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**CDF**

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## B MIXING AND CP VIOLATION AT CDF

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The mixing of the neutral B mesons and the violation of CP symmetry in the B sector can be investigated at the Tevatron proton-antiproton collider. The most severe challenge that these measurements pose is tagging the flavor of a B meson at production. Here we present in detail the method of same side tagging (SST), which is used to obtain a new measurement of the  $B^0$  mass difference  $\Delta m_d = 0.446 \pm 0.057(\text{stat}) + 0.034 - 0.031(\text{syst})\text{ps}^{-1}$ . The significance of SST and other tagging methods for physics during Run II of the Tevatron is discussed.

## 1 Introduction

## 1.1 Mixing and CP Violation

In the standard model CP violation<sup>1</sup> and  $B^0 - \bar{B}^0$  mixing<sup>2,3</sup> are entirely due to weak transitions between quarks, and depend on the complex elements of the Cabibbo-Kobayashi-Maskawa matrix<sup>4</sup>. The unitarity of this matrix is often represented by the well-known unitarity triangle<sup>5</sup>, in which the magnitudes of  $V_{td}$  and  $V_{ub}$  become the lengths of two sides of a triangle, and their phases become two of the angles. Mixing measurements determine the sides, and CP asymmetries determine the angles.

$B^0$  mixing is measured by forming the asymmetry in the number of mixed and unmixed  $B^0$ 's as a function of proper time:

$$A(t) = \frac{N_{B \rightarrow B}(t) - N_{B \rightarrow \bar{B}}(t)}{N_{B \rightarrow B}(t) + N_{B \rightarrow \bar{B}}(t)} = \cos(x_d t / \tau) \quad (1)$$

where  $x_d = \frac{\Delta m_d}{\Gamma}$  is the mixing parameter and depends on  $|V_{td}|$ . A measurement of  $B$  mixing needs to tag the flavor of the  $B$  meson at decay, which is relatively easy, and at production, which is the major experimental challenge.

CP violation at the hadron collider is most easily detected through the decay  $B^0 \rightarrow J/\psi K_s^0$ . Here one can measure the asymmetry:

$$A(t) = \frac{N_{B \rightarrow J/\psi K_s^0}(t) - N_{\bar{B} \rightarrow J/\psi K_s^0}(t)}{N_{B \rightarrow J/\psi K_s^0}(t) + N_{\bar{B} \rightarrow J/\psi K_s^0}(t)} \quad (2)$$

which in the standard model is given by  $-\sin(2\beta) \sin(x_d t / \tau)$ . Here, only the flavor of the  $B^0$  at production needs to be determined.

If the number of correctly tagged events is  $R$  and the number of incorrectly tagged events is

$W$ , then the observed asymmetries become:

$$A_{\text{obs}}(t) = \frac{R - W}{R + W} A(t) = D A(t) \quad (3)$$

where the constant  $D$  is known as the "dilution". For a given dilution  $D$  and tagging efficiency  $\epsilon$ , the error on the asymmetry is given by:

$$\sigma_A^2 = (1 - A^2 D^2) / N \epsilon D^2 \quad (4)$$

The statistical power of a tagging method is  $\epsilon D^2$ .

## 1.2 Same Side Tagging

Same side tagging (SST), uses the sign of nearby charged tracks to determine the flavor of the b-quark<sup>7</sup>. The principal is illustrated in figure 1: if the  $\bar{b}$  quark hadronizes to a  $B^+$  meson, the next particle in the fragmentation chain is either an unobserved neutral pion (or kaon) or a negative pion (or kaon). If it hadronizes to a  $B^0$ , the next particle is neutral or positive. Orbitally excited  $B$  mesons produce a similar correlation through the decays  $B^{*0} \rightarrow B^+ \pi^-$ , and  $B^{*+} \rightarrow B^0 \pi^+$ . Correlations between  $B^0$  and nearby tracks depend on the decay time due to mixing, while correlations between  $B^+$  and nearby tracks are time-independent. SST has been demonstrated previously by LEP experiments<sup>8</sup>.

## 2 Investigations of SST at CDF

We search for pion charge correlations with  $B^0$  and  $B^+$  in  $110 \text{ pb}^{-1}$  of data recorded with the CDF detector<sup>9</sup> at the Fermilab Tevatron Collider in two ways: first, using a large sample of partially reconstructed  $B$ 's from a high- $p_t$  single-lepton trigger, and second, using a smaller sample of fully reconstructed  $B$ 's from a  $J/\psi$  trigger.

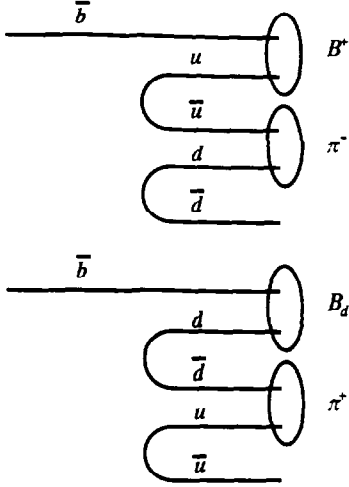


Figure 1: SST principle.

### 2.1 Pion correlations in partially reconstructed B mesons

In the partially reconstructed sample we find a signal of:

- 950  $B^0 \rightarrow D^{*-}\nu l^+, D^{*-} \rightarrow \bar{D}^0\pi^-, \bar{D}^0 \rightarrow K^+\pi^-$
- 770  $B^0 \rightarrow D^{*-}\nu l^+, D^{*-} \rightarrow \bar{D}^0\pi^-, \bar{D}^0 \rightarrow K^+\pi^-\pi^+\pi^-$
- 2400  $B^0 \rightarrow D^{*-}\nu l^+, D^{*-} \rightarrow \bar{D}^0\pi^-, \bar{D}^0 \rightarrow K^+\pi^-\pi^0$
- 1900  $B^0 \rightarrow D^-\nu l^+, D^- \rightarrow K^+\pi^-\pi^-$
- 2700  $B^+ \rightarrow \bar{D}^0\nu l^+, \bar{D}^0 \rightarrow K^+\pi^-$

In each case the  $D$  or  $D^*$  is first reconstructed by requiring that tracks come from a common vertex, and then vertexed again with the lepton to form the  $B$ -vertex. The proper time of the  $B$  at the decay point is estimated from:

$$c\tau = L_{xy}^B \frac{m_B}{p_t^B} = L_{xy}^B \frac{m_B}{p_t^D} K \quad (5)$$

where  $L_{xy}^B$  is the decay length of the  $B$  in the transverse plane,  $p_t^{lD} = |\mathbf{p}_t^D + \mathbf{p}_t^l|$ ,  $\mathbf{p}_t^B$ ,  $\mathbf{p}_t^D$ , and  $\mathbf{p}_t^l$  designate transverse momenta of  $B$ ,  $D$ , and lepton, and  $K=0.86$  is a constant determined from Monte Carlo. The resolution  $\sigma_{c\tau}$  is determined from Monte Carlo and can be parameterized by  $\sigma_{c\tau}^2 = \sigma_0^2 + \sigma_{3\gamma}^2(c\tau)^2$ , with  $\sigma_{3\gamma} = 11\%$  and  $\sigma_0$  varying from  $50\mu\text{m}$  to  $60\mu\text{m}$ , depending

on the channel. The lepton sign tags the flavor of the  $B$  meson at decay. To tag the flavor at production, we choose the track with the lowest momentum transverse to the  $D$  candidate,  $p_t^{r\ell}$ . An event is considered taggable if another track can be found with  $p_t > 400\text{ MeV}$  and with separation  $R = \sqrt{\Delta\eta^2 + \Delta\phi^2} < 0.7$  from the reconstructed  $B$  meson. A tagging track is further required to be within  $3\sigma$  of the primary vertex: this cut rejects pions from  $D^{**}$  decays. The efficiency is high (about 72%), and independent of the  $c\tau$ .

The taggable events are divided into 7 bins in  $c\tau$ ; within each bin the number of events showing the expected correlation with nearby charged tracks (“right sign” events) and the opposite correlation (“wrong sign” events) are determined by fitting a Gaussian plus a background shape. One source of background in each channel is crosstalk from the other channels: eg., if the soft pion is undetected in the decay  $B^0 \rightarrow D^{*-}\nu l^+$ ,  $D^{*-} \rightarrow \bar{D}^0\pi^-$ , then the event is background to the decay  $B^+ \rightarrow \bar{D}^0\nu l^+$ ,  $\bar{D}^0 \rightarrow K^+\pi^-$ .

Corrected asymmetries are calculated by estimating the crosstalk from Monte Carlo, then determining two physical asymmetries ( $B^0$  and  $B^+$ ), from the three observed asymmetries ( $l^+D^-$ ,  $l^+D^{*-}$ , and  $l^+D^0$ ) for each of the seven bins. The final asymmetries depend on  $f^{**} = BR(B \rightarrow \nu l D^{**})/BR(B \rightarrow \nu l X)$ , on  $f = BR(B \rightarrow \nu l D)/BR(B \rightarrow \nu l X)$ , on  $P_V$  (the fraction of  $D^{**}$  decays to  $D^*$ ),  $\epsilon(\pi_s)$  (the reconstruction efficiency of soft pions from  $D^*$ ), and  $\xi(c\tau)$  (the probability of accidentally tagging on a pion from  $D^{**}$ ).

Figure 2 shows the final corrected asymmetries. The upper plot is the asymmetry in  $B^+$ . It is fit to a flat line yielding a dilution of  $D_+ = 0.28 \pm 0.04(\text{stat}) + 0.05 - 0.03(\text{syst})$ . The lower plot shows the asymmetry for  $B^0$ . It shows a clear oscillatory behavior, and is fit to the convolution of a cosine and a resolution function, yielding  $D_0 = 0.22 \pm 0.03(\text{stat}) + 0.04 - 0.03(\text{syst})$ , and  $\Delta m_d = 0.446 \pm 0.057(\text{stat}) + 0.034 - 0.031(\text{syst})\text{ps}^{-1}$ . Table 1 summarizes the systematic errors.

Combining the efficiencies with the dilutions, we obtain:  $\epsilon D_+^2 = 5.7 \pm 1.5(\text{stat}) + 2.0 - 1.2(\text{syst})\%$ , and  $\epsilon D_0^2 = 3.4 \pm 1.0(\text{stat}) + 1.2 - 0.9(\text{syst})\%$ .

Source	Central value	Variation	$\Delta(\Delta m_d)$	$\Delta D_0$	$\Delta D_+$
$\epsilon(\pi_s)$	0.88	+0.12 -0.21	+0.003 -0.005	+0.006 -0.004	+0.039 -0.022
eff. $P_V$	0.61	+0.39 -0.41	+0.018 -0.005	+0.011 -0.019	+0.001 -0.009
$f^*/f$	3.7	+4.5 -2.9	+0.000 -0.001	+0.002 -0.000	0.000 -0.001
eff. $f^{**}$	0.21	$\pm 0.08$	+0.028 -0.029	+0.034 -0.025	+0.033 -0.025
$\epsilon_{norm}$	0.69	$\pm 0.17$	$\pm 0.002$	$\pm 0.005$	$\pm 0.004$
$B^0$ Lifetime	450 $\mu$ m	$\pm 33\mu$ m	+0.002 -0.004	0.0	-
Resolutions	-	-	+0.006 -0.005	$\pm 0.001$	-
Total	-	-	+0.034 -0.031	+0.04 -0.03	+0.05 -0.03

Table 1: Systematic errors for the partially reconstructed  $B$  analysis

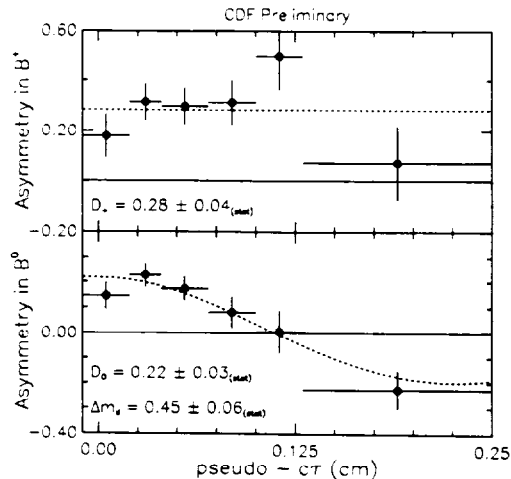


Figure 2: Final corrected asymmetries vs  $ct$ .

## 2.2 Pion correlations in Fully Reconstructed $B$ Mesons

For this study a same-side jet charge technique is used for tagging, rather than the technique described in the previous section. Charged and neutral  $B$  mesons are fully reconstructed in the channels  $B^+ \rightarrow J/\psi K^+$  and  $B^0 \rightarrow J/\psi K^*$ . Starting with 420,000  $J/\psi$ 's, we obtain 689  $B^+$  over a background of 290, and 320  $B^0$  over a background of 116. Tracks within a cone of radius 0.7 are used to compute a jet charge  $Q_{SST} = \frac{\sum q_i w_i}{\sum w_i}$ , where the weight  $w_i$  of the  $i^{th}$  track is a function only of the  $p_t^{rel}$ .

$$w_i = e^{-\frac{1}{2} \left( \frac{p_t^{rel} - 0.5}{0.3} \right)^2} \quad (6)$$

and the index  $i$  runs over all tracks with  $p_t > 700$  MeV. An event is considered taggable if  $|Q_{SST}| > 0.4$ : the dilutions and efficiencies are measured for

each species. Results are shown in table 2. In the case of  $B^0$ , these results must be corrected for the mixing; the corrected dilutions are also shown in the table. These dilutions have large errors but are consistent with those of the previous study.

## 3 CDF Run II

Run II of the Tevatron will begin in 1999 with major improvements to both the accelerator and the detector<sup>9</sup>. The design goal of the machine is to deliver  $2 \times 10^{32} \text{cm}^{-2} \text{s}^{-1}$  for a total integrated luminosity of  $2 \text{fb}^{-1}$ . Detector upgrades include a 96 cm, 7 layer double-sided silicon tracker. The z-readout will provide CDF with precision 3D tracking. The deadtimeless readout is capable of 50 kHz at level one; at level two this is exploited to trigger on high impact parameter tracks. We now discuss the discovery potential of CDF during Run II.

Three tagging methods are now understood: SST, soft muon and electron tagging, and jet charge tagging; the combined  $\epsilon D^2$  for these techniques is 4%. With additional effort and detector improvements, such as a time-of-flight counter for kaon tagging, this figure could rise to 8%.

### 3.1 $\sin 2\beta$

CP asymmetries in the decay  $B^0 \rightarrow J/\psi K_s^0$  determine the value of  $\sin 2\beta$ . The present sample of this decay, collected with a dimuon trigger, is  $239 \pm 22$  events, with a signal-to-noise ratio of 1.2. Taking into account the improvements in luminosity, lower trigger thresholds, a planned dielectron trigger, and a lower signal-to-noise ratio resulting from a 3D precision tracker, we expect to collect about 13,000 of these events, which results in an error  $\sigma_{\sin 2\beta} = 0.12$ , assuming  $\epsilon D^2$  of 4.0%.

### 3.2 $\sin 2\alpha$

CP asymmetries in the decay  $B^0 \rightarrow \pi^+\pi^-$  determine the value of  $\sin 2\alpha$ , modulo theoretical uncertainties from penguins. Here, the major challenge is to trigger on the decay. Triggering on pairs of oppositely charged pions with  $p_t > 2.0$  GeV results in a level one rate of 16kHz; applying a 100  $\mu\text{m}$  impact parameter cut at level 2 reduces this less than 20 Hz. We expect about 10,000 events. To obtain  $\sigma_{\sin 2\alpha} = 0.1$  would require  $\epsilon D^2$  of 8%.

### 3.3 $B_s$ mixing

The mixing of the neutral  $B_s$  meson is of interest because  $\frac{x_A}{x_s}$  determines  $\frac{|V_{cb}|}{|V_{cs}|}$  free from hadronic uncertainties. We have investigated the reconstruction of  $B_s \rightarrow D_s \nu l$ ,  $D_s \rightarrow \rho \pi$ , and also  $B_s \rightarrow D_s \pi^-\pi^+\pi^-$ . 250 decays of the previous type with a signal-to-noise ratio of about 1.8 have been observed at CDF using a single lepton trigger. In extrapolating to Run II we use the improvement in luminosity and trigger, and include additional decay channels of the  $D_s$ . We also extrapolate from the single lepton trigger to the dilepton trigger, which is a high-dilution flavor tagged sample. We expect 6,400 tagged  $B_s$  events. The  $\Delta m_s$  reach using this sample is limited by the poor  $c\tau$  resolution typical of a partially reconstructed decay, to  $\Delta m_s \approx 10\text{ps}^{-1}$ .

The channel  $B_s \rightarrow D_s \pi^-\pi^+\pi^-$  is harder to reconstruct but has superior  $c\tau$  resolution. It can enter the data sample through the  $B^0 \rightarrow \pi^+\pi^-$  trigger. Here an  $\epsilon D^2$  of 8% is needed to obtain 1,600 equivalent tagged events, which would make the experiment sensitive to  $\Delta m_s \approx 13\text{ps}^{-1}$ .

## 4 Conclusion

CDF has demonstrated, for the first time in a hadron collider, the feasibility of same side tagging; use of this tagging method yields a measurement of  $\Delta m_d = 0.446 \pm 0.057(\text{stat}) + 0.034 - 0.031(\text{syst})\text{ps}^{-1}$ . The combination of this and other tagging methods currently demonstrated at CDF yields a total  $\epsilon D^2$  of 4%, which puts the CP violating parameter  $\sin 2\beta$  within reach of the Tevatron in Run II.  $B_s$  mixing up to  $\Delta m_s \approx 10$  ps should be accessible. Measurement of  $\Delta m_s$  up to of 13 ps, and of the CP violating parameter  $\sin 2\alpha$  will require improvements in flavor tagging.

Sample	Dil. (%)	Eff. (%)	$\epsilon D^2$ (%)
$B^+$			
Data	$33 \pm 8$	$36 \pm 2$	$4.0 \pm 1.9$
MC	$42 \pm 1$	$29.0 \pm 0.2$	$5.2 \pm 0.2$
MC*	$37 \pm 1$	$26.9 \pm 0.3$	$3.6 \pm 0.2$

Uncorrected $B^0$			
Data	$10 \pm 10$	$41 \pm 3$	$0.4 \pm 0.9$
MC	$13 \pm 2$	$27.1 \pm 0.4$	$0.4 \pm 0.1$
MC*	$12 \pm 2$	$26.5 \pm 0.5$	$0.4 \pm 0.1$

Corrected $B^0$			
Data	$19 \pm 19 \pm 2$	$41 \pm 3$	$1.5 \pm 3.0 \pm 0.3$
MC	$25 \pm 4 \pm 2$	$27.1 \pm 0.4$	$1.7 \pm 0.5 \pm 0.3$
MC*	$23 \pm 4 \pm 2$	$26.5 \pm 0.5$	$1.4 \pm 0.5 \pm 0.3$

Table 2: Summary of the fully reconstructed  $B$  analysis. Sample labeled MC\* is Pythia Monte Carlo without  $B^{**}$ . Below,  $B^0$  dilutions have been corrected for mixing.

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