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## ABSTRACT

Hadron-nucleus elastic scattering is measured for  $\pi^{\pm}$ ,  $K^{\pm}$ ,  $p$  and  $\bar{p}$  scattering from Be, C, Al, Cu, Sn, and Pb targets at incident beam momenta of 70 and 175 GeV/c and for  $\pi^{+}$ ,  $K^{+}$ , and  $p$  scattering from Be, Al, and Pb targets at an incident beam momentum of 125 GeV/c. Parameterizations of  $d\sigma/dt$  in the forward direction for the reactions are presented.

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## INTRODUCTION

A measurement of hadron-nucleus elastic scattering is a fundamental one for any accelerator energy regime. In addition to testing theoretical approaches<sup>1,2</sup> to the scattering process, the data also provide valuable engineering information that aid in the design of high energy physics experiments. In this experiment the elastic scattering data include both interactions which leave the target nucleus in its ground state (coherent elastic scattering) and interactions which excite or break up the target nucleus (quasi-elastic scattering).

While data exist for hadron-nucleus elastic scattering at 20-30 GeV<sup>3,4</sup> and at 40 GeV,<sup>5</sup> we know of no comparable published measurements at higher energies for nuclear targets heavier than helium.<sup>6</sup> We have performed an experiment at Fermilab where we measured the distribution in  $t$ , the square of the four momentum transfer between the incident and forward scattered particle, for hadron-nucleus elastic scattering. Specifically, we studied  $\pi^+$ ,  $K^+$ ,  $p$ , and  $\bar{p}$  scattering from Be, C, Al, Cu, Sn, and Pb targets at incident beam momenta of 70 and 175 GeV/c and  $\pi^+$ ,  $K^+$ , and  $p$  scattering from Be, Al, and Pb targets at an incident beam momentum of 125 GeV/c. The  $t$  range covered varied with the incident momentum. In all cases the minimum  $-t$  is 0.001 (GeV/c)<sup>2</sup>; the maximum  $-t$  is 0.05, 0.15, 0.25 (GeV/c)<sup>2</sup> for incident beam momenta of 70, 125, and 175 GeV/c respectively.

We present parameterizations of  $d\sigma/dt$  in the very forward  $t$  region ( $0.001 < -t < 0.030$  (GeV/c)<sup>2</sup>). Hadron-nucleus elastic

scattering is concentrated in the forward direction; therefore this forward  $t$  region represents the bulk of the elastic scattering cross section. This is especially true as the atomic number of the nuclear target increases.

## APPARATUS

The experiment was performed in the M6 West beam line<sup>7</sup> at Fermilab. The apparatus, shown in Fig. 1, is a high resolution single arm spectrometer looking in the forward direction. The apparatus is described in detail in references 8 and 9; therefore this section reviews only the salient features.

The incident beam momentum was measured with a precision of 0.05% ( $\Delta p/p$ ), with a systematic uncertainty of  $\pm 0.25\%$ . The beam line was instrumented with four Cerenkov counters which allowed simultaneous identification of pions, kaons, and protons. Electrons and muons, a small fraction of the beam, were tagged at the downstream end of the experiment.

The detectors to measure the scattering angle and the nuclear target were mounted on a large reinforced concrete block to insure stability. The targets were placed in identical holders and precisely positioned in an evacuated pipe. This design allowed easy substitution of targets. Table I presents the properties of each nuclear target. At the upstream end of the concrete block were beam defining scintillation counters, B1 and B2, and a hole veto, VH1. Immediately downstream of the target were two scintillation counters, VH2 and VH3, used to suppress unwanted scatters from target electrons and hadronic inelastic scatters.

Two stations of high resolution, high pressure proportional wire chambers (PWCs)<sup>10</sup> on either side of the nuclear target (Stations 1-4 in Fig. 1) measured the scattering angle. At each station a measurement was made of the trajectory's x (horizontal) and y (vertical) coordinate. In addition, Station 3 also measured the u and v coordinate (rotated 45 and 135 degrees from the horizontal). The chambers had a 70  $\mu$ m resolution ( $\sigma$ ) and measured the scattering angle to an accuracy of 30  $\mu$ rad ( $\sigma$ ).

The spectrometer magnets used to determine the momentum of the scattered particle were two dipoles of the type used in the Fermilab main ring. Measurements of the integrated field length were made over the magnet aperture; these were uniform to 0.04%. A particle of the central momentum was bent 34 mrad in the horizontal plane. Using Station 6 (a pair of PWC's with an effective wire spacing of 1 mm) in conjunction with Stations 3 and 4, the outgoing momentum was measured to a precision of 0.1% ( $\Delta p/p_0$ ).

Finally a scintillation counter V was placed at the third focus, or veto plane, of the beam. The size<sup>9</sup> of this rectangular counter varied with the incident beam momentum and was chosen such that V vetoed unscattered beam tracks and scatters corresponding to  $-t < 0.001 \text{ (GeV/c)}^2$ .

#### DATA ACQUISITION

The data collection logic consisted of a two level trigger. The first level used the various scintillation counters of the apparatus; the second an analog device called the Hardware Focus Scatter Detector (HFSO).<sup>11</sup> An event satisfying both levels is referred to as a SCATTER. As the data acquisition system is described in detail in references 8 and 9, the system will be only briefly described here.

The basic criteria to pass the first level of the SCATTER trigger were

- 1) reasonable incoming beam trajectory defined as  $31 \cdot B2 \cdot VHI$  along with other beam defining counters, not shown in Fig. 1, located upstream of the concrete block,
- 2) proper particle identification by the Cerenkov counters,
- 3) no other incident particle detected within  $\pm 400 \text{ nsec}$  of the trigger,
- 4) the particle traversed the entire apparatus, and
- 5) no signal from the veto V at the third focus.

A second level of triggering was necessary since the first level was dominated by beam halo. The HFSO provided the second level to the SCATTER trigger. This analog device performed two tests using the track coordinates as measured in the high

resolution FWCs. Acting as a Hardware Focus Detector (HFD), the processor determined whether the track as extrapolated from the coordinates measured in the two high resolution FWCs upstream of the target intercepted a preset beam window in the veto plane. To pass the HFD test the track had to intercept the window in both the x and y projections. The second requirement was that the data from the two upstream and the most downstream high resolution chambers did not represent a colinear track. This test, with the processor in the Hardware Scatter Detector (HSD) mode, was required in only one projection. The analog processor took about 5  $\mu$ sec to make its decision.

There were two additional trigger types recorded along with the scattered events; in both, the HFSO requirement was not necessary. One was a specified fraction of SCATTER triggers without the HFSO requirement used to study the HFSO performance and any biases it may have introduced into the data. No such biases were found. The second, BEAM, was a sample of incident beam particles used to provide information for alignment and absolute normalization.

The online computer, a PDP15/40,<sup>12</sup> recorded approximately 500 triggers per one second spill. Typically 400 were SCATTERS; the rest were the other trigger types. The relative fraction of events recorded involving a particular projectile type was scaled to result in an apparatus live time of 60%.

#### DATA REDUCTION

We used the quantity  $q$  in the analysis where

$$q = \sqrt{-t} \approx P_b \theta \quad (1a)$$

where

$P_b$  = incident beam momentum

$\theta$  = scattering angle

and

$$d\sigma/dq = 2\sqrt{-t} d\sigma/dt \quad (1b)$$

There were two reasons for this choice. The first was that the resolution of the apparatus was constant in  $\theta$ , (30  $\mu$ rad;  $\sigma$ ). The second reason was that  $d\sigma/dq$  vs.  $q$  is a more slowly varying function than  $d\sigma/dt$  vs.  $t$ , thus reducing the sensitivity of the fitting procedure to the following effects: 1) integration of the cross section over the bin; 2) the migration of events from bin to bin due to resolution.

The data reduction process kept only those events with unambiguous single tracks before and after the nuclear target. The alignment procedure used a subset of BEAM events that had one and only one hit (a set of contiguous activated wires) per FWC. The target full and empty  $q$  distributions were normalized, and then a target empty subtraction was performed. The normalization was calculated using those BEAM events that traversed the entire

apparatus; thus there was no need to make any correction for the absorption of scattered particles downstream of the target or for overall PMC inefficiencies.

The major cuts applied to extract the elastic signal are given for some specific cases in Tables II and III. The number of events after cuts is presented in Table IV. The two cuts which eliminated the greatest fraction of triggers were the track reconstruction requirements on the PMC coordinates and that the scatter vertex was in the target region. The cut on the scatter vertex position eliminated a large fraction of events because the trigger accepted scatters originating from the high resolution PMCs immediately upstream and downstream of the target.

To extract the physics parameters of interest, a theoretical form of  $d\sigma/dq$  was corrected for the apparatus acceptance and then compared to the data. A Monte Carlo program calculated the acceptance as a function of  $q$ . Events were generated with the scattering vertex in the nuclear target with a flat distribution in  $q$  and then were traced through the apparatus. The incident beam phase space was provided by the beam tracks. Multiple scattering of the particle was simulated at the appropriate places and account was taken of any local PMC inefficiencies and of effects of the finite resolution. The acceptance was found to be projectile independent and is shown in Fig. 2 for one particular case.

To fit the data, we used a least squares' minimization procedure which employed the program MINUIT.<sup>13</sup> A theoretical cross section,  $d\sigma/dq$  (see next section), was convoluted with the acceptance. This convolution took into account migration of events from

one data bin to another. Next the convoluted theoretical form was compared to the quantity,  $\delta(q)$ , where

$$\delta(q) = \frac{N_s(q)}{I_o \cdot \Delta \cdot T} \quad (2)$$

where

- $N_s(q)$  = number of scattered particles in each  $q$  bin that pass all cuts
- $I_o$  = number of incident beam particles
- $\Delta$  =  $q$  bin size
- $T$  =  $N_{PM}/A$
- $N$  = Avogadro's number
- $\rho$  = target density
- $x$  = target length
- $A$  = atomic weight

The  $d\sigma/dt$  distribution was calculated as follows (using Eq.

(1b)):

$$d\sigma/dt = \delta(q)/2q \epsilon(q) \quad (3)$$

where

$\epsilon(q)$  = acceptance as a function of  $q$ .

## RESULTS

We parameterize the theoretical cross section as follows:

$$\frac{d\sigma}{dq} \Big|_{Th} = N_0 \left\{ \frac{2q}{\Gamma_w^2} \exp(-q^2/w^2) + \frac{8\pi e^4 z^2}{q^3} \cdot G_p^2 \cdot G_T^2 \left[ 1 - \frac{4w^2}{q^2} \left( 1 + \frac{2}{b^2} \left[ \frac{2q}{5w} \right] \right) \right]^{-1} + \frac{q G_A^2}{8\pi \hbar^2} \exp(-b_A q^2) + \frac{N_A q G_{hp}^2}{8\pi \hbar^2} \exp(b_p q^2) \right\} \quad (4)$$

where the Coulomb nuclear interference term is neglected, and

- $N_0$  = normalization factor
- $\hbar w$  = multiple Coulomb scattering parameters<sup>14</sup>
- $Z$  = atomic number
- $G_p$  = electromagnetic form factor of projectile<sup>15</sup>
- $G_T$  = electromagnetic form factor of nuclear target<sup>15</sup>
- $q_A$  = total cross section for projectile - nucleus scattering
- $b_A$  = forward slope for coherent projectile - nucleus elastic scattering
- $N_A$  = number of individual nucleons involved in incoherent projectile - nucleus scattering
- $q_{hp}$  = projectile - proton total cross section
- $b_p$  = forward slope of projectile - proton elastic scattering
- $r$  = as defined in Eq. 2

The terms in Eq. 4 represent the following processes. The first two terms represent single, plural, and multiple Coulomb scattering.<sup>16</sup> The third term describes coherent elastic scattering (from the nucleus as a whole); the fourth incoherent scattering (from individual nucleons). The incoherent scattering term represents interactions which excite or break up the nucleus (true elastic scattering leaves the nucleus in its ground state) but which are included in the elastic signal due to the apparatus' momentum resolution. The parameterization of the incoherent scattering follows the approach of Ref. 3. The parameters for the incoherent scattering term were taken from Ref. 3 and are given in Table V. The fitting program fits for  $N_0$ ,  $b_A$ , and  $q_A$  only.

Tables of  $d\sigma/dt$  for the reactions studied are given in Ref. 17. Figures 3 to 8 present  $d\sigma/dt$  distributions for some of the reactions measured. Figures 3 and 4 show  $d\sigma/dt$  distributions for proton scattering from the various targets (Be, C, Al, Cu, Sn, and Pb) at an incident momentum of 175 GeV/c. Figures 5 and 6 present the scattering from Be and Pb targets respectively of the various incident projectiles ( $\pi^+$ ,  $K^+$ ,  $p$ , and  $\bar{p}$ ) at an incident momentum of 175 GeV/c. Finally, figures 7 and 8 present the momentum dependence (incident momenta of 70, 125, and 175 GeV/c) of  $d\sigma/dt$  for proton scattering from Be and Pb targets respectively.

We note that as the atomic number of the target increases, the  $d\sigma/dt$  distributions become more sharply peaked. For the Cu, Sn, and Pb target data, a secondary maximum is observed. The position in  $t$  of the second maximum decreases for increasing atomic number

of the target. The shape of the  $t$  distributions does not depend in any significant manner on the incident beam momentum.

Table VI presents values of  $N_0$ ,  $b_A$ , and  $\sigma_A$  as derived from the fits. The solid lines in figures 3 to 8 present the results of these fits (using the parameterization of Eq. 4). Figure 9 shows the relative contribution of each term of Eq. 4 for two representative cases.

The systematic errors were calculated in the following manner. A series of fits were performed varying the cut on a particular kinematic variable (for example recoil mass squared) while keeping all other cuts constant. The systematic error was then defined as the absolute value of the range the parameters of interest (i.e.  $N_0$ ,  $b_A$ , and  $\sigma_A$ ) varied for the series of fits. In addition, we investigated the dependence of the results on the values of  $N_A$  and  $b_p$  in the incoherent scattering term (see Table V). A variation of 30% in  $N_A$  leads to negligible change in  $N_0$  and  $\sigma_A$ ; however there is some effect on  $b_A$ . This effect on  $b_A$  is 4% for Be, 3% for C, 2% for Al, 1% for Cu, 0.5% for Sn, and 0.25% for Pb. A variation of one unit in  $b_p$  has negligible effect on  $N_0$  and  $\sigma_A$  and, as compared to the effect due to the variation of  $N_A$ , a negligible effect on  $b_A$ .

The values of  $N_0$ ,  $\sigma_A$ , and  $b_A$  in Table VI give an excellent parameterization of our data. However the values of  $N_0$  differ from 1.0, and we interpret this as a systematic error on  $N_0$  (in addition to that shown in Table VI). Since  $\sigma_A$  and  $N_0$  are highly correlated (the correlation coefficient between  $N_0$  and  $\sigma_A$  range from 0.93 to 0.98), the values of  $\sigma_A$  have an additional uncertainty. This uncertainty, which is substantial when  $N_0$  is

significantly different from 1.0, is given in the brackets in Table VI. Note that this uncertainty is not symmetric. Also  $\sigma_A$  is derived assuming no Coulomb nuclear interference. An appreciable real part of the nuclear (coherent) scattering amplitude will affect the results for  $\sigma_A$ . The above statements do not apply to the determination of  $b_A$  because  $b_A$  and  $N_0$  are not highly correlated and the Coulomb nuclear interference term would only be important in the first few  $-t$  bins.

Table VII presents values  $b_A$  derived from fits over approximately the same  $t$  region for all reactions. Figures 10 to 15 present the values found for the forward slope for coherent hadron-nucleus scattering ( $b_A$ ) as a function of atomic weight. In general for a given beam momentum and nuclear target, the forward slope is steepest when the incident projectile is a proton or antiproton and the shallowest when the incident projectile is a kaon.

The data for the Cu, Sn, and Pb targets were fit substituting a Bessel function form for the exponential in the coherent term of Eq. 4 in order to attempt to fit beyond the first minimum exhibited by these data. The fits resulted in a large chi-squared per degree of freedom which implies a more sophisticated theoretical treatment<sup>12</sup> is necessary.



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- <sup>12</sup>Digital Equipment Corp., Maynard, Massachusetts.
- <sup>13</sup>F. James and M. Roos, CERN Computer 7600 Interim Program Library, D506 and D516.
- <sup>14</sup>The values of  $w$ , in units of  $(\text{GeV}/c)^{-2}$ , for the targets are 0.0031 (Be), 0.0034 (C), 0.0035 (Al), 0.0040 (Cu), 0.0047 (Sn), and 0.0038 (Pb). The values of  $\beta$  (unitless) for the targets are 12.03 (Be), 11.91 (C), 11.43 (Al), 11.08 (Cu), 10.77 (Sn), and 9.50 (Pb).

<sup>15</sup>  $G_P$  and  $G_T$  were taken as follows:

$$G_P = (1 + (.8)^2 q^2 / 12h^2)^{-2}$$

$G_T = \exp(q^2 R^2 / 6h^2)$  where  $R$  is the electromagnetic radius of the target nucleus (see Table V for values of  $R$  used). It was found that if a monopole form for the form factor was used for the pions and kaons, there was negligible effect on the fit results.

<sup>16</sup> "The Real Part of the Forward Nuclear Amplitude of Hadron - Proton Elastic Scattering Between 70 and 200 GeV/c," L. A. Fajardo, to be submitted as thesis, Yale University; H. A. Bethe, Phys. Rev. 89, 1256 (1953).

<sup>17</sup> "Hadron-Nucleus Elastic Scattering at 70, 125, and 175 GeV/c and A High Statistics Study of Hadron-Proton Elastic Scattering at 200 GeV/c," A. Schiz, to be submitted as thesis, Yale University.

<sup>18</sup> The solid lines in figures 3 to 8 are calculated as follows: the theoretical form of  $d\sigma/dt$  is convoluted by the acceptance and resolution of the apparatus. This convoluted form is then divided by the acceptance to get the fit results as shown in the figures. The fit results still exhibit effects of the apparatus resolution and therefore are not completely smooth.

TABLE I

Nuclear Target Parameters

Target	Z	A (amu)	Diameter (cm)	Length (cm)	Density (g/cm <sup>3</sup> )	Radiation Length, $L_R$ (g/cm <sup>2</sup> )	$L/L_R$
Be	4	9.01	5.40	1.600	1.85	65.19	0.045
C	6	12.01	5.73	1.259	1.64	42.70	0.048
Al	18	26.93	6.02	0.401	2.73	24.01	0.046
Cu	29	63.55	6.32	0.080	8.96	12.86	0.056
Sn	50	118.69	6.32	0.084	7.31	8.82	0.070
Pb	82	207.19	6.63	0.026	11.35	6.37	0.046

TABLE II  
CUTS TO EXTRACT ELASTIC SIGNAL  
Be +175 GeV/c

	Fraction of Events Remaining After Cut		
	$\pi^+$	$K^+$	p
1). Track reconstruction requirements on PWC coordinates.	.741	.741	.741
2). HFD test passed.	.734	.736	.736
3). Muon Detector does not signal presence of a muon.	.658	.614	.695
4). No count from VH2 and VH3	.626	.585	.657
5). Outgoing particle trajectory traversed the area inside spectrometer magnet apertures.	.623	.583	.654
6). $[7.9]^2 \leq \text{recoil mass squared} \leq [8.8 \text{ (GeV/c}^2)]^2$ .	.596	.554	.624
7). HSD test passed.	.575	.532	.607
8). Scatter vertex in target region.	.292	.258	.363
9). Outgoing particle trajectory passed $\geq 0.5$ mm from edges of V	.282	.249	.354
10). Track $\leq 1.5$ cm from center of PWC station 4.	.281	.248	.353
11). Events whose trajectories were in region of $> 90\%$ efficiency in PWC station 4.	.280	.247	.351

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TABLE III  
CUTS TO EXTRACT ELASTIC SIGNAL  
Pb +175 GeV/c

Cut	Fraction of Events Remaining After Cut		
	$\pi^+$	$K^+$	p
1). Track reconstruction requirements on PWC coordinates.	.721	.721	.721
2). HFD test passed.	.708	.718	.715
3). Muon Detector does not signal presence of a muon.	.636	.592	.680
4). No count from VH2 and VH3	.631	.587	.673
5). Outgoing particle trajectory traversed the area inside of spectrometer magnet apertures.	.630	.587	.673
6). $[192.6]^2 \leq \text{recoil mass squared} \leq [193.4 \text{ (GeV/c}^2)]^2$ .	.601	.556	.638
7). HSD test passed.	.571	.527	.608
8). Scatter vertex in target region.	.181	.172	.182
9). Outgoing particle trajectory passed $\geq 0.5$ mm from edges of V	.170	.162	.171
10). Track $\leq 1.5$ cm from center of PWC station 4.	.170	.162	.171
11). Events whose trajectories were in region of $> 90\%$ efficiency in PWC station 4.	.170	.162	.171

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TABLE IV  
HADRON-NUCLEUS ELASTIC SCATTERING EVENT TOTALS  
(in thousands)  
for  $-t > -t_{\min} \text{ (GeV/c)}^2$

Momentum (GeV/c)	Target	$\pi^+$	$K^+$	$p^+$	$\pi^-$	$K^-$	$\bar{p}$
175	Be	16.4	7.6	38.0	11.8	4.5	1.5
$(t_{\min} =$	C	18.5	9.0	41.2	9.2	3.4	1.1
$-.0018 \text{ (GeV/c)}^2)$	Al	12.0	6.0	23.8	5.1	1.9	0.5
	Cu	8.9	4.5	14.9	6.8	2.7	0.6
	Sn	12.6	6.9	18.9	8.8	3.6	0.7
	Pb	12.3	7.0	17.1	8.8	3.9	0.7
125	Be	9.4	3.7	23.3	-	-	-
$(t_{\min} =$	Al	11.5	6.6	23.3	-	-	-
$-.0016 \text{ (GeV/c)}^2)$	Pb	9.6	6.9	14.0	-	-	-
70	Be	8.2	4.1	13.7	10.0	4.4	8.1
$(t_{\min} =$	C	7.3	3.8	11.7	8.8	4.3	6.7
$-.0013 \text{ (GeV/c)}^2)$	Al	11.5	6.1	15.0	13.8	13.7	19.1
	Cu	11.0	6.4	11.0	8.2	8.4	9.2
	Sn	15.8	9.5	16.2	15.5	16.6	15.6
	Pb	9.8	6.1	8.9	7.1	7.6	6.4

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TABLE V  
INCOHERENT SCATTERING TERM PARAMETERS AND NUCLEAR CHARGE RADIUS, R

Reaction	Momentum (GeV/c)	$N_A$	$\sigma_{hp}^a$ (mb)	$b_p$ (GeV/c) <sup>-2</sup>	R (fm)
$\pi^\pm, K^\pm$ -Be	175, 125, 70	3.5	25., 20.	10.	2.20
$p, \bar{p}$ -Be	"	3.5	40.	12.	2.20
$\pi^\pm, K^\pm$ -C	175, 70	3.4	25., 20.	10.	2.42
$p, \bar{p}$ -C	"	3.4	40.	12.	2.42
$\pi^\pm, K^\pm$ -Al	175, 125, 70	4.5	25., 20.	10.	3.02
$p, \bar{p}$ -Al	"	4.5	40.	12.	3.02
$\pi^\pm, K^\pm$ -Cu	175, 70	6.7	25., 20.	10.	3.66
$p, \bar{p}$ -Cu	"	6.7	40.	12.	3.66
$\pi^\pm, K^\pm$ -Sn	175, 70	8.2	25., 20.	10.	4.55
$p, \bar{p}$ -Sn	"	8.2	40.	12.	4.55
$\pi^\pm, K^\pm$ -Pb	175, 125, 70	9.5	25., 20.	10.	5.42
$p, \bar{p}$ -Pb	"	9.5	40.	12.	5.42

<sup>a</sup>Second entry refers to Kaon case

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TABLE VI

Values of  $N_0$  (overall normalization),  $b_A$  (forward slope for hadron-nucleus coherent scattering), and  $\sigma_A$  (total cross section for hadron-nucleus scattering) as obtained from the fits. Systematic errors are in parenthesis. There is an additional uncertainty on  $b_A$  of  $\pm 4\%$  for Be,  $\pm 3\%$  for C,  $\pm 2\%$  for Al,  $\pm 1\%$  for Cu,  $\pm 0.5\%$  for Sn, and  $\pm 0.25\%$  for Pb, which is due to uncertainty in the values used in the parameterization of the incoherent scattering term in Eq. 4 (see text).

175 GeV/c:  $\pi^+$ ,  $K^+$ , p

	$ t $ Range (GeV/c) <sup>2</sup>	$N_0$	$\sigma_A$ (mb)		$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^+$ -Be	.0018-.0330	.86 $\pm$ .05(.04)	182.2 $\pm$ 7.2( 10.0) [ -13.2] <sup>a</sup>		64.9 $\pm$ 1.5(3.0)	18.0/18
$K^+$ -Be	.0018-.0330	.86 $\pm$ .05(.06)	149.3 $\pm$ 7.4( 8.0) [ -10.8]		58.0 $\pm$ 2.2(2.0)	20.1/18
p -Be	.0018-.0330	1.08 $\pm$ .06(.05)	249.2 $\pm$ 8.3( 10.0) [ 9.8]		74.7 $\pm$ 1.0(1.5)	20.3/18
$\pi^+$ -C	.0018-.0330	.82 $\pm$ .04(.04)	244.9 $\pm$ 7.5( 12.0) [ -23.1]		67.6 $\pm$ 1.3(3.0)	21.0/18
$K^+$ -C	.0018-.0330	.87 $\pm$ .04(.03)	195.4 $\pm$ 7.5( 5.0) [ -13.1]		60.4 $\pm$ 2.0(2.0)	18.3/18
p -C	.0018-.0330	.91 $\pm$ .04(.03)	345.2 $\pm$ 9.9( 15.0) [ -15.9]		74.0 $\pm$ 1.0(3.0)	21.6/18
$\pi^+$ -Al	.0018-.0330	.76 $\pm$ .04(.05)	507.8 $\pm$ 16.9( 15.0) [ -25.1]		106.9 $\pm$ 2.0(2.0)	22.1/18
$K^+$ -Al	.0018-.0330	.80 $\pm$ .04(.02)	442.1 $\pm$ 19.4( 10.0) [ -46.7]		108.6 $\pm$ 3.0(2.0)	22.5/18
p -Al	.0018-.0330	.72 $\pm$ .04(.03)	764.3 $\pm$ 23.5( 15.0) [ -115.8]		120.3 $\pm$ 1.5(2.0)	21.9/18
$\pi^+$ -Cu	.0018-.0195	.73 $\pm$ .03(.04)	1117.4 $\pm$ 47.9( 40.0) [ -162.8]		190.3 $\pm$ 4.8(3.0)	13.4/12
$K^+$ -Cu	.0018-.0195	.73 $\pm$ .04(.06)	926.1 $\pm$ 54.0( 45.0) [ -134.8]		185.3 $\pm$ 7.4(3.0)	9.5/12
p -Cu	.0018-.0195	.54 $\pm$ .03(.05)	1835.0 $\pm$ 79.9( 60.0) [ -486.6]		217.8 $\pm$ 3.2(2.0)	14.2/12
$\pi^+$ -Sn	.0018-.0160	.62 $\pm$ .03(.04)	2320.3 $\pm$ 102.0( 80.0) [ -493.2]		312.9 $\pm$ 6.2(3.0)	11.7/10
$K^+$ -Sn	.0018-.0160	.69 $\pm$ .03(.03)	1933.9 $\pm$ 106.4( 50.0) [ -327.5]		309.8 $\pm$ 8.7(3.0)	12.8/10
p -Sn	.0018-.0160	.47 $\pm$ .03(.05)	3465.6 $\pm$ 157.6( 130.0) [ -1089.9]		338.3 $\pm$ 4.6(3.0)	13.1/10
$\pi^+$ -Pb	.0018-.0096	.61 $\pm$ .04(.03)	3818.4 $\pm$ 279.3( 150.0) [ -836.0]		436.7 $\pm$ 15.5(8.0)	7.8/ 6
$K^+$ -Pb	.0018-.0096	.67 $\pm$ .04(.05)	3210.1 $\pm$ 286.7( 130.0) [ -582.5]		410.5 $\pm$ 20.9(7.0)	6.1/ 6
p -Pb	.0018-.0096	.55 $\pm$ .03(.05)	4803.3 $\pm$ 219.6( 80.0) [ -1241.0]		455.3 $\pm$ 10.1(5.0)	6.5/ 6

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TABLE VI (cont.)

125 GeV/c:  $\pi^+$ ,  $K^+$ , p

	$ t $ Range (GeV/c) <sup>2</sup>	$N_0$	$\sigma_A$ (mb)		$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^+$ -Be	.0016-.0306	.80 $\pm$ .06(.05)	190.3 $\pm$ 9.7( 6.0) [ -20.1] <sup>a</sup>		65.6 $\pm$ 2.1(1.0)	24.2/25
$K^+$ -Be	.0016-.0306	.88 $\pm$ .06(.03)	145.9 $\pm$ 8.1( 3.0) [ -9.0]		60.1 $\pm$ 2.4(1.0)	23.1/25
p -Be	.0016-.0306	.93 $\pm$ .07(.04)	269.0 $\pm$ 12.4( 8.0) [ -9.6]		70.7 $\pm$ 1.3(0.7)	27.4/25
$\pi^+$ -Al	.0016-.0306	.77 $\pm$ .04(.02)	521.4 $\pm$ 17.4( 11.0) [ -63.9]		108.1 $\pm$ 2.2(1.7)	27.2/25
$K^+$ -Al	.0016-.0306	.76 $\pm$ .04(.03)	442.0 $\pm$ 19.2( 15.0) [ -56.7]		102.5 $\pm$ 3.2(2.9)	26.0/25
p -Al	.0016-.0306	.70 $\pm$ .04(.02)	780.8 $\pm$ 25.9( 14.0) [ -127.6]		119.1 $\pm$ 1.5(1.8)	26.5/25
$\pi^+$ -Pb	.0016-.0100	.50 $\pm$ .04(.03)	4599.0 $\pm$ 349.3( 150.0) [ -1347.0]		448.1 $\pm$ 13.6(4.0)	4.8/10
$K^+$ -Pb	.0016-.0100	.59 $\pm$ .04(.03)	3864.7 $\pm$ 319.5( 175.0) [ -896.1]		436.2 $\pm$ 16.6(6.0)	9.7/10
p -Pb	.0016-.0100	.41 $\pm$ .04(.04)	6219.2 $\pm$ 461.0( 180.0) [ -2237.0]		475.3 $\pm$ 10.5(4.0)	11.0/10

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70 GeV/c:  $\pi^+$ ,  $K^+$ , p

$\pi^+$ -Be	.0013-.0324	1.00 $\pm$ .05(.04)	170.9 $\pm$ 6.7( 4.0) [ 0.0] <sup>a</sup>		65.1 $\pm$ 2.8(2.0)	32.2/45
$K^+$ -Be	.0013-.0324	1.02 $\pm$ .06(.03)	135.8 $\pm$ 6.9( 5.0) [ 1.4]		61.8 $\pm$ 4.4(6.0)	52.1/45
p -Be	.0013-.0324	1.06 $\pm$ .07(.02)	251.6 $\pm$ 10.8( 7.0) [ 7.4]		70.7 $\pm$ 4.8(3.0)	47.2/45
$\pi^+$ -C	.0013-.0324	.86 $\pm$ .04(.02)	237.8 $\pm$ 9.0( 6.0) [ -17.3]		63.5 $\pm$ 2.8(2.0)	44.1/45
$K^+$ -C	.0013-.0324	1.06 $\pm$ .05(.02)	167.6 $\pm$ 7.7( 7.0) [ 5.0]		58.7 $\pm$ 4.3(5.0)	46.6/45
p -C	.0013-.0324	1.00 $\pm$ .04(.03)	325.3 $\pm$ 7.5( 7.0) [ 0.0]		70.5 $\pm$ 2.4(2.0)	46.4/45

TABLE VI (cont.)

70 GeV/c:  $\pi^+$ ,  $K^+$ ,  $p$ 

	$ t $ Range (GeV/c) <sup>2</sup>	$N_0$	$\sigma_A$ (mb)		$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^+$ -Al	.0013-.0324	.85±.03(.04)	487.6± 13.8(10.0)	[ -38.1] <sup>a</sup>	107.0± 3.0(2.0)	33.8/45
$K^+$ -Al	.0013-.0324	.87±.03(.02)	408.9± 15.5( 8.0)	[ -27.5]	105.7± 4.4(2.0)	45.6/45
$p$ -Al	.0013-.0324	.82±.04(.03)	720.3± 22.6( 7.0)	[ -68.0]	118.8± 2.4(3.0)	50.7/45
$\pi^+$ -Cu	.0013-.0144	.77±.03(.02)	1090.6± 42.9(15.0)	[ -133.6]	187.4± 6.9(2.0)	26.8/27
$K^+$ -Cu	.0013-.0144	.79±.03(.02)	901.1± 47.6(15.0)	[ -100.2]	173.6±10.1(2.0)	25.9/27
$p$ -Cu	.0013-.0144	.70±.03(.02)	1477.5± 59.1(12.0)	[ -241.3]	184.0± 5.6(2.0)	28.2/27
$\pi^+$ -Sn	.0013-.0110	.73±.02(.02)	1905.2± 76.3(55.0)	[ -277.4]	259.4± 9.5(3.0)	14.1/22
$K^+$ -Sn	.0013-.0110	.79±.03(.02)	1512.2± 83.2(36.0)	[ -168.1]	229.8±13.9(4.0)	14.3/22
$p$ -Sn	.0013-.0110	.65±.03(.02)	2544.3±107.1(30.0)	[ -493.0]	283.5± 8.3(2.0)	26.8/22
$\pi^+$ -Pb	.0013-.0110	.65±.03(.01)	3795.5±220.1(20.0)	[ -735.5]	421.3±13.0(5.0)	21.6/22
$K^+$ -Pb	.0013-.0110	.75±.04(.02)	3028.9±231.9(50.0)	[ -405.8]	401.3±19.7(8.0)	24.4/22
$p$ -Pb	.0013-.0110	.62±.04(.01)	4348.2±273.0(45.0)	[ -924.4]	431.8±13.2(5.0)	23.8/22

70 GeV/c:  $\pi^-$ ,  $K^-$ ,  $\bar{p}$ 

$\pi^-$ -Be	.0013-.0324	.95±.04(.02)	165.9± 5.8( 2.0)	[ -4.2] <sup>a</sup>	61.0± 2.5(1.5)	45.9/46
$K^-$ -Be	.0013-.0324	.92±.05(.05)	150.7± 7.6(10.0)	[ -6.2]	69.7± 4.0(7.0)	47.2/46
$\bar{p}$ -Be	.0013-.0324	.90±.09(.06)	289.5± 17.6(10.0)	[ -14.9]	68.5± 3.6(4.0)	46.4/46

TABLE VI (cont.)

70 GeV/c:  $\pi^-$ ,  $K^-$ ,  $\bar{p}$ 

	$ t $ Range (GeV/c) <sup>2</sup>	$N_0$	$\sigma_A$ (mb)		$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^-$ -C	.0013-.0324	.88±.03(.02)	222.3± 7.4( 4.0)	[ -13.8] <sup>a</sup>	58.6± 2.6( 3.0)	45.8/45
$K^-$ -C	.0013-.0324	.93±.05(.03)	207.6± 9.5( 5.0)	[ -7.4]	68.2± 4.1( 3.0)	51.7/45
$\bar{p}$ -C	.0013-.0324	.82±.08(.04)	391.7± 23.1( 8.0)	[ -37.0]	72.3± 2.6( 4.0)	50.6/45
$\pi^-$ -Al	.0013-.0324	.79±.02(.02)	483.9± 12.4( 5.0)	[ -53.8]	103.8± 2.7( 1.5)	37.8/45
$K^-$ -Al	.0013-.0324	.84±.02(.03)	428.8± 11.4( 6.0)	[ -35.7]	103.3± 3.1( 3.0)	49.2/45
$\bar{p}$ -Al	.0013-.0324	.63±.03(.04)	868.8± 28.7( 11.0)	[ -179.2]	121.7± 2.0( 2.0)	53.8/45
$\pi^-$ -Cu	.0013-.0144	.69±.03(.03)	1077.5± 40.8( 55.0)	[ -182.5]	172.4± 7.7( 3.0)	29.2/27
$K^-$ -Cu	.0013-.0144	.77±.03(.03)	900.4± 40.6( 55.0)	[ -110.3]	162.1± 8.5( 4.0)	16.4/27
$\bar{p}$ -Cu	.0013-.0144	.56±.04(.03)	1755.5± 90.9( 75.0)	[ -441.8]	199.3± 6.4( 3.0)	26.3/27
$\pi^-$ -Sn	.0013-.0110	.67±.02(.02)	1825.6± 73.5( 40.0)	[ -331.8]	253.9± 9.4( 3.0)	21.7/22
$K^-$ -Sn	.0013-.0110	.78±.02(.02)	1524.8± 62.2( 25.0)	[ -178.1]	237.8± 9.9( 3.0)	24.3/22
$\bar{p}$ -Sn	.0013-.0110	.61±.03(.02)	2649.1±113.1( 90.0)	[ -580.1]	282.0± 8.0( 3.0)	24.1/22
$\pi^-$ -Pb	.0013-.0110	.65±.03(.03)	3186.6±213.8( 40.0)	[ -617.5]	386.6±16.4( 4.0)	17.1/22
$K^-$ -Pb	.0013-.0110	.67±.03(.05)	3088.6±194.3( 60.0)	[ -560.5]	386.4±15.5( 5.0)	23.7/22
$\bar{p}$ -Pb	.0013-.0110	.44±.04(.03)	5616.4±408.7(150.0)	[ -1890.9]	461.6±13.7(10.0)	25.2/22

TABLE VI(cont.)  
175 GeV/c:  $\pi^-$ ,  $K^-$ ,  $\bar{p}$

	$ t $ Range, (GeV/c) <sup>2</sup>	$N_0$	$\sigma_A$ (mb)	$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^-$ -Be	.0018-.0333	.96±.06(.06)	168.4± 7.4( 7.0) [ -3.4] <sup>a</sup>	65.8± 1.8( 4.0)	20.9/18
$\pi^-$ -Be	.0018-.0333	1.21±.09(.05)	128.0± 7.5( 5.0) [ 12.8]	61.6± 3.1( 2.0)	11.1/18
$\pi^-$ -Be	.0018-.0333	1.64±.31(.20)	191.0± 25.1( 16.0) [ 53.6]	79.0± 6.4( 4.0)	7.6/18
$\pi^-$ -C	.0018-.0333	.86±.05(.06)	237.1± 10.3( 7.0) [ -17.2]	67.5± 1.9( 2.0)	20.3/18
$\pi^-$ -C	.0018-.0333	1.05±.08(.06)	184.8± 11.3( 7.0) [ 4.6]	68.0± 3.6( 2.5)	20.1/18
$\pi^-$ -C	.0018-.0333	1.12±.26(.08)	317.6± 48.2( 15.0) [ 18.5]	79.6± 5.6( 2.0)	21.2/18
$\pi^-$ -Al	.0018-.0333	.83±.05(.06)	477.7± 23.4( 18.0) [ -42.5]	106.2± 3.2( 4.0)	19.5/18
$\pi^-$ -Al	.0018-.0333	.96±.08(.05)	378.7± 26.8( 10.0) [ -7.7]	94.3± 5.2( 3.0)	9.4/18
$\pi^-$ -Al	.0018-.0333	.15±.04(.10)	1820.9± 39.6( 60.0) [ -1115.7]	137.8± 4.3( 4.0)	24.8/18
$\pi^-$ -Cu	.0018-.0200	.63±.04(.05)	1208.9± 61.8( 45.0) [ -249.4]	193.4± 5.3( 2.0)	10.6/12
$\pi^-$ -Cu	.0018-.0200	.75±.05(.06)	978.7± 72.3( 40.0) [ -131.1]	193.8± 9.9( 3.0)	12.0/12
$\pi^-$ -Cu	.0018-.0200	.47±.19(.06)	2035.5± 507.4(100.0) [ -640.0]	225.9±15.3( 5.0)	13.0/12
$\pi^-$ -Sn	.0018-.0160	.55±.03(.02)	2310.8± 123.6( 70.0) [ -597.1]	299.1± 7.6( 3.0)	10.6/10
$\pi^-$ -Sn	.0018-.0160	.60±.05(.04)	2057.4± 163.9(120.0) [ -463.7]	294.4±12.5( 3.0)	9.7/10
$\pi^-$ -Sn	.0018-.0160	.31±.11(.08)	4469.9± 939.9(100.0) [ -1981.2]	348.9±20.8( 8.0)	12.3/10
$\pi^-$ -Pb	.0018-.0100	.59±.04(.06)	3594.9± 284.8(175.0) [ -833.6]	406.5±17.1( 9.0)	5.6/ 6
$\pi^-$ -Pb	.0018-.0100	.70±.06(.06)	3246.5± 365.6(280.0) [ -530.2]	418.6±25.9(18.0)	11.2/ 6
$\pi^-$ -Pb	.0018-.0100	.46±.17(.13)	5271.5±1772.6(400.0) [ -1696.2]	434.9±54.1(20.0)	6.8/ 6

<sup>a</sup> The numbers in square brackets represent the uncertainty in  $\sigma_A$  due to the deviation of  $N_0$  from unity. These uncertainties are not symmetric and are given by  $\frac{(1-N_0)}{|1-N_0|} (1-\sqrt{N_0}) \sigma_A$ . The uncertainty in the other direction is 0.0. If  $N_0$  is less (greater) than 1.0, then this uncertainty increases only the lower (upper) limit on  $\sigma_A$ .

	Momentum (GeV/c)	$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^+$ -Be	175	64.4± 2.7	2.3/ 8
$\pi^+$ -Be	175	57.2± 4.1	11.7/ 8
$\pi^+$ -Be	175	77.8± 2.5	9.1/ 8
$\pi^+$ -Be	175	63.3± 3.5	6.8/ 8
$\pi^+$ -Be	175	60.9± 5.6	3.7/ 8
$\pi^+$ -Be	175	75.4± 9.7	3.9/ 8
$\pi^+$ -C	175	62.3± 3.3	10.6/ 8
$\pi^+$ -C	175	57.5± 5.2	5.1/ 8
$\pi^+$ -C	175	74.1± 2.7	10.2/ 8
$\pi^+$ -C	175	65.4± 4.2	6.4/ 8
$\pi^+$ -C	175	59.8± 6.0	6.5/ 8
$\pi^+$ -C	175	85.5± 9.5	10.2/ 8
$\pi^+$ -Al	175	106.3± 4.8	10.3/ 8
$\pi^+$ -Al	175	111.1± 5.2	11.4/ 8
$\pi^+$ -Al	175	121.9± 2.6	10.3/ 8
$\pi^+$ -Al	175	109.2± 7.3	9.6/ 8
$\pi^+$ -Al	175	87.8± 9.4	10.9/ 8
$\pi^+$ -Al	175	131.4±10.7	8.5/ 8
$\pi^+$ -Al	175	186.9± 5.4	3.6/ 8
$\pi^+$ -Cu	175	183.6± 7.8	11.5/ 8
$\pi^+$ -Cu	175	217.4± 4.3	3.8/ 8
$\pi^+$ -Cu	175	192.8± 8.2	8.3/ 8
$\pi^+$ -Cu	175	192.7±13.1	7.2/ 8
$\pi^+$ -Cu	175	218.2±21.8	10.1/ 8
$\pi^+$ -Sn	175	308.1± 7.3	10.5/ 8
$\pi^+$ -Sn	175	299.8±11.2	12.1/ 8
$\pi^+$ -Sn	175	335.1± 5.3	4.1/ 8
$\pi^+$ -Sn	175	297.6± 7.9	9.3/ 8
$\pi^+$ -Sn	175	293.8±13.2	10.6/ 8
$\pi^+$ -Sn	175	345.5±21.6	8.2/ 8
$\pi^+$ -Pb	175	435.2±15.2	6.1/ 8
$\pi^+$ -Pb	175	411.6±20.1	7.2/ 8
$\pi^+$ -Pb	175	455.7± 9.8	6.2/ 8
$\pi^+$ -Pb	175	407.2±16.8	10.7/ 8
$\pi^+$ -Pb	175	419.3±25.4	7.4/ 8
$\pi^+$ -Pb	175	433.9±53.2	15.7/12
$\pi^+$ -Be	125	64.1± 3.9	10.6/12
$\pi^+$ -Be	125	57.8± 5.2	14.3/12
$\pi^+$ -Be	125	71.5± 3.3	9.3/12
$\pi^+$ -Al	125	110.1± 4.4	11.9/12
$\pi^+$ -Al	125	98.2± 5.1	13.7/12

TABLE VII  
Values of forward slope for hadron-nucleus coherent scattering,  $b_A$ , of  $d\sigma/dt$  in the region of  $0.0018 < -t < 0.0100$  (GeV/c)<sup>2</sup>

TABLE VII (cont.)

	Momentum (GeV/c)	$b_A$ (GeV/c) <sup>-2</sup>	$\chi^2/\text{DOF}$
$\pi^+$ -Pb	125	449.4 $\pm$ 13.3	5.5/12
$K^+$ -Pb	125	435.3 $\pm$ 16.4	10.3/12
$p$ -Pb	125	475.9 $\pm$ 10.1	12.7/12
$\pi^+$ -Be	70	65.0 $\pm$ 3.5	8.7/21
$K^+$ -Be	70	60.9 $\pm$ 5.3	22.1/21
$p$ -Be	70	71.9 $\pm$ 6.3	23.9/21
$\pi^-$ -Be	70	60.3 $\pm$ 5.3	20.2/21
$K^-$ -Be	70	64.8 $\pm$ 7.3	24.9/21
$p$ -Be	70	68.9 $\pm$ 6.5	19.6/21
$\pi^+$ -C	70	61.1 $\pm$ 4.3	13.7/21
$K^+$ -C	70	58.6 $\pm$ 6.7	16.1/21
$p$ -C	70	70.9 $\pm$ 3.8	24.2/21
$\pi^-$ -C	70	57.4 $\pm$ 5.6	26.3/21
$K^-$ -C	70	69.3 $\pm$ 6.6	24.0/21
$p$ -C	70	69.5 $\pm$ 3.5	25.6/21
$\pi^+$ -Al	70	107.6 $\pm$ 7.1	21.1/21
$K^+$ -Al	70	107.4 $\pm$ 8.2	15.6/21
$p$ -Al	70	117.0 $\pm$ 5.5	25.6/21
$\pi^-$ -Al	70	105.0 $\pm$ 4.4	14.8/21
$K^-$ -Al	70	102.4 $\pm$ 4.5	19.5/21
$p$ -Al	70	120.4 $\pm$ 3.8	21.0/21
$\pi^+$ -Cu	70	185.9 $\pm$ 7.9	23.8/21
$K^+$ -Cu	70	171.8 $\pm$ 11.1	23.3/21
$p$ -Cu	70	182.9 $\pm$ 6.3	25.7/21
$\pi^-$ -Cu	70	167.1 $\pm$ 8.2	18.8/21
$K^-$ -Cu	70	159.9 $\pm$ 9.9	13.4/21
$p$ -Cu	70	191.3 $\pm$ 9.5	15.8/21
$\pi^+$ -Sn	70	259.4 $\pm$ 7.8	12.4/21
$K^+$ -Sn	70	229.2 $\pm$ 12.1	13.8/21
$p$ -Sn	70	284.0 $\pm$ 7.4	25.1/21
$\pi^-$ -Sn	70	252.6 $\pm$ 9.7	19.1/21
$K^-$ -Sn	70	237.1 $\pm$ 10.3	24.8/21
$p$ -Sn	70	281.7 $\pm$ 8.5	26.4/21
$\pi^+$ -Pb	70	420.8 $\pm$ 12.7	21.3/21
$K^+$ -Pb	70	403.4 $\pm$ 18.8	25.2/21
$p$ -Pb	70	430.2 $\pm$ 12.9	23.5/21
$\pi^-$ -Pb	70	384.4 $\pm$ 15.7	15.9/21
$K^-$ -Pb	70	385.1 $\pm$ 15.3	22.3/21
$p$ -Pb	70	464.2 $\pm$ 13.2	24.8/21

FIGURE CAPTIONS

- Fig. 1: Experimental apparatus (not to scale left of vertical dashed line).
- Fig. 2: Apparatus acceptance for  $\pi^-$ ,  $K^-$ , and  $\bar{p}$  scattering from Pb at incident momentum of 70 GeV/c.
- Fig. 3:  $d\sigma/dt$  for elastic scattering at incident beam momentum of 175 GeV/c for the following: p-Be, p-C, p-Al; solid lines present results of a fit of the data to Eq. 4 (see text and footnote 18).
- Fig. 4:  $d\sigma/dt$  for elastic scattering at incident beam momentum of 175 GeV/c for the following: p-Cu, p-Sn; p-Pb; solid lines present results of a fit of the data to Eq. 4 (see text and footnote 18).
- Fig. 5:  $d\sigma/dt$  for elastic scattering at incident beam momentum of 175 GeV/c for the following: p-Be,  $\bar{p}$ -Be,  $K^+$ -Be,  $K^-$ -Be,  $\pi^+$ -Be,  $\pi^-$ -Be; solid lines present results of a fit of the data to Eq. 4 (see text and footnote 18).
- Fig. 6:  $d\sigma/dt$  for elastic scattering at incident beam momentum of 175 GeV/c for the following: p-Pb,  $\bar{p}$ -Pb,  $K^+$ -Pb,  $K^-$ -Pb,  $\pi^+$ -Pb,  $\pi^-$ -Pb; solid lines present results of a fit of the data to Eq. 4 (see text and footnote 18).
- Fig. 7:  $d\sigma/dt$  for p-Be elastic scattering at the following incident momenta: 175 GeV/c, 125 GeV/c, 70 GeV/c, solid lines present results of a fit of the data to Eq. 4 (see text and footnote 18).



Fig. 8:  $d\sigma/dt$  for p-Pb elastic scattering at the following incident momenta: 175 GeV/c, 125 GeV/c, 70 GeV/c; solid lines present results of a fit of the data to Eq. 4 (see text and footnote 18).

Fig. 9: Contributions of various terms in Eq. 4 (see text) to (a) p-Be at 175 GeV/c (b) p-Pb at 175 GeV/c. Dotted-dashed line is the contribution of Coulomb scattering. Dotted line is the contribution of coherent scattering. Dashed line is the contribution of incoherent scattering. Solid line is the sum of all contributions. Arrows indicate region of  $t$  fit over.

Fig. 10: Forward slope of coherent elastic scattering,  $b_A$ , versus target atomic weight,  $A$  for  $\pi^+$ . Fits for  $b_A$  were performed in the region of  $0.0018 \leq -t \leq 0.0100$  (GeV/c)<sup>2</sup>. Errors shown are statistical only (some errors not shown for presentation purposes). Dashed line has the form  $A^{2/3}$  normalized to  $b_A = 420$ . at Pb.

Fig. 11: Forward slope of coherent elastic scattering,  $b_A$ , versus target atomic weight,  $A$  for  $\pi^-$ . Fits for  $b_A$  were performed in the region of  $0.0018 \leq -t \leq 0.0100$  (GeV/c)<sup>2</sup>. Errors shown are statistical only (some errors not shown for presentation purposes). Dashed line has the form  $A^{2/3}$  normalized to  $b_A = 420$ . at Pb.

Fig. 12: Forward slope of coherent elastic scattering,  $b_A$ , versus target atomic weight,  $A$  for  $K^+$ . Fits for  $b_A$  were performed in the region of  $0.0018 \leq -t \leq 0.0100$  (GeV/c)<sup>2</sup>.

Fig. 13: Errors shown are statistical only (some errors not shown for presentation purposes). Dashed line has the form  $A^{2/3}$  normalized to  $b_A = 410$ . at Pb.

Fig. 14: Forward slope of coherent elastic scattering,  $b_A$ , versus target atomic weight,  $A$  for  $K^-$ . Fits for  $b_A$  were performed in the region of  $0.0018 \leq -t \leq 0.0100$  (GeV/c)<sup>2</sup>. Errors shown are statistical only (some errors not shown for presentation purposes). Dashed line has the form  $A^{2/3}$  normalized to  $b_A = 410$ . at Pb.

Fig. 15: Forward slope of coherent elastic scattering,  $b_A$ , versus target atomic weight,  $A$  for  $p$ . Fits for  $b_A$  were performed in the region of  $0.0018 \leq -t \leq 0.0100$  (GeV/c)<sup>2</sup>. Errors shown are statistical only (some errors not shown for presentation purposes). Dashed line has the form  $A^{2/3}$  normalized to  $b_A = 450$ . at Pb.

Fig. 16: Forward slope of coherent elastic scattering,  $b_A$ , versus target atomic weight,  $A$  for  $\bar{p}$ . Fits for  $b_A$  were performed in the region of  $0.0018 \leq -t \leq 0.0100$  (GeV/c)<sup>2</sup>. Errors shown are statistical only (some errors not shown for presentation purposes). Dashed line has the form  $A^{2/3}$  normalized to  $b_A = 450$ . at Pb.

# EXPERIMENTAL APPARATUS

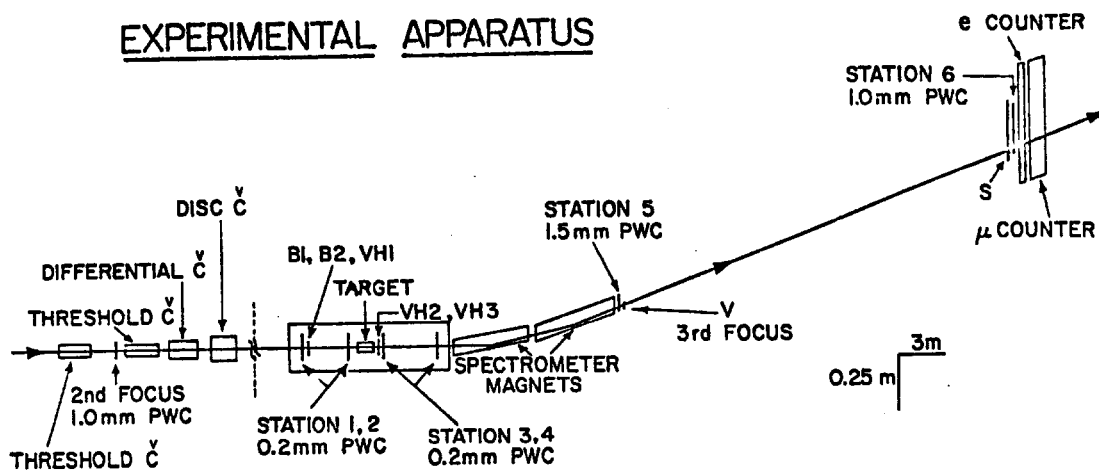


Fig. 1

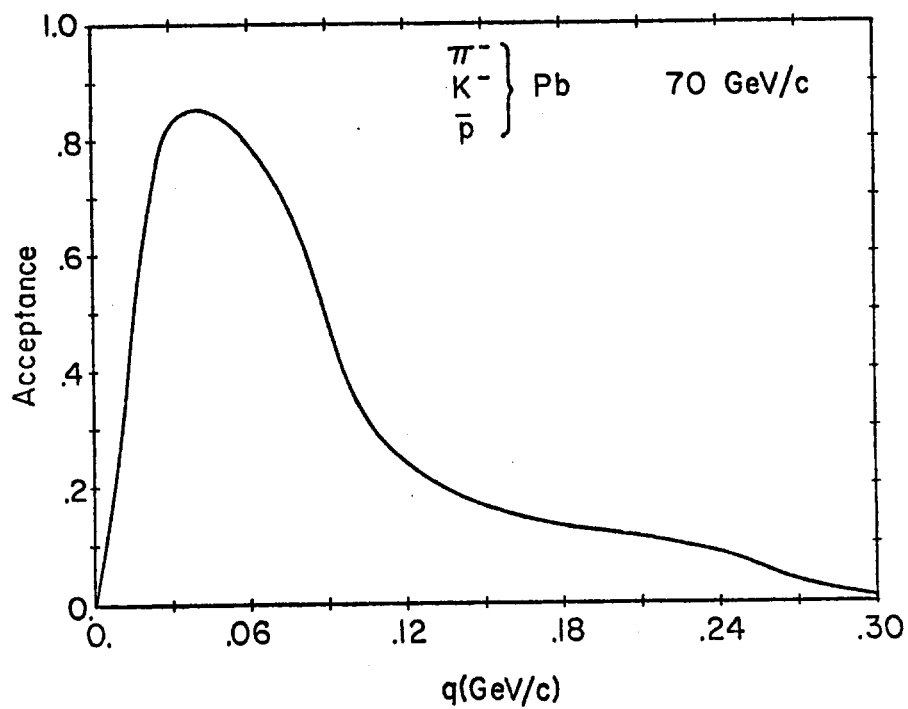


Fig. 2

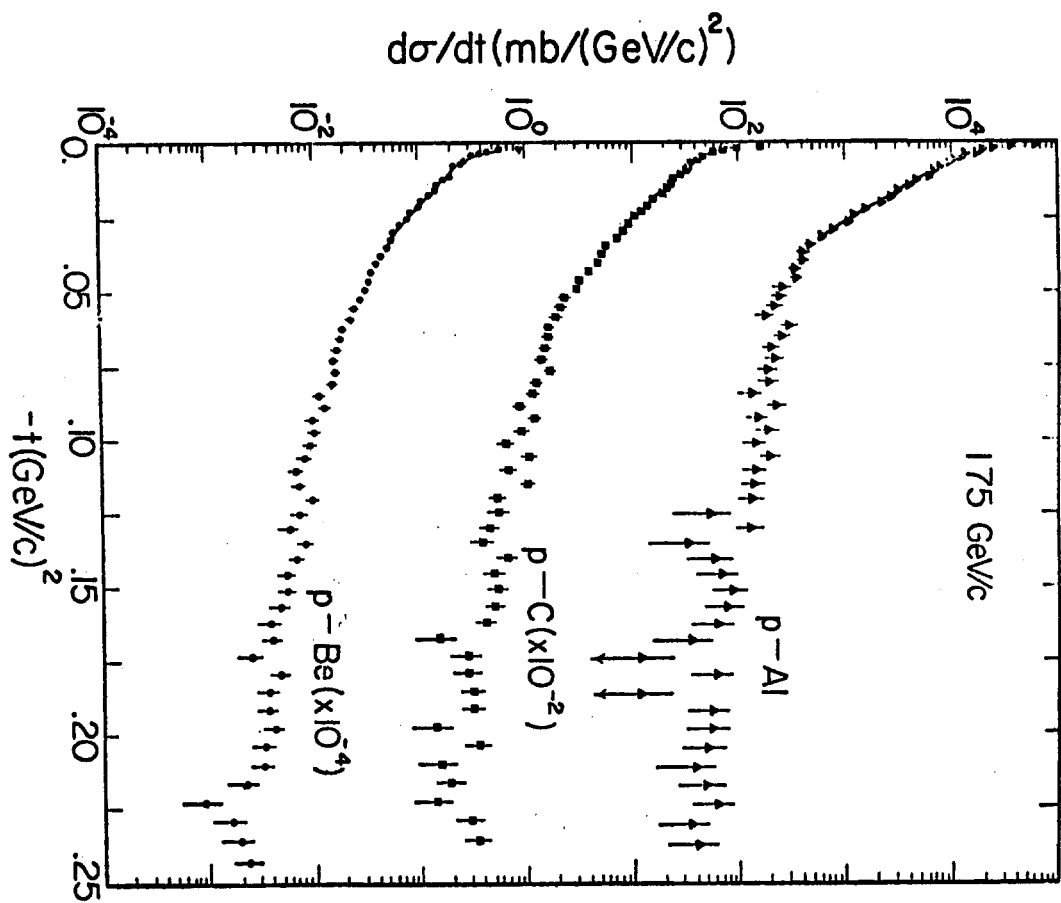


Fig. 3

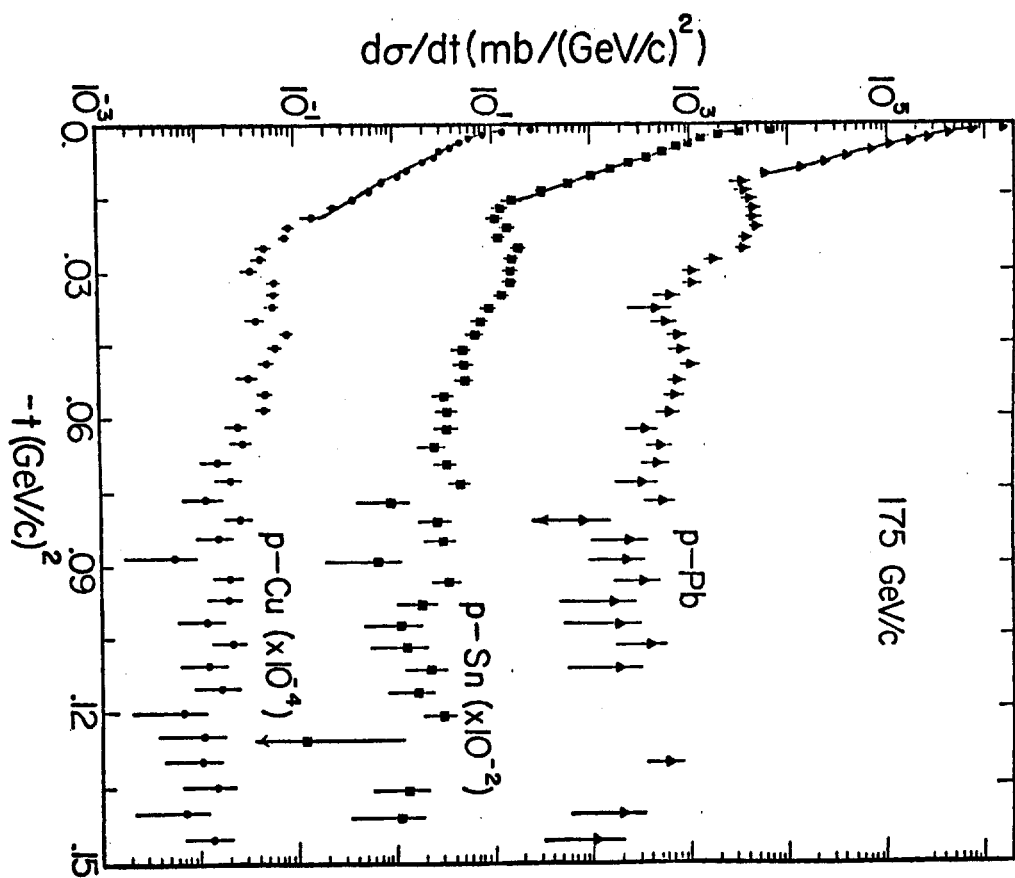


Fig. 4

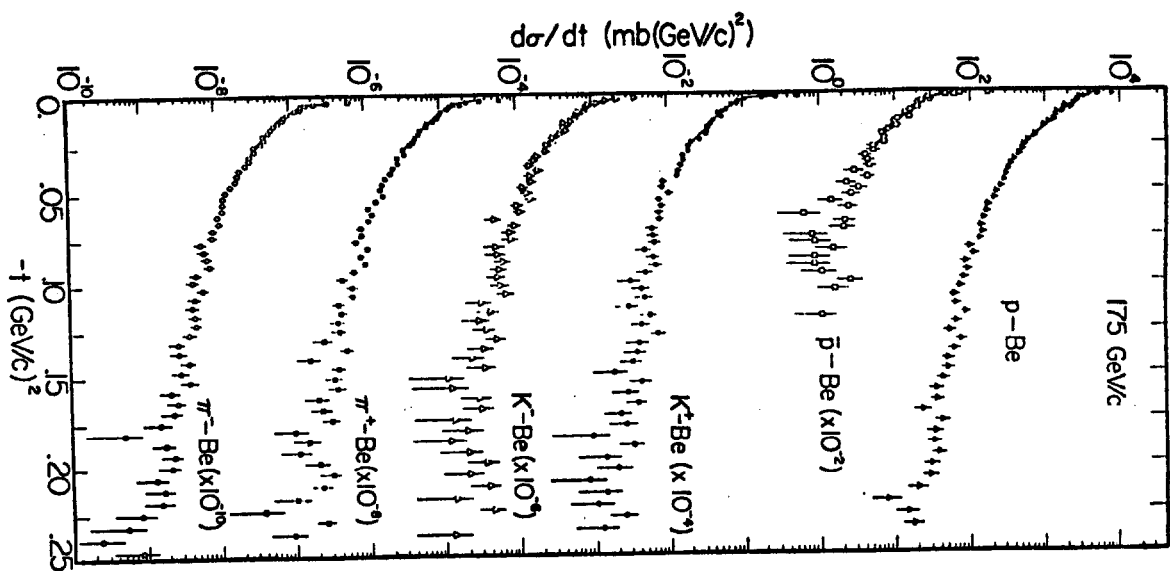


Fig. 5

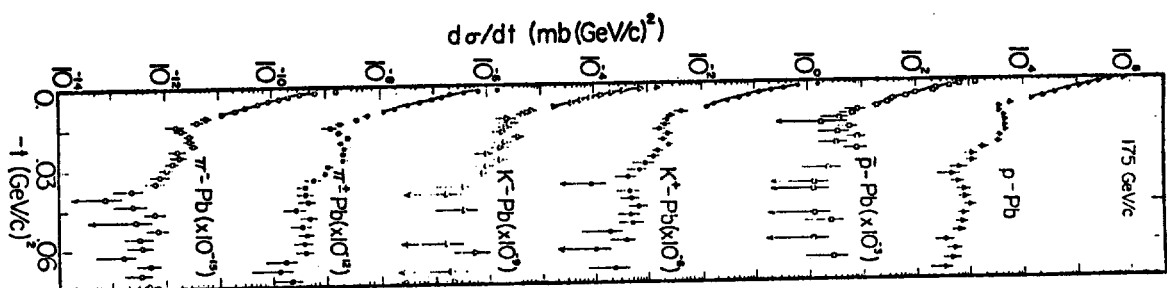


Fig. 6

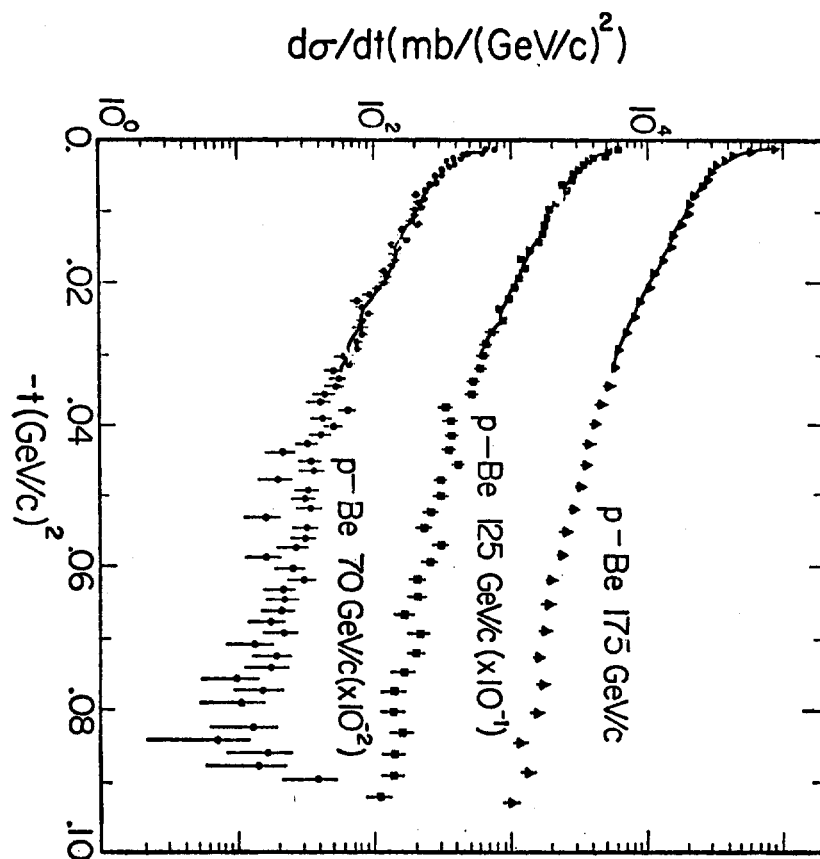


Fig. 7

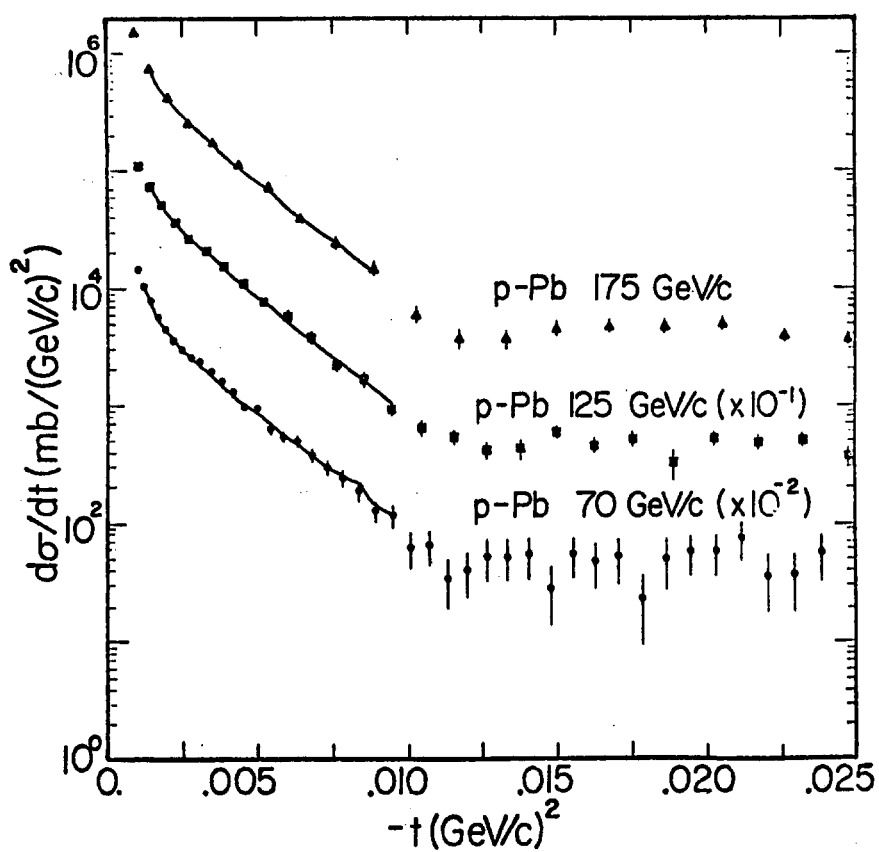
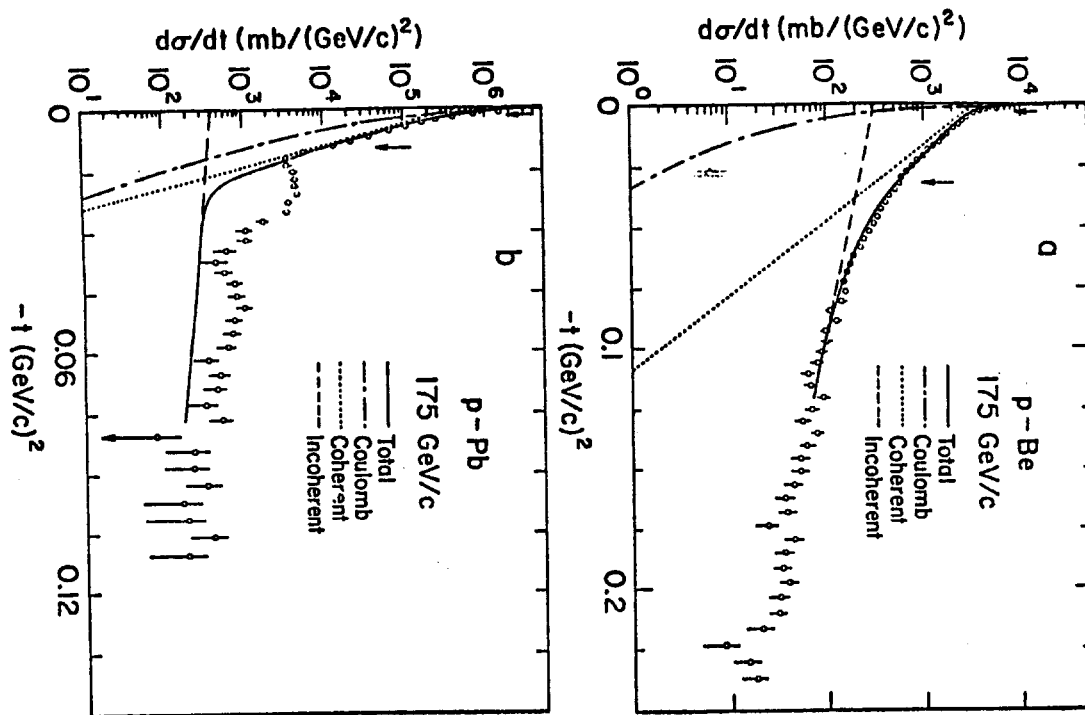


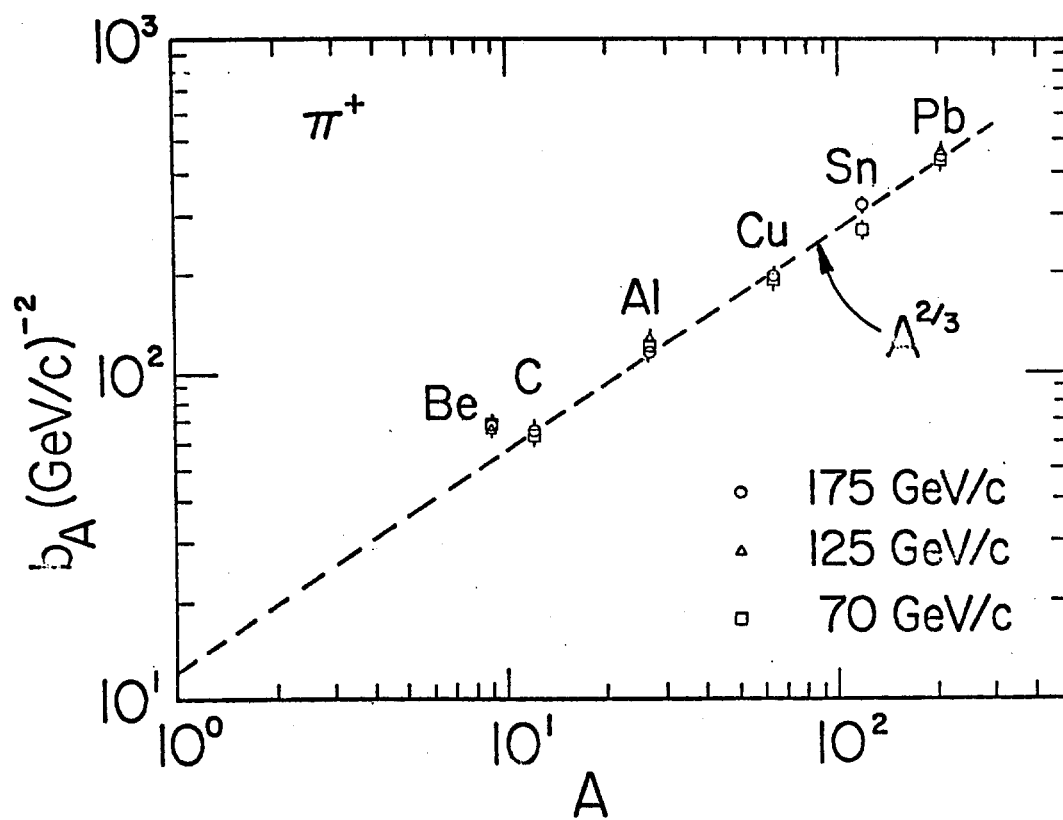
Fig. 8

Fig. 8

Fig. 9



-40-



-41-

Fig. 10

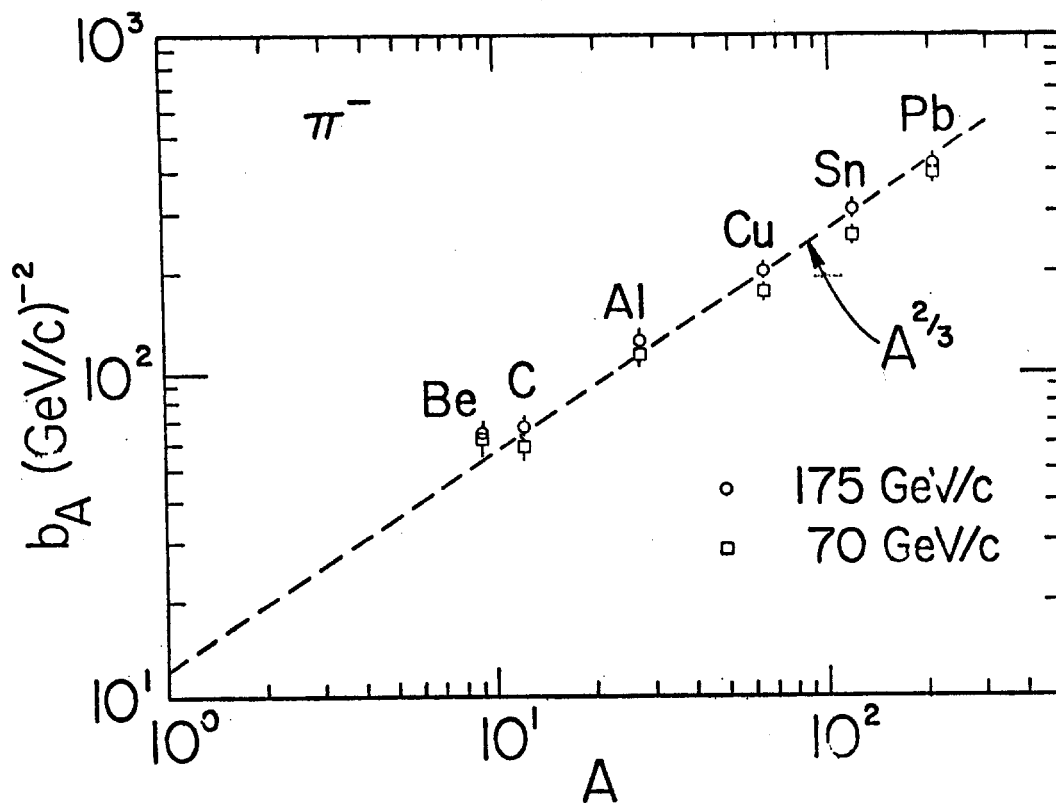


Fig. 11

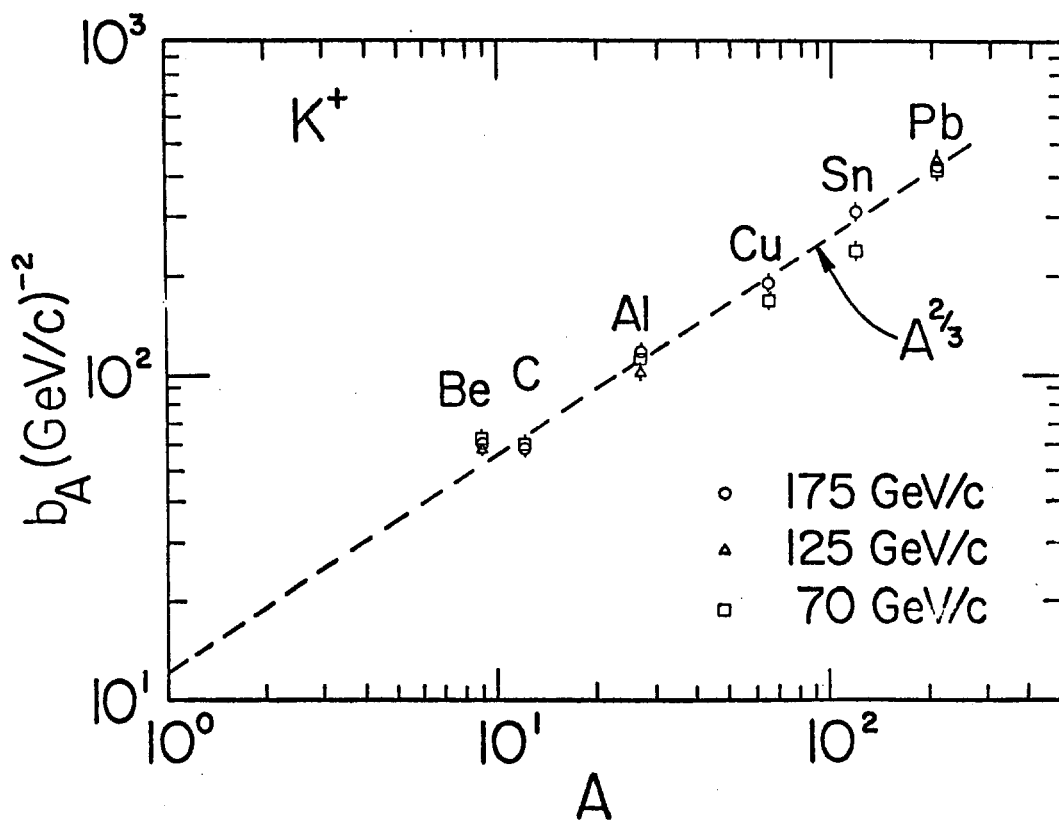


Fig. 12

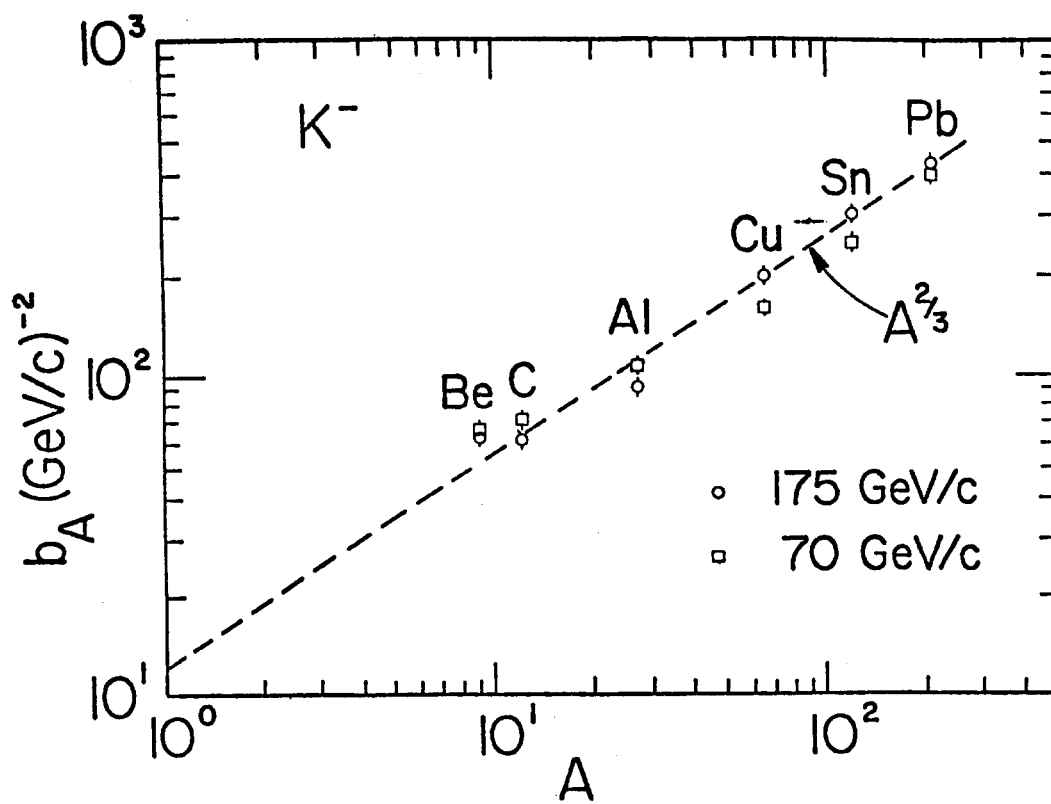


Fig. 13

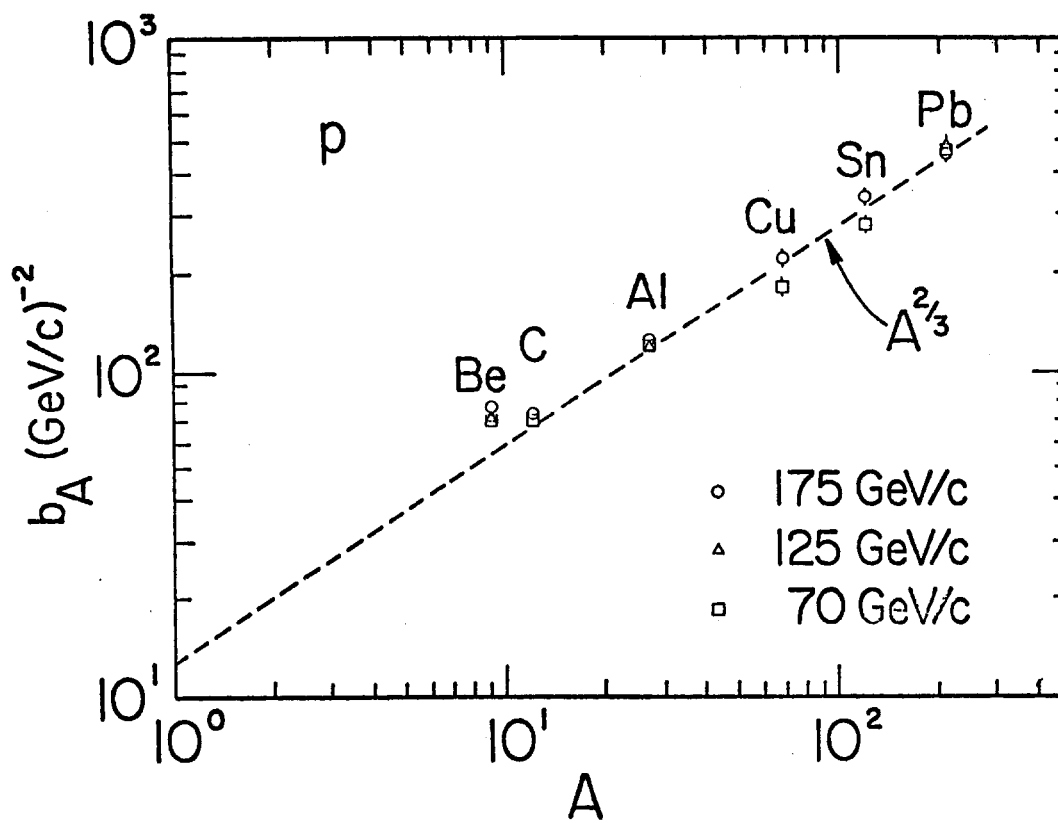


Fig. 14



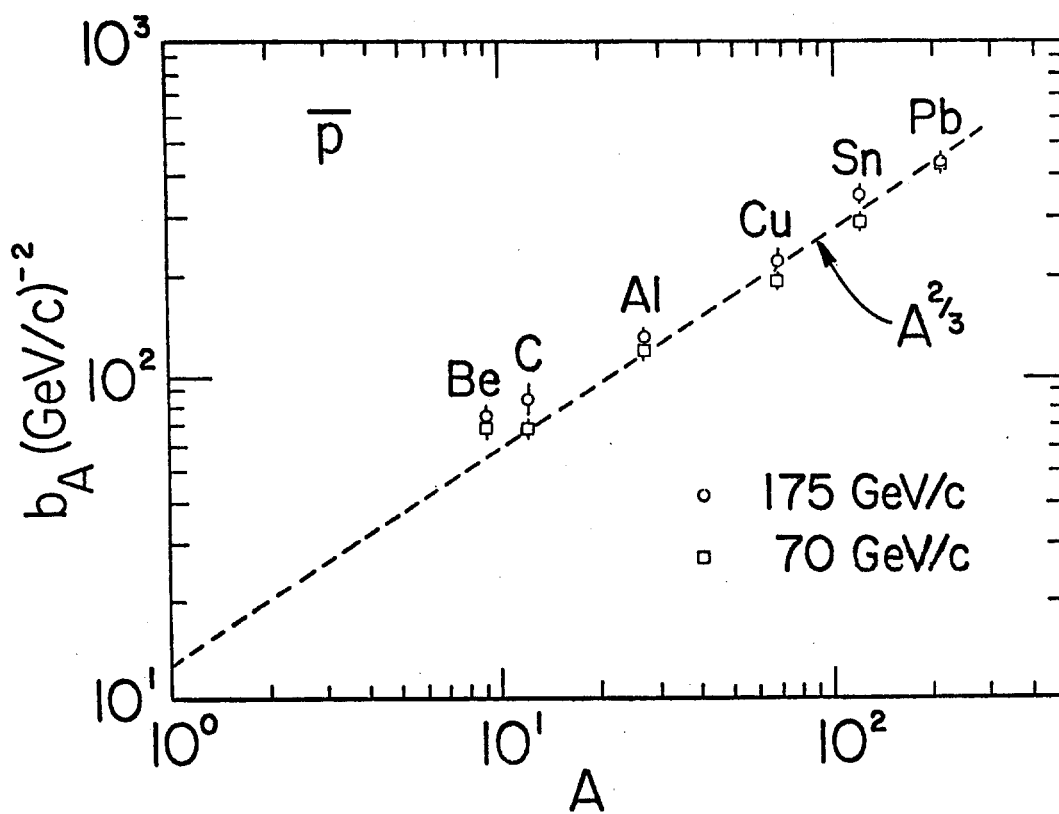


Fig. 15