

Carl H. Albright  
Northern Illinois University, DeKalb, Illinois 60115  
and  
Fermi National Accelerator Laboratory, Batavia, Illinois 60510

Nilendra G. Deshpande  
University of Oregon, Eugene, Oregon 97403

John F. Gunion  
University of California, Davis, California 95616

Howard E. Haber  
University of California, Santa Cruz, California 95064

### Summary

The production process  $pp \rightarrow \ell \ell' + X$ , where the leptons belong to two different generations and X refers to spectator jets, provides a clear signature for horizontal (generation-changing) bosons when the leptons are emitted nearly back-to-back and  $p_T^{\text{miss}} = 0$ . Cross sections and  $p_T$  distributions for each lepton are presented, and discovery limits on  $M_H$  are extracted for several different channels.

Present experimental evidence suggests that flavor-changing neutral currents (FCNC's) are very rare. Their absence can be neatly interpreted to mean that the GIM mechanism operates at both the quark and lepton levels. However, since the replication of quark and lepton families is still not well understood, one cannot dismiss the possibility that neutral current interactions exist in nature which violate this apparent flavor conservation principle. In particular, the exchange of neutral "horizontal" bosons can directly couple two different generations and lead directly to FCNC's. The only restriction is that the coupling be weak enough that the effects of these interactions have so far escaped experimental detection.

In order to restrict the parameters of a horizontal boson theory, it is conventional<sup>1</sup> to assume that the overall gauge theory can be written as (or contains) the direct product  $G_S \times G_H$ , where  $G_S$  is the standard model gauge group for one generation and  $G_H$  is the horizontal group in question. Among the groups discussed in the literature<sup>2</sup> are  $SU(2)_H$  and  $SU(3)_H$ . In the  $SU(2)_H$  case, the 3 neutral generators effect the transitions  $\Delta G = 0, \pm 1$  among the three generations of quarks and leptons belonging to the adjoint representation. In the latter case, the 8 generators effect transitions among the three generations belonging to the fundamental representation of  $SU(3)_H$ .

It is also convenient to classify<sup>3</sup> the horizontal boson exchange processes as diagonal or non-diagonal, according to whether the boson couples two neutral currents of the same type (UU, DD, NN or LL) or different types (UD, UN, UL, NL, etc.). To the extent that the horizontal boson masses are degenerate,  $\Delta G \neq 0$  processes are forbidden in the limit that G is conserved and no generation mixing occurs. With generation-mixing angles present,  $\Delta G = \pm 1$  and  $\pm 2$  processes are also allowed since G-conserving transitions can still take place at each vertex connected by the horizontal boson exchanged.

Present experimental lower limits on the horizontal boson masses taken from the paper by Cahn and Harari<sup>2</sup> are listed in Table I as functions of the horizontal coupling  $g_H$  and generation-mixing angles.

In the limit of zero mixing, the processes  $\mu N \rightarrow e N$ ,  $\mu \rightarrow 3e$ ,  $\mu \rightarrow e \gamma$  and the mass difference  $\Delta M(K_L - K_S)$  yield no information. Limits for the two non-diagonal processes,  $K_L \rightarrow e \mu$  and  $K^+ \rightarrow \pi e \mu$ ,

$$M_H > 4.6 \text{ TeV} \left| \frac{g_H}{g_W} \right| \cos \beta_{LD} \quad (1)$$

$$M_H > 18 \text{ TeV} \left| \frac{g_H}{g_W} \right| \cos \beta_{LD}$$

are based on the experimental branching ratios\*

$$B(K_L \rightarrow e \mu) < 6 \times 10^{-6} \quad (2)$$

$$B(K^+ \rightarrow \pi^+ e \mu) < (5-7) \times 10^{-9}$$

respectively. The coupling  $g_H$  is scaled relative to the weak coupling  $g_W$  under the assumption that the  $K_L \rightarrow e \mu$  process takes place through a V-A coupling, while the  $K^+ \rightarrow \pi^+ e \mu$  decay occur through a pure V interaction. Here in both cases, the non-diagonal (DL) horizontal exchange process involves  $ds \rightarrow e \mu$ .

Table I. Present limits on horizontal boson masses  $M_H$  or  $\Delta$ , where  $\Delta^{-2} = M_H^{-2} - M^2$ , cf. Ref. 3.

Process	$ \Delta G $	Interaction	Lower Limit (TeV)
$K_L \rightarrow e \mu^\pm$	0	V-A	$M_H > 4.5 \left  \frac{g_H}{g_W} \right  \cos \beta_{LD}$
$K^+ \rightarrow \pi^+ e \mu^\pm$	0	V	$M_H > 18 \left  \frac{g_H}{g_W} \right  \cos \beta_{LD}$
$\mu N \rightarrow e N$	1	V	$M_H > 85 \left  \frac{g_H}{g_W} \right   \sin \beta_{LU} \sin \beta_{LD} ^{1/2}$
$\mu \rightarrow 3e$	1	V-A	$\Delta > 13 \left  \frac{g_H}{g_W} \right   \sin \beta_L \cos \beta_L ^{1/2}$
$\mu \rightarrow e \gamma$	1	V	$\Delta > 11 \left  \frac{g_H}{g_W} \right   \sin \beta_L \cos \beta_L ^{1/2}$
$\Delta M(K_L - K_S)$	2	V-A	$\Delta > 400 \left  \frac{g_H}{g_W} \right  \sin \beta_D$

The SSC will prove to be a very useful tool to extend these limits to other non-diagonal processes involving  $qq' \rightarrow \ell \ell'$  transitions. In particular, lepton pairs such as  $e \mu^\pm$ ,  $e \tau^\pm$ ,  $\mu \tau^\pm$  emitted nearly back-to-back by a massive real or virtual horizontal boson produced in the s channel would provide an exceptionally clear signal. This is especially so for  $e \mu$  events since  $p_T^{\text{miss}} = 0$  and the events are expected to be very quiet hadronically. No conventional theoretical background will contribute to pair production of different generation leptons with no missing  $p_T$ . For example, Drell-Yan production of  $\tau$

pairs followed by  $\tau$  decay into a  $\mu$  which carries most of the  $\tau$  momentum, while mimicing the signal, is orders of magnitude smaller in cross section in the Jacobian peak region even when the coupling  $g_H$  is of order  $g_W$ . Since the "alignment" of the quark and lepton families into a given generation is not fully understood, we shall present results for quark pair annihilations of the type  $ds, db, sb, uc, ut, ct$  and their conjugates into the various lepton channels listed above.

The matrix element for the subprocess  $qq' + H^0 \rightarrow l l'$ , where  $H$  is the horizontal boson, is written in analogy to the weak interaction case as

$$M = \frac{g_H^2}{2} \frac{1}{(s-M_H^2) + iM_H\Gamma_H} \bar{u}_l \gamma_\mu A \nu_l \bar{\nu}_{q'} \gamma_\mu A u_q, \quad (3)$$

where  $A = 1$  or  $1/2(1+\gamma_5)$  for a pure  $V$  or  $V-A$  interaction, respectively, and a standard resonance denominator is introduced. From this one obtains the color-averaged differential cross section

$$\frac{d\hat{\sigma}}{dt} = \frac{\pi}{3} \frac{\alpha_H^2}{(s-M_H^2)^2 + M_H^2\Gamma_H^2} \begin{cases} 1/2 (t^2 + u^2)/s^2, & V \\ q^2/s^2, & V-A \end{cases} \quad (4)$$

for the subprocess. The corresponding  $H^0$  partial decay rate is given by

$$\Gamma(H \rightarrow ab) = \begin{cases} 1/6 \alpha_H M_H, & V \\ 1/12 \alpha_H M_H, & V-A \end{cases} \quad (5)$$

where  $ab$  represents a lepton pair. A color factor of 3 must be included for each quark pair channel. The total width for the horizontal boson then involves 2 quark and 2 lepton channels or a factor of 8 for the  $SU(3)_H$  group and 4 quark and 4 lepton channels or a factor of 16 for the  $SU(2)_H$  group.

In computing the inclusive cross section for horizontal gauge boson production followed by decay to a specific leptonic channel, one convolutes the cross section  $d\hat{\sigma}/dt$  of (4) with quark distribution functions (we employ EHLQ<sup>s</sup> structure functions with  $\Lambda_{QCD} = 200$  MeV). We compute<sup>6</sup>

$$\sigma = \int_{-Y}^Y dy_1 \int_{-Y}^Y dy_2 \int_{p_T^{\min}}^{p_T^{\max}(y_1, y_2)} \frac{d\hat{\sigma}}{dy_1 dy_2 dp_T} \quad (6)$$

where  $d\hat{\sigma}/dy_1 dy_2 dp_T$  is the inclusive cross section for production of lepton 1 at rapidity and transverse momentum  $y_1$  and  $p_T$  and lepton 2 at rapidity and transverse momentum  $y_2$  and  $-p_T$  (intrinsic quark  $k_T$  is neglected). We have chosen  $Y = 3$  in order to guarantee that both leptons appear in a moderate sized detector. We have used  $p_T^{\min} = 50$  GeV in order to reduce large lepton backgrounds.<sup>7</sup>

Qualitatively, one finds  $\sigma$  rises smoothly as a function of  $\sqrt{s}$  and shows very little structure. We therefore quote results only for the  $\sqrt{s} = 40$  TeV design energy of the SSC. In Fig. 1 the pp cross sections are plotted as functions of  $M_H$  with  $V$  or  $A$  coupling at the production and decay vertices. The results for  $V-A$  coupling are nearly identical and are not shown. Fig. 1a depicts  $\sigma$  for the two channels<sup>8</sup>

$$d\bar{s} + u\bar{c} \rightarrow e^+ \mu^+ \quad (7a)$$

and

$$s\bar{d} + c\bar{u} \rightarrow \mu^- e^+ \quad (7a')$$

for three choices of  $\alpha_H = 1.0, 0.1$  and  $\alpha_W = 0.035$ .

## V OR A HORIZONTAL GAUGE BOSON

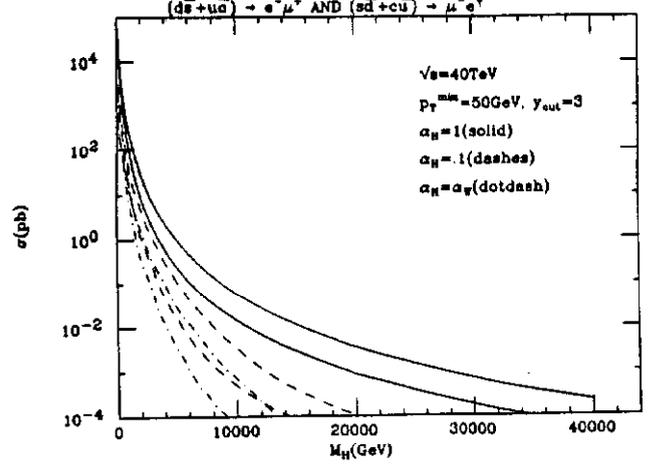


FIG. 1a.  $\sigma$  of Eq. (6) as a function of  $M_H$  for reaction (7a) and (7a') with  $V$  or  $A$  horizontal boson couplings. The higher curves of a given type are always those for process (7a).

Generation-mixing angles will be ignored throughout. The curves for (7a) lie higher due to the additional valence quark contributions which are not present in the (7a') case. With an integrated luminosity of  $10^{30} \text{ cm}^{-2}$ , the 35 event level corresponds to  $M_H$  values of 20, 10 and 7.8 TeV for (7a), while the charge conjugate process (7a'), involving only sea quarks, yields only 15, 7 and 5.5 TeV, for  $\alpha_H = 1.0, 0.1$  and  $\alpha_W$ , respectively. At the 5 event level, one is sensitive to  $M_H$  values 33, 15 and 11 TeV for (7a) and 24, 10 and 7.5 TeV for (7a'). Values for (7a) are listed in detail in Table II. The unequal discovery limits for two charge-conjugate channels in pp collisions can lead to an apparent charge asymmetry, i.e.,  $e^+ \mu^-$  vs.  $e^- \mu^+$ , and will help to confirm the nature of the signal. Such a charge asymmetry does not occur in pp reactions.

In Fig. 1b we compare the cross sections as a function of  $M_H$  for the three  $SU(3)_H$  channels (7a),

$$d\bar{b} + u\bar{t} \rightarrow e^+ \tau^+ \quad (7b)$$

and

$$s\bar{b} + c\bar{t} \rightarrow \mu^- \tau^+ \quad (7c)$$

Table II. Discovery limits on horizontal boson masses  $M_H$  with  $\sqrt{s} = 40$  TeV and  $\int d\tau dt = 10^{30} \text{ cm}^{-2}$ .

Process	$g_H$	35 Events	5 Events
$d\bar{s} + u\bar{c} \rightarrow e^+ \mu^+$	1.0	20 TeV	33 TeV
	0.1	10	15
	$\alpha_W$	7.8	11
$d\bar{b} + u\bar{t} \rightarrow e^+ \tau^+$	1.0	16	25
	0.1	8.3	12
	$\alpha_W$	6.4	9
$s\bar{b} + c\bar{t} \rightarrow \mu^- \tau^+$	1.0	9.7	16
	0.1	5	6.8
	$\alpha_W$	3.9	5
$d\bar{s} + s\bar{b} + u\bar{c} + c\bar{t} + e^+ \mu^- + \mu^+ \tau^-$	1.0	19	30
	0.1	11	17
	$\alpha_W$	8.1	12

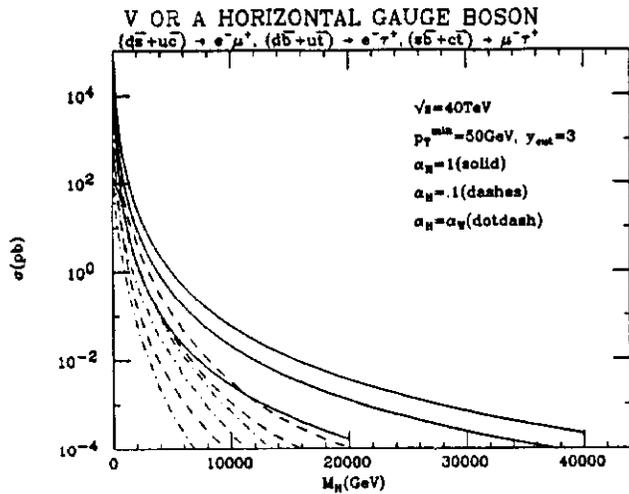


FIG. 1b.  $\sigma$  of Eq. (6) as a function of  $M_H$  for reaction (7a), (7b) and (7c) (V or A couplings). Curves of a given type follow the above process order.

The  $M_H$  discovery limits for (7b) and (7c) are somewhat smaller than those for (7a); on the other hand rare K decays yield no information for the (7b) and (7c) channels. Curves and limits for the  $SU(2)_H$  process involving

$$\bar{d}s + \bar{s}b + \bar{u}c + \bar{c}t + e^-\mu^+ + \mu^-\tau^+ \quad (8)$$

are similar to those for (7a); we give only the limits in Table II.

In order to be sensitive at the quoted  $M_H$  levels in reactions (7b), (7c) and (8), it is necessary that  $\tau$  identification be possible with good efficiency. For high mass horizontal bosons this can be achieved through vertex detection. At lower masses reconstructable  $\tau$  decay channels must be employed. Needless to say,  $e/\mu$  discrimination is required in order to distinguish horizontal gauge boson signals from those of new Z's.

In Fig. 2 the single lepton cross section,  $d\sigma/dy dp_T(|y_2| < Y)$ , is shown for process (7a) for  $y_1 = 0$  and 2 and three different pairings of  $\alpha_H$  and  $M_H$  chosen to correspond to the 35 event level in Table II. The  $p_T$  spectra for  $y_1 = 0$  clearly reflect the Jacobian peak at  $M_H/2$  for the more weakly coupled cases  $\alpha_H = 0.1$  and  $\alpha_H = \alpha_V$  for which the H width is significantly smaller than its mass. In general the distributions (which include effects from the full H propagator) are broad and demonstrate that the leptons carry off sizeable momentum, yielding hadronically quiet events and providing clear signatures for the horizontal boson processes.

In summary, the SSC will significantly extend the lower limits for the masses of hypothesized horizontal gauge bosons or, in fact, lead to their discovery as indicated above. However, the stringent limits on  $K_L \rightarrow \mu e$  imply that a horizontal gauge boson which mediates  $ds \rightarrow e\mu$  can not be observed at the SSC. Nonetheless, many other channels exist (such as  $uc \rightarrow e\mu$ ,  $ds \rightarrow \mu\tau$ , etc.) for which the SSC can either discover new FCNC's or significantly improve limits on the strength of FCNC transitions. Moreover, the present weak limits on FCNC's involving third generation fermions suggest that the tau has the potential of being a window of new physics beyond the standard model. As such, the large number of taus

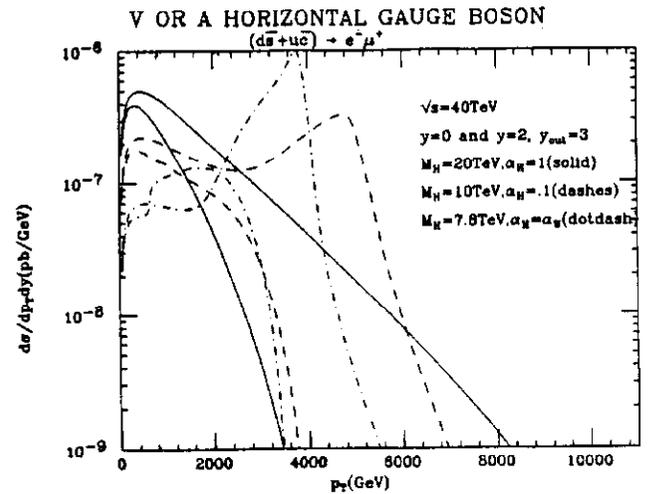


FIG. 2. Single lepton  $p_T$  distributions for reaction (7a) for three discovery limit pairings of  $\alpha_H$  and  $m_H$  (taken from Table II) at lepton rapidity  $y = 0$  and  $y = 2$ . The curves with the more restricted  $p_T$  range correspond to  $y = 2$ .

produced at the SSC could allow more stringent limits (or discovery) of rare decays, which would give an additional handle on the search for new horizontal gauge bosons.

#### Acknowledgments

We would like to acknowledge the helpful comments of other members of the "New W/Z" working group at Snowmass 1984. This work was supported in part by grants from the National Science Foundation (CHA and HEH) and contracts from the Department of Energy (NGD and JFG).

#### References

1. See, for example, F. Wilczek and A. Zee, Phys. Rev. Lett. **42**, 421 (1979).
2. T. Maehara and T. Yanagida, Prog. Theor. Phys. **60**, 822 (1978); *ibid.* **61**, 1434 (1979); F. Wilczek and A. Zee, ref. 1; H. Georgi, Nucl. Phys. **B186**, 126 (1979); E. Farhi and L. Susskind, Phys. Rev. **D20**, 3404 (1979); E. Eichten and K. Lane, Phys. Lett. **90B**, 125 (1980); R.N. Cahn and H. Harari, Nucl. Phys. **B176**, 135 (1980).
3. R.N. Cahn and H. Harari, ref. 2.
4. Particle Data Group, Phys. Lett. **111B** (1982).
5. E. Eichten, I. Hinchliffe, K. Lane and C. Quigg, Rev. of Mod. Phys., to be published.
6. See the lepton spectrum contribution by J.F. Gunion for more details.
7. J. Carr and E. Eichten, this Proceedings.
8. In many models the two processes  $d\bar{s} \rightarrow e\mu$  and  $uc \rightarrow e\mu$  are roughly equal numerically, but this need not be the case in general.