Heavy Flavor Physics at Hadron Colliders

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The search for the top quark has dominated heavy flavor physics at hadron colliders. For Standard model decay of top the present mass limit is \( m_t > 89 \text{ GeV} (95\% \text{ C.L.)} \). Bottom production cross sections are quite large at hadron colliders, thus providing enough statistics for extensive studies. Results on cross sections, \( B^0 - \bar{B}^0 \) mixing, exclusive channels and rare \( B \) decays will be summarized.

1 INTRODUCTION

The Standard Model includes three lepton and three quark doublets. Apart from a lack of direct observation of the \( \nu_\tau \), the top quark is the last missing block of the model. The measurement of backward-forward asymmetry in \( e^+e^- \rightarrow b\bar{b} \) and the absence of flavor changing neutral currents in \( b \) decays provide indirect evidence for the existence of an isodoublet partner of the bottom quark. The CDF experiment at the Tevatron Collider has reported a lower mass limits (95\% C.L.) of 89 GeV\(^4\). Recent fits to the Standard Model parameters, including radiative corrections to the \( W \) and \( Z \) masses, provide an upper limit of \( m_t < 210 \text{ GeV} \). We will review these results and discuss prospects for the future.

The cross section for \( b \) pair production at hadron colliders is predicted from QCD to be quite large (about 50 \( \mu b \) at the Tevatron Collider). The \( b \) cross section measurements of UA1 and CDF and their comparison to theoretical calculations will be discussed. Also, \( B^0 - \bar{B}^0 \) mixing measurements of UA1 and CDF will be reviewed. Because of the copious \( b \) production exclusive channels are now being detected by CDF, and limits on rare decay modes are reported by both CDF and UA1.

2 TOP SEARCH

Top production at a hadron collider can take place through the electroweak process \( p\bar{p} \rightarrow W \rightarrow t\bar{b} \) or the hard scattering process \( pp \rightarrow t\bar{t} \). For the first process to occur the top mass has to be below the \( W \) mass. Figure 1 shows the total cross sections for the two processes\(^3\) at \( \sqrt{s} = 0.63 \text{ and } 1.8 \text{ TeV} \). At CERN energies the electroweak process dominates, whereas at the Tevatron Collider the top production rate from hard scattering dominates. The hard scattering cross sections of Figure 1 are obtained by combining the higher order calculations of Nason et al\(^4\) with the structure functions of Diemoz et al\(^5\), using the method of Altarelli et al\(^6\).

2.1 STANDARD TOP DECAYS

The \( t \rightarrow Wb \) decay of the top quark via the charged weak current into a bottom quark and a virtual \( W \) (real for
m_{top} > m_W + m_b), provides the signatures to be exploited for a top search. The most copious channel is provided by the hadronic decay modes, which, however, suffers from severe backgrounds from QCD. A much cleaner signature is provided by the leptonic decay of the W, as these leptons have high PT and are isolated. Analyses have been done on a. events with one high PT lepton and jets, b. events with two high PT leptons, one from each W, and c. events of category a. with the requirement of an additional low PT lepton coming from the semileptonic decay of the b quark (b tag).

Backgrounds to semileptonic decays of top come from other physics processes and from lepton misidentification. The Drell-Yan process, W, Z production and b̄b pair production are sources of high PT leptons. These processes have to be understood in order to assess their contribution to the signals. For the lepton+jets final state the major background is due to b̄b and W+jets production. For the dilepton channels it is due to b̄b, Drell-Yan, and Z0 → τ± production. For the ee and μμ final states the Z mass region has to be removed altogether.

The results of the measurement made and the channel used are summarized in Table I. The most recent measurements are from CDF, where results from the eμ, ee, μμ, and ℓ + jets with a b tag (b → μ) channels have been combined. After selection of events, proper cuts to reduce non-lepton background and kinematic cuts to reduce the physics background, only one candidate event is left in the 4.1 pb⁻¹ analyzed in the eμ channel. Figure 2 shows the electron transverse energy (E_T) plotted versus the muon transverse momentum (P_T). The signal region is above 15 GeV for both variables. The one candidate at high E_T and high P_T is consistent with background calculations: 0.2 events from Z0 → τ± and 0.2 events from Z0 → b̄b. The expected number of events for WW production is 0.15 and for WZ is 0.05. For leptons of such high momenta (E_T > 30 GeV and P_T > 40 GeV/c) the probability of Z0 → τ± is ≤ 1%.

From these data, when the systematic uncertainties on luminosity, acceptance, detection efficiency etc., are convoluted with the Poisson distribution for the one event, the cross section upper limits of Figure 3 are obtained. The lowest value of the theoretical cross section intersects the experimental limit at 89 GeV. Assuming that top decays exclusively via the charged current mode (t → Wb) the preliminary CDF result¹ thus is:

m_t > 89 GeV with 95% C.L.

2.2 NON STANDARD TOP DECAYS

The top mass could be lower than 89 GeV if the predominant decays are other than those predicted by the Standard Model. For example, were a charged Higgs(H⁺) of mass smaller than that of the W to exist, the top could decay as t → H⁺b with a large branching ratio. For a top mass in the range m_H⁺ + m_b < m_t < m_W + m_b the decay into H⁺b would be about 100%. The decay modes
Figure 3: The 95\% C.L. upper limit of the top cross section as a function of the top mass, for several sets of CDF data: the published $e\mu$ data\textsuperscript{10}, the combination of all di-lepton channels, and the combination of the di-lepton channels and the lepton+2jets+low energy $\mu$ channels\textsuperscript{11}.

of the $H^+$ depend on the Higgs model used\textsuperscript{11}. In the simple extension of the Standard Model, there are two Higgs doublets which result in both charged and neutral Higgs bosons. The $H^+$ branching ratios depend on the couplings of the two Higgs doublets to quarks and leptons. The couplings depend on a parameter, $\tan \beta$, which is the ratio of the vacuum expectation values of the neutral components of the two Higgs doublets. For large values of $\tan \beta$ the dominant $H^+$ decay is $\tau\nu$, for small values of $\tan \beta$ the dominant decay is $H^+ \rightarrow o\phi$. The searches reported above would not detect such decay modes.

The UA1 experiment\textsuperscript{12} has searched for an excess of $\tau$ over $\mu$ and $e$ from $W'$s. The process is $t \rightarrow H^+b$ with subsequent decay of $H^+ \rightarrow \tau\nu$. The topologies studied are $\mu+ \geq 2$ jets and $\mu\mu+$ jet, for the case where the $b$ itself decays into a $\mu$ (non-isolated). This study is done by maximum likelihood method involving more then one variable. For the single muon analysis the variables used are: $P_T$ of the muon, $P_T^{miss}$ and $|\cos \theta_{j2}|$, where $\theta_{j2}$ is the angle of the second highest $E_T$ jet and the beam axis in the rest frame of the system $\mu$-jet$_1$-jet$_2$-$P_T^{miss}$. The distribution of the likelihood of the different hypotheses is shown in Figure 4. The $H^+$ hypothesis clearly does not fit the data, which is well explained by background. For this plot $\tan \beta=2$ is assumed, this gives $BR(H^+ \rightarrow \tau\nu) \geq 93\%$.

The top mass limit depends on the value of the $H^+$ mass and of the parameter $\tan \beta$ that determines the $H^+ \rightarrow \tau\nu$ branching ratio. The final result, for a 95 \% branching ratio is shown in Figure 5. This puts a limit to the top mass $m_t > 60$ GeV for $m_{H^+} = 43$ GeV.

2.1 TOP MASS FROM EWK PARAMETERS

The measurement of the $W$ mass at hadron colliders also provides information on the top mass, since it is related to the vector boson masses through the radiative corrections, $\Delta r$. In the standard electro-weak gauge theory, $\Delta r$ can be calculated perturbatively as the sum of many terms:

$$\Delta r = \Delta r^{(\alpha)} + \Delta r^{(\alpha\alpha\phi)} + \Delta r^{(\alpha^2)} + ...$$

In $\Delta r$ there are contributions proportional to $m_t$ resulting from virtual top quark effects which affect the $W$ and $Z$ propagator. The appearance of these terms is a direct consequence of the Higgs origin of the top quark mass. The top mass has a less strong dependence on the Higgs mass itself.

The $W$ mass has been recently measured at hadron colliders with high precision by UA2\textsuperscript{15} and CDF\textsuperscript{16}. The results are:
Figure 5: The 90% and 95% C.L. upper limit on the top mass as a function of the \( H^+ \) mass as obtained by the UA1 experiment\(^\text{12} \) assuming \( \text{BR}(H^+ \rightarrow \tau \nu) = 95\% \). The dashed lines delineate regions excluded at the 95% C.L. by \( e^+e^- \) experiments\(^\text{13} \), the dotted line shows the limit obtained at 90% C.L. by measurement of the \( W \) total width, \( \Gamma_W \), by CDF\(^\text{14} \).

\[
M_W = 80.35 \pm 0.37 \text{(stat. and syst.) GeV} \quad \text{UA2}
\]
\[
M_W = 79.91 \pm 0.39 \text{(stat. and syst.) GeV} \quad \text{CDF}
\]

with average:

\[
M_W = 80.14 \pm 0.27 \text{ GeV}
\]

The radiative corrections have been recently calculated with the higher order loop contributions by Halzen and Kniehl\(^\text{17} \). Their prediction is shown in Figure 6. The average \( W \) mass above is plotted as a band; the \( Z \) mass value of 91.174 is an average of the LEP results\(^\text{18} \). The top mass limits are as follows:

\[
m_t = 142^{+46}_{-41} \text{ GeV} \quad \text{for } M_H = 250 \text{ GeV}
\]

and the central value dependence on the Higgs mass is:

\[
m_t = 142^{+15}_{-18} \text{ GeV} \quad \text{for } M_H = 50-1000 \text{ GeV}
\]

the combination of the two uncertainties (see Figure 6) gives the limit \( m_t < 200 \text{ GeV} \) (90% C.L.). For fits of these data as well as the LEP and \( \nu \) scattering data, see the analyses reported in Ref. 2.

### 3.0 B PHYSICS AT HADRON COLLIDERS

Cross sections for \( b \) quark production are quite large at hadron colliders. In recent years, both UA1 and CDF have been studying mixing, exclusive and rare decays. We will survey here those results. Details of some of the CDF results can be found in the contribution by Hans Wenzel in these Proceedings\(^\text{19} \).

#### 3.1 BOTTOM CROSS SECTION

Nason, Dawson and Ellis (NDE)\(^\text{4} \), have calculated bottom production cross sections at hadron colliders to next to leading order (NLO) QCD.

Large uncertainty in the cross sections arise from uncertainties in the choice of the scale \( \mu \), \( \Lambda_{QCD} \), the bottom mass, and the the choice of structure functions. Figure 7 shows the results of ref. 4,3 for a range of values for these quantities.

Cross section measurements have been done by the UA1 and CDF collaborations. One of the methods used by both experiments has been the study of the inclusive lepton spectrum, which exploits the copious semileptonic decays of the B hadrons. Backgrounds to this final state come from leptons from charm decays, from W and Z production, and from hadrons misidentified as leptons. The major systematic errors come from uncertainties in the bottom quark fragmentation, the semileptonic branching ratio and the assumed bottom \( P_T \) distribution for accep-
3.1.1 THE UA1 MEASUREMENTS

The UA1 analysis\textsuperscript{20} is based on a sample of 6103 muons with \( P_T > 10 \text{ GeV}/c \) in an \(|\eta| < 1.5\) interval. At least one jet is required with \( P_T > 10 \text{ GeV}/c \) and separation from the muon of more than \( \Delta R = 1.0 \). Here \( \Delta R = \sqrt{\Delta(\phi)^2 + \Delta(\eta)^2} \), where \( \phi \) is the azimuthal angle and \( \eta \) the pseudorapidity. The direction of the jet to which the muon belongs is obtained by using only the charge particles (including the muon) within a cone of \( \Delta R < 0.6 \) with the muon direction. The variable used to study this sample is the \( P_T \) of the muon relative to the jet axis.

After additional requirements (including non-isolation) for removal of \( W \) and \( Z \) production, UA1 obtains\textsuperscript{20} the distribution of \( P_T^{rel} \) shown in Figure 8. The contribution from bottom, charm, and hadron backgrounds, as obtained from Monte Carlo, are shown. The result of the fit gives the fraction of \( \bar{b}b \) events to be \( 0.33 \pm 0.03 \text{(stat)} \pm 0.03 \text{(syst)} \).

These data provide \( b \) cross section measurements for \( \mu P_T \) above 10 GeV/c. The data is divided in bins to provide an inclusive integrated cross section for \( P_T^b \) greater than that of the assigned bin (determined by requiring that 90% of the muons come from \( b \) quarks with momentum above that bin value). The lowest \( P_T^b \) bin from inclusive muons is at 15 GeV/c. The systematic uncertainties come from \( b \) quark fragmentation (\( \pm 6\% \)), integrated luminosity (\( \pm 8\% \)), detector acceptance (\( \pm 8\% \)), \( b \rightarrow \mu \) branching ratio (assumed to be \( 10.2 \pm 1.0\% \)), jet \( E_T \) scale (\( \pm 12\% \)), and the assumed \( b \) quark spectrum (\( \pm 20\% \)).

The results are shown in Figure 9 superimposed to the NDE calculations\textsuperscript{4}. In Figure 9 results from di-muon events are also shown: for \( P_T > 6 \text{ GeV}/c \) (\( J/\psi \) events), \( P_T > 6 \text{ GeV}/c \) (low mass di-muon events), and \( P_T > 10 \text{ GeV}/c \) (high mass di-muon events). These analyses are described in Ref. 20,22. The agreement between the measurements and the calculations is quite good, within the experimental and theoretical uncertainties, for a \( P_T^{min} \) range from 6 to 54 GeV/c.

Normalizing the QCD predictions of Figure 9 to the first three data points and extrapolating to \( P_T^{min} = 0 \), they obtain a prediction for the inclusive \( b \) cross section of 12.8 \( \pm 4.7 \text{(exp.)} \pm 6 \text{(th.)} \) \( \mu b \) in the rapidity range \(|\eta| < 1.5\). Using the QCD rapidity distribution they obtain \( \sigma (p\bar{p} \rightarrow b\bar{b} + X) = 19.3 \pm 7 \text{(exp.)} \pm 9 \text{(th.)} \) \( \mu b \) at \( \sqrt{s} = 630 \text{ GeV} \).

3.1.2 THE CDF MEASUREMENTS

The CDF collaboration has measured the \( b \) quark cross section at \( \sqrt{s} = 1.8 \text{ TeV} \) using the inclusive electron spec-
The electron sample was obtained with two separate triggers. The 12 GeV electron trigger required a central calorimeter electromagnetic (EM) shower with cluster $E_T > 12$ GeV, accompanied by a charged track with $P_T > 6$ GeV/c pointing to it. The 7 GeV trigger had similar requirements but was prescaled. A total of $4.4 \, \text{pb}^{-1}$ and $175 \, \text{nb}^{-1}$ were collected for the two triggers, respectively. Electron identification in CDF relies on the fine calorimeter segmentation and the use of proportional chambers located at shower maximum in the calorimeter\textsuperscript{16,23}. In order to reduce the hadron background ($\pi^0$ overlapping with charged tracks) for electron energies as low as 7 GeV, more stringent requirements are applied to this sample\textsuperscript{24}. Photon conversion electrons and Dalitz pairs (from $\pi^0 \rightarrow e^+e^-\gamma$) are removed by rejecting events that have a second charged track, of opposite sign, that forms a low invariant mass pair with the electron. This algorithm, however, removes only 50% of the photon conversions, leaving a contamination estimated to be $(20 \pm 5)\%$ of the electron sample. The electron spectrum thus obtained is shown in Figure 10.

The contribution of the electrons from W is removed by requiring that the event have a $E_T^{\text{miss}} < 8\sqrt{E_T}$, where $E_T$ is the total transverse energy in the event, obtained adding all the calorimeter cells. The contribution from $Z$ decays is removed by rejecting events for which there is a second electron that gives a di-electron invariant mass greater than 80 GeV.

Remaining backgrounds are from hadrons misidentified as electrons and electrons from charm. The first contamination is estimated to be $(15 \pm 15)\%$ from a study of the electron selection variables. The charm contribution is estimated to be $(12 \pm 10)\%$ from the ISAJET Monte Carlo\textsuperscript{21}. Supporting evidence that this sample contains mostly electrons from the $b$ quark is shown in Figure 11. Here a search is made for the decay $\bar{B} \rightarrow e^-D^0X$, where the $D^0$ decays into a $K^-\pi^+$, i.e., the $e$ and the $K$ have the same sign. The correct (wrong) sign combinations, for $\bar{B} \rightarrow e^-D^0X$ and its charge conjugate decay, are shown in Figure 11a (11b). There are $75 \pm 17$ events with the correct sign combination in agreement with the calculated rate obtained using the measured branching ratios for this
To relate the electron spectrum to a parent $b$ quark, CDF used the same technique as employed by UA1 and previously described. The cross sections are calculated for three $P_T$ bins. The systematic errors from sources other than backgrounds come from the uncertainties in $b$ quark fragmentation (16%), electron identification efficiency (10%), trigger efficiency (10%), $B$ semileptonic branching ratio (10%) and integrated luminosity (7%). The results are shown in Figure 12, where the cross sections calculated by Nason et al$^4$ are also shown for comparison.

The second method used by CDF$^{24}$ to measure the $b$ quark cross section consists in reconstructing $B^{\pm}$ mesons decaying into $\psi + K^{\pm}$. The $\psi$ sample was obtained by triggering on two muons using the central muon chambers ($|\eta| < 0.65$). Two triggers were used, which required two muons with $P_T > 3$ GeV/c, or $P_T > 5$ GeV/c. These were implemented at different times during the run. The integrated luminosities were of 2.63 pb$^{-1}$ and 1.01 pb$^{-1}$ respectively.

The invariant mass distributions for same and opposite sign muons are shown in Figure 13. The $\psi$ signal is clearly visible in the opposite sign di-muon mass spectrum. The standard CDF muon selection criteria have been applied to this sample$^{16}$. The $J/\psi$ sample is obtained by requiring the invariant mass of the two muons to be $3097 \pm 50$ MeV and consists of 2500 events. The average $P_T$ for the $J/\psi$ is 8 GeV/c, due to the trigger requirements.

To reconstruct a given final state, the two muons from the $J/\psi$ are first constrained to the beam position and then mass constrained to improve the resolution. Next all tracks found in a cone of 60° around the $J/\psi$ direction are combined with the $J/\psi$, using the relevant mass assignment for the required final state. For the decay $B^{\pm} \rightarrow J/\psi + K^{\pm}$ the track is required to have a $P_T > 3$ GeV/c. For the $J/\psi + K^{*0}$ final state only the three highest tracks are used to form the $K\pi$ combinations, in order to reduce the combinatorial background. The invariant mass distribution for these two final states is shown in Figure 14. The signal at the $B$ mass includes $35 \pm 9$ events$^{24}$.

To measure the $b$ quark cross section only the $P_T > 3$ GeV/c trigger sample was used, containing $(10.5 \pm 4.0)$ $B^{\pm} \rightarrow J/\psi + K^{\pm}$ events. The branching ratio for $B$ decay...
in this final state with subsequent $J/\psi \rightarrow \mu^+\mu^-$ has been measured by both CLEO$^{25}$ and ARGUS$^{26}$. The average is:

$$\text{Br}(B^\pm \rightarrow J/\psi + K^\pm, J/\psi \rightarrow \mu^+\mu^-)=(5.2\pm 1.2) \times 10^{-5}$$

In order to calculate the acceptance and the $b$ quark spectrum corresponding to the reconstructed $B$ mesons, a simple Monte Carlo was used. The $b$ quark spectrum was generated according to the NDE calculations$^4$, flat in rapidity for $|\eta| < 1.0$, the $b$ quark was then fragmented according to the Peterson fragmentation function$^{27}$. Finally, the $B^\pm$ was assumed to be produced 40% of the times. Applying the analysis requirements CDF finds that 90% of the reconstructed $B$’s come from $b$ quarks with $P_T > 10$ GeV/c.

The uncertainty on the branching ratio constitutes the major systematic error in the cross section determination. Other contributions come from uncertainties on $b$ quark fragmentation (10%), tracking efficiency (10%), trigger efficiency (12%), and other smaller contributions. The result is shown in Figure 12. All the CDF cross section measurements appear to be larger than the expectation from the NDE calculation. At $\sqrt{s} = 630$ GeV instead, the agreement seems to be very good (Figure 9).

### 3.2 $B^0 - \bar{B}^0$ MIXING

The phenomenon of flavor oscillation, which produces mixing, has been first observed in the $K^0$- $\bar{K}^0$ system. It arises from $\Delta S = 2$ transitions (box diagrams) that change the $K^0$ into a $\bar{K}^0$. These transitions are allowed because the weak interactions do not conserve flavor. The effect is observable because the mass eigenstates, $K_S$ and $K_L$, have a non zero mass difference, $\Delta M$, and the $K^0$ lifetime is long enough for a number of oscillations (period $2\pi/\Delta M$) to occur before the $K^0$ system decays.

Mixing is therefore characterized by the parameter

$$z = \Delta M/\Gamma$$

Since the $B$ lifetime is quite large, $B^0 - \bar{B}^0$ mixing is observable for even small values of $\Delta M$. The parameter $z$ is related to some of the Cabibbo-Kobayashi-Maskawa matrix elements and to the top mass. The UA1 experiment$^{28}$ reported first the observation of mixing, later confirmed by the ARGUS and CLEO experiments$^{29}$.

Mixing has been measured in events where both the $b$ and the $\bar{b}$ decay semileptonically, and the charge of the leptons tags the flavor of the $b$ quark. A like-sign lepton pair indicates that one of the mesons has changed into its antiparticle. The magnitude of mixing is then measured...
by determining the ratio, \( R \), of like-sign (LS) to opposite-sign (OP) leptons. LS leptons can also be the result of a sequential \( b \) decay (i.e., \( b \to c \to \ell \)), therefore this has to be taken into account.

The mixing parameter \( \chi \) gives the probability of a \( B^0 \) hadron to transform into its antiparticle. It is defined as:

\[
\chi = \frac{2(1 - \chi) + [(1 - \chi)^2 + \chi^2] f_s}{[(1 - \chi)^2 + \chi^2] + 2(1 - \chi) f_s + f_c}
\]

where the denominator includes all possible hadrons formed by the \( b \) quark. The relation between \( R \) and \( \chi \) is:

\[
R = \frac{N_{LS}}{N_{OS}} = \frac{2\chi(1 - \chi) + [(1 - \chi)^2 + \chi^2] f_s}{[(1 - \chi)^2 + \chi^2] + 2\chi(1 - \chi) f_s + f_c}
\]

with

\[
f_s = \frac{N_s}{N_f}
\]

\[
f_c = \frac{N_c}{N_f}
\]

where \( N_f \) is the number of first generation \( b \) decays, \( N_s \) the number of sequential decays, and \( N_c \) the number of events from \( c \bar{c} \) decays.

At the \( \Upsilon(4S) \) only \( B_d \) is produced, so CLEO and ARGUS measure \( \chi_d \), whereas at hadron colliders and LEP a combination of \( B_d \) and \( B_s \) is produced and therefore the quantity measured is:

\[
\chi = P_d \chi_d + P_s \chi_s
\]

where

\[
P_s = \text{Prob}(b \to B_s^0 \to \ell^-) \frac{BR(B_s^0 \to \ell^-)}{BR(b \to B \to \ell^-)}
\]

We will discuss here the recent results of the CDF\textsuperscript{30,24} and the UA1\textsuperscript{31} collaborations.

CDF uses both the \( ee \) and the \( e\mu \) channels for this analysis. Using \( e\mu \) events has the advantage that the rate is high (twice that for \( ee \) or \( \mu\mu \)) and that there is no background from other lepton pair production mechanisms: Drell-Yan (DY), \( J/\psi \), and \( T \). For the \( e\mu \) events the trigger used required an EM shower with \( E_T > 5 \) GeV and a muon with \( P_T > 3 \) GeV/c. For the \( ee \) sample the trigger required two electron clusters with \( E_T > 5 \) GeV.

![Figure 15](image)

Figure 15: The invariant mass of the \( e\mu \) system for like-sign (LS) and opposite sign (OP) pairs used by CDF for the study of mixing\textsuperscript{24,30}.

After applying the standard \( e \) and \( \mu \) selection criteria\textsuperscript{16,23}, the opposite sign lepton events coming from same side sequential \( b \) decays (i.e., \( b \to \ell^- c \to c \to \ell^- \)) are removed by rejecting events for which the \( \ell \ell \) invariant mass is \( M(\ell\ell) < 5 \) GeV. This distribution is shown in Figure 15 for the \( e\mu \) events. For the \( ee \) events this removes the background from the \( J/\psi \) region, whereas the \( \Upsilon \) region is explicitly removed by another mass cut. The number of events for the two channels are: 900 for the \( e\mu \) (346 LS and 554 OS), 241 for the \( ee \) (92 LS and 149 OS).

For the \( e\mu \) sample the major background comes from hadrons misidentified as leptons. This source contributes equally to the LS and OS samples. This has been studied using a sample of minimum-bias events, checked with data obtained with other \( e \) triggers and augmented by information extracted from the CDF Monte Carlo. It was found that the background fraction is \((20 \pm 10)\%\). After background removal the value of \( R \) is

\[
R = 0.552 \pm 0.049(\text{stat.}) \pm 0.039(\text{syst.})
\]

For the \( ee \) events the backgrounds come from DY, photon conversions, Dalitz decays and from misidentified hadrons. Detailed studies of these background sources remove \(45 \pm 15\) OS events and \(11 \pm 4\) LS events from the sample. The
result for $R$ is

$$R = 0.587 \pm 0.113 \text{(stat)} \pm 0.043 \text{(sys)}$$

In the absence of mixing the expected values of $R$ would be $0.23 \pm 0.06$ for the $e\mu$ channel and $0.24 \pm 0.07$ for the $ee$ channel.

In order to extract $\chi$ from the $R$ measurements using Eq. 3, it is necessary to calculate $f_s$ and $f_e$ for the two samples. This is done by using the ISAJET~Monte Carlo and the CDF detector simulation. The ratio of second to first generation semileptonic decays is found to be $f_s = 0.25 \pm 0.06$ for both channels. The error includes systematic uncertainties from $b$ fragmentation, semileptonic branching ratios, and $b\bar{b}$ correlations coming from higher order processes. The ratio of charm to first generation $b$ semileptonic decays, $f_c$, is found to be $0.07 \pm 0.07$ for the $e\mu$ events and $0.02 \pm 0.02$ for the $ee$ channel.

These results lead to a combined value for $\chi$ of

$$\chi = 0.177 \pm 0.032 \text{(stat+sys)} \pm 0.032 \text{ (Monte Carlo)}$$

Figure 16 shows the observed $\mu$ spectra for the LS and OS $e\mu$ events compared with the Monte Carlo predictions.

The UA1 collaboration~used di-muon events obtained in $4.7 \text{ pb}^{-1}$ of data collected in the 1988-89 run. Muons are required to have $P_T > 3 \text{ GeV/cm}$ and to be within the $|\eta| < 2.5$ region. The muons are also required to be non-isolated and have associated jet activities, with the jet axis being within a cone of $\Delta R = 1.0$ with the muon. Again the variable $P_T^{rel}$ is used. There are 889 events left after all cuts, of which 537 are LS and 352 are OS.

The ISAJET~Monte Carlo and the UA1 detector simulation are used to determine the shape of the $P_T^{rel}$ distributions for the background, charm and sequential decays. These distributions are then used to fit the data with a maximum likelihood method. Absolute normalization for the background comes from the data. The DY and $t\bar{t}$ background are obtained from data and Monte Carlo. The background is found to be $(37.0 \pm 9.2)$% of the data, the $c\bar{c}$ contribution is $(11.0 \pm 5.5)$% of the OS events and the DY is $(1.2 \pm 0.2)$% of the OS events. Figure 17 shows the fits to the $P_T^{rel}$ distributions for the lower and higher $P_T$ muons. The final result of the analysis averaged with the previous UA1 result~gives:

$$\chi = 0.148 \pm 0.029 \text{(stat)} \pm 0.017 \text{(sys)} \text{ (UA1)}$$

Recent measurements from LEP experiments~give:

$$\chi = 0.139_{-0.026}^{+0.027} \text{ (ALEPH)}$$

$$\chi = 0.178_{-0.040}^{+0.040} \text{ (L3)}$$

The next challenge is to obtain $\tau_\sigma$ which is related to $\chi_\sigma$ by the relation:

$$\tau_\sigma = \sqrt{2\chi/(1 - 2\chi)}$$

The average of the CLEO and ARGUS results~gives $\tau_d = 0.72 \pm 0.13$. The Standard Model gives the relation~

$$\frac{\tau_\sigma}{\tau_d} = \left[ \frac{f_{B_s}}{f_{B_d}} \right]^2 \left[ \frac{V_{ts}}{V_{td}} \right]^2$$

where the $f_i$ are form factors and $V_i$ are CKM matrix elements. A limit on this ratio~from present fits of the
CKM matrix parameters using existing data is:
\[ x_s > 6.9 \]  
this implies that \( x_s \) is quite large.

In order to measure \( x_s \) we need to know \( P_s \) and \( P_d \) in Eq. 3. Assuming \( P_d = 0.375 \) and \( P_s = 0.150 \), it is possible to draw the curve in Figure 18, which shows the average of the ARGUS and CLEO results and the CDF result. This shows that from the Standard Model (Eqs. 6, 7) and the CLEO-ARGUS results, the allowed region is very small and that \( x_s \) is expected to be close to the maximum value of 0.5, i.e., that mixing in the \( B_s \) system is very large. The present measurements of \( x_s \), however, have very large uncertainties and are very far from testing the Standard Model. Clearly, measurements of \( P_d \) and \( P_s \) and much larger statistics or different methods will be needed. For example, the study of oscillations in the time dependence of \( B_s \) decays would provide a direct measurement of \( x_s \).

### 3.3 Rare B Decays

Both UA1 and CDF have implemented di-muon triggers that provide good statistics on \( J/\psi \) as well as on higher mass di-muons. This allows the study of rare decay modes like:

\[ B \to \mu\mu \quad \text{and} \quad B \to \mu\mu + X \]

These transitions occur via flavor changing neutral currents (FCNC), which are allowed at the one loop level through the penguin diagrams. For \( B \to \mu\mu \) the box diagram also contributes, and the branching ratio is expected to be of the order of \( 10^{-3} - 10^{-8} \) (for a top mass in the 100-200 GeV range).

CDF measured the \( B \to \mu\mu \) branching ratio by comparing its rate to the rate for \( \psi' \to \mu\mu \). The sample used has been discussed in Sec. 3.1.2 and the data has been shown in Figure 13. The \( \mu\mu \) invariant mass for the \( \psi' \) and the \( B \) regions are shown in Figure 19. The fitted curves give \( N_{\psi'} = 72 \pm 17 \) events and \( N(B \to \mu\mu) = 0.28 \pm 0.15 \) events above background. This corresponds to \( N < 12 \) (at 90% C.L.).

To obtain an absolute branching ratio the assumption is made that all the \( \psi' \) come from \( B \) decays. This assumption is based on the model by Glover et al. which predicts that direct \( pp \to \psi' + X \) production is very small. The ratio of
acceptances for the two channels is found to be about 4.
The $\psi'$ branching ratio, averaged from the CLEO\textsuperscript{36} and ARGUS\textsuperscript{36} results, and using the PDG value for $\psi' \rightarrow \mu\mu$, is

$$BR(B \rightarrow \psi') \times BR(\psi' \rightarrow \mu\mu) = (2.8 \pm 1.2) \times 10^{-5}$$

This gives

$$BR(B \rightarrow \mu\mu) < 3.2 \times 10^{-6} \ (90\%C.L.) \ CDF$$

The UA1 analysis\textsuperscript{37} is done on an integrated luminosity of 5.3 pb\textsuperscript{-1}, including the data discussed in Sec 3.1.1 and data taken in earlier runs. The $\mu\mu$ invariant mass for the region of interest is shown in Figure 20. Muon pairs with $P_T > 6$ GeV/c are used. In the B region they observe 6 events on a background of 5.0 ± 1.0 events. Using an efficiency in their acceptance region of (4.0 ± 1.7)% as calculated using the ISAJET Monte Carlo and the $b$ cross section measured by UA1 (see Sec. 3.1.1), they obtain

$$BR(B \rightarrow \mu\mu) < 8.3 \times 10^{-6} \ (90\%C.L.) \ UA1$$

For the $B \rightarrow \mu\mu + X_s$ search a $M(\mu\mu)$ mass region between 3.9 and 4.4 GeV is chosen, in order to avoid regions of interference between the matrix elements of the $B \rightarrow \psi'$ decay mode and the penguin diagrams, as discussed in the UA1 paper\textsuperscript{37}. This cut reduces the acceptance to (1.1 ± 0.3)%. UA1 observes 9 events on a background of 8.7 ± 1.7 and obtains:

$$BR(B \rightarrow \mu\mu X_s) < 5.0 \times 10^{-5} \ (90\%C.L.) \ UA1$$

With the same data UA1 also searched for $B \rightarrow \mu\mu K^{*0}$, by looking for a $K^{*0}$ signal in the associated tracks in a cone of $\Delta R = 1.0$ around the direction of the $\mu\mu$ system. The requirements on the two muons are less stringent to increase efficiency, the $K^*$ tracks are required to be above 100 MeV/c and the $K^*$ to have a $P_T > 2$ GeV/c. They observe two events in the data with a background of 1.0 ± 0.6 events. With an efficiency of (1.1 ± 0.3)% they obtain:

$$BR(B \rightarrow \mu\mu K^{*0}) < 2.3 \times 10^{-5} \ (90\%C.L.) \ UA1$$

The limits obtained by both CDF and UA1 are lower than the published results from ARGUS\textsuperscript{26} and CLEO\textsuperscript{38} of $5 \times 10^{-5}$ for $B^0 \rightarrow \mu\mu$, $2.4 \times 10^{-3}$ for $B^0 \rightarrow \mu\mu + X_s$ and $1.9 \times 10^{-4}$ for $B^0 \rightarrow \mu\mu K^{*0}$.

4.0 SUMMARY AND FUTURE PROSPECTS

The search for the top quark will be the domain of hadron colliders over the next few years. Present limits
For the Tevatron Collider run in 1992, CDF will have improved acceptance for the muon system and improved $b$ tagging capability using the silicon vertex detector (SVX), which is being installed. The integrated luminosity for the run is expected to increase the present CDF statistics by a factor five. A new detector, D0, will be taking data, thus increasing the overall chance of detecting the top. A mass reach of 130 GeV should be possible.

The $b$ physics potential of hadron colliders is becoming evident. The predicted cross sections are very large and measurements done by UA1 and CDF seem to confirm the QCD predictions. Mixing has been observed at hadron colliders first; the new results by both UA1 and CDF have been summarized here. Limits on rare decay modes reported by UA1 and CDF have improved existing limits from $e^+e^-$ machines by one order of magnitude in some cases. Prospects for studies of exclusive channels look very good.

$B$ physics capabilities for the next collider run should improve by large factors. CDF expects to gain by an order of magnitude in efficiency and has added capabilities in $b$ tagging due to the installation of the SVX. D0 has an excellent muon detector which can be exploited for $b$ tagging. Measurements of lifetimes for different $b$ charges and species should be possible, as well as studies of exclusive decay modes. The next collider run should also provide enough data to allow understanding on whether CP violation can be studied in hadron colliders.

7 REFERENCES


19. H. Wenzel, these Proceedings

