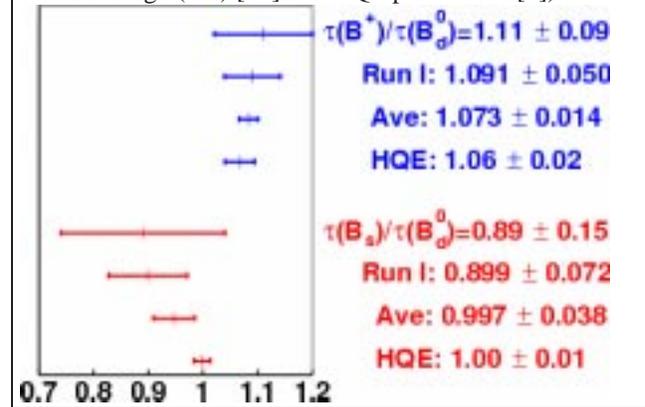
#### Inclusive $\tau_B$

Since all B hadrons can decay to  $J/\psi$ , reconstructing  $J/\psi$  vertices allows to find an average B lifetime, where the composition of the sample depends on the detector and selection criteria. Since the decay is not fully reconstructed,

Absolute Lifetimes (DØ [19] and CDF [20], Run II prelim.)

$B_u^+ \rightarrow J/\psi(\mu^+\mu^-)K^+$	DØ	$1.76 \pm 0.24(\text{stat}) \text{ ps}$
$B_u^+ \rightarrow J/\psi(\mu^+\mu^-)K^+$	CDF	$1.57 \pm 0.07 \pm 0.02 \text{ ps}$
$B_d^0 \rightarrow J/\psi(\mu^+\mu^-)K^{*0}$	CDF	$1.42 \pm 0.09 \pm 0.02 \text{ ps}$
$B_s^0 \rightarrow J/\psi(\mu^+\mu^-)\phi$	CDF	$1.26 \pm 0.20 \pm 0.02 \text{ ps}$

Lifetime Ratios (CDF [20], Run II prelim., compared with world average (ave) [17] and HQE predictions [4]):



**Table 4.** Lifetimes from  $B \rightarrow J/\psi X$  at Tevatron Run II. CDF data correspond to an integrated luminosity of  $70 \text{ pb}^{-1}$ .

the momentum of the B, which is needed to calculate the proper lifetime from  $\tau(B) = L_{xy}M(B)/(cp_t(B))$  is unknown. It can however be related to the  $J/\psi$  momentum via

$$p_t(B) = F(p_t(J/\psi)) \cdot p_t(J/\psi)$$

where  $F(p_t(J/\psi))$  is the mean ratio  $p_t(B)/p_t(J/\psi)$ , and the uncertainty on  $p_t(B)$  depends on the spread of that ratio for different momenta. Both the mean ratio and its variance are obtained from Monte Carlo. The results of such a Monte Carlo study at DØ are shown in Fig. 10. The measured average B-hadron lifetimes are

- DØ (March 03):  $\tau_B = 1.561 \pm 0.024 \pm 0.074 \text{ ps}$
- CDF (July 02):  $\tau_B = 1.526 \pm 0.034 \pm 0.035 \text{ ps}$

which is consistent with the world average of  $\tau_B = 1.573 \pm 0.007 \text{ ps}$  [17].

### 2.3.5 Semileptonic Decays With $\ell+$ IP Trigger

CDF is also using  $B \rightarrow D\ell\nu X$  and  $\Lambda_b \rightarrow \Lambda_c\ell\nu$  decays from the lepton plus displaced track trigger for lifetime measurements. The missing  $\nu$  momentum is accounted for using the same Monte Carlo-based method as in the inclusive B lifetime study discussed above. The main challenge is to correct the lifetime bias due to the impact parameter cuts in the trigger. The acceptance as a function of lifetime

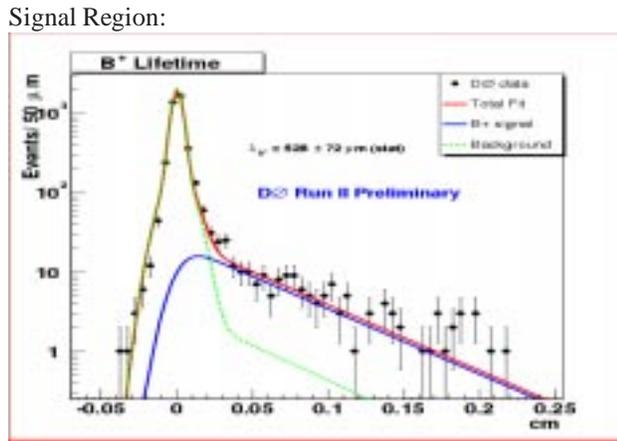
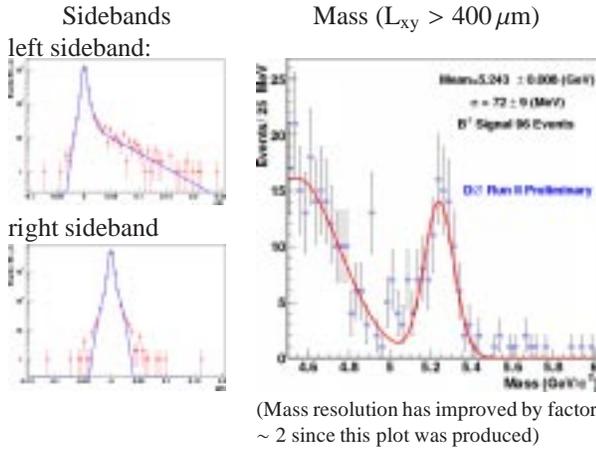


Figure 9. Life time fit at DØ

shown in Fig. 11 is found by a detailed Monte Carlo study. A fit to the  $B_s \rightarrow D_s \mu \nu$  life time distribution is shown in Fig. 12. The statistical precision achieved with the current data sample is  $\sigma_{\tau_{B^+}} = \sim 0.05$  ps,  $\sigma_{\tau_{B^0}} = \sim 0.06$  ps,  $\sigma_{\tau_{B_s}} = \sim 0.10$  ps,  $\sigma_{\tau_{\Lambda_b}} = \sim 0.13$  ps. The full results will be published as soon as the systematic errors are fully understood.

### 2.3.6 Lifetimes at the Tevatron - Summary & Prospects

The Tevatron is going to provide high statistics samples of all B-hadrons, including  $B_s, B_c, \Lambda_b$ . Preliminary Run II results from fully reconstructed hadronic decays are already approaching Run I precision, higher statistical precision is expected soon from the lepton+displaced track sample. The Run IIa projection (MC studies from Dec-01 [3]) for the life time ratios are

- $\sigma(\tau_{B_s}/\tau_{B_d^0}), \sigma(\tau_{\Lambda_b}/\tau_{B_d^0}) < 1\%$

which will provide a real test of theory for the  $B_s$  and, pending improved theoretical calculations, for the  $\Lambda_b$  lifetime.

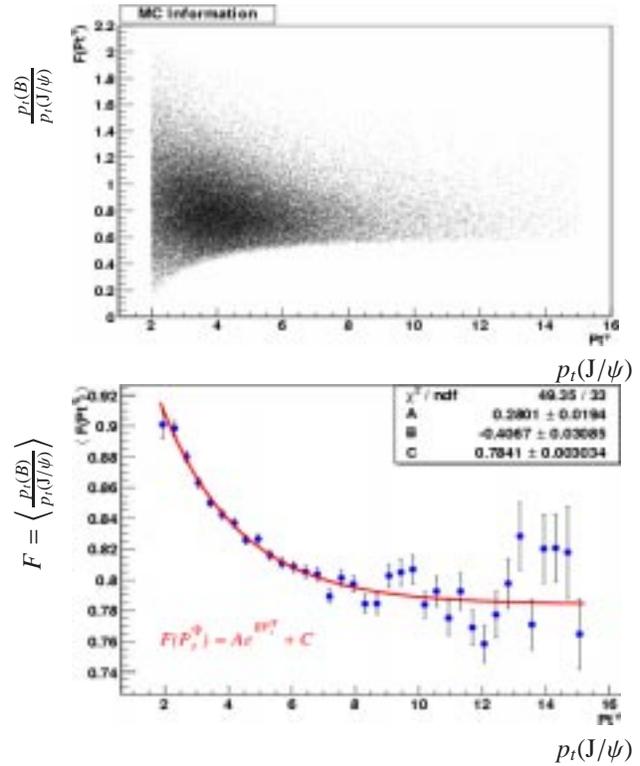


Figure 10. The F-factor (DØ)

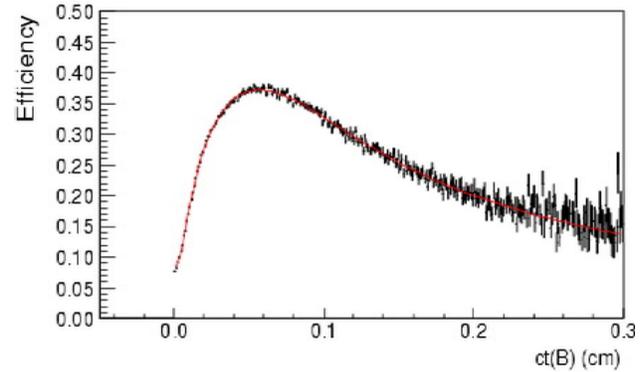


Figure 11. SVT acceptance as a function of  $ct_B$  (CDF)

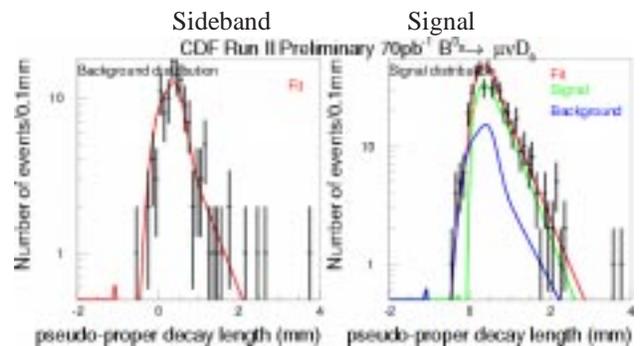


Figure 12. Fit to lifetime distribution from  $B_s \rightarrow D_s \mu \nu$

### 3 Lifetime Differences

#### 3.1 Introduction

The width difference between long and short lived CP eigenstates of the  $B_{s,d}^0 - \bar{B}_{s,d}^0$  system is predicted to be

- $\frac{\Delta\Gamma_s}{\Gamma_s} \sim \mathcal{O}(10)\%$
- $\frac{\Delta\Gamma_d}{\Gamma_d} \sim \mathcal{O}(1\%)$

$\frac{\Delta\Gamma_s}{\Gamma_s}$  is large enough to be experimentally accessible, soon. The width difference is directly proportional to the mass difference,

$$\Delta\Gamma_s = A \cdot \Delta m_s,$$

where the proportionality constant  $A$  is  $\sim 3 \cdot 10^{-3}$  in the Standard Model, but the value suffers from large hadronic uncertainties [9]. The mass difference  $\Delta m_s$ , accessible through the oscillation frequency in the  $B_s^0$  system, is itself an unknown parameter of great interest, and a major motivation for installing the precise vertex detectors at CDF and DØ during their upgrades for Run II. It is interesting to note that a large value for  $\Delta m_s$ , corresponding to fast  $B_s^0$  oscillations which are more difficult to measure, corresponds to a large value for  $\Delta\Gamma_s$ , which makes it easier to measure.  $\Delta\Gamma_s$  and  $\Delta m_s$  are complementary measurements. Given the current limits on  $\Delta m_s$ , a very small value for  $\Delta\Gamma_s$  would be a hint at new physics.

#### Theory Status

Recent theoretical predictions for  $\Delta\Gamma_d$  are (the different results are obtained using different expansions of Next-To-Leading Order QCD corrections [4]):

- $\frac{\Delta\Gamma_d}{\Gamma_d} = (2.6_{-1.6}^{+1.2}) \cdot 10^{-3}$  [7]
- $\frac{\Delta\Gamma_d}{\Gamma_d} = (3.0_{-1.4}^{+0.9}) \cdot 10^{-3}$  [4] using method in [3]

For  $\Delta\Gamma_s$ , recent predictions are:

- $\frac{\Delta\Gamma_s}{\Gamma_s} = (8.5 \pm 2.8)\%$  [4] using method in [9]
- $\frac{\Delta\Gamma_s}{\Gamma_s} = (9.0 \pm 2.8)\%$  [4] using method in [6]

#### 3.2 Strategies for Extracting $\Delta\Gamma_s$

In principle, one could simply fit two exponentials to the lifetime distribution of  $B_s^0$  decays to mixed CP states. However, since  $\frac{\Delta\Gamma_s}{\Gamma_s} \sim \mathcal{O}(10\%)$  only, this method would require very high statistics, therefore extra information is needed to separate the CP eigenstates. Possible strategies include [3]:

- Fit **lifetime** to purely CP-even  $B_s^0 \rightarrow D_s D_s$ . With certain assumptions  $B_s^0 \rightarrow D_s^{(*)} D_s^*$  is predicted to be mostly CP even, so that these decays could be included in the analysis. These assumption would have to be tested however, for example with a similar angular analysis as for the  $B_s^0 \rightarrow J/\psi\phi$  case. The result for the CP even life time can then be compared to the mean lifetime from CP-mixed channels to extract the lifetime difference.
- Fit 2 **lifetimes** to  $B_s^0 \rightarrow J/\psi\phi$ . This can have 3 angular momentum states, 2 CP even, 1 CP odd. These can be disentangled by an angular analysis.
- The **B.R.** Method: Assume that the width difference is entirely due to CP-even  $B_s^0 \rightarrow D_s^{(*)} D_s^*$ . In small velocity (Shifman-Voloshin) limit [3], [21]:

$$BR(B_s^0 \rightarrow D_s^{(*)} D_s^*) = \frac{\Delta\Gamma_s/\Gamma_s}{1 + \frac{1}{2}\Delta\Gamma_s/\Gamma_s}$$

#### 3.3 Current Values for $\Delta\Gamma$

Recent results for the width differences in the B system are

- $\frac{\Delta\Gamma_d}{\Gamma_d} < 0.18$  (95% CL) (DELPHI, 2002) [22]
- $\frac{\Delta\Gamma_s}{\Gamma_s} < 0.31$  (95% CL) (combined LEP, CDF, for  $1/\Gamma_s = \tau(B_d^0)$ , using lifetime method) [17]
- $\frac{\Delta\Gamma_s}{\Gamma_s} = 0.26_{-0.15}^{+0.30}$  (ALEPH, from B.R. method) [21]

#### 3.4 Prospects for $\Delta\Gamma$ at the Tevatron

CDF expects the following precisions on  $\Delta\Gamma_s$  by the end of Run IIa, from  $2 \text{ fb}^{-1}$ . The projections assume  $\frac{\Delta\Gamma_s}{\Gamma_s} = 15\%$  and are those given in [3] in December 2001. They refer to the statistical error only.

- From  $B_s \rightarrow J/\psi\phi$ :  $\sigma_{\text{stat}}(\frac{\Delta\Gamma_s}{\Gamma_s}) \sim 5\%$
- $B_s \rightarrow D_s D_s$  (no  $D_s^*$ ):  $\sigma_{\text{stat}}(\frac{\Delta\Gamma_s}{\Gamma_s}) \sim 6\%$
- $B_s \rightarrow D_s^{(*)} D_s^*$ :  $\sigma_{\text{stat}}(\frac{\Delta\Gamma_s}{\Gamma_s}) \sim 2.5\%$  (assume decay 100% CP even)
- B.R. method:  $\sigma_{\text{stat}}(\frac{\Delta\Gamma_s}{\Gamma_s}) \sim 1\%$  (model dependent)

Assuming a similar performance for  $B_s \rightarrow J/\psi\phi$  at DØ we arrive at a total statistical uncertainty at the Tevatron for  $2 \text{ fb}^{-1}$  of  $\sigma_{\text{stat}}(\frac{\Delta\Gamma_s}{\Gamma_s}) \sim 2\%$ , ignoring the B.R. method. A more conservative estimate of  $\sigma_{\text{stat}}(\frac{\Delta\Gamma_s}{\Gamma_s}) \sim 3\%$  is obtained if the assumption that  $B_s \rightarrow D_s^{(*)} D_s^*$  decays are 100% CP even is dropped and decays involving  $D_s^*$  are completely ignored.

## 4 Conclusion

### Lifetime ratios

Since they have started data taking, the B-factories have brought the error on  $\sigma(\tau_{B^+}/\tau_{B_d^0})$  down to 1.7%, so that the experimental accuracy for this ratio is now better than that of the HQE prediction. The agreement between theory and experiment is very good. Further improvements on  $\sigma(\tau_{B^+}/\tau_{B_d^0})$  can be expected from B-factories and Tevatron, soon.

Large numbers of  $B_s^0$  and  $\Lambda_b$  are currently being produced at the Tevatron. The uncertainty on the lifetime ratios  $\sigma(\tau_{B_s}/\tau_{B_d^0})$ ,  $\sigma(\tau_{\Lambda_b}/\tau_{B_d^0})$  is expected to be below 1% by the end of Run IIa. This will provide a real test of HQE for  $B_s$  for which precise predictions exist, while improved theoretical values are needed for  $\Lambda_b$ .

### Lifetime Differences

$\Delta\Gamma_s$  and  $\Delta m_s$  are complementary measurements, and both parameters combined are sensitive to New Physics contributions to  $B_s^0$  mixing. Recent calculations predict  $\frac{\Delta\Gamma_s}{\Gamma_s} = 9 \pm 3\%$  [4].

From data we get the following limit on the lifetime difference in the  $B_s$  system:  $\frac{\Delta\Gamma_s}{\Gamma_s} < 0.31$  (95% CL) [17]. First steps have been taken towards a  $\frac{\Delta\Gamma_s}{\Gamma_s}$  measurement at the Tevatron, where  $55 \pm 9$   $B_s \rightarrow J/\psi\phi$  events have been reconstructed at CDF, and an average  $B_s$  lifetime has been extracted from that decay. By the end of Run IIa a measurement of  $\frac{\Delta\Gamma_s}{\Gamma_s}$  with a statistical uncertainty of  $\sim 2\%$  is expected.

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