



Measurement of the ratio of differential cross sections for W and Z boson production as a function of transverse momentum in $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV

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We report on a measurement of the ratio of the differential cross sections for W and Z boson production as a function of transverse momentum in proton-antiproton collisions at $\sqrt{s} = 1.8$ TeV. The evaluation of the ratio of cross sections leads to reduced uncertainties for both the data and the theoretical predictions.

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I. INTRODUCTION

The DØ Collaboration has recently published [1,2] measurements of differential cross sections for W and Z boson production as a function of transverse momentum (p_T). Both measurements are in good agreement with combined resummed and perturbative QCD models, such as those in Refs. [3–5]. For the analyses of data taken during 1992–1996 (Fermilab Tevatron Run 1), we have used the resummed calculation of Ref. [4] fitted to our observed $Z \rightarrow e^+e^-$ differential cross section to extract the non-perturbative phenomenological parameters of the theory. The resummed calculation was then used to predict W boson observables such as the electron and neutrino transverse momenta and as input to a Monte Carlo model of W boson production and decay, which we used to extract the mass [6] and production cross section [7] of the W boson.

Ref. [8] proposes an alternative method of predicting W boson observables from measured Z boson quantities. This is based on the theoretical ratio of the W to Z boson differential cross sections with respect to variables that have been scaled by their corresponding vector boson masses. Because production properties of W and Z bosons are very similar, the large radiative corrections that affect the individual distributions cancel in the ratio. The ratio can therefore be calculated reliably using perturbative QCD (pQCD), with no need for resummation, even at small values of the transverse momenta of the vector bosons, for which the radiative corrections factorize from the hard process and therefore cancel in the ratio. The theoretical uncertainties stemming from the perturbative expansion are consequently well understood, and are smallest at very low p_T .

The basic proposal of Ref. [8] is to use pQCD calculations and the measured Z boson observables to extract the W boson observables. We will test the method using the W and Z boson differential cross sections as a function of transverse momentum. The main difference between the production properties of the W and the Z bosons arises from the difference in their masses. We will therefore introduce variables that are scaled by the corresponding vector boson mass M_V .

The ratio of differential cross sections for the scaled W and Z boson transverse momenta p_T^W/M_W and p_T^Z/M_Z is defined as

$$R_{p_T} = \left[\frac{d\sigma^W}{d(p_T^W/M_W)} \right] / \left[\frac{d\sigma^Z}{d(p_T^Z/M_Z)} \right], \quad (1)$$

where $d\sigma^V/dp_T^V$ is the standard differential cross section for vector boson production $\sigma(p\bar{p} \rightarrow V + X)$ as a function of transverse momentum p_T^V . Equation 1 can be used to predict the differential cross section for W bosons with respect to the non-scaled transverse momentum [8]:

$$\left. \frac{d\sigma^W}{dp_T^W} \right|_{\text{predicted}} = \frac{M_Z}{M_W} \times R_{p_T} \times \left. \frac{d\sigma^Z}{dp_T^Z} \right|_{\text{measured}}^{p_T^Z = \frac{M_Z}{M_W} p_T^W}, \quad (2)$$

where R_{p_T} is calculated using pQCD. In this paper, we present the first measurement of R_{p_T} , and compare it to the calculation of Ref. [8]. We then use our measured differential Z boson cross section in Eq. 2, and R_{p_T} from Ref. [8], to obtain the differential W boson cross section and compare it to our published result [1].

Compared to the standard method used previously to extract W boson observables, the present method reduces both theoretical and experimental systematic uncertainties. However, it introduces a statistical contribution to the uncertainty from the number of events in the Z boson candidate sample. Such a trade-off will eventually result in smaller overall uncertainties, especially when used with the high statistics samples expected from Run 2 of the Tevatron.

II. DATA SELECTION

We keep modifications to the published $D\bar{O}$ analyses [1,2] to a minimum, but, at the same time, we try to cancel as many experimental uncertainties as possible in measuring R_{p_T} . The uncertainty in the integrated luminosity of the data samples (4.3%) is the dominant uncertainty in the individual cross sections. It cancels completely when taking the ratio, as long as the same data sets are used to select the final W and Z boson candidate samples. In this analysis, we keep the event selections and corrections for background, efficiency, acceptance, and detector resolutions identical to those in the published results [1,2], but require total overlap in the data-taking runs for the W and Z boson event samples. In addition, we exclude events at collision times with large beam losses from the Main Ring accelerator [7]. These beam losses can create significant energy deposits in the calorimeter that produce events with large false transverse momentum imbalance that could pass our W boson selection criteria. Due to these additional requirements, the Z boson sample was reduced from 6407 to 4881 events. About half of the events were lost due to tightening of beam quality conditions, and half because the W trigger was not available or was prescaled. The W sample was reduced from 50488 to 50264 events when we removed runs for which the W trigger was prescaled. The final integrated luminosity for both samples is $(84.5 \pm 3.6)\text{pb}^{-1}$.

We have investigated whether additional sources of error could be cancelled in the ratio. There are four sources of systematic error that contribute to the W and Z boson cross sections. These arise from uncertainties in the background estimate, the event selection efficiency, and the unfolding procedure used to correct for acceptance and detector resolution.

The dominant sources of background in both the W and the Z boson analyses are from multijet and photon-jet events, where the jets pass our electron identification criteria. In the case of the W , a large imbalance in the transverse energy has to arise to mimic the presence of a neutrino. The way multijet or photon-jet events mimic W or Z boson events is quite different, and the methods used to estimate background are independent. We therefore cannot cancel any contribution to the error in the ratio arising from background estimates.

Acceptance and unfolding corrections are applied using a parameterized Monte Carlo [6]. The main contribution to the error is from the modeling of the detector. For the W analysis, we rely completely on the measurement of the energy of the recoiling hadrons, whereas for the Z boson measurement we use the electromagnetic energy deposited by the electrons. We therefore do not benefit from cancellation of errors in the acceptance/unfolding procedure.

The uncertainty in the efficiency has contributions from the trigger and offline electron identification. The Level 0 trigger, which requires the detection of an inelastic collision via simultaneous hits in the forward and backward Level 0 scintillation detectors [9], is common for W and Z boson events. The uncertainty in this trigger therefore cancels completely in the ratio. However, its contribution to the error in the efficiency is negligible (0.5% out of a total of 3.5%).

Although the triggers and the offline electron identification criteria used in the W and Z boson analyses are different, the main contribution (3%) to the error in the efficiency comes from a common source, the so-called u_{\parallel} efficiency [6]. This inefficiency arises when the energy flow close to the electron increases as recoiling hadrons approach the electron. It is therefore a topological effect produced by the proximity of the electron to the jet, and has the largest effect at a boson transverse momentum of about 20 GeV [2]. The u_{\parallel} efficiency is calculated on an electron-by-electron basis using the parameterized Monte Carlo. The error in the u_{\parallel} efficiency is estimated from W and Z boson events, generated in HERWIG [11], and overlaid with data taken from randomly selected $p\bar{p}$ collisions. Because this inefficiency depends on the proximity of electrons to jets, it is difficult to estimate how much of the uncertainty in the u_{\parallel} efficiency cancels in the ratio. To determine if further investigation of any possible cancellation of the uncertainty in u_{\parallel} efficiency was warranted, we estimated the effect on R_{p_T} of a complete cancellation of the contribution from the uncertainty in u_{\parallel} efficiency. This produced a maximum reduction of uncertainty in R_{p_T} of less than 5%. We therefore concluded that no cancellations beyond the uncertainty in the luminosity would improve significantly the measurement of R_{p_T} .

III. SCALED W AND Z BOSON CROSS SECTIONS

Equation 1 can be written

$$R_{p_T}^{\text{th}} = \left(\frac{d\sigma^W}{dp_T^W} \right) / \left(\frac{d\sigma^Z}{d(p_T^Z \times M_W/M_Z)} \right), \quad (3)$$

where we use the mass ratio from the Review of Particle Physics [10]

$$\frac{M_W}{M_Z} = 0.8820 \pm 0.0005. \quad (4)$$

In order to measure the scaled distributions without changing the p_T -binning of both the W and Z boson analyses, we keep the W bin boundaries (δ_i) identical to the ones in our published work, but because we require the same bin widths in the scaled variables p_T^W/M_W and p_T^Z/M_Z , we set the bin boundaries in the differential Z boson cross section to $\delta_i/0.8820$, and recompute the differential Z boson cross section accordingly.

Table I shows the modified results for the W and Z boson cross sections, with the statistical and systematic contributions to the uncertainties shown separately. It is clear that the error in the ratio is dominated by the systematic uncertainty in the W cross section.

IV. MEASUREMENT OF R_{p_T}

Based on the measured W and Z boson differential cross sections listed in Table I, we extract the ratio of scaled cross sections

$$R_{p_T}^{\text{exp}} = \left[\left(\frac{d\sigma^W}{dp_T^W} \right) / \left(\frac{d\sigma^Z}{dp_T^Z} \right) \right] \times \frac{M_W}{M_Z} \times \frac{B(Z \rightarrow ee)}{B(W \rightarrow e\nu)}. \quad (5)$$

It should be recognized that the prediction for R_{p_T} [8] was calculated for the ratio of the scaled W and Z boson differential cross sections $d\sigma^V/dp_T^V$, but we measure the differential cross sections multiplied by their branching fractions to electrons ($d\sigma^V/dp_T^V$) \times $B(V \rightarrow e)$. We therefore must multiply our measurement by the ratio of the Z to W boson branching fractions, which we also obtain from the Review of Particle Physics [10]:

$$B(Z \rightarrow ee) = 0.03367 \pm 0.00005 \quad (6)$$

$$B(W \rightarrow e\nu) = 0.1066 \pm 0.0020. \quad (7)$$

The result is shown in Fig. 1, and summarized in Table II. The data are plotted at the value of p_T for which the theoretical prediction for R_{p_T} is equal to its average in the bin, following the prescription of Ref. [12]. The only uncertainty included in the theoretical prediction is the one arising from the Monte Carlo integration. We observe that the measured R_{p_T} agrees with the pQCD prediction [8]: the χ^2 for the comparison between data and theory is 18.7 for 21 degrees of freedom (60% probability). If we only consider the results in the first 12 bins, the χ^2 is 13.3 for 11 degrees of freedom, which corresponds to a probability of 27%.

V. EXTRACTION OF $d\sigma^W/dp_T^W$

Based on Eq. 2, we use the calculated ratio R_{p_T} from Ref. [8], together with the measured $d\sigma^Z/dp_T^Z$, to predict the W boson transverse momentum spectrum, and compare it with our previously measured $d\sigma^W/dp_T^W$ [1]. The result is shown in Fig. 2. The measured differential cross section is plotted at the center of the bin. The upper and lower 68% confidence level limits for the prediction are plotted as histograms. The extracted transverse momentum distribution agrees well with the measurement: the Kolmogorov-Smirnov probability [13] κ is equal to 1.

VI. CONCLUSIONS

We have measured the ratio of scaled differential cross sections R_{p_T} for W and Z boson production, and compared it to a purely pQCD prediction. We observe good agreement between data and theory over the entire p_T spectrum. Using the theoretical prediction for R_{p_T} , together with our measurement of the differential Z boson production cross section, we also extracted the differential cross section for W production. This prediction agrees with our published result. From this first study of the new method of Ref. [8] for predicting W boson properties, we conclude that it should eventually lead to smaller overall uncertainties on the measured mass and width of the W boson, compared to current methods used at hadron colliders, once the high statistics samples of Z boson events expected from Run 2 at the Tevatron become available.

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TABLE I. Summary of the measured W and Z boson differential production cross sections as a function of transverse momentum used to calculate the ratio. The error in the ratio is dominated by the systematic error in the W cross section.

p_T Bin (GeV)	$\frac{d\sigma(W \rightarrow e\nu)}{dp_T^W}$ (pb/GeV)	Stat Error (pb/GeV)	Syst Error (pb/GeV)	$\frac{d\sigma(Z \rightarrow e^+e^-)}{dp_T^Z}$ (pb/GeV)	Stat Error (pb/GeV)	Syst Error (pb/GeV)
0-2	109.48	4.61	12.35	11.94	0.53	0.35
2-4	206.21	6.85	24.64	19.63	0.65	0.57
4-6	171.32	5.65	9.29	14.34	0.53	0.44
6-8	133.60	4.65	9.46	11.19	0.48	0.36
8-10	103.48	4.04	6.95	8.05	0.41	0.27
10-12	77.46	3.46	7.25	6.18	0.37	0.21
12-14	63.58	3.20	4.16	4.74	0.33	0.15
14-16	47.77	2.77	4.29	3.39	0.28	0.11
16-18	37.67	2.42	2.73	3.27	0.28	0.17
18-20	30.50	2.20	1.74	1.94	0.22	0.11
20-25	22.02	1.23	1.22	1.59	0.12	0.08
25-30	13.94	0.93	1.07	0.946	0.097	0.051
30-35	9.51	0.73	0.84	0.848	0.092	0.043
35-40	6.79	0.63	0.51	0.435	0.066	0.022
40-50	3.96	0.37	0.31	0.325	0.040	0.016
50-60	1.82	0.25	0.25	0.180	0.029	0.009
60-70	1.14	0.20	0.23	0.0848	0.0197	0.0045
70-80	0.749	0.178	0.170	0.0385	0.0129	0.0020
80-100	0.310	0.059	0.088	0.0141	0.0054	0.0008
100-120	0.0822	0.0287	0.0255	0.00764	0.00383	0.00032
120-160	0.0433	0.0119	0.0118	0.00358	0.00180	0.00018
160-200	0.00769	0.00545	0.00482	0.00163	0.00111	0.00010

TABLE II. Measured R_{p_T} . The uncertainty in the luminosity for the W and Z samples cancels completely when taking the ratio.

p_T Bin (GeV)	p_T (GeV)	R_{p_T}	Total Error
0-2	1.21	2.555	0.340
2-4	2.81	2.927	0.388
4-6	4.83	3.327	0.273
6-8	6.84	3.326	0.323
8-10	8.85	3.580	0.360
10-12	10.86	3.494	0.439
12-14	12.87	3.739	0.426
14-16	14.88	3.921	0.550
16-18	16.89	3.208	0.450
18-20	18.90	4.380	0.683
20-25	22.52	3.854	0.479
25-30	27.34	4.105	0.640
30-35	32.57	3.125	0.529
35-40	37.89	4.348	0.875
40-50	45.03	3.395	0.615
50-60	55.09	2.814	0.727
60-70	65.14	3.731	1.342
70-80	74.79	5.419	2.566
80-100	89.67	6.140	3.160
100-120	109.77	2.995	2.060
120-160	139.93	3.374	2.151
160-200	180.14	1.317	1.539

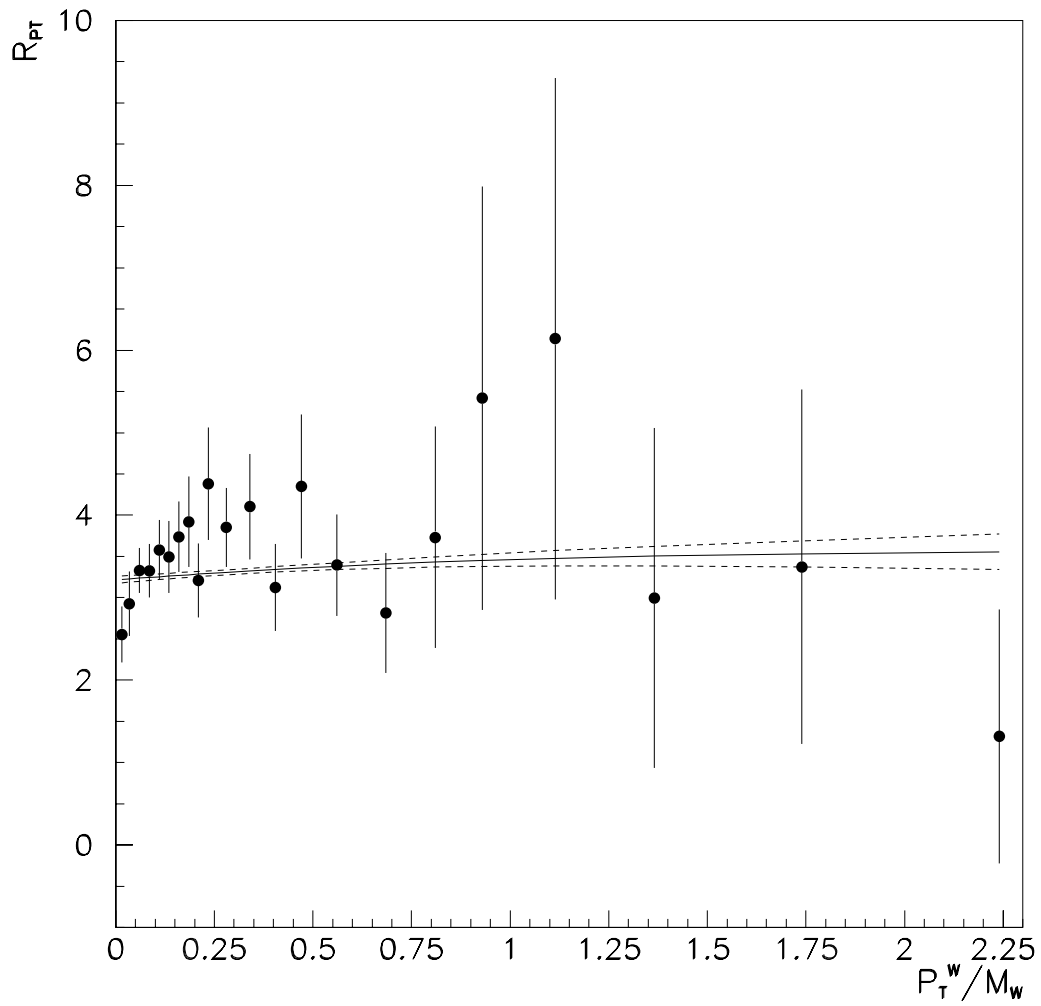


FIG. 1. Ratio of scaled differential cross sections R_{p_T} for W and Z production. The solid line is the order α_S^2 theoretical prediction of Ref. [8], and the dotted lines are the one standard deviation uncertainties due to Monte Carlo integration. The error in the luminosity cancels completely in the ratio of the measured cross sections.

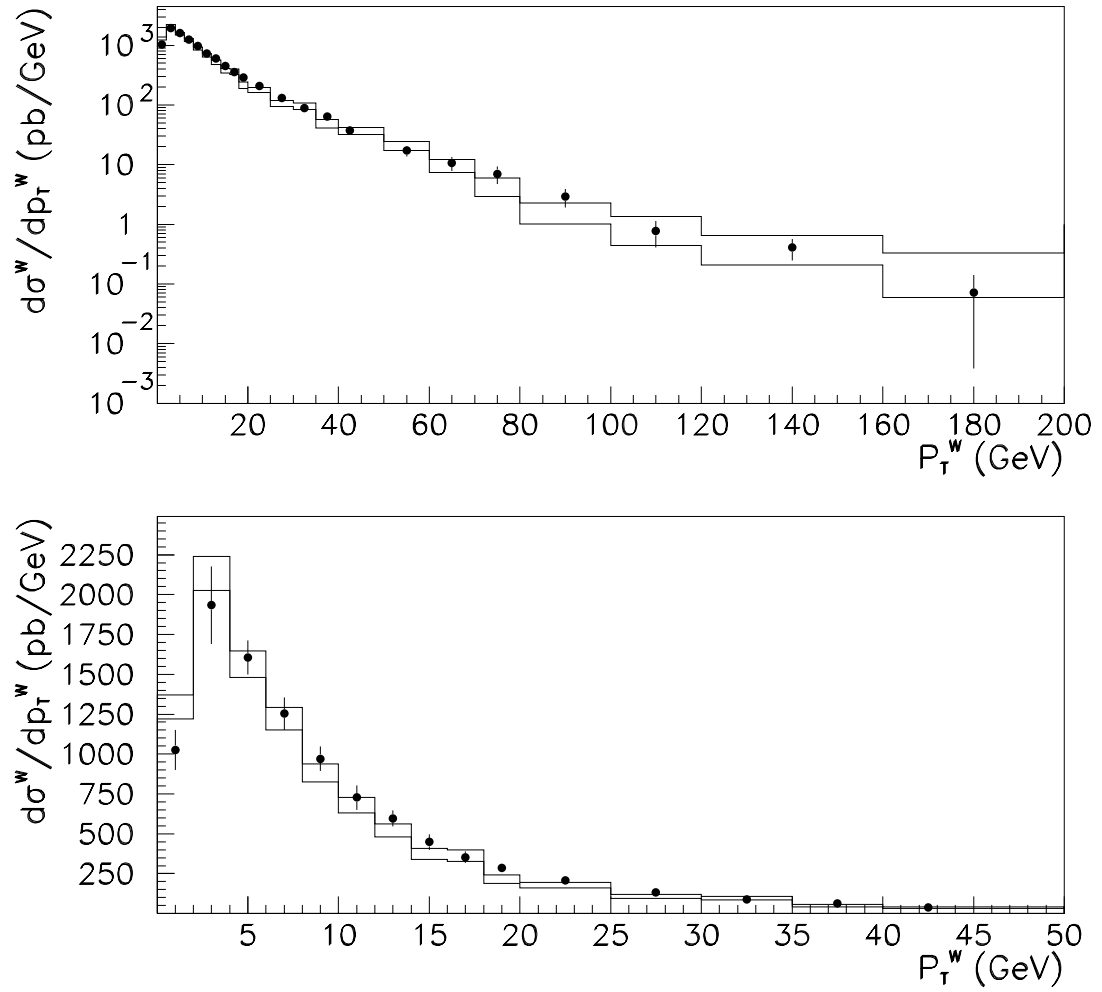


FIG. 2. Differential cross section for W boson production as a function of p_T^W shown for the entire p_T^W range (upper plot) and the low p_T^W region (lower plot). The points are the $D\bar{O}$ data; the error bars do not include the 4.3% error in the luminosity. The histograms represent the upper and lower 68% confidence level limits of the prediction [8] obtained from the ratio method.