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## WHY IS THE TEMPERATURE OF THE UNIVERSE 2.726 K?

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### ABSTRACT

NASA's Cosmic Background Explorer (COBE) Satellite has recently made the most accurate measurement of the temperature of the Universe determining it to be  $2.726 \pm 0.01$  K. In trying to understand why the temperature has this value, one is led to discover the most fundamental features of the Universe—an early, radiation-dominated epoch, enormous entropy per nucleon, synthesis of the light elements around three minutes after the bang, and a small excess of matter over antimatter—as well as some of the most pressing issues in cosmology today—the development of structure in the Universe and the identification of the nature of the ubiquitous dark matter.



# 1 The Cosmic Background Radiation

The existence of the cosmic background radiation (CBR) is one of the cornerstones of the standard cosmology, or hot big-bang model [1]. Indeed, its very existence provides the evidence that the Universe began from a hot state [2]. The temperature of the cosmic background radiation has recently been measured to unprecedented precision by the Far InfraRed Absolute Spectrophotometer (FIRAS) instrument on NASA's Cosmic Background Explorer (COBE) Satellite [3]:

$$T_0 = 2.726 \text{ K} \pm 0.01 \text{ K} \quad (1)$$

the FIRAS results are shown in Fig. 1.

Measurements of the CBR temperature, made over the period of almost thirty years since its discovery by Penzias and Wilson [4], now span almost three and half decades in wavelength, from about 0.04 cm to 70 cm, and are all consistent with the COBE temperature. Deviations from a perfect black-body spectrum are less than 0.03% over the wavelengths probed by COBE, 0.05 cm – 0.5 cm [3]. The CBR is probably the most well studied and best black body known; indeed, the COBE collaboration plans to use their data to test the form of the Planck Law itself [5].

With a number density of  $411 \text{ cm}^{-3}$  the photons in the CBR by a wide margin account for most of the (known) particles in the Universe, outnumbering atoms by a factor of around a billion. The surface of last scattering for the CBR is the Universe itself at an age of a few 100,000 years (see Fig. 2), and thus the CBR provides a fossil record of the infant Universe. As such its every property has been studied—spectrum, polarization, and spatial isotropy—revealing important information about the evolution of the Universe [6]. As I will discuss, just trying to answer the simple question, why is the temperature of the CBR 2.726 K?, reveals the most fundamental features of the Universe as well as several pressing problems in cosmology.

To begin, it is imprecise to say that the Universe has a temperature, as it is not in thermal equilibrium today. Earlier than a few 100,000 years the matter was ionized and a state of thermal equilibrium existed; at about this time the temperature was about 3000 K and the equilibrium ionization fraction of matter became very small. The Universe is said to have “recombined;” since neutral matter is transparent to the radiation, the CBR photons we detect today last scattered a few 100,000 years after the bang. After last scattering, the expansion simply red shifted the energy of CBR photons and diluted their number density, and, because of a remarkable feature of the expansion,

a Planck distribution was maintained with a temperature that decreased in proportion to the size of the Universe. For this reason, the Universe today is filled with thermal radiation of temperature 2.726 K despite the fact that the Universe is no longer in thermal equilibrium.

Since the temperature of the Universe is decreasing—and has been for some 15 billion years or so—the original question must be rephrased: Why did the temperature of the Universe reach about 3 K at an age of about 15 billion years old? (Several independent measures of the age, based upon the evolution of stars in the oldest globular clusters, the cooling of the oldest white dwarfs in the Galaxy, and the dating of certain radioactive isotopes, indicate that the Universe is between 12 and 18 billion years old [7].)

According to Einstein's equations, the present age of the Universe—that is, time since the bang—is related to the present energy density  $\rho_0$ :

$$t_0 = \frac{c}{\sqrt{6\pi G\rho_0}}; \quad (2)$$

where  $G = 6.67 \times 10^{-8} \text{ cm}^3 \text{ sec}^{-2} \text{ g}^{-1}$  is Newton's gravitational constant,  $c = 3.00 \times 10^{10} \text{ cm sec}^{-1}$  is the speed of light, and for simplicity I have assumed that the Universe is spatially flat ( $\Omega_0 = 1$ ). The quantity  $\Omega_0 = \rho_0/\rho_{\text{crit}}$  is the ratio of the mean energy density to the critical, or closure, energy density; the critical energy density  $\rho_{\text{crit}}$  corresponds to a mass density of  $3H_0^2/8\pi G \simeq 1.88 \times 10^{-29} (H_0/100 \text{ km s}^{-1} \text{ Mpc}^{-1})^2 \text{ g cm}^{-3}$  and  $H_0 = 40 \text{ km s}^{-1} \text{ Mpc}^{-1} - 100 \text{ km s}^{-1} \text{ Mpc}^{-1}$  is Hubble's constant, whose value is still only known to within a factor of two. "Low-density" universes,  $\Omega_0 < 1$ , are negatively curved and expand forever, while "high-density" universes,  $\Omega_0 > 1$ , are positively curved and eventually recollapse. The "critical" universe,  $\Omega_0 = 1$ , is spatially flat and also expands forever. In the general case,  $t_0 = \sqrt{3\Omega_0 c^2 f^2(\Omega_0)/8\pi G\rho_0}$ , where the function  $f(\Omega_0)$  varies between 1 and 2/3 for  $\Omega_0$  between 0 and 1.

We know at least one component of the energy density today: the CBR black-body radiation itself, which contributes an energy density

$$\rho_{\text{CBR}} = \frac{\pi^2 k_B^4 T_0^4}{15\hbar^3 c^3} \simeq 4.18 \times 10^{-13} \text{ erg cm}^{-3}. \quad (3)$$

where  $\hbar = 1.05 \times 10^{-27} \text{ erg sec}$  is Planck's constant divided by  $2\pi$ ,  $k_B = 1.38 \times 10^{-16} \text{ erg K}^{-1}$  is Boltzmann's constant, and  $\pi^2 k_B^4/15\hbar^3 c^3 = 7.56 \times 10^{-15} \text{ erg cm}^{-2} \text{ sec}^{-1} \text{ K}^{-4}$  is four times the Stefan-Boltzmann radiation constant divided by the speed of light. If the CBR were the only contribution to

the energy density. Eq. (2) would imply an age of about 1300 billion years, a factor of about 100 too large. Put another way, for the age to be consistent with the energy density in the CBR alone, the temperature would have to be closer to 30 K.

## 2 Matter in the Universe

By asking a simple question we have learned that the CBR black-body radiation must make a minor contribution to the energy density today,  $\rho_{\text{CBR}} \sim 10^{-4}\rho_0$ . What then accounts for the bulk of the present energy density? It could exist in other thermal backgrounds of relativistic particles; however, that would require the existence of several thousand additional massless particle species—and we know of at most three, the electron, muon, and tau neutrinos, which together contribute a energy density comparable to that of the CBR (provided all three neutrino species are massless, or nearly massless).

It is almost certain that the bulk of the energy density exists in the form of nonrelativistic matter [8]. Taking the age of the Universe to be 15 billion years, Eq. (2) implies a matter density of about  $3 \times 10^{-30} \text{g cm}^{-3}$  (energy density of about  $3 \times 10^{-9} \text{erg cm}^{-3}$ ). Today the energy density in matter is more than ten thousand times greater than that in the CBR, but that was not always the case. As the Universe expands the matter density decreases as  $R^{-3}$ , by the factor by which the volume increases;  $R(t)$  is the cosmic-scale factor which describes the linear expansion of the Universe. The energy density in radiation decreases faster, as  $R^{-4}$ , because the energy of each photon is also “red shifted” by the expansion, accounting for the additional factor of  $R^{-1}$ . Owing to the different scalings of the matter and radiation energy densities, when the Universe was about  $10^{-4}$  of its present size and a few thousand years old, the two energy densities were equal. Earlier than this the energy density in radiation exceeded that in matter, and the Universe is said to be “radiation dominated.”

Early on matter was a trace constituent in a Universe dominated by a hot plasma of thermal particles; at the earliest times,  $t \ll 10^{-5}$  sec, the hot plasma was a soup of the fundamental particles, quarks, leptons, and gauge bosons (the photon,  $W^\pm$  and  $Z^0$ , and gluons, the carriers of the forces). This is an extremely important feature of the Universe and has profound implication for the study of its earliest history. Among other things it means

that the formation of structure in the Universe—galaxies, clusters of galaxies, voids, superclusters, and so on—through the gravitational amplification of small inhomogeneities in the matter density only began a few thousand years after the bang [9]. This is because during the radiation-dominated phase the self-gravitational attraction of the matter was no match for the rapid expansion driven by the enormous energy density in radiation, and density perturbations could not grow (see Fig. 3).

A year ago, another instrument on the COBE satellite, the Differential Microwave Radiometer (DMR), detected tiny differences in the CBR temperature measured in different directions: on average about a part in  $10^5$  (or  $30\mu\text{K}$ ) between directions separated by  $10^\circ$ ; see Fig. 4 [10]. Inhomogeneities in the matter density give rise to temperature variations of a similar size, and this COBE discovery provided the first evidence for the existence of the primeval density fluctuations that are supposed to have seeded all the structure in the Universe. Moreover, since density fluctuations grow in proportion to the cosmic-scale factor and the level of inhomogeneity exceeds unity today (i.e.,  $\delta\rho/\rho > 1$ ), the amplitude of the primeval fluctuations needed to seed the observed structure is set roughly by the size of the scale factor when the matter and radiation energy densities were equal—about  $10^{-5}$  or so—a number which is determined by the present ratio of the energy density in radiation to that in matter. In a very real sense, the CBR temperature set the amplitude of temperature fluctuations that were expected!

The extreme uniformity of the temperature of the CBR across the sky, to better than a part in  $10^4$  on angular scales from arcminutes to  $180^\circ$  [11], reveals an important property of the Universe—its smoothness, or isotropy and homogeneity—and raises another question—why is it so smooth? Though the Universe was very small at early times, its rapid expansion limits the distance over which even photons could travel. At the epoch of last scattering this maximum travel distance, known as the distance to the horizon, corresponds to an angle of only about  $1^\circ$  on the sky; this fact precludes any causal physical process from explaining the temperature uniformity, and hence the smoothness of the Universe, on angular scales greater than this. Further, it raises the same question about the origin of the primeval density inhomogeneities; they too could not have been created on such large distances by causal processes operating at early times.

The smoothness and the primeval inhomogeneity needed to seed structure could have existed since the beginning. However, Guth showed that both can be explained by a very rapid period of expansion—called cosmic inflation—

that may have taken place about  $10^{-34}$  sec after the bang [12]. This rapid expansion is driven by the false-vacuum energy (particle physics analogue of latent heat) associated with a first-order phase transition. The basic idea is that a tiny patch of the Universe, which could have been made smooth early on, grew exponentially to a size that would encompass all that we can see today and well beyond. The enormous growth of the scale factor also allows quantum mechanical fluctuations arising during inflation on extremely small length scales to become density perturbations on length scales large enough to account for the primeval density inhomogeneities needed to seed the structure seen today [13]. (The COBE DMR results are consistent with the temperature variations predicted in inflationary models, as are two other models for the origin of the density fluctuations.) In addition, the tremendous growth in the size of the Universe—by a factor greater than that by which the Universe has grown since—also leads to a Universe that, regardless of its initial curvature, today still appears flat, making  $\Omega_0 = 1$  a “prediction” of inflation.

### 3 The Nucleon-to-Photon Ratio

Assuming that the present mass density exists in the form of ordinary matter, atoms made of nucleons—neutrons and protons—and electrons, a present nucleon density of about  $2 \times 10^{-6} \text{ cm}^{-3}$  is implied. From this we can form the dimensionless ratio of the nucleon-number density to the photon-number density:

$$\eta \equiv \frac{n_N}{n_\gamma} \sim 5 \times 10^{-9}. \quad (4)$$

This ratio indicates that CBR photons outnumber nucleons by a factor of around a billion. The inverse of  $\eta$ , the ratio of photons to nucleons, measures the entropy in radiation per nucleon (in units of  $k_B$ ). The radiative entropy per nucleon in a star like our sun is only about  $10^{-2}$ ; even in the highest entropy environment known, the center of a newly born neutron star, the entropy per nucleon is only a few. The Universe has such an extremely high entropy that it is very difficult to imagine that any physical process could have produced the CBR or added significantly to it. Further, because the CBR spectrum is so accurately Planckian, there are severe restrictions on any process that produces photons, e.g., radiation from an early generation of stars or the decay of relic neutrinos (if they are massive and unstable). The

entropy per nucleon *seems* to be an initial condition rather than a quantity that can be explained by familiar astrophysical processes.

The nucleon to photon ratio  $\eta$  also quantifies the net excess of nucleons over antinucleons per photon, which is the baryon number of the Universe. The net baryon number per photon is equal to  $\eta$  because there is no significant amount of antimatter in the Universe today (i.e.,  $n_{\bar{N}} \ll n_N$ ):

$$\frac{n_B}{n_\gamma} \equiv \frac{n_N - n_{\bar{N}}}{n_\gamma} \approx \frac{n_N}{n_\gamma}. \quad (5)$$

Baryon number, like charge, is known empirically to be conserved to a high degree of precision. (The longevity of the proton, lifetime greater than  $10^{32}$  yr, attests to this; were baryon number not conserved, the proton would be expected to decay in a fraction of a second.) Conservation (or even approximate conservation) of baryon number and the value of  $\eta$  imply that earlier than about  $10^{-5}$  sec, when it was hot enough for matter and antimatter to be freely created, there was approximately one more baryon than antibaryon for every billion or so of both. Looking at it the other way around, in the absence of this tiny excess, all the baryons and antibaryons would have annihilated as the Universe cooled leaving essentially no matter or antimatter today.

Though the details have not been worked out, many believe that this excess of matter over antimatter so crucial to the existence of matter today, evolved due to particle interactions in the very early Universe ( $\lesssim 10^{-12}$  sec) that neither respect the symmetry between matter and antimatter nor the conservation of baryon number [14]. (Violation of the conservation of baryon number is an almost universal prediction of theories that attempt to unify the forces of Nature, and also arises in the standard model of particle physics due to subtle quantum mechanical effects. The symmetry between matter and antimatter is observed to be violated by a small amount in the decays of the  $K^0$ ,  $\bar{K}^0$  mesons.) Explaining the small net baryon number, quantified by  $\eta$ , appears to be much more promising than trying to explain the large entropy, quantified by  $\eta^{-1}$ .

The high entropy plays a crucial role in determining the chemical composition of the Universe. Were the entropy per nucleon even a thousand times smaller, nuclear reactions taking place when the Universe was only a fraction of a second old and the energy equivalent of the temperature  $k_B T$  was few MeV would have quickly processed all the nucleons into tightly bound nuclei such as carbon, oxygen and on up to iron. Instead, most of the nucle-

ons remain in the form of protons with only the lightest isotopes, D,  $^3\text{He}$ ,  $^4\text{He}$ , and Li, being produced. (It is generally believed that the other elements were produced in stars or spallation reactions in the interstellar medium.) The lack of significant nucleosynthesis beyond the light elements traces directly to the high entropy: The enormous number of high-energy photons per nucleon delays the onset of nucleosynthesis until a temperature of order  $k_B T \sim 0.1 \text{ MeV}$  because earlier photons rapidly dissociated nuclei as they formed; when nucleosynthesis does begin coulomb repulsion between light nuclei prevent their fusion into the heavier, more tightly bound nuclei. (This fact was appreciated before the discovery of the CBR and led Gamow and others to predict the existence of a relic radiation with about the correct temperature [15].)

The predictions of primordial nucleosynthesis agree with the inferred primordial abundances of the light elements provided that the nucleon-to-photon ratio lies in the interval

$$3 \times 10^{-10} \lesssim \eta \lesssim 4 \times 10^{-10} \quad (6)$$

The very existence of a “concordance interval” is an important test of the standard cosmology, and as a bonus it provides the most accurate determination of the nucleon-to-photon ratio [16]. The predictions of big bang nucleosynthesis and the observed abundances of the light elements are shown in Fig. 5.

The success of the theory of primordial nucleosynthesis not only provides the earliest test of the big-bang model, but it also leads to a startling suggestion: that most of the matter in the Universe is something other than nucleons. From primordial nucleosynthesis and the temperature of the CBR the mass density contributed by nucleons can be computed:

$$\rho_N = m_N \eta n_\gamma \simeq 2.7 \times 10^{-31} \text{ g cm}^{-3}. \quad (7)$$

where  $m_N \simeq 1.7 \times 10^{-24} \text{ g}$  is the mass of a nucleon,  $n_\gamma = 2\zeta(3)k_B^3 T_0^3 / \pi^2 \hbar^3 c^3 = 411 \text{ cm}^{-3}$  is the number density of photons, and  $\zeta(3) = 1.20206 \dots$ . This is significantly lower than the earlier estimate of the total mass density derived from the age of the Universe, though to be sure, we made certain assumptions at the time. In any case, the small mass density in nucleons leads one to ask whether the mass density of the Universe is greater than that contributed by ordinary matter alone.

## 4 Dark Matter in the Universe

Let me very briefly review what we know about the mass density of the Universe [17]. Based upon the above determination of the density of ordinary matter and our imperfect knowledge of the Hubble constant, it follows that ordinary matter contributes between 1% and 10% of the critical density (the larger value for the lower value of the Hubble constant). From astronomical observations we know: (i) luminous matter, in the form of stars, contributes less than 1% of critical density; (ii) other observations that measure the amount of mass through its gravitational effects, e.g., the motion of stars in spiral galaxies [18], the motions of galaxies in clusters, and so on, indicate that the total amount of mass is *at least* 10%-20% of the critical density [19]; (iii) our motion with respect to the CBR suggests that the density is near critical; and (iv) no definitive measurement of the total amount of matter has yet been made(!).

The third point deserves further discussion; the CBR is hotter in the general direction of the constellations Hydra and Centaurus, by about 3 mK, and cooler in the opposite direction by the same amount [20]; see Fig. 6. The simplest—and now standard—interpretation is that our galaxy is moving with respect to the “cosmic rest frame” at a speed of about  $620 \text{ km s}^{-1}$ . (It is interesting to note that COBE detected a much smaller yearly modulation of the same kind arising due to Earth’s motion around the sun at  $30 \text{ km s}^{-1}$ ; this should convince any remaining “geocentrists” that the Earth does indeed move!) The motion of the Milky Way arises due to the gravitational tugs exerted on it by the thousands of galaxies within a hundred Mpc or so. Because the distribution of galaxies is not precisely homogeneous, the sum of these tugs does not cancel, but results in a net force in the direction of Hydra-Centaurus. Since the gravitational force on the Milky Way due to another galaxy is proportional to that galaxy’s mass, an estimate for the mass in this volume—and for the average mass density—can be made by relating our velocity to the observed distribution of galaxies in this volume. This technique samples the largest volume of space of any method yet, and indicates a value for  $\Omega_0$  that is close to unity [21].

Though our knowledge of the mass density of the Universe is still incomplete, we can already conclude that: (i) most of the matter in the Universe is dark, i.e., does not emit or absorb radiation of any wavelength; (ii) if the mass density of the Universe is at the lower limit of current estimates and if the density of ordinary matter is at its upper limit, then ordinary matter

could account for all the mass with  $\Omega_0$  being around 0.1; (iii) on the other hand, if the mass density is significantly greater than 10% of the critical density, then the dark matter must be something other than ordinary matter. This possibility is favored by many cosmologists, mainly the theorists, as theoretical considerations, including cosmic inflation and theories of structure formation, argue strongly for the critical Universe ( $\Omega_0 = 1$ ). I hasten to add that the observational situation is far from settled, and many, if not most, astronomers would say that the case for  $\Omega_0 = 0.1$  is the more compelling one at present.

It is interesting to note the crucial role played by the CBR temperature in reaching these conclusions. The outcome of primordial nucleosynthesis depends only upon the nucleon-to-photon ratio. Therefore the primordial abundances of the light elements serve to determine  $\eta$  rather than the nucleon mass density itself. To determine nucleon mass density the photon-number density—and hence CBR temperature—must be known. Were the CBR temperature a factor of three or so higher, the mass density contributed by ordinary matter would be close to the critical density.

If most of the mass in the Universe is not ordinary matter, what is it? The most promising idea is that it exists in the form of elementary particles left over from the early, fiery moments of the Universe [22]. In this case, another dimensionless ratio can be formed, the ratio of the number density of “exotic particles” to CBR photons,

$$\eta_X \equiv \frac{n_X}{n_\gamma} \simeq 7 \times 10^{-9} \left( \frac{m_N}{m_X} \right), \quad (8)$$

where  $m_X$  is the mass of the exotic and for simplicity I have assumed that exotic particles contribute critical density and a Hubble constant of  $50 \text{ km s}^{-1} \text{ Mpc}^{-1}$ .

As it turns out, there are a handful of interesting candidates for the dark matter. They include a massive neutrino; the neutralino; and the axion. All three possibilities are motivated by particle-physics considerations first with their important cosmological consequence as a bonus—and perhaps even a hint that the particle dark-matter hypothesis is on the right track.

How do these particles arise as relics of the big bang? In the early Universe thermodynamics dictated a kind of particle democracy, with all species being roughly equally abundant. As the Universe cooled pair creation of massive particles became energetically forbidden, and massive particle species disappeared through particle-antiparticle annihilations. If a particle species is

stable, it can have a significant relic abundance because in the expanding Universe annihilations eventually cease as particles and antiparticles become too sparse to encounter one another and annihilate. The relic abundance depends upon the potency of annihilations, quantified by the annihilation cross section,  $\sigma_{\text{ann}}$ , which has units of area.

In the case of neutrinos, annihilations became ineffective before they could start significantly reducing the neutrino abundance relative to photons, and so  $\eta_X$  is expected to be around one (more precisely 3/11). Thus the contribution of neutrinos to the mass density is dictated by their mass: They contribute critical density for a mass of about  $2.5 \times 10^{-8} m_N$ , or a mass energy of about twenty electronvolts (eV). Such a mass is in the ballpark predicted for neutrino masses by many unified theories of particle interactions [23]. While experimental evidence rules out a mass this large for the electron neutrino, it is still possible that either the muon or tau neutrino has such a mass.

The neutralino is a particle that is predicted to exist in supersymmetric extensions of the standard model of particle physics [24]; predictions for its mass are rather uncertain, ranging from ten to thousand times that of the nucleon. (Supersymmetry dictates a spin one-half partner for every integer spin particle, and vice versa; in the simplest supersymmetric models the neutralino is the spin one-half partner of the photon.) In the case of the neutralino, annihilations significantly decrease the number of neutralinos from their early abundance of one per photon. Their relic abundance is inversely proportional to their annihilation cross section, very roughly

$$\eta_X \sim \frac{(\hbar/c)^2}{m_X m_{\text{Pl}} \sigma_{\text{ann}}}. \quad (9)$$

where  $m_{\text{Pl}} = \sqrt{\hbar c/G} \simeq 2.2 \times 10^{-5} \text{ g}$  is the Planck mass. Note that the relic abundance depends inversely upon the neutralino mass, so that it cancels out when computing the relic mass density of neutralinos. Remarkably, the condition that the neutralino contribute critical density becomes a condition on its annihilation cross section alone,

$$\sigma_{\text{ann}} \sim \frac{10^{-2} \hbar^2}{k_B T_0 m_{\text{Pl}}} \sim 10^{-36} \text{ cm}^2. \quad (10)$$

The cross section required is of the order of magnitude of a weak-interaction cross section, which is the general size expected for the neutralino annihilation cross section.

The axion is a particle whose existence traces to trying to solve a nagging problem of the standard model of particle physics, the strong- $CP$  problem. Subtle quantum mechanical effects associated with Quantum-Chromodynamics (QCD), the theory of the strong interactions that bind quarks together, result in a predicted value for the electric-dipole moment of the neutron that is nine orders of magnitude larger than the current experimental upper limit. In 1977 Peccei and Quinn proposed an elegant solution: the introduction of a new symmetry (now referred to as PQ symmetry) that solves the problem and leads to the prediction of a new particle, the axion [25]. The axion interacts more feebly than neutrinos do, which explains why its existence has yet to be verified or falsified, and, for the same reason it would not have been produced in the thermal plasma during the earliest moments.

Relic axions arise in a different and rather unusual way. Because the axion interacts so weakly, the value of the axion field is left undetermined at early times, taking on whatever random value it had at the beginning; eventually, at about  $10^{-5}$  sec, due to QCD effects, the axion field begins to relax to its equilibrium value. In so doing, it overshoots that value and is left oscillating. These cosmic harmonic oscillations correspond to an extremely high density of very low momentum axions that should still be with us today. If the rest mass energy of the axion is around  $10^{-5}$  electronvolts relic axions provide closure density [26]. Theoretical considerations do little to pin down the mass of the axion; however, a host of laboratory experiments and astrophysical/cosmological arguments have narrowed the allowed window for its mass to  $10^{-6}$  eV to  $10^{-3}$  eV, roughly the range where it would contribute close to the critical density [27].

All three particle candidates for the dark matter are sufficiently attractive that experimental efforts are underway to test their candidacies [28]; in the case of the axion and neutralino, the experiments involve actually detecting the particles that comprise the dark halo of our own galaxy [29]. For the neutrino, direct laboratory measurements restrict the electron-neutrino mass to be less than about 8 eV, too small to account for the critical density. Direct measurements of the muon and tau neutrino masses are far more difficult and cannot come close to probing a mass as small as 20 eV; indirect experiments, such as neutrino oscillation experiments and solar neutrino observations, can provide some information, but thus far no conclusive positive evidence [30].

## 5 Development of Structure in the Universe

One of the most pressing questions in cosmology concerns the details of how the abundance of structure seen in the Universe today came to be. If the bulk of the matter in the Universe exists in the form of particle relics from the big bang there are profound implications for how structure formed. First, the process can begin earlier, as soon as the Universe becomes matter dominated, a few 1000 years after the bang; if there is only ordinary matter the growth of the primeval density perturbations cannot begin until matter and radiation decouple, a few 100,000 years after the bang, when matter is freed from the drag of the radiation. Because density inhomogeneities can start growing sooner, their initial amplitude can be smaller, leading to smaller predicted variations in the CBR temperature.

The COBE DMR result is consistent with this smaller prediction, but by no means confirms the existence of exotic dark matter. One of the three viable scenarios of structure formation involves ordinary matter only. This minimalist picture, proposed by Peebles [31], postulates a Universe with baryonic matter only, the dark matter existing in the form of “dark” stars (low-mass stars or the remnants of high-mass stars—neutron stars or black holes). The density fluctuations arise from local fluctuations in the number of baryons (of unknown origin) and the spectrum is adjusted to both explain the observed structure and to be consistent with the level of CBR anisotropy. The weak point of this model is that  $\Omega_0$  must be about 0.2 in order to form the observed structure, which violates the nucleosynthesis bound since all the matter is baryonic.

There are two broad classes of models for structure formation with particle dark matter: hot dark matter models, where the dark matter exists in the form of neutrinos, and cold dark matter models, where it exists in the form of neutralinos or axions. In the case of hot dark matter the primeval density fluctuations on small length scales are erased by the streaming of fast moving neutrinos from regions of higher density into those of lower density, and the structures that form first are very large—superclusters—and smaller structures—galaxies and so on—must be formed by fragmentation. This so-called “top-down” scenario is disfavored as structures as large as superclusters are just forming today, making it difficult to explain the existence of distant galaxies that must have formed long ago [32].

The erasing of fluctuations on small length scales does not occur with cold dark matter because the dark-matter particles move very slowly—neutralinos

because they are so heavy and axions because they were born with very low momentum. With cold dark matter structure develops “bottom-up,” from galaxies to clusters of galaxies to superclusters. Cold dark matter seems to work much better, though not perfectly [33]. It has been suggested that the cold dark matter scenario could be improved by “mixing” in a small amount of hot dark matter, in the form of neutrinos of mass  $7\text{ eV} - 10\text{ eV}$ , referred to as mixed dark matter [34]. An even more radical suggestion for improving cold dark matter involves the idea that baryons and cold dark matter only account for about 20% of the critical density, with vacuum energy (in more conventional terms, a cosmological constant) contributing the other 80% [8].

To complete the description of a scenario for structure formation the origin of the primeval fluctuations must be specified. One possibility involves quantum fluctuations arising during inflation, discussed earlier. This leads to the fairly successful (in this author’s opinion) and very well studied “cold dark matter” scenario. Another possibility is that the primeval fluctuations involve topological defects—monopoles, string, or texture—that act as gravitational seeds and were produced in a cosmological phase transition that occurred about  $10^{-36}$  sec after the bang. These scenarios are less well developed, but look promising [35].

At present there are three viable pictures of structure formation, two early-Universe scenarios—inflation-produced density fluctuations plus cold dark matter and topological defects plus cold (or possibly hot) dark matter—and the minimalist scenario involving only ordinary matter. Further study of the the tiny variations in the CBR temperature on angular scales of order  $1^\circ$  should soon help to whittle the list down.

## 6 Conclusion

The cosmic background radiation is arguably the most important cosmological relic yet discovered, and much has and will be learned from its study. The CBR is so fundamental to the standard cosmology that just trying to understand why its temperature is 2.726 K today leads one to discover the most fundamental features of the Universe as well as some of the most pressing cosmological problems—the origin of structure and the nature of the dark matter. In the end, we have no firm explanation as to why the Universe even has a temperature; that is, where the fiery radiation came from. According to the inflationary scenario its existence traces to the decay of the false-vacuum

energy. However, its explanation, like that of the expansion itself, may well involve physics yet to be understood.

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## 7 Figure Captions

**Figure 1:** The COBE FIRAS measurements of the CBR spectrum [3] and the spectrum of a 2.726 K black body. Note, the COBE one-sigma error flags have been enlarged by a factor of 100.

**Figure 2:** A schematic diagram illustrating the last-scattering surface. Also shown is the size of the horizon at that epoch, which subtends an angle of about  $1^\circ$ .

**Figure 3:** Primeval density perturbations grow in proportion to the cosmic-scale factor  $R$  (whose value today is taken to be one). With ordinary matter only, perturbations begin growing when matter and radiation decouple ( $R \simeq 10^{-3}$ ); with particle dark matter perturbations begin growing much earlier, as soon as the Universe becomes matter dominated ( $R \simeq 3 \times 10^{-5}$ ), and thus smaller primeval density inhomogeneities are required. Also shown is the ratio of energy density in the CBR to that in matter, which decreases as  $R^{-1}$ .

**Figure 4:** The COBE DMR measurements of  $\langle \Delta T(\theta)^2 \rangle$ , the temperature difference squared between two points on the sky separated by angle  $\theta$  and averaged over the entire sky (from [10]). The much larger temperature anisotropy of about  $3000 \mu\text{K}$  due to our motion with respect to the cosmic rest frame has been removed.

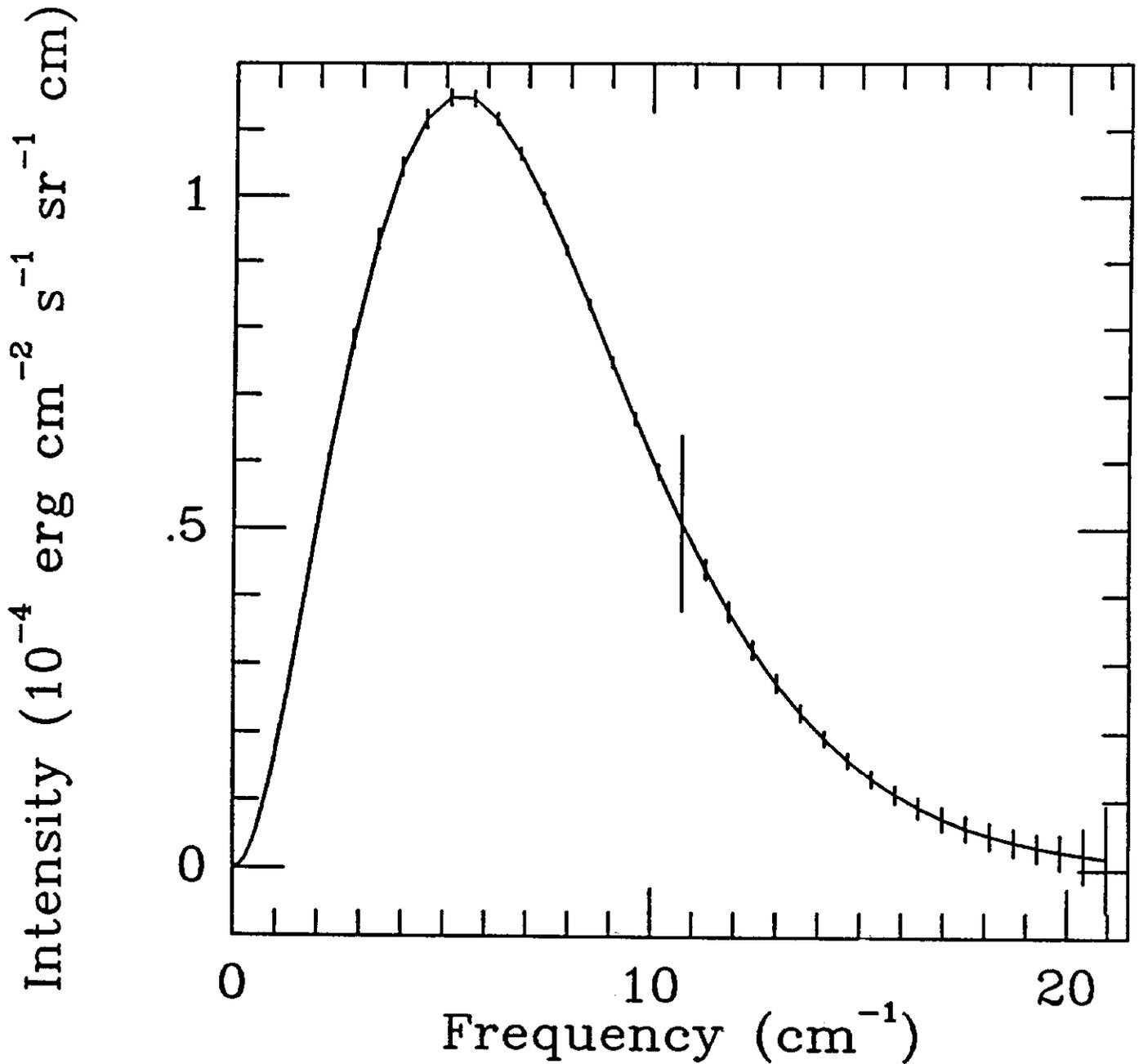
**Figure 5:** The predictions of primordial nucleosynthesis and the inferred primordial abundances of D,  $^3\text{He}$ ,  $^4\text{He}$ , and  $^7\text{Li}$  [16]. The  $^4\text{He}$  abundance is the mass fraction of nucleons in  $^4\text{He}$ ,  $Y_p$ , and is shown on a linear scale; the thickened line indicates the theoretical uncertainty in  $Y_p$  which is all due to the uncertainty in the neutron lifetime. Abundances for the other elements are given as the number of atoms per Hydrogen atom and are shown on logarithmic scales. The boxes indicate the observational uncertainties in the inferred primordial abundances and the concordance intervals; the overall concordance interval is shaded.

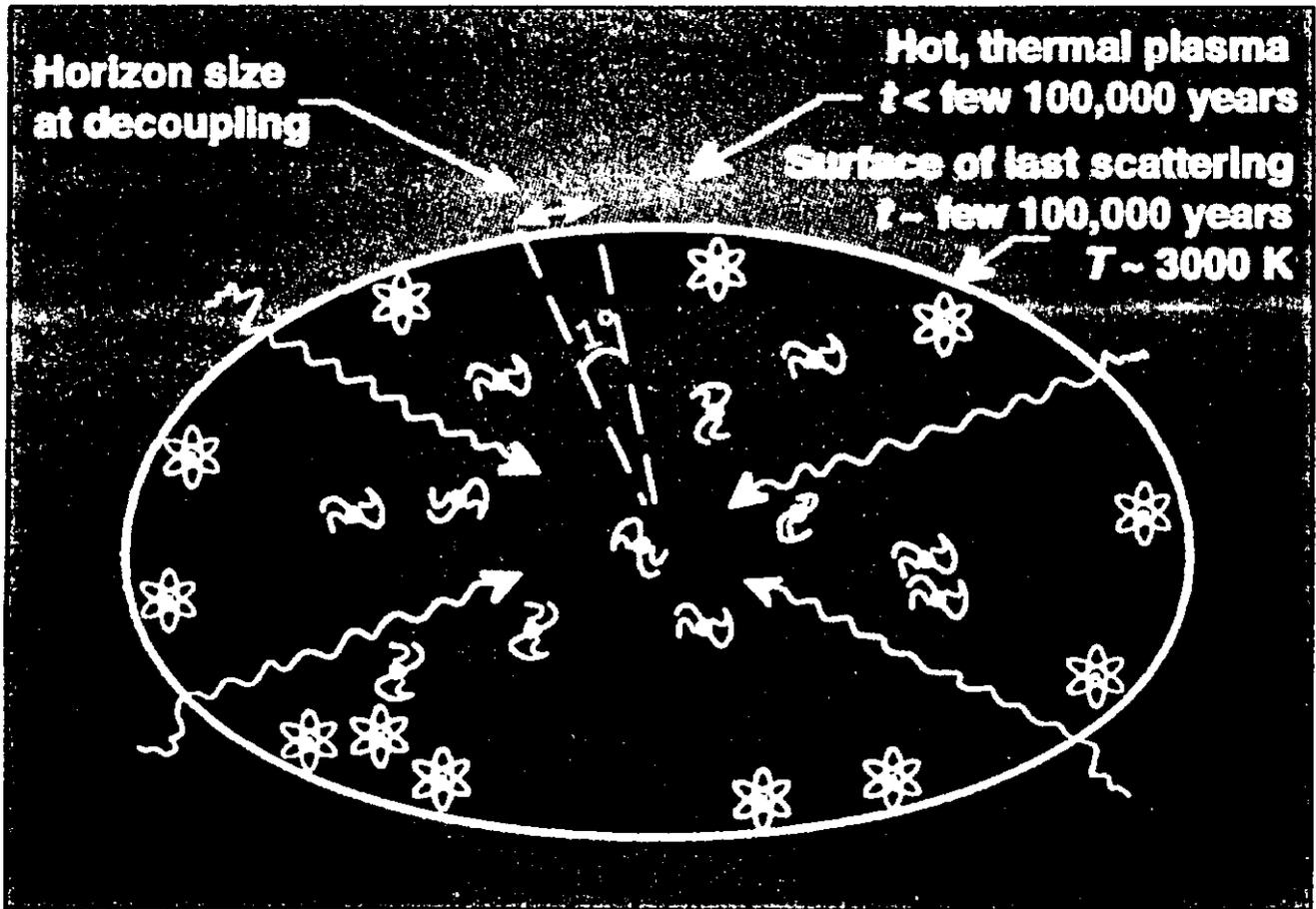
**Figure 6:** COBE DMR temperature maps of the sky. The variation in the CBR temperature is represented on a color scale (pink is hot, blue is cold) on a sky projection where the plane of our the Milky Way runs across the middle. Map (a): The dipole anisotropy due to our motion with respect to the cosmic rest frame is clearly seen; some galactic emission can also be seen.

Map (b): The dipole anisotropy has been subtracted and the color scale made more sensitive; the temperature fluctuations are partly due to density perturbations on the last-scattering surface and partly due to instrumental noise in the DMR.

WHY IS THE TEMPERATURE OF THE  
UNIVERSE 2.726K?

FIGURE 1

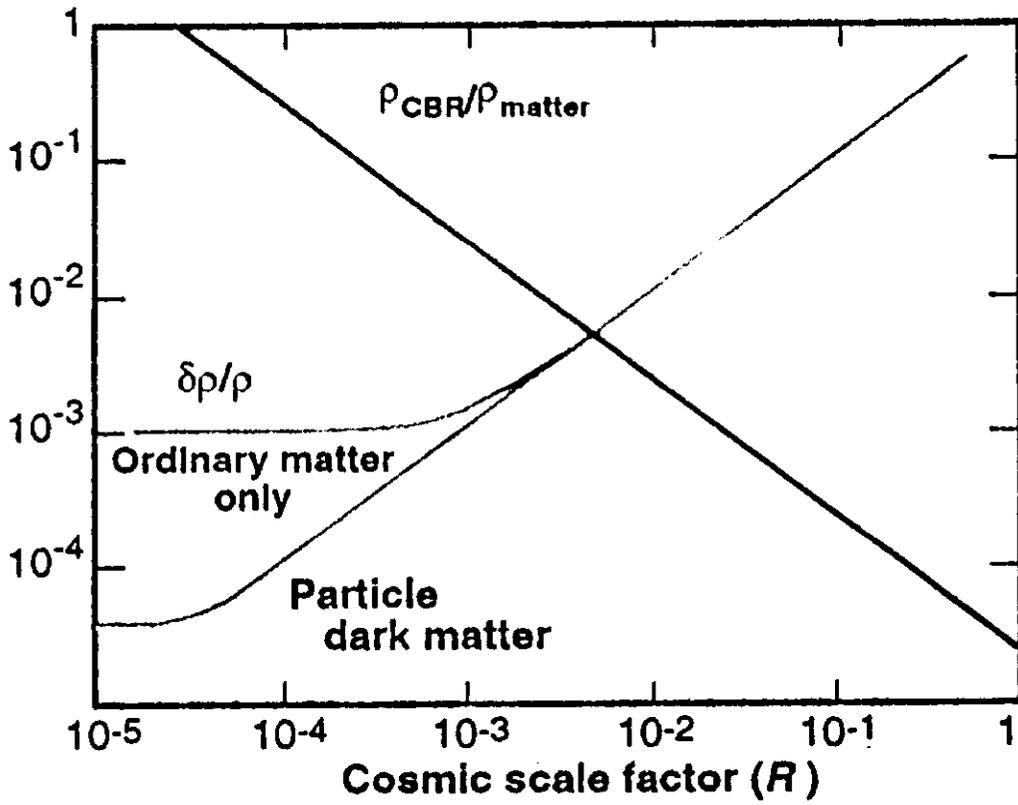




Turner

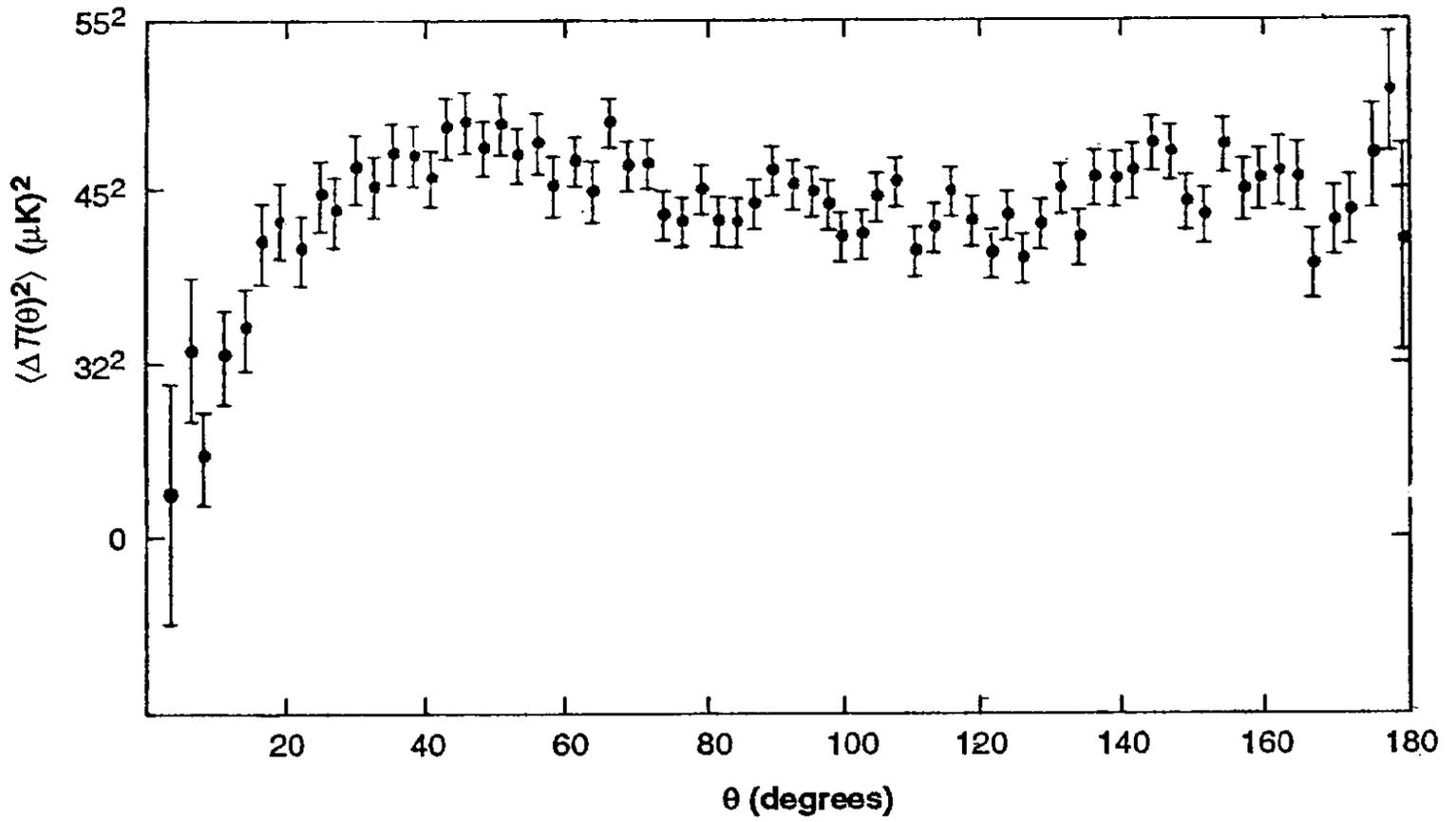
x 18 picas  
Science

Fig. 2



**x 14 picas**

**Turner Science Fig. 3**

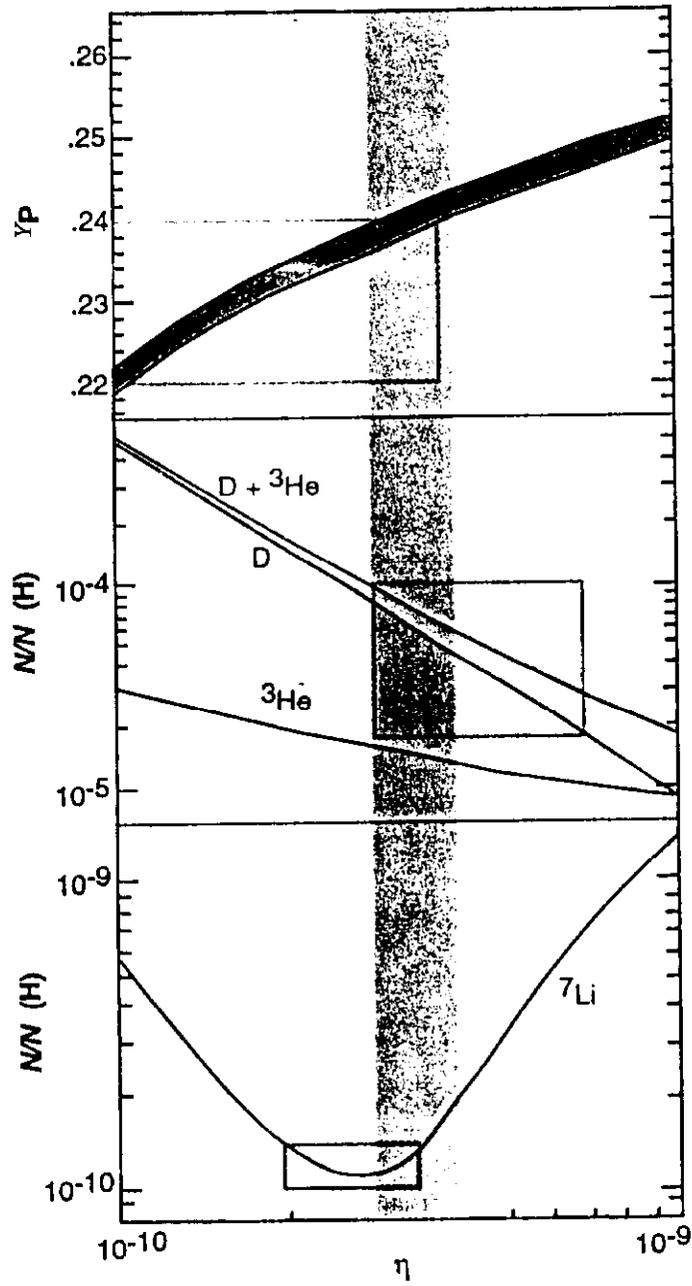


Turner

26 picas (to float)

Fig. 4

Science



Turner

14 picas  
Science

Fig 5

M



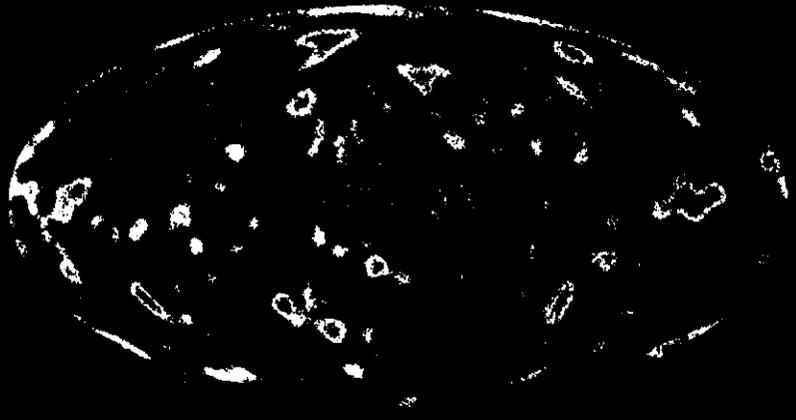
C

BK

A



B



TURNER



21 PICAS  
SCIENCE

FIG 6