



Fermi National Accelerator Laboratory

FERMILAB-Conf-91/227

**Measurement of ρ , the Ratio of the Real to Imaginary
Part of the $\bar{p}p$ Forward Elastic Scattering Amplitude,
at $\sqrt{s} = 1.8$ TeV**

R. Rubinstein

*Fermi National Accelerator Laboratory
P.O. Box 500, Batavia, Illinois 60510*

August 1991

* Presented at *Particles and Fields '91*, University of Vancouver, Vancouver, British Columbia, Canada, August 18-22, 1991.



Operated by Universities Research Association Inc. under contract with the United States Department of Energy

MEASUREMENT OF ρ , THE RATIO OF THE REAL TO IMAGINARY
PART OF THE $\bar{p}p$ FORWARD ELASTIC SCATTERING AMPLITUDE,
AT $\sqrt{s} = 1.8$ TEV

ROY RUBINSTEIN
Fermi National Accelerator Laboratory
Batavia, Illinois 60510
(For the E-710 Collaboration*)

ABSTRACT

We have measured ρ , the ratio of the real to the imaginary part of the $\bar{p}p$ forward elastic scattering amplitude, at $\sqrt{s} = 1.8$ TeV. Our result, $\rho = 0.140 \pm 0.069$, is consistent with the expected value, and thus no new physics is required.

1. Introduction

Fits to $\bar{p}p$ and pp measurements of ρ and the total cross section σ_T available up to ISR energies have been used, together with dispersion relations, to predict values of ρ and σ_T at SPS and Tevatron Collider energies.^{1,2} The predictions for total cross sections were in agreement with measured values when they became available. However the SPS UA4 measurement³ at $\sqrt{s} = 546$ GeV of $\rho = 0.24 \pm 0.04$, was ~ 2.5 standard deviations from the expected value of ~ 0.14 . To explain a value of 0.24, some new physics is required, although some models were later ruled out by our subsequent measurement⁴ of σ_T at $\sqrt{s} = 1.8$ TeV.

2. Experimental Method

Our apparatus and event selection have been described in earlier publications⁴⁻⁷. Because our drift chamber horizontal (x) coordinate readouts (based on charge division) were known with substantially less accuracy than the vertical (y) coordinate readouts, we integrated over x and only used the y coordinate in our analysis. In order to determine ρ , elastic scattering was measured down to $|t| \sim 0.001(\text{GeV}/c)^2$, where the maximum interference between coulomb and nuclear scattering occurs.

We use the following expression for the observed elastic differential cross section.

$$\frac{1}{L} \frac{dN_{el}}{dt} = \frac{d\sigma}{dt} = \frac{4\pi\alpha^2(\hbar c)^2 G^4(t)}{|t|^2} + \frac{\alpha(\rho - \alpha\phi)\sigma_T G^2(t)}{|t|} e^{-B|t|/2} + \frac{\sigma_T^2(1+\rho^2)}{16\pi(\hbar c)^2} e^{-B|t|} \quad (1)$$

The three terms are due to, respectively, coulomb scattering, coulomb-nuclear interference, and nuclear scattering. L is the integrated accelerator luminosity; α is the fine structure constant, ϕ is the known relative coulomb-nuclear phase; $G(t)$ is the known nucleon electromagnetic form factor. We also use the following two equations:

$$\sigma_T^2 = \frac{1}{L} \frac{16\pi(\hbar c)^2}{(1+\rho^2)} \left. \frac{dN_{el}^n}{dt} \right|_{t=0} ; \quad \sigma_T = \frac{1}{L} (N_{el}^n + N_{inel}) \quad (2,3)$$

N_{el}^n is the total number of nuclear elastic events, obtained from the observed elastic distribution in the t region where nuclear scattering dominates, and extrapolated to $t = 0$ and $t = \infty$ using the form $\exp(-B|t|)$.

$\left. \frac{dN_{el}^n}{dt} \right|_{t=0}$ is the observed differential number of nuclear elastic events extrapolated to $t = 0$ using the same form. N_{inel} is the total number of inelastic events, obtained as described earlier.⁴ We use our elastic data and N_{inel} , together with Eqs. (1), (2) and (3), to obtain simultaneously σ_T , B and ρ . As explained earlier, this procedure was modified in practice, although not in principle, because instead of using measurements of

$\left. \frac{dN_{el}}{dt} \right|_{t=0}$ as input, we used $\frac{dN_{el}}{dy}$ where y is the vertical distance from the beam center, and where each y bin covers a range of t .

3. Results and Conclusions

The result obtained from the simultaneous fit to our data described above was

$$\rho = 0.140 \pm 0.069; B = 16.99 \pm 0.47 \text{ (GeV/c)}^{-2}; \sigma_T = 72.8 \pm 3.1 \text{ mb}$$

The new values of B and σ_T given above are consistent with our earlier published results.

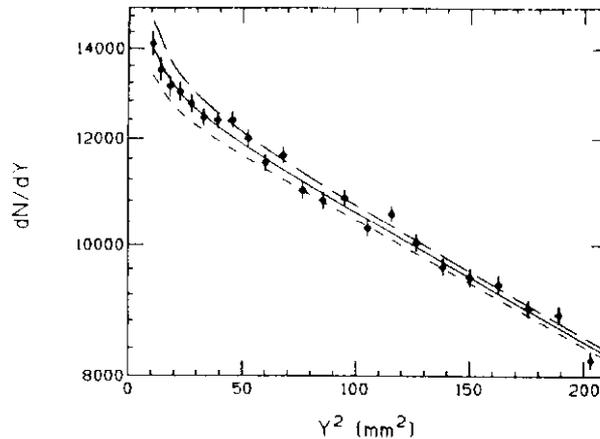


Fig. 1

We show in Fig. 1 our elastic data as a function y^2 , together with our fit, for only the small y^2 region. Also shown are two curves (long dashed for $\rho = 0.28$ and short dashed for $\rho = 0$) illustrating the effect of changing ρ , but keeping B and $\sigma_T(1+\rho^2)$ fixed. [Note that B and $\sigma_T(1+\rho^2)$ are essentially determined from the larger y data].

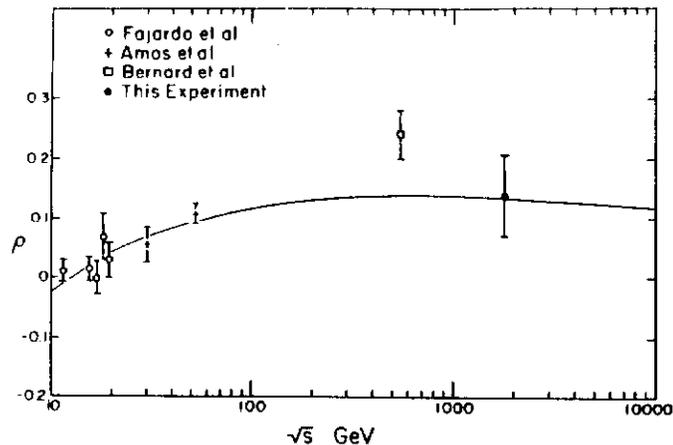


Fig. 2

Our result for ρ is shown in Fig. 2, together with results at lower energies^{3,8,9}, and a curve¹⁰ showing the dispersion relation prediction based on existing data except for the ρ value at $\sqrt{s} = 546$ GeV. It can be seen that our value of ρ is consistent with that expected, and thus our result does not require the addition of any new physics.

References

*N. A. Amos, C. Avila, W. F. Baker, M. Bertani, M. M. Block, D. A. Dimitroyannis, D. P. Eartly, R. W. Ellsworth, G. Giacomelli, B. Gomez, J. A. Goodman, C. M. Guss, A. J. Lennox, M. R. Mondardini, J. P. Negret, J. Orear, S. M. Pruss, R. Rubinstein, S. Sadr, J. C. Sanabria, S. Shukla, M. Spagnoli, I. Veronesi, and S. Zucchelli. (Universita di Bologna, Cornell University, Fermilab, University of Maryland, George Mason University, Northwestern University). This work was supported by the U.S. Department of Energy, the U.S. National Science Foundation, the Italian Ministero Pubblica Istruzione and the North Atlantic Treaty Organization.

1. U. Amaldi et al., *Phys Lett* **B66**, 390 (1977)
2. M. M. Block and R. N. Cahn, *Phys Lett* **B149**, 245 (1984); *Rev Mod Phys* **57**, 563 (1985)
3. D. Bernard et al., *Phys Lett* **B 198**, 583 (1985)
4. N. A. Amos et al., *Phys Lett* **B243**, 158 (1990)
5. N. A. Amos et al., *Phys Rev Lett* **61**, 525 (1988)
6. N. A. Amos et al., *Phys Rev Lett* **63**, 2784 (1989)
7. N. A. Amos et al., *Phys Lett* **B247**, 127 (1990)
8. L. Fajardo et al., *Phys Rev* **D24**, 46 (1981)
9. N. A. Amos et al., *Nucl Phys* **B262**, 689 (1985)
10. See Reference 2. The curve shown is taken from a later version, M. M. Block et al., *Phys Rev* **D41**, 978 (1990)