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**CDF**

## **Measurement of the CP Asymmetry Parameter $\sin(2\beta)$ at CDF**

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# MEASUREMENT OF THE CP ASYMMETRY PARAMETER $\sin(2\beta)$ AT CDF

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We present a measurement of the time-dependent asymmetry in the rate for  $\overline{B}_d^0$  versus  $B_d^0$  decays to  $J/\psi K_S^0$ . In the context of the Standard Model this is interpreted as a measurement of the  $CP$ -violation parameter  $\sin(2\beta)$ . A total of  $198 \pm 17$   $B_d^0/\overline{B}_d^0$  decays were observed in  $p\overline{p}$  collisions at  $\sqrt{s} = 1.8$  TeV by the CDF detector at the Fermilab Tevatron. The initial  $b$ -flavor is determined by a same side flavor tagging technique. Our analysis results in  $\sin(2\beta) = 1.8 \pm 1.1(\text{stat}) \pm 0.3(\text{syst})$ .

## 1 Introduction

The origin of Charge-Conjugation-Parity ( $CP$ ) non-conservation in weak interactions has been an outstanding question in physics since its unexpected discovery in  $K_L^0 \rightarrow \pi^+\pi^-$  decays in 1964<sup>1</sup>. The favored mechanism for explaining  $CP$  violation is through the relationship between the weak interaction and the mass eigenstates of quarks, which is described in the Standard Model (SM) by the Cabibbo-Kobayashi-Maskawa (CKM) mixing matrix<sup>2</sup>. With the addition of the third generation of quarks, top and bottom, this matrix gains a physical complex phase capable of explaining  $CP$  violation.

After more than three decades, the  $K^0$  remains the only system where  $CP$  violation has been observed. Searches for  $CP$  violation have recently been extended to inclusive  $B$  meson decays. However, the effects are expected to be small ( $\sim 10^{-3}$ ), and no measurement has had the precision to reveal an effect<sup>3</sup>.

$CP$  violation is expected to have a large effect in the relative decay rate of  $B_d^0$  and  $\overline{B}_d^0$  to the  $CP$  eigenstate  $J/\psi K_S^0$ <sup>4</sup>. The interference of direct decays ( $B_d^0 \rightarrow J/\psi K_S^0$ ) vs. those that have undergone mixing ( $B_d^0 \rightarrow \overline{B}_d^0 \rightarrow J/\psi K_S^0$ ) gives rise to a decay asymmetry

$$\mathcal{A}_{CP}(t) \equiv \frac{\overline{B}_d^0(t) - B_d^0(t)}{\overline{B}_d^0(t) + B_d^0(t)} = \sin(2\beta) \sin(\Delta m_d t), \quad (1)$$

where  $B_d^0(t)$  ( $\overline{B}_d^0(t)$ ) is the number of decays to  $J/\psi K_S^0$  at proper time  $t$  given that the produced meson (at  $t = 0$ ) was a  $B_d^0$  ( $\overline{B}_d^0$ ). The  $CP$  phase difference between the two decay paths appears via the factor  $\sin(2\beta)$ , and the flavor oscillation through the mass difference  $\Delta m_d$  between the two  $B_d^0$  mass eigenstates. Within the SM, constraints on the CKM matrix imply  $0.30 \leq \sin(2\beta) \leq 0.88$  at 95% C.L. <sup>5</sup>. Using a  $J/\psi K_S^0$  sample, the OPAL Collaboration has recently reported  $\sin(2\beta) = 3.2_{-2.0}^{+1.8} \pm 0.5$  <sup>6</sup>.

Here we report on an analysis using  $B_d^0/\overline{B}_d^0 \rightarrow J/\psi K_S^0$  decays extracted from a  $110 \text{ pb}^{-1}$  data sample of  $p\overline{p}$  collisions at  $\sqrt{s} = 1.8 \text{ TeV}$  collected in 1992-96 by the CDF detector at the Fermilab Tevatron collider. A description of the CDF detector may be found in Refs. 7,8.

## 2 Event Selection

The  $B_d^0/\overline{B}_d^0 \rightarrow J/\psi K_S^0$  sample selection closely parallels Ref. 9. The  $J/\psi$  is reconstructed via the  $\mu^+\mu^-$  mode. Both muons must be measured by our silicon vertex detector (SVX) <sup>8</sup>, thereby providing a precise decay length measurement.  $K_S^0$  candidates are sought by fitting pairs of oppositely charged tracks, assumed to be pions, to the  $K_S^0 \rightarrow \pi^+\pi^-$  hypothesis. The  $J/\psi$  and  $K_S^0$  daughter tracks are combined in a four particle fit assuming they arise from  $B_d^0/\overline{B}_d^0 \rightarrow J/\psi K_S^0$ : the  $\mu^+\mu^-$  and  $\pi^+\pi^-$  are constrained to their parents' world average masses and separate decay vertices, and the  $K_S^0$ ,  $J/\psi$ , and  $B$  are constrained to point back to their points of origin. A  $B$  candidate is accepted if its transverse momentum with respect to the beam line  $p_T(B)$  is greater than  $4.5 \text{ GeV}/c$ , and if the  $K_S^0$  candidate has  $p_T(K_S^0) > 0.7 \text{ GeV}/c$  and a decay vertex significantly displaced from the  $J/\psi$  vertex. Fit quality criteria are also applied.

We define  $M_N \equiv (M_{FIT} - M_0)/\sigma_{FIT}$ , where  $M_{FIT}$  is the mass of the  $B$  candidate from the fit described above,  $\sigma_{FIT}$  is its uncertainty (typically  $\sim 9 \text{ MeV}/c^2$ ), and  $M_0$  is the central value of the  $B_d^0$  mass peak. The decay length of the  $B$  is used to calculate its proper decay length  $ct$ , which includes the sign from the scalar product of the transverse components of the vectors for the  $B$  decay vertex displacement from the  $p\overline{p}$  interaction vertex and the  $B$  momentum. The normalized masses  $M_N$  for the accepted candidates with  $ct > 0$  are shown in Fig. 1a along with the results of the likelihood fit described later. The fit yields (for all  $ct$ )  $198 \pm 17 B_d^0/\overline{B}_d^0$  mesons.

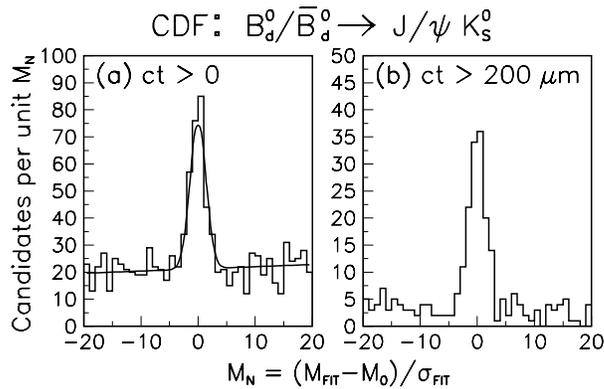


Figure 1: The normalized mass distribution of the  $J/\psi K_S^0$  candidates with  $ct > 0$  and  $200 \mu\text{m}$ . The curve is the Gaussian signal plus linear background from the likelihood fit (see text).

### 3 Flavor Identification

Measuring  $\mathcal{A}_{CP}(t)$  is predicated upon knowing whether the production “flavor” of the meson was  $B_d^0$  or  $\bar{B}_d^0$ . We determine this by a same side tagging (SST) method which relies upon the correlation between the  $B$  flavor and the charge of a nearby particle. Such a correlation can arise from the fragmentation processes which form a  $B$  meson from a  $\bar{b}$  quark, as well as from the pion from the decay of  $B^{**}$  mesons<sup>10</sup>. In both cases a  $B_d^0$  is preferentially associated with a positive particle, and a  $\bar{B}_d^0$  with a negative one. The effectiveness of this method has been demonstrated by tagging  $B \rightarrow \nu \ell D^{(*)}$  decays and observing the time dependence of the  $B_d^0$ - $\bar{B}_d^0$  oscillation and measuring  $\Delta m_d$ . (Fig. 2) We have also measured the amplitude of the oscillation (*i.e.*, the strength of the correlation) in a lower-statistics  $B_d^0 \rightarrow J/\psi K^{*0}$  sample and found it to be consistent with the  $\nu \ell D^{(*)}$  data<sup>9,11</sup>.

Our SST method, following Ref. 11, selects a single charged particle as a flavor tag from those within an  $\eta$ - $\phi$  cone of half-angle 0.7 around the  $B$  direction, where  $\eta \equiv -\ln[\tan(\theta/2)]$  is the pseudorapidity,  $\theta$  is the polar angle relative to the outgoing proton beam direction, and  $\phi$  is the azimuthal angle around the beam line. The tag must have  $p_T > 400 \text{ MeV}/c$  and come from the  $p\bar{p}$  interaction vertex (*i.e.*, have a transverse impact parameter within 3 standard deviations of the interaction vertex). If there is more than one candidate, the one with the smallest  $p_T^{rel}$  is selected as *the* flavor tag, where the  $p_T^{rel}$  of a particle is the component of its momentum transverse to the

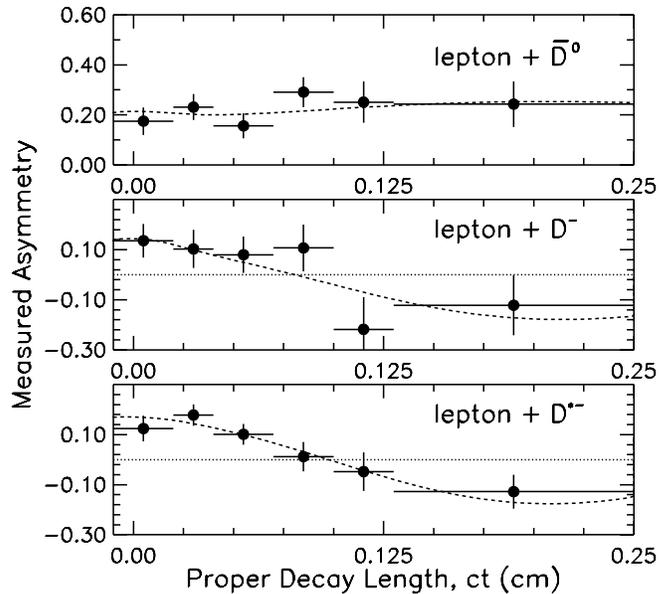


Figure 2:  $B$  Meson oscillations. The top sample is composed primarily of charged  $B$ 's. Only a small modulation due to mixing is visible. The bottom two samples are composed predominantly of neutral  $B$ 's; the asymmetry modulation due to flavor mixing is correspondingly larger.

momentum of the combined  $B$ +particle system.

#### 4 Measuring the $J/\psi + K_s^0$ Asymmetry

We apply the SST method to the  $J/\psi K_s^0$  sample. The tagging efficiency is  $\sim 65\%$ . The breakdown of tags is given in Table 1 in proper time bins. We call  $|M_N| < 3$  the “signal region” and  $3 < |M_N| < 20$  the “sidebands.” Since negative (positive) tags are associated with  $\bar{B}_d^0$ 's ( $B_d^0$ 's), we form the asymmetry

$$\mathcal{A}(ct) \equiv \frac{N^-(ct) - N^+(ct)}{N^-(ct) + N^+(ct)} \quad (2)$$

Table 1: Tags for the  $J/\psi K_S^0$  candidates in proper decay length ( $ct$ ) bins. The signal region is  $|M_N| < 3$ , and the sidebands are  $3 < |M_N| < 20$ . The “+,” “-,” and “0” headings are for positive, negative, and untagged events. The last column is the sideband-subtracted tagging asymmetry [Eq. (2)]. The asymmetry for the background-dominated first row is not quoted because there is not a tagged, sideband-subtracted excess.

$ct$ ( $\mu\text{m}$ )	Signal			Sidebands			Asymmetry (%)
	-	+	0	-	+	0	
-200 - 0	42	21	43	167	193	174	—
0 - 100	53	48	49	156	175	205	$20 \pm 25$
100 - 200	14	14	15	26	34	24	$8 \pm 32$
200 - 400	12	18	19	17	22	10	$-22 \pm 24$
400 - 800	26	13	22	11	18	11	$42 \pm 18$
800 - 1400	6	4	9	6	6	2	$25 \pm 40$
1400 - 2000	3	1	1	0	0	2	$50 \pm 43$

analogous to Eq. (1), where  $N^\pm(ct)$  are the numbers of positive and negative tags in a given  $ct$  bin. The signal events generally have a positive asymmetry (*i.e.*, favoring negative tags) at large  $ct$ . The sidebands show a consistent negative asymmetry (positive tags), but this has a small effect in the sideband-subtracted asymmetry at larger  $ct$ , where the signal purity is high (see Fig. 1b).

The sideband-subtracted asymmetries of Table 1 are displayed in Fig. 3 along with a  $\chi^2$  fit (dashed curve) to  $\mathcal{A}_0 \sin(\Delta m_d t)$ , where  $\Delta m_d$  is fixed to  $0.474 \text{ ps}^{-1}$ . The amplitude,  $\mathcal{A}_0 = 0.36 \pm 0.19$ , measures  $\sin(2\beta)$  attenuated by a “dilution factor”  $\mathcal{D}_0 \equiv 2\mathcal{P}_0 - 1$ , where  $\mathcal{P}_0$  is the probability that the tag correctly identifies the  $B_d^0$  flavor. The determination of  $\mathcal{A}_0$  is dominated by the asymmetries at larger  $ct$ ’s due to the  $\sin(\Delta m_d t)$  shape; this is also where the background is very low.

We refine the fit using an unbinned maximum likelihood fit based on Ref. 9. This fit makes optimal use of the low statistics by fitting signal and background distributions in  $M_N$  and  $ct$ , including sideband and  $ct < 0$  events which help constrain the background. The likelihood fit also incorporates resolution effects and corrections for systematic biases, such as the inherent charge asymmetry favoring positive tracks resulting from the wire plane orientation in the main drift chamber.

We measure the intrinsic charge asymmetry of the tagging in a large inclusive (unflavored)  $J/\psi$  sample with displaced decay vertices ( $> 90\%$   $b$  hadrons) and parameterize its dependence on track  $p_T$  and event occupancy. The occupancy dependence is weak. At 400 MeV/ $c$ , the SST  $p_T$  threshold, the asym-

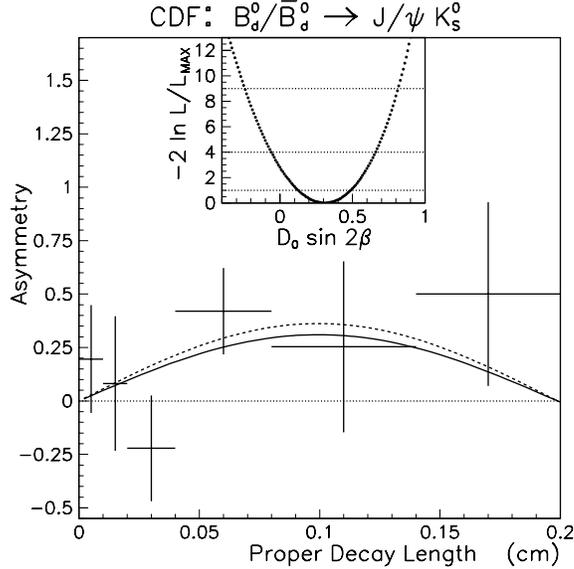


Figure 3: The sideband-subtracted tagging asymmetry as a function of the reconstructed  $J/\psi K_S^0$  proper decay length (points). The dashed curve is the result of a simple  $\chi^2$  fit to  $\mathcal{A}_0 \sin(\Delta m_d t)$ . The solid curve is the likelihood fit result, and the inset shows a scan through the log-likelihood function as  $\mathcal{D}_0 \sin(2\beta)$  is varied about the best fit value.

metry is  $5.6 \pm 1.1\%$ , falling as  $p_T^{-4}$  to  $0.14 \pm 0.86\%$  at high  $p_T$  (the average tag asymmetry in the  $J/\psi$  sample is  $1.6 \pm 0.7\%$ ), all favoring positive tags. This correction is applied to the signal in the likelihood fit; the charge asymmetry of the  $J/\psi K_S^0$  background is measured independently by the fit itself.

The solid curve in Fig. 3 is the result of the likelihood fit, which gives  $\mathcal{D}_0 \sin(2\beta) = 0.31 \pm 0.18$ . As expected, the two fits give similar results, indicating that our result is dominated by the sample size and that the corrections and improvements of the likelihood fit introduce no dramatic effects. Also shown in the Fig. 3 inset is the relative log-likelihood as a function of  $\mathcal{D}_0 \sin(2\beta)$ ; the shape is parabolic, indicating Gaussian errors.

As noted above, the sidebands favor positive tags. The maximized likelihood ascribes an asymmetry of  $16.7 \pm 8.2\%$ , or an  $\sim 2\sigma$  excess of positive tags, to the long-lived backgrounds (*e.g.*,  $B \rightarrow J/\psi X$  with an unassociated  $K_S^0$ ). Prompt background (consistent with  $ct$ -resolution) has an asymmetry of  $0.6 \pm 4.5\%$  favoring negative tags.

## 5 Systematic Uncertainties

Systematic effects from  $B$  backgrounds have been considered. For instance, the decay  $B_d^0 \rightarrow J/\psi K^{*0}$ ,  $K^{*0} \rightarrow K_S^0 \pi^0$ , where we do not reconstruct the  $\pi^0$ , has a negligible effect on the result. Background asymmetries were also studied in  $J/\psi K^+$  and  $J/\psi K^{*0}$  modes<sup>9</sup>. No systematic pattern emerged. Since no other biases have been found aside from the above small effects, we attribute the background asymmetry largely to statistical fluctuations. Again, the effect of these asymmetries is small as the total background fraction is small at large  $ct$  (see Fig. 1b) where  $\sin(\Delta m_d t)$  is large.

We determine the systematic uncertainty on  $\mathcal{D}_0 \sin(2\beta)$  by shifting the central value of each fixed input parameter to the fit by  $\pm 1\sigma$  and refitting to find the shift in  $\mathcal{D}_0 \sin(2\beta)$ . Varying the  $B_d^0$  lifetime ( $468 \pm 18 \mu\text{m}$ ) shifts the central value by  $\pm 0.001$ . The parameterization of the intrinsic charge asymmetry is also varied, yielding a  ${}_{-0.019}^{+0.016}$  uncertainty. The largest systematic uncertainty is due to  $\Delta m_d = 0.474 \pm 0.031 \text{ ps}^{-1}$ , which gives a  ${}_{-0.025}^{+0.029}$  shift. These systematic uncertainties are added in quadrature, giving  $\mathcal{D}_0 \sin(2\beta) = 0.31 \pm 0.18 \pm 0.03$ .

## 6 $\sin(2\beta)$

To obtain  $\sin(2\beta)$ , we use dilution measurements from other  $B$  meson samples. Our best single  $\mathcal{D}_0$  measurement, from a large  $B \rightarrow \ell D^{(*)} X$  sample, is  $0.181_{-0.032}^{+0.036}$ <sup>9,11</sup>. Because of differing lepton  $p_T$  trigger thresholds, the average  $p_T$  of the semileptonic  $B$ 's is  $\sim 21 \text{ GeV}/c$ , but it is only  $12 \text{ GeV}/c$  in the  $J/\psi K_S^0$  data. We correct for this difference by using a version of the PYTHIA event generator tuned to CDF data<sup>9</sup>. We supplement the above measurement of  $\mathcal{D}_0$  with the dilution  $\mathcal{D}_+$  measured from  $B^+$ 's in the same  $\ell D^{(*)}$  sample, as well as measurements from  $B \rightarrow J/\psi K^+$  and  $J/\psi K^{*0}$ . The simulation also accounts for the systematic difference between  $B_d^0$  and  $B^+$  dilutions. The  $\mathcal{D}_0$  appropriate for our  $J/\psi K_S^0$  sample is then  $0.166 \pm 0.018 \pm 0.013$ , a small shift from 0.181. The first error is due to the uncertainty in the dilution measurements, and the second is due to the Monte Carlo extrapolation. The latter is determined by surveying a range of simulation parameters<sup>9</sup>.

Using this  $\mathcal{D}_0$ , we find that  $\sin(2\beta) = 1.8 \pm 1.1 \pm 0.3$ . The central value is unphysical since the amplitude of the measured asymmetry is larger than  $\mathcal{D}_0$ . If one wishes to frame this result in terms of confidence intervals, various alternatives are available. We follow the frequentist construction of Ref. 12, which gives proper confidence intervals even for measurements in the unphysical region. Our measurement thereby corresponds to excluding  $\sin(2\beta) < -0.20$  at a 95% confidence level (C.L.). We also calculate that if the true value of

$\sin(2\beta)$  were 1, the median expectation of an exclusion for an experiment like ours would be  $\sin(2\beta) < -0.89$  at 95% C.L. This is a measure of experimental sensitivity<sup>12</sup>; our limit is higher, reflecting the excursion into the unphysical region.

It is interesting to note that if  $\mathcal{D}_0 \neq 0$ , the exclusion of  $\sin(2\beta) = 0$  is *independent* of the value of  $\mathcal{D}_0$ . Given  $\mathcal{D}_0 > 0$ , the same prescription as above yields a dilution-independent exclusion of  $\sin(2\beta) < 0$  at 90% C.L.

We have explored the robustness of our result by varying selection and tagging criteria. None had a significant effect on the asymmetry with the exception of the tagging  $p_T$  threshold. In principle, any choice of the threshold would give an unbiased estimator of  $\mathcal{D}_0 \sin(2\beta)$ . The 400 MeV/ $c$  threshold, however, was our *a priori* choice. A significantly lower choice would have induced larger systematic uncertainties from the tracking asymmetry below 400 MeV, and a substantially higher choice would have induced larger statistical uncertainties due to the reduced tagging efficiency at higher  $p_T$ .

When varying the  $p_T$  threshold we found that  $\mathcal{D}_0 \sin(2\beta)$  drops rather sharply in going from 0.5 to 0.6 GeV/ $c$ , and then gradually rises. The probability of observing such a large change in an  $\sim 100$  MeV/ $c$  step is estimated to be  $\sim 5\%$ . The smallest value of  $\mathcal{D}_0 \sin(2\beta)$  is  $-0.12 \pm 0.21$  (stat. error only) for a 0.7 GeV/ $c$  threshold. This variation cannot be attributed to the dependence of  $\mathcal{D}_0$  on the  $p_T$  threshold: both the charged and neutral dilution measurements vary slowly, in good agreement with the PYTHIA calculations<sup>9</sup>. Moreover, no systematic effects have been found which are able to account for such a variation.

As we can identify no mechanism to give the particular behavior seen, we characterize the variation of  $\mathcal{D}_0 \sin(2\beta)$  with the  $p_T$  threshold by calculating the probability that the variation in the data agrees with the slow variation in the simulation. To this end we employ the  $\chi^2$  procedure used in Ref. 9 to study the dilution variation in a  $B^+ \rightarrow J/\psi K^+$  sample. We compare the data with Monte Carlo pseudo-experiments of similar size and find that the probability of obtaining a higher  $\chi^2$  (*worse* agreement) than the data is 42%, considering only statistical fluctuations. Thus, the observed variation of  $\mathcal{D}_0 \sin(2\beta)$  with the SST  $p_T$  threshold is consistent with statistical fluctuations expected for a sample of this size. The uncertainty on  $\sin(2\beta)$  due to this is already included in the statistical uncertainty on the measurement.

## 7 Conclusions and Acknowledgements

In summary, we have applied a same side flavor tagging method to a sample of  $B_d^0/\bar{B}_d^0 \rightarrow J/\psi K_s^0$  decays and measured  $\sin(2\beta) = 1.8 \pm 1.1 \pm 0.3$ . Although

the sensitivity of the result on the tagging  $p_T$  threshold complicates the interpretation, our result favors current Standard Model expectations of a positive value of  $\sin(2\beta)$ .

This result establishes the feasibility of measuring  $CP$  asymmetries in  $B$  meson decays at a hadron collider. Operation of the Main Injector in the next Tevatron Collider run should provide more than an order of magnitude increase in luminosity. Detector upgrades will further enlarge our  $B$  samples. If current expectations are correct, these large samples should be sufficient to observe and study  $CP$  violation in  $J/\psi K_S^0$ , and possibly in other modes as well<sup>13</sup>.

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